

**Laboratory of Robust Identification and Control (01PDXOV-01PDXQW-01PDXND)**

**Diego Regruto**

Exam simulation

<b>Surname</b>	<b>Name</b>
<b>Student ID</b>	

The student is required to solve the following two exercises:

**Exercise 1**

- (A) **4 Points** — Formulate the problem of identifying the mathematical model of the plant in the set-membership framework, on the basis of the following information:
- the plant can be modeled by a discrete-time linear time-invariant systems described by the following transfer function
$$G(z) = \frac{\beta_1 z + \beta_2}{z^2 + \alpha_1 z + \alpha_2}.$$
  - A set of 50 input-output data pair (available in the data file *data\_exam\_1A*) has been collected to describe the input-output behavior of the plant.
  - The input sequence is assumed to be exactly known, while the output data are known to be corrupted by an additive noise  $\eta(t)$  having absolute value of amplitude bounded by  $\Delta_\eta = 1$ .
- (B) **3 Points** — Provide a mathematical formulation of the optimization problems to be solved for the computation of the PUIs.
- (C) **5 Points** — Provide a accurate description of the data structure to be built in order to solve the problem with the sparsePOP software.
- (D) **6 Points** — Write a MATLAB script for the computation of the PUIs.

**Exercise 2**

- (A) **4 Points** — Formulate the problem of identifying the mathematical model of the plant in the set-membership framework, on the basis of the following information:
- the plant can be modeled by discrete-time linear time-invariant subsystem described by the following transfer function
$$G(z) = \frac{\beta_1 z + \beta_2}{z + \alpha_1}$$
  - The steady-state gain of the plant is know to belong to the range  $[5, 9]$

- The plant is known to have a zero belonging to the range  $[0.1, 0.5]$
  - A set of 30 input-output data pair (available in the data file  $S:\backslash LRIC\data\_exam\_2A\_dg$ ) has been collected to describe the input-output behavior of the plant.
  - Input and the output data sequences are known to be corrupted by additive noise signals  $\epsilon(t)$  and  $\eta(t)$  respectively, having absolute value of amplitude bounded by  $\Delta_\epsilon = \Delta_\eta = 0.07$ .
- (B) **3 Points** — Provide a mathematical formulation of the optimization problems to be solved for the computation of the PUIs.
- (C) **5 Points** — Provide a accurate description of the data structure to be built in order to solve the problem with the sparsePOP software.
- (D) **6 Points** — Write a MATLAB script for the computation of the PUIs.

**All the details of student's solution must be reported on the written examination papers. Each step of the proposed solution must be properly discussed.**