Modelling of DBH and height of Maple and Linden

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Task is to create regression models for diameter and height of linden (lehmus) and maple (vaahtera). Laser scanning-based features are used as explanatory variables. Data: Modeling data (koepuut.xlsx): The file contains 1138 trees from the test area. DBH and species (puulaji) have been determined from every tree. In addition, height is known for about half of the trees. 10 ALS metrics have been calculated for each tree. The data contains several tree species. Trees with no measured DBH and height (mallinnettavat.xlsx): 10 ALS metrics have been calculated for each tree. DBH and height are predicted with models. The data consists of linden and maples.

Fork flow: Creating the models with modelling data - Separate linden and maples from the data (there are also other species in the modelling data).

Choose (by testing) best predictors from ALS features for each model (best features may vary between species).

Predicting variables

- Form your own functions that utilize the created models models' explanatory variables are used as parameters for the functions
- Form a loop structure that runs through all trees in mallinnettavat.txt and calls for the correct functions according to tree species save the predicted diameter (mm) and height (dm) values for example in dbh and h vectors
- Create a result matrix that contains the following columns: tree number (Puunro), tree species (puulaji), dbh in cm and height in m
- Export the matrix into csv file

```
rm(list = ls())
setwd("C:/Users/oyeda/Desktop/R_COURSE/modelling")
#Load the data
data1 <- read.table("koepuut.txt", header = T, sep = "\t")
data2 <- read.table("mallinnettavat.txt", header = T, sep = "\t")
## NOTE: linden (lehmus) and maple (vaahtera)</pre>
```

firstly, I have to use the data with some known heights to create the model

```
##
## Call:
## lm(formula = dbh_mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 +
       p30 + p50 + p70 + p90, data = linden1)
##
## Residuals:
                1Q Median
##
       Min
                                30
                                       Max
           -29.34
                     -3.79
## -292.65
                             25.34
                                    305.10
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                                    -3.216 0.001378 **
## (Intercept)
                -70.199
                            21.831
                  6.818
## Hmax
                             3,268
                                     2.086 0.037429 *
## Hmean
                 64.526
                            27.326
                                     2.361 0.018555 *
## h30
                -31.825
                            12.282
                                    -2.591 0.009817 **
## h50
                 -3.033
                            11.354
                                    -0.267 0.789448
## h70
                -23.176
                            10.823
                                    -2.141 0.032687 *
## h90
                             7.800
                                     1.660 0.097488 .
                 12.948
## p30
                 46.208
                            39.959
                                     1.156 0.248025
## p50
               -195.585
                            46.578 -4.199 3.12e-05 ***
## p70
                 18.229
                            55.552
                                     0.328 0.742926
                                     3.369 0.000807 ***
## p90
                158.242
                            46.969
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 58.55 on 552 degrees of freedom
## Multiple R-squared: 0.8024, Adjusted R-squared: 0.7988
## F-statistic: 224.2 on 10 and 552 DF, p-value: < 2.2e-16
```

from the above, we can take away h50, p30, and p70, because, they all have p values below 0.05 thus, i'm left with $dbh_mm \sim Hmax + Hmean + h30 + h70 + p50 + h90 + p90$

To further corroborate this, I use a stepwise regression next

```
# Stepwise Regression
library(MASS)
linfit dbh <- 1m(dbh mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30
                  + p50 + p70 + p90, linden1)
#?stepAIC
step <- stepAIC(linfit_dbh, direction = "both")</pre>
## Start: AIC=4593.59
## dbh mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
##
           Df Sum of Sq
                             RSS
                                     AIC
## - h50
            1
                     245 1892613 4591.7
## - p70
            1
                     369 1892738 4591.7
## - p30
            1
                    4584 1896953 4593.0
## <none>
                         1892368 4593.6
## - h90
                    9446 1901815 4594.4
```

```
## - Hmax
            1
                  14919 1907287 4596.0
## - h70
            1
                  15719 1908087 4596.3
## - Hmean 1
                  19115 1911484 4597.3
## - h30
            1
                  23018 1915387 4598.4
## - p90
            1
                  38912 1931281 4603.1
## - p50
                  60447 1952815 4609.3
            1
##
## Step: AIC=4591.67
## dbh_mm \sim Hmax + Hmean + h30 + h70 + h90 + p30 + p50 + p70 + p90
##
           Df Sum of Sq
##
                            RSS
                                   AIC
## - p70
            1
                   436 1893050 4589.8
## - p30
                   4364 1896977 4591.0
            1
## <none>
                        1892613 4591.7
## - h90
                  11043 1903656 4592.9
            1
## + h50
            1
                    245 1892368 4593.6
## - Hmax
            1
                  15483 1908096 4594.3
## - h70
            1
                  17339 1909952 4594.8
## - Hmean 1
                  21290 1913903 4596.0
## - h30
            1
                  23304 1915917 4596.6
## - p90
            1
                  38770 1931383 4601.1
                  60302 1952915 4607.3
## - p50
            1
##
## Step: AIC=4589.8
## dbh mm \sim Hmax + Hmean + h30 + h70 + h90 + p30 + p50 + p90
##
##
           Df Sum of Sq
                            RSS
                                   AIC
## - p30
                   3995 1897044 4589.0
            1
## <none>
                        1893050 4589.8
## - h90
            1
                  12371 1905421 4591.5
## + p70
                    436 1892613 4591.7
            1
## + h50
            1
                    312 1892738 4591.7
## - h70
            1
                  19327 1912377 4593.5
## - Hmax
            1
                  19588 1912638 4593.6
## - Hmean 1
                  20913 1913962 4594.0
## - h30
            1
                  22937 1915987 4594.6
## - p50
                  78604 1971654 4610.7
            1
## - p90
            1
                 122382 2015432 4623.1
##
## Step: AIC=4588.98
## dbh mm ~ Hmax + Hmean + h30 + h70 + h90 + p50 + p90
##
##
           Df Sum of Sq
                            RSS
                                   AIC
## <none>
                        1897044 4589.0
## + p30
                  3995 1893050 4589.8
            1
## - h90
         1
                  12304 1909348 4590.6
## + p70
            1
                     67 1896977 4591.0
                     36 1897008 4591.0
## + h50
            1
## - h70
            1
                  16364 1913408 4591.8
            1 17685 1914729 4592.2
## - Hmax
```

```
## - Hmean
                  19105 1916149 4592.6
            1
            1
## - h30
                  22130 1919175 4593.5
## - p90
            1
                 118980 2016024 4621.2
            1
                 119950 2016994 4621.5
## - p50
step$anova # display results
## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## dbh_mm ~ Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
## Final Model:
## dbh mm ~ Hmax + Hmean + h30 + h70 + h90 + p50 + p90
##
##
##
               Deviance Resid. Df Resid. Dev
      Step Df
                                                   AIC
## 1
                              552
                                      1892368 4593.594
## 2 - h50 1
               244.6803
                              553
                                      1892613 4591.667
                              554
## 3 - p70 1 436.4771
                                      1893050 4589.796
## 4 - p30 1 3994.8186
                              555
                                      1897044 4588.983
```

The result of the analysis confirms earlier the choice made earlier. Thus, my final model for dbh for linden would be: $dbh_m m = a + b_1 H max + b_2 H mean + b_4 h 30 + b_5 h 70 + b_6 p 50 + b_7 h 90 + b_8 p 90$

Next is for the diameter

```
linden1 <- data1[data1$puulaji == "lehmus",]</pre>
#linear model for dbh of linden
linfit_h < -lm(h_dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30)
               + p50 + p70 + p90, linden1)
summary(linfit_h)
##
## Call:
## lm(formula = h_dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 +
       p50 + p70 + p90, data = linden1)
##
## Residuals:
##
                                 3Q
       Min
                10 Median
                                        Max
## -88.831 -5.673
                              7.379 27.274
                     1.032
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                              8.298
                                      0.626
## (Intercept)
                  5.192
                                             0.53223
                                      2.994 0.00307 **
## Hmax
                  3.693
                              1.233
                -12.727
## Hmean
                             12.139 -1.048
                                             0.29559
## h30
                  9.596
                              5.316
                                      1.805 0.07242
```

```
## h50
                            4.706 -1.970 0.05012 .
                -9.270
                                    2.791 0.00572 **
## h70
                13.175
                            4.720
## h90
                 4.222
                            3.102
                                    1.361 0.17489
                 4.994
                           14.336
                                    0.348 0.72790
## p30
## p50
                -29.220
                           17.123 -1.707 0.08935 .
## p70
                22.127
                           21.603
                                    1.024
                                           0.30686
## p90
                14.675
                           18.186
                                    0.807
                                           0.42060
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.51 on 216 degrees of freedom
     (336 observations deleted due to missingness)
## Multiple R-squared: 0.8759, Adjusted R-squared: 0.8702
## F-statistic: 152.5 on 10 and 216 DF, p-value: < 2.2e-16
```

from the above, I can eliminate Hmean, h50, h90, p30, p50, p70 and p90. Model can then be: $h_d m = a + b_1 H max + b_2 h30 + b_3 h70$

*Stepwise regression for height of linden

```
#next, use stepwise regression to eliminate the redundant variables:
step_h <- stepAIC(linfit_h, direction = ("both"))</pre>
## Start: AIC=1225.26
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
           Df Sum of Sq
##
                          RSS
                                  AIC
## - p30
                  25.57 45533 1223.4
## - p90
            1
                 137.18 45645 1223.9
## - p70
            1
                 221.03 45729 1224.4
## - Hmean 1
                 231.61 45739 1224.4
## - h90
            1
                 390.34 45898 1225.2
## <none>
                        45508 1225.3
## - p50
            1
                 613.55 46121 1226.3
## - h30
            1
                 686.63 46194 1226.7
## - h50
            1
                 817.58 46325 1227.3
## - h70
            1
                1641.67 47150 1231.3
## - Hmax
            1
                1888.66 47397 1232.5
##
## Step: AIC=1223.38
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p50 + p70 + p90
##
           Df Sum of Sq
##
                          RSS
                                  AIC
## - p90
                 138.33 45672 1222.1
## - p70
            1
                 201.39 45735 1222.4
## - Hmean 1
                 265.40 45799 1222.7
## - h90
            1
                 401.54 45935 1223.4
                        45533 1223.4
## <none>
## - h30
            1
                 707.02 46240 1224.9
```

```
## + p30 1 25.57 45508 1225.3
## - h50
            1
                 794.42 46328 1225.3
## - p50
            1
                864.75 46398 1225.7
## - h70
                1730.34 47264 1229.8
            1
                1899.14 47433 1230.7
## - Hmax
            1
##
## Step: AIC=1222.07
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p50 + p70
##
           Df Sum of Sq
                         RSS
                                 AIC
## - Hmean 1
                 283.46 45955 1221.5
## - h90
                 342.99 46015 1221.8
            1
## <none>
                        45672 1222.1
## + p90
                 138.33 45533 1223.4
## - h30
            1
                 693.68 46365 1223.5
## - h50
            1
                718.62 46390 1223.6
## + p30
            1
                 26.72 45645 1223.9
## - p50
                1124.71 46796 1225.6
            1
## - Hmax
            1
                1760.83 47433 1228.7
## - p70
            1
                1821.60 47493 1229.0
## - h70
            1
                2056.69 47728 1230.1
##
## Step: AIC=1221.48
## h dm ~ Hmax + h30 + h50 + h70 + h90 + p50 + p70
##
##
           Df Sum of Sq
                         RSS
                                 AIC
## - h90
                 107.23 46062 1220.0
                        45955 1221.5
## <none>
## - h30
                 469.95 46425 1221.8
            1
## + Hmean 1
                 283.46 45672 1222.1
## + p90
            1
                 156.38 45799 1222.7
## + p30
            1
                 62.65 45893 1223.2
## - p50
            1
                 954.70 46910 1224.1
## - h50
            1
                1463.41 47419 1226.6
## - Hmax
            1
                1479.51 47435 1226.7
## - p70
            1
                1765.41 47721 1228.0
## - h70
                1855.17 47810 1228.5
            1
##
## Step: AIC=1220.01
## h_dm \sim Hmax + h30 + h50 + h70 + p50 + p70
##
##
           Df Sum of Sa
                         RSS
                                 AIC
## <none>
                        46062 1220.0
## - h30
                  438.9 46501 1220.2
            1
## + h90
                  107.2 45955 1221.5
            1
## + p90
            1
                   99.3 45963 1221.5
## + p30
            1
                   51.7 46011 1221.8
                  47.7 46015 1221.8
## + Hmean 1
## - p50
            1
                 1010.2 47073 1222.9
            1 1472.8 47535 1225.2
## - h50
```

```
## - p70
                 1942.9 48005 1227.4
## - Hmax
            1
                 2207.3 48270 1228.6
## - h70
            1
                 4046.5 50109 1237.1
step h$anova #display results
## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
## Final Model:
## h dm \sim Hmax + h30 + h50 + h70 + p50 + p70
##
##
        Step Df Deviance Resid. Df Resid. Dev
                                                     AIC
## 1
                                       45507.84 1225.257
                                 216
## 2
       - p30 1 25.56837
                                 217
                                       45533.41 1223.384
## 3
       - p90 1 138.32822
                                 218
                                       45671.74 1222.073
## 4 - Hmean 1 283.46075
                                 219
                                       45955.20 1221.477
## 5 - h90 1 107.22846
                                 220
                                       46062.43 1220.006
```

final model: $h_d m = H m a x + h 30 + h 50 + h 70 + p 50 + p 70$

multiple regression analysis and stepwise regression for Diameter At Breast Height of *Maple*

```
#subset the dataframe to vaahtera species
maple1 <- data1[data1$puulaji == "vaahtera", ]</pre>
#multiple linear regression, using all the variables
mapfit_dbh < -1m(dbh_mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30
                 + p50 + p70 + p90, maple1)
#get the summary details
summary(mapfit dbh)
##
## Call:
## lm(formula = dbh_mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 +
       p30 + p50 + p70 + p90, data = maple1)
##
##
## Residuals:
                       Median
        Min
                  10
                                     30
                                             Max
## -109.381 -22.123
                        -8.636
                                 19.235 257.898
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -75.3943
                             44.0312
                                     -1.712
                                                0.0920 .
## Hmax
                                       0.287
                  1.6715
                              5.8207
                                               0.7750
```

```
## Hmean
                -45.3215
                             62.3283 -0.727
                                               0.4700
                                       2.424
## h30
                 54.2880
                             22.3993
                                               0.0184 *
## h50
                 10.4815
                             21.7662
                                       0.482
                                               0.6319
                 11.6399
                             21.3723
                                       0.545
## h70
                                               0.5880
## h90
                 -0.6115
                            10.1094
                                     -0.060
                                               0.9520
                -94.5943
## p30
                            135.6017
                                      -0.698
                                               0.4881
## p50
                116.8221
                           116.4486
                                       1.003
                                               0.3198
## p70
               -166.7410
                            119.9211
                                      -1.390
                                               0.1695
                                               0.0119 *
## p90
                192.9563
                            74.3820
                                       2.594
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 55.9 on 60 degrees of freedom
## Multiple R-squared: 0.6733, Adjusted R-squared: 0.6188
## F-statistic: 12.36 on 10 and 60 DF, p-value: 2.707e-11
#Perform a stepwise regression to remove the redundant variables
m_step_dbh <- stepAIC(mapfit_dbh, direction = ("both"))</pre>
## Start: AIC=581.39
## dbh \ mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
##
           Df Sum of Sq
                           RSS
                                   AIC
## - h90
            1
                   11.4 187484 579.39
## - Hmax
            1
                  257.7 187730 579.49
## - h50
            1
                  724.6 188197 579.66
## - h70
            1
                  926.8 188399 579.74
## - p30
            1
                 1520.5 188993 579.96
## - Hmean 1
                 1652.1 189125 580.01
## - p50
                 3144.6 190617 580.57
## <none>
                         187473 581.39
## - p70
            1
                 6040.6 193513 581.64
## - h30
            1
                18353.8 205826 586.02
## - p90
            1
                21026.6 208499 586.94
##
## Step: AIC=579.39
## dbh_mm ~ Hmax + Hmean + h30 + h50 + h70 + p30 + p50 + p70 + p90
##
##
           Df Sum of Sa
                           RSS
                                   AIC
## - Hmax
            1
                    302 187786 577.51
## - h50
            1
                   1088 188572 577.80
## - h70
            1
                   1231 188715 577.86
## - p30
                   1738 189222 578.05
            1
## - p50
            1
                   3174 190658 578.58
                        187484 579.39
## <none>
## - p70
            1
                   6070 193555 579.66
## - Hmean
            1
                   6766 194250 579.91
## + h90
            1
                     11 187473 581.39
## - p90
            1
                  21034 208518 584.94
```

```
## - h30 1 50811 238295 594.42
##
## Step: AIC=577.51
## dbh_mm \sim Hmean + h30 + h50 + h70 + p30 + p50 + p70 + p90
##
##
           Df Sum of Sq
                           RSS
                                  AIC
## - h50
           1
                   869 188655 575.83
## - h70
            1
                   1077 188863 575.91
## - p30
                   1490 189276 576.07
            1
## - p50
            1
                   4088 191874 577.04
## <none>
                        187786 577.51
## - p70
                   5871 193657 577.69
            1
## - Hmean 1
                   7891 195677 578.43
## + Hmax
            1
                   302 187484 579.39
## + h90
            1
                     56 187730 579.49
## - p90
            1
                  21209 208996 583.10
## - h30
            1
                  50931 238717 592.55
##
## Step: AIC=575.83
## dbh_mm ~ Hmean + h30 + h70 + p30 + p50 + p70 + p90
##
##
           Df Sum of Sq
                           RSS
                                  AIC
## - p30
           1
                   1238 189893 574.30
## - p50
            1
                   4045 192700 575.34
## - h70
           1
                   5135 193790 575.74
## <none>
                        188655 575.83
## - p70
            1
                   7121 195777 576.47
## - Hmean 1
                   7383 196039 576.56
## + h50
            1
                    869 187786 577.51
## + h90
            1
                    404 188251 577.68
## + Hmax
            1
                     83 188572 577.80
## - p90
            1
                  22211 210866 581.74
## - h30
                  52506 241162 591.27
##
## Step: AIC=574.3
## dbh mm \sim Hmean + h30 + h70 + p50 + p70 + p90
##
##
           Df Sum of Sq
                           RSS
                                  AIC
## - p50
                   3089 192982 573.44
            1
## - h70
                   4171 194065 573.84
            1
## <none>
                        189893 574.30
## - Hmean 1
                   6301 196195 574.62
## - p70
            1
                   6459 196353 574.67
                   1238 188655 575.83
## + p30
            1
## + h50
            1
                    617 189276 576.07
## + h90
            1
                    564 189329 576.09
## + Hmax
            1
                    122 189771 576.25
                  24353 214247 580.87
## - p90
            1
## - h30
            1
                  51795 241689 589.42
##
```

```
## Step: AIC=573.44
## dbh mm \sim Hmean + h30 + h70 + p70 + p90
##
##
           Df Sum of Sq
                           RSS
                                  AIC
## - h70
            1
                   3379 196362 572.68
## - p70
            1
                   4344 197327 573.03
## - Hmean 1
                   5255 198237 573.35
## <none>
                        192982 573.44
## + p50
                   3089 189893 574.30
## + h50
            1
                   972 192010 575.09
                    893 192089 575.12
## + Hmax
            1
## + h90
                    675 192307 575.20
          1
## + p30
            1
                    282 192700 575.34
## - p90
           1
                  21724 214706 579.02
## - h30
                  50677 243659 588.00
##
## Step: AIC=572.68
## dbh mm \sim Hmean + h30 + p70 + p90
##
##
           Df Sum of Sq
                           RSS
                                  AIC
## - Hmean 1
                   4655 201017 572.34
## <none>
                        196362 572.68
## + h50
                   3948 192414 573.24
            1
## - p70
            1
                   7703 204064 573.41
## + h90
         1
                   3424 192938 573.43
## + h70
           1
                   3379 192982 573.44
                  2297 194065 573.84
## + p50
           1
## + p30
                   504 195858 574.49
           1
## + Hmax
            1
                    202 196160 574.60
## - p90
            1
                  25231 221593 579.26
## - h30
            1
                  87926 284287 596.95
##
## Step: AIC=572.34
## dbh mm \sim h30 + p70 + p90
##
           Df Sum of Sq
##
                                  AIC
                          RSS
## + h90
                   7600 193417 571.60
            1
## <none>
                        201017 572.34
## + Hmean 1
                   4655 196362 572.68
## + h70
            1
                   2780 198237 573.35
## + h50
            1
                  2159 198858 573.57
## + p50
            1
                   1874 199143 573.68
## + Hmax
            1
                  686 200330 574.10
## + p30
                   441 200576 574.18
            1
## - p70
            1
                  15680 216696 575.67
## - p90
            1
                  36596 237612 582.22
## - h30
            1
                 336023 537040 640.11
##
## Step: AIC=571.6
## dbh_mm \sim h30 + p70 + p90 + h90
```

```
##
##
           Df Sum of Sq
                            RSS
                                   AIC
## - p70
            1
                   4738 198155 571.32
## <none>
                         193417 571.60
## - h90
            1
                   7600 201017 572.34
## + p50
            1
                   2578 190839 572.65
## + h50
            1
                     939 192477 573.26
## + h70
            1
                     793 192624 573.31
## + Hmax
            1
                     686 192731 573.35
## + Hmean
            1
                     479 192938 573.43
## + p30
            1
                     452 192964 573.44
## - p90
                  22894 216311 577.55
            1
## - h30
            1
                  157000 350417 611.80
##
## Step: AIC=571.32
## dbh_mm \sim h30 + p90 + h90
##
##
           Df Sum of Sq
                            RSS
                                   AIC
## <none>
                         198155 571.32
## + p70
                   4738 193417 571.60
            1
## + h50
                   1778 196377 572.68
            1
## + Hmax
            1
                   1505 196650 572.78
## + p30
            1
                   1396 196759 572.82
## + h70
            1
                   1370 196785 572.83
## + p50
            1
                   1333 196822 572.84
## + Hmean
            1
                     809 197346 573.03
## - h90
            1
                  18541 216696 575.67
## - p90
                   28738 226893 578.94
            1
## - h30
            1
                 228507 426662 623.78
m_step_dbh$anova #display results
## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## dbh_mm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
## Final Model:
## dbh_mm ~ h30 + p90 + h90
##
##
##
                   Deviance Resid. Df Resid. Dev
         Step Df
                                                        AIC
## 1
                                     60
                                          187472.6 581.3883
## 2
        - h90
                   11.43085
               1
                                    61
                                          187484.1 579.3926
## 3
       - Hmax
                                    62
                                          187786.3 577.5070
               1
                  302.20328
## 4
        - h50
               1
                  869.04424
                                    63
                                          188655.3 575.8348
## 5
        - p30
               1 1238.14149
                                    64
                                          189893.4 574.2992
## 6
     - p50 1 3088.65800
                                    65
                                          192982.1 573.4448
```

```
## 7 - h70
              1 3379.43011
                                  66
                                       196361.5 572.6773
## 8
     - Hmean
              1 4655.13389
                                  67
                                       201016.7 572.3409
## 9
       + h90
              1 7599.78245
                                  66
                                       193416.9 571.6046
## 10 - p70 1 4738.08029
                                  67
                                       198155.0 571.3229
```

Final Model based on the chosen variables by stepwise regression: $dbh_m m = h30 + p90 + h90$

linear model and Stepwise regression for height of maple trees

```
#Linear model using all the variables
mapfit_h < -1m(h_dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30)
               + p50 + p70 + p90, maple1)
summary(mapfit h)
##
## Call:
## lm(formula = h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 +
       p50 + p70 + p90, data = maple1)
##
##
## Residuals:
##
       Min
                10 Median
                                3Q
                                        Max
## -30.644 -8.948
                     1.248
                             8.017
                                    24.733
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 32.953
                            18.310
                                     1.800
                                              0.0845 .
                                     0.543
                                              0.5922
## Hmax
                  1.531
                             2.820
## Hmean
                -34.497
                            34.361 -1.004
                                              0.3254
## h30
                 26.208
                            11.809
                                     2.219
                                              0.0362 *
## h50
                             8.264 -1.192
                 -9.848
                                              0.2450
## h70
                 21.393
                            15.222
                                    1.405
                                              0.1727
## h90
                  5.025
                                     0.964
                                              0.3446
                             5.211
                            67.419
                                     0.146
## p30
                  9.811
                                              0.8855
## p50
                -60.450
                            52.854 -1.144
                                              0.2640
## p70
                 33.589
                            51.193 0.656
                                              0.5180
## p90
                -10.524
                            28.321 -0.372
                                              0.7134
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 16.23 on 24 degrees of freedom
     (36 observations deleted due to missingness)
## Multiple R-squared: 0.841, Adjusted R-squared:
## F-statistic: 12.69 on 10 and 24 DF, p-value: 2.527e-07
#Stepwise regression
m_step_h <- stepAIC(mapfit_h, direction = ("both"))</pre>
## Start: AIC=203.86
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
```

```
##
       p90
##
##
           Df Sum of Sq
                           RSS
                                   AIC
## - p30
            1
                  5.58 6324.2 201.89
## - p90
            1
                  36.36 6355.0 202.06
## - Hmax
            1
                  77.62 6396.3 202.28
## - p70
                 113.34 6432.0 202.48
            1
## - h90
            1
                 244.74 6563.4 203.19
## - Hmean
            1
                 265.36 6584.0 203.30
## - p50
                 344.39 6663.0 203.71
            1
## <none>
                        6318.6 203.86
## - h50
                 373.93 6692.6 203.87
            1
## - h70
            1
                 519.96 6838.6 204.62
## - h30
            1
                1296.64 7615.3 208.39
##
## Step: AIC=201.89
## h_dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p50 + p70 + p90
##
##
           Df Sum of Sq
                           RSS
                                   AIC
## - p90
            1
                  31.67 6355.9 200.06
## - p70
                 110.95 6435.2 200.50
            1
## - Hmax
            1
                 229.71 6553.9 201.14
## - h90
            1
                 285.49 6609.7 201.43
## <none>
                        6324.2 201.89
## - h50
                 376.00 6700.2 201.91
## - p50
            1
                 399.23 6723.4 202.03
## - Hmean 1
                 502.47 6826.7 202.56
## - h70
                 753.28 7077.5 203.83
            1
## + p30
            1
                   5.58 6318.6 203.86
## - h30
            1
                1867.73 8191.9 208.94
##
## Step:
         AIC=200.06
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p50 + p70
##
##
           Df Sum of Sq
                           RSS
                                   AIC
## - p70
                  82.99 6438.9 198.52
            1
## - h90
                 276.67 6632.6 199.55
            1
## - Hmax
                 290.35 6646.2 199.63
            1
## - h50
            1
                 359.96 6715.9 199.99
                        6355.9 200.06
## <none>
## - p50
            1
                 378.31 6734.2 200.09
## - Hmean 1
                 481.24 6837.1 200.62
## - h70
            1
                 724.02 7079.9 201.84
## + p90
                 31.67 6324.2 201.89
            1
## + p30
            1
                   0.89 6355.0 202.06
## - h30
            1
                1855.55 8211.4 207.03
##
## Step: AIC=198.52
## h_dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p50
```

```
##
           Df Sum of Sq RSS AIC
## - Hmax
           1
                 222.97 6661.8 197.71
## - h90
            1
                 306.24 6745.1 198.14
## <none>
                        6438.9 198.52
## - h50
                430.79 6869.7 198.78
## - p50
            1
                437.12 6876.0 198.82
## - Hmean 1
                529.50 6968.4 199.28
## + p70
           1
                82.99 6355.9 200.06
## + p90
           1
                  3.71 6435.2 200.50
## + p30
           1
                  3.40 6435.5 200.50
## - h70
           1
                858.06 7296.9 200.90
## - h30
               1982.91 8421.8 205.91
            1
##
## Step: AIC=197.71
## h_dm \sim Hmean + h30 + h50 + h70 + h90 + p50
##
##
           Df Sum of Sq
                          RSS
                                 AIC
## - p50
                245.08 6906.9 196.97
## - h90
                 309.97 6971.8 197.30
           1
## <none>
                        6661.8 197.71
## - Hmean 1
                422.11 7084.0 197.86
## - h50
           1
                505.19 7167.0 198.27
## + Hmax
                222.97 6438.9 198.52
           1
               94.55 6567.3 199.21
## + p30
           1
## + p90
           1
                15.88 6646.0 199.62
## + p70
           1
                15.61 6646.2 199.63
## - h70
           1
                806.35 7468.2 199.71
## - h30
           1
               1918.83 8580.7 204.57
##
## Step: AIC=196.97
## h dm ~ Hmean + h30 + h50 + h70 + h90
##
           Df Sum of Sq
                          RSS
                                 AIC
## - h90
                 246.97 7153.9 196.20
## <none>
                        6906.9 196.97
## - h50
                407.89 7314.8 196.98
           1
## - Hmean 1
                531.06 7438.0 197.56
## + p50
           1
                245.08 6661.8 197.71
                164.41 6742.5 198.13
## + p90
           1
## + p70
                153.96 6753.0 198.18
           1
## + p30
           1
                78.54 6828.4 198.57
## + Hmax
           1
                30.93 6876.0 198.82
## - h70
           1
                922.91 7829.8 199.36
## - h30
            1
               2293.52 9200.5 205.01
##
## Step: AIC=196.2
## h_dm \sim Hmean + h30 + h50 + h70
##
##
          Df Sum of Sq RSS
                                 AIC
## - Hmean 1 299.56 7453.5 195.64
```

```
## <none>
                        7153.9 196.20
## + h90
            1
                 246.97 6906.9 196.97
## + p50
            1
                 182.09 6971.8 197.30
## + p90
                 107.42 7046.5 197.67
            1
## + p70
            1
                  97.81 7056.1 197.72
## - h70
            1
                 758.68 7912.6 197.73
## + p30
            1
                  31.81 7122.1 198.05
## + Hmax
            1
                  13.93 7140.0 198.13
## - h50
            1
                1287.55 8441.4 200.00
                2727.59 9881.5 205.51
## - h30
            1
##
## Step: AIC=195.64
## h dm ~ h30 + h50 + h70
##
##
           Df Sum of Sq
                            RSS
                                    AIC
## <none>
                         7453.5 195.64
## + p50
            1
                  359.1
                        7094.4 195.91
## + Hmean 1
                  299.6
                        7153.9 196.20
## + p70
            1
                  205.1 7248.4 196.66
## + p90
            1
                  128.5 7325.0 197.03
## + Hmax
                  125.3 7328.1 197.04
            1
## + p30
            1
                   72.0 7381.5 197.30
## - h70
                  863.1 8316.6 197.47
            1
## + h90
            1
                   15.5 7438.0 197.56
## - h50
            1
                  995.2 8448.7 198.03
## - h30
            1
                12258.4 19711.8 227.68
m_step_h$anova #display results
## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## h dm \sim Hmax + Hmean + h30 + h50 + h70 + h90 + p30 + p50 + p70 +
##
       p90
##
## Final Model:
## h dm ~ h30 + h50 + h70
##
##
##
        Step Df
                  Deviance Resid. Df Resid. Dev
## 1
                                   24
                                        6318.642 203.8569
## 2
       - p30 1
                  5.575097
                                   25
                                        6324.217 201.8878
## 3
       - p90 1
                 31.669329
                                   26
                                        6355.887 200.0626
## 4
       - p70 1 82.989887
                                   27
                                        6438.877 198.5166
## 5
      - Hmax 1 222.971013
                                   28
                                        6661.848 197.7081
             1 245.078713
## 6
       - p50
                                   29
                                        6906.926 196.9726
## 7
       - h90 1 246.972425
                                   30
                                        7153.899 196.2023
## 8 - Hmean 1 299.563677
                                   31 7453.462 195.6380
```

Final Model chosen after using the pvalues and stepwise regression: $h_dm \sim h30 + h50 + h70$

The final models created are:

```
FOR LINDEN dbh_m m = Hmax + Hmean + h30 + h70 + p50 + h90 + p90 h_d m = Hmax + h30 + h50 + h70 + p50 + p70
```

```
FOR MAPLE dbh_m m = h30 + p90 + h90 h_d m h30 + h50 + h70
```

Final creation of models based on the chosen predictors

LINDEN

```
#for diameter at breast height(DBH)
lindbh model <- lm(dbh mm \sim Hmax + Hmean + h30 + h70)
                    + p50 + h90 + p90, linden1)
lindbh_coef <- coef(lindbh_model) #extract the coefficients</pre>
#model for height for linden species
linh model <-
  lm(h dm \sim Hmax + h30 + h50 + h70 + p50 + p70, linden1)
linh coef <- coef(linh model) #extract the coefficients</pre>
#MAPLES
#model for diameter at breast height(DBH) of maple
mapdbh_model \leftarrow lm(dbh_mm \sim Hmax + Hmean + h30 + h70 + p50)
                    + h90 + p90, maple1)
mapdbh coef <- coef(mapdbh model) #extract the coefficients</pre>
#model for height of maple
maph model <-1m(h dm \sim h30 + h50 + h70, maple1)
maph_coef <- coef(maph_model) #extract the coefficients</pre>
```

Creating functions to calculate the parameters

```
#function for calculating the Height of linden, by using the model
lin H fun <- function(Hmax, h30 , h50, h70, p50, p70) {
  linh mod <- round((</pre>
    linh_coef[1] + (linh_coef[2] * Hmax) +
      (linh coef[3] * h30) + linh coef[4] * h50 + linh coef[5] *
      h70 + linh_coef[6] * p50
    + (linh_coef[7] * p70)
  ),
  2)
  return(linh_mod)
}
#create function for calculating the DBH of maple, by using the model
map_DBH_fun <-
  function(Hmax , Hmean , h30 , h70 , p50 , h90 , p90) {
    mapdbh mod <-
      round((
        mapdbh_coef[1] + (mapdbh_coef[2] * Hmax) + (mapdbh_coef[3] * Hmean) +
          (mapdbh\_coef[4] * h30) + mapdbh\_coef[5] * h70 + mapdbh\_coef[6] *
p50
        + (mapdbh_coef[7] * h90) + (mapdbh_coef[8] * p90)
      ),
      2)
    return(mapdbh_mod)
  }
#create function for calculating the Height of Maple, by using the model
map_H_fun <- function(h30 , h50, h70) {</pre>
  maph mod <- round((</pre>
    maph coef[1] + (maph coef[2] * h30)
    + maph coef[3] * h50 + maph coef[4] * h70
  ), 2)
  return(maph_mod)
```

Loop to calculate the predictions into a dataframe

```
data2$h30[i] ,
          data2$h70[i] ,
          data2$p50[i]
          data2$h90[i],
          data2$p90[i]
      )
      h ln <-
        append(
          h ln,
          lin_H_fun(
            data2$Hmax[i] ,
            data2$h30[i],
            data2$h50[i],
            data2$h70[i]
            data2$p50[i],
            data2$p70[i]
          )
        )
      puunro <- append(puunro, data2$Puunro[i])</pre>
      puulaji <- append(puulaji, as.character(data2$puulaji[i]))</pre>
    }
#here, I can also use else alone instead of if (data2$puulaji[i] ==
"vaahtera")
    if (data2$puulaji[i] == "vaahtera") {
      dbh map <-
        append(dbh_map, (
          map_DBH_fun(
            data2$Hmax[i] ,
            data2$Hmean[i],
            data2$h30[i]
            data2$h70[i],
            data2$p50[i],
            data2$h90[i],
            data2$p90[i]
        ))
      h map <-
        append(h_map, (map_H_fun(data2$h30[i], data2$h50[i],
data2$h70[i])))
      puunro <- append(puunro, data2$Puunro[i])</pre>
      puulaji <- append(puulaji, as.character(data2$puulaji[i]))</pre>
```

```
}
  #combine the dbh and height vectors created for linden column-wise
  a <- cbind(dbh ln, h ln)
  #combine the dbh and height vectors created for maple column-wise
  b <- cbind(dbh_map, h_map)</pre>
  #now, combine both data but row wise since we want them to be merged
  c <- rbind(a, b)
#finally, add the plot number and names of the species which are
  #vectors created earlier for the entire data
  maple linden <- cbind.data.frame(puunro, puulaji, c)</pre>
  #reset the index/rownames to default index
  rownames(maple linden) <- NULL</pre>
  #rownames(maple linden)<-rownames(maple linden, do.NULL=T, prefix = "Obs.")</pre>
 #rename columns one and two
 colnames(maple_linden)[colnames(maple_linden)=="dbh_ln"] <- "DBH"</pre>
 colnames(maple_linden)[colnames(maple_linden)=="h_ln"] <- "height"</pre>
 #names(maple_linden)[1]<-"DBH" #wont use this cos column number might</pre>
change
  #names(maple linden) = c("DBH", "height")
#write the data into csv format
write.csv(maple linden, file =
"C:/Users/oyeda/Desktop/R_COURSE/modelling/Trees_DBH_H"
          , row.names = TRUE)
```

NOTE: THERE ARE SIMPLER APPROACHES TO CALCULATING THE HEIGHT AND DBH INTO NEW COLUMNS E.G DATA\$DBH<- FORUMA(USING NECESSARY COLUMNS). BUT I CHOSE TO TRY OUT LOOPING, BINDING AND APPENDING.