

$$\top \equiv \lambda xy. x$$

$$\perp \equiv \lambda xy. y$$

$$NOT\ b \equiv (\lambda cab). b\ \perp\ \top \equiv b\ \perp\ \top \equiv b\ (\lambda xy. y)\ (\lambda xy. x) \equiv b\ (\lambda y. y)$$

Alors :

$$NOT\ \top \equiv \top\ (\lambda y. y) \equiv (\lambda xy. x)\ (\lambda y. y) \equiv (\lambda zy. y) \equiv \perp$$

Mais :

$$NOT\ \perp \equiv \perp\ (\lambda y. y) \equiv (\lambda xy. y)\ (\lambda y. y) \equiv (\lambda y. y) \not\equiv \perp$$