

Q₂: Basic operation = comparing 2 elements.

Ozan Arslan
Özgen
1901052259

$$\sum_{i=1}^n 2 = \underbrace{2 + 2 + \dots + 2}_{n-1 \text{ times}} = 2(n-1) = 2n - 2 \approx O(n)$$

In homework 3 the complexity equals $O(n^2)$ because in that algorithm we have 2 for loop (one is inside of other one).

On the other hand that algorithm calculates same values more than one time but dynamic programming does not allow that.

Brute force algorithm calculates all possibilities but dynamic programming algorithm calculating like:

3	-5	2	11	-8	9	-5
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For example in here algorithm compares current and maximum value and $13 - 8$, $13 > 5 \Rightarrow$ current value equals 5 but maximum does not change.

after that algorithm went 9 and current goes $9 + 5 = 14$ and compares 13 and 14 $14 > 13$ so maximum equals 14.

Q₂: Basic operation = + (Sum)

$$\sum_{i=1}^n \sum_{j=0}^i 2 = \sum_{i=1}^n \underbrace{2+2+\dots+2}_{i \text{ times}} \Rightarrow \sum_{i=1}^n 2i = 2 \sum_{i=1}^n i$$

$$= \sum_{i=1}^n i = 1+2+\dots+n = \frac{n \cdot (n+1)}{2} = \frac{n^2+n}{2} \approx \underline{\underline{O(n^2)}}$$

Because of dynamic programming instead of calculating all values algorithm calculates maximum profit of every enter one time.

maxVal array holds the maximum price of every length. And on calculating new maximum value adds an individual value and any maximum value for test new maximum value. In inner for if statement looks for $\text{maxValue}[i+j-1] + \text{arr}[j]$. $i+j-1+j = i-1$ so it means that adding maximum values to every individual costs for finding the best. (because of $i+j-1+j = i-1$, every new values length equals the wanted length.)

Q₃: For basic operation = + (Sum). sort = $O(n \log n)$

$$\sum_{i=0}^n 2 = \underbrace{2+2+\dots+2}_{n \text{ times}} = 2n \approx O(n)$$

But Interval sort and sorting algorithm of python equals $O(n \log n)$ so Time complexity of algorithm $\approx O(n \log n)$

In greedy algorithm I calculate the value of every kg of cheeses. Because greedy algorithm says put most valuable thing at first than second, third...

I put most valuable things and check the lefted space for cutting and filling of bag.

Q4: Basic operation = lessons, append

$$\sum_{i=0}^n 1 = \underbrace{1+1+\dots+1}_{n \text{ times}} \Rightarrow n \approx \underline{O(n)}$$

But les. sort takes $O(n \log n)$ times.

In that algorithm I searched first finished lesson and any lesson that starts after that and finishes first. array was sorted for that with their finishing time.