#### **IEEE WCCI/CEC 2024**

# Competition on "numerical optimization considering accuracy and speed"

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#### Reference:

KV Price, A Kumar, PN Suganthan, "Trial-based dominance for comparing both the speed and accuracy of stochastic optimizers with standard non-parametric tests", Swarm and Evolutionary Computation, 78, 101287, 2023.

# **Contents**

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#### **Bound constrained single objective optimization problems (BC-SOPs)**

**Test Problems:** The 29 real-parameter numerical optimization problems with 30*D* in CEC2017 [1] are adopted as test problems.

**Number of Trials/Problem:** 25 independent runs.

**Maximum Number of Function Evaluations:** Max\_FEs = 10000\*D, where *D* is the dimensionality of the optimization problems.

**Population Size:** You are free to have an appropriate population size to suit your algorithm while not exceeding the Max\_FEs.

**Sampling Points:** The best EV (Error Value) every 10\*D evaluations will be recorded for each run. For example, the maximum number of function evaluations Max\_FEs is 10000\*D, then 1000 EVs should be saved

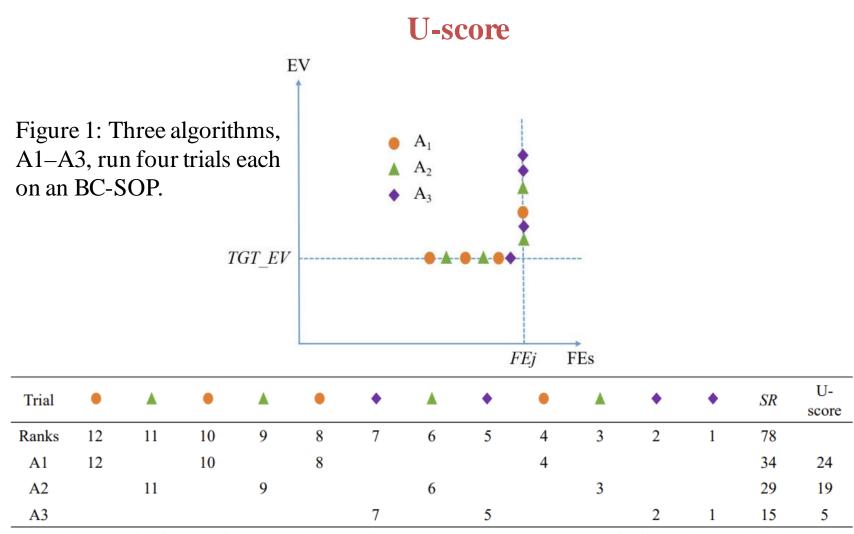
**Target Error Values:** The target error value, TGT\_EV for each problem, will be determined after the competition. Hence, all algorithms should be executed until the Maximum number of Function Evaluations (Max\_FEs) are consumed.

#### Bound constrained single objective optimization problems (BC-SOPs)

**Presentation of Results:** The results can be saved in the form of Table 1, where Min\_EV is the best error value of each run at each sampling point. The value should be recorded every 10\*D FEs. Thus, for each algorithm, 29 files should be zipped and sent to the organizers, where 29 represents the total number of test functions.

**Table 1**Results saved in "PaperID\_FJ\_Min\_EV.mat" where J=1,2,3,...29 problems.

	Run 1	Run 2	Run 3		Run 25
Min_EV at Initialisation FEs					
Min_EV at 10*D FEs		[			
Min_EV at 20*D FEs					
Min_EV at Max_FEs					



The "correction factor" (cf) is n(n+1)/2 = 4 \* 5/2 = 10, where n denotes the number of trails. SR denotes the sum of ranks. The scores of algorithms are calculated by the "SR" minus the "cf" according to the U-score algorithm.

Figure 2: U-score ranks for algorithms A1, A2 and A3.

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#### Constrained single objective optimization problems (CSOPs)

**Test Problems:** The 28 constrained real-parameter optimization problems with 30*D* in CEC2017 [2] are adopted as test problems.

**Number of Trials/Problem:** 25 independent runs.

**Maximum Number of Function Evaluations:** Max\_FEs = 20000\*D, where *D* is the dimensionality of the optimization problems.

**Population Size:** You are free to have an appropriate population size to suit your algorithm while not exceeding the Max\_FEs.

**Sampling Points:** Record  $f_{min}$  values and LCV every 10\*D evaluations. For example, if the maximum number of function evaluations Max\_FEs is 20000\*D, then  $2000 f_{min}$  values are recorded for trials with one or more feasible solutions. When the whole population is infeasible, the lowest LCV value of the population should be saved at the respective sampling points.

**Target Error Values:** The target error value will be determined after the competition. Hence, all algorithms should be executed until Maximum number of Function Evaluations (Max\_FEs) are consumed.

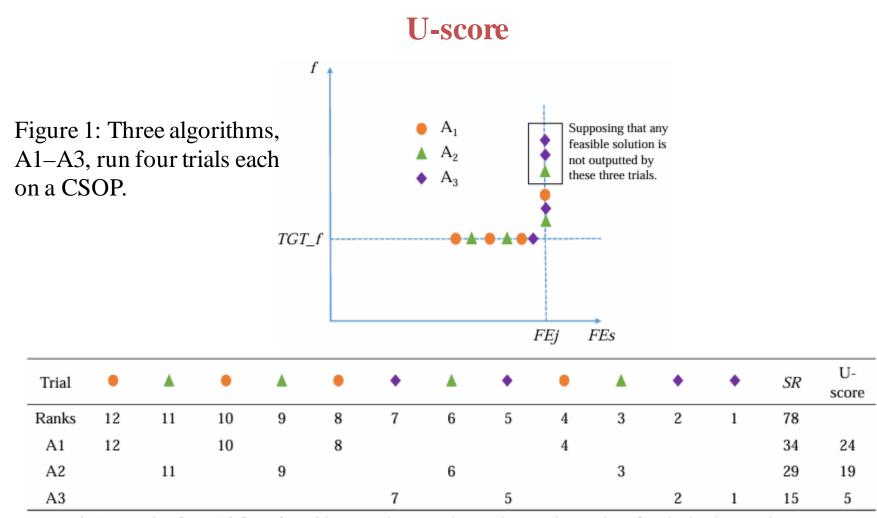
#### Constrained single objective optimization problems (CSOPs)

**Presentation of Results:** Save your results as shown in Table 2, in which the first entry is for the evaluation of the initial population. The cumulative FEs at each sampling point should be saved in the first column. Meanwhile, the corresponding *f min* and *LCV* results should be saved in the second and third columns, respectively. So, for a function, one run requires one file in mat format. Please note that if no feasible solution exists at one sampling point, the *f min* result should be expressed by "NaN".

$$LCV = \min : CV(P_i), i = 1,...,NP$$

Table 2
Results saved in "PaperID\_CPJ.mat" where J=1,2,...,28 problems

FEs	Run1		R	un2	 Ru	n25
1 L5	$f_{min}$	LCV	$f_{min}$	LCV	$f_{min}$	LCV
at Initialisation FEs						
Sampling Point 1, FEs=1*10D						
Sampling Point 2, FEs=2*10D						
Last Sampling Point, Max_FEs						



The "correction factor" (cf) is n(n + 1)/2 = 4 \* 5/2 = 10, where n denotes the number of trails. SR denotes the sum of ranks. The scores of algorithms are calculated by the "SR" minus the "cf" according to the U-score algorithm.

Figure 2: U-score ranks for CSOPs.

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#### Bound constrained multi-objective optimization problems (BC-MOPs)

**Test Problems:** We adopt the benchmark of [3] including 10 multi-objective problems to rank the optimizers of MOPs without constraints.

**Number of Trials/Problem:** 30 independent runs.

Maximum Number of Function Evaluations: 100000 for each function.

**Population Size:** 100.

**Sampling Points:** The *IGD* values will be recorded once every 200 function evaluations. For example, if the maximum number of evaluations Max\_FEs is 100000, then 500 *IGD* values are saved.

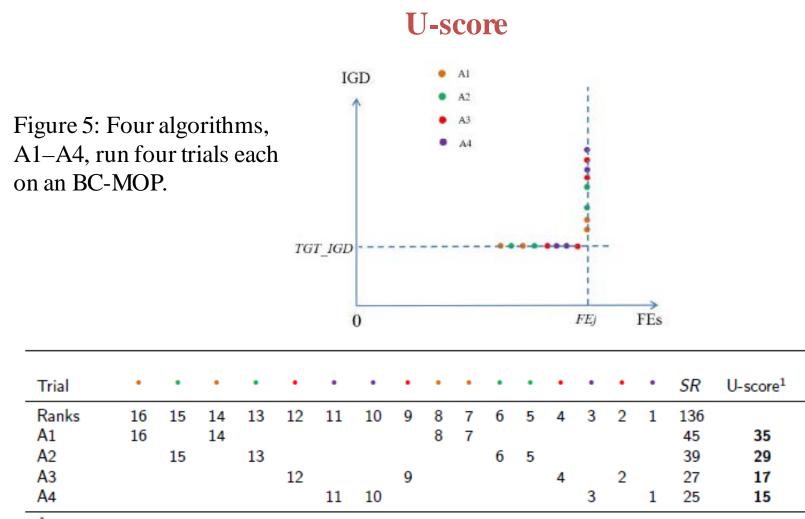
**Target Error Values:** The target *IGD* value will be determined after the competition. Hence, all algorithms should be executed until Maximum number of Function Evaluations (Max\_FEs) are consumed.

#### Bound constrained multi-objective optimization problems (BC-MOPs)

**Presentation of Results:** To compare and evaluate the algorithms participating in the competition, it is necessary that the authors email the results as shown in Table 4 to the organizers after submitting the final version of the accepted paper.

Table 4
Results saved in "PaperID RCMJ IGD.txt" where J=1,2,...,10 problems

	Run 1	Run 2	Run 3	 Run 30
IGD at Initialisation FEs				
IGD at Sampling Point 1				
IGD at Sampling Point 2				
IGD at Sampling Point 500, 100K FEs				



<sup>&</sup>lt;sup>1</sup> The "correction factor" cf is n(n+1)/2 = 4 \* 5/2 = 10, where n denotes the number of trials. SR denotes the sum of ranks. The scores of algorithms are calculated by the "SR" minus the "cf" according to the U-score algorithm.

Figure 6: U-score ranks for BC-MOEAs.

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#### Constrained multi-objective optimization problems (CMOPs)

**Test Problems:** The latest constrained multiobjective optimization problems with scalable decision space constraints (SDC problems) [4] are adopted as test problems. SDC benchmark contains 15 problems.

**Number of Trials/Problem:** 30 independent runs.

Maximum Number of Function Evaluations: 200000 for each function.

Population Size: 100. Dimension: 30 for each SDC function.

**Sampling Points:** The IGD values will be recorded once every 200 function evaluations. For example, if the maximum number of evaluations Max\_FEs is 200000, then 1000 IGD values are saved.

**Target Error Values:** The target IGD value will be determined after the competition. Hence, all algorithms should be executed until the Maximum number of Function Evaluations (Max\_FEs) are consumed. Please note that the minimal IGD value is unknown for multiobjective optimization problems. So, the mean or median IGD value of all trials from all algorithms participating in the competition will be set as the target IGD value

#### Constrained multi-objective optimization problems (CMOPs)

**Presentation of Results:** To compare and evaluate the algorithms participating in the competition, it is necessary that the authors email the results in the format as shown in Table 5 to the organizers, after submitting the final version of the accepted papers.

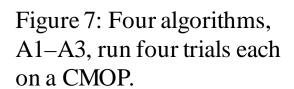
$$MCV = \frac{\sum_{i=1}^{PF} CV(P_i)}{PF}$$

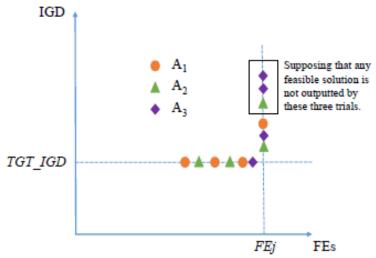
Table 5
Results saved in "PaperID SDCJ.mat" where J=1,2,...,15 problems.

at initialization FEs
Sampling point 1
Sampling point 2
...
Sampling point 1000

l .	un1	Run2			n 30
IGD	MCV	IGD	MCV	IGD	MCV







Trial	•	<b>A</b>	•	<b>A</b>	•	•	<b>A</b>	•	•	<b>A</b>	•	•	SR	U-
														score
Ranks	12	11	10	9	8	7	6	5	4	3	2	1	78	
A1	12		10		8				4				34	24
A2		11		9			6			3			29	19
A3						7		5			2	1	15	5

The "correction factor" (cf) is n(n+1)/2 = 4 \* 5/2 = 10, where n denotes the number of trails. SR denotes the sum of ranks. The scores of algorithms are calculated by the "SR" minus the "cf" according to the U-score algorithm.

Figure 8: U-score ranks for CMOPs.

## **Contents**

- >Introduction
- > Test problems suite
- >Indicators and rules
- > Participators
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BlockEA	♦ Xuhong Qi. Algorithm report for Block Evolutionary Algorithm, <a href="https://github.com/QiXuhong520/Algorithm-report">https://github.com/QiXuhong520/Algorithm-report</a> , 2024.
iEACOP	◆ Andrea Tangherloni, Vasco Coelho, Francesca M. Buffa, Paolo Cazzaniga. A modified EACOP implementation for Real-Parameter Single Objective Optimization Problems, 2024.
RDE	♦ Sichen Tao, Kaiyu Wang, Shangce Gao. An Efficient Reconstructed Differential Evolution Variant by Some of the Current State-of-the-art Strategies for Solving Single Objective Bound Constrained Problems, 2024.
mLSHADE	◆ Anupam Trivedi. A Multi-operator Ensemble LSHADE with Restart and Local Search Mechanisms for Single-objective Optimization, <a href="https://github.com/9997ravi/Technincal-Report-of-LSHADE-RL-for-IEEE-CEC-2024-Bound-Constrained-Real-Parameter-Optimization">https://github.com/9997ravi/Technincal-Report-of-LSHADE-RL-for-IEEE-CEC-2024-Bound-Constrained-Real-Parameter-Optimization</a> , 2024.
L-SRDE	♦ Vladimir Stanovov, Eugene Semenkin. Success Rate-based Adaptive Differential Evolution L-SRTDE for CEC 2024 Competition, 2024.
jSO	◆ Petr Bujok. Progressive Archive in Adaptive jSO Algorithm, <a href="https://github.com/PetBuj/jSOa/blob/main/jSOaGitHub.pdf">https://github.com/PetBuj/jSOa/blob/main/jSOaGitHub.pdf</a> , 20224.

Algorithm	Ranking	Authors	Paper title/link
BlockEA	1	Xuhong Qi	https://github.com/QiXuhong520/Algorith m-report
iEACOP	<b>2</b>	Andrea Tangherloni Vasco Coelho Francesca M. Buffa Paolo Cazzaniga	A modified EACOP implementation for Real-Parameter Single Objective Optimization Problems
RDE	<b>₩</b> 3	Sichen Tao Kaiyu Wang Shangce Gao	An Efficient Reconstructed Differential Evolution Variant by Some of the Current State-of-the-art Strategies for Solving Single Objective Bound Constrained Problems

Algorithm	Ranking	Authors	Paper title/link
mLSHADE	4	Anupam Trivedi	https://github.com/9997ravi/Technincal- Report-of-LSHADE-RL-for-IEEE-CEC- 2024-Bound-Constrained-Real-Parameter- Optimization
L-SRDE	5	Vladimir Stanovov Eugene Semenkin	Success Rate-based Adaptive Differential Evolution L-SRTDE for CEC 2024 Competition
jSO	6	Petr Bujok	https://github.com/PetBuj/jSOa/blob/main/j SOaGitHub.pdf

Prob\Alg							Prob\A						
0	BlockEA	iEACOP	RDE	mLSHADE	L-SRDE	jSO	lgo	BlockEA	iEACOP	RDE	mLSHADE	L-SRDE	jSO
f 01	2500 <mark>/2</mark>	3125/1	1250/4	1875 <mark>/3</mark>	346 <mark>/5</mark>	279/6	<i>f</i> 16	3125/1	2500/2	150/6	1825/3	1200/4	575 <mark>/5</mark>
f 02	25/6	1250/4	2235/3	600/5	2668/1	2597/2	f 17	3125/1	0/6	863/5	2500 <mark>/2</mark>	1473/3	1414/4
f 03	0/6	3125/1	1550/4	625/5	2350/2	1725/3	<i>f</i> 18	2547 <mark>/2</mark>	3060/1	1890/3	181/6	887/4	810/5
f 04	3125/1	2500/2	1875/3	1250/4	625/5	0/6	f 19	1850/3	3125/1	2500/2	1275/4	625/5	0/6
f 05	3125/1	2500/2	1875/3	1250/4	625/5	0/6	f 20	3125/1	2500/2	1875/3	1250/4	625/5	0/6
f 06	3125/1	2500/2	1875/3	1250/4	625/5	0/6	f 21	3125/1	2500/2	1875/3	1250/4	625/5	0/6
f 07	3125/1	2500/2	1875 <mark>/3</mark>	1250/4	625/5	0/6	f 22	3125/1	2500/2	1875/3	1250/4	625/5	0/6
f 08	2400/2	1198/5	134/6	2850/1	1521/3	1272/4	f 23	3125/1	2500/2	1875/3	1250/4	625/5	0/6
f 09	3125/1	2500/2	1875/3	1250/4	625/5	0/6	f 24	3125/1	2500/2	1875/3	1250/4	625/5	0/6
f 10	2919/1	2550 <mark>/2</mark>	231/6	1850/3	1225/4	600/5	f 25	3125/1	2500/2	1800/3	1275/4	650/5	25/6
$\frac{-f}{f}$ 11	3125/1	495/6	1718/3	2500/ <mark>2</mark>	797/4	740/5	f 26	3125/1	2500/2	1875/3	1250/4	625/5	0/6
	2783/1	2842/2	625/5	0/6	1614/3	1511/4	f 27	3125/1	2500/2	1875/3	1250/4	625/5	0/6
$\frac{f12}{f12}$	32/6	2341/2	2543/1	750/5	1893/3	1816/4	f 28	3125/1	2500 <mark>/2</mark>	75 <mark>/6</mark>	1850 <mark>/3</mark>	1225/4	600/5
f 13							f 29	3125/1	835/4	1668/3	2500/2	656/ <mark>5</mark>	591/6
<i>f</i> 14	369/6	3119/1	1434/3	2400/2	1075/4	978/5	sum/	74800/	67065/	44591/	39856/	29180/	16383
f 15	3125/1	2500/2	1425/4	0/6	1475/3	850/5	RS	54	68	103	110	122	/152

Algorithm	Ranking	Authors	Paper title/link
CL-SRDE	<b>1</b>	Vladimir Stanovov Eugene Semenkin	Differential Evolution with Success Rate-based adaptation CL-SRDE for Constrained Optimization
UDE-III	<b>2</b>	Anupam Trivedi	https://github.com/9997ravi/ Technical-Report-of-UDE- III-for-IEEE-CEC-2024- Real-parameter-Constrained- Optimization

**CL-SRDE** 

◆ Vladimir Stanovov, Eugene Semenkin. Differential Evolution with Success Rate-based adaptation CL-SRDE for Constrained Optimization, 2024.

**UDE-III** 

◆ Anupam Trivedi. UDE-III: An Enhanced Unified Differential Evolution Algorithm for Constrained Optimization Problems. <a href="https://github.com/9997ravi/Technical-Report-of-UDE-III-for-IEEE-CEC-2024-Real-parameter-Constrained-Optimization">https://github.com/9997ravi/Technical-Report-of-UDE-III-for-IEEE-CEC-2024-Real-parameter-Constrained-Optimization</a>, 2024.

Prob\Algo	CL-SRDE	UDE-III
C01	1875 <mark>/1</mark>	1250/2
C02	1875 <mark>/1</mark>	1250/2
C03	1250/2	1875/1
C04	1250/2	2447/1
C05	1875 <mark>/1</mark>	1250/2
C06	2237/1	2157 <mark>/2</mark>
C07	2172/1	2222/2
C08	2825/1	1575 <mark>/2</mark>
C09	2684/1	1716 <mark>/2</mark>
C10	2825/1	1575 <mark>/2</mark>
C11	1859/1	1266 <mark>/2</mark>
C12	1388/2	1737/1
C13	1853/1	1272 <mark>/2</mark>
C14	1250/2	1875/1

Prob\Algo	CL-SRDE	UDE-III
C15	1875/1	1250/2
C16	1250/2	1875/1
C17	1632/1	1493/2
C18	1250 <mark>/2</mark>	1875 <mark>/1</mark>
C19	1875 <mark>/1</mark>	1250 <mark>/2</mark>
C20	1304/2	1821/1
C21	1357/2	2340/1
C22	1875 <mark>/1</mark>	1250/2
C23	1550 <mark>/2</mark>	1575/1
C24	1875 <mark>/1</mark>	1250/2
C25	1250 <mark>/2</mark>	1875/1
C26	1808/1	1317/2
C27	1250 <mark>/2</mark>	1875/1
C28	1875 <mark>/1</mark>	1250/2
sum/RS	49244/39	45763 <mark>/45</mark>

Algorithm	Ranking	Authors	Paper ID		
TFBCEIBEA	1	Peng Chen Jing Liang Kangjia Qia Ponnuthurai Nagaratnam Suganthan Xuanxuan Ban	A Two-stage Evolutionary Framework For Multi-objective Optimization		
TGFMMOEA	<b>2</b>	Peng Chen	A Two-stage Evolutionary Framework For Multi-objective Optimization		
TEMOFNSGA3	3	Peng Chen	A Two-stage Evolutionary Framework For Multi-objective Optimization		

**TFBCEIBEA** ◆ Peng Chen, Jing Liang, Kangjia Qiao, P. N. Suganthan, Xuanxuan Ban. A Two-stage Evolutionary Framework For Multi-objective Optimization, 2024

Prob\Algo	TFBCEIBEA	TGFMMOEA	TEMOFNSGA3
, ,			
MaOP1	1467/1	447/3	786/2
MaOP2	1331/1	197/3	1172/2
MaOP3	924 <mark>/2</mark>	541/3	1235/1
MaOP4	311/3	1266 <mark>/1</mark>	1123/2
MaOP5	1138/1	545/3	1017/2
MaOP6	1459 <mark>/1</mark>	207/3	1034/2
MaOP7	842 <mark>/2</mark>	1065/1	793 <mark>/3</mark>
MaOP8	890/2	1086/1	724/3
MaOP9	685/3	1209/1	806/2
MaOP10	879/3	1013/1	808/2
sum/RS	9926/19	7576/ <mark>20</mark>	9498/21

#### DESDE ◆ Xuanxuan Ban. A Dynamic Exemplars Selection-based Differential Evolution Algorithm for Constrained Multi-objective Optimization, <a href="https://github.com/xxuanban/DESDE/blob/main/DESDE.pdf">https://github.com/xxuanban/DESDE/blob/main/DESDE.pdf</a>, 2024. ◆ Xiaoyu Zhong. Constrained Multi-Objective Optimization via Competitive and Cooperative Evolutionary Multitasking (CCEMT), <a href="https://github.com/wcq1536113693/zxyCCEMT">https://github.com/wcq1536113693/zxyCCEMT</a>, 2024. **CCEMT** ◆ Dezheng Zhang. Evolutionary Constrained Multiobjective Optimization: Scalable High-Dimensional Constraint Benchmarks and Algorithm, <a href="https://github.com/DezhengZ/Algorithm-Description-IMTCMO">https://github.com/DezhengZ/Algorithm-Description-IMTCMO</a>, **IMTCMO** 2024. and Competition-Based Tri-Population Evolutionary Algorithm for ◆ Lianhe Duan. A Cooperation Constrained Multi-objective Optimization Problems, <a href="https://github.com/LianheDuan/Algorithm-">https://github.com/LianheDuan/Algorithm-</a> **CCPTEA** Description.git, 2024. ◆ Wenhao Wu. A Novel Genetic Algorithm for CEC2024, <a href="https://github.com/zaishuiyifang1507/A-noverl-">https://github.com/zaishuiyifang1507/A-noverl-</a> genetic-algorithm-forCEC2024, 2024. **MTCMMO**

Algorithm	Ranking	Authors	Paper title/link
DESDE	1	Xuanxuan Ban	https://github.com/xxuanban/DESDE/blob/main/DESDE.pdf
CCEMT	2	Xiaoyu Zhong	https://github.com/wcq1536113693/z xyCCEMT
IMTCMO	<b>3</b>	Dezheng Zhang	https://github.com/DezhengZ/Algorit hm-Description-IMTCMO
CCPTEA	4	Lianhe Duan	https://github.com/LianheDuan/Algo rithm-Description.git
MTCMMO	5	Wenhao Wu	https://github.com/zaishuiyifang1507 /A-noverl-genetic-algorithm- forCEC2024

<b>7</b>	DEGDE		D (TEC) (C)		) (TIC) (1 (C)	Prob\Alg					MTCMM
Prob\Algo	DESDE	CCEMT	IMTCMO	CCPTEA	MTCMMO	О	DESDE	CCEMT	IMTCMO	CCPTEA	O
SDC1	2745/1	2526/ <mark>2</mark>	1916/3	1813/4	0/5	SDC9	3600/1	1387/4	1830 <mark>/2</mark>	1715 <mark>/3</mark>	468/5
SDC2	2844/1	2217 <mark>/2</mark>	1995/3	1944 <mark>/4</mark>	0/5	SDC10	2420/1	2159/2	1767 <mark>/4</mark>	1945 <mark>/3</mark>	709/5
SDC3	3001/1	2080/2	1733 <mark>/3</mark>	1321/4	865/5	SDC11	2864/1	2071 <mark>/2</mark>	2062/3	2003/4	0/5
SDC4	2589/1	1844 <mark>/4</mark>	2321/2	2246/3	0/5	SDC12	1633/4	2578/1	2492 <mark>/2</mark>	2297 <mark>/3</mark>	0/5
SDC5	2966/1	2006/2	1645 <mark>/4</mark>	1896 <mark>/3</mark>	487/5	SDC13	3575/1	1273/4	1496/3	1596/ <mark>2</mark>	1060/5
SDC6	2337/1	2168 <mark>/2</mark>	2045/3	1891/4	559 <mark>/5</mark>	SDC14	3189/1	1337/4	1560/3	1677 <mark>/2</mark>	1237/5
SDC7	1789 <mark>/4</mark>	2576/1	2528 <mark>/2</mark>	2107/3	0/5	SDC15	2877/1	2617 <mark>/2</mark>	1593/4	1739/3	174/5
						sum/	40389/	31246/	29268/	28538/	5559/
SDC8	1960 <mark>/4</mark>	2407/1	2285/3	2348/2	0/5	RS	24	35	44	47	75

#### **Verification**

Ranking related codes and data are made available online

Codes of top performing algorithms will be released online.

We will verify over the next few weeks.



# Thanks for your attention! Questions?