

$$\top \equiv \lambda xy. x$$

$$\perp \equiv \lambda xy. y$$

$$NOT\ b \equiv \lambda b. ((\lambda cab) (b\ \perp\ \top)) \equiv \lambda b. b\ \perp\ \top \equiv \lambda b. b\ (\lambda xy. y)\ (\lambda xy. x) \equiv \lambda b. b\ (\lambda y. y)$$

Alors :

$$NOT\ \top \equiv \top\ (\lambda y. y) \equiv (\lambda xy. x)\ (\lambda y. y) \equiv (\lambda zy. y) \equiv \perp$$

Mais :

$$NOT\ \perp \equiv \perp\ (\lambda y. y) \equiv (\lambda xy. y)\ (\lambda y. y) \equiv (\lambda y. y) \not\equiv \perp$$