250518-Spectural-Clustering

2025-05-18

Define Spectural Clusterng Function

```
## Compute the Similarity Matrix with Gaussian Radial Kernel
S <- function(X) {
  exp(-0.5 * as.matrix(dist(X)))
## Weighted adjacency matrix with 10 nearest neighbors
knn = function(values, K){
  index = order(values, decreasing = TRUE)[(1:K) + 1]
  values[-index] = NA
  return(values)
## Compute the weight Matrix
W <- function(S, type = "Full", extra = NA) {
  if (type == "Soft") {
    lambda <- extra$lambda
    W <- S - lambda
    W[W < 0] <- 0
  ## Epsilon neighborhood
  } else if (type == "Epsilon") {
    S > epsilon
  ## Fully Connected Graph
  } else {
    W \leftarrow apply(S, 2, function(x) knn(x, K = 10))
    W = (W + t(W)) / 2
    W[is.na(W)] = 0
  }
## Compute the Laplacian
L <- function(W) {
 D <- diag(rowSums(W))</pre>
  D - W
}
## Pick the K smallest eigenvalues of L and corrsponding eigenvectors
bottomK <- function(L, K) {</pre>
```

```
n <- nrow(L)
  E <- eigen(L)
 U \leftarrow E$vectors[,(n-K+1):n]
 U
}
## K-mean Cluster rows of U
KM <- function(U, K) {</pre>
 kmeans(U, centers = K, iter.max = 100, nstart = 10)$cluster
}
## Wrapper Function
spectralClust <- function(X, K, cancerType = "All", extra = NA) {</pre>
 s <- S(X) ## Similarity
  w <- W(s, "Full", extra) ## Weight
  1 <- L(w) ## Laplacian
  u <- bottomK(1, K) ## Eigen values
  clustVec <- KM(u, K)</pre>
  par(mfrow = c(1,2))
  ## Plot first two eigenvectors, colored by cluster
  library(ggplot2)
  U2 <- data.frame(cbind(u[,1:2], clustVec))</pre>
  colnames(U2) <- c("U1", "U2", "C")</pre>
  plot(U2[,1], U2[,2], col = factor(clustVec),
       main = "Clustering in top 2 eigenvectors",
       xlab = "U1", ylab = "U2")
  ## Plot Grpah Rrepresentation
  library(igraph)
  G = graph_from_adjacency_matrix(w, mode="undirected", weighted = TRUE)
  layout_circle <- layout_in_circle(G)</pre>
  plot(G, vertex.size=3, vertex.label=NA,
       layout = layout_circle,
       main = paste("Spectral Graph for ", cancerType))
  mtext(cancerType,
        side = 3, line = -2, outer = TRUE, cex = 1.5)
  clustVec
```

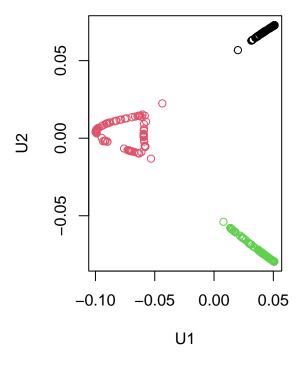
Test Trial using Class Example

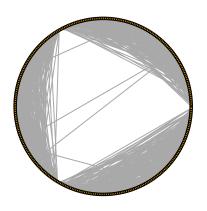
```
## Generate Data
set.seed(226)
n = 100
r1 = 0.3
r2 = 1
r3 = 1.8
```

```
X1 = matrix(rnorm(n * 2), n, 2)
X1 = X1/sqrt(rowSums(X1^2)) * r1
X2 = matrix(rnorm(n * 2), n, 2)
X2 = X2/sqrt(rowSums(X2^2)) * r2
X3 = matrix(rnorm(n * 2), n, 2)
X3 = X3/sqrt(rowSums(X3^2)) * r3
E = matrix(rnorm(3*n * 2, 0, 0.1), 3*n, 2)
X = rbind(X1, X2, X3) + E
X = scale (X, scale = F, center = T)
colnames(X) = c("x1", "x2")
K <- 3
specClusters <- spectralClust(X, K, "All")</pre>
## Warning: package 'ggplot2' was built under R version 4.4.3
## Warning: package 'igraph' was built under R version 4.4.3
## Attaching package: 'igraph'
## The following object is masked _by_ '.GlobalEnv':
##
##
       knn
## The following objects are masked from 'package:stats':
##
##
       decompose, spectrum
## The following object is masked from 'package:base':
##
##
       union
```

Clustering in top 2 eigenvectors

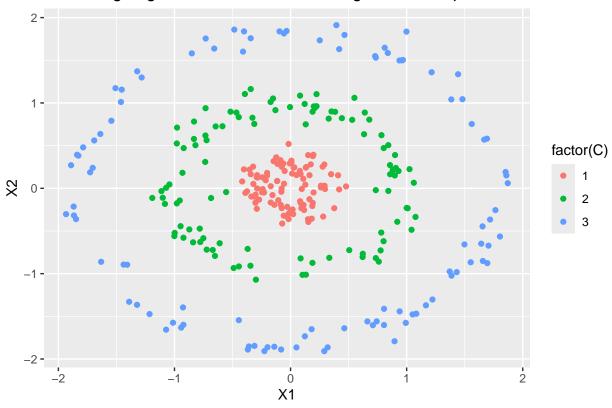
Spectral Graph for All





```
ggplot(cbind(X, "C" = specClusters)) +
   geom_point(aes(x1, x2, color = factor(C))) +
   xlab("X1") +
   ylab("X2") +
   ggtitle("Clustering of genes in the the first two eigenvectors' space")
```

Clustering of genes in the the first two eigenvectors' space



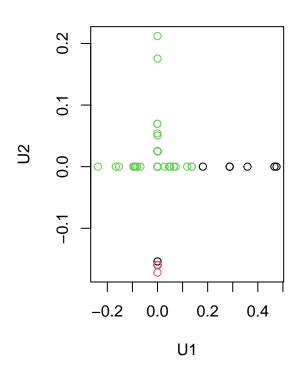
Shared Gene Networks

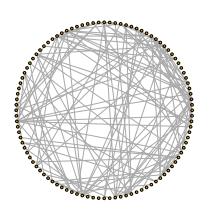
```
library(tidyverse)
```

```
## Warning: package 'purrr' was built under R version 4.4.3
## -- Attaching core tidyverse packages -----
                                                  ----- tidyverse 2.0.0 --
## v dplyr
               1.1.4
                          v readr
                                      2.1.5
## v forcats
               1.0.0
                                      1.5.1
                          v stringr
## v lubridate 1.9.4
                          v tibble
                                      3.2.1
## v purrr
               1.0.4
                          v tidyr
                                      1.3.1
## -- Conflicts ----
                                                     ----- tidyverse_conflicts() --
## x lubridate::%--%()
                             masks igraph::%--%()
## x dplyr::as_data_frame() masks tibble::as_data_frame(), igraph::as_data_frame()
## x purrr::compose()
                             masks igraph::compose()
## x tidyr::crossing()
                             masks igraph::crossing()
## x dplyr::filter()
                             masks stats::filter()
## x dplyr::lag()
                             masks stats::lag()
## x purrr::simplify()
                             masks igraph::simplify()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
```

Clustering in top 2 eigenvectors

Spectral Graph for All



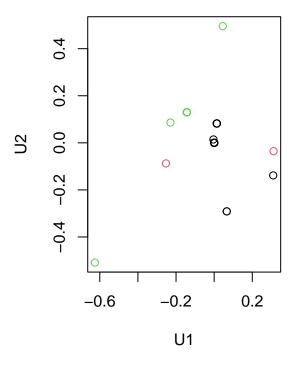


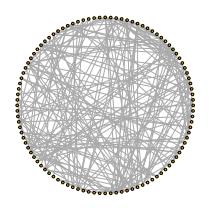
Cancer-Specific Gene Networks

```
cancerFrameList <- split(data.frame(t(X)), cancerTypes)

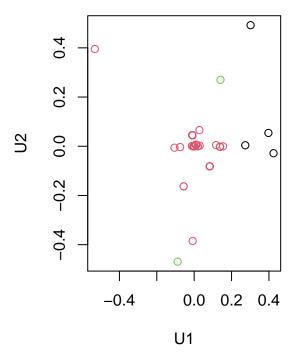
for (cancer in names(cancerFrameList)) {
   paste("Cancer type:", cancer, "\n")
   X <- t(cancerFrameList[[cancer]])
   sClusters <- spectralClust(X, 3, cancer)
}</pre>
```

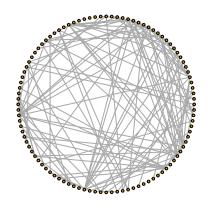
Bladder Cancer Clustering in top 2 eigenvectors Spectral Graph for Bladder Canc



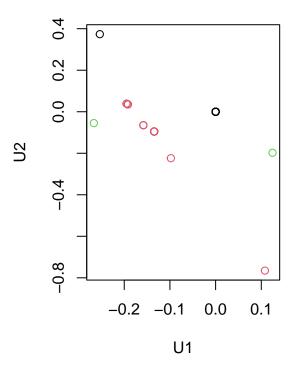


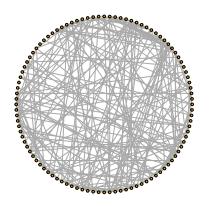
Blood Cancer
Clustering in top 2 eigenvectors Spectral Graph for Blood Cance



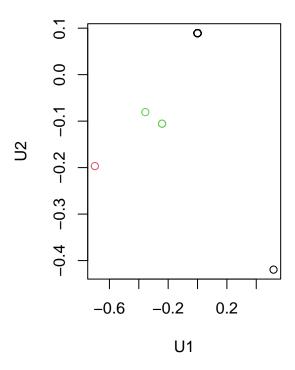


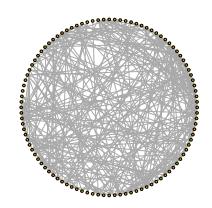
Breast Cancer
Clustering in top 2 eigenvectors Spectral Graph for Breast Cance



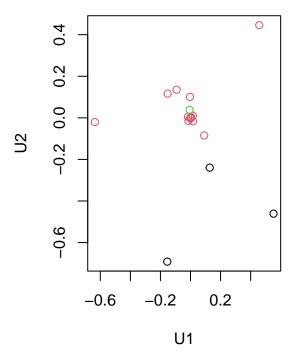


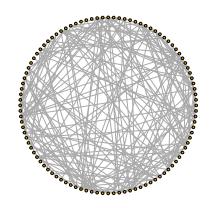
Colorectal Cancer Clustering in top 2 eigenvectors Spectral Graph for Colorectal Can





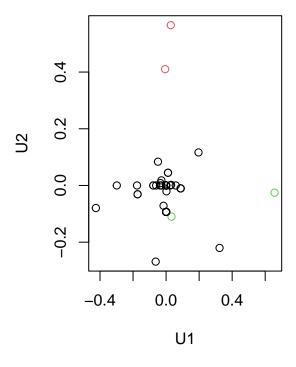
Lung Cancer
Clustering in top 2 eigenvectors Spectral Graph for Lung Cance

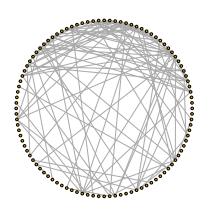




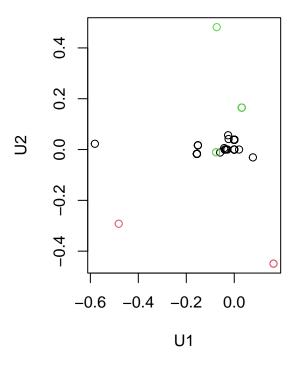
Clustering in top 2 eigenvectors

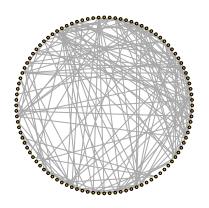
Spectral Graph for Normal





Pancreatic Cancer Clustering in top 2 eigenvectors Spectral Graph for Pancreatic Can





Renal Cancer
Clustering in top 2 eigenvectors Spectral Graph for Renal Cance

