# Applications of Newton's Laws of Motion

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### The Runaway Car

Suppose a car is released from rest at the top of the incline, and the distance from the front edge of the car to the bottom is *d. How long does it take the front edge to* reach the bottom, and what is its speed just as it gets there?

Because  $a_x = \text{constant}$ , we can apply  $x_f - x_i = v_{xi}t + \frac{1}{2}a_xt^2$ , to analyze the car's motion

replace displacement by 
$$x_f - x_i = d$$

Put,  $v_{xi} = 0$ , we get  $d = \frac{1}{2}a_x t^2$ 

(1) 
$$\sum F_x = mg \sin \theta = ma_x$$

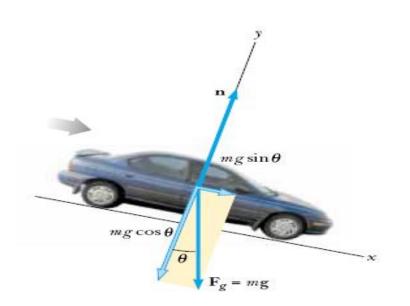
(2) 
$$\sum F_{y} = n - mg\cos\theta = 0$$

Solving (1) for 
$$a_x$$
  $a_x = g \sin \theta$ 

put the value of  $a_x$  in  $d = \frac{1}{2}a_x t^2$  and find time, as follows

$$t = \sqrt{\frac{2d}{a_x}}$$

$$t = \sqrt{\frac{2d}{g\sin\theta}}$$



## **Calculation for Final Velocity**

Using 
$$v_{xf}^{2} = v_{xi}^{2} + 2a_{x}(x_{f} - x_{i})$$
  
with  $v_{xi} = 0$ ,  $x_{f} - x_{i} = d$   
 $v_{xf}^{2} = 2a_{x}d$ 

 $v_{xf} = \sqrt{2gd \sin \theta}$ 

$$mg \sin \theta$$

$$mg \cos \theta$$

$$\mathbf{F}_g = mg$$

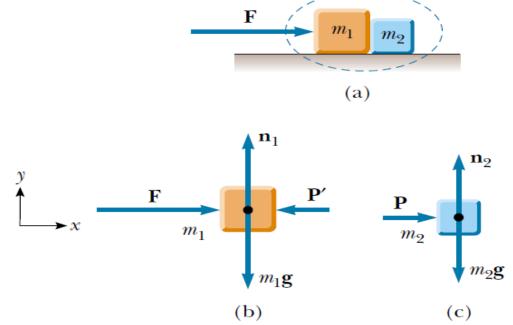
## **Conclusion**

We see that the time t needed to reach the bottom and the speed  $v_{xf}$ , are independent of the car's mass.

#### **One Block Pushes Another**

Two blocks of masses  $m_1$  and  $m_2$  are placed in contact with each other on a frictionless horizontal surface. A constant horizontal force  $\mathbf{F}$  is applied to the block of mass  $m_1$ . (a) Determine the magnitude of the acceleration of the two-block system.

(b) Determine the magnitude of the contact force between the two blocks.



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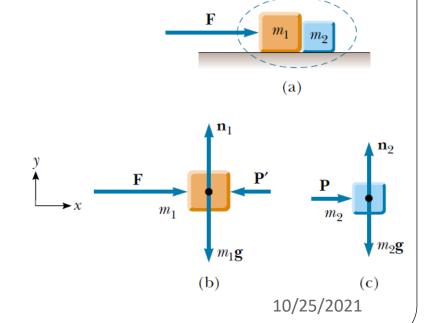
## Solution

we know that both blocks must experience the same acceleration because they remain in contact with each other.

**F** is the only external horizontal force acting on the system (the two blocks), we have

$$\sum F_x(\text{system}) = F = (m_1 + m_2) a_x$$

$$(1) a_x = \frac{F}{m_1 + m_2}$$



(b) Determine the magnitude of the contact force between the two blocks.

To solve this part of the problem, we must treat each block separately with its own free-body diagram, We denote the contact force by **P**.

From Figure c, we see that the only horizontal force acting on block 2 is the contact force **P**(the force exerted by block 1 on block 2), which is directed to the right. Applying Newton's second law to block 2 gives

$$(2) \qquad \sum F_x = P = m_2 a_x$$

Substituting into (2) the value of  $a_x$  given by (1), we obtain

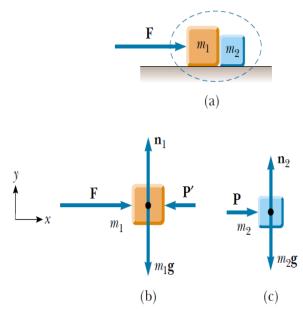
(3) 
$$P = m_2 a_x = \left(\frac{m_2}{m_1 + m_2}\right) F$$

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From this result, we see that the contact force  $\mathbf{P}$  exerted by block 1 on block 2 is *less* than the applied force  $\mathbf{F}$ . This is consistent with the fact that the force required to accelerate block 2 alone must be less than the force required to produce the same acceleration for the two-block system.

It is instructive to check this expression for P by considering the forces acting on block 1, shown in Figure b. The horizontal forces acting on this block are the applied force  $\mathbf{F}$  to the right and the contact force  $\mathbf{P}'$  to the left (the force exerted by block 2 on block 1). From Newton's third law,  $\mathbf{P}'$  is the reaction to  $\mathbf{P}$ , so that  $|\mathbf{P}'| = |\mathbf{P}|$ . Applying Newton's second law to block 1 produces

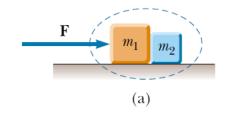
(4) 
$$\sum F_x = F - P' = F - P = m_1 a_x$$

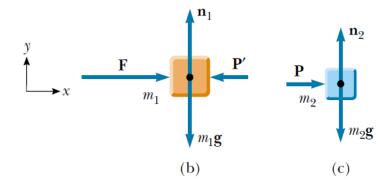


(4) 
$$\sum F_x = F - P' = F - P = m_1 a_x$$

Substituting into (4) the value of  $a_x$  from (1), we obtain

$$P = F - m_1 a_x = F - \frac{m_1 F}{m_1 + m_2} = \left(\frac{m_2}{m_1 + m_2}\right) F$$





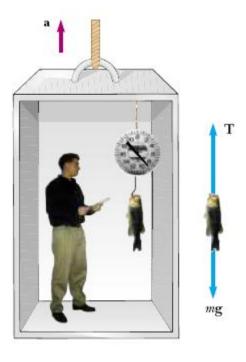
## Task 1

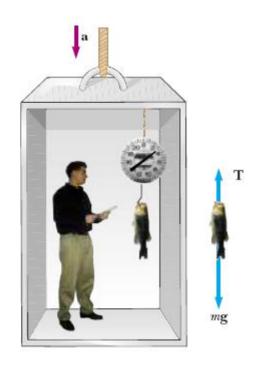
**Exercise** If  $m_1 = 4.00 \text{ kg}$ ,  $m_2 = 3.00 \text{ kg}$ , and F = 9.00 N, find the magnitude of the acceleration of the system and the magnitude of the contact force.

**Answer**  $a_x = 1.29 \text{ m/s}^2$ ; P = 3.86 N.

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## Weighing a fish in an Elevator

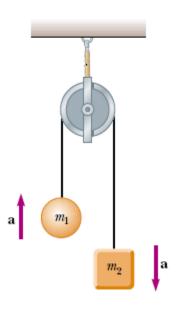




$$\sum F_y = T - mg = ma_y$$

$$T = ma_y + mg = mg\left(\frac{a_y}{g} + 1\right)$$

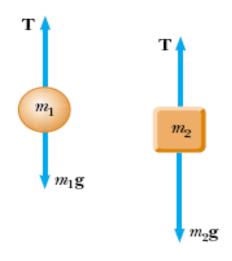
#### **The Atwood Machine**



$$\sum F_{y} = T - m_{1}g = m_{1}a_{y}$$

$$\sum F_y = m_2 g - T = m_2 a_y$$

$$a_y = \left(\frac{m_2 - m_1}{m_1 + m_2}\right) g$$



$$T = \left(\frac{2m_1m_2}{m_1 + m_2}\right)g$$