

Homework 12

1. Watch these videos

[ZK Proofs what are they_good for](#)

[Halo2 circuits](#)

[Performance and Security](#)

2. Arithmetic circuits

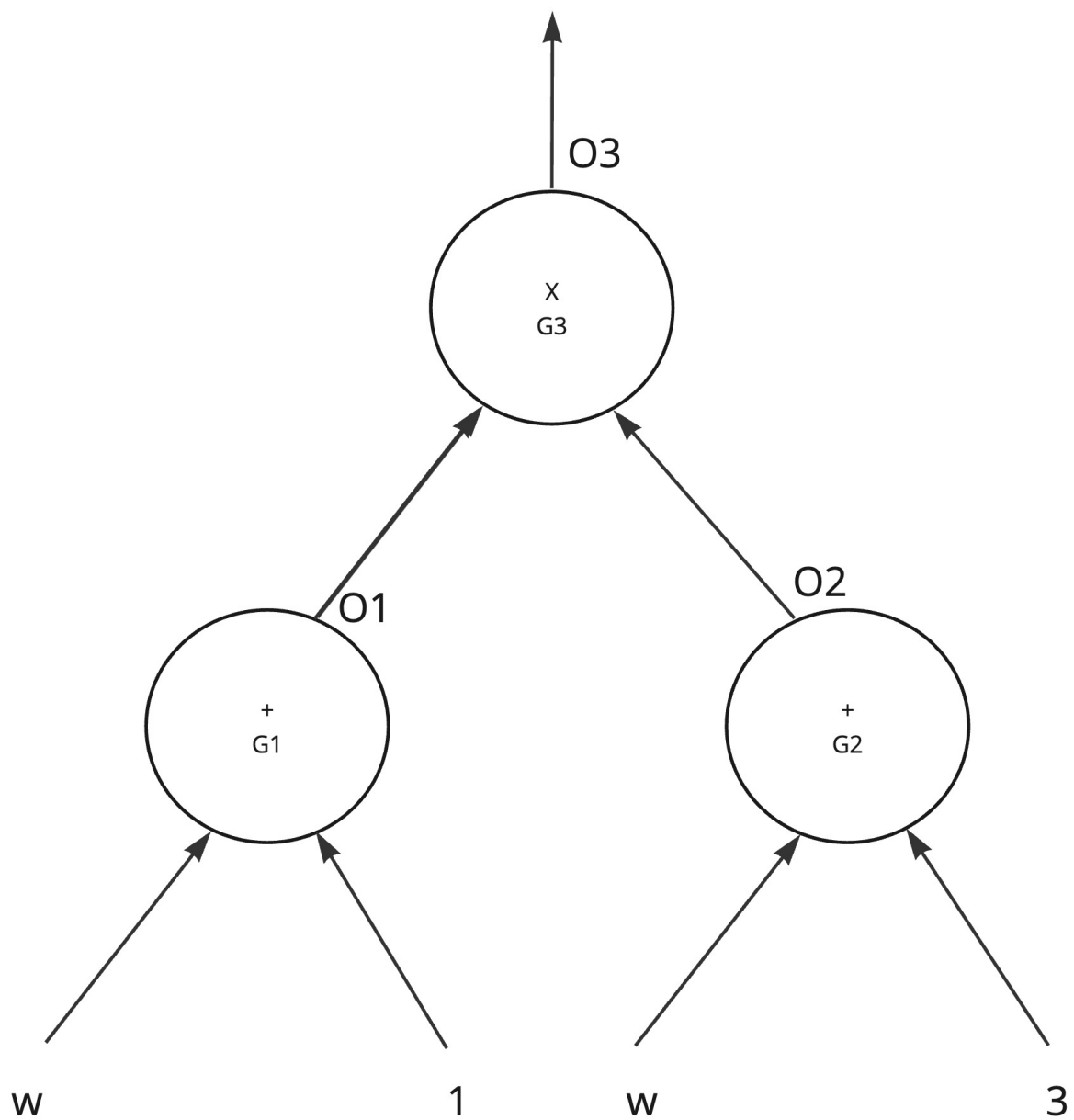
Example arithmetic circuit

Taking this example, we have 3 gates :

G1 an addition gate, with output O1

G2 an addition gate with output O2

G3 a multiplication gate with output O3



1. Thinking of the output O3, what polynomial does this represent (our variable is w)
2. If the output O3 is required to be 24, can you find a satisfying value of w
3. For each gate write out a constraint in terms of the inputs and outputs
4. Can you add selectors $S1, S2, S3$ for the constraints you have written

See page 3

$$1- (w+1) * (w+3) = 03$$

$$2- w^2 + 4w + 3 = 24$$

$$w^2 + 4w - 21 = 0$$

21 is divisible by

$$1 \quad -1$$

$$3 \quad -3$$

$$7 \quad -7$$

$$\begin{array}{r|rrr} & 1 & 4 & -21 \\ 3 & & 3 & 21 \\ \hline & 1 & 7 & 0 \end{array}$$

$$\boxed{x=3}$$

$$3- G1$$

$$= w+1 = 01$$

$$G2$$

$$= w+3 = 02$$

$$G3 = G1 \cdot G2 = 03$$

$$= (w+1) \cdot (w+3) = 03$$

$$4- G1$$

$$s_1(a_1 + b_1) - c_1 = 0$$

$$G2$$

$$s_2(a_2 + b_2) - c_2 = 0$$

$$s_1(w+1) - 01 = 0$$

$$s_2(w+3) - 02 = 0$$

$$G3$$

$$(1-s_3) \cdot G1 \cdot G2 - 03 = 0$$

$$(1-s_3) \cdot (s_1(a_1 + b_1) - c_1) \cdot (s_2(a_2 + b_2) - c_2) - c_3 = 0$$