#### Lecture 23:

# Efficiently Evaluating Deep Networks

Parallel Computer Architecture and Programming CMU 15-418/15-618, Spring 2017

#### Tunes

## Something Good

Alt-J

(An Awesome Wave)

"Good things happen to students that come to class late in the semester."

- All musicians, everywhere.

## Today

- High-performance <u>evaluation</u> of deep neural networks
- We will focus on the parallelism challenges of <u>training</u>
   deep networks next time

#### Training/evaluating deep neural networks

#### Technique leading to many high-profile Al advances in recent years

Speech recognition/natural language processing



Image interpretation and understanding







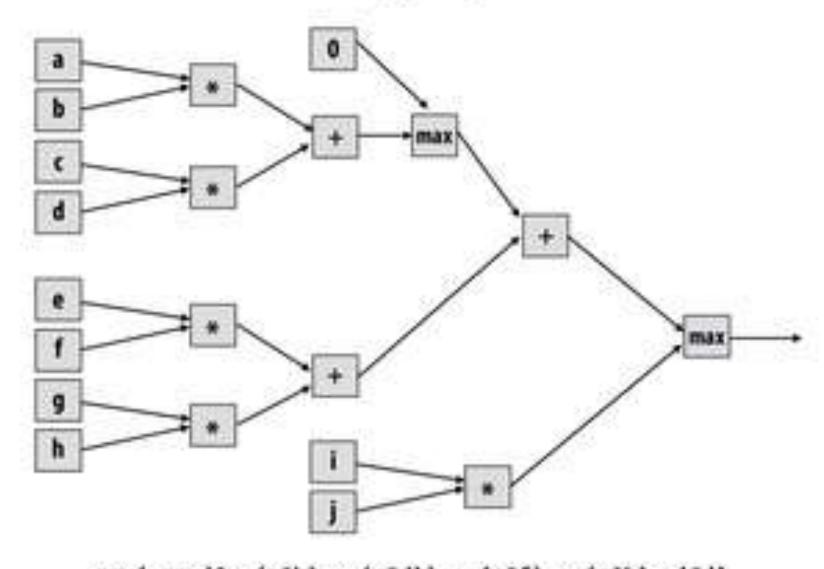








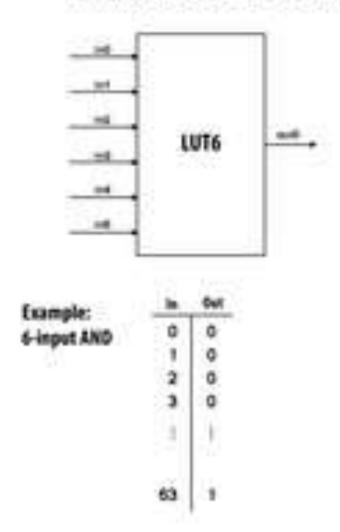
## Consider the following expression

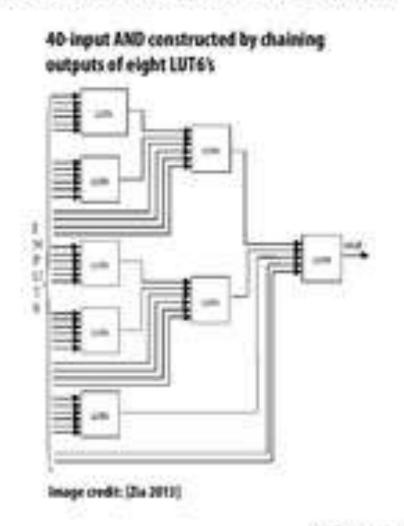


 $\max(\max(\theta, (a*b) + (c*d)) + (e*f) + (g*h), i*j)$ 

#### Consider expressing logic via a lookup table

- Example: 6-input, 1 output lookup table (LUT) in Xilinx Virtex-7 FPGAs
  - Think of a LUT6 as a 64 element table capable of expression functions of 6 bit inputs

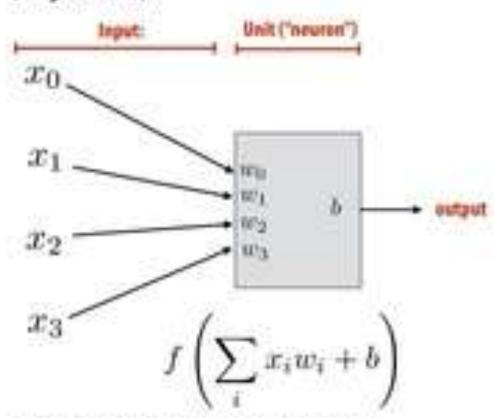




#### What is a deep neural network?

#### A basic unit:

Unit with n inputs described by n+1 parameters (weights + bias)



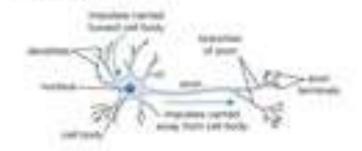
#### Example: rectified linear unit (ReLU)

$$f(x) = max(0, x)$$

#### Basic computational interpretation: It's just a circuit!

#### Biological inspiration:

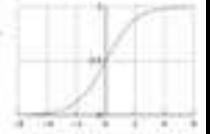
unit output corresponds loosely to activation of neuron



#### Machine learning interpretation:

binary classifier: interpret output as the probability of one class

$$f(x) = \frac{1}{1 + e^{-x}}$$



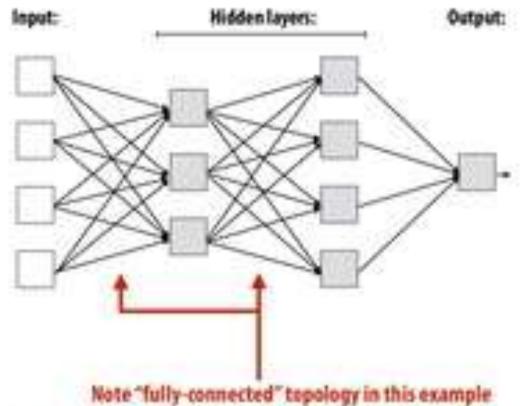
#### What is a deep neural network: topology

This network has: 4 inputs, 1 output, 7 hidden units

"Deep" = at least one hidden layer

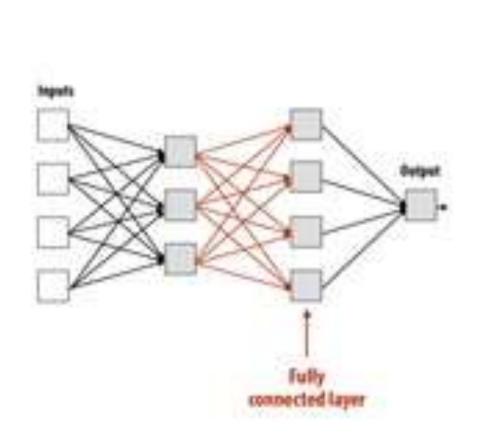
Hidden layer 1: 3 units x (4 weights + 1 bias) = 15 parameters

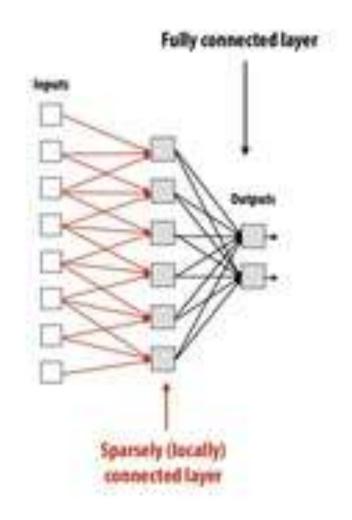
Hidden layer 2: 4 units x (3 weights + 1 bias) = 16 parameters



(every hidden unit receives input from all units on prior layer)

## What is a deep neural network: topology





#### Recall image convolution (3x3 conv)

```
int MIDTH - 1824;
                                                              Carrer
int HEIGHT - 1024;
float input[(WIDTH+2) * (HEIGHT+2)];
float output[WIDTH * HEIGHT];
float weights[] = {1.0/9, 1.0/9, 1.0/9,
                    1.0/9, 1.0/9, 1.0/9,
                    1.0/9, 1.0/9, 1.0/9);
for (int j-0; jeHEIGHT; j++) (
                                             Convolutional layer: locally connected AND all units in layer
  for (int 1=0; icwIDTH; 1++) (
                                             share the same parameters (same weights + same bias):
    float tmp = 0.f;
                                             inete: eathered idustration only shows links for a 1D core:
    for (int jj-0; jj:3; jj++)
                                             a.k.a. one iteration of £1 loop
      for (int ii=0; ii<3; ii++)
        tep ++ input[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
    output[j*HIDTH + 1] = tmp;
```

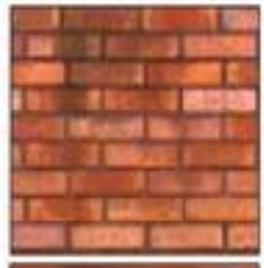
#### Strided 3x3 convolution

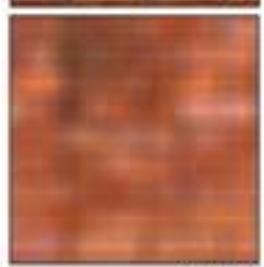
```
int WIDTH - 1024;
int HEIGHT - 1024;
int STRIDE = 2;
float imput[(WIDTH+2) * (HEIGHT+2)];
float output[(WIDTH/STRIDE) * (HEIGHT/STRIDE)];
float weights[] = {1.0/9, 1.0/9, 1.0/9,
                   1.0/9, 1.0/9, 1.0/9,
                   1.0/9, 1.0/9, 1.0/9);
for (int j=0; jeHEIGHT; j+=STREDE) (
  for (int 1-0; icwIDTH; i++5THIDE) (
    float tmp = 0.f;
                                                                 Convolutional layer with stride 2
    for (int jj-0; jje3; jj++)
      for (int 11:0; 11<3; 11++) (
         tmp += imput[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
      output[(j/STRIDE)*WIDTH + (1/STRIDE)] - tmp;
```

# What does convolution using these filter weights do? [111 111 111 111 Box blur"









## What does convolution using these filter

weights do? [.075 .124 .075]

"Gaussian Blur"









#### What does convolution with these filters do?

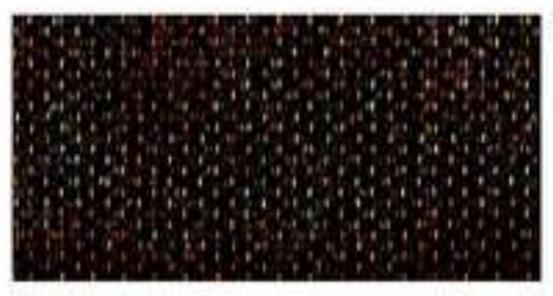
$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

Extracts horizontal gradients

Extracts vertical gradients

#### **Gradient detection filters**



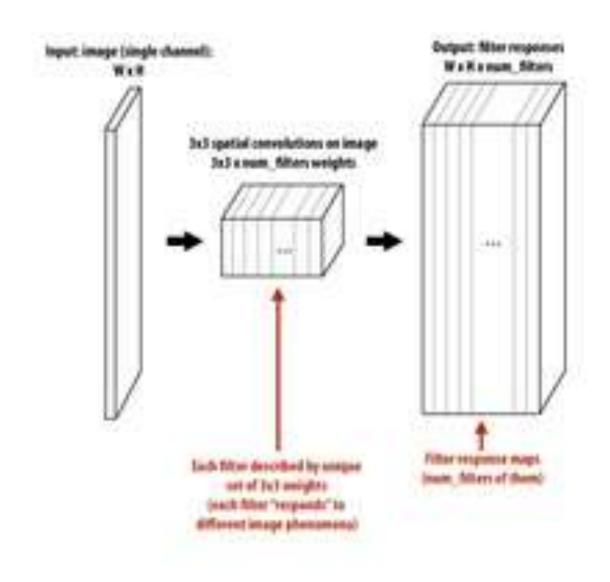
Horizontal gradients



**Vertical gradients** 

Note: you can think of a filter as a "detector" of a pattern, and the magnitude of a pixel in the output image as the "response" of the filter to the region surrounding each pixel in the input image

## Applying many filters to an image at once

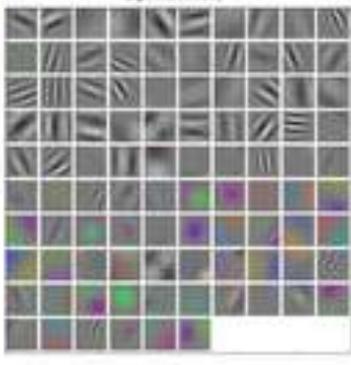


## Applying many filters to an image at once

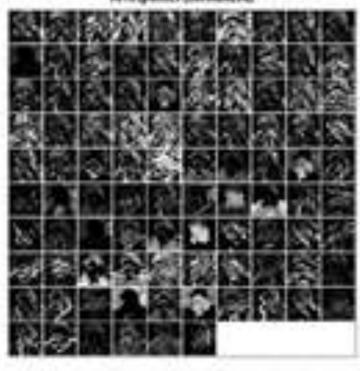
Input RGB image (Wx N x S)



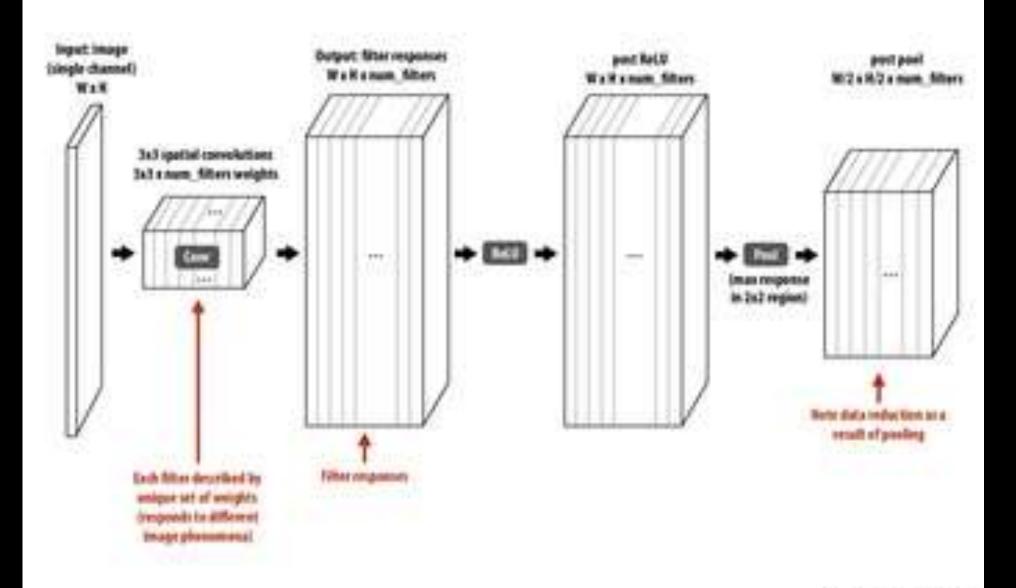
56 The Uted filters (operate on RGB)







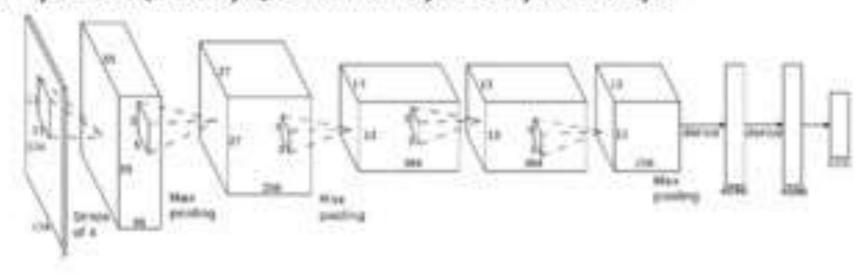
### Adding additional layers



#### Example: "AlexNet" object detection network

Sequences of conv + reLU + pool (optional) layers

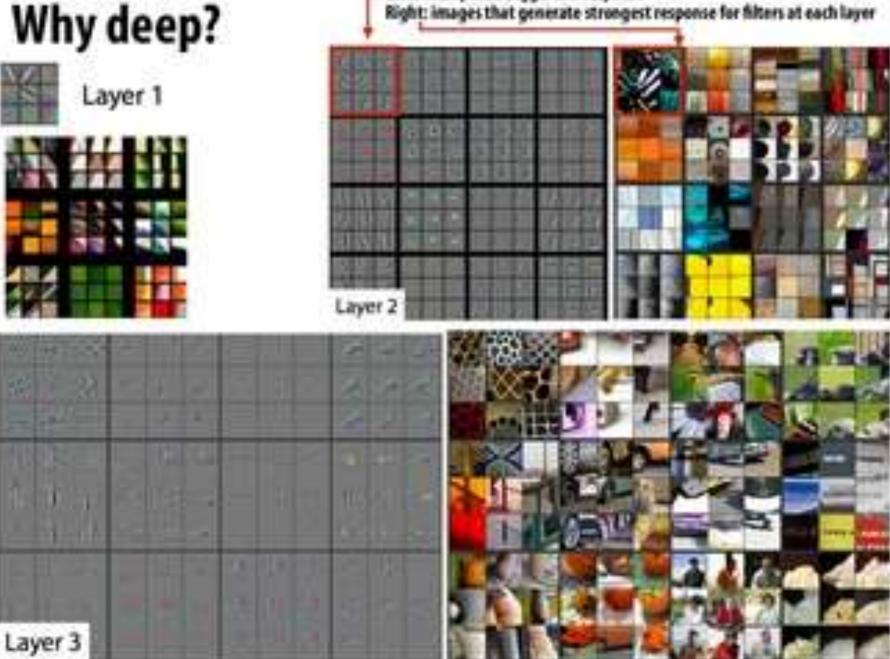
Example: AlexNet (Krizhevsky12): 5 convolutional layers + 3 fully connected layers



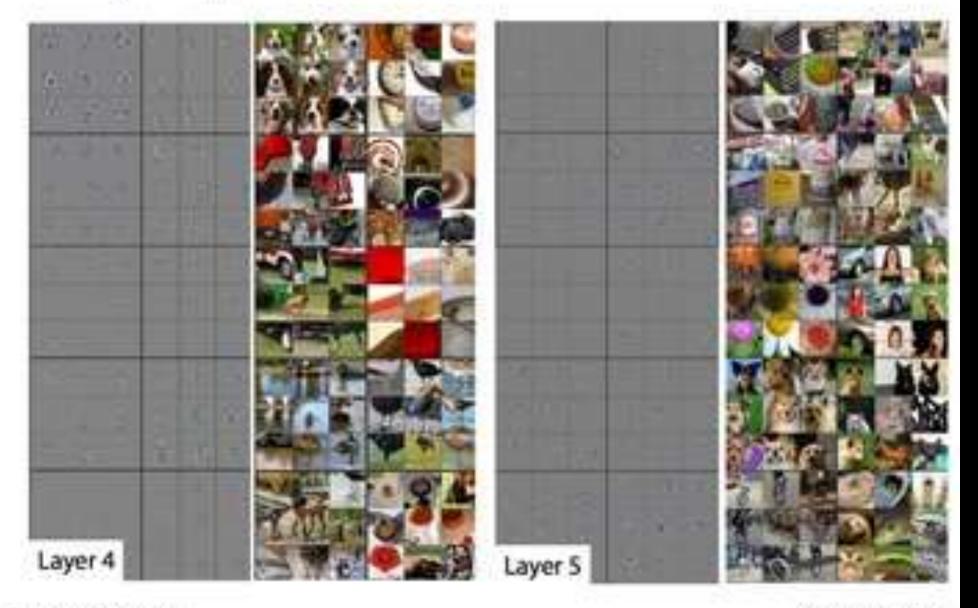
#### Another example: VGG-16 [Simonyan15]: 13 convolutional layers

input: 224 x 224 RGB	conventity 3x5x12hx256	committee 3 days 12 d 512
construit it indistruit	convinel@: 3x3x256x256	convincial: 3x3x512x512
convinctil: 3x3x64x64	committel (0): 3x3x256x256	concintil: 3x3x512x512
maxpool	maxpool	margeal
commetti: 3x3x64x128	construction 3x3x256x512	fully-connected 4096
convincial: 3x3x128x128	committed in helpfall (2x512x512)	fully connected 4096
maxpool	converted 3x3x512x512	fully-connected 1000
	manned	suff-max

# Left: what pixels trigger the response Why deep? Layer 1

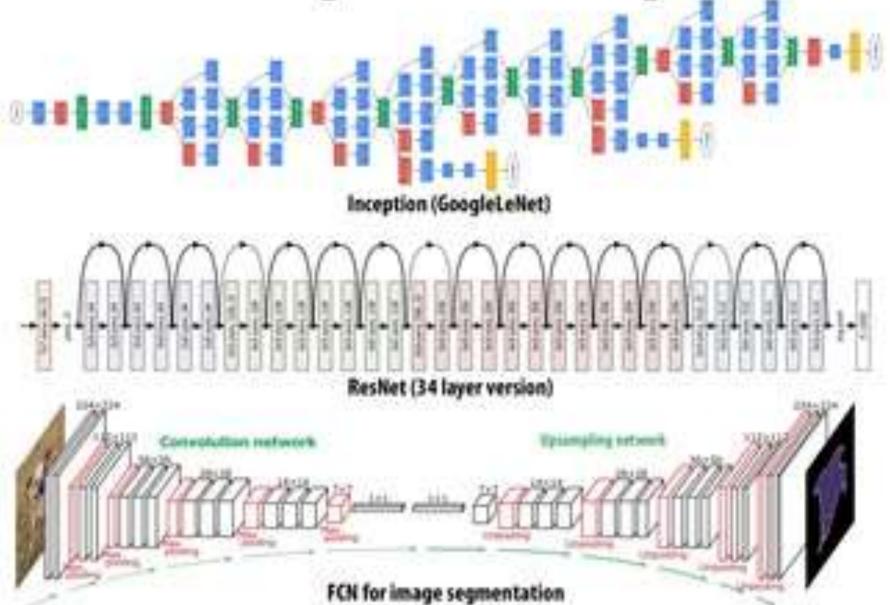


## Why deep?



[Image credit: Zeiler 14]

# More recent image understanding networks



#### Deep networks learn useful representations

- Simultaneous, multi-scale learning of useful concepts for the task at hand
  - Example on previous slides: subparts detectors emerged in network for object classification
- But wait... how did you learn the values of all the weights?
  - Next class!
  - For today, assume the weights are given (today is about evaluating deep networks, not training them)

## Efficiently implementing convolution layers

#### Dense matrix multiplication

```
float A[M][K];
float S[K][N];

float C[M][N];

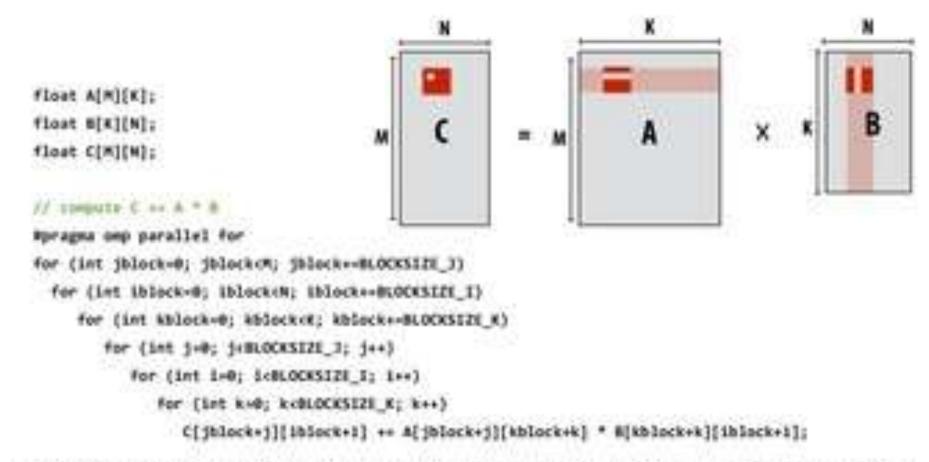
// cospute C -= A * 0

Mpragma comp parallel for
for (int j=0; j<M; j++)
   for (int k=0; k<K; k++)
        C[j][1] -= A[j][k] * B[k][1];</pre>
```

#### What is the problem with this implementation?

Low arithmetic intensity (does not exploit temporal locality in access to A and B)

#### Blocked dense matrix multiplication



Idea: compute partial result for block of C while required blocks of A and B remain in cache (Assumes BLOCKSIZE chosen to allow block of A, B, and C to remain resident)

Self check: do you want as big a BLOCKSIZE as possible? Why?

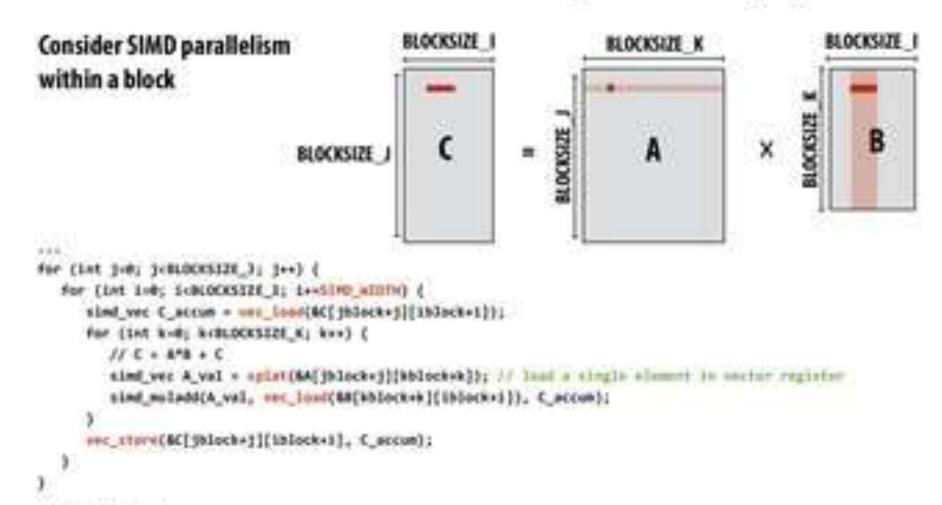
#### Hierarchical blocked matrix mult

#### Exploit multi-level of memory hierarchy

```
float A[A][K];
float m[#][M];
float C[M][N]:
// sproute C ++ A * S
Apragma omp parallel for
for (int jblock2+0; jblock1<ff; jblock2++L1_fil0CK5III_J)
 for (int iblock)+0; iblock2cN; iblock2++12_810CCS12%_I)
     For (int shiock3+8; shiock2+8; shiock2++L2 SLOCK137E K)
       For (Lot (blockles; [Blocklets StOCKSITE_F) (blocklest) StOCKSITE_3)
           for (int iblock:-0; iblock::ii miocks::: iblock::-ii mocks::: i)
             for (Set Ablocks-B; Ablocks-L1_DIDEXSERS_E; Ablocks-L1_SCOCKSERS_E)
                 FOR (100 300) SERIBOXXIII (S-300)
                     for (let let) lett/costat_[, let)
                       ther [300 9+0; $vMiDOSSZS_6; 8+4]
                          ...
```

Not shown: final level of "blocking" for register locality...

## Blocked dense matrix multiplication (1)

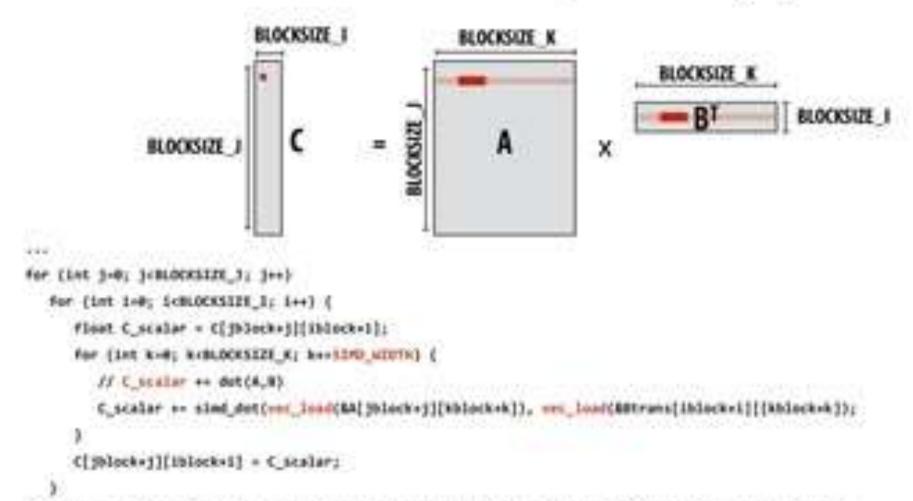


#### Vectorize i loop

Good: also improves spatial locality in access to B

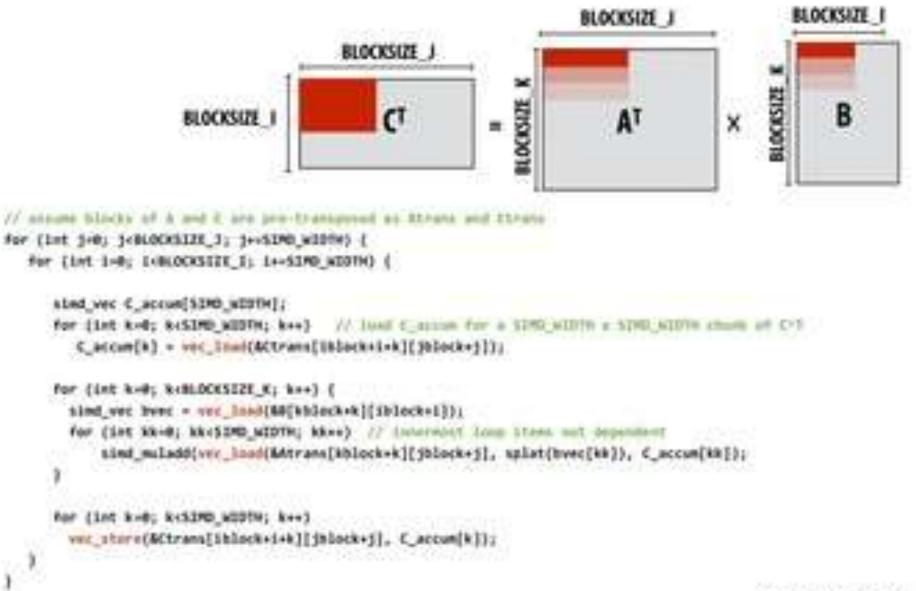
Bad: working set increased by SIMD\_WIDTH, still walking over B in large steps

#### Blocked dense matrix multiplication (2)



Assume i dimension is small. Previous vectorization scheme (1) would not work well. Pre-transpose block of B (copy block of B to temp buffer in transposed form) Vectorize innermost loop

### Blocked dense matrix multiplication (3)

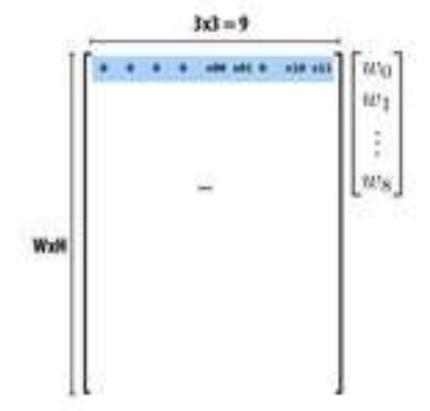


#### Convolution as matrix-vector product

Construct matrix from elements of input image

X <sub>ee</sub>	Xes	X43	X <sub>11</sub>	-	
Xoa	XII	X <sub>10</sub>	X <sub>rs</sub>	-	
X <sub>im</sub>	X <sub>11</sub>	X <sub>02</sub>	X <sub>C</sub>	-	
X,e	Xir	1,0	$\mathbf{I}_{0}$	-	
-		-	-		
	L	_		Ш	+

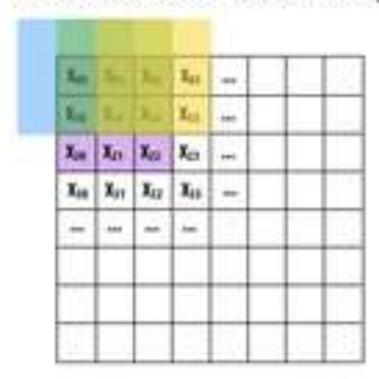
O(N) storage multiplier for filter with N elements Must construct input data matrix



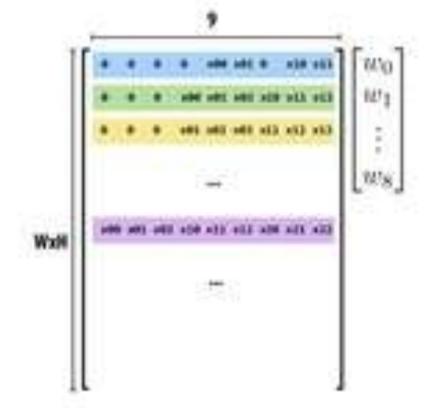
Note: 0-pad matrix

#### 3x3 convolution as matrix-vector product

Construct matrix from elements of input image

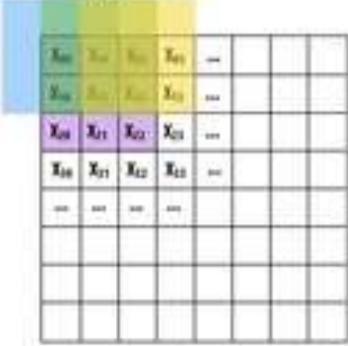


O(N) storage overhead for filter with N elements Must construct input data matrix



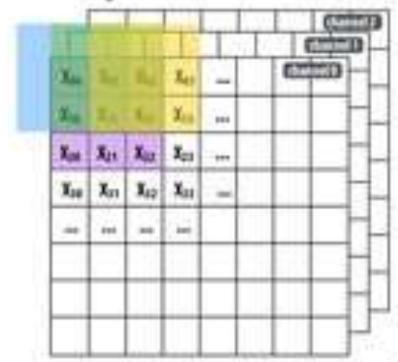
Note: 0-pad matrix

## Multiple convolutions as matrix-matrix mult



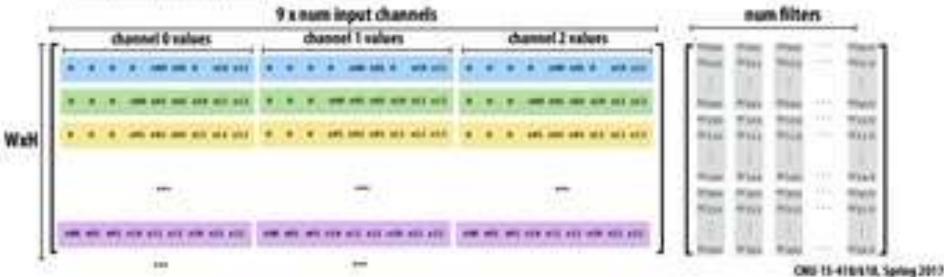
WXH

#### Multiple convolutions on multiple input channels



For each filter, sum responses over input channels

Equivalent to (3 x 3 x num\_channels) convolution on (W x H x num\_channels) input data



# VGG memory footprint Calculations assume 32-bit values (image batch size = 1)

hatch size

nuttiply by next layer's come window size to form input matrix to next cone Departs (for YOU's 3x). data amplification

	weights mem:	(per image)	(mem)
input: 224 x 224 RGB image	-	224x224x3	150K
conv. (DaSal) a 64	6.5 KB	224x224x64	12.3 MB
conv: (3x3x64) x 64	144 83	224x224x64	12.3 Mg
maxpool	-	112x112x64	3.1 MB
conv: (3x3x64) x 128	228 KB	112x112x128	6.2 MB
conv: (3x3x128) x 128	576 KB	112x112x128	62 MB
maxpool	-	\$6x56x128	1.5 MB
conv. (3x3x128) x 256	1.1 MS	56x56x256	3.1 MB
coev: (3x3x256) x 256	2.3 MB	56x56x256	3.1 MB
conv. (3x3x256) x 256	2.3 MB	56x56x256	3.1 MB
maxpool	-	28x28x256	766 KB
conv: (3x3x256) x 512	4.5 MB	28x28x512	1.5 MB
comy: (3x3x512) x 512	9 MB	28x28x512	1.5 MB
conv. (3x3x512) x 512	9.MB	28x28x512	1.5 MB
maxpool	-	14x14x512	383 KB
conv: (3x2x512) x 512	9MB	14x14x512	383.88
conv: (3x3x512) x 512	9 MB	14:14:512	383 88
conv: (3x3x512) x 512	9M6	14x14x512	383 108
maxpool	-	7x7x512	98 KB
fully connected 4096	392 MB	4096	16 KB
fully-connected 4096	64 MB	4096	16 KB
fully-connected 3000	15.6 MB	1000	4 88
soft-max		1000	4 808
		110000	

#### Direct implementation of conv layer

```
float input[imput_editor][imput_editor][imput_btpre];
float output[IMPUT_MEIGHT][IMPUT_MIDTH][LARER_MUM_FILTERS];
Float layer_weights[LAYER_COMO*][LAYER_COMOX][IMPUT_DEFTH]]
// debess newelstre strike in i
for (int imp-0; lag-DAGE_BATCH_SIZE; lag-+)
   for (int j=0; j<1MUT_ME1SH1; j++)
      for (LAT 1-0; 1/DAPUT WIRTH; 1+4)
        for (int fee; felaver mm filters; fee) (
            metput[j][i][f] = #.f;
           for (lot ak-0; akecumut control akee)
              Nor (int 3)=0; jjcLAYER_COMPY; 33++)
                                                      If spatial consolyties (V)
                  for (let 11-0; 11-13978_COWN; 11+) // spottal commistion (3)
                      output[5][1][4] +- layer_weights[4][33][11][8k] * laput[5+33][1+11][8k];
```

Seven loops with significant input data reuse: reuse of filter weights (during convolution), and reuse of input values (across different filters)

Avoids O(N) footprint increase by avoiding materializing input matrix.

In theory loads O(N) times less data (potentially higher arithmetic intensity... but matrix mult is typically compute bound).

East must roll your own highly optimized implementation of complicated loop nest.

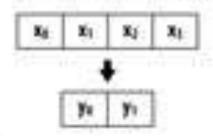
### Conv layer in Halide

```
// Input parama: susume initialized
int in w, in h, in ch = 4;
                                   // assume Angust Function is initialized
fued in functi
int num_f, f_w, f_h, pad, stride; // parameters of the same layer
func forward - Func("conv");
Var x("x"), y("y"), x("x"), x("x"); // = 10 minibatch dimension
// This creates a padded input to avoid checking boundary
// conditions while computing the actual convenietion
f in bound - BoundaryConditions::repeat_edge(in_func, 0, in_w, 0, in_h);
// Create image buffers for Layer paraestors
Imageofloats W(f.w. f.h. in ch. num f)
Image: float: b(www.f);
Abos r(0, f_w, 0, f_h, 0, in_ch);
// lartialize to bise
forward(x, y, z, z) = b(z);
forward(x, y, z, h) \leftrightarrow W(r, x, r, y, r, z, z) *
                       f in bound(x*stride + r.x = pad,
                                 y'stride + r.y - pad,
                                F. L. B. .
```

Consider scheduling this seven-dimensional loop nest.

## Algorithmic improvements

- Direct convolution can be implemented efficiently in Fourier domain (convolution → element-wise multiplication)
  - Overhead: FFT to transform inputs into Fourier domain, inverse FFT to get responses back to spatial domain (NIgN)
  - Inverse transform amortized over all input channels (due to summation over inputs)
- Direct convolution using work-efficient Winograd convolutions
   1D example: consider producing two outputs of a 3-tap 1D convolution with weights: w<sub>0</sub> w<sub>1</sub> w<sub>2</sub>



 $\begin{bmatrix} y_0 \\ y_1 \end{bmatrix} = \begin{bmatrix} x_0 & x_1 & x_2 \\ x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} w_0 \\ w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} m_1 + m_2 + m_3 \\ m_2 - m_3 - m_4 \end{bmatrix}$ 

10 3-tap total cost:

4 multiplies

8 additions

(4 to compute m's + 4 to reduce final result)

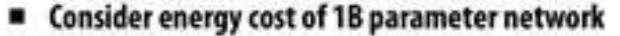
Direct convolution: 6 multiplies, 4 adds

$$m_1 = (x_0 - x_1)w_0$$
  
 $m_2 = (x_1 + x_2) \frac{w_0 + w_1 + w_2}{2}$  (can be precomputed)  
 $m_3 = (x_2 - x_1) \frac{w_0 - w_1 + w_2}{2}$   
 $m_4 = (x_1 - x_3)w_2$ 

(3x3 filter: 2.25x fewer multiples for 2x2 block of output)

## Reducing network footprint

- Large storage cost for model parameters
  - AlexNet model: ~200 MB
  - VGG-16 model: ~500 MB
  - This doesn't even account for intermediates during evaluation
- Footprint: cumbersome to store, download, etc.
  - 500 MB app downloads make users unhappy!

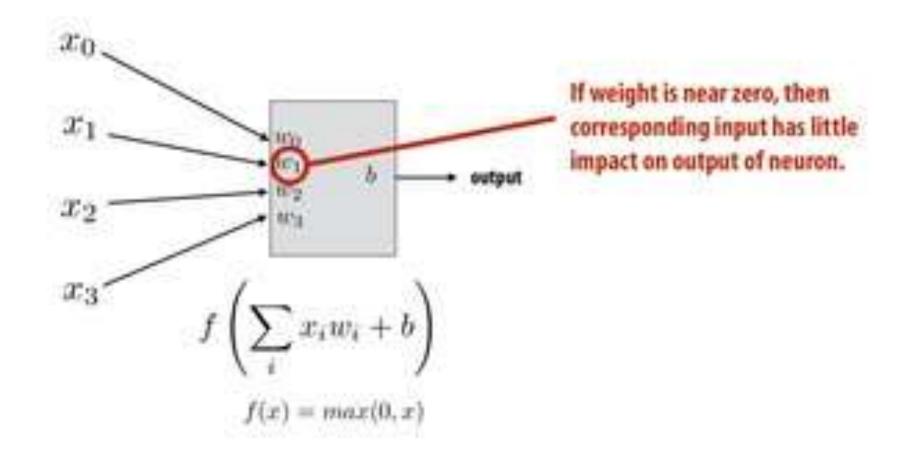


- Running on input stream at 20 Hz
- 640 pJ per 32-bit DRAM access
- (20 x 1B x 640pJ) = 12.8W for DRAM access

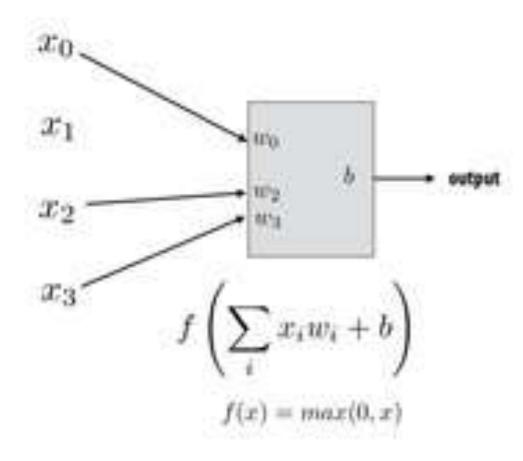
(more than power budget of any modern smartphone)



# "Pruning" (sparsifying) a network



# "Pruning" (sparsifying) a network



Idea: prune connections with near zero weight

Remove entire units if all connections are pruned.

### Representing "sparsified" networks

Step 1: prune low-weight links (iteratively retrain network, then prune)

- Over 90% of weights in fully connected layers can be removed without significant loss of accuracy
- Store weight matrices in compressed sparse row (CSR) format

```
Indices 1 4 9 ... 9 1.8 0 0 0.5 0 0 0 1.1 ...
```

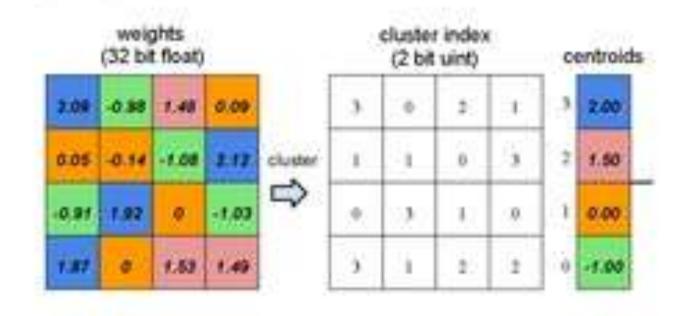
Reduce storage over head of indices by delta encoding them to fit in 8 bits

```
Indices 1 3 6 ...
Value 1.8 0.5 2.1
```

## Efficiently storing the surviving connections

Step 2: Weight sharing: make surviving connections share a small set of weights

- Cluster weights via k-means clustering
- Compress weights by only storing index of assigned cluster (lg(k) bits)
- This is lossy compression



Step 3: Huffman encode quantized weights and CSR indices (lossless compression)

### VGG-16 compression

### Substantial savings due to combination of pruning, quantization, Huffman encoding \*

Lajor	Weights	Weighte/S- (P)	Weigh hiss (P=Q)	Weight hits (P+Q+H)	State State (P+Q)	Indes No. (P+Q+H)	Compress rate (P+Q)	Compress rate (P+Q+H)
cate L.F.	2K	59%	-	6.5	5	1.7	40.0%	29.97%
comit.2	37K	22%	8	6.5	5	2.6	9.8%	6.99%
cries2.1	24K	34%	8	3.6	5	2.4	14.3%	8.91%
cres 2.2	14000	34%	.00	5.9	5	2.3	14.7%	9.31%
L.Denos	295K	33%		4.9	5	1.8	21.7%	11.13%
mm.1.2	7990W.	24%	W.	4.0	9.	2.0	9.7%	5.67%
C.Como	590K	42%		4.6	5	2.2	17.0%	8.99/3
com-4.1	IM	32%	8	4.6	5	2.6	13.1%	7.29%
com4.3	258	27%	8	4.2	5	2.9	10.9%	7.93%
Cremi 4.3	254	34%	.00	4.4	5	2.5	1400%	7.47%
L.benn	294	35%		4.2	2	2.5	14.3%	8.009
med.2	2M	299	W	4.0	9.	2.7	11.7%	6.52%
Cours.	234	7695		4.6	5	2.3	14.8%	7.79%
foh:	10334	4%	3.	3.6	3	3.5	1.6%	1.10%
67	17M	45	8	4	5	4.3	1.59	1.25%
0/8	4M	276	6	4	5	3.4	7.1%	5.24%
Timal	13000	2.5%(13×):	6.4	4.1	1	3.1	3.25 (31 / )	2,05% (49)

P -- connection gruning (prome low weight connections)

Q = quantitie surviving weights (using shared weights)

H = Huffman encode

#### ImageNet Image Classification Performance

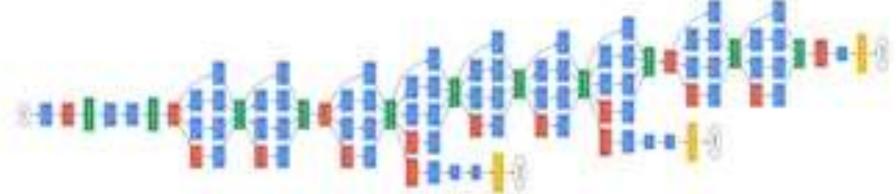
	Top 1 firms	Top-5 Error	Value Annual Landing	17
VOG-16 Rut	31.50%	11.52%	552 506	
VOG-IN Congressial	33.17%	100,907%	11.3 MB	44-

<sup>\*</sup> Benefits of automatic pruning apply mainly to fully connected layers, but many modern networks are dominated by costs of convolutional layers

## More efficient topologies

- Original DNNs for image recognition where overprovisioned
- Can think of modern designs as hand-designed to be sparser

SqueezeNet: [landola 2017] Reduced number of parameters in AlexNet by S0x, with similar performance on image classification



Inception (GoogleLeNet) — 27 total layers, 7M parameters



ResNet (34 layer version)

### Deep neural networks on GPUs

- Many high-performance DNN implementations target GPUs
  - High arithmetic intensity computations (computational characteristics similar to dense matrix-matrix multiplication)
  - Benefit from flop-rich architectures
  - Highly-optimized library of kernels exist for GPUs (cuDNN)

Most CPU-based implementations use basic matrix-multiplication-based formulation (good implementations could run faster!)





# Increasing efficiency through specialization

Example: Google's Tensor Processing Unit (TPU)
Accelerates deep learning operations



## Emerging architectures for deep learning

- NVIDIA Pascal (NVIDIA's latest GPU)
  - Adds double-throughput 16-bit floating point ops
  - This feature is already common on mobile GPUs
- Intel Xeon Phi (Knights Landing)
  - Flop rich 68-core x86 processor for scientific computing and machine learning
- FPGAs, ASICs
  - Not new: FPGA solutions have been explored for years
  - Significant amount of ongoing industry and academic research
  - Google's TPU

# Programming frameworks for deep learning

- Heavyweight processing (low-level kernels) carried out by target-optimized libraries (NVIDIA cuDNN, Intel MKL)
- Popular frameworks use these kernel libraries
  - Caffe, Torch, Theano, TensorFlow, MxNet
- DNN application development involves constructing novel network topologies







## Summary: efficiently evaluating deep nets

- Computational structure
  - Convlayers: high arithmetic intensity, significant portion of cost of evaluating a network
  - Similar data access patterns to dense-matrix multiplication (exploiting temporal reuse is key)
  - But straight reduction to matrix-matrix multiplication is often sub-optimal
  - Work-efficient techniques for convolutional layers (FFT-based, Wingrad convolutions)
- Large numbers of parameters: significant interest in reducing size of networks for both training and evaluation
- Many ongoing studies of specialized hardware architectures for efficient evaluation
  - Future CPUs/GPUs, ASICs, FPGS, ...
  - Specialization will be important to achieving "always on" applications