

Problem Definitions and Evaluation Criteria for the CEC 2020 Special Session and Competition on Single Objective Bound Constrained Numerical Optimization

C. T. Yue¹, K. V. Price², P. N. Suganthan³, J. J. Liang¹ M. Z. Ali⁴ and B. Y. Qu⁵

¹School of Electrical Engineering, Zhengzhou University, Zhengzhou, China

²836 Owl Circle, Vacaville, CA, U.S.A.

³School of EEE, Nanyang Technological University, Singapore

⁴School of Computer Information Systems, Jordan University of Science and Technology, Jordan

⁵School of Electric and Information Engineering, Zhongyuan University of Technology, Zhengzhou, China

zzuyueaitong@163.com, kvprice@pacbell.net, epnsugan@ntu.edu.sg, liangjing@zzu.edu.cn,
mzali.bn@ntu.edu.sg, qby1984@hotmail.com

Technical Report 201911, Computational Intelligence Laboratory,

Zhengzhou University, Zhengzhou China

And

Technical Report, Nanyang Technological University, Singapore

November 2019

Single objective optimization algorithms are the foundation upon which more complex methods, like multi-objective, niching and constrained optimization algorithms, are built. Consequently, improvements to single objective optimization algorithms are important because they can impact other domains as well. These algorithmic improvements depend in part on feedback from trials conducted with single objective benchmark functions, which themselves are the elemental building blocks for more complex tasks, like dynamic, niching, composition and computationally expensive problems. As algorithms improve, ever more challenging functions must be developed. This interplay between methods and problems drives progress, so we have developed the CEC'20 Special Session on Real-Parameter Optimization to promote this symbiosis.

Improved methods and problems sometimes require updating traditional testing criteria. In recent years, many novel optimization algorithms have been proposed to solve the bound-constrained, single objective problems offered in the CEC'05^[1], CEC'13^[2], CEC'14^[3] and CEC'17^[4] Special Sessions on Real-Parameter Optimization. In those competitions, the maximum allowed number of function evaluations—unlike problem complexity—did not scale exponentially with dimension. To address this disparity, this competition significantly increases the maximum number of allowed function evaluations for 10 scalable benchmark problems beyond their prior contest limits, with the goal of determining the extent to which this extra time translates into improved solution accuracy.

Participants are required to send their final results to the organizers in the format specified in this technical report. Based on these results, organizers will present a comparative analysis that includes statistical tests on convergence performance to compare algorithms with similar final solutions. Participants may not explicitly use the equations of the test functions, e.g. to compute gradients. This competition also excludes surrogate and meta-models. Papers on novel concepts that help us to understand problem characteristics are also welcome. The C and Matlab codes for CEC'20 test suite can be downloaded from the website below:

<https://github.com/P-N-Suganthan>

1. Introduction to the CEC'20 Benchmark Suite

1.1. Some Definitions:

All test functions are minimization problems defined as follows:

$$\text{Min } f(\mathbf{x}), \mathbf{x} = [x_1, x_2, \dots, x_D]^T$$

D : number of dimensions.

$\mathbf{o}_{il} = [o_{i1}, o_{i2}, \dots, o_{iD}]^T$: the shifted global optimum (defined in “shift_data_x.txt”), which is randomly distributed in $[-80, 80]^D$. All test functions are shifted to \mathbf{o} and are scalable.

Search range: $[-100, 100]^D$. For convenience, the same search ranges are defined for all test functions.

M: rotation matrix. Different rotation matrix are assigned to each function and each basic function.

Considering that linkages seldom exists among all variables in real-world problems, CEC'20 randomly divides variables into subcomponents. The rotation matrix for each set of subcomponents is generated from standard normally distributed entries by Gram-Schmidt ortho-normalization with condition number c that is equal to 1 or 2.

1.2. Summary of the CEC'20 Test Suite

	No.	Functions	$F_i^* = F_i(\mathbf{x}^*)$
Unimodal Function	1	Shifted and Rotated Bent Cigar Function (CEC 2017 ^[4] F1)	100
Basic Functions	2	Shifted and Rotated Schwefel's Function (CEC 2014 ^[3] F11)	1100
	3	Shifted and Rotated Lunacek bi-Rastrigin Function (CEC 2017 ^[4] F7)	700
	4	Expanded Rosenbrock's plus Griewangk's Function (CEC2017 ^[4] f ₁₉)	1900
Hybrid Functions	5	Hybrid Function 1 ($N = 3$) (CEC 2014 ^[3] F17)	1700
	6	Hybrid Function 2 ($N = 4$) (CEC 2017 ^[4] F16)	1600
	7	Hybrid Function 3 ($N = 5$) (CEC 2014 ^[3] F21)	2100
Composition Functions	8	Composition Function 1 ($N = 3$) (CEC 2017 ^[4] F22)	2200
	9	Composition Function 2 ($N = 4$) (CEC 2017 ^[4] F24)	2400
	10	Composition Function 3 ($N = 5$) (CEC 2017 ^[4] F25)	2500
Search range: $[-100,100]^D$			

*Please Note: These problems should be treated as black-box problems. The explicit equations of the problems are not to be used.

1.3. Definitions of the Basic Functions

1) Bent Cigar Function

$$f_1(\mathbf{x}) = x_1^2 + 10^6 \sum_{i=2}^D x_i^2 \quad (1)$$

2) Rastrigin's Function

$$f_2(x) = \sum_{i=1}^D \left(x_i^2 - 10 \cos(2\pi x_i) + 10 \right) \quad (2)$$

3) High Conditioned Elliptic Function

$$f_3(x) = \sum_{i=1}^D \left(10^6 \right)^{\frac{i-1}{D-1}} x_i^2 \quad (3)$$

4) HGBat Function

$$f_4(\mathbf{x}) = \left| \left(\sum_{i=1}^D x_i^2 \right)^2 - \left(\sum_{i=1}^D x_i \right)^2 \right|^{1/2} + \left(0.5 \sum_{i=1}^D x_i^2 + \sum_{i=1}^D x_i \right) / D + 0.5 \quad (4)$$

5) Rosenbrock's Function

$$f_5(\mathbf{x}) = \sum_{i=1}^{D-1} \left(100 \left(x_i^2 - x_{i+1} \right)^2 + \left(x_i - 1 \right)^2 \right) \quad (5)$$

6) Griewank's Function

$$f_6(\mathbf{x}) = \sum_{i=1}^D \frac{x_i^2}{4000} - \prod_{i=1}^D \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1 \quad (6)$$

7) Ackley's Function

$$f_7(\mathbf{x}) = -20 \exp(-0.2 \sqrt{\frac{1}{D} \sum_{i=1}^D x_i^2}) - \exp\left(\frac{1}{D} \sum_{i=1}^D \cos(2\pi x_i)\right) + 20 + e \quad (7)$$

8) HappyCat Function

$$f_8(\mathbf{x}) = \left| \sum_{i=1}^D x_i^2 - D \right|^{1/4} + \left(0.5 \sum_{i=1}^D x_i^2 + \sum_{i=1}^D x_i \right) / D + 0.5 \quad (8)$$

9) Discus Function

$$f_9(\mathbf{x}) = 10^6 x_1^2 + \sum_{i=2}^D x_i^2 \quad (9)$$

10) Lunacek bi-Rastrigin Function

$$f_{10}(\mathbf{x}) = \min \left(\sum_{i=1}^D (\hat{x}_i - \mu_0)^2, dD + s \sum_{i=1}^D (\hat{x}_i - \mu_1)^2 \right) + 10 \left(D - \sum_{i=1}^D \cos(2\pi \hat{z}_i) \right) \quad (10)$$

$$\begin{aligned} \mu_0 &= 2.5, \mu_1 = -\sqrt{\frac{\mu_0^2 - d}{s}}, s = 1 - \frac{1}{2\sqrt{D+20}} - 8.2, d = 1 \\ y &= \frac{10(x-o)}{100}, \frac{x_i}{x_i} = 2 \operatorname{sign}(x_i^*) y_i + \mu_0, \text{ for } i = 1, 2, \dots, D \\ z &= \Lambda^{100}(\hat{x} - \mu_0) \end{aligned}$$

11) Modified Schwefel's Function

$$f_{11}(x) = 418.9829 \times D - \sum_{i=1}^D g(z_i) \quad (11),$$

$$z_i = x_i + 4.209687462275036e + 002$$

$$g(z_i) = \begin{cases} z_i \sin(|z_i|^{1/2}) & \text{if } |z_i| \leq 500 \\ (500 - \operatorname{mod}(z_i, 500)) \sin(\sqrt{|500 - \operatorname{mod}(z_i, 500)|}) - \frac{(z_i - 500)^2}{10000D} & \text{if } z_i > 500 \\ (\operatorname{mod}(|z_i|, 500) - 500) \sin(\sqrt{|\operatorname{mod}(|z_i|, 500) - 500|}) - \frac{(z_i + 500)^2}{10000D} & \text{if } z_i < -500 \end{cases}$$

12) Expanded Schaffer's Function

$$\text{Schaffer's Function: } g(x, y) = 0.5 + \frac{\left(\sin^2(\sqrt{x^2 + y^2}) - 0.5 \right)}{\left(1 + 0.001(x^2 + y^2) \right)^2}$$

$$f_{12}(\mathbf{x}) = g(x_1, x_2) + g(x_2, x_3) + \dots + g(x_{D-1}, x_D) + g(x_D, x_1) \quad (12)$$

13) Expanded Rosenbrock's plus Griewangk's Function

$$f_{13}(\mathbf{x}) = f_6(f_5(x_1, x_2)) + f_6(f_5(x_2, x_3)) + \dots + f_6(f_5(x_{D-1}, x_D)) + f_6(f_5(x_D, x_1)) \quad (13)$$

14) Weierstrass Function

$$f_{14}(\mathbf{x}) = \sum_{i=1}^D \left(\sum_{k=0}^{k_{\max}} [a^k \cos(2\pi b^k (x_i + 0.5))] \right) - D \sum_{k=0}^{k_{\max}} [a^k \cos(2\pi b^k \cdot 0.5)] \quad (14)$$

$$a = 0.5, b = 3, k_{\max} = 20$$

1.4. Definitions of the CEC'20 Test Suite

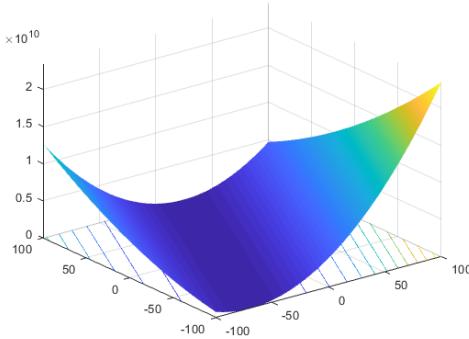
A. Basic Functions

1) Bent Cigar Function

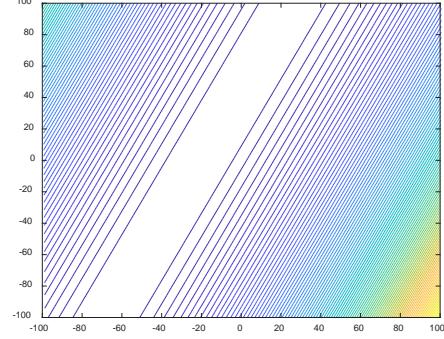
$$F_1(\mathbf{x}) = f_1(\mathbf{M}(\mathbf{x} - o_1)) + F_1^* \quad (15)$$

Properties:

- Unimodal
- Non-separable
- Smooth but narrow ridge



(a) 3-D map for 2-D function

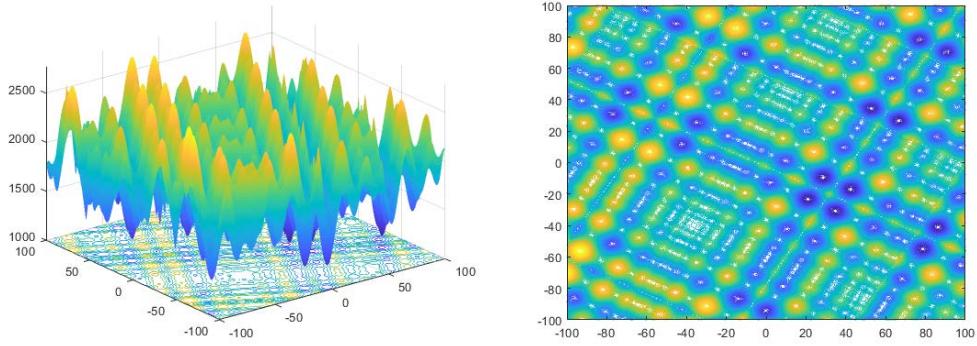


(b) Contour map for 2-D function

Figure 1 Bent Cigar Function

2) Shifted and Rotated Schwefel's Function (the same as F11 in CEC2014^[3])

$$F_2(\mathbf{x}) = f_{11}\left(\mathbf{M}\left(\frac{1000(\mathbf{x} - \mathbf{o}_2)}{100}\right)\right) + F_2^* \quad (16)$$



(a) 3-D map for 2-D function

(b) Contour map for 2-D function

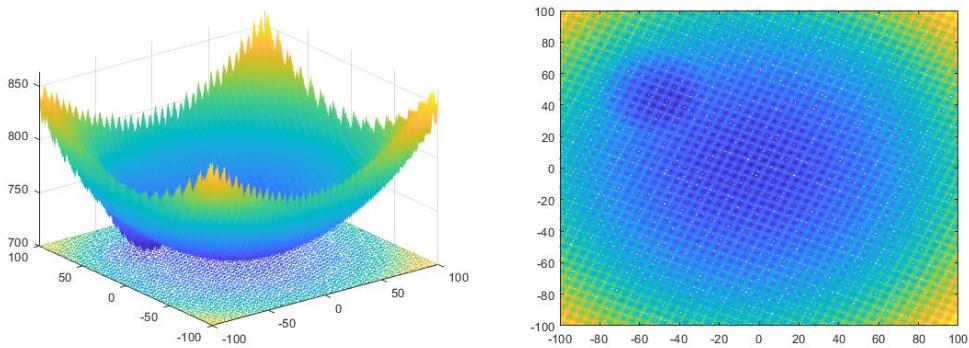
Figure 2 Shifted and Rotated Schwefel's Function

Properties:

- Multi-modal
- Non-separable
- Local optima's number is huge and the penultimate local optimum is far from the global optimum.

3) Shifted and Rotated Lunacek bi-Rastrigin Function (the same as F7 in CEC2017^[4])

$$F_3(x) = f_{10} \left(\mathbf{M} \left(\frac{600(x - o_3)}{100} \right) \right) + F_3^* \quad (17)$$



(a) 3-D map for 2-D function

(b) Contour map for 2-D function

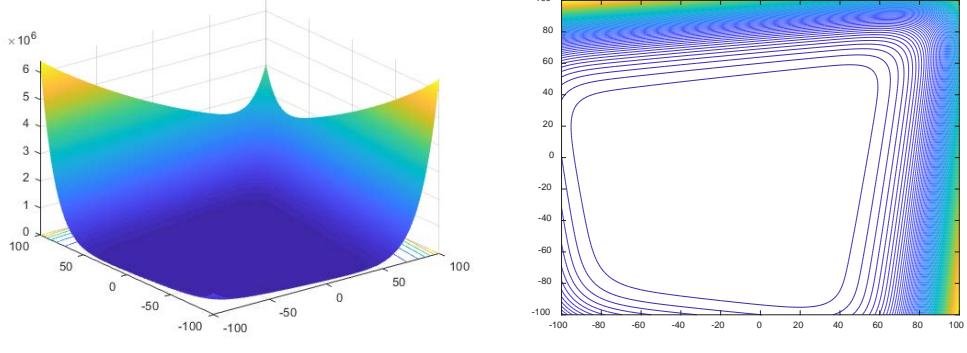
Figure 3 Shifted and Rotated Lunacek bi-Rastrigin Function

Properties:

- Multi-modal
- Non-separable
- Asymmetrical
- Continuous everywhere yet differentiable nowhere

4) Expanded Rosenbrock's plus Griewangk's Function (the same as f_{19} in CEC2017^[4])

$$F_4(\mathbf{x}) = f_6(f_5(x_1, x_2)) + f_6(f_5(x_2, x_3)) + \dots + f_6(f_5(x_{D-1}, x_D)) + f_6(f_5(x_D, x_1)) + F_4^* \quad (18)$$



(a) 3-D map for 2-D function (b) Contour map for 2-D function

Figure 4 Expanded Rosenbrock's plus Griewangk's Function

Properties:

- Non-separable
- Optimal point locates in flat area

B. Hybrid Functions

Considering that in the real-world optimization problems, different subcomponents of the variables may have different properties^[5]. In this set of hybrid functions, the variables are randomly divided into some subcomponents and then different basic functions are used for different subcomponents.

$$F(\mathbf{x}) = g_1(\mathbf{M}_1 z_1) + g_2(\mathbf{M}_2 z_2) + \dots + g_N(\mathbf{M}_N z_N) + F^*(\mathbf{x}) \quad (19)$$

$F(\mathbf{x})$: hybrid function

$g_i(\mathbf{x})$: i^{th} basic function used to construct the hybrid function

N : number of basic functions

$$\mathbf{z} = [z_1, z_2, \dots, z_N]$$

$$z_1 = [y_{S_1}, y_{S_2}, \dots, y_{S_m}], z_2 = [y_{S_{n+1}}, y_{S_{n+2}}, \dots, y_{S_{n+1}}], \dots, z_N = [y_{S_{N-1}}, y_{S_{N-1}}, \dots, y_{S_D}]$$

$$y = x - o_i, S = \text{randperm}(1:D)$$

p_i : used to control the percentage of $g_i(\mathbf{x})$

$$n_i : \text{dimension for each basic function } \sum_{i=1}^N n_i = D$$

$$n_1 = \lceil p_1 D \rceil, n_2 = \lceil p_2 D \rceil, \dots, n_{N-1} = \lceil p_{N-1} D \rceil, n_N = D - \sum_{i=1}^{N-1} n_i$$

Properties:

- Multi-modal or Unimodal, depending on the basic function
- Non-separable subcomponents
- Different properties for different variables subcomponents

5) Hybrid Function 1 (the same as F17 in CEC2014^[3])

$N = 3$

$p = [0.3, 0.3, 0.4]$

g_1 : Modified Schwefel's Function f_{11}

g_2 : Rastrigin's Function f_2

g_3 : High Conditioned Elliptic Function f_3

6) Hybrid Function 2 (the same as F16 in CEC2017^[4])

$N = 4$

$p = [0.2, 0.2, 0.3, 0.3]$

g_1 : Expanded Schaffer Function f_{12}

g_2 : HGBat Function f_4

g_3 : Rosenbrock's Function f_5

g_4 : Modified Schwefel's Function f_{11}

7) Hybrid Function 3 (the same as F21 in CEC2014^[3])

$N = 5$

$p = [0.1, 0.2, 0.2, 0.2, 0.3]$

g_1 : Expanded Schaffer Function f_{12}

g_2 : HGBat Function f_4

g_3 : Rosenbrock's Function f_5

g_4 : Modified Schwefel's Function f_{11}

g_5 : High Conditioned Elliptic Function f_3

8) Hybrid Function 4 (the same as f19 in CEC2017^[4])

$$F_7(\mathbf{x}) = f_{13}(\mathbf{x}) + F_7^*$$

C. Composition Functions

$$F(\mathbf{x}) = \sum_{i=1}^N \left\{ \omega_i^* [\lambda_i g_i(\mathbf{x}) + bias_i] \right\} + F^* \quad (20)$$

$F(\mathbf{x})$: composition function

$g_i(\mathbf{x})$: i^{th} basic function used to construct the composition function

N : number of basic functions

\mathbf{o}_i : new shifted optimum position for each $g_i(\mathbf{x})$, define the global and local optima's position

$bias_i$: defines which optimum is global optimum

σ_i : used to control each $g_i(\mathbf{x})$'s coverage range, a small σ_i gives a narrow range for that $g_i(\mathbf{x})$

λ_i : used to control each $g_i(\mathbf{x})$'s height

ω_i : weight value for each $g_i(\mathbf{x})$, calculated as below:

$$\omega_i = \frac{1}{\sqrt{\sum_{j=1}^D (x_j - o_{ij})^2}} \exp \left(-\frac{\sum_{j=1}^D (x_j - o_{ij})^2}{2D\sigma_i^2} \right) \quad (21)$$

Then normalize the weight $\omega_i = w_i / \sum_{i=1}^n w_i$

So when $\mathbf{x} = \mathbf{o}_i$, $\omega_j = \begin{cases} 1 & j = i \\ 0 & j \neq i \end{cases}$ for $j = 1, 2, \dots, N$, $f(\mathbf{x}) = bias_i + f^*$.

The local optimum which has the smallest bias value is the global optimum. The composition function merges the properties of the sub-functions better and maintains continuity around the global/local optima.

Functions $F_i' = F_i - F^*$ are used as g_i . In this way, the function values of global optima of g_i are equal to 0 for all composition functions in this report.

In CEC'14^[3], the hybrid functions are also used as the basic functions for composition functions (Composition Function 7 and Composition Function 8). With hybrid functions as the basic functions, the composition function can have different properties for different variables subcomponents.

Please Note: All the basic functions that have been used in composition functions are shifted and rotated functions.

9) Composition Function 1 (the same as F22 in CEC2017^[4])

$N=3$

$\sigma = [10, 20, 30]$

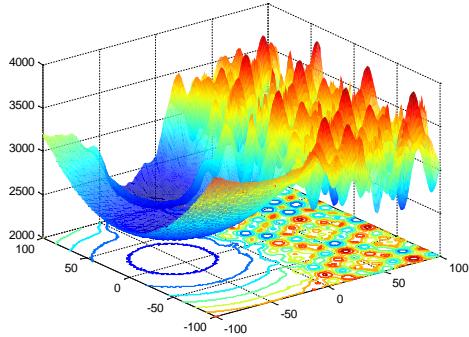
$\lambda = [1, 10, 1]$

$bias = [0, 100, 200]$

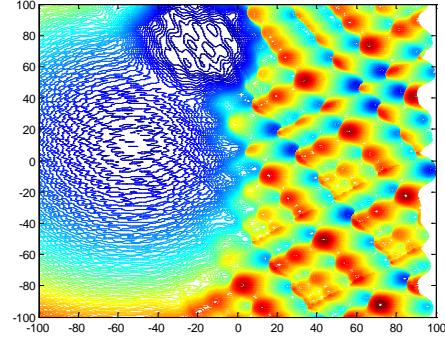
g_1 : Rastrigin's Function f_2

g_2 : Griewank's Function f_6

g_3 : Modified Schwefel's Function f_{11}



(a) 3-D map for 2-D function



(b) Contour map for 2-D function

Figure 5 Composition Function 1

Properties:

- Multi-modal
- Non-separable
- Asymmetrical
- Different properties around different local optima

10) Composition Function 2 (the same as F24 in CEC2017^[4])

$N=4$

$\sigma = [10, 20, 30, 40]$

$\lambda = [10, 1e-6, 10, 1]$

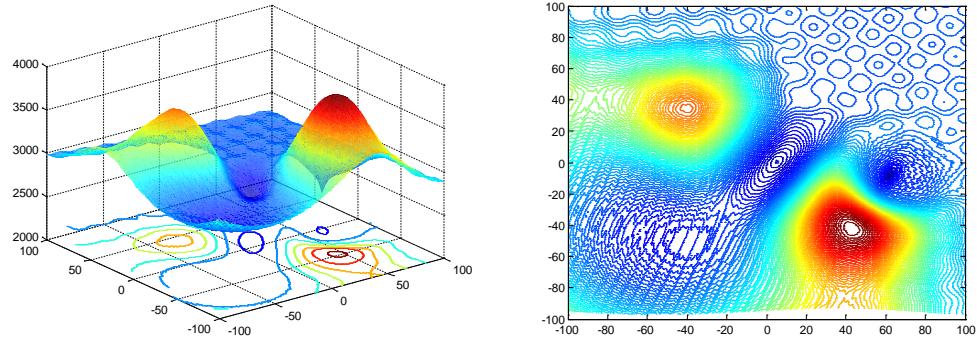
$bias = [0, 100, 200, 300]$

g_1 : Ackley's Function f_7

g_2 : High Conditioned Elliptic Function f_3

g_3 : Griewank's Function f_6

g_4 : Rastrigin's Function f_2



(a) 3-D map for 2-D function

(b) Contour map for 2-D function

Figure 6 Composition Function 2

11) Composition Function 3 (the same as F25 in CEC2017^[4])

$N=5$

$\sigma = [10, 20, 30, 40, 50]$

$\lambda = [10, 1, 10, 1e - 6, 1]$

$bias = [0, 100, 200, 300, 400]$

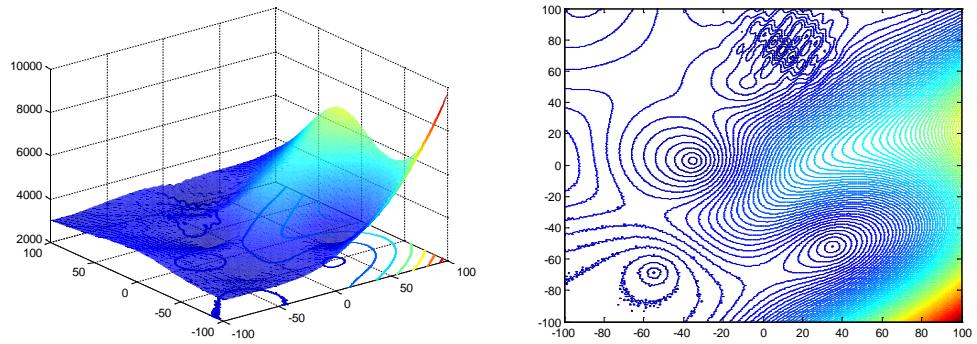
g_1 : Rastrigin's Function f_2

g_2 : HappyCat Function f_8

g_3 : Ackley's Function f_7

g_4 : Discus Function f_9

g_5 : Rosenbrock's Function f_5



(a) 3-D map for 2-D function

(b) Contour map for 2-D function

Figure 7 Composition Function 3

Properties:

- Multi-modal
- Non-separable

- Asymmetrical
- Different properties around different local optima

2. Evaluation Criteria

2.1. Experimental Setting

Problems: 10 minimization problems

Dimensions: $D = 5, 10, 15, 20$

Runs / problem: 30 (**Do not run many 30-trial runs to pick the best run**)

MaxFES:

MaxFES	
$D = 5$	50,000
$D = 10$	1,000,000
$D = 15$	3,000,000
$D = 20$	10,000,000

Search Range: $[-100,100]^D$

Initialization: Uniform random initialization within the search space. Random seed is based on time, Matlab users can use `rand ('state', sum(100*clock))`.

Global Optimum: All problems have the global optimum within the given bounds and there is no need to search outside of the given bounds for these problems.

$$F_i(\mathbf{x}^*) = F_i(\mathbf{o}_i) = F_i^*$$

Termination: Terminate when reaching MaxFES or the error value is smaller than 10^{-8} .

2.2. Results Record

1) **Record function error value ($F_i(\mathbf{x}) - F_i(\mathbf{x}^*)$) after $\left\lfloor D^{\frac{k}{5}-3} \text{MaxFEs} \right\rfloor$ ($k = 0, 1, 2, 3, \dots, 15$) for each run.**

For example, in problems with $D = 5$; the function error value after $\left\lfloor 5^{\frac{1}{5}-3} \times 50,000 \right\rfloor, \left\lfloor 5^{\frac{2}{5}-3} \times 50,000 \right\rfloor, \dots, \left\lfloor 5^{\frac{15}{5}-3} \times 50,000 \right\rfloor$ for each run need to be recorded.

In this case, **16** error values are recorded for each function for each run. Sort the error values achieved after MaxFES in 30 runs from the smallest (best) to the largest (worst) and present the best, worst, mean, median and standard variance values of function error values for the 30 runs.

Please Notice: Error values smaller than 10^{-8} will be taken as zero.

2) Performance Measure

- a) The evaluation criteria will be divided into two parts:
 1. 50% summation of error values for all dimensions
 2. 50% rank-based for each problem in each dimension
- b) Higher weight will be given for higher dimensions.

3) Algorithm Complexity

- a) Run the test program below:

```
x = 0.55  
for i = 1: 1000000  
    x = x + x; x = x / 2; x = x * x; x = sqrt(x); x = log(x); x = exp(x); x = x / (x + 2);  
end
```

Computing time for the above = T_0 ;

Evaluate the computing time just for Function 7. For 200000 evaluations of a certain dimension D , it gives T_1 ;

The complete computing time for the algorithm with 200000 evaluations of the same D dimensional Function 7 is T_2 .

Execute step c five times and get five T_2 values. $\bar{T}_2 = \text{Mean}(T_2)$

The complexity of the algorithm is reflected by: \bar{T}_2 , T_1 , T_0 , and $\bar{T}_2 - T_1/T_0$

The algorithm complexities are calculated on 5, 10, 15 dimensions, to show the algorithm complexity's relationship with dimension. Also provide sufficient details on the computing system and the programming language used. In step c, we execute the complete algorithm five times to accommodate variations in execution time due adaptive nature of some algorithms.

Please Note: Similar programming styles should be used for all T_0 , T_1 and T_2 .

(For example, if m individuals are evaluated at the same time in the algorithm, the same style should be employed for calculating T_1 ; if parallel calculation is employed for calculating T_2 , the same way should be used for calculating T_0 and T_1 . In other word, the complexity calculation should be fair.)

4) Parameters

Participants must not search for a distinct set of parameters for each problem/dimension/etc. Please provide details on the following whenever applicable:

- a) All parameters to be adjusted
- b) Corresponding dynamic ranges
- c) Guidelines on how to adjust the parameters
- d) Estimated cost of parameter tuning in terms of number of FEs

e) Actual parameter values used.

5) Encoding

If the algorithm requires encoding, then the encoding scheme should be independent of the specific problems and governed by generic factors such as the search ranges.

6) Results Format

The participants are required to send the final results as the following format to the organizers and the organizers will present an overall analysis and comparison based on these results.

Create one txt document with the name “AlgorithmName_FunctionNo._D.txt” for each test function and for each dimension.

For example, PSO results for test function 5 and $D = 10$, the file name should be “PSO_5_10.txt”.

Then save the results matrix (*the gray shadowing part*) as Table I in the file:

Table I Information Matrix for D Dimensional Function X

***.txt	Run1	Run2	...	Run30
Function error values when $FES = \left[D^{\frac{0}{5}-3} \text{MaxEFEs} \right]$				
Function error values when $FES = \left[D^{\frac{1}{5}-3} \text{MaxEFEs} \right]$				
Function error values when $FES = \left[D^{\frac{2}{5}-3} \text{MaxEFEs} \right]$				
Function error values when $FES = \left[D^{\frac{3}{5}-3} \text{MaxEFEs} \right]$				
.....				
Function error values when $FES = \left[D^{\frac{14}{5}-3} \text{MaxEFEs} \right]$				
Function error values when $FES = \left[D^{\frac{15}{5}-3} \text{MaxEFEs} \right]$				

Thus $10*4$ (5D, 10D, 15D, 20D) files should be zipped and sent to the organizers. Each file contains a $16*30$ matrix.

Notice: All participants are allowed to improve their algorithms further after submitting the initial version of their papers to CEC2020. And they are required to submit their results in the introduced format to the organizers after submitting the **final** version of paper as soon as possible.

2.3. Results Temple

Language: Matlab 2008a

Algorithm: Particle Swarm Optimizer (PSO)

Results

Notice:

Considering the length limit of the paper, only Error Values Achieved with MaxFES are need to be listed. While the authors are required to send all results (10*4 files described in section 2.2) to the organizers for a better comparison among the algorithms.

Table II Results for 5D

Func.	Best	Worst	Median	Mean	Std
1					
2					
3					
4					
5					
6					
7					
8					
9					
10					

Table III Results for 10D

...

Table IV Results for 15D

...

Table V Results for 20D

...

Algorithm Complexity

Table VI Computational Complexity

	T0	T1	T2	$T_2 - T_1 / T_0$
$D = 5$				
$D = 10$				
$D = 15$				

Parameters

- a) All parameters to be adjusted
- b) Corresponding dynamic ranges
- c) Guidelines on how to adjust the parameters
- d) Estimated cost of parameter tuning in terms of number of FES
- e) Actual parameter values used.

References

- [1] P. N. Suganthan, N. Hansen, J. J. Liang, K. Deb, Y. P. Chen, A. Auger & S. Tiwari, "Problem Definitions and Evaluation Criteria for the CEC 2005 Special Session on Real-Parameter Optimization," Technical Report, Nanyang Technological University, Singapore, May 2005 and KanGAL Report #2005005, IIT Kanpur, India, 2005.
- [2] J. J. Liang, B. Y. Qu, P. N. Suganthan, Alfredo G. Hernández-Díaz, "Problem Definitions and Evaluation Criteria for the CEC 2013 Special Session and Competition on Real-Parameter Optimization", Computational Intelligence Laboratory, Zhengzhou University, Zhengzhou China and Technical Report, Nanyang Technological University, Singapore, January 2013.
- [3] J. J. Liang, B. Y. Qu, P. N. Suganthan, "Problem Definitions and Evaluation Criteria for the CEC 2014 Special Session and Competition on Real-Parameter Optimization", Computational Intelligence Laboratory, Zhengzhou University, Zhengzhou China and Technical Report, Nanyang Technological University, Singapore, January 2014.
- [4] N. H. Awad, M. Z. Ali, P. N. Suganthan, J. J. Liang, B. Y. Qu, " Problem Definitions and Evaluation Criteria for the CEC 2017 Special Session and Competition on Single Objective Real-Parameter Numerical Optimization", Computational Intelligence Laboratory, Zhengzhou University, Zhengzhou China and Technical Report, Nanyang Technological University, Singapore, October 2016.
- [5] Xiaodong Li, Ke Tang, Mohammad N. Omidvar, Zhenyu Yang, and Kai Qin, "Benchmark Functions for the CEC'2013 Special Session and Competition on Large-Scale Global Optimization", Technical Report, 2013.