

Plan Merging in Asprilo's m-Domain

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- 1 Asprilo and its m-Domain
- 2 Plan Merging and our Approach
- 3 Merging Strategies
- 4 Evaluation

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What is *asprilo*?

- Framework for intra-logistics & warehouse automation based on Answer Set Programming (ASP)
- Consists of
 - domain specifications (a, b, c and m)
 - plan checker
 - instance generator
 - visualizer
- Goal: Allow for generation of plans, that account for robot movement and fulfillment of orders

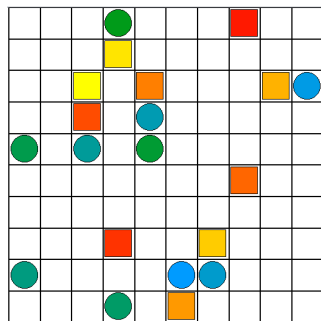


Figure: an asprilo warehouse in its visualizer

- The simplest domain, “movement only”

square A robot

circle A destination for any robot

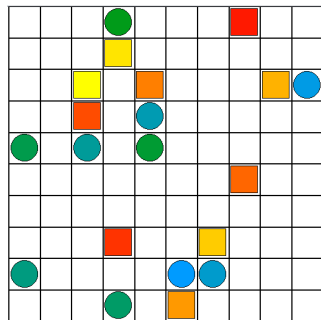


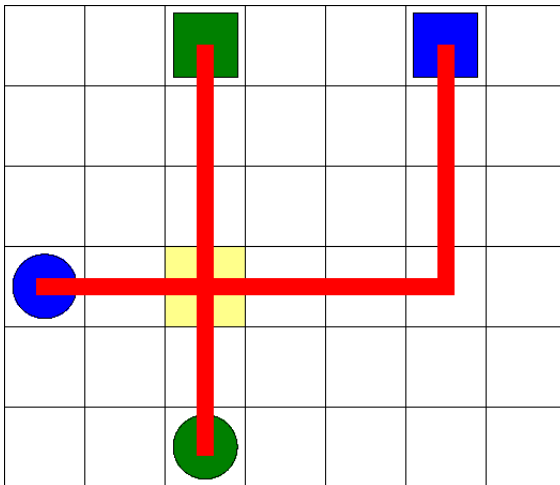
Figure: an asprilo instance of the m-domain

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What is Plan Merging?

Unlike global planning, distributed planning needs plan merging



What is Plan Merging?

Unlike global planning, distributed planning needs plan merging

Advantages of plan merging are:

- Reduced complexity and computation time
- Avoiding re-planning when adding plans
- Plans can be computed in parallel

Important considerations are:

- Conflicts between single plans, such as robot collisions
- Plan has to stay valid
- Optimization of merged plan

Our Approach for Plan Merging

Standard, global approach:

- ① **Centralized Plan generation**

... for all robots by allowing arbitrary movements and forbidding collisions and unfulfilled orders

Our distributed approach:

- ① **Target assignment**

... optimizing for the smallest single distance between robot and shelf

- ② **Plan generation**

... without collision constraints

- ③ **Plan merging**

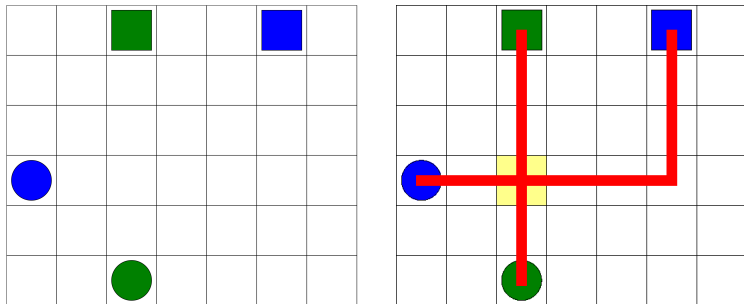
Target Assignment

```
1 { assigned(R,S) : isShelf(S) } = 1 :- isRobot(R).  
2 distance(R,S,D) :- position(R,(RX,RY),0),  
3                     position(S,(SX,SY),0),  
4                     assigned(R,S),  
5                     D = |RX - SX| + |RY - SY|.   
6 #minimize { D : distance(R,S,D) }.
```

`assigned(R,S)` : robot R is assigned to shelf S

Plan Generation

- Standard m-encoding but without collision constraints
 - assigns each robot a destination
 - plans moves without avoiding collisions
- Parallel independent planning for all robots at once



$\text{planmov}(R,D,T)$: robot R plans to take step in direction D at time step t

$\text{planpos}(R,C,T)$: robot R plans to be at cell C at time step T

- We generally allow for arbitrary movement, but forbid certain moves using different strategies
- Strategies add constraints based on the plans
- Strategies can be freely combined to further reduce the search space

atoms after merging of all plans:

`move(R,D,T)` : robot R takes step in direction D at time step t

`position(R,C,T)` : robot R is at cell C at time step T

Plan Merging: *basefile.lp*

- Merge baseline, and included in every merge call
- Contains move generation and position calculation
- Avoids moves that would lead to crashing of robots
- Generates itself a valid plan

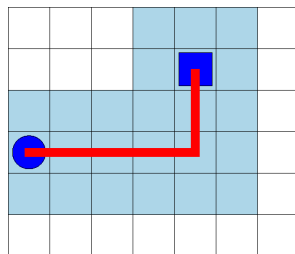
```
1 { move(R,D,T) : direction(D) } 1 :- isRobot(R),  
    time(T).  
2 :- error(_).  
  
...
```

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Corridor

```
1  surrounds((-s..s,-s..s)).  
2  possible(R,(X+DX,Y+DY)):-  
    planpos(R,(X,Y),_),  
    surrounds((DX,DY)).  
3  :- isRobot(R), position(R,C,_),  
    not possible(R,C).
```

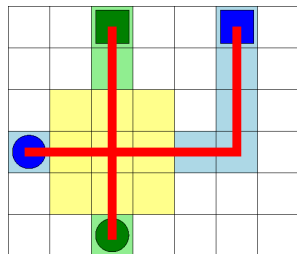


$s = 1$
time(0)

Idea: Allow each robot only to move to squares close to its planned trajectory

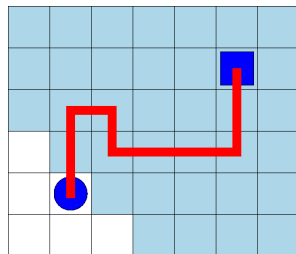
Bottleneck

```
1 possible(R,C) :- planpos(R,C,-).
2 possible(R1,(X+DX,Y+DY)) :-
    planpos(R1,(X,Y,-),
    planpos(R2,(X,Y,-),
    R2 != R1, surrounds((DX,DY)).
3 :- isRobot(R), position(R,C,-),
    not possiblePosB(R,C).
```



Idea: Constraint moves even further than corridor, by only allowing to deviate from the plan at conflict cells

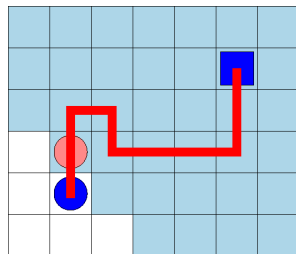

```
1 :- position(R, (X1,Y1),T),  
    planpos(R, (X2,Y2),T),  
    assigned(R,S),  
    position(S, (SX,SY),0),  
    D1 = |SX-X1| + |SY-Y1| ,  
    D2 = |SX-X2| + |SY-Y2| ,  
    D1 > D2.
```



time(0)

Idea: Disallow robot to fall behind its plan in terms of distance to its goal

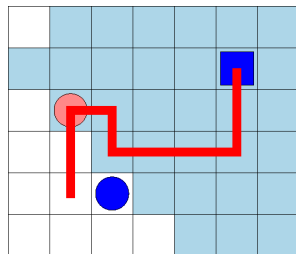
```
1 :- position(R, (X1,Y1),T),  
    planpos(R, (X2,Y2),T),  
    assigned(R,S),  
    position(S, (SX,SY),0),  
    D1 = |SX-X1| + |SY-Y1| ,  
    D2 = |SX-X2| + |SY-Y2| ,  
    D1 > D2.
```



time(1)

Idea: Disallow robot to fall behind its plan in terms of distance to its goal

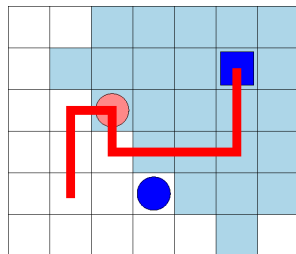
```
1 :- position(R, (X1,Y1),T),  
    planpos(R, (X2,Y2),T),  
    assigned(R,S),  
    position(S, (SX,SY),0),  
    D1 = |SX-X1| + |SY-Y1| ,  
    D2 = |SX-X2| + |SY-Y2| ,  
    D1 > D2.
```



time(2)

Idea: Disallow robot to fall behind its plan in terms of distance to its goal

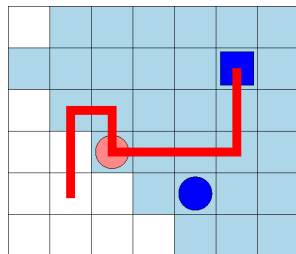
```
1 :- position(R, (X1, Y1), T),  
    planpos(R, (X2, Y2), T),  
    assigned(R, S),  
    position(S, (SX, SY), 0),  
    D1 = |SX-X1| + |SY-Y1| ,  
    D2 = |SX-X2| + |SY-Y2| ,  
    D1 > D2.
```



time(3)

Idea: Disallow robot to fall behind its plan in terms of distance to its goal

```
1 :- position(R, (X1,Y1),T),  
    planpos(R, (X2,Y2),T),  
    assigned(R,S),  
    position(S, (SX,SY),0),  
    D1 = |SX-X1| + |SY-Y1| ,  
    D2 = |SX-X2| + |SY-Y2| ,  
    D1 > D2.
```

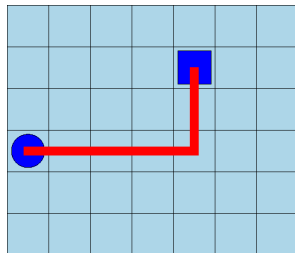


time(4)

Idea: Disallow robot to fall behind its plan in terms of distance to its goal

Homesick

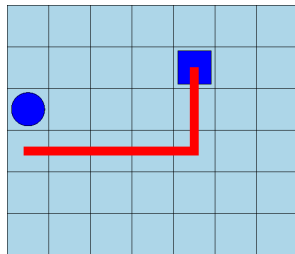
```
1 homesick(T) :- time(T),  
    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
```



interval = 3
time(0)

Idea: Make robots converge to their original trajectory every few moves

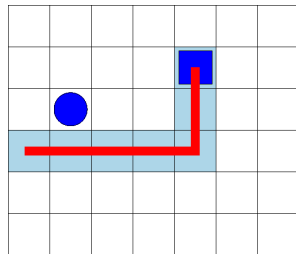
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    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
```



interval = 3
time(1)

Idea: Make robots converge to their original trajectory every few moves

```
1 homesick(T) :- time(T),  
    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
```

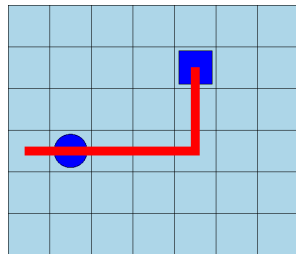


interval = 3
time(2)

Idea: Make robots converge to their original trajectory every few moves

Homesick

```
1 homesick(T) :- time(T),  
    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
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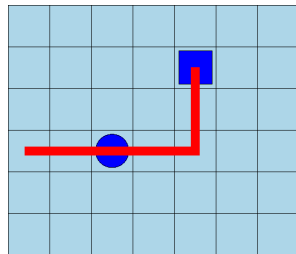


interval = 3
time(3)

Idea: Make robots converge to their original trajectory every few moves

Homesick

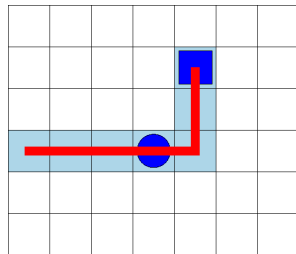
```
1 homesick(T) :- time(T),  
    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
```



interval = 3
time(4)

Idea: Make robots converge to their original trajectory every few moves

```
1 homesick(T) :- time(T),  
    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
```

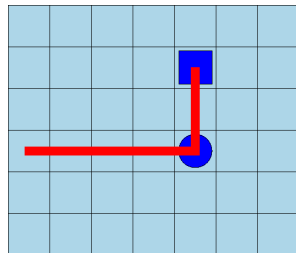


interval = 3
time(5)

Idea: Make robots converge to their original trajectory every few moves

Homesick

```
1 homesick(T) :- time(T),  
    T \ interval = 0.  
2 :- homesick(T), isRobot(R),  
    position(R,C,T),  
    not planpos(R,C,-).
```

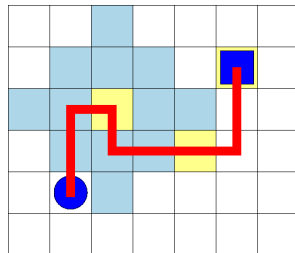


interval = 3
time(6)

Idea: Make robots converge to their original trajectory every few moves

Checkpoints

- 1 $\text{:- checkpoint}(R, CP, C),$
 $\text{position}(R, CP, T),$
 $\text{not reached}(R, CP, T),$
 $T = CP * \text{step}.$
- 2 $\text{:- goalpoint}(R, CP, C),$
 $\text{reached}(R, CP, T1),$
 $\text{move}(R, D, T2), T1 > T2.$

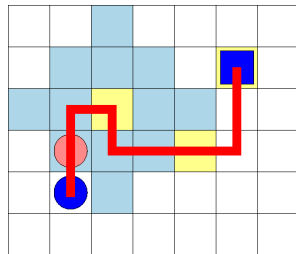


interval = 3
time(0)

Idea: Force robots to visit their planned cell every few moves

Checkpoints

- 1 $\text{:- checkpoint}(R, CP, C),$
 $\text{position}(R, CP, T),$
 $\text{not reached}(R, CP, T),$
 $T = CP * \text{step}.$
- 2 $\text{:- goalpoint}(R, CP, C),$
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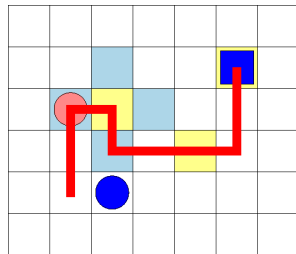


interval = 3
time(1)

Idea: Force robots to visit their planned cell every few moves

Checkpoints

```
1 :- checkpoint(R,CP,C),  
    position(R,CP,T),  
    not reached(R,CP,T),  
    T = CP*step.  
2 :- goalpoint(R,CP,C),  
    reached(R,CP,T1),  
    move(R,D,T2), T1 > T2.
```

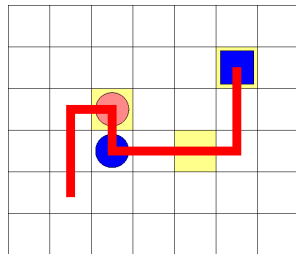


interval = 3
time(2)

Idea: Force robots to visit their planned cell every few moves

Checkpoints

```
1 :- checkpoint(R, CP, C),  
    position(R, CP, T),  
    not reached(R, CP, T),  
    T = CP*step.  
2 :- goalpoint(R, CP, C),  
    reached(R, CP, T1),  
    move(R, D, T2), T1 > T2.
```

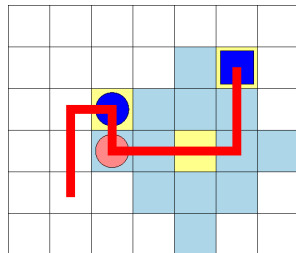


interval = 3
time(3)

Idea: Force robots to visit their planned cell every few moves

Checkpoints

- 1 $\text{:- checkpoint}(R, CP, C),$
 $\text{position}(R, CP, T),$
 $\text{not reached}(R, CP, T),$
 $T = CP * \text{step}.$
- 2 $\text{:- goalpoint}(R, CP, C),$
 $\text{reached}(R, CP, T1),$
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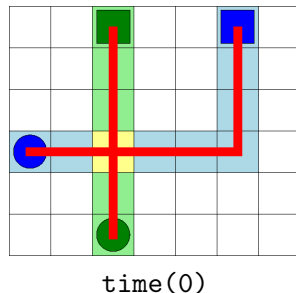


interval = 3
time(4)

Idea: Force robots to visit their planned cell every few moves

Crossroad

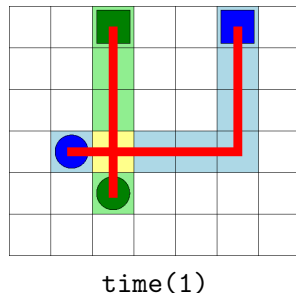
- 1 $\text{:- not orderedPlan}(R, _, O, D),$
 $\text{orderedMoves}(R, _, O, D).$
- 2 $\text{:- not orderedMoves}(R, _, O, D),$
 $\text{orderedPlan}(R, _, O, D).$
- 3 $\text{:- orderedPlan}(R, T, O, _),$
 $\text{orderedMoves}(R, T', O, _),$
 $|T - T'| > \text{maximumOffset}.$



Idea: Allow to change the timing of moves but keep their order

Crossroad

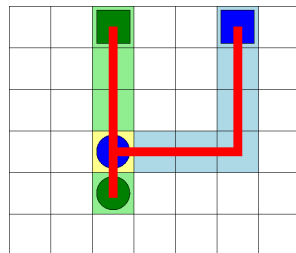
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- 2 $\text{:- not orderedMoves}(R, _, O, D),$
 $\text{orderedPlan}(R, _, O, D).$
- 3 $\text{:- orderedPlan}(R, T, O, _),$
 $\text{orderedMoves}(R, T', O, _),$
 $|T - T'| > \text{maximumOffset}.$



Idea: Allow to change the timing of moves but keep their order

Crossroad

- 1 `:- not orderedPlan(R,_,O,D),
orderedMoves(R,_,O,D).`
- 2 `:- not orderedMoves(R,_,O,D),
orderedPlan(R,_,O,D).`
- 3 `:- orderedPlan(R,T,O,_),
orderedMoves(R,T',O,_),
|T - T'| > maximumOffset.`

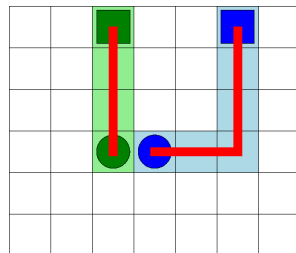


time(2)

Idea: Allow to change the timing of moves but keep their order

Crossroad

- 1 `:- not orderedPlan(R,_,O,D),
orderedMoves(R,_,O,D).`
- 2 `:- not orderedMoves(R,_,O,D),
orderedPlan(R,_,O,D).`
- 3 `:- orderedPlan(R,T,O,_),
orderedMoves(R,T',O,_),
|T - T'| > maximumOffset.`



time(3)

Idea: Allow to change the timing of moves but keep their order

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Benchmark Setup

- Executed on V-Server with the following specs:
 - 16 VCores Intel Xenon E5-2680-v3
 - 32GB RAM
 - Debian 18.04.4 LTS
 - Python 3.7.7
 - clingo 5.4.0
- Additional strategy “replan” was benchmarked:
complete replanning after target assignment and plan generation
→ Baseline for other strategies
Only basefile.lp without any strategy

- Three types of quadratic instances according to asprilo's m-domain specifications:
 - Sparse** 10% of edge length as robots
 - Normal** 100% of edge length as robots
 - Cluttered** 10% of number of cells as robots
- 10 instances each for edge lengths of 10, 20, 30, \dots , 100
- For cluttered edge lengths of over 50 were infeasible to ground, so we have generated additional instances between 30 and 50

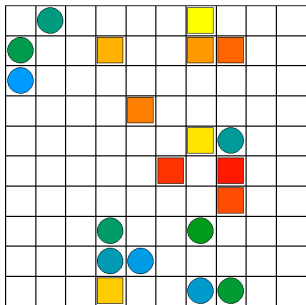


Figure: cluttered 10x10

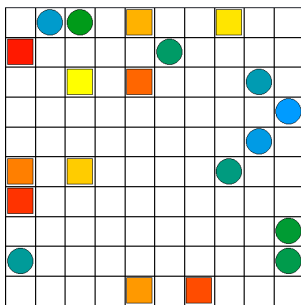


Figure: normal 10x10

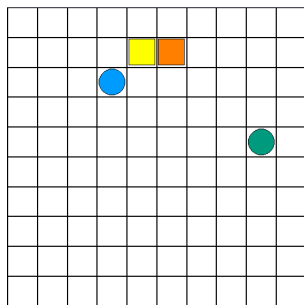


Figure: sparse 10x10

Hypothesis on Single Strategies

| Corridor | Bottleneck | Checkpoints |
|---------------------|---------------------------|---------------------|
| ~ ok performance | + better than Corridor | ~ ok performance |

| Homesick | Deathlaser | Crossroad |
|----------------------------|----------------------------|----------------------|
| + very good performance | + very good performance | - bad performance |

Configuration Clingo 5.4.0 + baseline.lp + Strategy

Hypothesis on Strategy Combinations

| | Corridor | Bottleneck | Checkp. | Homesick | Deathlaser |
|------------|----------------------------|-------------------------------|--|--------------------|------------|
| Bottleneck | — Corridor redundant | | | | |
| Checkp. | + | — Checkpoints redundant | | | |
| Homesick | ~ | — Homesick redundant | ~ Highly depends on hyper- parameters | | |
| Deathlaser | + | + | — Deathlaser redundant | + = Checkpoints | |
| Crossroad | — no benefit | — no benefit | — no benefit | — no benefit | + |

Configuration Clingo 5.4.0 + baseline.lp + Strategies

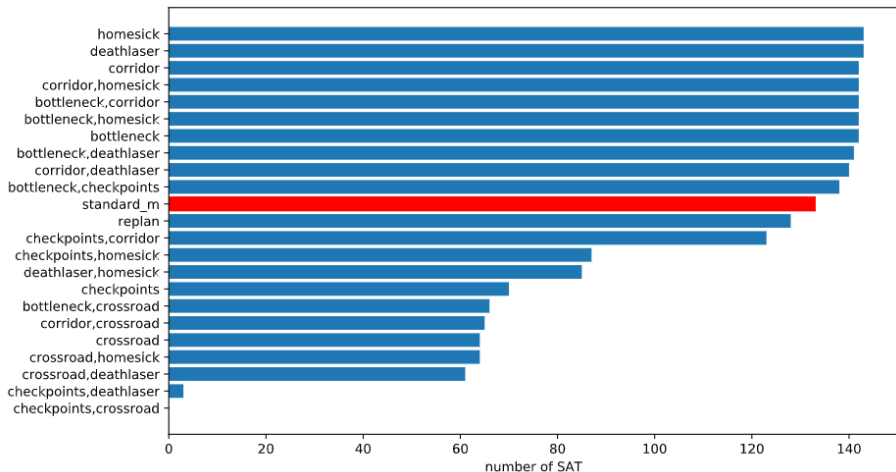
General Benchmark Results

- Total time determined by grounding time of merge step
- Combining strategies did **not** improve the performance
- Strategies performed very differently on different instance types
- Solving time of the merge is strongly correlated with number of rules and choice rules

General Benchmark Results

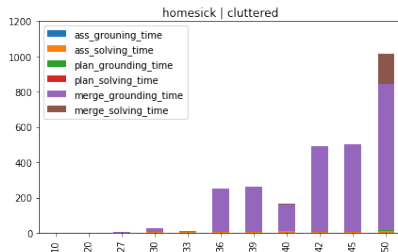
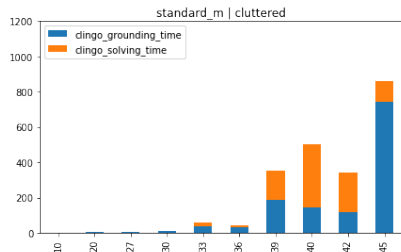
- Checkpoints strategy almost always timed out, combinations with checkpoints performed very poorly
- Combination of checkpoints and crossroad solved no instances
- Crossroad is the worst non-combined strategy
- Standard m-encoding performed the best on cluttered instances

Benchmark Results



timeout 20min

Comparison with Standard m-Encoding



- Best performance on cluttered instances
- By far the lowest grounding times of all strategies on cluttered, comparable on other types
- Generally a much higher solving time than well-performing strategies

Comparison with Hypothesis

| Corridor | Bottleneck | Checkpoints |
|-------------------------|----------------------------|------------------------|
| $+$ good performance | $+$ worse than Corridor | $-$ bad performance |

| Homesick | Deathlaser | Crossroad |
|-------------------------|--------------------------------|--------------------------|
| $+$ best performance | $+$ second best performance | $-$ worst performance |

Comparison with Hypothesis

| | Corridor | Bottleneck | Checkp. | Homesick | Deathlaser |
|------------|--|--|--|--------------|--------------|
| Bottleneck | <div>+</div> <div>good for normal and sparse</div> | | | | |
| Checkp. | <div>—</div> <div>limited by implementation of checkpoints</div> | <div>—</div> <div>worse than Bottleneck on ist own</div> | | | |
| Homesick | <div>~</div> <div>works well on normal and sparse</div> | <div>~</div> <div>works well on normal and sparse</div> | <div>~</div> <div>performed well on sparse</div> | | |
| Deathlaser | <div>+</div> <div>good on cluttered</div> | <div>+</div> <div>very good for normal and cluttered</div> | <div>—</div> | <div>—</div> | |
| Crossroad | <div>—</div> | <div>—</div> | <div>—</div> | <div>—</div> | <div>—</div> |

Brief comparrison of stats

Grouping related stats (means):

| strategies | grounding time | merge constraints | con- | merge variables |
|------------|----------------|-------------------|------|-----------------|
| homesick | 124 | 42301.9 | | 225590.7 |
| standard-m | 125 | 1353323 | | 6227959 |

Solving related stats (means):

| strategies | solving time | merge conflicts |
|------------|--------------|-----------------|
| homesick | 3.226768 | 148.2 |
| standard-m | 29 | 559.2105 |

We have much more detailed information. If one is interested we can show them afterwards!

Conclusion

- Combining strategies is not worth
- No strategy performed well on all instance types
- Using normalized scores, homesick and bottleneck alone performed the best, checkpoints and its combinations performed the worst
- The m-encoding performed surprisingly well due to small grounding times
- Our hypothesis focused on the performance of solving rather than grounding

- Optimization of grounding in merge step!
- Implementation of more strategies that ground faster
- Optimization of hyperparameters