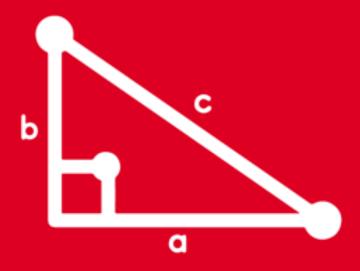
TRIGONOMETRY ADVISORY





TOMOS 5 y 6





1. Simplifique la expresión: $E = \frac{\cos(x + y)}{\sin x \cos y} - \cot x$

RESOLUCIÓN

$$cos(x+y) = cosx.cosy-senx.seny$$

$$E = \frac{\cos(x + y)}{\sin x \cos y} - \cot x$$

$$E = \frac{\cos x \cos y - \sin x \sin y}{\sin x \cos y} - \cot x$$

$$E = \frac{\cos x \cos y}{\sec x \cos y} - \frac{\sec x \sec y}{\sec x \cos y} - \cot x$$

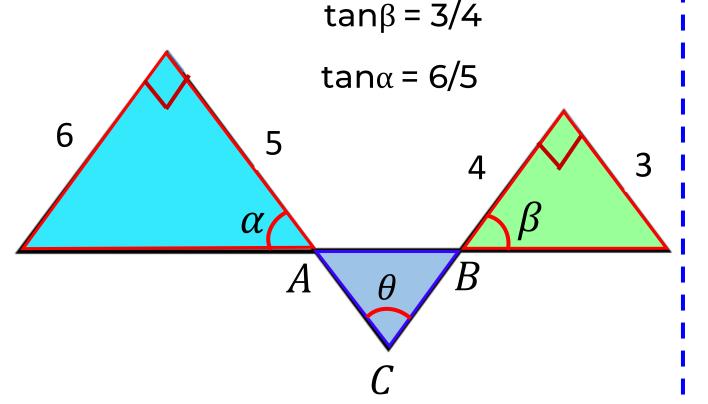
$$E = \frac{\cos x}{\sin x} - \frac{\sin y}{\cos y} - \cot x$$

$$E = \cot x - \tan y - \cot x$$



2. Del gráfico, halle el valor de $tan\theta$.

RESOLUCIÓN



Si
$$x + y + z = 180^{\circ}$$
, se cumple:
tanx + tany + tanz = tanx.tany.tanz

ABC: $\alpha + \beta + \theta = 180^{\circ}$ $\tan \alpha + \tan \beta + \tan \theta = \tan \alpha \cdot \tan \beta \cdot \tan \theta$ $\frac{6}{5} + \frac{3}{4} + \tan\theta = \frac{6}{5} \cdot \frac{3}{4} \cdot \tan\theta$ $\frac{39}{20} + \tan\theta = \frac{18}{20} \cdot \tan\theta$ $\frac{2}{20} = -\frac{2}{20} \cdot \tan\theta$

 $\therefore \tan\theta = -39/2$



3. Simplifica la expresión:

$$T = \frac{\sin^3 x - \cos^3 x}{\sin x - \cos x} + 5\sin x \cos x$$

RESOLUCIÓN

$$T = \frac{\text{sen}^3 x - \cos^3 x}{\text{sen} x - \cos x} + 5 \text{sen} x \cos x$$

$$T = \frac{(\text{senx} - \cos x)(\text{sen}^2 x + \text{senxcosx} + \cos^2 x)}{(\text{senx} - \cos x)} + 5\text{senxcosx}$$

$$T = sen^2x + cos^2x + senxcosx + 5senxcosx$$

$$T = 1 + 3(2 \frac{\text{senxcosx}}{\text{sen2x}})$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

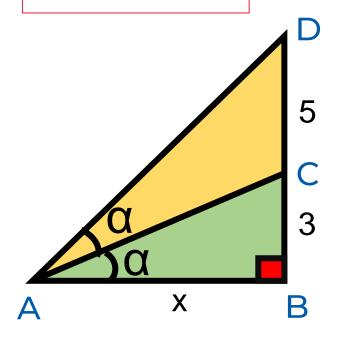
$$sen 2x = 2 sen x cos x$$

$$\sin^2 x + \cos^2 x = 1$$





RESOLUCIÓN



$$tan2\alpha = \frac{2tan\alpha}{1-tan^2\alpha}$$

$$\triangle$$
ABC: $\tan \alpha = \frac{3}{x}$

ABD:
$$\tan 2\alpha = \frac{8}{x}$$

$$\Rightarrow \frac{2\tan\alpha}{1-\tan^2\alpha} = \frac{8}{x}$$

$$\Rightarrow \frac{2\left(\frac{3}{X}\right)}{1-\left(\frac{3}{X}\right)^2} = \frac{8}{X}$$

$$\Rightarrow \frac{\frac{6}{x}}{1 - \frac{9}{x^2}} = \frac{8}{x}$$

$$\Rightarrow x \left(\frac{6}{x} \right) = 8 \left(1 - \frac{9}{x^2} \right)$$

$$\Rightarrow 6 = 8 - \frac{72}{x^2} \Rightarrow \frac{72}{x^2} = 2$$





De la condición: tanx + cotx = 12Calcule: sen2x

RESOLUCIÓN

Recordar:
$$cot(x) + tan(x) = 2csc(2x)$$



$$\csc(x) = \frac{1}{\text{sen}(x)}$$

$$\cot x + \tan x = 12$$

$$2\csc 2x = 12$$

$$csc2x = 6$$

$$\therefore$$
 sen2x = $\frac{1}{6}$



6. Reduzca la expresión: $=\frac{+}{-}\frac{\theta}{\theta}-\frac{+}{-}$

Recordar:

 $2\cos^2(x) = 1 + \cos(2x)$

 $2\mathrm{sen}^2(x) = 1 - \cos(2x)$

sen 2x = 2 sen x cos x

$$\csc^2 x - \cot^2 x = 1$$

$$\cot x = \frac{\cos x}{\sin x}$$

$$cscx = \frac{1}{sen x}$$

RESOLUCIÓN

$$P = \frac{4(1+\cos 4\theta)}{1-\cos 8\theta} - \frac{1+\cos 4\theta}{1-\cos 4\theta} \qquad P = \frac{4\cos^2 2\theta}{4\sin^2 2\theta\cos^2 2\theta} - \cot^2 2\theta$$

$$P = \frac{4(2\cos^{2}2\theta)}{2\sin^{2}4\theta} - \frac{2\cos^{2}2\theta}{2\sin^{2}2\theta} \qquad P = \frac{1}{\sin^{2}2\theta} - \cot^{2}2\theta$$

$$P = \frac{4\cos^2 2\theta}{(sen 4\theta)^2} - \frac{\cos^2 2\theta}{sen^2 2\theta}$$

$$P = \frac{4\cos^2 2\theta}{(2\sin 2\theta \cos 2\theta)^2} - \cot^2 2\theta \qquad \therefore P = 1$$

$$P = \frac{4\cos^2 2\theta}{4\sin^2 2\theta \cos^2 2\theta} - \cot^2 2\theta$$

$$P = \frac{1}{sen^2 2\theta} - cot^2 2\theta$$

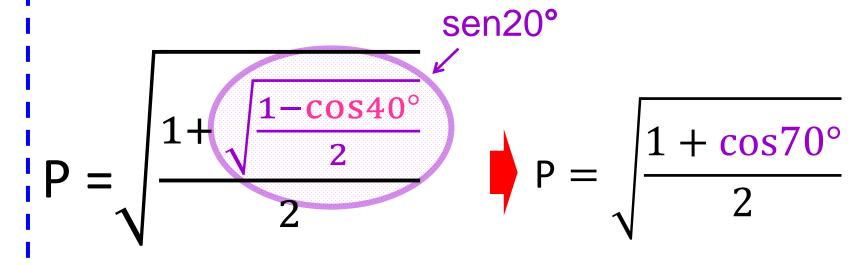
$$P = csc^2 2\theta - cot^2 2\theta$$



RESOLUCIÓN

$$\operatorname{sen}(\frac{x}{2}) = \pm \sqrt{\frac{1 - \cos x}{2}}$$

$$\cos(\frac{x}{2}) = \pm \sqrt{\frac{1+\cos x}{2}}$$



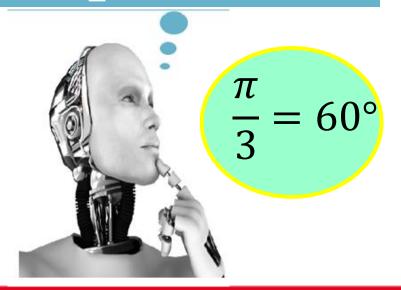
$$\therefore$$
 P = cos35°



8. Dar el valor de:
$$= \left(\frac{\pi}{-} \right)$$

RESOLUCIÓN

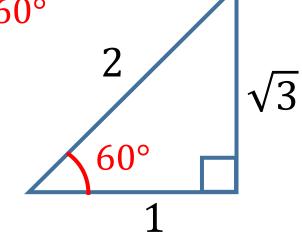
$$\cot\left(\frac{x}{2}\right) = \csc x + \cot x$$



$$\cot\left(\frac{x}{2}\right) = \csc x + \cot x \qquad E = \cot\left(\frac{37^{\circ}}{2}\right) - \sec\left(\frac{\pi}{3}\right)$$

$$E = csc(37^{\circ}) + cot(37^{\circ}) - sec60^{\circ}$$

$$E = \frac{5}{3} + \frac{4}{3} - 2$$

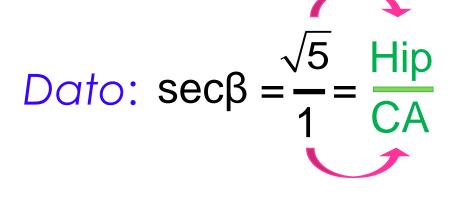


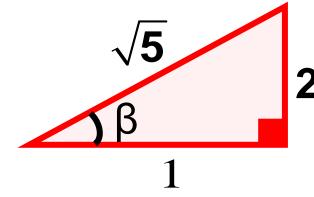


9. Si un ángulo β , cumple que $\beta = \sqrt{}$. Calcule

$$\beta = \sqrt{}$$
. Calcule β

RESOLUCIÓN





 \Rightarrow tan $\beta = 2$

Recordar:

$$tan3x = \frac{3tanx - tan^3x}{1 - 3tan^2x}$$

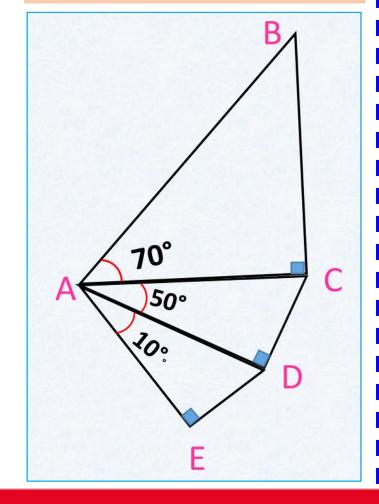


Piden:

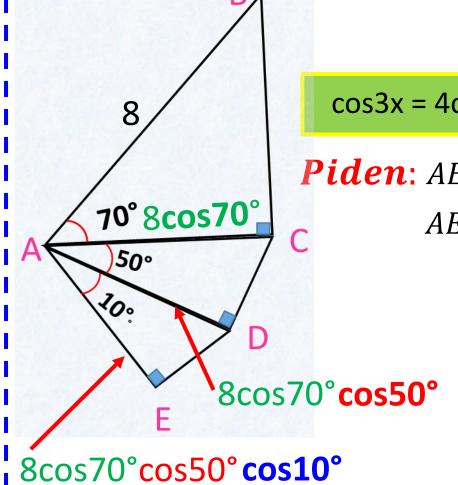
$$tan3\beta = \frac{3(2)-(2)^3}{1-3(2)^2} = \frac{-2}{-11}$$



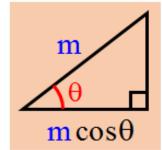
10. En la figura, AB = 8. Halle AE



RESOLUCIÓN



Recordar:



$$\cos 3x = 4\cos x.\cos(60^{\circ}-x).\cos(60^{\circ}+x)$$

Piden: $AE = 8.\cos 70^{\circ}\cos 50^{\circ}\cos 10^{\circ}$

$$AE = 2.4\cos 10^{\circ}\cos 50^{\circ}\cos 70^{\circ}$$

$$AE = 2\cos(3(10^\circ))$$

$$AE = 2\cos 30^{\circ} = 2.\frac{\sqrt{3}}{2}$$

$$\therefore$$
 AE = $\sqrt{3}$