

# Plan merging

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**Abstract.** We are talking about plan merging here

## 1 Definition

Plan merging aim to solve MAPF[1][2] problems by computing individual plan for each agent to their goal regardless of conflict, and then, by using these previous plan, merge them into a conflict-free plan. The task can be divided in three; target assignment, individual pathfinding and plan-merging.

### 1.1 Classic MAPF

We can base plan merging definition on classic MAPF's one; the paper "A General Formal Framework for Pathfinding Problems with Multiple Agents"[1] provides a standart defintion for non-anonymous MAPF. And it is defined as such; it takes as input a tuple  $\langle G, s, f \rangle$  where  $G = (V, E)$  represent a graph.  $s : [1, \dots, k] \rightarrow V$  maps an an agent to a "start" vertex. Finally,  $f : [1, \dots, k] \rightarrow V$  maps an agent to a "final" vertex. The output is a set of  $k$  single-agent plan, where a plan  $\pi$  is denoted as a sequence of action  $a_1, \dots, a_n$ , each of them being a function defined as  $a : V \rightarrow V$ . Plans must satisfy these properties:

1. considering an agent  $r$  and its plan  $\pi_r$ ,  $\pi_r[[\pi_r]] = f(a_n(\dots(a_1(s(r)))))$
2. do not contain any vertex conflict. Vertex conflict exist between  $\pi_i$  and  $\pi_j$  iff for any time step  $t$ ,  $\pi_i[t] = \pi_j[t]$ .
3. do not contain any edge conflict. Edge conflict exist between  $\pi_i$  and  $\pi_j$  iff for any time step  $t$ ,  $\pi_i[t+1] = \pi_j[t]$  and  $\pi_i[t] = \pi_j[t+1]$ .

### 1.2 Target assignment

Basing ourselves on MAPF definition, we can then define target assignment (TA)[1][3]; it takes as input a tuple  $\langle G, s, F \rangle$ ,  $G = (V, E)$  representing a graph,  $s : [1, \dots, k] \rightarrow V$  maps an agent to a "start" and  $F$  a set of  $k$  vertices denoting "final" vertices. The output would be a tuple  $\langle G, s, f \rangle$  where  $G = (V, E)$  representing a graph,  $s : [1, \dots, k] \rightarrow V$  maps an agent to a "start" vertex. Finally,  $f : [1, \dots, k] \rightarrow V$  maps an agent to a "final" vertex.

### 1.3 Individual Pathfinding

We would then define individual pathfinding (IP); the input of would be TA's output  $\langle G, s, f \rangle$ . IP would then give as output,  $\langle G, \theta \rangle$  where each agent provides at least one solution. Formally, for each agent  $r$ , we have  $\theta[r] = \{\pi_1, \dots, \pi_n\}$ . Plans contained in  $\theta$  must only satisfy property 1.

### 1.4 Plan merging

Finally, we can define plan merging (PM). It takes as input  $\langle G, \theta \rangle$  since we can deduce start and final position from plans. And gives as output MAPF's one: a solution being a set of  $k$  conflict-free plan  $\pi$ .

## References

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2. A General Formal Framework for Pathfinding Problems with Multiple Agents. Written by Esra Erdem, Doga G. Kisa, Umut Oztok and Peter Schüller
3. Structure and Intractability of Optimal Multi-Robot Path Planning on Graphs. Written by Jingjin Yu and Steven M. LaValle