

The code:

```
import numpy as np
import math

def P(x):
    return math.exp(-x**2)/math.sqrt(math.pi)

def f(x):
    return x**2

N = 100
xL = -10. # 10 is close enough to infinity
xR = 10.

xvals = np.linspace(xL, xR, N)
fsum = 0
for x in xvals:
    fsum += f(x)*P(x)

print(fsum/N*(xR-xL))
```

Computes the integral:

$$\int_{-\infty}^{\infty} x^2 \frac{e^{-x^2}}{\sqrt{\pi}} dx$$

Since the above code is equivalent to:

$$\frac{1}{N(b-a)} \sum_{i=1}^N f(x_i) P(x_i)$$

Where $a = x_L, b = x_R$ and $x_i = a + \Delta x \cdot i$. This can be written as:

$$\sum_{i=1}^N \Delta x f(x_i) P(x_i)$$

In the limiting case as $N \rightarrow \infty$ we get:

$$\lim_{N \rightarrow \infty} \sum_{i=1}^N \Delta x (f(x_i) P(x_i)) = \int_a^b (f(x) P(x)) dx = \int_a^b x^2 \frac{e^{-x^2}}{\sqrt{\pi}} dx$$

Then as $a \rightarrow -\infty$ and $b \rightarrow \infty$ we get the integral as required.