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Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

svn co <https://github.com/gadepall/school/trunk/control/codes>

1 STABILITY

2 ROUTH HURWITZ CRITERION

3 COMPENSATORS

4 NYQUIST PLOT

4.1 Polar plot

4.1. Sketch direct and inverse polar plots for a unity feedback system with open loop transfer function

$$G(s) = \frac{1}{s(1+s)^2} \quad (4.1.1)$$

Solution: For Unity feedback system, given the open loop transfer function

$$G(s) = \frac{1}{s(1+s)^2} \quad (4.1.2)$$

Now, Polar plot is defined as: The plot of points (represented as $r.e^{j\phi}$) obtained by varying ω from 0 to ∞ where

$$r = |H(j\omega)||G(j\omega)| \quad (4.1.3)$$

$$\phi = \angle H(j\omega)G(j\omega) \quad (4.1.4)$$

Inverse Polar plot is similar, in this we have;

$$r = \frac{1}{|H(j\omega)||G(j\omega)|} \quad (4.1.5)$$

$$\phi = -\angle H(j\omega)G(j\omega) \quad (4.1.6)$$

The system we're analysing is unity feedback which means $H(j\omega) = 1$ Therefore ;

$$|H(j\omega)||G(j\omega)| = |1| \cdot \frac{1}{|j\omega|(1+j\omega)^2|} \quad (4.1.7)$$

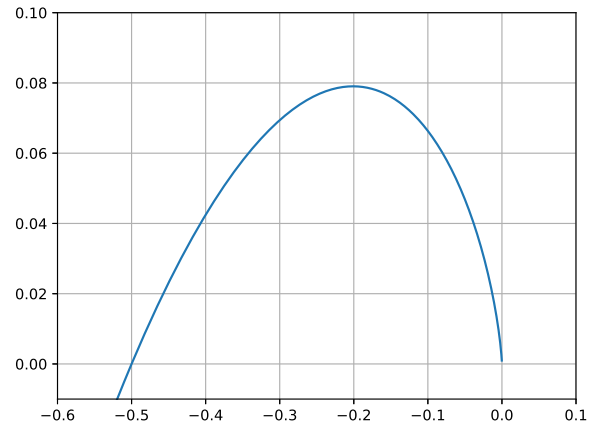


Fig. 4.1

$$|H(j\omega)||G(j\omega)| = \frac{1}{\omega(1+\omega^2)} \quad (4.1.8)$$

and to calculate Phase of $G(j\omega)$

$$H(j\omega)G(j\omega) = 1.e^0 \cdot 1.e^0 \cdot \frac{1}{\omega.e^{j\pi/2}} \cdot \left\{ \frac{1}{\sqrt{1^2 + \omega^2}.e^{j\tan^{-1}(\omega)}} \right\}^2 \quad (4.1.9)$$

$$H(j\omega)G(j\omega) = 1.e^0 \cdot 1.e^0 \omega^{-1} \cdot e^{-j\pi/2} \cdot (1^2 + \omega^2)^{-1} \cdot e^{-2j\tan^{-1}(\omega)} \quad (4.1.10)$$

Therefore

$$\angle H(j\omega)G(j\omega) = \frac{-\pi}{2} - 2\tan^{-1}(\omega) \quad (4.1.11)$$

The following code plots the polar and inverse polar plots

codes/ee18btech11002/polarplot.py

4.2. Find the frequency at which $|G(j\omega)| = 1$ and corresponding phase angle $\angle G(j\omega)$

Solution: For $|G(j\omega)| = 1$

$$\frac{1}{\omega(1+\omega^2)} = 1 \quad (4.2.1)$$

$$\omega + \omega^3 - 1 = 0 \quad (4.2.2)$$

and for the corresponding phase

$$\angle G(j\omega) = \frac{-\pi}{2} - 2\tan^{-1}(\omega) \quad (4.2.3)$$

The following code calculates the value of ω and $\angle G(j\omega)$

codes/ee18btech11002/solution.py

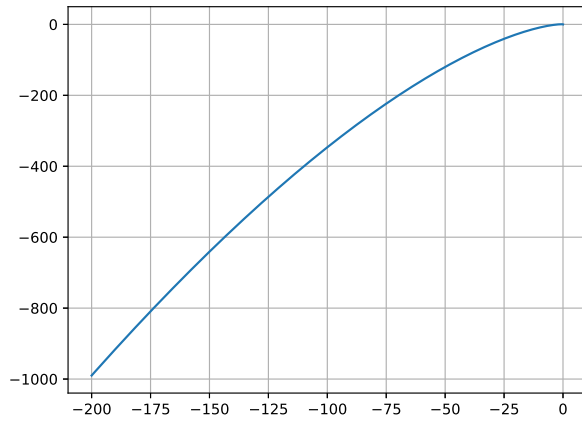


Fig. 4.2

and we get

$$\omega = 0.682 \quad (4.2.4)$$

$$\angle G(j\omega) = -\frac{52}{59}\pi \quad (4.2.5)$$