



GEOMETRÍA

Capítulo 5

Sesión 2

3th
SECONDARY

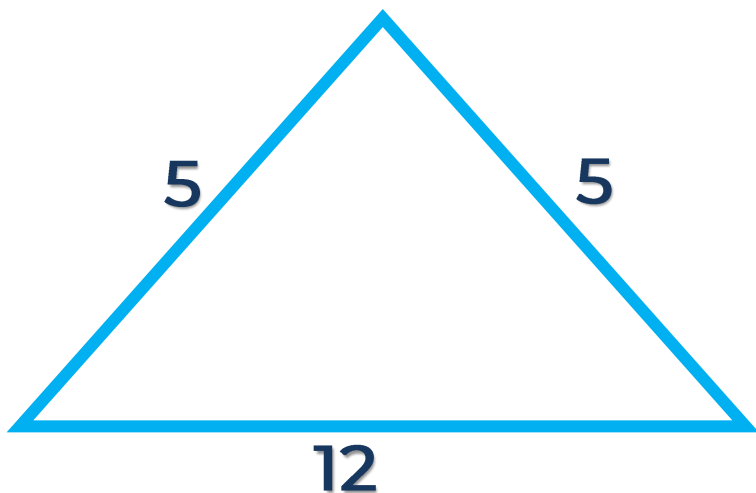
TRIÁNGULOS



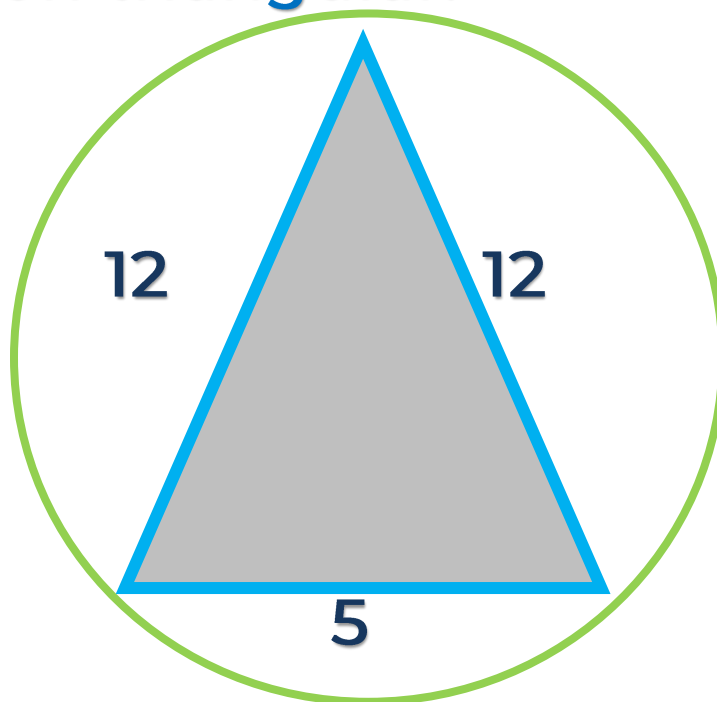
 **SACO OLIVEROS**

1. Los lados de un triángulo isósceles miden 12 y 5cm. Calcule el perímetro de la región triangular.

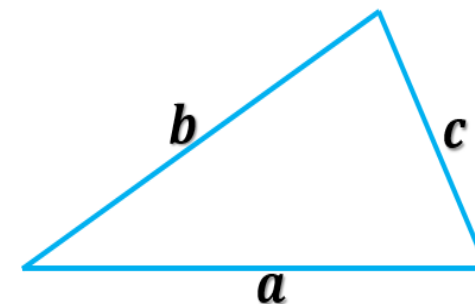
Resolución



$$\begin{aligned} 5-5 &< 12 < 5+5 \\ 0 &< 12 < 10 \end{aligned}$$



$$\begin{aligned} 12-12 &< 5 < 12+12 \\ 0 &< 5 < 24 \end{aligned}$$



donde: $c < b < a$

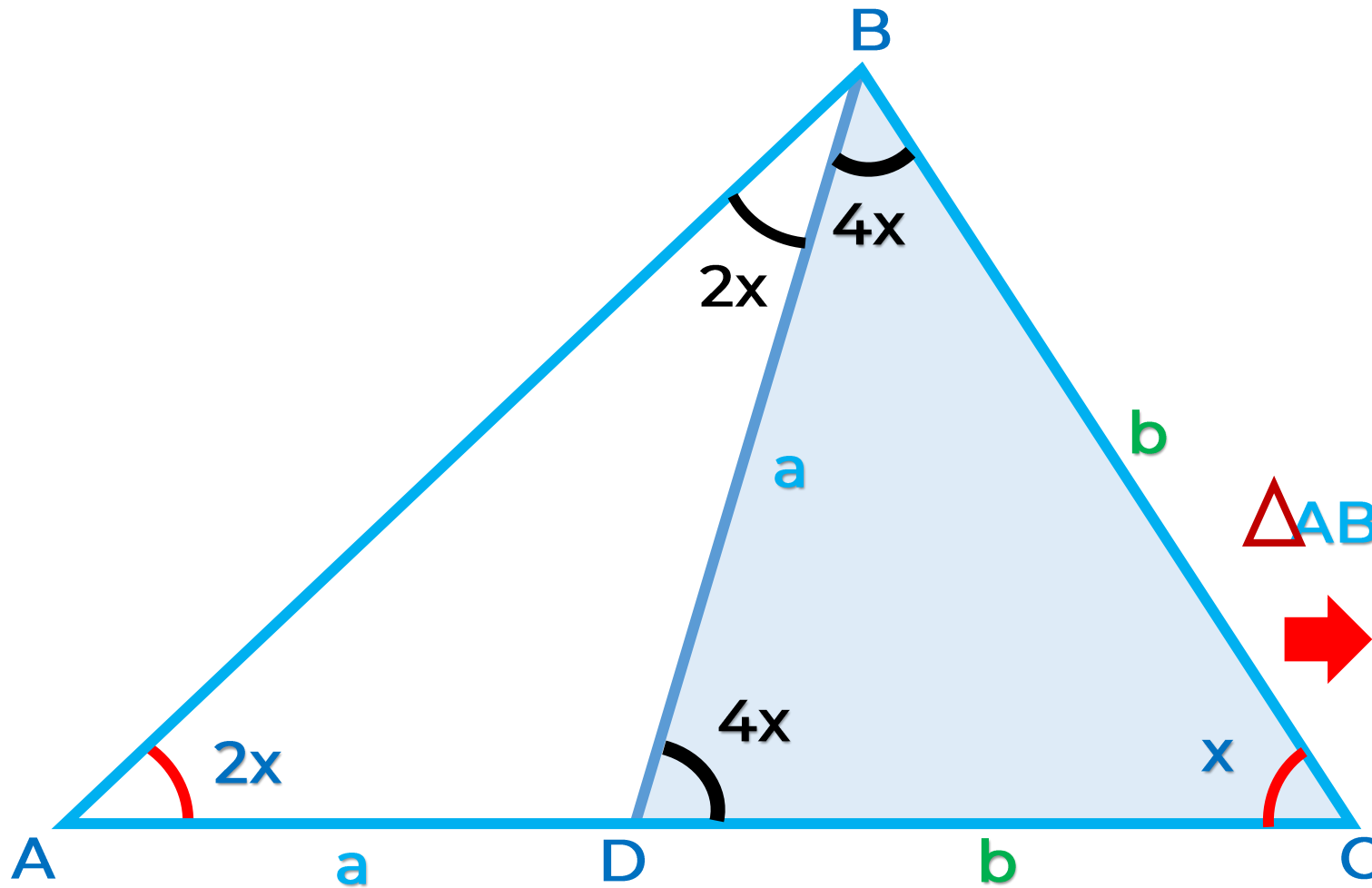
$$b-c < a < b+c$$

NOS PIDEN

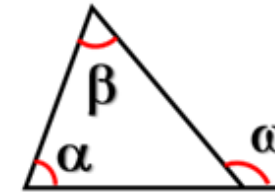
$$\rightarrow 2p_{\triangle} = 12 + 12 + 5$$

$$2p_{\triangle} = 29$$

2. Halle el valor de x , si $AD = DB$ y $BC = CD$.



Resolución



$$\omega = \alpha + \beta$$

$\triangle ABD$ y $\triangle BCD$: ISÓSCELES

$$\Rightarrow 4x + 4x + x = 180^\circ$$

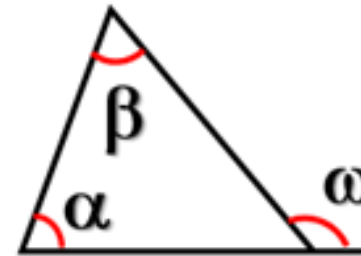
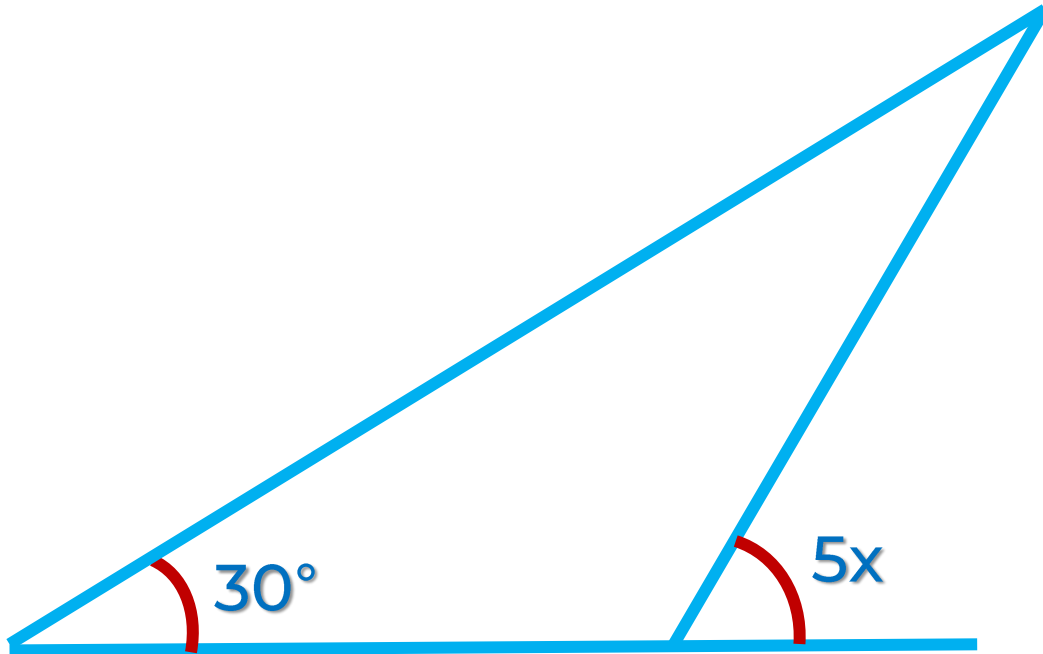
$$9x = 180^\circ$$

$$x = 20^\circ$$

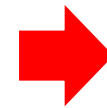


3. Halle el menor valor entero que puede tomar x .

Resolución



$$\omega = \alpha + \beta$$



$$30^\circ < 5x$$

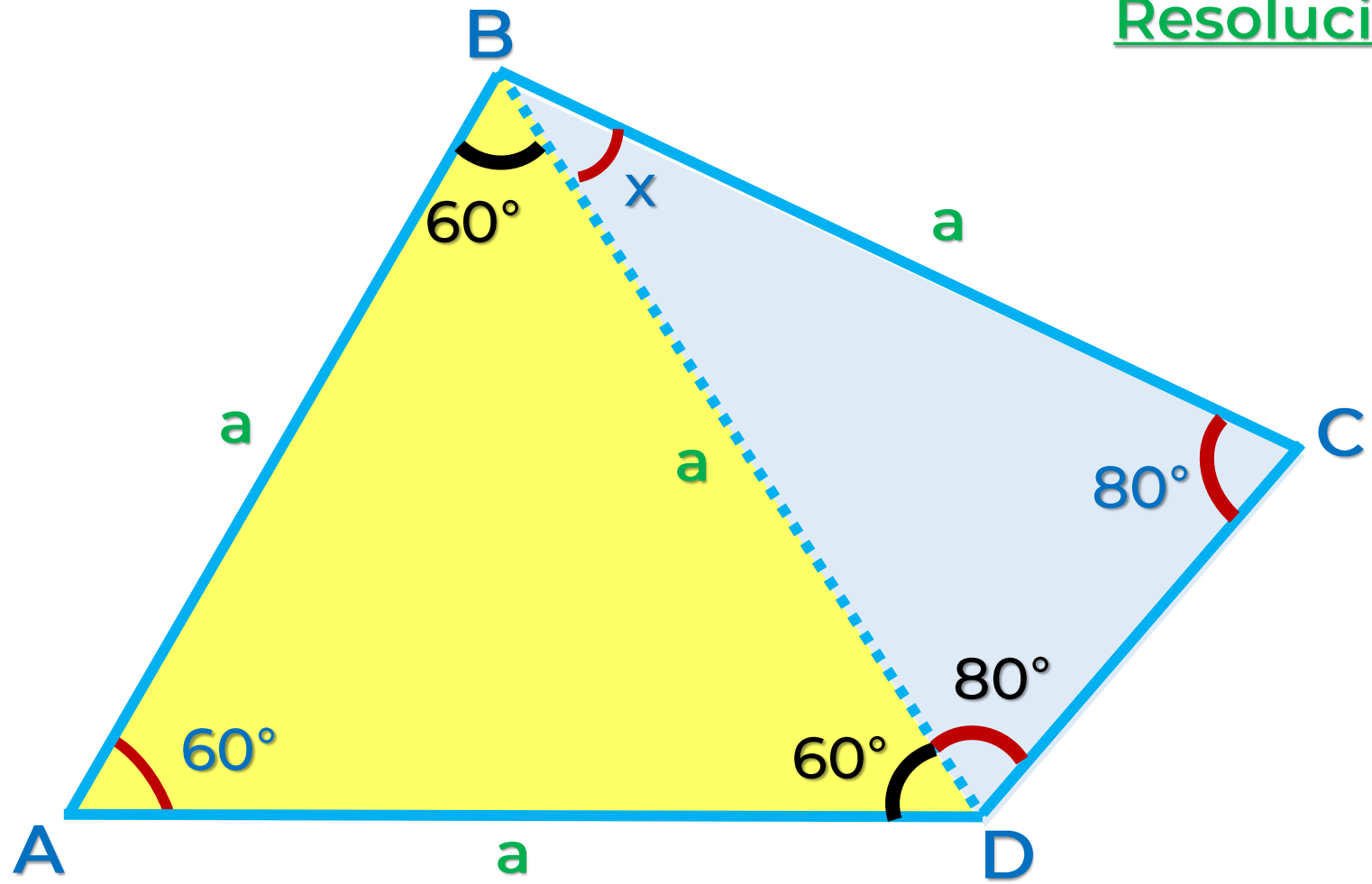
$$6^\circ < x$$

$$x = 7^\circ, 8^\circ, 9^\circ \dots$$

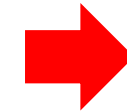
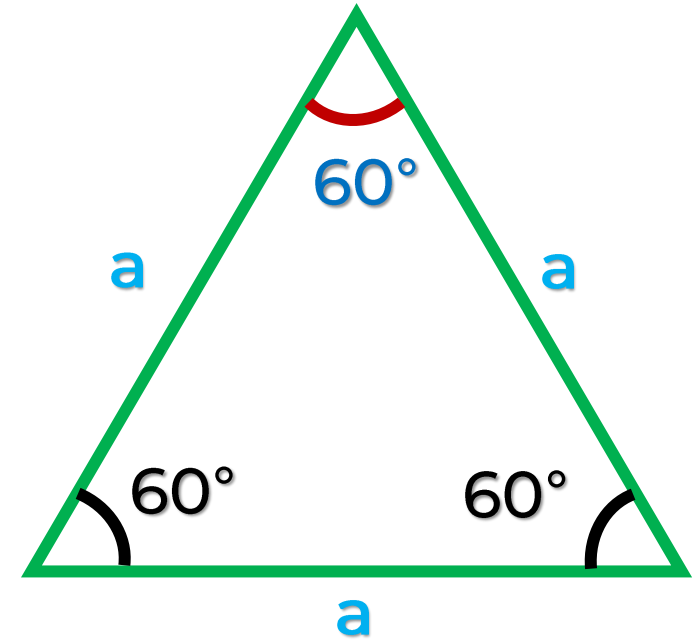
$$x_{\min} = 7^\circ$$



4. Halle el valor de x si $AB = AD = BC$.



Resolución



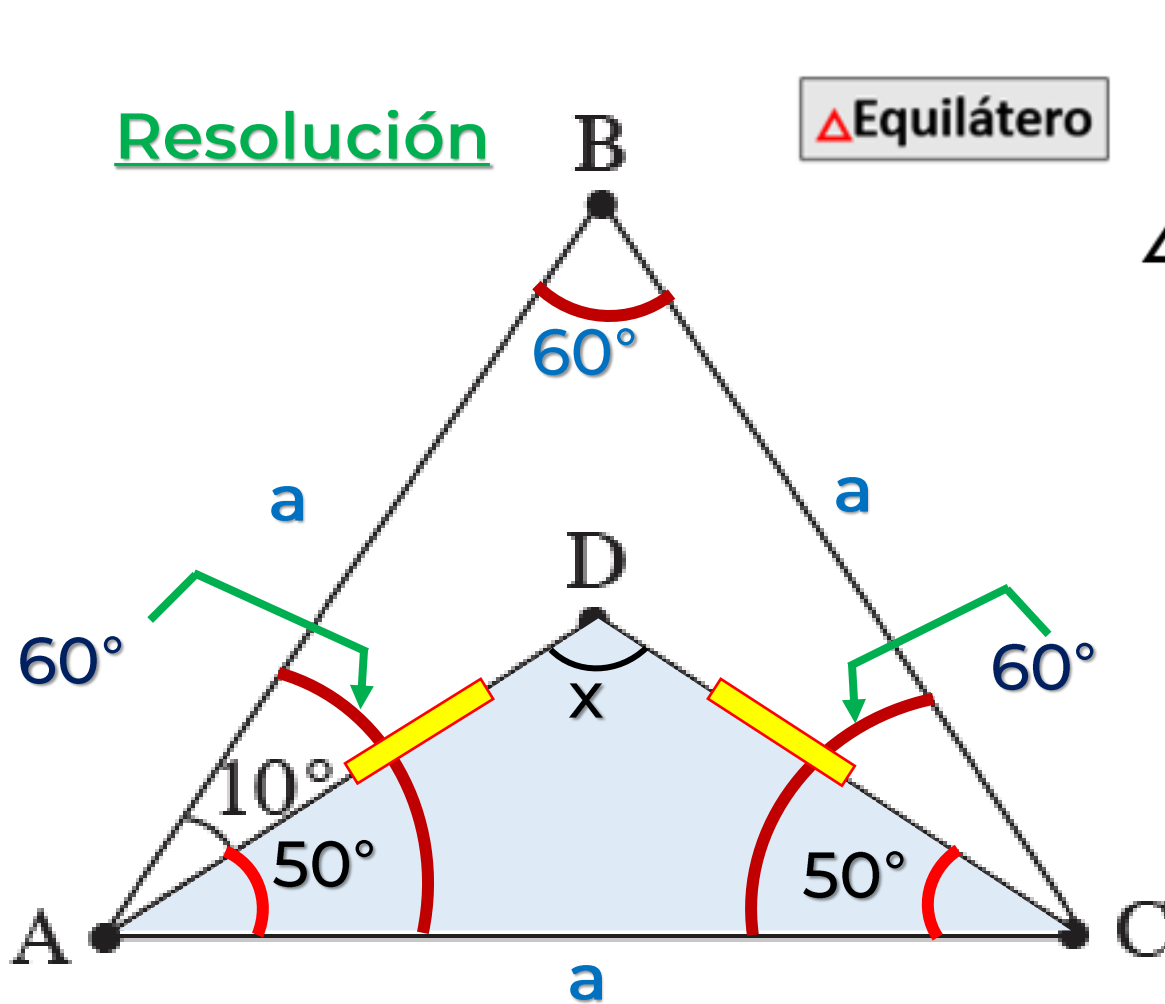
$\triangle BCD$: ISÓSCELES

$$x = 20^\circ$$

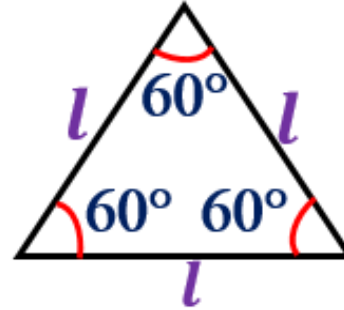


5. Si ABC es un triángulo equilátero y $AD = DC$, Halle el valor de x .

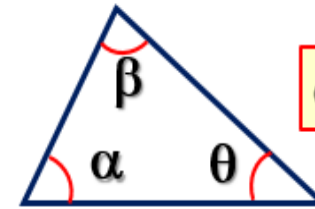
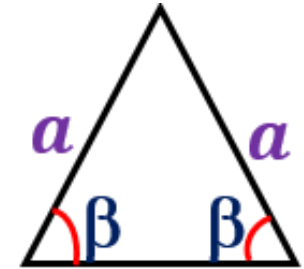
Resolución



△ Equilátero



△ Isósceles



$$\alpha + \beta + \theta = 180^\circ$$

△ ACD : Isósceles



$$50^\circ + 50^\circ + x = 180^\circ$$

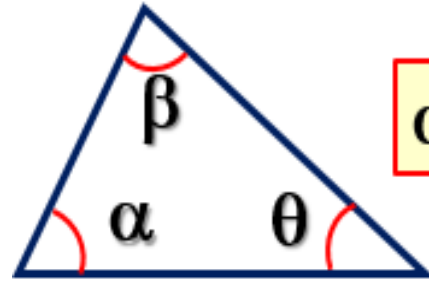
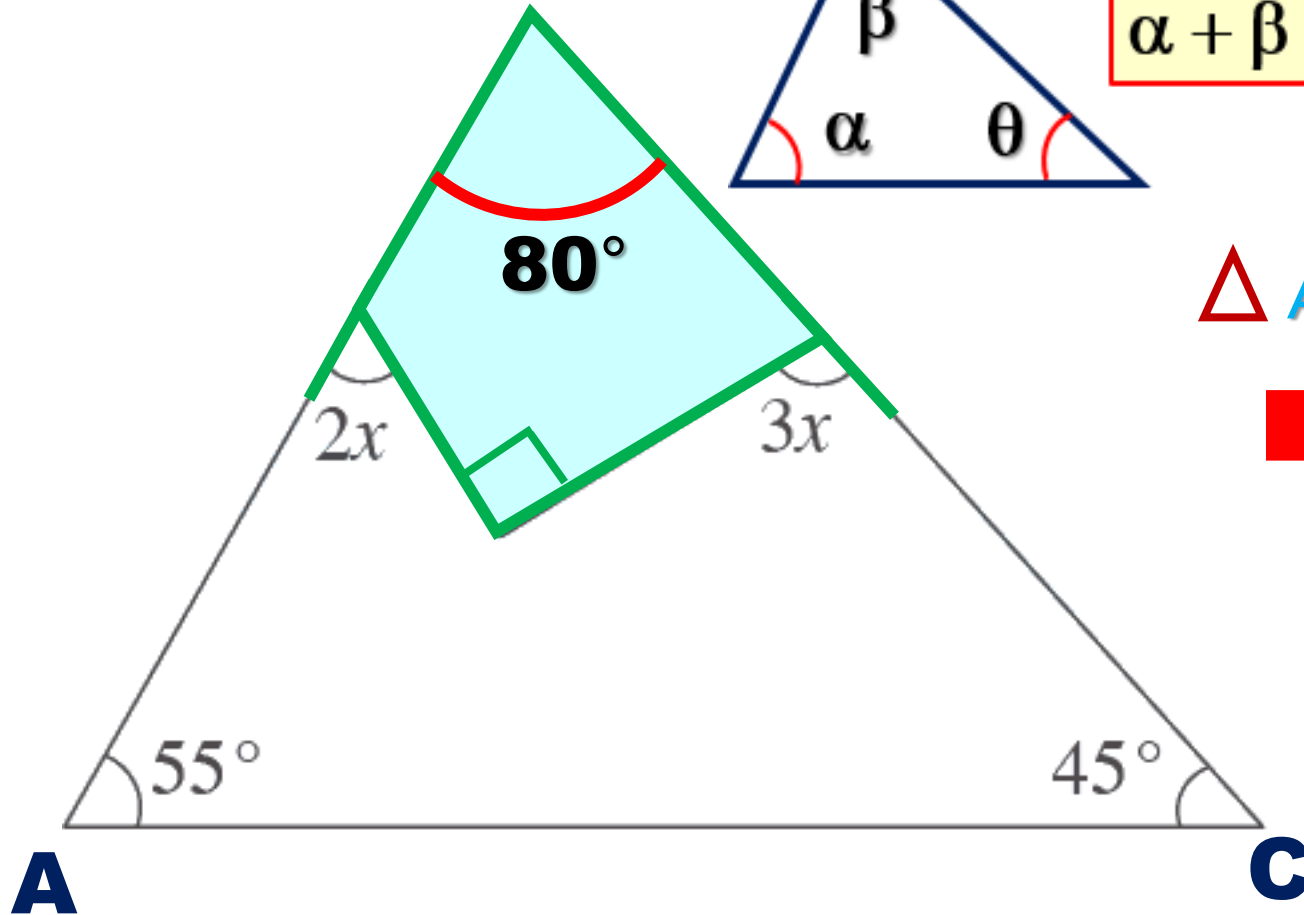
$$x = 80^\circ$$



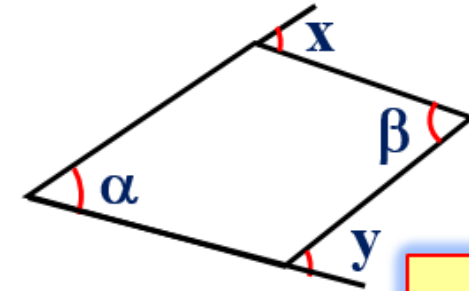
6. Halle el valor entero de x.

Resolución

B



$$\alpha + \beta + \theta = 180^\circ$$



$$x + y = \alpha + \beta$$

$\triangle ABC$:



$$\begin{aligned} \bullet \quad 55^\circ + 45^\circ + \beta &= 180^\circ \\ \beta &= 80^\circ \end{aligned}$$

$$\begin{aligned} \bullet \quad 80^\circ + 90^\circ &= 2x + 3x \\ 170^\circ &= 5x \end{aligned}$$

$$x = 34^\circ$$



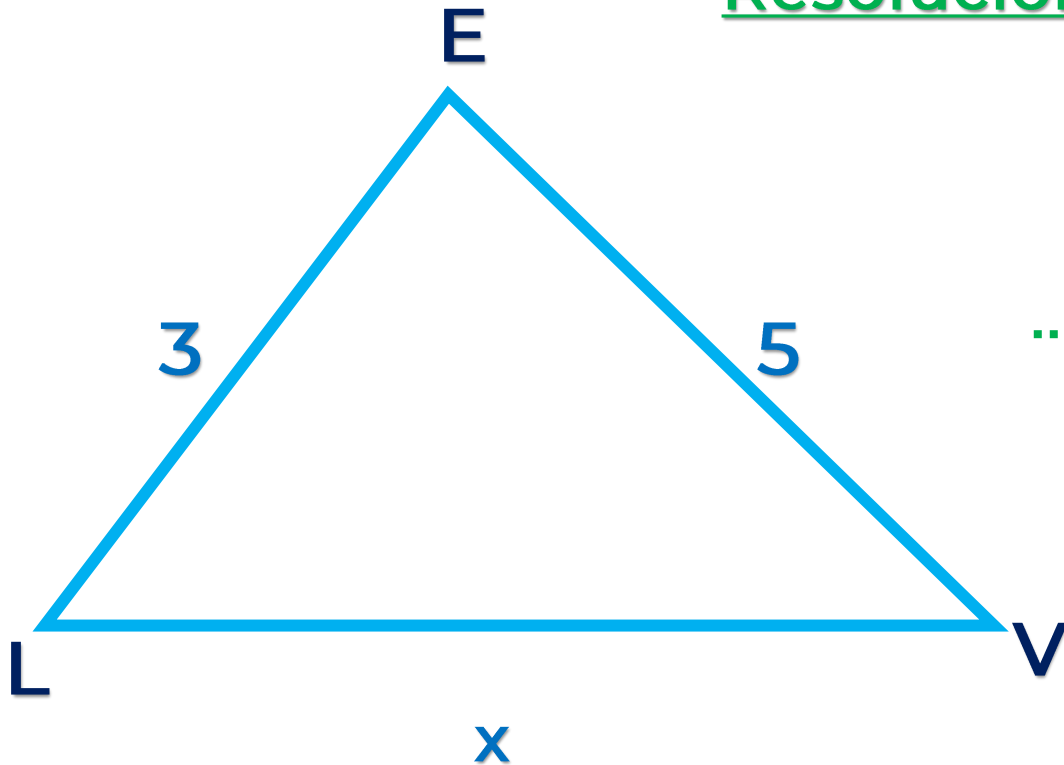
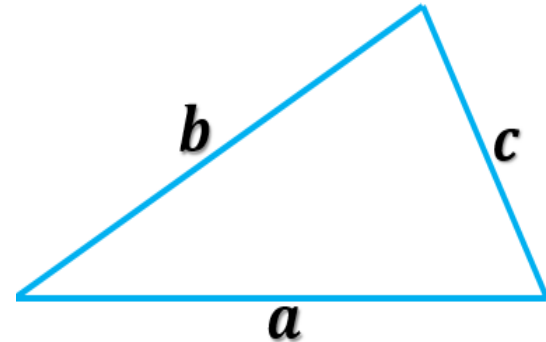
7. Calcule la suma de valores enteros de LV si LEV es un triángulo escaleno.

Resolución

• Teorema de la existencia

donde: $c < b < a$

$$b - c < a < b + c$$



$$5 - 3 < x < 5 + 3$$

$$2 < x < 8$$

$$x = 3 ; 4 ; 5 ; 6 ; 7$$

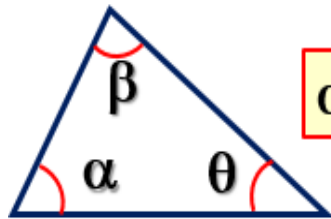
Nos piden:

$$3 + 4 + 5 + 6 + 7 = 25$$

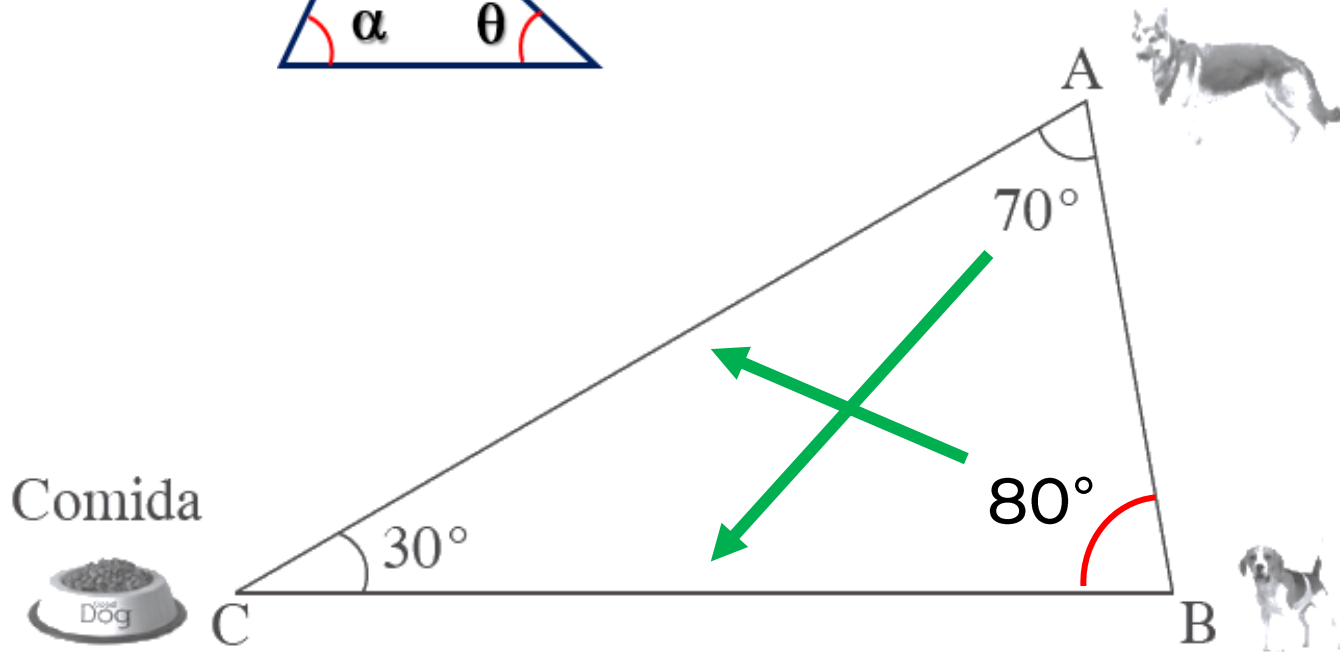


8. En la figura, ¿Cuál de los dos canes se encuentra más cerca a la comida.

Resolución



$$\alpha + \beta + \theta = 180^\circ$$



• Teorema de la correspondencia



Si: $\beta < \alpha$

$$b < a$$

$$BC < AC$$

El can en el vértice B