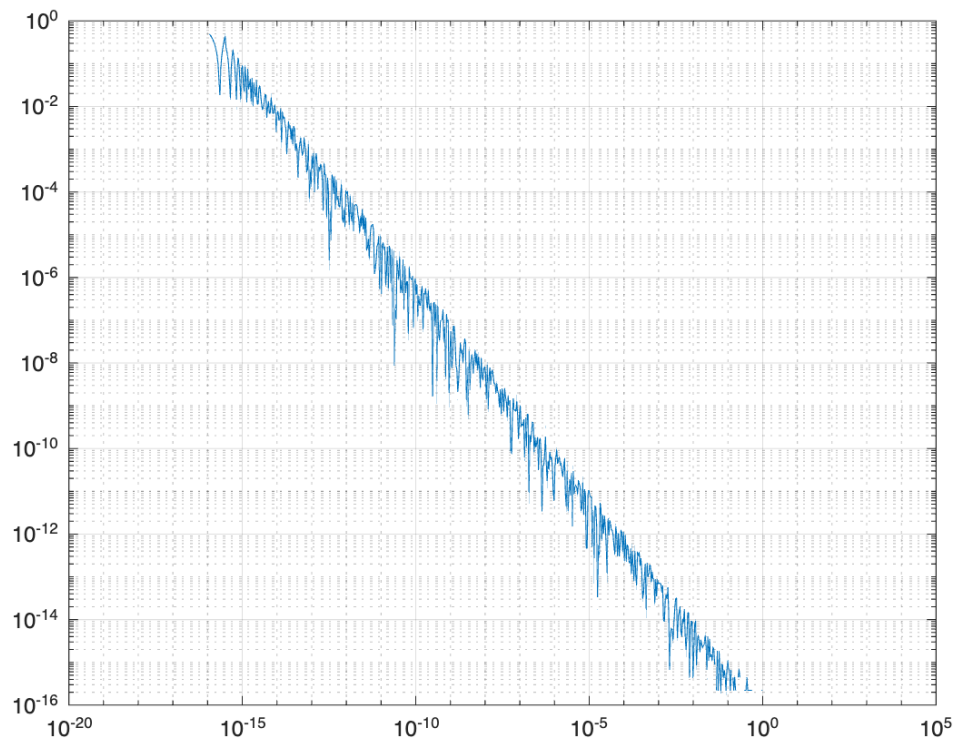


```
cl c; cl ear
```

Aufgabe1

```
cl c; cl ear;  
del ta = logspace(-20, 5, 1000);  
  
x = zeros(1, length(del ta));  
y = zeros(1, length(del ta));  
x_exact = 1.0; %  
for i = 1:length(del ta)  
    % del ta = 10 ^ (i -21);  
    P1 = [0. 1.];  
    P2 = [del ta(i) 1. + del ta(i)];  
    x(:, i) = del ta(i);  
    x_num = lineintersection(P1, P2);  
    y(:, i) = abs(x_exact - x_num);  
end  
  
loglog(x, y);  
grid on
```



Aufgabe 2

```
cl c; cl ear;
```

```
format long
```

```
x_node = [0.0 1.0 2.0 3.0 4.0];  
f_node = [0.0 0.031250 0.131687 0.237304 0.327680];
```

```
x = 0:0.01:4;  
y = (x./(x+1)).^5;  
% 0.6 是要推断的点
```

2.1 Grad 1

```
f1 = LagrangePolynom(0.6, 1, x_node, f_node)
```

```
f1 =  
0.0187500000000000
```

```
df1 = LagrangeDerivPolynom(0.6, 1, x_node, f_node)
```

```
df1 =  
0.0312500000000000
```

2.2 Grad 4

```
f4 = LagrangePolynom(0.6, 4, x_node, f_node)
```

```
f4 =  
0.0053986784000000
```

```
df4 = LagrangeDerivPolynom(0.6, 4, x_node, f_node)
```

```
df4 =  
0.0465926493333333
```

2.3 Grad 80

```
% 不使用原来的 x, fx, 而是使用[0.0, 4.0]区间内的 x 和对应的 y  
x80 = 0:0.05:4;  
y80 = (x80./(x80+1)).^5;  
f80 = LagrangePolynom(0.6, 80, x80, y80)
```

```
f80 =  
0.007415771484375
```

```
df80 = LagrangeDerivPolynom(0.6, 80, x80, y80)
```

```
df80 =  
0.038623370313570
```

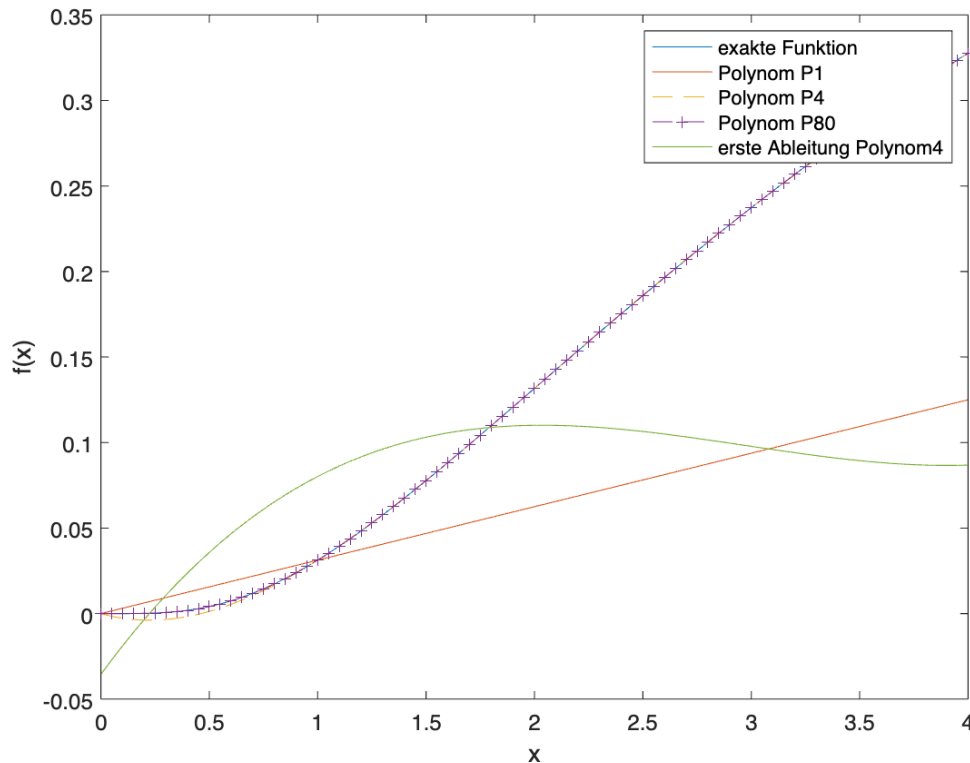
Plot

```
plot(x, y, ...  
     x, LagrangePolynom(x, 1, x_node, f_node), ...  
     x, LagrangePolynom(x, 4, x_node, f_node), '--', ...  
     x80, LagrangePolynom(x80, 80, x80, y80), '--+', ...  
     x, LagrangeDerivPolynom(x, 4, x_node, f_node))  
xlabel('x');
```

```

ylabel('f(x)');
legend('exakte Funktion', 'Polynom P1', 'Polynom P4', ...
      'Polynom P80', 'erste Ableitung Polynom4')

```



```

function x_numeric = lineintersection(P1, P2)
% "计算两个点的交点的数值解";
% y= kx+b y=2, b=1
% k=(y2-y1)/(x2-x1)
k = (P2(2) - P1(2))/(P2(1) - P1(1));
x_numeric = 1/k;
end

function wert_basis = LagrangeBasis(x, n, i, x_node)
wert_basis = 1;
for k = 1: n+1
    if k ~= i
        wert_basis = wert_basis .* (x - x_node ...
            (k))./(x_node(i) - x_node(k));
    % else
    % wert_basis = wert_basis*1;
    end
end
end

function wert_poly = LagrangePolynom(x, n, x_node, f_node)
wert_poly = 0;

```

% 原版是 $k = 1:n+1$, i 对应课件

```
for i = 1: n+1
```

```
    wert_poly = wert_poly + LagrangeBasis(x, n, i, x_node). *f_node(i);
```

```
end
```

```
end
```

```
function wert_dBasis = LagrangeDerivBasis(x, n, i, x_node)
```

```
wert_dBasis=0;
```

```
for m=1:n+1
```

```
    value_inner=1;
```

```
    if m~=i
```

```
        for k=1:n+1
```

```
            if k~=i && k~=m
```

```
                value_inner=value_inner. *(x-x_node(k))/(x_node(i)-x_node(k));
```

```
            % else
```

```
            %     value_inner = 1. *value_inner;
```

```
            end
```

```
        end
```

```
        wert_dBasis = wert_dBasis + value_inner ./ (x_node(i) - x_node(m));
```

```
    % else
```

```
    %     wert_dBasis=wert_dBasis;
```

```
end
```

```
end
```

```
end
```

```
function wert_dpoly = LagrangeDerivPolynom(x, n, x_node, f_node)
```

```
wert_dpoly = 0;
```

```
for i = 1:n+1
```

```
    wert_dpoly = wert_dpoly + LagrangeDerivBasis(x, n, i, x_node). *f_node(i);
```

```
end
```

```
end
```