

IEEE Working Group P3109 Interim Report on 8-bit Binary Floating-point Formats

Questions and comments via GitHub issues at
<https://github.com/P3109/Public>

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1 Introduction

This document represents ongoing discussions and current matters of consensus from IEEE Working Group P3109, “Standard for Arithmetic Formats for Machine Learning”. The Project Authorization Request (PAR) for P3109 defines the scope, need, and stakeholders as follows:

Scope of proposed standard: This standard defines a binary arithmetic and data format for machine learning-optimized domains. It also specifies the default handling of exceptions that occur in this arithmetic. This standard provides a consistent and flexible arithmetic framework optimized for Machine Learning Systems (MLS) in hardware and/or software implementations to minimize the work required to make MLS interoperable with each other, as well as other dependent systems. This standard is aligned with IEEE Std 754-2019 for Floating-Point Arithmetic.

Need for this Work: Machine Learning Systems have different arithmetic requirements from most other domains. Precisions tend to be lower, and accuracy is measured in dimensions other than just numerical (e.g. inference accuracy). Furthermore, machine learning systems are often integrated into mission-critical and safety-critical systems. With no standards specifically addressing these needs, Machine Learning Systems are built with inconsistent expectations and assumptions that hinder the compatibility and reuse of machine learning hardware, software, and training data.

Stakeholders for the Standard: System developers, vendors, and users of machine learning applications across many industries and interests including but not limited to computation, storage, medical, telecommunications, e-commerce, fleet management, automotive, robotics, and security.

The scope of this interim release is interchange formats only. The working group continues to deliberate on the specification of operations.

1.1 Typographical conventions and notation

Bold text describes the decisions and specifications of this document.

Text that is not bold is background material, typically providing rationale and arguments that represent discussions of the working group leading to a decision and specification.

This document specifies 8-bit floating-point interchange formats (binary formats) and associated operations. Binary formats are parameterized by their width, the number of bits spanned in memory (here, 8); and their precision (p), the number of bits spanned by the true significand (this is one more than the bits of the significand that are stored explicitly).

The formats defined herein shall be referred to as “binary8” formats, and further qualified by precision yielding names “binary8 pp ”.

For example, “binary8p3” is a format with 3 bits of precision (one implied – “the hidden bit” – and two explicit),

2 Values

This section describes the set of values that a binary8 format shall represent. The universe of values in existing floating point usage encompasses some finite real numerical values, the non-finite numerical values positive and negative infinity ($-\text{Inf}$, $+\text{Inf}$), the non-numeric not-a-number values (NaN, NaN_1, \dots), and negative zero (-0.0). The value set for each binary8 format specifies the set of values that are available in that format.

Each binary format shall be associated with a unique encoding. An 8-bit binary encoding is a mapping from 8-bit strings to values. Some of these mappings are included in Appendix C.

Values are considered either “special” or “ordinary”. The special values are Zero, $\pm\text{Inf}$, NaN. The ordinary values consist of the normal and subnormal values. The special values have encodings that are shared by all binary8 formats:

Special Value	Hexadecimal Encoding	Bit Sequence
Zero	0x00	0000 0000
Positive Infinity ($+\text{Inf}$)	0x7F	0111 1111
Negative Infinity ($-\text{Inf}$)	0xFF	1111 1111
Not a Number (NaN)	0x80	1000 0000

Table 1: Special Value Encodings

These mappings are shared by all binary8 formats.

Parameter	binary8p{p}	binary8p5	binary8p4	binary8p3	binary16	binary32	binary64
Storage width in bits k	8	8	8	8	16	32	64
Precision in bits p	p	5	4	3	11	24	53
Max exponent e_{max}	$\lceil 2^{8-p-1} - 1 \rceil$	3	7	15	15	127	1023
Sign bit	1	1	1	1	1	1	1
Exponent field width w	$8 - p$	3	4	5	5	8	11
Exponent bias, bias	$e_{\text{max}} + (p > 1)$	4	8	16	15	127	1023
Trailing significand field width in bits t	$p - 1$	4	3	2	10	23	52

Table 2: Parameters for binary formats

Format-defining parameters in bold, derived parameters in normal font.

Adapted from Table 3.5 of IEEE Std 754-2019, and extended to include the binary8pp formats. Concepts are explained in detail in this section.

The finite floating-point numbers representable with a binary format is determined by two *format-defining* parameters:

- Precision p , the number of digits in the significand including the implicit leading bit.
- Maximum exponent e_{max} , the exponent of the largest finite value.

IEEE Std 754-2019 includes the radix b and the minimum exponent e_{min} in a list of format-defining parameters, this document excludes both of them for these two reasons:

- This document covers binary (radix 2) formats only, so b is not a format parameter.

- The quantity $emin$ is determined by p and $emax$; it cannot be varied independently, and so cannot be a format-defining parameter.

P3109 formats shall define $emax(p)$ to be $\lceil 2^{8-p-1} - 1 \rceil$. In IEEE-754, $emax$ was set for all defined formats to be $2^{w-1} - 1$, where w is the exponent field width in bits. In this report, this convention is formalized: $emax$ is a fixed function of p , written $emax(p)$, with the formula as given above.

This choice of formula yields the following properties:

- the binary8pp value sets are subsets of the IEEE-754 binary16 value set for $p > 2$
- values are distributed close to symmetrically below and above the value 1.

For $p = 8$, the IEEE-754 formula yields $emax = -\frac{1}{2}$, meaning all non-special values are irrational. Rounding the computation upward yields $emax(8) = 0$, with the consequence that the value sets and encodings for binary8p7 and binary8p8 are identical.

The choice of $emax$ for a given format then determines the exponent bias for that format. The bias is chosen so that the exponent of the largest finite value is $emax$. For IEEE-754 formats, the largest finite value corresponds to an exponent field which has all but the zeroth bit set (e.g. 11110 for binary16), because all of the values with all-bits-one exponents (ABOE values) are occupied by non-finite values (Not-a-Numbers or Infinities). Thus, the biased exponent of the largest finite value is $2^w - 2$, from which bias is computed as

$$emax = (2^w - 2) - bias \implies bias = (2^w - 2) - (2^{w-1} - 1) = 2^{w-1} - 2 + 1 = emax$$

For the binary8 formats in this document where $p > 1$, only one of the ABOE values is non-finite ($\pm Infinity$), so the biased exponent of the largest finite value is $2^w - 1$. Hence the bias calculation becomes

$$bias = (2^w - 1) - (2^{w-1} - 1) = 2^{w-1} - 1 + 1 = emax + 1$$

For $p = 1$, there are zero trailing significand bits, so all ABOE values are special, and again $bias = emax$.

2.1 Subnormals

Binary8 value sets shall include subnormals.

IEEE-754 value sets include subnormals. A value with trailing significand field m and exponent e is interpreted as $1.m \times 2^{e-b}$ except when all bits of the exponent bitfield are 0, in which case the value is $0.m \times 2^{e-b}$.

When training models, it is common to represent near-zero values for gradients. Subnormal numbers induce equal quantization steps around zero; this expands the reach of binary8 trainable models. In statistical applications, the subnormal range is useful for uniform and similar distributions; subnormals are uniformly spaced around zero. They also support working with Gaussian-like distributions, where numbers around zero are more probable.

2.2 Not a number (NaN)

Binary8 value sets shall include exactly one NaN, which shall not signal.

Other floating-point formats define several NaN values, denoted (NaN, NaN₁, ...). NaNs are returned from operations with results outside the set of values. For example, DIV(0, 0), or ADD(Inf, -Inf). Multiple NaN encodings are used in other formats to allow different exceptional conditions to be distinguished.

In the context of machine learning systems, uses of NaN include:

- Debugging of code running on accelerator hardware. In AI accelerators, exceptions may be difficult or expensive to convey back to user code, so it is common practice to allow NaN values to propagate through calculations to indicate that an error has occurred.
- Use as a 'notable value' indicator. In some datasets, for example, tabular data, values may be missing. It is useful to use a value outside the normal numeric range to indicate the position of these values. Particularly when memory usage is a concern, as may be expected in applications where 8-bit formats are being considered, the use of a separate "mask" array, or a list of indices, imposes additional memory overhead. In some cases, Inf can be used as a missing value, but given the restricted range of binary8 formats, it is likely that infinity shall be used as a separate indicator of rounding from values outside of the finite range.
- The use of multiple NaN payloads is known in statistical code (e.g. the R system has NaN and N/A), but it is not widely used, and in the context of binary8, multiple NaNs impose either additional hardware complexity (using only a subset of the significand range), or a large reduction in encoding space (e.g. 8 codes for E5, 16 codes for E4, 32 codes for E3).

2.3 Zero

Binary8 formats shall have exactly one zero. This zero value is nonnegative.

The inclusion of negative zero would incur the cost of an additional code point. Given the decision to encode only a single NaN, placing that NaN at the negative zero code point enables the strictly positive and strictly negative number ranges to be symmetric.

A key rationale for including -0 in IEEE-754 was the consistent implementation of branch cuts in the atan2 function [4, 5]. Although the atan function is common in deep learning, it is generally used as an activation function, rather than a trigonometric operation, and the atan2 function is rare, if not unknown, in deep learning applications. Furthermore, it is not expected that this standard shall define either atan or atan2 .

A secondary reason for providing -0 is the hardware simplification offered by its presence in the implementation of sign/magnitude arithmetic. However, the existence of in-market implementations is evidence that the small hardware simplification has not been sufficient to balance the loss of one code point.

It might be considered that the use of integer comparisons in sorting would argue against placing NaN at the negative zero code point. For example, the JAX machine learning framework is known to sort using integer comparison [3]. However, such sorting still requires $O(n)$ preprocessing and postprocessing steps to enable the use of twos-complement integer comparison, and already has special treatment of NaN and -0 , so eliminating -0 and placing NaN in the -0 position imposes negligible additional burden. Sorting using comparison operations, as typically implemented, is undefined in the presence of NaNs. However, existing practice is to sort NaNs using `totalOrder`.

2.4 Infinities

Binary8 formats shall include positive and negative infinities.

This decision causes a reduction in dynamic range (252 values rather than 254), while offering improved numerical robustness in important machine learning use cases.

Two generic classes of such usage are:

- Mask values, for example, in Transformer models in machine learning [1].

- Representation of overflow.

As illustrated in Appendix A, both usages are facilitated by the presence of infinity.

2.5 Extremal Values

Format	minSubnormal	maxSubnormal	minNormal	maxNormal	maxFinite
binary8p2	1×2^{-32}	1×2^{-32}	1×2^{-31}	1×2^{31}	1×2^{31}
binary8p3	1×2^{-17}	$3/2 \times 2^{-16}$	1×2^{-15}	$3/2 \times 2^{15}$	$3/2 \times 2^{15}$
binary8p4	1×2^{-10}	$7/4 \times 2^{-8}$	1×2^{-7}	$7/4 \times 2^7$	$7/4 \times 2^7$
binary8p5	1×2^{-7}	$15/8 \times 2^{-4}$	1×2^{-3}	$15/8 \times 2^3$	$15/8 \times 2^3$
binary8p6	1×2^{-6}	$31/16 \times 2^{-2}$	1×2^{-1}	$31/16 \times 2^1$	$31/16 \times 2^1$
binary8p7	1×2^{-6}	$63/32 \times 2^{-1}$	1×2^0	$63/32 \times 2^0$	$63/32 \times 2^0$

Table 3: Extremal values

It is practical to offer extremal finite values for supported 8-bit binary interchange formats. Following IEEE 754-2019 naming patterns, we adopt: $\text{maxNormal}(T)$, $\text{minNormal}(T)$, $\text{minSubnormal}(T)$ where T is a binary8 format. For example: $\text{maxNormal}(\text{binary8p4}) = 7/4 \times 2^7$, $\text{minNormal}(\text{binary8p5}) = 1 \times 2^{-3}$.

Table 3 shows these values in binary8 formats for $1 < p < 8$.

3 Classification operators

Conforming implementations shall provide these classification predicates and the classifier function. The classification predicates and the classifier function shall not signal exceptions.

The classification operators comprise: 1) a set of functions with a boolean return value, taking a single binary8 value as input; 2) a function `class(x)` that returns a single value of enumeration type, describing the input value's properties.

Predicates shall behave as follows:

Predicate	Definition
<code>isZero</code>	iff ^a x is 0
<code>isNaN</code>	iff x is NaN
<code>isInfinite</code>	iff x is infinite
<code>isFinite</code>	iff x is zero, subnormal or normal
<code>isNormal</code>	iff x is normal, hence finite
<code>isSubnormal</code>	iff x is subnormal
<code>isSignMinus</code>	iff x has a negative sign ^b
<code>isCanonical</code>	True ^c
<code>isSignaling</code>	False ^d

^aiff abbreviates "if and only if"

^b`isSignMinus(NaN)` is True: NaN is 0x80 (0b10000000).

^cThere are no non-canonical binary8 interchange formats.

^dAll binary8 formats have one NaN; it does not signal.

Table 4: Classification Predicates

3.1 Classifications

The Classifier function `class(x)` shall return enumeration values as follows:

Enumeration	Condition
<code>NaN</code>	<code>isNaN(x)</code>
<code>Zero</code>	<code>isZero(x)</code>
<code>positiveInfinity</code>	<code>isInfinite(x)</code> and not(<code>isSignMinus(x)</code>)
<code>positiveNormal</code>	<code>isNormal(x)</code> and not(<code>isSignMinus(x)</code>)
<code>positiveSubnormal</code>	<code>isSubnormal(x)</code> and not(<code>isSignMinus(x)</code>)
<code>negativeInfinity</code>	<code>isInfinite(x)</code> and <code>isSignMinus(x)</code>
<code>negativeNormal</code>	<code>isNormal(x)</code> and <code>isSignMinus(x)</code>
<code>negativeSubnormal</code>	<code>isSubnormal(x)</code> and <code>isSignMinus(x)</code>

Table 5: Classifier Logic

4 Comparison operators

Conforming implementations shall provide the following comparison operators and the `totalOrder(x, y)` function.

Comparison operators are two argument predicates and their negations that return True or False. Comparisons shall not raise exceptions. Comparisons may be ordered or unordered. A comparison is unordered iff either argument is NaN. All other comparisons are ordered.

For $\{=, >, \geq, <, \leq, \leqslant\}$, if any argument is NaN, the result is False.

For $\{\neq, \not>, \not\geq, \not<, \not\leq, \not\leqslant\}$, if any argument is NaN, the result is True.

Otherwise, the result of a comparison shall match the mathematical result.

math symbol	predicate <i>true relations</i>	math symbol	negation <i>true relations</i>
=	CompareEqual <i>equal</i>	\neq , NOT =	CompareNotEqual <i>less than, greater than, unordered</i>
>	CompareGreater <i>greater than</i>	$\not>$, NOT >	CompareNotGreater <i>less than, equal, unordered</i>
\geq	CompareGreaterEqual <i>equal, greater than</i>	$\not\geq$, NOT \geq	CompareLessUnordered <i>less than, unordered</i>
<	CompareLess <i>less than</i>	$\not<$, NOT <	CompareNotLess <i>greater than, equal, unordered</i>
\leq	CompareLessEqual <i>less than, equal</i>	$\not\leq$, NOT \leq	CompareGreaterUnordered <i>greater than, unordered</i>
\leqslant	CompareOrdered <i>less than, equal, greater than</i>	$\not\leqslant$, NOT \leqslant	CompareUnordered <i>unordered</i>

Table 6: Comparison Predicates and Negations

4.1 The totalOrder predicate

`totalOrder(x, y)` provides a total ordering over each binary8 format's value set.

The predicate `totalOrder(x, y)` shall return { True, False } in accord with the logic given below. It shall not raise any exceptions.

```
boolean totalOrder(x, y)
    if isNaN(x): return True
    if isNaN(y): return False
    return compareLessEqual(x, y)
end
```

Note: Following 754's definition of `totalOrder(x, y)`, binary8 NaNs (0x80) compare as the most negative value. The most significant bit of NaN is set, so to be consistent with 754, NaN is ordered before all numerical values.

A Numerical Examples

A.1 Mask Values

A common use for ∞ is to create masks, for example, in Transformer models in machine learning, [1].

These values, assembled in mask matrix M with values $M_{ij} \in \{0, -\infty\}$ are typically added to computed values A , in a computation such as:

$$\log(\text{sum}(\exp(\tau * (A + M))))$$

where τ is a “temperature” or “base” parameter [2]. This calculation depends on the property $\exp(\tau * (A_{ij} - \infty)) = 0$.

If a floating point encoding does not provide infinity, then instead M_{ij} will be replaced by a large float (e.g. 480). This is not in itself a difficulty: if all the A values are bounded (e.g. the results of a softmax operation), then $\exp?(1.0 - 480)$ is an extremely small number, which will certainly round to zero. Therefore, an explicit representation of infinity is *not* needed in order for this computation to yield its desired value.

However, careful implementations do not execute the calculation as written, and instead fuse the $\log(\text{sum}(\exp(v)))$ operation into a single operation $\text{logsumexp}(v)$, whose implementation makes use of the identity transformation

$$\text{logsumexp}(v) \rightarrow \text{logsumexp}(v - \max(v)) + \max(v)$$

Without the “sticky” properties of Inf, this would produce incorrect answers. For example, in a format where $\text{MaxFloat}=240$ without Inf, and $\text{MaxFloat}=224$ with Inf:

$$\text{logsumexp}(\tau * [-224, -\infty]) \rightarrow \text{logsumexp}(\tau * [0, -\infty])$$

while

$$\text{logsumexp}(\tau * [-224, -240]) \rightarrow \text{logsumexp}(\tau * [0, -16])$$

If $\tau = 1$ and all calculations are done in 8-bit floating point, then the answer will be the same, because $\exp(-16) \approx 1.1 \times 10^{-7}$, which will round to zero in all precisions $p > 2$; but if τ is small, or calculations are done in mixed precision, as is common with 8-bit floating point, the loss of “stickiness” will silently yield unexpected answers. It is not expected that the full calculation shall be done in 8-bit floating point, but the subtraction of the maximum value (and computation of the maximum) might reasonably be in 8-bit floating point.

A.2 Overflow to Infinity

A second use of infinity is to indicate overflow on conversion to the `binary8` type. Existing implementations offer several behaviors on overflow: overflow to infinity, saturation to `MaxFloat`, and overflow to NaN. The existence of a code point for infinity allows any of these options to be implemented in a given instantiation, while removing the code point removes the possibility of implementing the first.

B External Formats

This table summarizes the points of difference and agreement between the formats proposed in this document and a number of existing formats, some of which have hardware implementations.

OCP: Open Compute Platform [6], describing hardware implementations including nVidia, Intel, and ARM.

AGQ: AMD, Graphcore, Qualcomm[7], implemented in Graphcore’s C600 product, and AMD’s gfx940.

TSL: Tesla Dojo Technology [8], A Guide to Tesla’s Configurable Floating Point Formats & Arithmetic

Format	P3109			OCP		AGQ		TSL	
Subformat	P3	P4	P5	E5	E4	E5	E4	E4	E5
Special values shared by all subformats	Y			N		Y		N	
Exactly one NaN	Y			N		Y		Y	
Positive and negative infinity	Y			N	Y	N		N	
Include negative zero	N			N		Y		N	
Max exponent emax	15	7	3	15	8	15	7	N/A	N/A

C Value Tables

Value tables mapping 8-bit strings to value sets are provided in this section.

A typical entry is of the form:

HEX BINARY = BINARY_FLOAT = DECIMAL
 0x01 = 0_00000_01 = +0b0.01 x 2⁻¹⁵ = 7.62939453125E-06

Where the fields are interpreted as follows:

HEX Hexadecimal encoding of the code point
 BINARY Binary expansion of the code point, underscores separate `sign` `exponent` `significand`
 BINARY_FLOAT The precise float value as a binary fraction followed by 2^e with decimal exponent e
 DECIMAL A decimal expansion of the value. If the expansion is not an exact representation of the precise float value, the equals sign is replaced by “approximately equals” ≈.

C.1 Value Table: P2, $p = 2$, $\text{emax} = 31$

0x00 = 0.000000.0 = 0.0	0x40 = 0.100000.0 = +0b1.0×2 ⁰ = 1.0	0x80 = 1.000000.0 = NaN	0xc0 = 1.100000.0 = -0b1.0×2 ⁰ = -1.0
0x01 = 0.000000.1 = +0b0.1×2 ⁻³¹ ≈ 2.3283064E-10	0x41 = 0.100000.1 = +0b1.1×2 ⁰ = 1.5	0x81 = 1.000000.1 = -0b0.1×2 ⁻³¹ ≈ -2.3283064E-10	0xc1 = 1.100000.1 = -0b1.1×2 ⁰ = -1.5
0x02 = 0.000001.0 = +0b1.0×2 ⁻³¹ ≈ 4.6566129E-10	0x42 = 0.100001.0 = +0b1.0×2 ¹ = 2.0	0x82 = 1.000001.0 = -0b1.0×2 ⁻³¹ ≈ -4.6566129E-10	0xc2 = 1.100001.0 = -0b1.0×2 ¹ = -2.0
0x03 = 0.000001.1 = +0b1.1×2 ⁻³¹ ≈ 6.9849193E-10	0x43 = 0.100001.1 = +0b1.1×2 ¹ = 3.0	0x83 = 1.000001.1 = -0b1.1×2 ⁻³¹ ≈ -6.9849193E-10	0xc3 = 1.100001.1 = -0b1.1×2 ¹ = -3.0
0x04 = 0.000010.0 = +0b1.0×2 ⁻³⁰ ≈ 9.3132257E-10	0x44 = 0.100010.0 = +0b1.0×2 ² = 4.0	0x84 = 1.000010.0 = -0b1.0×2 ⁻³⁰ ≈ -9.3132257E-10	0xc4 = 1.100010.0 = -0b1.0×2 ² = -4.0
0x05 = 0.000010.1 = +0b1.1×2 ⁻³⁰ ≈ 1.3969839E-09	0x45 = 0.100010.1 = +0b1.1×2 ² = 6.0	0x85 = 1.000010.1 = -0b1.1×2 ⁻³⁰ ≈ -1.3969839E-09	0xc5 = 1.100010.1 = -0b1.1×2 ² = -6.0
0x06 = 0.000011.0 = +0b1.0×2 ⁻²⁹ ≈ 1.8626451E-09	0x46 = 0.100011.0 = +0b1.0×2 ³ = 8.0	0x86 = 1.000011.0 = -0b1.0×2 ⁻²⁹ ≈ -1.8626451E-09	0xc6 = 1.100011.0 = -0b1.0×2 ³ = -8.0
0x07 = 0.000011.1 = +0b1.1×2 ⁻²⁹ ≈ 2.7939677E-09	0x47 = 0.100011.1 = +0b1.1×2 ³ = 12.0	0x87 = 1.000011.1 = -0b1.1×2 ⁻²⁹ ≈ -2.7939677E-09	0xc7 = 1.100011.1 = -0b1.1×2 ³ = -12.0
0x08 = 0.000010.1 = +0b1.0×2 ⁻²⁸ ≈ 3.7252903E-09	0x48 = 0.100100.0 = +0b1.0×2 ⁴ = 16.0	0x88 = 1.000100.0 = -0b1.0×2 ⁻²⁸ ≈ -3.7252903E-09	0xc8 = 1.100100.0 = -0b1.0×2 ⁴ = -16.0
0x09 = 0.000100.1 = +0b1.1×2 ⁻²⁸ ≈ 5.5879354E-09	0x49 = 0.100100.1 = +0b1.1×2 ⁴ = 24.0	0x89 = 1.000100.1 = -0b1.1×2 ⁻²⁸ ≈ -5.5879354E-09	0xc9 = 1.100100.1 = -0b1.1×2 ⁴ = -24.0
0x0a = 0.000101.0 = +0b1.0×2 ⁻²⁷ ≈ 7.4505806E-09	0x4a = 0.100101.0 = +0b1.0×2 ⁵ = 32.0	0x8a = 1.000101.0 = -0b1.0×2 ⁻²⁷ ≈ -7.4505806E-09	0xca = 1.100101.0 = -0b1.0×2 ⁵ = -32.0
0x0b = 0.000101.1 = +0b1.1×2 ⁻²⁷ ≈ 1.1175871E-08	0x4b = 0.100101.1 = +0b1.1×2 ⁵ = 48.0	0x8b = 1.000101.1 = -0b1.1×2 ⁻²⁷ ≈ -1.1175871E-08	0xcb = 1.100101.1 = -0b1.1×2 ⁵ = -48.0
0x0c = 0.000110.0 = +0b1.0×2 ⁻²⁶ ≈ 1.4901161E-08	0x4c = 0.100110.0 = +0b1.0×2 ⁶ = 64.0	0x8c = 1.000110.0 = -0b1.0×2 ⁻²⁶ ≈ -1.4901161E-08	0xcc = 1.100110.0 = -0b1.0×2 ⁶ = -64.0
0x0d = 0.000110.1 = +0b1.1×2 ⁻²⁶ ≈ 2.2351742E-08	0x4d = 0.100110.1 = +0b1.1×2 ⁶ = 96.0	0x8d = 1.000110.1 = -0b1.1×2 ⁻²⁶ ≈ -2.2351742E-08	0xcd = 1.100110.1 = -0b1.1×2 ⁶ = -96.0
0x0e = 0.000111.0 = +0b1.0×2 ⁻²⁵ ≈ 2.9802322E-08	0x4e = 0.100111.0 = +0b1.0×2 ⁷ = 128.0	0x8e = 1.000111.0 = -0b1.0×2 ⁻²⁵ ≈ -2.9802322E-08	0xce = 1.100111.0 = -0b1.0×2 ⁷ = -128.0
0x0f = 0.000111.1 = +0b1.1×2 ⁻²⁵ ≈ 4.4703484E-08	0x4f = 0.100111.1 = +0b1.1×2 ⁷ = 192.0	0x8f = 1.000111.1 = -0b1.1×2 ⁻²⁵ ≈ -4.4703484E-08	0xcf = 1.100111.1 = -0b1.1×2 ⁷ = -192.0
0x10 = 0.001000.0 = +0b1.0×2 ⁻²⁴ ≈ 5.9604645E-08	0x50 = 0.101000.0 = +0b1.0×2 ⁸ = 256.0	0x90 = 1.001000.0 = -0b1.0×2 ⁻²⁴ ≈ -5.9604645E-08	0xd0 = 1.101000.0 = -0b1.0×2 ⁸ = -256.0
0x11 = 0.001000.1 = +0b1.1×2 ⁻²⁴ ≈ 8.9406967E-08	0x51 = 0.101000.1 = +0b1.1×2 ⁸ = 384.0	0x91 = 1.001000.1 = -0b1.1×2 ⁻²⁴ ≈ -8.9406967E-08	0xd1 = 1.101000.1 = -0b1.1×2 ⁸ = -384.0
0x12 = 0.001001.0 = +0b1.0×2 ⁻²³ ≈ 1.1920929E-07	0x52 = 0.101001.0 = +0b1.0×2 ⁹ = 512.0	0x92 = 1.001001.0 = -0b1.0×2 ⁻²³ ≈ -1.1920929E-07	0xd2 = 1.101001.0 = -0b1.0×2 ⁹ = -512.0
0x13 = 0.001001.1 = +0b1.1×2 ⁻²³ ≈ 1.7881393E-07	0x53 = 0.101001.1 = +0b1.1×2 ⁹ = 768.0	0x93 = 1.001001.1 = -0b1.1×2 ⁻²³ ≈ -1.7881393E-07	0xd3 = 1.101001.1 = -0b1.1×2 ⁹ = -768.0
0x14 = 0.001010.0 = +0b1.0×2 ⁻²² ≈ 2.3841858E-07	0x54 = 0.101010.0 = +0b1.0×2 ¹⁰ = 1024.0	0x94 = 1.001010.0 = -0b1.0×2 ⁻²² ≈ -2.3841858E-07	0xd4 = 1.101010.0 = -0b1.0×2 ¹⁰ = -1024.0
0x15 = 0.001010.1 = +0b1.1×2 ⁻²² ≈ 3.5762787E-07	0x55 = 0.101010.1 = +0b1.1×2 ¹⁰ = 1536.0	0x95 = 1.001010.1 = -0b1.1×2 ⁻²² ≈ -3.5762787E-07	0xd5 = 1.101010.1 = -0b1.1×2 ¹⁰ = -1536.0
0x16 = 0.001011.0 = +0b1.0×2 ⁻²¹ ≈ 4.7683716E-07	0x56 = 0.101011.0 = +0b1.0×2 ¹¹ = 2048.0	0x96 = 1.001011.0 = -0b1.0×2 ⁻²¹ ≈ -4.7683716E-07	0xd6 = 1.101011.0 = -0b1.0×2 ¹¹ = -2048.0
0x17 = 0.001011.1 = +0b1.1×2 ⁻²¹ ≈ 7.1525574E-07	0x57 = 0.101011.1 = +0b1.1×2 ¹¹ = 3072.0	0x97 = 1.001011.1 = -0b1.1×2 ⁻²¹ ≈ -7.1525574E-07	0xd7 = 1.101011.1 = -0b1.1×2 ¹¹ = -3072.0
0x18 = 0.001100.0 = +0b1.0×2 ⁻²⁰ ≈ 9.5367432E-07	0x58 = 0.101100.0 = +0b1.0×2 ¹² = 4096.0	0x98 = 1.001100.0 = -0b1.0×2 ⁻²⁰ ≈ -9.5367432E-07	0xd8 = 1.101100.0 = -0b1.0×2 ¹² = -4096.0
0x19 = 0.001100.1 = +0b1.1×2 ⁻²⁰ ≈ 1.4305115E-06	0x59 = 0.101100.1 = +0b1.1×2 ¹² = 6144.0	0x99 = 1.001100.1 = -0b1.1×2 ⁻²⁰ ≈ -1.4305115E-06	0xd9 = 1.101100.1 = -0b1.1×2 ¹² = -6144.0
0x1a = 0.001101.0 = +0b1.0×2 ⁻¹⁹ ≈ 1.9073486E-06	0x5a = 0.101101.0 = +0b1.0×2 ¹³ = 8192.0	0x9a = 1.001101.0 = -0b1.0×2 ⁻¹⁹ ≈ -1.9073486E-06	0xda = 1.101101.0 = -0b1.0×2 ¹³ = -8192.0
0x1b = 0.001101.1 = +0b1.1×2 ⁻¹⁹ ≈ 2.8610229E-06	0x5b = 0.101101.1 = +0b1.1×2 ¹³ = 12288.0	0x9b = 1.001101.1 = -0b1.1×2 ⁻¹⁹ ≈ -2.8610229E-06	0xdb = 1.101101.1 = -0b1.1×2 ¹³ = -12288.0
0x1c = 0.001110.0 = +0b1.0×2 ⁻¹⁸ ≈ 3.8146973E-06	0x5c = 0.101110.0 = +0b1.0×2 ¹⁴ = 16384.0	0x9c = 1.001110.0 = -0b1.0×2 ⁻¹⁸ ≈ -3.8146973E-06	0xdc = 1.101110.0 = -0b1.0×2 ¹⁴ = -16384.0
0x1d = 0.001110.1 = +0b1.1×2 ⁻¹⁸ ≈ 5.7220459E-06	0x5d = 0.101110.1 = +0b1.1×2 ¹⁴ = 24576.0	0x9d = 1.001110.1 = -0b1.1×2 ⁻¹⁸ ≈ -5.7220459E-06	0xdd = 1.101110.1 = -0b1.1×2 ¹⁴ = -24576.0
0x1e = 0.001111.0 = +0b1.0×2 ⁻¹⁷ ≈ 7.6293945E-06	0x5e = 0.101111.0 = +0b1.0×2 ¹⁵ = 32768.0	0x9e = 1.001111.0 = -0b1.0×2 ⁻¹⁷ ≈ -7.6293945E-06	0xde = 1.101111.0 = -0b1.0×2 ¹⁵ = -32768.0
0x1f = 0.001111.1 = +0b1.1×2 ⁻¹⁷ ≈ 1.1444092E-05	0x5f = 0.101111.1 = +0b1.1×2 ¹⁵ = 49152.0	0x9f = 1.001111.1 = -0b1.1×2 ⁻¹⁷ ≈ -1.1444092E-05	0xdf = 1.101111.1 = -0b1.1×2 ¹⁵ = -49152.0
0x20 = 0.010000.0 = +0b1.0×2 ⁻¹⁶ ≈ 1.5258789E-05	0x60 = 0.110000.0 = +0b1.0×2 ¹⁶ = 65536.0	0xa0 = 1.010000.0 = -0b1.0×2 ⁻¹⁶ ≈ -1.5258789E-05	0xea0 = 1.110000.0 = -0b1.0×2 ¹⁶ = -65536.0
0x21 = 0.010000.1 = +0b1.1×2 ⁻¹⁶ ≈ 2.2888184E-05	0x61 = 0.110000.1 = +0b1.1×2 ¹⁶ = 98304.0	0xa1 = 1.010000.1 = -0b1.1×2 ⁻¹⁶ ≈ -2.2888184E-05	0xea1 = 1.110000.1 = -0b1.1×2 ¹⁶ = -98304.0
0x22 = 0.010001.0 = +0b1.0×2 ⁻¹⁵ ≈ 3.0517578E-05	0x62 = 0.110001.0 = +0b1.0×2 ¹⁷ = 131072.0	0xa2 = 1.010001.0 = -0b1.0×2 ⁻¹⁵ ≈ -3.0517578E-05	0xea2 = 1.110001.0 = -0b1.0×2 ¹⁷ = -131072.0
0x23 = 0.010001.1 = +0b1.1×2 ⁻¹⁵ ≈ 4.5776367E-05	0x63 = 0.110001.1 = +0b1.1×2 ¹⁷ = 196608.0	0xa3 = 1.010001.1 = -0b1.1×2 ⁻¹⁵ ≈ -4.5776367E-05	0xea3 = 1.110001.1 = -0b1.1×2 ¹⁷ = -196608.0
0x24 = 0.010010.0 = +0b1.0×2 ⁻¹⁴ ≈ 6.1035156E-05	0x64 = 0.110010.0 = +0b1.0×2 ¹⁸ = 262144.0	0xa4 = 1.010010.0 = -0b1.0×2 ⁻¹⁴ ≈ -6.1035156E-05	0xea4 = 1.110010.0 = -0b1.0×2 ¹⁸ = -262144.0
0x25 = 0.010010.1 = +0b1.1×2 ⁻¹⁴ ≈ 9.1552734E-05	0x65 = 0.110010.1 = +0b1.1×2 ¹⁸ = 393216.0	0xa5 = 1.010010.1 = -0b1.1×2 ⁻¹⁴ ≈ -9.1552734E-05	0xea5 = 1.110010.1 = -0b1.1×2 ¹⁸ = -393216.0
0x26 = 0.010011.0 = +0b1.0×2 ⁻¹³ ≈ 0.00012207031	0x66 = 0.110011.0 = +0b1.0×2 ¹⁹ = 524288.0	0xa6 = 1.010011.0 = -0b1.0×2 ⁻¹³ ≈ -0.00012207031	0xea6 = 1.110011.0 = -0b1.0×2 ¹⁹ = -524288.0
0x27 = 0.010011.1 = +0b1.1×2 ⁻¹³ ≈ 0.00018310547	0x67 = 0.110011.1 = +0b1.1×2 ¹⁹ = 786432.0	0xa7 = 1.010011.1 = -0b1.1×2 ⁻¹³ ≈ -0.00018310547	0xea7 = 1.110011.1 = -0b1.1×2 ¹⁹ = -786432.0
0x28 = 0.010100.0 = +0b1.0×2 ⁻¹² ≈ 0.000244140625	0x68 = 0.110100.0 = +0b1.0×2 ²⁰ = 1048576.0	0xa8 = 1.010100.0 = -0b1.0×2 ⁻¹² ≈ -0.000244140625	0xea8 = 1.110100.0 = -0b1.0×2 ²⁰ = -1048576.0
0x29 = 0.010100.1 = +0b1.1×2 ⁻¹² ≈ 0.00036621094	0x69 = 0.110100.1 = +0b1.1×2 ²⁰ = 1572864.0	0xa9 = 1.010100.1 = -0b1.1×2 ⁻¹² ≈ -0.00036621094	0xea9 = 1.110100.1 = -0b1.1×2 ²⁰ = -1572864.0
0x2a = 0.010101.0 = +0b1.0×2 ⁻¹¹ ≈ 0.00048828125	0x6a = 0.110101.0 = +0b1.0×2 ²¹ = 2097152.0	0xaa = 1.010101.0 = -0b1.0×2 ⁻¹¹ ≈ -0.00048828125	0xea = 1.110101.0 = -0b1.0×2 ²¹ = -2097152.0
0x2b = 0.010101.1 = +0b1.1×2 ⁻¹¹ ≈ 0.000732421875	0x6b = 0.110101.1 = +0b1.1×2 ²¹ = 3145728.0	0xab = 1.010101.1 = -0b1.1×2 ⁻¹¹ ≈ -0.000732421875	0xeb = 1.110101.1 = -0b1.1×2 ²¹ = -3145728.0
0x2c = 0.010110.0 = +0b1.0×2 ⁻¹⁰ ≈ 0.0009765625	0x6c = 0.110110.0 = +0b1.0×2 ²² = 4194304.0	0xac = 1.010110.0 = -0b1.0×2 ⁻¹⁰ ≈ -0.0009765625	0xec = 1.110110.0 = -0b1.0×2 ²² = -4194304.0
0x2d = 0.010110.1 = +0b1.1×2 ⁻¹⁰ ≈ 0.00146484375	0x6d = 0.110110.1 = +0b1.1×2 ²² = 6291456.0	0xad = 1.010110.1 = -0b1.1×2 ⁻¹⁰ ≈ -0.00146484375	0xed = 1.110110.1 = -0b1.1×2 ²² = -6291456.0
0x2e = 0.010111.0 = +0b1.0×2 ⁻⁹ ≈ 0.001953125	0x6e = 0.110111.0 = +0b1.0×2 ²³ = 8388608.0	0xae = 1.010111.0 = -0b1.0×2 ⁻⁹ ≈ -0.001953125	0xee = 1.110111.0 = -0b1.0×2 ²³ = -8388608.0
0x2f = 0.010111.1 = +0b1.1×2 ⁻⁹ ≈ 0.0029296875	0x6f = 0.110111.1 = +0b1.1×2 ²³ = 12582912.0	0xaf = 1.010111.1 = -0b1.1×2 ⁻⁹ ≈ -0.0029296875	0xef = 1.110111.1 = -0b1.1×2 ²³ = -12582912.0
0x30 = 0.011000.0 = +0b1.0×2 ⁻⁸ ≈ 0.00390625	0x70 = 0.111000.0 = +0b1.0×2 ²⁴ = 16777216.0	0xb0 = 1.011000.0 = -0b1.0×2 ⁻⁸ ≈ -0.00390625	0xf0 = 1.111000.0 = -0b1.0×2 ²⁴ = -16777216.0
0x31 = 0.011000.1 = +0b1.1×2 ⁻⁸ ≈ 0.005859375	0x71 = 0.111000.1 = +0b1.1×2 ²⁴ = 25165824.0	0xb1 = 1.011000.1 = -0b1.1×2 ⁻⁸ ≈ -0.005859375	0xf1 = 1.111000.1 = -0b1.1×2 ²⁴ = -25165824.0
0x32 = 0.011001.0 = +0b1.0×2 ⁻⁷ ≈ 0.0078125	0x72 = 0.111001.0 = +0b1.0×2 ²⁵ = 33554432.0	0xb2 = 1.011001.0 = -0b1.0×2 ⁻⁷ ≈ -0.0078125	0xf2 = 1.111001.0 = -0b1.0×2 ²⁵ = -33554432.0
0x33 = 0.011001.1 = +0b1.1×2 ⁻⁷ ≈ 0.01171875	0x73 = 0.111001.1 = +0b1.1×2 ²⁵ = 50331648.0	0xb3 = 1.011001.1 = -0b1.1×2 ⁻⁷ ≈ -0.01171875	0xf3 = 1.111001.1 = -0b1.1×2 ²⁵ = -50331648.0
0x34 = 0.011010.0 = +0b1.0×2 ⁻⁶ ≈ 0.015625	0x74 = 0.111010.0 = +0b1.0×2 ²⁶ = 67108864.0	0xb4 = 1.011010.0 = -0b1.0×2 ⁻⁶ ≈ -0.015625	0xf4 = 1.111010.0 = -0b1.0×2 ²⁶ = -67108864.0
0x35 = 0.011010.1 = +0b1.1×2 ⁻⁶ ≈ 0.0234375	0x75 = 0.111010.1 = +0b1.1×2 ²⁶ = 102466329.6	0xb5 = 1.011010.1 = -0b1.1×2 ⁻⁶ ≈ -0.0234375	0xf5 = 1.111010.1 = -0b1.1×2 ²⁶ = -102466329.6
0x36 = 0.011011.0 = +0b1.0×2 ⁻⁵ ≈ 0.03125	0x76 = 0.111011.0 = +0b1.0×2 ²⁷ = 134217728.0	0xb6 = 1.011011.0 = -0b1.0×2 ⁻⁵ ≈ -0.03125	0xf6 = 1.111011.0 = -0b1.0×2 ²⁷ = -134217728.0
0x37 = 0.011011.1 = +0b1.1×2 ⁻⁵ ≈ 0.046875	0x77 = 0.111011.1 = +0b1.1×2 ²⁷ = 201326592.0	0xb7 = 1.011011.1 = -0b1.1×2 ⁻⁵ ≈ -0.046875	0xf7 = 1.111011.1 = -0b1.1×2 ²⁷ = -201326592.0
0x38 = 0.011100.0 = +0b1.0×2 ⁻⁴ ≈ 0.0625	0x78 = 0.111100.0 = +0b1.0×2 ²⁸ = 268435456.0	0xb8 = 1.011100.0 = -0b1.0×2 ⁻⁴ ≈ -0.0625	0xf8 = 1.111100.0 = -0b1.0×2 ²⁸ = -268435456.0
0x39 = 0.011100.1 = +0b1.1×2 ⁻⁴ ≈ 0.09375	0x79 = 0.111100.1 = +0b1.1×2 ²⁸ = 402653184.0	0xb9 = 1.011100.1 = -0b1.1×2 ⁻⁴ ≈ -0.09375	0xf9 = 1.111100.1 = -0b1.1×2 ²⁸ = -402653184.0
0x3a = 0.011101.0 = +0b1.0×2 ⁻³ ≈ 0.125	0x7a = 0.111101.0 = +0b1.0×2 ²⁹ = 536870912.0	0xba = 1.011101.0 = -0b1.0×2 ⁻³ ≈ -0.125	0xfa = 1.111101.0 = -0b1.0×2 ²⁹ = -536870912.0
0x3b = 0.011101.1 = +0b1.1×2 ⁻³ ≈ 0.1875	0x7b = 0.111101.1 = +0b1.1×2 ²⁹ = 805306368.0	0xbb = 1.011101.1 = -0b1.1×2 ⁻³ ≈ -0.1875	0xfb = 1.111101.1 = -0b1.1×2 ²⁹ = -805306368.0
0x3c = 0.011110.0 = +0b1.0×2 ⁻² ≈ 0.25	0x7c = 0.111110.0 = +0b1.0×2 ³⁰ = 1073741824.0	0xbc = 1.011110.0 = -0b1.0×2 ⁻² ≈ -0.25	0xfc = 1.111110.0 = -0b1.0×2 ³⁰ = -1073741824.0
0x3d = 0.011110.1 = +0b1.1×2 ⁻² ≈ 0.375	0x7d = 0.111110.1 = +0b1.1×2 ³⁰ = 1610612736.0	0xbd = 1.011110.1 = -0b1.1×2 ⁻² ≈ -0.375	0xfd = 1.111110.1 = -0b1.1×2 ³⁰ = -1610612736.0
0x3e = 0.011111.0 = +0b1.0×2 ⁻¹ ≈ 0			

C.2 Value Table: P3, $p = 3$, $\text{emax} = 15$

0x00 = 0.00000.00 = 0.0	0x40 = 0.10000.00 = +0b1.00×2 ⁰ = 1.0	0x80 = 1.00000.00 = NaN	0xc0 = 1.10000.00 = -0b1.00×2 ⁰ = -1.0
0x01 = 0.00000.01 = +0b0.01×2 ⁻¹⁵ ≈ 7.6293945E-06	0x41 = 0.10000.01 = +0b1.01×2 ⁰ = 1.25	0x81 = 1.00000.01 = -0b0.01×2 ⁻¹⁵ ≈ -7.6293945E-06	0xc1 = 1.10000.01 = -0b1.01×2 ⁰ = -1.25
0x02 = 0.00000.10 = +0b0.10×2 ⁻¹⁵ ≈ 1.5258789E-05	0x42 = 0.10000.10 = +0b1.10×2 ⁰ = 1.5	0x82 = 1.00000.10 = -0b0.10×2 ⁻¹⁵ ≈ -1.5258789E-05	0xc2 = 1.10000.10 = -0b1.10×2 ⁰ = -1.5
0x03 = 0.00000.11 = +0b0.11×2 ⁻¹⁵ ≈ 2.2888184E-05	0x43 = 0.10000.11 = +0b1.11×2 ⁰ = 1.75	0x83 = 1.00000.11 = -0b0.11×2 ⁻¹⁵ ≈ -2.2888184E-05	0xc3 = 1.10000.11 = -0b1.11×2 ⁰ = -1.75
0x04 = 0.00001.00 = +0b1.00×2 ⁻¹⁵ ≈ 3.0517578E-05	0x44 = 0.10001.00 = +0b1.00×2 ¹ = 2.0	0x84 = 1.00001.00 = -0b1.00×2 ⁻¹⁵ ≈ -3.0517578E-05	0xc4 = 1.10001.00 = -0b1.00×2 ¹ = -2.0
0x05 = 0.00001.01 = +0b1.01×2 ⁻¹⁵ ≈ 3.8146973E-05	0x45 = 0.10001.01 = +0b1.01×2 ¹ = 2.5	0x85 = 1.00001.01 = -0b1.01×2 ⁻¹⁵ ≈ -3.8146973E-05	0xc5 = 1.10001.01 = -0b1.01×2 ¹ = -2.5
0x06 = 0.00001.10 = +0b1.10×2 ⁻¹⁵ ≈ 4.5776367E-05	0x46 = 0.10001.10 = +0b1.10×2 ¹ = 3.0	0x86 = 1.00001.10 = -0b1.10×2 ⁻¹⁵ ≈ -4.5776367E-05	0xc6 = 1.10001.10 = -0b1.10×2 ¹ = -3.0
0x07 = 0.00001.11 = +0b1.11×2 ⁻¹⁵ ≈ 5.3405762E-05	0x47 = 0.10001.11 = +0b1.11×2 ¹ = 3.5	0x87 = 1.00001.11 = -0b1.11×2 ⁻¹⁵ ≈ -5.3405762E-05	0xc7 = 1.10001.11 = -0b1.11×2 ¹ = -3.5
0x08 = 0.00010.00 = +0b1.00×2 ⁻¹⁴ ≈ 6.1035156E-05	0x48 = 0.10010.00 = +0b1.00×2 ² = 4.0	0x88 = 1.00010.00 = -0b1.00×2 ⁻¹⁴ ≈ -6.1035156E-05	0xc8 = 1.10010.00 = -0b1.00×2 ² = -4.0
0x09 = 0.00010.01 = +0b1.01×2 ⁻¹⁴ ≈ 7.6293945E-05	0x49 = 0.10010.01 = +0b1.01×2 ² = 5.0	0x89 = 1.00010.01 = -0b1.01×2 ⁻¹⁴ ≈ -7.6293945E-05	0xc9 = 1.10010.01 = -0b1.01×2 ² = -5.0
0x0a = 0.00010.10 = +0b1.10×2 ⁻¹⁴ ≈ 9.1552734E-05	0x4a = 0.10010.10 = +0b1.10×2 ² = 6.0	0x8a = 1.00010.10 = -0b1.10×2 ⁻¹⁴ ≈ -9.1552734E-05	0xca = 1.10010.10 = -0b1.10×2 ² = -6.0
0x0b = 0.00010.11 = +0b1.11×2 ⁻¹⁴ ≈ 0.00010681152	0x4b = 0.10010.11 = +0b1.11×2 ² = 7.0	0x8b = 1.00010.11 = -0b1.11×2 ⁻¹⁴ ≈ -0.00010681152	0xcb = 1.10010.11 = -0b1.11×2 ² = -7.0
0x0c = 0.00011.00 = +0b1.00×2 ⁻¹³ ≈ 0.00012207031	0x4c = 0.10011.00 = +0b1.00×2 ³ = 8.0	0x8c = 1.00011.00 = -0b1.00×2 ⁻¹³ ≈ -0.00012207031	0xcc = 1.10011.00 = -0b1.00×2 ³ = -8.0
0x0d = 0.00011.01 = +0b1.01×2 ⁻¹³ ≈ 0.00015258789	0x4d = 0.10011.01 = +0b1.01×2 ³ = 10.0	0x8d = 1.00011.01 = -0b1.01×2 ⁻¹³ ≈ -0.00015258789	0xcd = 1.10011.01 = -0b1.01×2 ³ = -10.0
0x0e = 0.00011.10 = +0b1.10×2 ⁻¹³ ≈ 0.00018310547	0x4e = 0.10011.10 = +0b1.10×2 ³ = 12.0	0x8e = 1.00011.10 = -0b1.10×2 ⁻¹³ ≈ -0.00018310547	0xce = 1.10011.10 = -0b1.10×2 ³ = -12.0
0x0f = 0.00011.11 = +0b1.11×2 ⁻¹³ ≈ 0.00021362305	0x4f = 0.10011.11 = +0b1.11×2 ³ = 14.0	0x8f = 1.00011.11 = -0b1.11×2 ⁻¹³ ≈ -0.00021362305	0xcf = 1.10011.11 = -0b1.11×2 ³ = -14.0
0x10 = 0.00100.00 = +0b1.00×2 ⁻¹² = 0.000244140625	0x50 = 0.10100.00 = +0b1.00×2 ⁴ = 16.0	0x90 = 1.00100.00 = -0b1.00×2 ⁻¹² ≈ -0.000244140625	0xd0 = 1.10100.00 = -0b1.00×2 ⁴ = -16.0
0x11 = 0.00100.01 = +0b1.01×2 ⁻¹² ≈ 0.00030517578	0x51 = 0.10100.01 = +0b1.01×2 ⁴ = 20.0	0x91 = 1.00100.01 = -0b1.01×2 ⁻¹² ≈ -0.00030517578	0xd1 = 1.10100.01 = -0b1.01×2 ⁴ = -20.0
0x12 = 0.00100.10 = +0b1.10×2 ⁻¹² ≈ 0.00036621094	0x52 = 0.10100.10 = +0b1.10×2 ⁴ = 24.0	0x92 = 1.00100.10 = -0b1.10×2 ⁻¹² ≈ -0.00036621094	0xd2 = 1.10100.10 = -0b1.10×2 ⁴ = -24.0
0x13 = 0.00100.11 = +0b1.11×2 ⁻¹² ≈ 0.00042724609	0x53 = 0.10100.11 = +0b1.11×2 ⁴ = 28.0	0x93 = 1.00100.11 = -0b1.11×2 ⁻¹² ≈ -0.00042724609	0xd3 = 1.10100.11 = -0b1.11×2 ⁴ = -28.0
0x14 = 0.00101.00 = +0b1.00×2 ⁻¹¹ ≈ 0.00048828125	0x54 = 0.10101.00 = +0b1.00×2 ⁵ = 32.0	0x94 = 1.00101.00 = -0b1.00×2 ⁻¹¹ ≈ -0.00048828125	0xd4 = 1.10101.00 = -0b1.00×2 ⁵ = -32.0
0x15 = 0.00101.01 = +0b1.01×2 ⁻¹¹ ≈ 0.00061035156	0x55 = 0.10101.01 = +0b1.01×2 ⁵ = 40.0	0x95 = 1.00101.01 = -0b1.01×2 ⁻¹¹ ≈ -0.00061035156	0xd5 = 1.10101.01 = -0b1.01×2 ⁵ = -40.0
0x16 = 0.00101.10 = +0b1.10×2 ⁻¹¹ ≈ 0.000732421875	0x56 = 0.10101.10 = +0b1.10×2 ⁵ = 48.0	0x96 = 1.00101.10 = -0b1.10×2 ⁻¹¹ ≈ -0.000732421875	0xd6 = 1.10101.10 = -0b1.10×2 ⁵ = -48.0
0x17 = 0.00101.11 = +0b1.11×2 ⁻¹¹ ≈ 0.00085449219	0x57 = 0.10101.11 = +0b1.11×2 ⁵ = 56.0	0x97 = 1.00101.11 = -0b1.11×2 ⁻¹¹ ≈ -0.00085449219	0xd7 = 1.10101.11 = -0b1.11×2 ⁵ = -56.0
0x18 = 0.00110.00 = +0b1.00×2 ⁻¹⁰ = 0.0009765625	0x58 = 0.10110.00 = +0b1.00×2 ⁶ = 64.0	0x98 = 1.00110.00 = -0b1.00×2 ⁻¹⁰ = -0.0009765625	0xd8 = 1.10110.00 = -0b1.00×2 ⁶ = -64.0
0x19 = 0.00110.01 = +0b1.01×2 ⁻¹⁰ = 0.001220703125	0x59 = 0.10110.01 = +0b1.01×2 ⁶ = 80.0	0x99 = 1.00110.01 = -0b1.01×2 ⁻¹⁰ ≈ -0.0012207031	0xd9 = 1.10110.01 = -0b1.01×2 ⁶ = -80.0
0x1a = 0.00110.10 = +0b1.01×2 ⁻¹⁰ = 0.00146484375	0x5a = 0.10110.10 = +0b1.01×2 ⁶ = 96.0	0x9a = 1.00110.10 = -0b1.01×2 ⁻¹⁰ ≈ -0.00146484375	0xda = 1.10110.10 = -0b1.01×2 ⁶ = -96.0
0x1b = 0.00110.11 = +0b1.11×2 ⁻¹⁰ = 0.001708984375	0x5b = 0.10110.11 = +0b1.11×2 ⁶ = 112.0	0x9b = 1.00110.11 = -0b1.11×2 ⁻¹⁰ ≈ -0.0017089844	0xdb = 1.10110.11 = -0b1.11×2 ⁶ = -112.0
0x1c = 0.00111.00 = +0b1.00×2 ⁻⁹ = 0.001953125	0x5c = 0.10111.00 = +0b1.00×2 ⁷ = 128.0	0x9c = 1.00111.00 = -0b1.00×2 ⁻⁹ = -0.001953125	0xdc = 1.10111.00 = -0b1.00×2 ⁷ = -128.0
0x1d = 0.00111.01 = +0b1.01×2 ⁻⁹ = 0.00244140625	0x5d = 0.10111.01 = +0b1.01×2 ⁷ = 160.0	0x9d = 1.00111.01 = -0b1.01×2 ⁻⁹ = -0.00244140625	0xdd = 1.10111.01 = -0b1.01×2 ⁷ = -160.0
0x1e = 0.00111.10 = +0b1.10×2 ⁻⁹ = 0.0029296875	0x5e = 0.10111.10 = +0b1.10×2 ⁷ = 192.0	0x9e = 1.00111.10 = -0b1.10×2 ⁻⁹ = -0.0029296875	0xde = 1.10111.10 = -0b1.10×2 ⁷ = -192.0
0x1f = 0.00111.11 = +0b1.11×2 ⁻⁹ = 0.00341796875	0x5f = 0.10111.11 = +0b1.11×2 ⁷ = 224.0	0x9f = 1.00111.11 = -0b1.11×2 ⁻⁹ = -0.00341796875	0xdf = 1.10111.11 = -0b1.11×2 ⁷ = -224.0
0x20 = 0.01000.00 = +0b1.00×2 ⁻⁸ = 0.00390625	0x60 = 0.11000.00 = +0b1.00×2 ⁸ = 256.0	0xa0 = 1.01000.00 = -0b1.00×2 ⁻⁸ = -0.00390625	0xe0 = 1.11000.00 = -0b1.00×2 ⁸ = -256.0
0x21 = 0.01000.01 = +0b1.01×2 ⁻⁸ = 0.0048828125	0x61 = 0.11000.01 = +0b1.01×2 ⁸ = 320.0	0xa1 = 1.01000.01 = -0b1.01×2 ⁻⁸ = -0.0048828125	0xe1 = 1.11000.01 = -0b1.01×2 ⁸ = -320.0
0x22 = 0.01000.10 = +0b1.10×2 ⁻⁸ = 0.005859375	0x62 = 0.11000.10 = +0b1.10×2 ⁸ = 384.0	0xa2 = 1.01000.10 = -0b1.10×2 ⁻⁸ = -0.005859375	0xe2 = 1.11000.10 = -0b1.10×2 ⁸ = -384.0
0x23 = 0.01000.11 = +0b1.11×2 ⁻⁸ = 0.0068359375	0x63 = 0.11000.11 = +0b1.11×2 ⁸ = 448.0	0xa3 = 1.01000.11 = -0b1.11×2 ⁻⁸ = -0.0068359375	0xe3 = 1.11000.11 = -0b1.11×2 ⁸ = -448.0
0x24 = 0.01001.00 = +0b1.00×2 ⁻⁷ = 0.0078125	0x64 = 0.11001.00 = +0b1.00×2 ⁹ = 512.0	0xa4 = 1.01001.00 = -0b1.00×2 ⁻⁷ = -0.0078125	0xe4 = 1.11001.00 = -0b1.00×2 ⁹ = -512.0
0x25 = 0.01001.01 = +0b1.01×2 ⁻⁷ = 0.009765625	0x65 = 0.11001.01 = +0b1.01×2 ⁹ = 640.0	0xa5 = 1.01001.01 = -0b1.01×2 ⁻⁷ = -0.009765625	0xe5 = 1.11001.01 = -0b1.01×2 ⁹ = -640.0
0x26 = 0.01001.10 = +0b1.10×2 ⁻⁷ = 0.01171875	0x66 = 0.11001.10 = +0b1.10×2 ⁹ = 768.0	0xa6 = 1.01001.10 = -0b1.10×2 ⁻⁷ = -0.01171875	0xe6 = 1.11001.10 = -0b1.10×2 ⁹ = -768.0
0x27 = 0.01001.11 = +0b1.11×2 ⁻⁷ = 0.013671875	0x67 = 0.11001.11 = +0b1.11×2 ⁹ = 896.0	0xa7 = 1.01001.11 = -0b1.11×2 ⁻⁷ = -0.013671875	0xe7 = 1.11001.11 = -0b1.11×2 ⁹ = -896.0
0x28 = 0.01010.00 = +0b1.00×2 ⁻⁶ = 0.015625	0x68 = 0.11010.00 = +0b1.00×2 ¹⁰ = 1024.0	0xa8 = 1.01010.00 = -0b1.00×2 ⁻⁶ = -0.015625	0xe8 = 1.11010.00 = -0b1.00×2 ¹⁰ = -1024.0
0x29 = 0.01010.01 = +0b1.01×2 ⁻⁶ = 0.01953125	0x69 = 0.11010.01 = +0b1.01×2 ¹⁰ = 1280.0	0xa9 = 1.01010.01 = -0b1.01×2 ⁻⁶ = -0.01953125	0xe9 = 1.11010.01 = -0b1.01×2 ¹⁰ = -1280.0
0x2a = 0.01010.10 = +0b1.10×2 ⁻⁶ = 0.0234375	0x6a = 0.11010.10 = +0b1.10×2 ¹⁰ = 1536.0	0xaa = 1.01010.10 = -0b1.10×2 ⁻⁶ = -0.0234375	0xea = 1.11010.10 = -0b1.10×2 ¹⁰ = -1536.0
0x2b = 0.01010.11 = +0b1.11×2 ⁻⁶ = 0.02734375	0x6b = 0.11010.11 = +0b1.11×2 ¹⁰ = 1792.0	0xab = 1.01010.11 = -0b1.11×2 ⁻⁶ = -0.02734375	0xeb = 1.11010.11 = -0b1.11×2 ¹⁰ = -1792.0
0x2c = 0.01011.00 = +0b1.00×2 ⁻⁵ = 0.03125	0x6c = 0.11011.00 = +0b1.00×2 ¹¹ = 2048.0	0xac = 1.01011.00 = -0b1.00×2 ⁻⁵ = -0.03125	0xec = 1.11011.00 = -0b1.00×2 ¹¹ = -2048.0
0x2d = 0.01011.01 = +0b1.01×2 ⁻⁵ = 0.0390625	0x6d = 0.11011.01 = +0b1.01×2 ¹¹ = 2560.0	0xad = 1.01011.01 = -0b1.01×2 ⁻⁵ = -0.0390625	0xed = 1.11011.01 = -0b1.01×2 ¹¹ = -2560.0
0x2e = 0.01011.10 = +0b1.10×2 ⁻⁵ = 0.046875	0x6e = 0.11011.10 = +0b1.10×2 ¹¹ = 3072.0	0xae = 1.01011.10 = -0b1.10×2 ⁻⁵ = -0.046875	0xee = 1.11011.10 = -0b1.10×2 ¹¹ = -3072.0
0x2f = 0.01011.11 = +0b1.11×2 ⁻⁵ = 0.0546875	0x6f = 0.11011.11 = +0b1.11×2 ¹¹ = 3584.0	0xaf = 1.01011.11 = -0b1.11×2 ⁻⁵ = -0.0546875	0xef = 1.11011.11 = -0b1.11×2 ¹¹ = -3584.0
0x30 = 0.01100.00 = +0b1.00×2 ⁻⁴ = 0.0625	0x70 = 0.11100.00 = +0b1.00×2 ¹² = 4096.0	0xb0 = 1.01100.00 = -0b1.00×2 ⁻⁴ = -0.0625	0xf0 = 1.11100.00 = -0b1.00×2 ¹² = -4096.0
0x31 = 0.01100.01 = +0b1.01×2 ⁻⁴ = 0.078125	0x71 = 0.11100.01 = +0b1.01×2 ¹² = 5120.0	0xb1 = 1.01100.01 = -0b1.01×2 ⁻⁴ = -0.078125	0xf1 = 1.11100.01 = -0b1.01×2 ¹² = -5120.0
0x32 = 0.01100.10 = +0b1.10×2 ⁻⁴ = 0.09375	0x72 = 0.11100.10 = +0b1.10×2 ¹² = 6144.0	0xb2 = 1.01100.10 = -0b1.10×2 ⁻⁴ = -0.09375	0xf2 = 1.11100.10 = -0b1.10×2 ¹² = -6144.0
0x33 = 0.01100.11 = +0b1.11×2 ⁻⁴ = 0.109375	0x73 = 0.11100.11 = +0b1.11×2 ¹² = 7168.0	0xb3 = 1.01100.11 = -0b1.11×2 ⁻⁴ = -0.109375	0xf3 = 1.11100.11 = -0b1.11×2 ¹² = -7168.0
0x34 = 0.01101.00 = +0b1.00×2 ⁻³ = 0.125	0x74 = 0.11101.00 = +0b1.00×2 ¹³ = 8192.0	0xb4 = 1.01101.00 = -0b1.00×2 ⁻³ = -0.125	0xf4 = 1.11101.00 = -0b1.00×2 ¹³ = -8192.0
0x35 = 0.01101.01 = +0b1.01×2 ⁻³ = 0.15625	0x75 = 0.11101.01 = +0b1.01×2 ¹³ = 10240.0	0xb5 = 1.01101.01 = -0b1.01×2 ⁻³ = -0.15625	0xf5 = 1.11101.01 = -0b1.01×2 ¹³ = -10240.0
0x36 = 0.01101.10 = +0b1.10×2 ⁻³ = 0.1875	0x76 = 0.11101.10 = +0b1.10×2 ¹³ = 12288.0	0xb6 = 1.01101.10 = -0b1.10×2 ⁻³ = -0.1875	0xf6 = 1.11101.10 = -0b1.10×2 ¹³ = -12288.0
0x37 = 0.01101.11 = +0b1.11×2 ⁻³ = 0.21875	0x77 = 0.11101.11 = +0b1.11×2 ¹³ = 14336.0	0xb7 = 1.01101.11 = -0b1.11×2 ⁻³ = -0.21875	0xf7 = 1.11101.11 = -0b1.11×2 ¹³ = -14336.0
0x38 = 0.01110.00 = +0b1.00×2 ⁻² = 0.25	0x78 = 0.11110.00 = +0b1.00×2 ¹⁴ = 16384.0	0xb8 = 1.01110.00 = -0b1.00×2 ⁻² = -0.25	0xf8 = 1.11110.00 = -0b1.00×2 ¹⁴ = -16384.0
0x39 = 0.01110.01 = +0b1.01×2 ⁻² = 0.3125	0x79 = 0.11110.01 = +0b1.01×2		

C.3 Value Table: P4, $p = 4$, $\text{emax} = 7$

0x00 = 0.0000.000 = 0.0	0x40 = 0.1000.000 = +0b1.000×2 ⁷⁰ = 1.0	0x80 = 1.0000.000 = NaN	0xc0 = 1.1000.000 = −0b1.000×2 ⁷⁰ = -1.0
0x01 = 0.0000.001 = +0b0.001×2 ⁻⁷ = 0.0009765625	0x41 = 0.1000.001 = +0b1.001×2 ⁷⁰ = 1.125	0x81 = 1.0000.001 = −0b0.001×2 ⁻⁷ = -0.0009765625	0xc1 = 1.1000.001 = −0b1.001×2 ⁷⁰ = -1.125
0x02 = 0.0000.010 = +0b0.010×2 ⁻⁷ = 0.001953125	0x42 = 0.1000.010 = +0b1.010×2 ⁷⁰ = 1.25	0x82 = 1.0000.010 = −0b0.010×2 ⁻⁷ = -0.001953125	0xc2 = 1.1000.010 = −0b1.010×2 ⁷⁰ = -1.25
0x03 = 0.0000.011 = +0b0.011×2 ⁻⁷ = 0.0029296875	0x43 = 0.1000.011 = +0b1.011×2 ⁷⁰ = 1.375	0x83 = 1.0000.011 = −0b0.011×2 ⁻⁷ = -0.0029296875	0xc3 = 1.1000.011 = −0b1.011×2 ⁷⁰ = -1.375
0x04 = 0.0000.100 = +0b0.100×2 ⁻⁷ = 0.00390625	0x44 = 0.1000.100 = +0b1.100×2 ⁷⁰ = 1.5	0x84 = 1.0000.100 = −0b0.100×2 ⁻⁷ = -0.00390625	0xc4 = 1.1000.100 = −0b1.100×2 ⁷⁰ = -1.5
0x05 = 0.0000.101 = +0b0.101×2 ⁻⁷ = 0.0048828125	0x45 = 0.1000.101 = +0b1.101×2 ⁷⁰ = 1.625	0x85 = 1.0000.101 = −0b0.101×2 ⁻⁷ = -0.0048828125	0xc5 = 1.1000.101 = −0b1.101×2 ⁷⁰ = -1.625
0x06 = 0.0000.110 = +0b0.110×2 ⁻⁷ = 0.005859375	0x46 = 0.1000.110 = +0b1.110×2 ⁷⁰ = 1.75	0x86 = 1.0000.110 = −0b0.110×2 ⁻⁷ = -0.005859375	0xc6 = 1.1000.110 = −0b1.110×2 ⁷⁰ = -1.75
0x07 = 0.0000.111 = +0b0.111×2 ⁻⁷ = 0.0068359375	0x47 = 0.1000.111 = +0b1.111×2 ⁷⁰ = 1.875	0x87 = 1.0000.111 = −0b0.111×2 ⁻⁷ = -0.0068359375	0xc7 = 1.1000.111 = −0b1.111×2 ⁷⁰ = -1.875
0x08 = 0.0001.000 = +0b1.000×2 ⁻⁶ = 0.0078125	0x48 = 0.1001.000 = +0b1.000×2 ⁷¹ = 2.0	0x88 = 1.0001.000 = −0b1.000×2 ⁻⁶ = -0.0078125	0xc8 = 1.1001.000 = −0b1.000×2 ⁷¹ = -2.0
0x09 = 0.0001.001 = +0b1.001×2 ⁻⁶ = 0.0087890625	0x49 = 0.1001.001 = +0b1.001×2 ⁷¹ = 2.25	0x89 = 1.0001.001 = −0b1.001×2 ⁻⁶ = -0.0087890625	0xc9 = 1.1001.001 = −0b1.001×2 ⁷¹ = -2.25
0x0a = 0.0001.010 = +0b1.010×2 ⁻⁶ = 0.009765625	0x4a = 0.1001.010 = +0b1.010×2 ⁷¹ = 2.5	0x8a = 1.0001.010 = −0b1.010×2 ⁻⁶ = -0.009765625	0xca = 1.1001.010 = −0b1.010×2 ⁷¹ = -2.5
0x0b = 0.0001.011 = +0b1.011×2 ⁻⁶ = 0.0107421875	0x4b = 0.1001.011 = +0b1.011×2 ⁷¹ = 2.75	0x8b = 1.0001.011 = −0b1.011×2 ⁻⁶ = -0.0107421875	0xcb = 1.1001.011 = −0b1.011×2 ⁷¹ = -2.75
0x0c = 0.0001.100 = +0b1.100×2 ⁻⁶ = 0.01171875	0x4c = 0.1001.100 = +0b1.100×2 ⁷¹ = 3.0	0x8c = 1.0001.100 = −0b1.100×2 ⁻⁶ = -0.01171875	0xcc = 1.1001.100 = −0b1.100×2 ⁷¹ = -3.0
0x0d = 0.0001.101 = +0b1.101×2 ⁻⁶ = 0.0126953125	0x4d = 0.1001.101 = +0b1.101×2 ⁷¹ = 3.25	0x8d = 1.0001.101 = −0b1.101×2 ⁻⁶ = -0.0126953125	0xcd = 1.1001.101 = −0b1.101×2 ⁷¹ = -3.25
0x0e = 0.0001.110 = +0b1.110×2 ⁻⁶ = 0.013671875	0x4e = 0.1001.110 = +0b1.110×2 ⁷¹ = 3.5	0x8e = 1.0001.110 = −0b1.110×2 ⁻⁶ = -0.013671875	0xce = 1.1001.110 = −0b1.110×2 ⁷¹ = -3.5
0x0f = 0.0001.111 = +0b1.111×2 ⁻⁶ = 0.0146484375	0x4f = 0.1001.111 = +0b1.111×2 ⁷¹ = 3.75	0x8f = 1.0001.111 = −0b1.111×2 ⁻⁶ = -0.0146484375	0xcf = 1.1001.111 = −0b1.111×2 ⁷¹ = -3.75
0x10 = 0.0010.000 = +0b1.000×2 ⁻⁵ = 0.015625	0x50 = 0.1010.000 = +0b1.000×2 ⁷² = 4.0	0x90 = 1.0010.000 = −0b1.000×2 ⁻⁵ = -0.015625	0xd0 = 1.1010.000 = −0b1.000×2 ⁷² = -4.0
0x11 = 0.0010.001 = +0b1.001×2 ⁻⁵ = 0.017578125	0x51 = 0.1010.001 = +0b1.001×2 ⁷² = 4.5	0x91 = 1.0010.001 = −0b1.001×2 ⁻⁵ = -0.017578125	0xd1 = 1.1010.001 = −0b1.001×2 ⁷² = -4.5
0x12 = 0.0010.010 = +0b1.010×2 ⁻⁵ = 0.01953125	0x52 = 0.1010.010 = +0b1.010×2 ⁷² = 5.0	0x92 = 1.0010.010 = −0b1.010×2 ⁻⁵ = -0.01953125	0xd2 = 1.1010.010 = −0b1.010×2 ⁷² = -5.0
0x13 = 0.0010.011 = +0b1.011×2 ⁻⁵ = 0.021484375	0x53 = 0.1010.011 = +0b1.011×2 ⁷² = 5.5	0x93 = 1.0010.011 = −0b1.011×2 ⁻⁵ = -0.021484375	0xd3 = 1.1010.011 = −0b1.011×2 ⁷² = -5.5
0x14 = 0.0010.100 = +0b1.100×2 ⁻⁵ = 0.0234375	0x54 = 0.1010.100 = +0b1.100×2 ⁷² = 6.0	0x94 = 1.0010.100 = −0b1.100×2 ⁻⁵ = -0.0234375	0xd4 = 1.1010.100 = −0b1.100×2 ⁷² = -6.0
0x15 = 0.0010.101 = +0b1.101×2 ⁻⁵ = 0.025390625	0x55 = 0.1010.101 = +0b1.101×2 ⁷² = 6.5	0x95 = 1.0010.101 = −0b1.101×2 ⁻⁵ = -0.025390625	0xd5 = 1.1010.101 = −0b1.101×2 ⁷² = -6.5
0x16 = 0.0010.110 = +0b1.110×2 ⁻⁵ = 0.02734375	0x56 = 0.1010.110 = +0b1.110×2 ⁷² = 7.0	0x96 = 1.0010.110 = −0b1.110×2 ⁻⁵ = -0.02734375	0xd6 = 1.1010.110 = −0b1.110×2 ⁷² = -7.0
0x17 = 0.0010.111 = +0b1.111×2 ⁻⁵ = 0.029296875	0x57 = 0.1010.111 = +0b1.111×2 ⁷² = 7.5	0x97 = 1.0010.111 = −0b1.111×2 ⁻⁵ = -0.029296875	0xd7 = 1.1010.111 = −0b1.111×2 ⁷² = -7.5
0x18 = 0.0011.000 = +0b1.000×2 ⁻⁴ = 0.03125	0x58 = 0.1011.000 = +0b1.000×2 ⁷³ = 8.0	0x98 = 1.0011.000 = −0b1.000×2 ⁻⁴ = -0.03125	0xd8 = 1.1011.000 = −0b1.000×2 ⁷³ = -8.0
0x19 = 0.0011.001 = +0b1.001×2 ⁻⁴ = 0.03515625	0x59 = 0.1011.001 = +0b1.001×2 ⁷³ = 9.0	0x99 = 1.0011.001 = −0b1.001×2 ⁻⁴ = -0.03515625	0xd9 = 1.1011.001 = −0b1.001×2 ⁷³ = -9.0
0x1a = 0.0011.010 = +0b1.010×2 ⁻⁴ = 0.0390625	0x5a = 0.1011.010 = +0b1.010×2 ⁷³ = 10.0	0x9a = 1.0011.010 = −0b1.010×2 ⁻⁴ = -0.0390625	0xda = 1.1011.010 = −0b1.010×2 ⁷³ = -10.0
0x1b = 0.0011.011 = +0b1.011×2 ⁻⁴ = 0.04296875	0x5b = 0.1011.011 = +0b1.011×2 ⁷³ = 11.0	0x9b = 1.0011.011 = −0b1.011×2 ⁻⁴ = -0.04296875	0xdb = 1.1011.011 = −0b1.011×2 ⁷³ = -11.0
0x1c = 0.0011.100 = +0b1.100×2 ⁻⁴ = 0.046875	0x5c = 0.1011.100 = +0b1.100×2 ⁷³ = 12.0	0x9c = 1.0011.100 = −0b1.100×2 ⁻⁴ = -0.046875	0xdc = 1.1011.100 = −0b1.100×2 ⁷³ = -12.0
0x1d = 0.0011.101 = +0b1.101×2 ⁻⁴ = 0.05078125	0x5d = 0.1011.101 = +0b1.101×2 ⁷³ = 13.0	0x9d = 1.0011.101 = −0b1.101×2 ⁻⁴ = -0.05078125	0xdd = 1.1011.101 = −0b1.101×2 ⁷³ = -13.0
0x1e = 0.0011.110 = +0b1.110×2 ⁻⁴ = 0.0546875	0x5e = 0.1011.110 = +0b1.110×2 ⁷³ = 14.0	0x9e = 1.0011.110 = −0b1.110×2 ⁻⁴ = -0.0546875	0xde = 1.1011.110 = −0b1.110×2 ⁷³ = -14.0
0x1f = 0.0011.111 = +0b1.111×2 ⁻⁴ = 0.05859375	0x5f = 0.1011.111 = +0b1.111×2 ⁷³ = 15.0	0x9f = 1.0011.111 = −0b1.111×2 ⁻⁴ = -0.05859375	0xdf = 1.1011.111 = −0b1.111×2 ⁷³ = -15.0
0x20 = 0.0100.000 = +0b1.000×2 ⁻³ = 0.0625	0x60 = 0.1100.000 = +0b1.000×2 ⁷⁴ = 16.0	0xa0 = 1.0100.000 = −0b1.000×2 ⁻³ = -0.0625	0xe0 = 1.1100.000 = −0b1.000×2 ⁷⁴ = -16.0
0x21 = 0.0100.001 = +0b1.001×2 ⁻³ = 0.0703125	0x61 = 0.1100.001 = +0b1.001×2 ⁷⁴ = 18.0	0xa1 = 1.0100.001 = −0b1.001×2 ⁻³ = -0.0703125	0xe1 = 1.1100.001 = −0b1.001×2 ⁷⁴ = -18.0
0x22 = 0.0100.010 = +0b1.010×2 ⁻³ = 0.078125	0x62 = 0.1100.010 = +0b1.010×2 ⁷⁴ = 20.0	0xa2 = 1.0100.010 = −0b1.010×2 ⁻³ = -0.078125	0xe2 = 1.1100.010 = −0b1.010×2 ⁷⁴ = -20.0
0x23 = 0.0100.011 = +0b1.011×2 ⁻³ = 0.0859375	0x63 = 0.1100.011 = +0b1.011×2 ⁷⁴ = 22.0	0xa3 = 1.0100.011 = −0b1.011×2 ⁻³ = -0.0859375	0xe3 = 1.1100.011 = −0b1.011×2 ⁷⁴ = -22.0
0x24 = 0.0100.100 = +0b1.100×2 ⁻³ = 0.09375	0x64 = 0.1100.100 = +0b1.100×2 ⁷⁴ = 24.0	0xa4 = 1.0100.100 = −0b1.100×2 ⁻³ = -0.09375	0xe4 = 1.1100.100 = −0b1.100×2 ⁷⁴ = -24.0
0x25 = 0.0100.101 = +0b1.101×2 ⁻³ = 0.1015625	0x65 = 0.1100.101 = +0b1.101×2 ⁷⁴ = 26.0	0xa5 = 1.0100.101 = −0b1.101×2 ⁻³ = -0.1015625	0xe5 = 1.1100.101 = −0b1.101×2 ⁷⁴ = -26.0
0x26 = 0.0100.110 = +0b1.110×2 ⁻³ = 0.109375	0x66 = 0.1100.110 = +0b1.110×2 ⁷⁴ = 28.0	0xa6 = 1.0100.110 = −0b1.110×2 ⁻³ = -0.109375	0xe6 = 1.1100.110 = −0b1.110×2 ⁷⁴ = -28.0
0x27 = 0.0100.111 = +0b1.111×2 ⁻³ = 0.1171875	0x67 = 0.1100.111 = +0b1.111×2 ⁷⁴ = 30.0	0xa7 = 1.0100.111 = −0b1.111×2 ⁻³ = -0.1171875	0xe7 = 1.1100.111 = −0b1.111×2 ⁷⁴ = -30.0
0x28 = 0.0101.000 = +0b1.000×2 ⁻² = 0.125	0x68 = 0.1101.000 = +0b1.000×2 ⁷⁵ = 32.0	0xa8 = 1.0101.000 = −0b1.000×2 ⁻² = -0.125	0xe8 = 1.1101.000 = −0b1.000×2 ⁷⁵ = -32.0
0x29 = 0.0101.001 = +0b1.001×2 ⁻² = 0.140625	0x69 = 0.1101.001 = +0b1.001×2 ⁷⁵ = 36.0	0xa9 = 1.0101.001 = −0b1.001×2 ⁻² = -0.140625	0xe9 = 1.1101.001 = −0b1.001×2 ⁷⁵ = -36.0
0x2a = 0.0101.010 = +0b1.010×2 ⁻² = 0.15625	0x6a = 0.1101.010 = +0b1.010×2 ⁷⁵ = 40.0	0xaa = 1.0101.010 = −0b1.010×2 ⁻² = -0.15625	0xea = 1.1101.010 = −0b1.010×2 ⁷⁵ = -40.0
0x2b = 0.0101.011 = +0b1.011×2 ⁻² = 0.171875	0x6b = 0.1101.011 = +0b1.011×2 ⁷⁵ = 44.0	0xab = 1.0101.011 = −0b1.011×2 ⁻² = -0.171875	0xeb = 1.1101.011 = −0b1.011×2 ⁷⁵ = -44.0
0x2c = 0.0101.100 = +0b1.100×2 ⁻² = 0.1875	0x6c = 0.1101.100 = +0b1.100×2 ⁷⁵ = 48.0	0xac = 1.0101.100 = −0b1.100×2 ⁻² = -0.1875	0xec = 1.1101.100 = −0b1.100×2 ⁷⁵ = -48.0
0x2d = 0.0101.101 = +0b1.101×2 ⁻² = 0.203125	0x6d = 0.1101.101 = +0b1.101×2 ⁷⁵ = 52.0	0xad = 1.0101.101 = −0b1.101×2 ⁻² = -0.203125	0xed = 1.1101.101 = −0b1.101×2 ⁷⁵ = -52.0
0x2e = 0.0101.110 = +0b1.110×2 ⁻² = 0.21875	0x6e = 0.1101.110 = +0b1.110×2 ⁷⁵ = 56.0	0xae = 1.0101.110 = −0b1.110×2 ⁻² = -0.21875	0xee = 1.1101.110 = −0b1.110×2 ⁷⁵ = -56.0
0x2f = 0.0101.111 = +0b1.111×2 ⁻² = 0.234375	0x6f = 0.1101.111 = +0b1.111×2 ⁷⁵ = 60.0	0xaf = 1.0101.111 = −0b1.111×2 ⁻² = -0.234375	0xef = 1.1101.111 = −0b1.111×2 ⁷⁵ = -60.0
0x30 = 0.0110.000 = +0b1.000×2 ⁻¹ = 0.25	0x70 = 0.1110.000 = +0b1.000×2 ⁷⁶ = 64.0	0xb0 = 1.0110.000 = −0b1.000×2 ⁻¹ = -0.25	0xf0 = 1.1110.000 = −0b1.000×2 ⁷⁶ = -64.0
0x31 = 0.0110.001 = +0b1.001×2 ⁻¹ = 0.28125	0x71 = 0.1110.001 = +0b1.001×2 ⁷⁶ = 72.0	0xb1 = 1.0110.001 = −0b1.001×2 ⁻¹ = -0.28125	0xf1 = 1.1110.001 = −0b1.001×2 ⁷⁶ = -72.0
0x32 = 0.0110.010 = +0b1.010×2 ⁻¹ = 0.3125	0x72 = 0.1110.010 = +0b1.010×2 ⁷⁶ = 80.0	0xb2 = 1.0110.010 = −0b1.010×2 ⁻¹ = -0.3125	0xf2 = 1.1110.010 = −0b1.010×2 ⁷⁶ = -80.0
0x33 = 0.0110.011 = +0b1.011×2 ⁻¹ = 0.34375	0x73 = 0.1110.011 = +0b1.011×2 ⁷⁶ = 88.0	0xb3 = 1.0110.011 = −0b1.011×2 ⁻¹ = -0.34375	0xf3 = 1.1110.011 = −0b1.011×2 ⁷⁶ = -88.0
0x34 = 0.0110.100 = +0b1.100×2 ⁻¹ = 0.375	0x74 = 0.1110.100 = +0b1.100×2 ⁷⁶ = 96.0	0xb4 = 1.0110.100 = −0b1.100×2 ⁻¹ = -0.375	0xf4 = 1.1110.100 = −0b1.100×2 ⁷⁶ = -96.0
0x35 = 0.0110.101 = +0b1.101×2 ⁻¹ = 0.40625	0x75 = 0.1110.101 = +0b1.101×2 ⁷⁶ = 104.0	0xb5 = 1.0110.101 = −0b1.101×2 ⁻¹ = -0.40625	0xf5 = 1.1110.101 = −0b1.101×2 ⁷⁶ = -104.0
0x36 = 0.0110.110 = +0b1.110×2 ⁻¹ = 0.4375	0x76 = 0.1110.110 = +0b1.110×2 ⁷⁶ = 112.0	0xb6 = 1.0110.110 = −0b1.110×2 ⁻¹ = -0.4375	0xf6 = 1.1110.110 = −0b1.110×2 ⁷⁶ = -112.0
0x37 = 0.0110.111 = +0b1.111×2 ⁻¹ = 0.46875	0x77 = 0.1110.111 = +0b1.111×2 ⁷⁶ = 120.0	0xb7 = 1.0110.111 = −0b1.111×2 ⁻¹ = -0.46875	0xf7 = 1.1110.111 = −0b1.111×2 ⁷⁶ = -120.0
0x38 = 0.0111.000 = +0b1.000×2 ⁻¹ = 0.5	0x78 = 0.1111.000 = +0b1.000×2 ⁷⁷ = 128.0	0xb8 = 1.0111.000 = −0b1.000×2 ⁻¹ = -0.5	0xf8 = 1.1111.000 = −0b1.000×2 ⁷⁷ = -128.0
0x39 = 0.0111.001 = +0b1.001×2 ⁻¹ = 0.5625	0x79 = 0.1111.001 = +0b1.001×2 ⁷⁷ = 144.0	0xb9 = 1.0111.001 = −0b1.001×2 ⁻¹ = -0.5625	0xf9 = 1

C.4 Value Table: P5, $p = 5$, $\text{emax} = 3$

0x00 = 0.000.0000 = 0.0	0x40 = 0.100.0000 = +0b1.0000×2 ⁰ = 1.0	0x80 = 1.000.0000 = NaN	0xc0 = 1.100.0000 = -0b1.0000×2 ⁰ = -1.0
0x01 = 0.000.0001 = +0b0.0001×2 ⁻³ = 0.0078125	0x41 = 0.100.0001 = +0b1.0001×2 ⁰ = 1.0625	0x81 = 1.000.0001 = -0b0.0001×2 ⁻³ = -0.0078125	0xc1 = 1.100.0001 = -0b1.0001×2 ⁰ = -1.0625
0x02 = 0.000.0010 = +0b0.0010×2 ⁻³ = 0.015625	0x42 = 0.100.0010 = +0b1.0010×2 ⁰ = 1.125	0x82 = 1.000.0010 = -0b0.0010×2 ⁻³ = -0.015625	0xc2 = 1.100.0010 = -0b1.0010×2 ⁰ = -1.125
0x03 = 0.000.0011 = +0b0.0011×2 ⁻³ = 0.0234375	0x43 = 0.100.0011 = +0b1.0011×2 ⁰ = 1.1875	0x83 = 1.000.0011 = -0b0.0011×2 ⁻³ = -0.0234375	0xc3 = 1.100.0011 = -0b1.0011×2 ⁰ = -1.1875
0x04 = 0.000.0100 = +0b0.0100×2 ⁻³ = 0.03125	0x44 = 0.100.0100 = +0b1.0100×2 ⁰ = 1.25	0x84 = 1.000.0100 = -0b0.0100×2 ⁻³ = -0.03125	0xc4 = 1.100.0100 = -0b1.0100×2 ⁰ = -1.25
0x05 = 0.000.0101 = +0b0.0101×2 ⁻³ = 0.0390625	0x45 = 0.100.0101 = +0b1.0101×2 ⁰ = 1.3125	0x85 = 1.000.0101 = -0b0.0101×2 ⁻³ = -0.0390625	0xc5 = 1.100.0101 = -0b1.0101×2 ⁰ = -1.3125
0x06 = 0.000.0110 = +0b0.0110×2 ⁻³ = 0.046875	0x46 = 0.100.0110 = +0b1.0110×2 ⁰ = 1.375	0x86 = 1.000.0110 = -0b0.0110×2 ⁻³ = -0.046875	0xc6 = 1.100.0110 = -0b1.0110×2 ⁰ = -1.375
0x07 = 0.000.0111 = +0b0.0111×2 ⁻³ = 0.0546875	0x47 = 0.100.0111 = +0b1.0111×2 ⁰ = 1.4375	0x87 = 1.000.0111 = -0b0.0111×2 ⁻³ = -0.0546875	0xc7 = 1.100.0111 = -0b1.0111×2 ⁰ = -1.4375
0x08 = 0.000.1000 = +0b0.1000×2 ⁻³ = 0.0625	0x48 = 0.100.1000 = +0b1.1000×2 ⁰ = 1.5	0x88 = 1.000.1000 = -0b0.1000×2 ⁻³ = -0.0625	0xc8 = 1.100.1000 = -0b1.1000×2 ⁰ = -1.5
0x09 = 0.000.1001 = +0b0.1001×2 ⁻³ = 0.0703125	0x49 = 0.100.1001 = +0b1.1001×2 ⁰ = 1.5625	0x89 = 1.000.1001 = -0b0.1001×2 ⁻³ = -0.0703125	0xc9 = 1.100.1001 = -0b1.1001×2 ⁰ = -1.5625
0x0a = 0.000.1010 = +0b0.1010×2 ⁻³ = 0.078125	0x4a = 0.100.1010 = +0b1.1010×2 ⁰ = 1.625	0x8a = 1.000.1010 = -0b0.1010×2 ⁻³ = -0.078125	0xca = 1.100.1010 = -0b1.1010×2 ⁰ = -1.625
0x0b = 0.000.1011 = +0b0.1011×2 ⁻³ = 0.0859375	0x4b = 0.100.1011 = +0b1.1011×2 ⁰ = 1.6875	0x8b = 1.000.1011 = -0b0.1011×2 ⁻³ = -0.0859375	0xcb = 1.100.1011 = -0b1.1011×2 ⁰ = -1.6875
0x0c = 0.000.1100 = +0b0.1100×2 ⁻³ = 0.09375	0x4c = 0.100.1100 = +0b1.1100×2 ⁰ = 1.75	0x8c = 1.000.1100 = -0b0.1100×2 ⁻³ = -0.09375	0xcc = 1.100.1100 = -0b1.1100×2 ⁰ = -1.75
0x0d = 0.000.1101 = +0b0.1101×2 ⁻³ = 0.1015625	0x4d = 0.100.1101 = +0b1.1101×2 ⁰ = 1.8125	0x8d = 1.000.1101 = -0b0.1101×2 ⁻³ = -0.1015625	0xcd = 1.100.1101 = -0b1.1101×2 ⁰ = -1.8125
0x0e = 0.000.1110 = +0b0.1110×2 ⁻³ = 0.109375	0x4e = 0.100.1110 = +0b1.1110×2 ⁰ = 1.875	0x8e = 1.000.1110 = -0b0.1110×2 ⁻³ = -0.109375	0xce = 1.100.1110 = -0b1.1110×2 ⁰ = -1.875
0x0f = 0.000.1111 = +0b0.1111×2 ⁻³ = 0.1171875	0x4f = 0.100.1111 = +0b1.1111×2 ⁰ = 1.9375	0x8f = 1.000.1111 = -0b0.1111×2 ⁻³ = -0.1171875	0xcf = 1.100.1111 = -0b1.1111×2 ⁰ = -1.9375
0x10 = 0.001.0000 = +0b1.0000×2 ⁻³ = 0.125	0x50 = 0.101.0000 = +0b1.0000×2 ¹ = 2.0	0x90 = 1.001.0000 = -0b1.0000×2 ⁻³ = -0.125	0xd0 = 1.101.0000 = -0b1.0000×2 ¹ = -2.0
0x11 = 0.001.0001 = +0b1.0001×2 ⁻³ = 0.1328125	0x51 = 0.101.0001 = +0b1.0001×2 ¹ = 2.125	0x91 = 1.001.0001 = -0b1.0001×2 ⁻³ = -0.1328125	0xd1 = 1.101.0001 = -0b1.0001×2 ¹ = -2.125
0x12 = 0.001.0010 = +0b1.0010×2 ⁻³ = 0.140625	0x52 = 0.101.0010 = +0b1.0010×2 ¹ = 2.25	0x92 = 1.001.0010 = -0b1.0010×2 ⁻³ = -0.140625	0xd2 = 1.101.0010 = -0b1.0010×2 ¹ = -2.25
0x13 = 0.001.0011 = +0b1.0011×2 ⁻³ = 0.1484375	0x53 = 0.101.0011 = +0b1.0011×2 ¹ = 2.375	0x93 = 1.001.0011 = -0b1.0011×2 ⁻³ = -0.1484375	0xd3 = 1.101.0011 = -0b1.0011×2 ¹ = -2.375
0x14 = 0.001.0100 = +0b1.0100×2 ⁻³ = 0.15625	0x54 = 0.101.0100 = +0b1.0100×2 ¹ = 2.5	0x94 = 1.001.0100 = -0b1.0100×2 ⁻³ = -0.15625	0xd4 = 1.101.0100 = -0b1.0100×2 ¹ = -2.5
0x15 = 0.001.0101 = +0b1.0101×2 ⁻³ = 0.1640625	0x55 = 0.101.0101 = +0b1.0101×2 ¹ = 2.625	0x95 = 1.001.0101 = -0b1.0101×2 ⁻³ = -0.1640625	0xd5 = 1.101.0101 = -0b1.0101×2 ¹ = -2.625
0x16 = 0.001.0110 = +0b1.0110×2 ⁻³ = 0.171875	0x56 = 0.101.0110 = +0b1.0110×2 ¹ = 2.75	0x96 = 1.001.0110 = -0b1.0110×2 ⁻³ = -0.171875	0xd6 = 1.101.0110 = -0b1.0110×2 ¹ = -2.75
0x17 = 0.001.0111 = +0b1.0111×2 ⁻³ = 0.1796875	0x57 = 0.101.0111 = +0b1.0111×2 ¹ = 2.875	0x97 = 1.001.0111 = -0b1.0111×2 ⁻³ = -0.1796875	0xd7 = 1.101.0111 = -0b1.0111×2 ¹ = -2.875
0x18 = 0.001.1000 = +0b1.1000×2 ⁻³ = 0.1875	0x58 = 0.101.1000 = +0b1.1000×2 ¹ = 3.0	0x98 = 1.001.1000 = -0b1.1000×2 ⁻³ = -0.1875	0xd8 = 1.101.1000 = -0b1.1000×2 ¹ = -3.0
0x19 = 0.001.1001 = +0b1.1001×2 ⁻³ = 0.1953125	0x59 = 0.101.1001 = +0b1.1001×2 ¹ = 3.125	0x99 = 1.001.1001 = -0b1.1001×2 ⁻³ = -0.1953125	0xd9 = 1.101.1001 = -0b1.1001×2 ¹ = -3.125
0x1a = 0.001.1010 = +0b1.1010×2 ⁻³ = 0.203125	0x5a = 0.101.1010 = +0b1.1010×2 ¹ = 3.25	0x9a = 1.001.1010 = -0b1.1010×2 ⁻³ = -0.203125	0xda = 1.101.1010 = -0b1.1010×2 ¹ = -3.25
0x1b = 0.001.1011 = +0b1.1011×2 ⁻³ = 0.2109375	0x5b = 0.101.1011 = +0b1.1011×2 ¹ = 3.375	0x9b = 1.001.1011 = -0b1.1011×2 ⁻³ = -0.2109375	0xdb = 1.101.1011 = -0b1.1011×2 ¹ = -3.375
0x1c = 0.001.1100 = +0b1.1100×2 ⁻³ = 0.21875	0x5c = 0.101.1100 = +0b1.1100×2 ¹ = 3.5	0x9c = 1.001.1100 = -0b1.1100×2 ⁻³ = -0.21875	0xdc = 1.101.1100 = -0b1.1100×2 ¹ = -3.5
0x1d = 0.001.1101 = +0b1.1101×2 ⁻³ = 0.2265625	0x5d = 0.101.1101 = +0b1.1101×2 ¹ = 3.625	0x9d = 1.001.1101 = -0b1.1101×2 ⁻³ = -0.2265625	0xdd = 1.101.1101 = -0b1.1101×2 ¹ = -3.625
0x1e = 0.001.1110 = +0b1.1110×2 ⁻³ = 0.234375	0x5e = 0.101.1110 = +0b1.1110×2 ¹ = 3.75	0x9e = 1.001.1110 = -0b1.1110×2 ⁻³ = -0.234375	0xde = 1.101.1110 = -0b1.1110×2 ¹ = -3.75
0x1f = 0.001.1111 = +0b1.1111×2 ⁻³ = 0.2421875	0x5f = 0.101.1111 = +0b1.1111×2 ¹ = 3.875	0x9f = 1.001.1111 = -0b1.1111×2 ⁻³ = -0.2421875	0xdf = 1.101.1111 = -0b1.1111×2 ¹ = -3.875
0x20 = 0.010.0000 = +0b1.0000×2 ⁻² = 0.25	0x60 = 0.110.0000 = +0b1.0000×2 ² = 4.0	0xa0 = 1.010.0000 = -0b1.0000×2 ⁻² = -0.25	0xe0 = 1.110.0000 = -0b1.0000×2 ² = -4.0
0x21 = 0.010.0001 = +0b1.0001×2 ⁻² = 0.265625	0x61 = 0.110.0001 = +0b1.0001×2 ² = 4.25	0xa1 = 1.010.0001 = -0b1.0001×2 ⁻² = -0.265625	0xe1 = 1.110.0001 = -0b1.0001×2 ² = -4.25
0x22 = 0.010.0010 = +0b1.0010×2 ⁻² = 0.28125	0x62 = 0.110.0010 = +0b1.0010×2 ² = 4.5	0xa2 = 1.010.0010 = -0b1.0010×2 ⁻² = -0.28125	0xe2 = 1.110.0010 = -0b1.0010×2 ² = -4.5
0x23 = 0.010.0011 = +0b1.0011×2 ⁻² = 0.296875	0x63 = 0.110.0011 = +0b1.0011×2 ² = 4.75	0xa3 = 1.010.0011 = -0b1.0011×2 ⁻² = -0.296875	0xe3 = 1.110.0011 = -0b1.0011×2 ² = -4.75
0x24 = 0.010.0100 = +0b1.0100×2 ⁻² = 0.3125	0x64 = 0.110.0100 = +0b1.0100×2 ² = 5.0	0xa4 = 1.010.0100 = -0b1.0100×2 ⁻² = -0.3125	0xe4 = 1.110.0100 = -0b1.0100×2 ² = -5.0
0x25 = 0.010.0101 = +0b1.0101×2 ⁻² = 0.328125	0x65 = 0.110.0101 = +0b1.0101×2 ² = 5.25	0xa5 = 1.010.0101 = -0b1.0101×2 ⁻² = -0.328125	0xe5 = 1.110.0101 = -0b1.0101×2 ² = -5.25
0x26 = 0.010.0110 = +0b1.0110×2 ⁻² = 0.34375	0x66 = 0.110.0110 = +0b1.0110×2 ² = 5.5	0xa6 = 1.010.0110 = -0b1.0110×2 ⁻² = -0.34375	0xe6 = 1.110.0110 = -0b1.0110×2 ² = -5.5
0x27 = 0.010.0111 = +0b1.0111×2 ⁻² = 0.359375	0x67 = 0.110.0111 = +0b1.0111×2 ² = 5.75	0xa7 = 1.010.0111 = -0b1.0111×2 ⁻² = -0.359375	0xe7 = 1.110.0111 = -0b1.0111×2 ² = -5.75
0x28 = 0.010.1000 = +0b1.1000×2 ⁻² = 0.375	0x68 = 0.110.1000 = +0b1.1000×2 ² = 6.0	0xa8 = 1.010.1000 = -0b1.1000×2 ⁻² = -0.375	0xe8 = 1.110.1000 = -0b1.1000×2 ² = -6.0
0x29 = 0.010.1001 = +0b1.1001×2 ⁻² = 0.390625	0x69 = 0.110.1001 = +0b1.1001×2 ² = 6.25	0xa9 = 1.010.1001 = -0b1.1001×2 ⁻² = -0.390625	0xe9 = 1.110.1001 = -0b1.1001×2 ² = -6.25
0x2a = 0.010.1010 = +0b1.1010×2 ⁻² = 0.40625	0x6a = 0.110.1010 = +0b1.1010×2 ² = 6.5	0xaa = 1.010.1010 = -0b1.1010×2 ⁻² = -0.40625	0xea = 1.110.1010 = -0b1.1010×2 ² = -6.5
0x2b = 0.010.1011 = +0b1.1011×2 ⁻² = 0.421875	0x6b = 0.110.1011 = +0b1.1011×2 ² = 6.75	0xab = 1.010.1011 = -0b1.1011×2 ⁻² = -0.421875	0xeb = 1.110.1011 = -0b1.1011×2 ² = -6.75
0x2c = 0.010.1100 = +0b1.1100×2 ⁻² = 0.4375	0x6c = 0.110.1100 = +0b1.1100×2 ² = 7.0	0xac = 1.010.1100 = -0b1.1100×2 ⁻² = -0.4375	0xec = 1.110.1100 = -0b1.1100×2 ² = -7.0
0x2d = 0.010.1101 = +0b1.1101×2 ⁻² = 0.453125	0x6d = 0.110.1101 = +0b1.1101×2 ² = 7.25	0xad = 1.010.1101 = -0b1.1101×2 ⁻² = -0.453125	0xed = 1.110.1101 = -0b1.1101×2 ² = -7.25
0x2e = 0.010.1110 = +0b1.1110×2 ⁻² = 0.46875	0x6e = 0.110.1110 = +0b1.1110×2 ² = 7.5	0xae = 1.010.1110 = -0b1.1110×2 ⁻² = -0.46875	0xee = 1.110.1110 = -0b1.1110×2 ² = -7.5
0x2f = 0.010.1111 = +0b1.1111×2 ⁻² = 0.484375	0x6f = 0.110.1111 = +0b1.1111×2 ² = 7.75	0xaf = 1.010.1111 = -0b1.1111×2 ⁻² = -0.484375	0xef = 1.110.1111 = -0b1.1111×2 ² = -7.75
0x30 = 0.011.0000 = +0b1.0000×2 ⁻¹ = 0.5	0x70 = 0.111.0000 = +0b1.0000×2 ³ = 8.0	0xb0 = 1.011.0000 = -0b1.0000×2 ⁻¹ = -0.5	0xf0 = 1.111.0000 = -0b1.0000×2 ³ = -8.0
0x31 = 0.011.0001 = +0b1.0001×2 ⁻¹ = 0.53125	0x71 = 0.111.0001 = +0b1.0001×2 ³ = 8.5	0xb1 = 1.011.0001 = -0b1.0001×2 ⁻¹ = -0.53125	0xf1 = 1.111.0001 = -0b1.0001×2 ³ = -8.5
0x32 = 0.011.0010 = +0b1.0010×2 ⁻¹ = 0.5625	0x72 = 0.111.0010 = +0b1.0010×2 ³ = 9.0	0xb2 = 1.011.0010 = -0b1.0010×2 ⁻¹ = -0.5625	0xf2 = 1.111.0010 = -0b1.0010×2 ³ = -9.0
0x33 = 0.011.0011 = +0b1.0011×2 ⁻¹ = 0.59375	0x73 = 0.111.0011 = +0b1.0011×2 ³ = 9.5	0xb3 = 1.011.0011 = -0b1.0011×2 ⁻¹ = -0.59375	0xf3 = 1.111.0011 = -0b1.0011×2 ³ = -9.5
0x34 = 0.011.0100 = +0b1.0100×2 ⁻¹ = 0.625	0x74 = 0.111.0100 = +0b1.0100×2 ³ = 10.0	0xb4 = 1.011.0100 = -0b1.0100×2 ⁻¹ = -0.625	0xf4 = 1.111.0100 = -0b1.0100×2 ³ = -10.0
0x35 = 0.011.0101 = +0b1.0101×2 ⁻¹ = 0.65625	0x75 = 0.111.0101 = +0b1.0101×2 ³ = 10.5	0xb5 = 1.011.0101 = -0b1.0101×2 ⁻¹ = -0.65625	0xf5 = 1.111.0101 = -0b1.0101×2 ³ = -10.5
0x36 = 0.011.0110 = +0b1.0110×2 ⁻¹ = 0.6875	0x76 = 0.111.0110 = +0b1.0110×2 ³ = 11.0	0xb6 = 1.011.0110 = -0b1.0110×2 ⁻¹ = -0.6875	0xf6 = 1.111.0110 = -0b1.0110×2 ³ = -11.0
0x37 = 0.011.0111 = +0b1.0111×2 ⁻¹ = 0.71875	0x77 = 0.111.0111 = +0b1.0111×2 ³ = 11.5	0xb7 = 1.011.0111 = -0b1.0111×2 ⁻¹ = -0.71875	0xf7 = 1.111.0111 = -0b1.0111×2 ³ = -11.5
0x38 = 0.011.1000 = +0b1.1000×2 ⁻¹ = 0.75	0x78 = 0.111.1000 = +0b1.1000×2 ³ = 12.0	0xb8 = 1.011.1000 = -0b1.1000×2 ⁻¹ = -0.75	0xf8 = 1.111.1000 = -0b1.1000×2 ³ = -12.0
0x39 = 0.011.1001 = +0b1.1001×2 ⁻¹ = 0.78125	0x79 = 0.111.1001 = +0b1.1001×2 ³ = 12.5	0xb9 = 1.011.1001 = -0b1.1001×2 ⁻¹ = -0.78125	0xf9 = 1.111.1001 = -0b1.1001×2 ³ = -12.5
0x3a = 0.011.1010 = +0b1.1010×2 ⁻¹ = 0.8125	0x7a = 0.111.1010 = +0b1.1010×2 ³ = 13.0	0xba = 1.011.1010 = -0b1.1010×2 ⁻¹ = -0.8125	0xfa = 1.111.1010 = -0b1.1010×2 ³ = -13.0
0x3b = 0.011.1011 = +0b1.1011×2 ⁻¹ = 0.84375	0x7b = 0.111.1011 = +0b1.1011×2 ³ = 13.5	0xbb = 1.011.1011 = -0b1.1011×2 ⁻¹ = -0.84375	0xfb = 1.111.1011 = -0b1.1011×2 ³ = -13.5
0x3c = 0.011.1100 = +0b1.1100×2 ⁻¹ = 0.875	0x7c = 0.111.1100 = +0b1.1100×2 ³ = 14.0	0xbc = 1.011.1100 = -0b1.1100×2 ⁻¹ = -0.875	0xfc = 1.111.1100 = -0b1.1100×2 ³ = -14.0
0x3d = 0.011.1101 = +0b1.1101×2 ⁻¹ = 0.90625	0x7d = 0.111.1101 = +0b1.1101×2 ³ = 14.5	0xbd = 1.011.1101 = -0b1.1101×2 ⁻¹ = -0.90625	0xfd = 1.111.1101 = -0b1.1101×2 ³ = -14.5
0x3e = 0.011.1110 = +0b1.1110×2 ⁻¹ = 0.9375	0x7e = 0.111.1110 = +0b1.1110×2 ³ = 15.0	0xbe = 1.011.1110 = -0b1.1110×2 ⁻¹ = -0.9375	0xfe = 1.111.1110 = -0b1.1110×2 ³ = -15.0
0x3f = 0.011.1111 = +0b1.1111×2 ⁻¹ = 0.96875	0x7f = 0.111.1111 = +Inf	0xbf = 1.011.1111 = -0b1.1111×2 ⁻¹ = -0.96875	0xff = 1.111.1111 = -Inf

C.5 Value Table: P6, $p = 6$, $\text{emax} = 1$

0x00 = 0.00.00000 = 0.0	0x40 = 0.10.00000 = +0b1.00000×2 ⁰ = 1.0	0x80 = 1.00.00000 = NaN	0xc0 = 1.10.00000 = -0b1.00000×2 ⁰ = -1.0
0x01 = 0.00.00001 = +0b0.00001×2 ⁻¹ = 0.015625	0x41 = 0.10.00001 = +0b1.00001×2 ⁰ = 1.03125	0x81 = 1.00.00001 = -0b0.00001×2 ⁻¹ = -0.015625	0xc1 = 1.10.00001 = -0b1.00001×2 ⁰ = -1.03125
0x02 = 0.00.00010 = +0b0.00010×2 ⁻¹ = 0.03125	0x42 = 0.10.00010 = +0b1.00010×2 ⁰ = 1.0625	0x82 = 1.00.00010 = -0b0.00010×2 ⁻¹ = -0.03125	0xc2 = 1.10.00010 = -0b1.00010×2 ⁰ = -1.0625
0x03 = 0.00.00011 = +0b0.00011×2 ⁻¹ = 0.046875	0x43 = 0.10.00011 = +0b1.00011×2 ⁰ = 1.09375	0x83 = 1.00.00011 = -0b0.00011×2 ⁻¹ = -0.046875	0xc3 = 1.10.00011 = -0b1.00011×2 ⁰ = -1.09375
0x04 = 0.00.00100 = +0b0.00100×2 ⁻¹ = 0.0625	0x44 = 0.10.00100 = +0b1.00100×2 ⁰ = 1.125	0x84 = 1.00.00100 = -0b0.00100×2 ⁻¹ = -0.0625	0xc4 = 1.10.00100 = -0b1.00100×2 ⁰ = -1.125
0x05 = 0.00.00101 = +0b0.00101×2 ⁻¹ = 0.078125	0x45 = 0.10.00101 = +0b1.00101×2 ⁰ = 1.15625	0x85 = 1.00.00101 = -0b0.00101×2 ⁻¹ = -0.078125	0xc5 = 1.10.00101 = -0b1.00101×2 ⁰ = -1.15625
0x06 = 0.00.00110 = +0b0.00110×2 ⁻¹ = 0.09375	0x46 = 0.10.00110 = +0b1.00110×2 ⁰ = 1.1875	0x86 = 1.00.00110 = -0b0.00110×2 ⁻¹ = -0.09375	0xc6 = 1.10.00110 = -0b1.00110×2 ⁰ = -1.1875
0x07 = 0.00.00111 = +0b0.00111×2 ⁻¹ = 0.109375	0x47 = 0.10.00111 = +0b1.00111×2 ⁰ = 1.21875	0x87 = 1.00.00111 = -0b0.00111×2 ⁻¹ = -0.109375	0xc7 = 1.10.00111 = -0b1.00111×2 ⁰ = -1.21875
0x08 = 0.00.01000 = +0b0.01000×2 ⁻¹ = 0.125	0x48 = 0.10.01000 = +0b1.01000×2 ⁰ = 1.25	0x88 = 1.00.01000 = -0b0.01000×2 ⁻¹ = -0.125	0xc8 = 1.10.01000 = -0b1.01000×2 ⁰ = -1.25
0x09 = 0.00.01001 = +0b0.01001×2 ⁻¹ = 0.140625	0x49 = 0.10.01001 = +0b1.01001×2 ⁰ = 1.28125	0x89 = 1.00.01001 = -0b0.01001×2 ⁻¹ = -0.140625	0xc9 = 1.10.01001 = -0b1.01001×2 ⁰ = -1.28125
0x0a = 0.00.01010 = +0b0.01010×2 ⁻¹ = 0.15625	0x4a = 0.10.01010 = +0b1.01010×2 ⁰ = 1.3125	0x8a = 1.00.01010 = -0b0.01010×2 ⁻¹ = -0.15625	0xca = 1.10.01010 = -0b1.01010×2 ⁰ = -1.3125
0x0b = 0.00.01011 = +0b0.01011×2 ⁻¹ = 0.171875	0x4b = 0.10.01011 = +0b1.01011×2 ⁰ = 1.34375	0x8b = 1.00.01011 = -0b0.01011×2 ⁻¹ = -0.171875	0xcb = 1.10.01011 = -0b1.01011×2 ⁰ = -1.34375
0x0c = 0.00.01100 = +0b0.01100×2 ⁻¹ = 0.1875	0x4c = 0.10.01100 = +0b1.01100×2 ⁰ = 1.375	0x8c = 1.00.01100 = -0b0.01100×2 ⁻¹ = -0.1875	0xcc = 1.10.01100 = -0b1.01100×2 ⁰ = -1.375
0x0d = 0.00.01101 = +0b0.01101×2 ⁻¹ = 0.203125	0x4d = 0.10.01101 = +0b1.01101×2 ⁰ = 1.40625	0x8d = 1.00.01101 = -0b0.01101×2 ⁻¹ = -0.203125	0xcd = 1.10.01101 = -0b1.01101×2 ⁰ = -1.40625
0x0e = 0.00.01110 = +0b0.01110×2 ⁻¹ = 0.21875	0x4e = 0.10.01110 = +0b1.01110×2 ⁰ = 1.4375	0x8e = 1.00.01110 = -0b0.01110×2 ⁻¹ = -0.21875	0xce = 1.10.01110 = -0b1.01110×2 ⁰ = -1.4375
0x0f = 0.00.01111 = +0b0.01111×2 ⁻¹ = 0.234375	0x4f = 0.10.01111 = +0b1.01111×2 ⁰ = 1.46875	0x8f = 1.00.01111 = -0b0.01111×2 ⁻¹ = -0.234375	0xcf = 1.10.01111 = -0b1.01111×2 ⁰ = -1.46875
0x10 = 0.00.10000 = +0b0.10000×2 ⁻¹ = 0.25	0x50 = 0.10.10000 = +0b1.10000×2 ⁰ = 1.5	0x90 = 1.00.10000 = -0b0.10000×2 ⁻¹ = -0.25	0xd0 = 1.10.10000 = -0b1.10000×2 ⁰ = -1.5
0x11 = 0.00.10001 = +0b0.10001×2 ⁻¹ = 0.265625	0x51 = 0.10.10001 = +0b1.10001×2 ⁰ = 1.53125	0x91 = 1.00.10001 = -0b0.10001×2 ⁻¹ = -0.265625	0xd1 = 1.10.10001 = -0b1.10001×2 ⁰ = -1.53125
0x12 = 0.00.10010 = +0b0.10010×2 ⁻¹ = 0.28125	0x52 = 0.10.10010 = +0b1.10010×2 ⁰ = 1.5625	0x92 = 1.00.10010 = -0b0.10010×2 ⁻¹ = -0.28125	0xd2 = 1.10.10010 = -0b1.10010×2 ⁰ = -1.5625
0x13 = 0.00.10011 = +0b0.10011×2 ⁻¹ = 0.296875	0x53 = 0.10.10011 = +0b1.10011×2 ⁰ = 1.59375	0x93 = 1.00.10011 = -0b0.10011×2 ⁻¹ = -0.296875	0xd3 = 1.10.10011 = -0b1.10011×2 ⁰ = -1.59375
0x14 = 0.00.10100 = +0b0.10100×2 ⁻¹ = 0.3125	0x54 = 0.10.10100 = +0b1.10100×2 ⁰ = 1.625	0x94 = 1.00.10100 = -0b0.10100×2 ⁻¹ = -0.3125	0xd4 = 1.10.10100 = -0b1.10100×2 ⁰ = -1.625
0x15 = 0.00.10101 = +0b0.10101×2 ⁻¹ = 0.328125	0x55 = 0.10.10101 = +0b1.10101×2 ⁰ = 1.65625	0x95 = 1.00.10101 = -0b0.10101×2 ⁻¹ = -0.328125	0xd5 = 1.10.10101 = -0b1.10101×2 ⁰ = -1.65625
0x16 = 0.00.10110 = +0b0.10110×2 ⁻¹ = 0.34375	0x56 = 0.10.10110 = +0b1.10110×2 ⁰ = 1.6875	0x96 = 1.00.10110 = -0b0.10110×2 ⁻¹ = -0.34375	0xd6 = 1.10.10110 = -0b1.10110×2 ⁰ = -1.6875
0x17 = 0.00.10111 = +0b0.10111×2 ⁻¹ = 0.359375	0x57 = 0.10.10111 = +0b1.10111×2 ⁰ = 1.71875	0x97 = 1.00.10111 = -0b0.10111×2 ⁻¹ = -0.359375	0xd7 = 1.10.10111 = -0b1.10111×2 ⁰ = -1.71875
0x18 = 0.00.11000 = +0b0.11000×2 ⁻¹ = 0.375	0x58 = 0.10.11000 = +0b1.11000×2 ⁰ = 1.75	0x98 = 1.00.11000 = -0b0.11000×2 ⁻¹ = -0.375	0xd8 = 1.10.11000 = -0b1.11000×2 ⁰ = -1.75
0x19 = 0.00.11001 = +0b0.11001×2 ⁻¹ = 0.390625	0x59 = 0.10.11001 = +0b1.11001×2 ⁰ = 1.78125	0x99 = 1.00.11001 = -0b0.11001×2 ⁻¹ = -0.390625	0xd9 = 1.10.11001 = -0b1.11001×2 ⁰ = -1.78125
0x1a = 0.00.11010 = +0b0.11010×2 ⁻¹ = 0.40625	0x5a = 0.10.11010 = +0b1.11010×2 ⁰ = 1.8125	0x9a = 1.00.11010 = -0b0.11010×2 ⁻¹ = -0.40625	0xda = 1.10.11010 = -0b1.11010×2 ⁰ = -1.8125
0x1b = 0.00.11011 = +0b0.11011×2 ⁻¹ = 0.421875	0x5b = 0.10.11011 = +0b1.11011×2 ⁰ = 1.84375	0x9b = 1.00.11011 = -0b0.11011×2 ⁻¹ = -0.421875	0xdb = 1.10.11011 = -0b1.11011×2 ⁰ = -1.84375
0x1c = 0.00.11100 = +0b0.11100×2 ⁻¹ = 0.4375	0x5c = 0.10.11100 = +0b1.11100×2 ⁰ = 1.875	0x9c = 1.00.11100 = -0b0.11100×2 ⁻¹ = -0.4375	0xdc = 1.10.11100 = -0b1.11100×2 ⁰ = -1.875
0x1d = 0.00.11101 = +0b0.11101×2 ⁻¹ = 0.453125	0x5d = 0.10.11101 = +0b1.11101×2 ⁰ = 1.90625	0x9d = 1.00.11101 = -0b0.11101×2 ⁻¹ = -0.453125	0xdd = 1.10.11101 = -0b1.11101×2 ⁰ = -1.90625
0x1e = 0.00.11110 = +0b0.11110×2 ⁻¹ = 0.46875	0x5e = 0.10.11110 = +0b1.11110×2 ⁰ = 1.9375	0x9e = 1.00.11110 = -0b0.11110×2 ⁻¹ = -0.46875	0xde = 1.10.11110 = -0b1.11110×2 ⁰ = -1.9375
0x1f = 0.00.11111 = +0b0.11111×2 ⁻¹ = 0.484375	0x5f = 0.10.11111 = +0b1.11111×2 ⁰ = 1.96875	0x9f = 1.00.11111 = -0b0.11111×2 ⁻¹ = -0.484375	0xdf = 1.10.11111 = -0b1.11111×2 ⁰ = -1.96875
0x20 = 0.01.00000 = +0b1.00000×2 ⁻¹ = 0.5	0x60 = 0.11.00000 = +0b1.00000×2 ¹ = 2.0	0xa0 = 1.01.00000 = -0b1.00000×2 ⁻¹ = -0.5	0xe0 = 1.11.00000 = -0b1.00000×2 ¹ = -2.0
0x21 = 0.01.00001 = +0b1.00001×2 ⁻¹ = 0.515625	0x61 = 0.11.00001 = +0b1.00001×2 ¹ = 2.0625	0xa1 = 1.01.00001 = -0b1.00001×2 ⁻¹ = -0.515625	0xe1 = 1.11.00001 = -0b1.00001×2 ¹ = -2.0625
0x22 = 0.01.00010 = +0b1.00010×2 ⁻¹ = 0.53125	0x62 = 0.11.00010 = +0b1.00010×2 ¹ = 2.125	0xa2 = 1.01.00010 = -0b1.00010×2 ⁻¹ = -0.53125	0xe2 = 1.11.00010 = -0b1.00010×2 ¹ = -2.125
0x23 = 0.01.00011 = +0b1.00011×2 ⁻¹ = 0.546875	0x63 = 0.11.00011 = +0b1.00011×2 ¹ = 2.1875	0xa3 = 1.01.00011 = -0b1.00011×2 ⁻¹ = -0.546875	0xe3 = 1.11.00011 = -0b1.00011×2 ¹ = -2.1875
0x24 = 0.01.00100 = +0b1.00100×2 ⁻¹ = 0.5625	0x64 = 0.11.00100 = +0b1.00100×2 ¹ = 2.25	0xa4 = 1.01.00100 = -0b1.00100×2 ⁻¹ = -0.5625	0xe4 = 1.11.00100 = -0b1.00100×2 ¹ = -2.25
0x25 = 0.01.00101 = +0b1.00101×2 ⁻¹ = 0.578125	0x65 = 0.11.00101 = +0b1.00101×2 ¹ = 2.3125	0xa5 = 1.01.00101 = -0b1.00101×2 ⁻¹ = -0.578125	0xe5 = 1.11.00101 = -0b1.00101×2 ¹ = -2.3125
0x26 = 0.01.00110 = +0b1.00110×2 ⁻¹ = 0.59375	0x66 = 0.11.00110 = +0b1.00110×2 ¹ = 2.375	0xa6 = 1.01.00110 = -0b1.00110×2 ⁻¹ = -0.59375	0xe6 = 1.11.00110 = -0b1.00110×2 ¹ = -2.375
0x27 = 0.01.00111 = +0b1.00111×2 ⁻¹ = 0.609375	0x67 = 0.11.00111 = +0b1.00111×2 ¹ = 2.4375	0xa7 = 1.01.00111 = -0b1.00111×2 ⁻¹ = -0.609375	0xe7 = 1.11.00111 = -0b1.00111×2 ¹ = -2.4375
0x28 = 0.01.01000 = +0b1.01000×2 ⁻¹ = 0.625	0x68 = 0.11.01000 = +0b1.01000×2 ¹ = 2.5	0xa8 = 1.01.01000 = -0b1.01000×2 ⁻¹ = -0.625	0xe8 = 1.11.01000 = -0b1.01000×2 ¹ = -2.5
0x29 = 0.01.01001 = +0b1.01001×2 ⁻¹ = 0.640625	0x69 = 0.11.01001 = +0b1.01001×2 ¹ = 2.5625	0xa9 = 1.01.01001 = -0b1.01001×2 ⁻¹ = -0.640625	0xe9 = 1.11.01001 = -0b1.01001×2 ¹ = -2.5625
0x2a = 0.01.01010 = +0b1.01010×2 ⁻¹ = 0.65625	0x6a = 0.11.01010 = +0b1.01010×2 ¹ = 2.625	0xaa = 1.01.01010 = -0b1.01010×2 ⁻¹ = -0.65625	0xea = 1.11.01010 = -0b1.01010×2 ¹ = -2.625
0x2b = 0.01.01011 = +0b1.01011×2 ⁻¹ = 0.671875	0x6b = 0.11.01011 = +0b1.01011×2 ¹ = 2.6875	0xab = 1.01.01011 = -0b1.01011×2 ⁻¹ = -0.671875	0xeb = 1.11.01011 = -0b1.01011×2 ¹ = -2.6875
0x2c = 0.01.01100 = +0b1.01100×2 ⁻¹ = 0.6875	0x6c = 0.11.01100 = +0b1.01100×2 ¹ = 2.75	0xac = 1.01.01100 = -0b1.01100×2 ⁻¹ = -0.6875	0xec = 1.11.01100 = -0b1.01100×2 ¹ = -2.75
0x2d = 0.01.01101 = +0b1.01101×2 ⁻¹ = 0.703125	0x6d = 0.11.01101 = +0b1.01101×2 ¹ = 2.8125	0xad = 1.01.01101 = -0b1.01101×2 ⁻¹ = -0.703125	0xed = 1.11.01101 = -0b1.01101×2 ¹ = -2.8125
0x2e = 0.01.01110 = +0b1.01110×2 ⁻¹ = 0.71875	0x6e = 0.11.01110 = +0b1.01110×2 ¹ = 2.875	0xae = 1.01.01110 = -0b1.01110×2 ⁻¹ = -0.71875	0xee = 1.11.01110 = -0b1.01110×2 ¹ = -2.875
0x2f = 0.01.01111 = +0b1.01111×2 ⁻¹ = 0.734375	0x6f = 0.11.01111 = +0b1.01111×2 ¹ = 2.9375	0xaf = 1.01.01111 = -0b1.01111×2 ⁻¹ = -0.734375	0xef = 1.11.01111 = -0b1.01111×2 ¹ = -2.9375
0x30 = 0.01.10000 = +0b1.10000×2 ⁻¹ = 0.75	0x70 = 0.11.10000 = +0b1.10000×2 ¹ = 3.0	0xb0 = 1.01.10000 = -0b1.10000×2 ⁻¹ = -0.75	0xf0 = 1.11.10000 = -0b1.10000×2 ¹ = -3.0
0x31 = 0.01.10001 = +0b1.10001×2 ⁻¹ = 0.765625	0x71 = 0.11.10001 = +0b1.10001×2 ¹ = 3.0625	0xb1 = 1.01.10001 = -0b1.10001×2 ⁻¹ = -0.765625	0xf1 = 1.11.10001 = -0b1.10001×2 ¹ = -3.0625
0x32 = 0.01.10010 = +0b1.10010×2 ⁻¹ = 0.78125	0x72 = 0.11.10010 = +0b1.10010×2 ¹ = 3.125	0xb2 = 1.01.10010 = -0b1.10010×2 ⁻¹ = -0.78125	0xf2 = 1.11.10010 = -0b1.10010×2 ¹ = -3.125
0x33 = 0.01.10011 = +0b1.10011×2 ⁻¹ = 0.796875	0x73 = 0.11.10011 = +0b1.10011×2 ¹ = 3.1875	0xb3 = 1.01.10011 = -0b1.10011×2 ⁻¹ = -0.796875	0xf3 = 1.11.10011 = -0b1.10011×2 ¹ = -3.1875
0x34 = 0.01.10100 = +0b1.10100×2 ⁻¹ = 0.8125	0x74 = 0.11.10100 = +0b1.10100×2 ¹ = 3.25	0xb4 = 1.01.10100 = -0b1.10100×2 ⁻¹ = -0.8125	0xf4 = 1.11.10100 = -0b1.10100×2 ¹ = -3.25
0x35 = 0.01.10101 = +0b1.10101×2 ⁻¹ = 0.828125	0x75 = 0.11.10101 = +0b1.10101×2 ¹ = 3.3125	0xb5 = 1.01.10101 = -0b1.10101×2 ⁻¹ = -0.828125	0xf5 = 1.11.10101 = -0b1.10101×2 ¹ = -3.3125
0x36 = 0.01.10110 = +0b1.10110×2 ⁻¹ = 0.84375	0x76 = 0.11.10110 = +0b1.10110×2 ¹ = 3.375	0xb6 = 1.01.10110 = -0b1.10110×2 ⁻¹ = -0.84375	0xf6 = 1.11.10110 = -0b1.10110×2 ¹ = -3.375
0x37 = 0.01.10111 = +0b1.10111×2 ⁻¹ = 0.859375	0x77 = 0.11.10111 = +0b1.10111×2 ¹ = 3.4375	0xb7 = 1.01.10111 = -0b1.10111×2 ⁻¹ = -0.859375	0xf7 = 1.11.10111 = -0b1.10111×2 ¹ = -3.4375
0x38 = 0.01.11000 = +0b1.11000×2 ⁻¹ = 0.875	0x78 = 0.11.11000 = +0b1.11000×2 ¹ = 3.5	0xb8 = 1.01.11000 = -0b1.11000×2 ⁻¹ = -0.875	0xf8 = 1.11.11000 = -0b1.11000×2 ¹ = -3.5
0x39 = 0.01.11001 = +0b1.11001×2 ⁻¹ = 0.890625	0x79 = 0.11.11001 = +0b1.11001×2 ¹ = 3.5625	0xb9 = 1.01.11001 = -0b1.11001×2 ⁻¹ = -0.890625	0xf9 = 1.11.11001 = -0b1.11001×2 ¹ = -3.5625
0x3a = 0.01.11010 = +0b1.11010×2 ⁻¹ = 0.90625	0x7a = 0.11.11010 = +0b1.11010×2 ¹ = 3.625	0xba = 1.01.11010 = -0b1.11010×2 ⁻¹ = -0.90625	0xfa = 1.11.11010 = -0b1.11010×2 ¹ = -3.625
0x3b = 0.01.11011 = +0b1.11011×2 ⁻¹ = 0.921875	0x7b = 0.11.11011 = +0b1.11011×2 ¹ = 3.6875	0xbb = 1.01.11011 = -0b1.11011×2 ⁻¹ = -0.921875	0xfb = 1.11.11011 = -0b1.11011×2 ¹ = -3.6875
0x3c = 0.01.11100 = +0b1.11100×2 ⁻¹ = 0.9375	0x7c = 0.11.11100 = +0b1.11100×2 ¹ = 3.75	0xbc = 1.01.11100 = -0b1.11100×2 ⁻¹ = -0.9375	0xfc = 1.11.11100 = -0b1.11100×2 ¹ = -3.75
0x3d = 0.01.11101 = +0b1.11101×2 ⁻¹ = 0.953125	0x7d = 0.11.11101 = +0b1.11101×2 ¹ = 3.8125	0xbd = 1.01.11101 = -0b1.11101×2 ⁻¹ = -0.953125	0xfd = 1.11.11101 = -0b1.11101×2 ¹

C.6 Value Table: P7 (Linear), $p = 7$, $e_{\max} = 0$

0x00 = 0.0.000000 = 0.0	0x40 = 0.1.000000 = +0b1.000000×2 ⁰ = 1.0	0x80 = 1.0.000000 = NaN	0xc0 = 1.1.000000 = -0b1.000000×2 ⁰ = -1.0
0x01 = 0.0.000001 = +0b0.000001×2 ⁰ = 0.015625	0x41 = 0.1.000001 = +0b1.000001×2 ⁰ = 1.015625	0x81 = 1.0.000001 = -0b0.000001×2 ⁰ = -0.015625	0xc1 = 1.1.000001 = -0b1.000001×2 ⁰ = -1.015625
0x02 = 0.0.000010 = +0b0.000010×2 ⁰ = 0.03125	0x42 = 0.1.000010 = +0b1.000010×2 ⁰ = 1.03125	0x82 = 1.0.000010 = -0b0.000010×2 ⁰ = -0.03125	0xc2 = 1.1.000010 = -0b1.000010×2 ⁰ = -1.03125
0x03 = 0.0.000011 = +0b0.000011×2 ⁰ = 0.046875	0x43 = 0.1.000011 = +0b1.000011×2 ⁰ = 1.046875	0x83 = 1.0.000011 = -0b0.000011×2 ⁰ = -0.046875	0xc3 = 1.1.000011 = -0b1.000011×2 ⁰ = -1.046875
0x04 = 0.0.000100 = +0b0.000100×2 ⁰ = 0.0625	0x44 = 0.1.000100 = +0b1.000100×2 ⁰ = 1.0625	0x84 = 1.0.000100 = -0b0.000100×2 ⁰ = -0.0625	0xc4 = 1.1.000100 = -0b1.000100×2 ⁰ = -1.0625
0x05 = 0.0.000101 = +0b0.000101×2 ⁰ = 0.078125	0x45 = 0.1.000101 = +0b1.000101×2 ⁰ = 1.078125	0x85 = 1.0.000101 = -0b0.000101×2 ⁰ = -0.078125	0xc5 = 1.1.000101 = -0b1.000101×2 ⁰ = -1.078125
0x06 = 0.0.000110 = +0b0.000110×2 ⁰ = 0.09375	0x46 = 0.1.000110 = +0b1.000110×2 ⁰ = 1.09375	0x86 = 1.0.000110 = -0b0.000110×2 ⁰ = -0.09375	0xc6 = 1.1.000110 = -0b1.000110×2 ⁰ = -1.09375
0x07 = 0.0.000111 = +0b0.000111×2 ⁰ = 0.109375	0x47 = 0.1.000111 = +0b1.000111×2 ⁰ = 1.109375	0x87 = 1.0.000111 = -0b0.000111×2 ⁰ = -0.109375	0xc7 = 1.1.000111 = -0b1.000111×2 ⁰ = -1.109375
0x08 = 0.0.001000 = +0b0.001000×2 ⁰ = 0.125	0x48 = 0.1.001000 = +0b1.001000×2 ⁰ = 1.125	0x88 = 1.0.001000 = -0b0.001000×2 ⁰ = -0.125	0xc8 = 1.1.001000 = -0b1.001000×2 ⁰ = -1.125
0x09 = 0.0.001001 = +0b0.001001×2 ⁰ = 0.140625	0x49 = 0.1.001001 = +0b1.001001×2 ⁰ = 1.140625	0x89 = 1.0.001001 = -0b0.001001×2 ⁰ = -0.140625	0xc9 = 1.1.001001 = -0b1.001001×2 ⁰ = -1.140625
0x0a = 0.0.001010 = +0b0.001010×2 ⁰ = 0.15625	0x4a = 0.1.001010 = +0b1.001010×2 ⁰ = 1.15625	0x8a = 1.0.001010 = -0b0.001010×2 ⁰ = -0.15625	0xca = 1.1.001010 = -0b1.001010×2 ⁰ = -1.15625
0x0b = 0.0.001011 = +0b0.001011×2 ⁰ = 0.171875	0x4b = 0.1.001011 = +0b1.001011×2 ⁰ = 1.171875	0x8b = 1.0.001011 = -0b0.001011×2 ⁰ = -0.171875	0xcb = 1.1.001011 = -0b1.001011×2 ⁰ = -1.171875
0x0c = 0.0.001100 = +0b0.001100×2 ⁰ = 0.1875	0x4c = 0.1.001100 = +0b1.001100×2 ⁰ = 1.1875	0x8c = 1.0.001100 = -0b0.001100×2 ⁰ = -0.1875	0xcc = 1.1.001100 = -0b1.001100×2 ⁰ = -1.1875
0x0d = 0.0.001101 = +0b0.001101×2 ⁰ = 0.203125	0x4d = 0.1.001101 = +0b1.001101×2 ⁰ = 1.203125	0x8d = 1.0.001101 = -0b0.001101×2 ⁰ = -0.203125	0xcd = 1.1.001101 = -0b1.001101×2 ⁰ = -1.203125
0x0e = 0.0.001110 = +0b0.001110×2 ⁰ = 0.21875	0x4e = 0.1.001110 = +0b1.001110×2 ⁰ = 1.21875	0x8e = 1.0.001110 = -0b0.001110×2 ⁰ = -0.21875	0xce = 1.1.001110 = -0b1.001110×2 ⁰ = -1.21875
0x0f = 0.0.001111 = +0b0.001111×2 ⁰ = 0.234375	0x4f = 0.1.001111 = +0b1.001111×2 ⁰ = 1.234375	0x8f = 1.0.001111 = -0b0.001111×2 ⁰ = -0.234375	0xcf = 1.1.001111 = -0b1.001111×2 ⁰ = -1.234375
0x10 = 0.0.010000 = +0b0.010000×2 ⁰ = 0.25	0x50 = 0.1.010000 = +0b1.010000×2 ⁰ = 1.25	0x90 = 1.0.010000 = -0b0.010000×2 ⁰ = -0.25	0xd0 = 1.1.010000 = -0b1.010000×2 ⁰ = -1.25
0x11 = 0.0.010001 = +0b0.010001×2 ⁰ = 0.265625	0x51 = 0.1.010001 = +0b1.010001×2 ⁰ = 1.265625	0x91 = 1.0.010001 = -0b0.010001×2 ⁰ = -0.265625	0xd1 = 1.1.010001 = -0b1.010001×2 ⁰ = -1.265625
0x12 = 0.0.010010 = +0b0.010010×2 ⁰ = 0.28125	0x52 = 0.1.010010 = +0b1.010010×2 ⁰ = 1.28125	0x92 = 1.0.010010 = -0b0.010010×2 ⁰ = -0.28125	0xd2 = 1.1.010010 = -0b1.010010×2 ⁰ = -1.28125
0x13 = 0.0.010011 = +0b0.010011×2 ⁰ = 0.296875	0x53 = 0.1.010011 = +0b1.010011×2 ⁰ = 1.296875	0x93 = 1.0.010011 = -0b0.010011×2 ⁰ = -0.296875	0xd3 = 1.1.010011 = -0b1.010011×2 ⁰ = -1.296875
0x14 = 0.0.010100 = +0b0.010100×2 ⁰ = 0.3125	0x54 = 0.1.010100 = +0b1.010100×2 ⁰ = 1.3125	0x94 = 1.0.010100 = -0b0.010100×2 ⁰ = -0.3125	0xd4 = 1.1.010100 = -0b1.010100×2 ⁰ = -1.3125
0x15 = 0.0.010101 = +0b0.010101×2 ⁰ = 0.328125	0x55 = 0.1.010101 = +0b1.010101×2 ⁰ = 1.328125	0x95 = 1.0.010101 = -0b0.010101×2 ⁰ = -0.328125	0xd5 = 1.1.010101 = -0b1.010101×2 ⁰ = -1.328125
0x16 = 0.0.010110 = +0b0.010110×2 ⁰ = 0.34375	0x56 = 0.1.010110 = +0b1.010110×2 ⁰ = 1.34375	0x96 = 1.0.010110 = -0b0.010110×2 ⁰ = -0.34375	0xd6 = 1.1.010110 = -0b1.010110×2 ⁰ = -1.34375
0x17 = 0.0.010111 = +0b0.010111×2 ⁰ = 0.359375	0x57 = 0.1.010111 = +0b1.010111×2 ⁰ = 1.359375	0x97 = 1.0.010111 = -0b0.010111×2 ⁰ = -0.359375	0xd7 = 1.1.010111 = -0b1.010111×2 ⁰ = -1.359375
0x18 = 0.0.011000 = +0b0.011000×2 ⁰ = 0.375	0x58 = 0.1.011000 = +0b1.011000×2 ⁰ = 1.375	0x98 = 1.0.011000 = -0b0.011000×2 ⁰ = -0.375	0xd8 = 1.1.011000 = -0b1.011000×2 ⁰ = -1.375
0x19 = 0.0.011001 = +0b0.011001×2 ⁰ = 0.390625	0x59 = 0.1.011001 = +0b1.011001×2 ⁰ = 1.390625	0x99 = 1.0.011001 = -0b0.011001×2 ⁰ = -0.390625	0xd9 = 1.1.011001 = -0b1.011001×2 ⁰ = -1.390625
0x1a = 0.0.011010 = +0b0.011010×2 ⁰ = 0.40625	0x5a = 0.1.011010 = +0b1.011010×2 ⁰ = 1.40625	0x9a = 1.0.011010 = -0b0.011010×2 ⁰ = -0.40625	0xda = 1.1.011010 = -0b1.011010×2 ⁰ = -1.40625
0x1b = 0.0.011011 = +0b0.011011×2 ⁰ = 0.421875	0x5b = 0.1.011011 = +0b1.011011×2 ⁰ = 1.421875	0x9b = 1.0.011011 = -0b0.011011×2 ⁰ = -0.421875	0xdb = 1.1.011011 = -0b1.011011×2 ⁰ = -1.421875
0x1c = 0.0.011100 = +0b0.011100×2 ⁰ = 0.4375	0x5c = 0.1.011100 = +0b1.011100×2 ⁰ = 1.4375	0x9c = 1.0.011100 = -0b0.011100×2 ⁰ = -0.4375	0xdc = 1.1.011100 = -0b1.011100×2 ⁰ = -1.4375
0x1d = 0.0.011101 = +0b0.011101×2 ⁰ = 0.453125	0x5d = 0.1.011101 = +0b1.011101×2 ⁰ = 1.453125	0x9d = 1.0.011101 = -0b0.011101×2 ⁰ = -0.453125	0xdd = 1.1.011101 = -0b1.011101×2 ⁰ = -1.453125
0x1e = 0.0.011110 = +0b0.011110×2 ⁰ = 0.46875	0x5e = 0.1.011110 = +0b1.011110×2 ⁰ = 1.46875	0x9e = 1.0.011110 = -0b0.011110×2 ⁰ = -0.46875	0xde = 1.1.011110 = -0b1.011110×2 ⁰ = -1.46875
0x1f = 0.0.011111 = +0b0.011111×2 ⁰ = 0.484375	0x5f = 0.1.011111 = +0b1.011111×2 ⁰ = 1.484375	0x9f = 1.0.011111 = -0b0.011111×2 ⁰ = -0.484375	0xdf = 1.1.011111 = -0b1.011111×2 ⁰ = -1.484375
0x20 = 0.0.100000 = +0b0.100000×2 ⁰ = 0.5	0x60 = 0.1.100000 = +0b1.100000×2 ⁰ = 1.5	0xa0 = 1.0.100000 = -0b0.100000×2 ⁰ = -0.5	0xe0 = 1.1.100000 = -0b1.100000×2 ⁰ = -1.5
0x21 = 0.0.100001 = +0b0.100001×2 ⁰ = 0.515625	0x61 = 0.1.100001 = +0b1.100001×2 ⁰ = 1.515625	0xa1 = 1.0.100001 = -0b0.100001×2 ⁰ = -0.515625	0xe1 = 1.1.100001 = -0b1.100001×2 ⁰ = -1.515625
0x22 = 0.0.100010 = +0b0.100010×2 ⁰ = 0.53125	0x62 = 0.1.100010 = +0b1.100010×2 ⁰ = 1.53125	0xa2 = 1.0.100010 = -0b0.100010×2 ⁰ = -0.53125	0xe2 = 1.1.100010 = -0b1.100010×2 ⁰ = -1.53125
0x23 = 0.0.100011 = +0b0.100011×2 ⁰ = 0.546875	0x63 = 0.1.100011 = +0b1.100011×2 ⁰ = 1.546875	0xa3 = 1.0.100011 = -0b0.100011×2 ⁰ = -0.546875	0xe3 = 1.1.100011 = -0b1.100011×2 ⁰ = -1.546875
0x24 = 0.0.100100 = +0b0.100100×2 ⁰ = 0.5625	0x64 = 0.1.100100 = +0b1.100100×2 ⁰ = 1.5625	0xa4 = 1.0.100100 = -0b0.100100×2 ⁰ = -0.5625	0xe4 = 1.1.100100 = -0b1.100100×2 ⁰ = -1.5625
0x25 = 0.0.100101 = +0b0.100101×2 ⁰ = 0.578125	0x65 = 0.1.100101 = +0b1.100101×2 ⁰ = 1.578125	0xa5 = 1.0.100101 = -0b0.100101×2 ⁰ = -0.578125	0xe5 = 1.1.100101 = -0b1.100101×2 ⁰ = -1.578125
0x26 = 0.0.100110 = +0b0.100110×2 ⁰ = 0.59375	0x66 = 0.1.100110 = +0b1.100110×2 ⁰ = 1.59375	0xa6 = 1.0.100110 = -0b0.100110×2 ⁰ = -0.59375	0xe6 = 1.1.100110 = -0b1.100110×2 ⁰ = -1.59375
0x27 = 0.0.100111 = +0b0.100111×2 ⁰ = 0.609375	0x67 = 0.1.100111 = +0b1.100111×2 ⁰ = 1.609375	0xa7 = 1.0.100111 = -0b0.100111×2 ⁰ = -0.609375	0xe7 = 1.1.100111 = -0b1.100111×2 ⁰ = -1.609375
0x28 = 0.0.101000 = +0b0.101000×2 ⁰ = 0.625	0x68 = 0.1.101000 = +0b1.101000×2 ⁰ = 1.625	0xa8 = 1.0.101000 = -0b0.101000×2 ⁰ = -0.625	0xe8 = 1.1.101000 = -0b1.101000×2 ⁰ = -1.625
0x29 = 0.0.101001 = +0b0.101001×2 ⁰ = 0.640625	0x69 = 0.1.101001 = +0b1.101001×2 ⁰ = 1.640625	0xa9 = 1.0.101001 = -0b0.101001×2 ⁰ = -0.640625	0xe9 = 1.1.101001 = -0b1.101001×2 ⁰ = -1.640625
0x2a = 0.0.101010 = +0b0.101010×2 ⁰ = 0.65625	0x6a = 0.1.101010 = +0b1.101010×2 ⁰ = 1.65625	0xaa = 1.0.101010 = -0b0.101010×2 ⁰ = -0.65625	0xea = 1.1.101010 = -0b1.101010×2 ⁰ = -1.65625
0x2b = 0.0.101011 = +0b0.101011×2 ⁰ = 0.671875	0x6b = 0.1.101011 = +0b1.101011×2 ⁰ = 1.671875	0xab = 1.0.101011 = -0b0.101011×2 ⁰ = -0.671875	0xeb = 1.1.101011 = -0b1.101011×2 ⁰ = -1.671875
0x2c = 0.0.101100 = +0b0.101100×2 ⁰ = 0.6875	0x6c = 0.1.101100 = +0b1.101100×2 ⁰ = 1.6875	0xac = 1.0.101100 = -0b0.101100×2 ⁰ = -0.6875	0xec = 1.1.101100 = -0b1.101100×2 ⁰ = -1.6875
0x2d = 0.0.101101 = +0b0.101101×2 ⁰ = 0.703125	0x6d = 0.1.101101 = +0b1.101101×2 ⁰ = 1.703125	0xad = 1.0.101101 = -0b0.101101×2 ⁰ = -0.703125	0xed = 1.1.101101 = -0b1.101101×2 ⁰ = -1.703125
0x2e = 0.0.101110 = +0b0.101110×2 ⁰ = 0.71875	0x6e = 0.1.101110 = +0b1.101110×2 ⁰ = 1.71875	0xae = 1.0.101110 = -0b0.101110×2 ⁰ = -0.71875	0xee = 1.1.101110 = -0b1.101110×2 ⁰ = -1.71875
0x2f = 0.0.101111 = +0b0.101111×2 ⁰ = 0.734375	0x6f = 0.1.101111 = +0b1.101111×2 ⁰ = 1.734375	0xaf = 1.0.101111 = -0b0.101111×2 ⁰ = -0.734375	0xef = 1.1.101111 = -0b1.101111×2 ⁰ = -1.734375
0x30 = 0.0.110000 = +0b0.110000×2 ⁰ = 0.75	0x70 = 0.1.110000 = +0b1.110000×2 ⁰ = 1.75	0xb0 = 1.0.110000 = -0b0.110000×2 ⁰ = -0.75	0xf0 = 1.1.110000 = -0b1.110000×2 ⁰ = -1.75
0x31 = 0.0.110001 = +0b0.110001×2 ⁰ = 0.765625	0x71 = 0.1.110001 = +0b1.110001×2 ⁰ = 1.765625	0xb1 = 1.0.110001 = -0b0.110001×2 ⁰ = -0.765625	0xf1 = 1.1.110001 = -0b1.110001×2 ⁰ = -1.765625
0x32 = 0.0.110010 = +0b0.110010×2 ⁰ = 0.78125	0x72 = 0.1.110010 = +0b1.110010×2 ⁰ = 1.78125	0xb2 = 1.0.110010 = -0b0.110010×2 ⁰ = -0.78125	0xf2 = 1.1.110010 = -0b1.110010×2 ⁰ = -1.78125
0x33 = 0.0.110011 = +0b0.110011×2 ⁰ = 0.796875	0x73 = 0.1.110011 = +0b1.110011×2 ⁰ = 1.796875	0xb3 = 1.0.110011 = -0b0.110011×2 ⁰ = -0.796875	0xf3 = 1.1.110011 = -0b1.110011×2 ⁰ = -1.796875
0x34 = 0.0.110100 = +0b0.110100×2 ⁰ = 0.8125	0x74 = 0.1.110100 = +0b1.110100×2 ⁰ = 1.8125	0xb4 = 1.0.110100 = -0b0.110100×2 ⁰ = -0.8125	0xf4 = 1.1.110100 = -0b1.110100×2 ⁰ = -1.8125
0x35 = 0.0.110101 = +0b0.110101×2 ⁰ = 0.828125	0x75 = 0.1.110101 = +0b1.110101×2 ⁰ = 1.828125	0xb5 = 1.0.110101 = -0b0.110101×2 ⁰ = -0.828125	0xf5 = 1.1.110101 = -0b1.110101×2 ⁰ = -1.828125
0x36 = 0.0.110110 = +0b0.110110×2 ⁰ = 0.84375	0x76 = 0.1.110110 = +0b1.110110×2 ⁰ = 1.84375	0xb6 = 1.0.110110 = -0b0.110110×2 ⁰ = -0.84375	0xf6 = 1.1.110110 = -0b1.110110×2 ⁰ = -1.84375
0x37 = 0.0.110111 = +0b0.110111×2 ⁰ = 0.859375	0x77 = 0.1.110111 = +0b1.110111×2 ⁰ = 1.859375	0xb7 = 1.0.110111 = -0b0.110111×2 ⁰ = -0.859375	0xf7 = 1.1.110111 = -0b1.110111×2 ⁰ = -1.859375
0x38 = 0.0.111000 = +0b0.111000×2 ⁰ = 0.875	0x78 = 0.1.111000 = +0b1.111000×2 ⁰ = 1.875	0xb8 = 1.0.111000 = -0b0.111000×2 ⁰ = -0.875	0xf8 = 1.1.111000 = -0b1.111000×2 ⁰ = -1.875
0x39 = 0.0.111001 = +0b0.111001×2 ⁰ = 0.890625	0x79 = 0.1.111001 = +0b1.111001×2 ⁰ = 1.890625	0xb9 = 1.0.111001 = -0b0.111001×2 ⁰ = -0.890625	0xf9 = 1.1.111001 = -0b1.111001×2 ⁰ = -1.890625
0x3a = 0.0.111010 = +0b0.111010×2 ⁰ = 0.90625	0x7a = 0.1.111010 = +0b1.111010×2 ⁰ = 1.90625	0xba = 1.0.111010 = -0b0.111010×2 ⁰ = -0.90625	0xfa = 1.1.111010 = -0b1.111010×2 ⁰ = -1.90625
0x3b = 0.0.111011 = +0b0.111011×2 ⁰ = 0.921875	0x7b = 0.1.111011 = +0b1.111011×2 ⁰ = 1.921875	0xbb = 1.0.111011 = -0b0.111011×2 ⁰ = -0.921875	0xfb = 1.1.111011 = -0b1.

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