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# Imputation of Incomplete Multilevel Data with mice

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#### Abstract

This is a tutorial paper on imputing incomplete multilevel data with **mice**. Footnotes in the current version show work in progress/under construction. The last section is not part of the manuscript, but purely for reminders. We aim to submit at JSS, so there is no word count limit ("There is no page limit, nor a limit on the number of figures or tables"). [Just adding some text to get a better guess of what the actura abstract will look like: Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua. Ut enim ad minim veniam, quis nostrud exercitation ullamco laboris nisi ut aliquip ex ea commodo consequat. Duis aute irure dolor in reprehenderit in voluptate velit esse cillum dolore eu fugiat nulla pariatur. Excepteur sint occaecat cupidatat non proident, sunt in culpa qui officia deserunt mollit anim id est laborum.]

Keywords: missing data, multilevel, clustering, mice, R.

## 1. Introduction

In many contemporary data analysis efforts, some form of hierarchical or clustered data structures are recorded. In the simplest case, such a structure entails the nesting of units within clusters (e.g., students within school classes). More complex clustered structures may occur when there are multiple hierarchical levels (e.g., patients within hospitals within regions or countries), or when the clustering is non-nested (e.g., electronic health record data from

	Table 1. Concepts in multilevel methods				
${f Concept}$	Details				
ICC	The variability due to clustering is often measured by means of the				
	intraclass coefficient (ICC). The ICC can be seen as the percentage				
	of variance that can be attributed to the cluster-level, where a high				
	ICC would indicate that a lot of variability is due to the cluster				
	structure.				
Random intercept	Multilevel models typically accommodate for variability by including				
	a separate group mean for each cluster. In addition to random				
	intercepts, multilevel models can also include random effects and				
	heterogeneous residual error variances across clusters [see e.g.				
	@gelm06, @hox17 and @jong21].				

Table 1: Concepts in multilevel methods

	cluster	$X_1$	$X_2$	$X_3$	 $X_p$
1	1			NA	
2	1				
3	2		NA		
4	2		NA	NA	
n	N				

Figure 1: Missingness in multilevel data

diverse settings and populations within large databases). The clustered structure of multilevel data should be taken into account when developing analysis models: 1) for the simple reason that groups of observations share some common variance, and 2) because ignoring multilevel structures can be harmful to the statistical inferences and introduce bias in estimators (Hox, Moerbeek, and van de Schoot 2017). There are many names for models that take clustering into account. Some popular examples are 'multilevel models', 'hierarchical models', 'mixed effect models' and 'random effect models'. Table 1 provides an overview of some key concepts in multilevel modeling.

#### 1.1. Missingness in multilevel data

The process of analyzing multilevel data is further complicated when not all data entries are observed. Just as with single level data, missingness may occur at the unit level. But with multiple levels of data comes the potential for clustered missingness. Therefore, incomplete multilevel data can be categorized into two general patterns: systematic missingness and sporadic missingness (Resche-Rigon, White, Bartlett, Peters, and Thompson 2013). Systematic missingness implies that one or more variables are never observed in a certain cluster. With sporadic missingness there may be observed data for some but not all units in a cluster (Van Buuren 2018; Jolani 2018). We have visualized this difference in Figure 1, which shows an  $n \times p$  set  $\mathbf{X} = X_1, \dots, X_p$ , with n units distributed over N clusters and p variables.

Table 2:	Concepts i	in missing	data methods

Concept	Details
MCAR	Missing Completely At Random, where the probability to be missing is equal
	across all data entries
MAR	Missing At Random, where the probability to be missing depends on observed
	information
MNAR	Missing Not At Random (MNAR), where the probability to be missing
	depends on unrecorded information, making the missingness non-ignorable
	[@rubi76; @meng94].
	[TODO: add congeniality.]

Column  $X_1$  in Figure 1 is completely observed, column  $X_2$  is systematically missing in cluster 2, and column  $X_3$  is sporadically missing. To analyze these incomplete data, we have to take the nature of the missingness and the cluster structure into account. For example, the sporadic missingness in  $X_3$  could be easily amended if this would be a cluster-level variable (and thus constant within clusters). We could then just extrapolate the true (but missing) value of  $X_3$  for unit 1 from unit 2, and the value for unit 4 from unit 3. If  $X_3$  would instead be a unit-level variable (which may vary within clusters), we could not just recover the unobserved 'truth', but would need to use some kind of missing data method, or discard the incomplete units altogether (i.e., complete case analysis). Complete case analysis can however introduce bias in statistical inferences and lowers statistical power. Further, with the systematic missingness in  $X_2$ , it would be impossible to fit a multilevel model without accommodating the missingness in some way. Complete case analysis in that case would mean excluding the entire cluster from the analyses. The wrong choice of missing data handling method can thus be extremely harmful to the inferences.

A key characteristic of the missing data to take into account in analyses is the mechanism behind the missingness. We distinguish between MCAR, MAR and MNAR in theory (see Table 2), but in practice this distinction is less clear. Since the essence of the true non-response mechanism may not be known, it is generally inferred or assumed to be ignorable (i.e., MCAR or MAR). [TODO: add that this assumption may not always be valid, especially with modern types of big dasta sources.] Depending on the actual missingness-generating mechanism, missing data handling strategies may be more or less suitable, see e.g., Yucel (2008) and Hox, van Buuren, and Jolani (2015).

Since excluding observations is not a desirable workflow, the missingness in multilevel data should be accommodated <u>before</u> or <u>within</u> the analysis of scientific interest. In this paper, we focus on the former approach: imputing (i.e., filling in) the missing data with plausible values, whereafter the completed data may be analyzed as if it were completely observed. Imputation separates the missing data problem from the scientific problem, which makes the missing data strategy very generic and popular. If each missing value is replaced multiple times, the resulting inferences may validly convey the uncertainty due to missingness (c.f. Rubin 1976). The R package **mice** has become the de-facto standard for imputation by chained equations, which iteratively solves the missingness on a variable-by-variable basis. **mice** is known to yield valid inferences under many different missing data circumstances (Van Buuren 2018). In this paper, we will discuss how to use **mice** in the context of multilevel data.

TODO: clarify why clustering is relevant during imputation, and why this exposes the need

|--|

Table 5.	Concepts in missing data methods
Concept	Details
	[TODO: explain lme4 notation here]

for specialized imputation methods and more attention during their implementation ("thou shall not simply run mice() on any incomplete dataset"). And add overview of possible predictor matrix values.]

#### 1.2. Aim of this paper

This papers serves as a tutorial for imputing incomplete multilevel data with **mice** in R. We provide practical guidelines and code snippets for different missing data situations, including non-ignorable mechanisms. For reasons of brevity, we focus on multilevel imputation by chained equations with **mice** exclusively; other imputation methods and packages (e.g., **jomo** and **mdmb**) are outside the scope of this tutorial. Assumed knowledge includes basic familiarity with multilevel imputation (see e.g. Audigier, White, Jolani, Debray, Quartagno, Carpenter, van Buuren, and Resche-Rigon 2018, and Grund, Lüdtke, and Robitzsch (2018)) and the **lme4** notation for multilevel models (see Table 3).

# 2. Case study

We illustrate how to impute incomplete multilevel data by means of a case study: impact from the **metamisc** package (empirical data on traumatic brain injuries, n = 11,022 units across N = 15 clusters, Debray and de Jong 2021). [TODO: add more info about the complete data.] The impact data set contains traumatic brain injury data on n = 11022 patients clustered in N = 15 studies with the following 11 variables:

- name Name of the study,
- type Type of study (RCT: randomized controlled trial, OBS: observational cohort),
- age Age of the patient,
- motor\_score Glasgow Coma Scale motor score,
- pupil Pupillary reactivity,
- ct Marshall Computerized Tomography classification,
- hypox Hypoxia (0=no, 1=yes),
- hypots Hypotension (0=no, 1=yes),
- tsah Traumatic subarachnoid hemorrhage (0=no, 1=yes),
- edh Epidural hematoma (0=no, 1=yes),
- mort 6-month mortality (0=alive, 1=dead).

The analysis model for this dataset is a prediction model with mort as the outcome. In this tutorial we'll estimate the adjusted prognostic effect of ct on unfortunate outcomes. The estimand is the adjusted odds ratio for ct, after including type, age motor\_score and pupil into the analysis model:

```
R> mod <- mort ~ 1 + type + age + motor_score + pupil + ct + (1 | name)
```

Note that variables hypots, hypox, tsah and edh are not part of the analysis model, and may thus serve as auxiliary variables for imputation.

#### 2.1. Setup

[TODO: Add environment info, seed and version number(s) somewhere.] Set up the R environment and load the necessary packages:

```
R> set.seed(2022)
R> library(mice)  # for imputation
R> library(ggmice)  # for visualization
R> library(ggplot2)  # for visualization
R> library(dplyr)  # for data wrangling
R> library(lme4)  # for multilevel modeling
R> library(broom.mixed)  # for multilevel estimates
R> library(mitml)  # for multilevel pooling
```

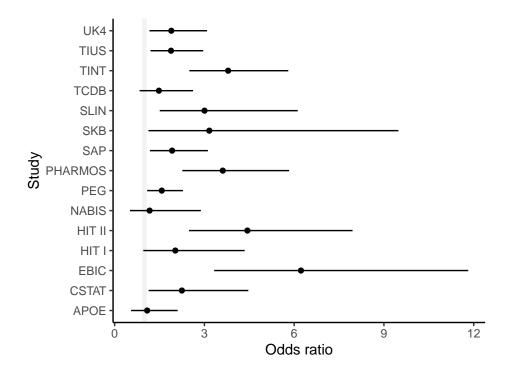
The impact data included in the **metamisc** package is a complete data set. The original data has already been imputed once (Steyerberg et al, 2008). For the purpose of this tutorial we have induced missingness (mimicking the missing data in the original data set before imputation). The resulting incomplete data can be accessed from zenodo link to be created. Load the complete and incomplete data into the R workspace:

```
R> data("impact", package = "metamisc")  # complete data
R> dat <- read.table("link/to/the/data.txt") # incomplete data</pre>
```

We will use the following estimates as comparative truth in this tutorial [TODO: make this a table or forest plot instead, to see if there is heterogeneity in the association of ct with mort]:

```
R> fit <- glmer(mod, family = "binomial", data = impact) # fit the model
R> tidy(fit, conf.int = TRUE, exponentiate = TRUE) # print estimates
```

```
# A tibble: 11 x 9
   effect group term
                       estimate std.error statistic
                                                         p.value conf.low conf.high
                                                           <dbl>
                                                                     <dbl>
                                                                               <dbl>
   <chr>
          <chr> <chr>
                          <dbl>
                                     <dbl>
                                               <dbl>
                                                       4.94e- 41
 1 fixed <NA>
                                   0.0173
                                              -13.4
                                                                   0.0723
                                                                               0.141
                (Int~
                          0.101
 2 fixed
          <NA>
                type~
                          0.713
                                   0.123
                                               -1.96
                                                       5.01e-
                                                                   0.509
                                                                               1.00
 3 fixed
          <NA>
                          1.03
                                   0.00165
                                               20.2
                                                       2.13e-90
                                                                   1.03
                                                                               1.04
                age
                                                       1.95e- 17
                                                                   0.482
4 fixed <NA>
                moto~
                          0.553
                                   0.0386
                                               -8.50
                                                                               0.634
 5 fixed <NA>
                moto~
                          0.405
                                   0.0289
                                              -12.7
                                                       8.43e- 37
                                                                   0.352
                                                                               0.466
6 fixed <NA>
                          0.275
                                   0.0202
                                              -17.6
                                                       1.67e- 69
                                                                   0.239
                                                                               0.318
                moto~
7 fixed <NA>
                pupi~
                          3.73
                                  0.230
                                               21.4
                                                       2.09e-101
                                                                   3.31
                                                                               4.21
                pupi~
                                                       1.36e- 18
8 fixed <NA>
                          1.87
                                   0.133
                                                8.80
                                                                   1.63
                                                                               2.15
9 fixed
          <NA>
                          2.25
                                   0.157
                                               11.6
                                                       5.12e- 31
                                                                    1.96
                                                                               2.58
                ctIII
10 fixed <NA>
                ctIV~
                          2.30
                                   0.136
                                               14.0
                                                       9.47e- 45
                                                                   2.05
                                                                               2.58
11 ran_p~ name
                sd__~
                          0.277
                                               NΑ
                                                      NA
                                                                  NA
                                                                              NA
                                 NA
```

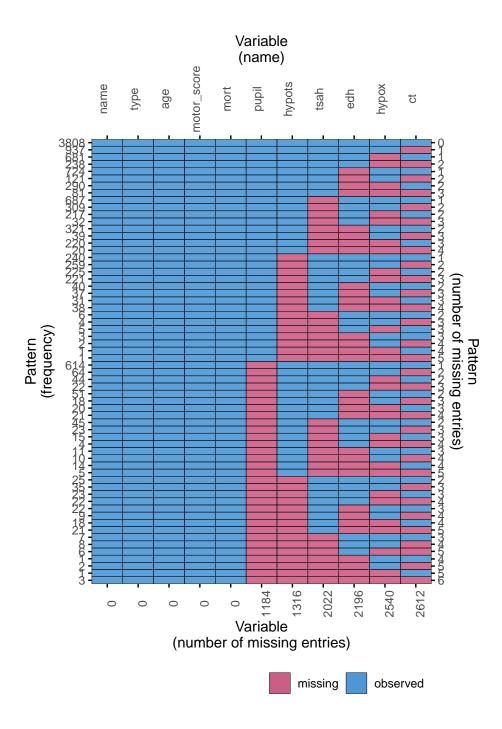


[TODO: add ICC before/after imputation and interpret: This tells us that the multilevel structure of the data should probably be taken into account. If we don't, we'll may end up with incorrect imputations, biasing the effect of the clusters towards zero.]

[TODO: add descriptive statistics of the complete and incomplete data.]

### 2.2. Missingness

To explore the missingness, it is wise to look at the missing data pattern:

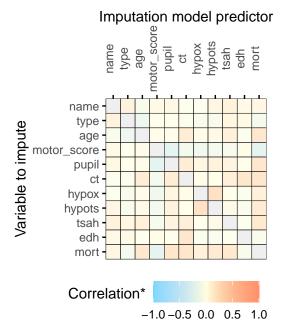


This shows... [TODO: fill in that we need to impute ct and pupil.]

To develop the best imputation model, we need to investigate the relations between the observed values of the incomplete variables and the observed values of other variables, and the relation between the missingness indicators of the incomplete variables and the observed values of the other variables. To see whether the missingness depends on the observed values of other variables, we... [TODO: fill in that we can test this statistically or use visual inspection (e.g. a histogram faceted by the missingness indicator).]

We should impute the variables ct and pupil and any auxiliary variables we might want to use to impute these incomplete analysis model variables. We can evaluate which variables may be useful auxiliaries by plotting the pairwise complete correlations:

R> plot\_corr(dat, rotate = TRUE) # plot correlations



\*pairwise complete observations

This shows us that hypox and hypot would not be useful auxiliary variables for imputing ct. Depending on the minimum required correlation, tsah could be useful, while edh has the strongest correlation with ct out of all the variables in the data and should definitely be included in the imputation model. For the imputation of pupil, none of the potential auxiliary variables has a very strong relation, but hypots could be used. We conclude that we can exclude hypox from the data, since this is neither an analysis model variable nor an auxiliary variable for imputation:

R> dat <- select(dat, !hypox) # remove variable

#### 2.3. Complete case analysis

As previously stated, complete case analysis lowers statistical power and may bias results. The complete case analysis estimates are:

```
R> fit <- glmer(mod, family = "binomial", data = na.omit(dat)) # fit the model
R> tidy(fit, conf.int = TRUE, exponentiate = TRUE) # print estimates
# A tibble: 11 x 9
    effect group term estimate std.error statistic p.value conf.low conf.high
```

	<chr></chr>	<chr></chr>	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
1	fixed	<na></na>	(Int~	0.0863	0.0182	-11.6	2.99e-31	0.0571	0.130
2	fixed	<na></na>	type~	0.757	0.137	-1.54	1.22e- 1	0.531	1.08
3	fixed	<na></na>	age	1.03	0.00265	12.9	7.40e-38	1.03	1.04
4	fixed	<na></na>	moto~	0.651	0.0732	-3.82	1.34e- 4	0.522	0.811
5	fixed	<na></na>	moto~	0.489	0.0555	-6.30	2.97e-10	0.391	0.611
6	fixed	<na></na>	moto~	0.274	0.0321	-11.0	2.28e-28	0.218	0.345
7	fixed	<na></na>	pupi~	3.20	0.317	11.7	8.18e-32	2.63	3.88
8	fixed	<na></na>	pupi~	1.75	0.195	5.06	4.27e- 7	1.41	2.18
9	fixed	<na></na>	ctIII	2.41	0.268	7.89	3.05e-15	1.94	2.99
10	fixed	<na></na>	ctIV~	2.30	0.214	8.95	3.55e-19	1.92	2.76
11	ran_pa~	name	sd~	0.230	NA	NA	NA	NA	NA

As we can see... [TODO: fill in.]

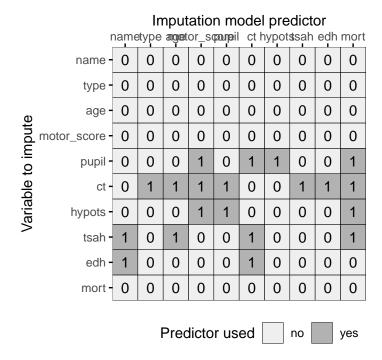
#### 2.4. Imputation model

The first imputation model that we'll use is likely to be invalid. We do <u>not</u> use the cluster identifier <u>name</u> as imputation model predictor. With this model, we ignore the multilevel structure of the data, despite the high ICC. This assumes exchangeability between units. We include it purely to illustrate the effects of ignoring the clustering in our imputation effort. We'll use the default imputation methods in <u>mice()</u> (predictive mean matching to impute the continuous variables and logistic regression to impute binary variables).

Updated until here!

Create a methods vector and predictor matrix, and make sure name is not included as predictor:

```
R> meth <- make.method(dat) # methods vector
R> pred <- quickpred(dat) # predictor matrix
R> plot_pred(pred)
```



[TODO: mutate data to get the right data types for imputation (e.g. integer for clustering variable).]

# 3. Discussion

- JOMO in mice -> on the side for now
- Additional levels of clustering
- More complex data types: timeseries and polynomial relationship in the clustering.

### 4. Think about

- Adding some kind of help function to mice that suggests a suitable predictor matrix to the user, given a certain analysis model.
- Adding a multilevel\_ampute() wrapper function in mice.
- Exporting mids objects to other packages like lme4 or coxme?
- Adding a ICC=0 dataset to show that even if there is no clustering it doesn't hurt.
- Show use case for deductive imputation for cluster level variables?
- env dump in repo

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