IEEE Working Group P3109 Interim Report on Binary Floating-point Formats for Machine Learning

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Contents

1	Con	tributors	4
2	Intro	oduction	5
	2.1	Typographical conventions and notation	5
	2.2	Scope	5
_	_		_
3	Forn		6
	3.1	Format parameters and value sets	6
		3.1.1 Computation of bias	6
		3.1.2 Computation of bias, $SE = 1 \dots \dots \dots \dots \dots \dots \dots \dots \dots$	7
		3.1.3 Computation of bias, $SE = 0$	7
		3.1.4 Observations on P3109 value sets	7
	3.2	Encodings and special values	8
	3.3	Subnormals	8
	3.4	Not a number (NaN)	9
	3.5	Zero	9
	3.6		10
	3.7	Extremal values for $K=8$	10
	3.8	Equivalences	10
4	0		11
4	_		11
	4.1		12
	4.2		12
			12
			12
	4.3		13
	4.4		13
	4.5	1	14
	4.6		15
			15
		4.6.2 Project	16
		4.6.3 RoundToPrecision	17
			18
		4.6.5 Encode	19
	4.7	Conversion operations	20
		4.7.1 Specification of IEEE Std 754 formats	20
		4.7.2 Conversion from IEEE Std 754 formats to P3109	21
		4.7.3 Conversion from P3109 to IEEE Std 754	22
			23
	4.8		24
		<u>.</u>	24
			25
		7 & 1	26
			27

		4.8.5 Scaled addition	28
		4.8.6 Scaled multiplication	29
	4.9	Mixed IEEE Std 754 and P3109 operations	30
		4.9.1 Scaled Fused Multiply Add	31
	4.10	Comparisons, predicates, and classification	32
		4.10.1 Minimum and Maximum	32
		4.10.2 Comparisons	33
		4.10.3 Predicates and classification	34
		4.10.4 Classifier operation	35
		4.10.5 Total order predicate	36
		4.10.6 Comparison predicates	37
Аp	pendi	ices	38
A	Ratio	onales	38
	A.1	Use of infinity in computation of attention masks	38
	A.2		38
			39
		A.3.1 binary8p3	39
		A.3.2 binary8p4	39
			39
		* 1	39
В	Exte	rnal Formats	40
C	8-bit	: Value Tables	40
•			41
	C.2	·	42
			 43
	C.4	-,	44
	C.5		 45
	C.6	-,,	46
			47

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2 Introduction

This document represents ongoing discussions and current matters of consensus from IEEE Working Group P3109, "Standard for Arithmetic Formats for Machine Learning". The Project Authorization Request (PAR) for P3109 defines the scope, need, and stakeholders as follows:

Scope of proposed standard: This standard defines a binary arithmetic and data format for machine learning-optimized domains. It also specifies the default handling of exceptions that occur in this arithmetic. This standard provides a consistent and flexible arithmetic framework optimized for Machine Learning Systems (MLS) in hardware and/or software implementations to minimize the work required to make MLS interoperable with each other, as well as other dependent systems. This standard is aligned with IEEE Std 754-2019 for Floating-Point Arithmetic.

Need for this Work: Machine Learning Systems have different arithmetic requirements from most other domains. Precisions tend to be lower, and accuracy is measured in dimensions other than just numerical (e.g. inference accuracy). Furthermore, machine learning systems are often integrated into mission-critical and safety-critical systems. With no standards specifically addressing these needs, Machine Learning Systems are built with inconsistent expectations and assumptions that hinder the compatibility and reuse of machine learning hardware, software, and training data.

Stakeholders for the Standard: System developers, vendors, and users of machine learning applications across many industries and interests including but not limited to computation, storage, medical, telecommunications, e-commerce, fleet management, automotive, robotics, and security.

2.1 Typographical conventions and notation

Bold text describes the decisions and specifications of this document.

Text that is not in boldface is background material, typically providing rationale and arguments that represent discussions of the working group leading to a decision and specification.

2.2 Scope

This document specifies compact floating-point interchange formats (binary formats) and associated operations.

Binary formats are parameterized by their width in bits and their precision—the number of bits in the true significand (which is one more than the number of bits in the trailing significand).

The 8-bit formats defined herein shall be referred to as "binary8" formats, and further qualified by precision yielding names "binary8pP" for values $1 \le P \le 7$.

For example, "binary8p3" is an 8-bit format with 1 sign bit, 5 exponent bits and 3 bits of precision (of which only two need to be explicitly represented).

This version of the interim report covers interchange formats and scalar operations including rounding with saturation modes and conversion between P3109 and IEEE Std 754. vector operations, block formats, stochastic rounding, and conversion between P3109 and BFloat16 are not discussed here. These topics may be included in a later version.

3 Formats

This section describes P3109 formats, and the set of values that such formats shall represent.

The universe of values in existing floating-point usage is the finite reals, the non-finite values positive and negative infinity (Inf, -Inf), the value negative zero (-0), and not-a-number values (NaN, NaN₁, ...), subscripted by NaN payload.

A K-bit binary floating-point format \mathcal{F} comprises: the *value set*: a subset $\mathcal{V}_{\mathcal{F}}$ of the universe of values; and an *encoding*: a mapping from integers $0 \dots 2^K - 1$ to $\mathcal{V}_{\mathcal{F}}$.

3.1 Format parameters and value sets

The finite floating-point numbers representable with a binary format are determined by two format-defining parameters:

- Storage width K, the total size of the format in bits
- Precision P, the number of bits in the significand including the implicit leading bit.

All other parameters, such as the exponent of the largest finite value emax, are derived from the format-defining parameters.

IEEE Std 754-2019 includes the radix B and the minimum exponent emin in a list of format-defining parameters, this document excludes both of them for these two reasons:

- This document covers binary (radix 2) formats only, so B is not a format parameter.
- The quantity emin is determined by P and emax; it cannot be varied independently, so it cannot be a formatdefining parameter.

P3109 formats shall be defined by the parameters of storage width K, and precision P, where $1 \leq P < K$

In IEEE Std 754, emax was set for all defined formats to be $2^{W-1} - 1$, where W is the exponent field width in bits. In this document, this convention is formalized: emax is a fixed function of P, written emax(K, P), with the formula following IEEE Std 754, noting that W = K - P.

P3109 formats shall define emax(K, P) to be $2^{K-P-1} - 1$

3.1.1 Computation of bias

The choice of emax for a given format then determines the exponent bias for that format. The bias is chosen so that the exponent of the largest finite value is emax.

For IEEE Std 754 formats, the largest finite value corresponds to an exponent field which has all but the zeroth bit set (e.g. 11110 for Binary16), because all of the values with all-bits-one exponents are occupied by non-finite values (Not-a-Numbers or Infinities). This derived parameter of a format is termed *all-special exponent*, and denoted by the symbol SE, where SE = 1 indicates that all-bits-one exponent fields are entirely occupied by special values. For P3109 values, the all-bits-one exponent contains only one special value (\pm Inf) and hence SE = 0 unless P = 1. Hence, for P3109, SE = (P = 1).

Table 1: Parameters for binary formats

	Parameter	Derived		b	inary	8pP,	K = 8	, P =		IEEI	E754-20	19, K =
Symbol	Description	Value	7	6	5	4	3	2	1	16	32	64
K P	storage (bits) precision (bits)	K P	8 7	8 6	8 5	8 4	8 3	8 2	8 1	16 11	32 24	64 53
S W	sign (bits) exponent (bits)	1 K – P	1 1	1 2	1 3	1 4	1 5	1 6	1 7	1 5	1 8	1 11
T	trailing significand (bits)	P-1	6	5	4	3	2	1	0	10	23	52
SE emax	all-special exponent maximum exponent	$\begin{array}{c c} & SE \\ 2^{W-1} - 1 \end{array}$	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0 1	0	0 7	0 15	0 31	1 63	1 15	1 127	1 1023
emin bias	minimum exponent exponent bias	$\begin{array}{c} SE - emax \\ 1 - emin \end{array}$	0	-1 2	-3 4	-7 8	-15 16	-31 32	-62 63	-14 15	-126 127	-1022 1023

Format-defining parameters in bold, derived parameters in normal font. Adapted from Table 3.5 of IEEE Std 754-2019, and extended to include the binary8pP formats. Concepts are explained in detail in this section.

3.1.2 Computation of bias, SE = 1

With P3109 formats where P = 1, in common with IEEE Std 754, the biased exponent of the largest finite value is $2^W - 2$, from which bias should be defined so that

$$(2^W - 2) - bias = emax$$

Rearranging, we obtain the following

bias =
$$(2^{W} - 2) - (2^{W-1} - 1) = 2 \cdot (2^{W-1} - 1) - (2^{W-1} - 1) = 2^{W-1} - 1 = \text{emax}$$

Hence bias = emax.

3.1.3 Computation of bias, SE = 0

For the binary8 formats in this document where P > 1, only one of the values that has exponents with all-bits-one is non-finite ($\pm Inf$), so the biased exponent of the largest finite value is $2^W - 1$. Hence the bias calculation becomes

bias =
$$(2^{W} - 1) - (2^{W-1} - 1) = 2^{W-1} - 1 + 1 = \text{emax} + 1$$

As, by formula, emax is odd, the bias term in the P > 1 formats is typically even, yielding a more symmetrical range, where emin = -emax.

3.1.4 Observations on P3109 value sets

Table 1 shows some properties of the P3109 value sets for K = 8.

For $P \ge 1$, the value sets are subsets of the IEEE Std 754 Binary32 value set. For $P \ge 3$, the binary8pP value sets are also subsets of the IEEE Std 754 Binary16 value set.

The precision P is to be strictly less than K, hence formats where P = K are not defined in this document. Rationale: strictly following Table 1 would yield emax $= -\frac{1}{2}$ which means all ordinary values are irrational. Rounding this computation upward yields emax = 0 and bias = 1, where all representations within the format are subnormal, with the consequence that the value sets and encodings for P = K - 1 and P = K are identical except for a scaling factor of 1/2.

The following notes from IEEE Std 754-2019 have not been found to apply to the definitions in this document:

- "For binary formats, the precision [P] should be at least 3, as some numerical properties do not hold for lower precisions."
- "Similarly, emax should be at least 2 to support the operations listed in 9.2. [sin/cos/exp/log/etc]"

3.2 Encodings and special values

Encodings are mappings from integers $0...2^{K} - 1$ to the value set, and are defined in §4.6.5 below.

Values are considered either "special" or "ordinary". Encodings of the special values, shared by all P3109 formats, are shown in Table 2. P3109 formats have only a single NaN, located at the position that -0 would occupy in an analogous IEEE-754 encoding, providing an increased range. The ordinary values consist of the normal and subnormal values and zero.

Table 2: Special value encodings

Special Value	Symbol	Code point	Code point $(K = 8)$
Positive Infinity	Inf	$2^{K-1} - 1$ $2^{K} - 1$ 2^{K-1}	0×7F
Negative Infinity	-Inf		0×FF
Not a Number	NaN		0×80

These mappings are shared by all P3109 formats with bit-width K.

3.3 Subnormals

P3109 value sets shall include subnormals.

IEEE Std 754 value sets include subnormals. A value with trailing significand field T and exponent field E is interpreted as $1.T \times 2^{E-\text{bias}}$ except when all bits of the exponent bitfield are 0, in which case the value is $0.T \times 2^{\text{emin}}$.

Subnormal numbers extend the dynamic range of floating-point values and induce equal quantization steps close to zero. They can be useful when training models, where it is common to represent near-zero values for gradients. Subnormals can also be useful to represent random values drawn from certain distributions. For example, model weights are initialized to small random values at training. Subnormals are uniformly spaced around zero, and values near zero are more probable values drawn from Gaussian-like distributions. Finally, formats with narrow exponent widths necessarily have a limited range; subnormals extend this range by a power of 2 for every bit in the trailing significand.

3.4 Not a number (NaN)

P3109 value sets shall include exactly one NaN, encoded as 2^{K-1}, which shall not signal.

Many other floating-point formats define several NaN values which are returned from operations with results outside the set of values, e.g., DIV(0,0), or ADD(+Inf,-Inf). Multiple NaN encodings are used in other formats to allow different exceptional conditions to be distinguished.

In the context of machine learning systems, uses of NaN include:

- Debugging of code running on accelerator hardware. In A.I. accelerators, exceptions may be difficult or expensive
 to convey back to user code, so it is common practice to allow NaN values to propagate through calculations to
 indicate that an error has occurred.
- Use as a sentinel value. In some datasets, for example, where individual element values may be missing or out of range, a sentinel may be used to record the position of these values. In many cases, this will require less memory than storing such information out-of-band, such as in a coordinate-list (COO) format array. In some cases, \pm Inf can be used as a missing value, but given the restricted range of P3109 formats, it is likely that infinity shall be used as a separate indicator of rounding from values outside of the finite range.
- The use of multiple NaN payloads is known in statistical code (e.g. the R system has NaN and N/A), but it is not widely used. In the context of P3109, supporting multiple NaN swould reduce the already limited encoding space (e.g., occupying all code points where the exponent field is all ones, thereby reducing dynamic range) and would likely add additional hardware complexity.

3.5 Zero

P3109 formats shall have exactly one zero, encoded as the integer 0. This zero value is non-negative.

The inclusion of negative zero (-0) would incur the cost of an additional code point. Given the decision to encode only a single NaN, placing that NaN at the negative zero code point enables the strictly positive and strictly negative number ranges to be symmetric.

A key rationale for including -0 in IEEE Std 754 was the consistent implementation of branch cuts in the atan2 function [1, 2]. Although the atan function is common in deep learning, it is generally used as an activation function, rather than a trigonometric operation, and the atan2 function is rare, if not unknown, in deep learning applications. Hence, it is not expected that this standard shall define either atan or atan2.

A secondary reason for providing -0 is the hardware simplification offered by its presence in the implementation of sign/magnitude arithmetic. However, the existence of in-market implementations is evidence that the small hardware simplification has not been sufficient to balance the loss of one code point.

It might be considered that the use of integer comparisons in sorting would argue against placing NaN at the negative zero code point. For example, the JAX machine learning framework is known to sort using integer comparison [3]. However, such sorting still requires O(n) prepossessing and postprocessing steps to enable the use of twos-complement integer comparison, and already has special treatment of NaN and -0, so eliminating -0 and placing NaN in the -0 position imposes negligible additional burden. Although sorting using comparison operations is undefined in the presence of NaN s, existing practice is to sort NaN susing totalOrder.

3.6 Infinities

P3109 formats shall include positive and negative infinities, encoded as $2^{K-1} - 1$ and $2^K - 1$, respectively.

This decision causes a reduction in dynamic range (252 values rather than 254 for binary8, for example), while offering improved numerical robustness in important machine learning use cases.

Examples of such usage are:

- Mask values, for example, in Transformer models in machine learning. See §A.1 for more detailed discussion on this usage.
- Representation of overflow, for example, to adjust dynamic loss scaling factors [4]. Existing implementations offer several behaviors on overflow: overflow to infinity, saturation to MaxFloat, and overflow to NaN. The existence of a code point for infinity allows any of these options to be implemented in a given instantiation, while removing the code point removes the possibility of implementing the first.

3.7 Extremal values for K=8

Table 3: Extremal values

Format	minSubnormal	maxSubnormal	minNormal	maxNormal
binary8p1	N/A	N/A	1×2^{-62}	1×2^{63}
binary8p2	1×2^{-32}	1×2^{-32}	1×2^{-31}	1×2^{31}
binary8p3	1×2^{-17}	$3/2 \times 2^{-16}$	1×2^{-15}	$3/2 \times 2^{15}$
binary8p4	1×2^{-10}	$7/4 \times 2^{-8}$	1×2^{-7}	$7/4 \times 2^{7}$
binary8p5	1×2^{-7}	$15/8 \times 2^{-4}$	1×2^{-3}	$15/8 \times 2^{3}$
binary8p6	1×2^{-6}	$31/16 \times 2^{-2}$	1×2^{-1}	$31/16 \times 2^{1}$
binary8p7	1×2^{-6}	$63/32 \times 2^{-1}$	1×2^0	$63/32 \times 2^{0}$

It is practical to list extremal finite values defined by the binary8 formats. Following IEEE Std 754-2019 naming patterns, we adopt: $\max Normal(\tau), \min Normal(\tau), \min Subnormal(\tau)$ where τ is a binary8 format. For example: $\max Normal(binary8p4) = 7/4 \times 2^7$ and $\min Normal(binary8p5) = 1 \times 2^{-3}$.

Table 3 shows the extremal values for $1 \le P \le 7$. For reference, section C provides complete tables of 8-bit values.

3.8 Equivalences

The P=K-1 formats are equivalent to a signed-magnitude fixed-point integer, except there are code points reserved for NaN and $\pm Inf$.

The P=1 formats are "purely exponential" formats, where all values are of the form 2^n , excepting 0, NaN, $\pm Inf$.

4 Operations

This section defines the *behavior* (with no constraint as to the implementation) of operations which P3109 systems may provide. Such operations include:

- conversion between P3109 formats and between P3109 formats and IEEE-754 formats.
- · comparison, classification, and informational operations
- · addition, multiplication and fused multiply add

In the definitions of the above operations, certain mathematical *functions* are also defined. We emphasize that the definitions in this document are specifications of behavior, not implementation. All arithmetic represented as operating on extended real values is to be interpreted in the usual mathematical sense.

An implementation of any of the operations defined herein is conforming if it computes the same output as the defined operation, for all possible inputs. This may be attested by any proof method, including direct computation.

As defined above, a K-bit P3109 floating-point value (referred to in general as a $P3109 \ value$) is encoded by an integer in the range 0 to 2^K-1 . Operation specifications operate on such values using integer arithmetic (e.g., divide and modulo) operations. Implementations may perform these operations in any equivalent manner, for example bit shifting and masking.

For arithmetic operations, an implementation may provide an α -approximate implementation. Such an implementation will compute values whose maximum difference from the defined outputs, over all inputs producing finite outputs, does not exceed α units in the last place. This may be attested by any proof method, including direct computation.

4.1 Operation variants and superset specifications

Each operation definition in this document is *parameterized*. Example parameters might include input and output formats, rounding modes and saturation modes. In addition operand types may be specified as if to infinite precision (e.g. s in the template definition below is defined as an integer). The set of variants so defined for a given operation is called a *superset specification*.

No implementation is required to provide all variants of a given operation, but rather should clearly define the implemented variants.

It is required that the use of an operation name defined in this document, in the context of declaration of P3109 compliance, specify precisely the variants implemented, and that the name be used only for variants which exactly follow these specifications.

For example, an implementation might declare as follows. (See later sections for definitions of terms in this example.)

"This implementation conforms to P3109, providing the following operation variants:

```
ConvertToP3109, \phi in {Binary16, Binary32}, f in {binary8p3, binary8p4, binary8p5} AddScaled, with s_x=0, s_y\in\{-128\dots127\}, \{f_x,f_y,f_z\}\subset\{binary8p3, binary8p4, binary8p5} MultiplyScaled, with s\in\{-32\dots32\}
```

In all cases, provided projection modes π obey $\mathsf{Rnd}_\pi \in \{\mathsf{NearestTiesToEven}, \, \mathsf{NearestTiesToAway}\}$ and $\mathsf{Sat}_\pi \in \{\mathsf{SatFinite}, \mathsf{OvfInf}\}$ "

This example is truncated—realistic compliance declarations might run to many pages. Such declarations may be compressed by defining common *profiles*, outside of the scope of this current document.

4.2 Notation and definitions

4.2.1 Mathematical notations

We denote by $\mathbb{1}[b]$ the value 1 if b = True, or 0 if b = False.

lsEven(I) is true if integer I is even, false otherwise.

Integer division is denoted by $x \div y$.

Comments are introduced with an em-dash, and are right-justified

—An example comment

4.2.2 The set of extended reals

The set of *extended reals* is the set $\mathbb{R} \cup \{-\infty, \infty\}$ of real numbers augmented with positive and negative infinity, also known as the "affinely extended real numbers". In common with existing mathematical treatments, there is no negative zero in this set. In the extended reals, certain operations, such as $\infty - \infty$, are *undefined*. The definitions in this specification are constructed such that no operation on extended real quantities produces an undefined result.

Operation specifications will, in general, convert floating-point operands to extended real values in order to define their behaviors.

4.3 Projection specifications

Operations on P3109 values are defined via conversion to extended real values, on which the mathematical operation is performed, before conversion back to the appropriate P3109 range. In general, operation results will not be exact P3109 values, and hence will be *projected* into the P3109 range via rounding and overflow handling. A *projection specification* is a pair (rounding mode, saturation mode). For a given projection specification π , these are written Rnd_{π} , Sat_{π} .

The defined rounding modes are as follows. The precise specifications of these modes are in the function RoundToPrecision (§4.6.2):

NearestTiesToEven Round to nearest, ties to even

NearestTiesToAway Round to nearest, ties away from zero

TowardPositive Round toward positive Round toward negative TowardZero Round toward zero

Values are first rounded to the target precision, with exponent unbounded above. Those which are then outside the maximum value in the target format are then treated according to the saturation mode.

The defined saturation modes are as follows. The precise specifications of these modes are in the function Saturate (§4.6.4):

SatMax All return values are clamped to the representable finite range.

SatFinite Finite out-of-range values are clamped to the representable finite range, infinities are preserved.

Ovflnf Out-of-range values are replaced with extreme value, positive or negative infinity as indicated by the

rounding mode.

4.4 Non-requirement for operator side effects

The operator definitions herein describe no side effects, such as the setting of flags, or the triggering of interrupts, and hence do not return values other than the defined return value. Typically NaN is returned when input values are out of range (e.g. $\log(-1.0)$). When saturation is specified, there is no direct mechanism to distinguish overflowed values from values which round to the format's maximum value. An implementation which has side effects will still conform to this specification providing its return value on all inputs matches the definitions herein.

4.5 Operator definition template

Operations are defined according to the following template:

```
Signature
```

```
Operator _f(x,s) \to Z —Naming the operator, its parameters, operands and result.

Parameters —Parameters specify a family of related operations f: format, precision \mathsf{P}_f
```

Operands

```
x:P3109 value, in format f s:Integer scale
```

Output

```
Z : extended real value or NaN
```

-Result value and type

—An ordered sequence of pattern-matching declarations.

Behavior

```
\begin{array}{lll} \mathsf{Operator}(\mathsf{NaN},0) \to \mathsf{NaN} & \qquad & -\mathsf{Exact} \ \mathsf{pattern:} \ \mathsf{only} \ \mathsf{the} \ \mathsf{provided} \ \mathsf{operands} \ \mathsf{match.} \\ \mathsf{Operator}(x \in \{\mathsf{-Inf},\mathsf{Inf}\},0) \to x & \qquad & -\mathsf{Match} \ \mathsf{for} \ \mathsf{all} \ x \ \mathsf{values} \ \mathsf{in} \ \mathsf{the} \ \mathsf{given} \ \mathsf{set.} \\ \mathsf{Operator}(*,0) \to 0 & \qquad & -\mathsf{The} \ * \ \mathsf{symbol} \ \mathsf{matches} \ \mathsf{any} \ \mathsf{value.} \\ \mathsf{Operator}(x,s < 0) \to -\mathsf{Operator}_f(x,-s) & -\mathsf{Operators} \ \mathsf{in} \ \mathsf{pattern} \ \mathsf{RHS} \ \mathsf{have} \ \mathsf{explicit} \ \mathsf{parameters.} \\ \end{array}
```

Notes

Notes on the operation.

In a sequence of pattern-matching declarations, the first matching pattern in the order presented in this document defines the behavior for a given operand sequence.

In pattern matching, certain shorthand notations are used, as follows. Consider an operation which takes a P3109 value x in format f_x , and returns a P3109 value in format f_y . One matching pattern might be $\operatorname{Operator}(\operatorname{NaN}) \to \operatorname{NaN}$, where the input and output NaN values are in different formats, although this is not explicitly marked. A more explicit presentation, such as $\operatorname{Operator}(\operatorname{NaN}_{f_x}) \to \operatorname{NaN}_{f_y}$ was considered to increase difficulty of comprehension without a compensatory reduction in ambiguity.

Similarly, parameter subscripts are elided on the left-hand-side of patterns where they are common to all, but are written explicitly on the right.

Ancillary information, typically parameters, may include information such as an operand's format or rounding behaviors. An implementation may choose to provide that information using any appropriate mechanism. For example, available mechanisms in a hardware implementation might include passing the information in a hardware register, or as additional bits in an operation's opcode.

4.6 Functions

This section defines mathematical functions which are referenced in the later definitions of operations, but which themselves need not (and, in cases where the inputs or outputs are real, cannot) be provided in a conforming implementation.

Behavior that is specified through cases should be read from top to bottom.

4.6.1 Decode

Decode P3109 value to extended real or NaN.

Signature

$$\mathsf{Decode}_f(x) \to X$$

Parameters

f: format, width K_f , precision P_f , exponent bias b_f

Operands

x:P3109 value, in format f

Output

X : extended real value or NaN

$$\begin{split} & \operatorname{Decode}(2^{\mathsf{K}_f-1}) \to \operatorname{NaN} \\ & \operatorname{Decode}(2^{\mathsf{K}_f-1}-1) \to \infty \\ & \operatorname{Decode}(2^{\mathsf{K}_f-1} < x < 2^{\mathsf{K}_f}) \to -\operatorname{Decode}_f(x-2^{\mathsf{K}_f-1}) \\ & \operatorname{Decode}(0 \le x < 2^{\mathsf{K}_f-1}-1) \to X \\ & \mathbf{where} \\ & \underbrace{Y - \int (0+T \times 2^{1-\mathsf{P}_f}) \times 2^{E+1}}_{X} \quad \mathbf{if} \ E = -b_f \end{split}$$

$$X = \begin{cases} (0 + T \times 2^{1-\mathsf{P}_f}) \times 2^{E+1} & \text{if } E = -b_f \\ (1 + T \times 2^{1-\mathsf{P}_f}) \times 2^E & \text{Otherwise} \end{cases}$$
 —Normal
$$T = x \mod 2^{\mathsf{P}_f - 1}$$

$$E = x \div 2^{\mathsf{P}_f - 1} - b_f$$

4.6.2 Project

Project extended real value to P3109 format f, applying specified rounding and saturation.

Signature

```
\mathsf{Project}_{f,\pi}(X) \to x
```

Parameters

```
f: target format, precision \mathsf{P}_f, exponent bias b_f, maximum finite value M_f \pi: projection specification: rounding mode \mathsf{Rnd}_\pi, saturation \mathsf{Sat}_\pi
```

Operands

X : extended real value

Output

```
x:P3109 value, format f
```

4.6.3 RoundToPrecision

Convert extended real value to extended real value representable with a given precision. The exponent is bounded below by 2 - P - b and unbounded above.

Signature

RoundToPrecision_{P.b.Rnd} $(X) \rightarrow Z$

Parameters

P:integer precision
b:exponent bias
Rnd:rounding mode

Operands

X : extended real value

Output

Z : extended real value, of the form $N \times 2^E$, where $N \in \mathbb{Z}$, $0 \le |N| < 2^P$, and $2 - P - b \le E$.

Behavior

$$\begin{aligned} & \operatorname{RoundToPrecision}(X \in \{0, -\infty, \infty\}) \to X \\ & \operatorname{RoundToPrecision}(X) \to Z \\ & \operatorname{where} \\ & E = \max(\lfloor \log_2(|X|) \rfloor, 1 - b) - \mathsf{P} + 1 \\ & Subnormals \ \text{handled by } \max(\cdot, 1 - b) \\ & S = |X| \times 2^{-E} \\ & \Delta = S - \lfloor S \rfloor \\ & \operatorname{CodelsEven} = \begin{cases} \mathsf{IsEven}(\lfloor S \rfloor) & \text{if } \mathsf{P} > 1 \\ (\lfloor S \rfloor = 0) \lor \mathsf{IsEven}(E + b) & \text{Otherwise} \end{cases} \\ & I = \lfloor S \rfloor + \mathbb{1}[\mathsf{RoundAway}(\mathsf{Rnd})] \\ & Z = \operatorname{sign}(X) \times I \times 2^E \\ & \mathbf{and} \\ & \operatorname{RoundAway}(\mathsf{NearestTiesToEven}) = \Delta > 0.5 \lor \left(\Delta = 0.5 \land \neg \mathsf{CodelsEven}\right) \\ & \operatorname{RoundAway}(\mathsf{NearestTiesToAway}) = \Delta \geq 0.5 \\ & \operatorname{RoundAway}(\mathsf{TowardPositive}) = \Delta > 0 \land X > 0 \\ & \operatorname{RoundAway}(\mathsf{TowardNegative}) = \Delta > 0 \land X < 0 \\ & \operatorname{RoundAway}(\mathsf{TowardZero}) = \mathsf{False} \end{cases}$$

Notes

The P = 1 logic for CodelsEven uses the observation that $I = 0 \implies Z = 0$, hence the code is 0, hence even.

Only precision and bias are needed for this definition, not format width.

Note that I may be set to 2^{P} , which might appear to preclude its representation in $\mathsf{P}-1$ bits of explicit significand, but the computed real value is then $(1+0)\times 2^{E+1+\mathsf{P}}$, representable as the first number in the next binade.

4.6.4 Saturate

Saturate extended real to $\pm \infty$, or to maximum value, according to projection specification parameters Sat, Rnd.

Signature

$$\mathsf{Saturate}_M(\mathsf{Sat},\mathsf{Rnd},X) o Z$$

Parameters

M: real maximum value

Operands

Sat: saturation mode
Rnd: rounding mode
X: extended real value

Output

Z: extended real value

Behavior

```
\begin{aligned} &\mathsf{Saturate}(*,*,X\in[-M,M])\to X\\ &\mathsf{Saturate}(\mathsf{SatMax},*,X\notin[-M,M])\to \mathrm{sign}(X)\times M\\ &\mathsf{Saturate}(\mathsf{SatFinite},*,X\in\{\pm\infty\})\to X\\ &\mathsf{Saturate}(\mathsf{SatFinite},*,|X|\in[M,\infty))\to \mathrm{sign}(X)\times M\\ &\mathsf{Saturate}(\mathsf{Ovflnf},*,X\in\{\pm\infty\})\to X\\ &\mathsf{Saturate}(\mathsf{Ovflnf},\mathsf{TowardZero},|X|\in[M,\infty))\to \mathrm{sign}(X)\times M\\ &\mathsf{Saturate}(\mathsf{Ovflnf},\mathsf{TowardPositive},X\in(-\infty,-M))\to -M\\ &\mathsf{Saturate}(\mathsf{Ovflnf},\mathsf{TowardNegative},X\in(M,\infty))\to M\\ &\mathsf{Saturate}(\mathsf{Ovflnf},*,X)\to \mathrm{sign}(X)\times\infty \end{aligned}
```

Note

In Saturate, all values above M are sent to either M or ∞ . Nevertheless, Project (§4.6.2) has the property that values below $M + \frac{1}{2}\operatorname{ulp}(M)$ will round to M because RoundToPrecision precedes saturation in the definition of Project.

4.6.5 Encode

Encode extended real value or NaN to P3109 format f. Encode must be applied only to a value which is in the value set of format f. Such a value may be produced by, for example RoundToPrecision and Saturate, or the input may be known to be in the value set, for example, in the negation of a value already in the set.

Signature

$$\mathsf{Encode}_f(X) \to z$$

Parameters

f: target format, width K_f , precision P_f , exponent bias b_f

Operands

X: extended real value or NaN, in the value set of format f

Output

$$z$$
:P3109 value, format f

Behavior

$$\begin{split} &\operatorname{Encode}(\operatorname{NaN}) \to 2^{\operatorname{K}_f - 1} \\ &\operatorname{Encode}(\infty) \to 2^{\operatorname{K}_f - 1} - 1 \\ &\operatorname{Encode}(X < 0) \to \operatorname{Encode}_f(-X) + 2^{\operatorname{K}_f - 1} \\ &\operatorname{Encode}(0) \to 0 \\ &\operatorname{Encode}(X > 0) \to z \\ &\operatorname{\mathbf{where}} \\ &z = \begin{cases} T & \text{if } S < 2^{\operatorname{P}_f - 1} \\ T + (E + b_f) \times 2^{\operatorname{P}_f - 1} & \operatorname{Otherwise} \end{cases} \\ &\operatorname{\mathbf{and}} \\ &E = \max(\lfloor \log_2(X) \rfloor, 1 - b_f) \\ &S = X \times 2^{-E} \times 2^{\operatorname{P}_f - 1} & -S \text{ is the significand} \\ &T = S \mod 2^{\operatorname{P}_f - 1} \end{cases} \end{split}$$

Note

Because of the precondition that X is in the value set of format f, it follows that $S \in \mathbb{N}$.

4.7 Conversion operations

4.7.1 Specification of IEEE Std 754 formats

In specifying IEEE Std 754 formats, the symbol ϕ is used, from which format parameters are extracted as needed as follows:

 M_{ϕ} : maximum finite value (e.g., 65504.0 for Binary16)

 P_{ϕ} : precision (e.g., 11 for Binary16)

 B_{ϕ} : exponent bias (e.g., 15 for Binary16)

We will make use of the function Encode754, defined as follows:

Signature

```
Encode754_{\phi}(X) \rightarrow z
```

Parameters

 ϕ : target IEEE Std 754 format

Operands

X : NaN or extended real value, in the value set of format ϕ

Output

```
z : IEEE Std 754 value, format \phi
```

Behavior

```
Encode754(NaN) \rightarrow Any quiet IEEE Std 754 NaN Encode754(X) \rightarrow The code in \phi that decodes to X
```

Notes

In this document, the Encode754 function is only called with arguments in the value set of format ϕ , therefore encoding is unambiguous and independent of rounding mode. Conversely, it is an error in this document if this condition is not guaranteed.

An implementation may return any quiet NaN. It is recommended that the quiet NaN with zero payload is returned.

4.7.2 Conversion from IEEE Std 754 formats to P3109

Convert a value in an IEEE Std 754 format to the corresponding value in a given P3109 format, considering rounding and saturation.

Signature

```
ConvertToP3109_{\phi,f,\pi}(X) \rightarrow z
```

Parameters

```
\phi: source IEEE Std 754 format f: target format \pi: projection specification
```

Operands

```
X: IEEE-754 value, format \phi
```

Output

```
z:P3109 value, format f
```

Behavior

Note

AsExtendedReal $_{\phi}$ is a function which converts a non-NaN encoded IEEE Std 754 value to a value in the extended reals. AsExtendedReal $(-0) \rightarrow 0$.

4.7.3 Conversion from P3109 to IEEE Std 754

Convert a P3109 value to a value in an IEEE Std 754 format. We note that for IEEE Std 754 binary $\{K\}$ formats for K > 16, all P3109 values are values in the target format, hence the conversion of non-NaN values is unambiguous. For Binary16 outputs, some P3109 values will be out of the target range; it is necessary to be precise about rounding and saturation.

Signature

```
ConvertToIEEE754_{f,\pi,\phi}(x) \to X
```

Parameters

```
f:input format
```

 π : projection specification

 ϕ : IEEE Std 754 result format, precision P_{ϕ} , bias B_{ϕ} , maximum value M_{ϕ}

Operands

```
x:P3109 value, format f
```

Output

X: IEEE-754 value, format ϕ

```
\begin{aligned} \mathsf{ConvertToIEEE754}(\mathsf{NaN}) &\to \mathsf{Encode754}_{\phi}(\mathsf{NaN}) \\ \mathsf{ConvertToIEEE754}(x) &\to \mathsf{Encode754}_{\phi}(X) \\ &\quad \mathbf{where} \\ &\quad Y = \mathsf{Decode}_f(x) \\ &\quad R = \mathsf{RoundToPrecision}_{P_{\phi}, B_{\phi}, \mathsf{Rnd}_{\pi}}(Y) \\ &\quad X = \mathsf{Saturate}_{M_{\phi}}(\mathsf{Sat}_{\pi}, \mathsf{Rnd}_{\pi}, R) \end{aligned}
```

4.7.4 Conversion from P3109 to P3109

Convert a P3109 value to another P3109 format.

Signature

```
ConvertP3109ToP3109_{f_x,f_z,\pi}(x) 
ightarrow z
```

Parameters

```
f_x: input format f_z: target format \pi: projection specification
```

Operands

```
x:P3109 value, format f_x
```

Output

```
z:P3109 value, format f_z
```

```
\begin{array}{ll} {\sf ConvertP3109ToP3109(NaN)} \to {\sf NaN} \\ {\sf ConvertP3109ToP3109}(x) \to {\sf Project}_{f_z,\pi}(X) \quad {\bf where} \quad X = {\sf Decode}_{f_x}(x) \end{array}
```

4.8 Arithmetic operations

Arithmetic operations which take one or more P3109 values as arguments, and return one or more P3109 values are defined in this section. Arithmetic operations which mix IEEE Std 754 and P3109 values are described in §4.9.

4.8.1 Unary sign operations

Operations which take P3109 values as input, and whose outputs are guaranteed to be exact values in the same P3109 format. These operations do not permit the output format to be different from the input format.

Signature

Operation
$$f(x) \rightarrow z$$

Parameters

f: input and output format

Operands

$$x$$
:P3109 value, format f

Output

$$z$$
:P3109 value, format f

Behavior

$$\mathsf{Abs}(x) \to \begin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \\ \mathsf{Encode}_f(|X|) & \mathsf{Otherwise} \end{cases}$$

$$\mathbf{where} \quad X = \mathsf{Decode}_f(x)$$

$$\mathsf{Negate}(x) o egin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \\ \mathsf{Encode}_f(-X) & \mathsf{Otherwise} \end{cases}$$
 $\mathbf{where} \quad X = \mathsf{Decode}_f(x)$

Note

The extended reals do not have negative zero, hence -0 = 0 and Abs(0) = 0.

4.8.2 Binary sign operations

Signature

$$\mathsf{Operation}_f(x,y) o z$$

Parameters

f: input and output format

Operands

$$x$$
:P3109 value, format f y :P3109 value, format f

Output

z:P3109 value, format f

$$\begin{aligned} & \mathsf{CopySign}(x,y) \rightarrow \begin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \lor \mathsf{isNaN}(y) \\ \mathsf{Abs}(x) & Y \geq 0 \\ \mathsf{Negate}(\mathsf{Abs}(x)) & Y < 0 \end{cases} \\ & \mathbf{where} \quad Y = \mathsf{Decode}_f(y) \end{aligned}$$

4.8.3 Binary arithmetic operations

These operations take two P3109 values as input, and return a P3109 value. The definitions allow for all input and output formats to differ, a given implementation may supply any subset of the defined operations.

Signature

```
\mathsf{Operation}_{f_x,f_y,f_z,\pi}(x,y) \to z
```

Parameters

```
f_x: format of x

f_y: format of y

f_z: format of z

\pi: projection specification
```

Operands

```
x:P3109 value, format f_x
y:P3109 value, format f_y
```

Output

```
z:P3109 value, format f_z
```

Behavior

```
\mathsf{Add}(*,\mathsf{NaN})\to\,\mathsf{NaN}
Add(NaN,*) \rightarrow NaN
Add(-Inf, Inf) \rightarrow NaN
Add(Inf, -Inf) \rightarrow NaN
Add(x,y) \rightarrow Project_{f_x,\pi}(X+Y) where X = Decode_{f_x}(x), Y = Decode_{f_y}(y)
Subtract(*, NaN) \rightarrow NaN
Subtract(NaN, *) \rightarrow NaN
Subtract(Inf, Inf) \rightarrow NaN
Subtract(-Inf, -Inf) \rightarrow NaN
\mathsf{Subtract}(x,y) \to \mathsf{Project}_{f_x,\pi}(X-Y) \quad \mathbf{where} \quad X = \mathsf{Decode}_{f_x}(x), Y = \mathsf{Decode}_{f_y}(y)
Multiply(*, NaN) \rightarrow NaN
Multiply(NaN,*) \rightarrow NaN
Multiply(0, \pm Inf) \rightarrow NaN
Multiply(\pm Inf, 0) \rightarrow NaN
\mathsf{Multiply}(x,y) \to \mathsf{Project}_{f_x,\pi}(X \times Y) \quad \mathbf{where} \quad X = \mathsf{Decode}_{f_x}(x), Y = \mathsf{Decode}_{f_x}(y)
Divide(*, NaN) \rightarrow NaN
Divide(NaN, *) \rightarrow NaN
\mathsf{Divide}(*,0) \to \mathsf{NaN}
\mathsf{Divide}(x,y) \to \mathsf{Project}_{f_x,\pi}(X/Y) where X = \mathsf{Decode}_{f_x}(x), Y = \mathsf{Decode}_{f_y}(y)
```

Notes

Divide($x,\pm Inf$) where x is finite yields 0.

Divide(x,0) yields NaN. With x finite, it would be inconsistent to return $lnf: 1/(1/-lnf) \rightarrow lnf$.

Unary mathematical operations 4.8.4

Signature

$$\mathsf{Operation}_{f_x,f_z,\pi}(x) \to z$$

Parameters

 f_x :input format f_z : output format

 π : projection specification

Operands

x:P3109 value, format f_x

Output

z:P3109 value, format f_z

$$\mathsf{Sqrt}(x) \to \begin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \\ \mathsf{NaN} & X < 0 \\ \mathsf{Project}_{f_z,\pi}(\sqrt{X}) & X \geq 0 \end{cases}$$

$$\mathbf{where} \quad X = \mathsf{Decode}_{f_x}(x)$$

where
$$X = \mathsf{Decode}_{f_x}(x)$$

$$\mathsf{Exp}(x) o egin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \ \mathsf{Project}_{f_z,\pi}(e^X) & \mathsf{Otherwise} \ & \mathbf{where} & X = \mathsf{Decode}_{f_x}(x) \end{cases}$$

$$\operatorname{Exp2}(x) o egin{cases} \operatorname{NaN} & \operatorname{isNaN}(x) \\ \operatorname{Project}_{f_z,\pi}(2^X) & \operatorname{Otherwise} \end{cases}$$

where
$$X = \mathsf{Decode}_{f_x}(x)$$

$$\mathsf{Log}(x) \to \begin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \\ \mathsf{NaN} & X < 0 \\ \mathsf{Project}_{f_z,\pi}(\log(X)) & X \geq 0 \end{cases}$$

$$\mathbf{where} \quad X = \mathsf{Decode}_{f_x}(x)$$

$$\mathsf{Log2}(x) \to \begin{cases} \mathsf{NaN} & \mathsf{isNaN}(x) \\ \mathsf{NaN} & X < 0 \\ \mathsf{Project}_{f_z,\pi}(\log_2(X)) & X \geq 0 \end{cases}$$

4.8.5 Scaled addition

Compute $X \times 2^{s_x} + Y \times 2^{s_y}$, and return a P3109 value. Scaling is applied in the extended reals, before projection to the target format.

Signature

```
\mathsf{AddScaled}_{f_x,f_y,f_z,\pi}(x,s_x,y,s_y) \to z
```

Parameters

```
f_x: format of x

f_y: format of y

f_z: format of z

\pi: projection specification
```

Operands

```
x:P3109 value, format f_x
s_x: integer log-scale factor for x
y:P3109 value, format f_y
s_y: integer log-scale factor for y
```

Output

```
z:P3109 value, format f_z
```

Behavior

```
\begin{array}{l} \mathsf{AddScaled}(\mathsf{NaN},*,*,*) \to \mathsf{NaN} \\ \mathsf{AddScaled}(*,*,\mathsf{NaN},*) \to \mathsf{NaN} \\ \mathsf{AddScaled}(-\mathsf{Inf},*,\mathsf{Inf},*) \to \mathsf{NaN} \\ \mathsf{AddScaled}(\mathsf{Inf},*,-\mathsf{Inf},*) \to \mathsf{NaN} \\ \mathsf{AddScaled}(x,s_x,y,s_y) \to \mathsf{Project}_{f_z,\pi}(Z) \\ & \mathbf{where} \\ & Z = X \times 2^{s_x} + Y \times 2^{s_y} \\ & X = \mathsf{Decode}_{f_x}(x) \\ & Y = \mathsf{Decode}_{f_y}(y) \end{array}
```

Note

The valid range of the log-scale factors s_x and s_y is not specified. Implementers shall declare the provision of AddScaled with specified constraints on legal values for these operands.

Example declarations might include

```
"AddScaled, with log-scale factors in \{-32\dots31\}" "AddScaled, with s_x=0, s_y\in\{-128\dots127\}" "AddScaled, with s_x\in\{-128\dots127\}, s_y=s_x"
```

See §4.1 for further discussion.

4.8.6 Scaled multiplication

Compute $X \times Y \times 2^s$, and return a P3109 value. Scaling is applied in the extended reals, before projection to the target format.

Signature

```
\mathsf{MultiplyScaled}_{f_x,f_y,f_z,\pi}(x,y,s) 	o z
```

Parameters

```
f_x: format of x

f_y: format of y

f_z: format of z

\pi: projection specification
```

Operands

```
x:P3109 value, format f_x
y:P3109 value, format f_y
s:integer log-scale factor
```

Output

```
z:P3109 value, format f_z
```

Behavior

```
\begin{split} & \mathsf{MultiplyScaled}(*,\mathsf{NaN},*) \to \mathsf{NaN} \\ & \mathsf{MultiplyScaled}(\mathsf{NaN},*,*) \to \mathsf{NaN} \\ & \mathsf{MultiplyScaled}(0,\pm\mathsf{Inf},*) \to \mathsf{NaN} \\ & \mathsf{MultiplyScaled}(\pm\mathsf{Inf},0,*) \to \mathsf{NaN} \\ & \mathsf{MultiplyScaled}(x,y,s) \to \mathsf{Project}_{f_z,\pi}(Z) \\ & \mathbf{where} \\ & Z = X \times Y \times 2^s \\ & X = \mathsf{Decode}_{f_x}(x) \\ & Y = \mathsf{Decode}_{f_y}(y) \end{split}
```

Note

The valid range of the log-scale factor s is not specified. Implementations shall declare the provision of MultiplyScaled with specified constraints on legal values for these operands.

An example such declaration might be

```
"MultiplyScaled, with log-scale factor in \{-32...31\}"
```

See §4.1 for further discussion.

4.9 Mixed IEEE Std 754 and P3109 operations

This section describes operations which take a mix of IEEE Std 754 and P3109 operands and return IEEE Std 754 values. An implementation is free to define additional fused operations in which P3109 operands are upconverted to IEEE Std 754 before operating.

This section addresses operations that cannot be expressed as a fused sequence of operations. For instance, it is not possible to upconvert all values from binary8p1 to Binary16. Moreover, the operations described here may include saturation and rounding modes not available in definitions based solely on upconversion.

Like the operations defined previously, these are superset specifications. An implementation might provide any subset of the parameterized set of operations, accompanied by a statement specifying which subset is implemented.

These definitions make use of the functions AsExtendedReal and Encode754 defined above.

4.9.1 Scaled Fused Multiply Add

Compute $Z = A \times 2^{s_a} + X \times Y \times 2^s$, with A and Z in the same format. Scaling is applied in the extended reals, before projection to the target format.

Signature

```
\mathsf{ScaledFMA}_{\phi,f_x,f_y,\pi}(a,s_a,x,y,s) 	o z
```

Parameters

```
\phi: IEEE Std 754 format of a and target, precision P_{\phi}, bias B_{\phi}, maximum value M_{\phi} f_x: format of x f_y: format of y \pi: projection specification
```

Operands

```
a: \text{IEEE Std 754 value, format } \phi \\ s_a: \text{integer log-scale factor} \\ x: \text{P3109 value, format } f_x \\ y: \text{P3109 value, format } f_y \\ s: \text{integer log-scale factor}
```

Output

```
z : IEEE Std 754 value, format \phi
```

Behavior

```
\begin{array}{l} \mathsf{ScaledFMA}(\mathsf{NaN},*,*,*,*) \to \mathsf{NaN} \\ \mathsf{ScaledFMA}(*,*,\mathsf{NaN},*,*) \to \mathsf{NaN} \\ \mathsf{ScaledFMA}(*,*,\mathsf{NaN},*) \to \mathsf{NaN} \\ \mathsf{ScaledFMA}(a,s_a,x,y,s) \to z \\ & \mathbf{where} \\ & A = \mathsf{AsExtendedReal}_{\phi}(a) \\ & X = \mathsf{Decode}_{f_x}(x) \\ & Y = \mathsf{Decode}_{f_y}(y) \\ & Z = A \times 2^{s_a} + X \times Y \times 2^s \\ & Z' = \mathsf{RoundToPrecision}_{P_{\phi},B_{\phi},\mathsf{Rnd}_{\pi}}(Z) \\ & Z'' = \mathsf{Saturate}_{M_{\phi}}(\mathsf{Sat}_{\pi},\mathsf{Rnd}_{\pi},Z') \\ & z = \mathsf{Encode754}_{\phi}(Z'') \\ & -Z'' \text{ guaranteed representable in format } \phi \end{array}
```

Note

The valid range of the log-scale factors are not specified. Implementations shall declare the provision of ScaledFMA with specified constraints on legal values for these operands.

An example such declaration might be:

"ScaledFMA, with log-scale factors in $\{-32\dots31\}$, $f_x=f_y$ in $\{$ binary8p3, binary8p4 $\}$, ϕ in $\{$ Binary16, Binary32 $\}$ "

4.10 Comparisons, predicates, and classification

4.10.1 Minimum and Maximum

These operations take two P3109 values as input, and return a P3109 value. Operands and return value are in the same format.

Signature

```
Operation f(x,y) \rightarrow z
```

Parameters

```
f: format
```

Operands

```
x:P3109 value, format f y:P3109 value, format f
```

Output

```
z:P3109 value, format f
```

Behavior

```
\begin{array}{ll} \mathsf{Minimum}(*,\mathsf{NaN}) \to \mathsf{NaN} \\ \mathsf{Minimum}(\mathsf{NaN},*) \to \mathsf{NaN} \\ \mathsf{Minimum}(x,y) \to \mathsf{Encode}_f(\min(X,Y)) & \mathbf{where} \quad X = \mathsf{Decode}_f(x), Y = \mathsf{Decode}_f(y) \\ \mathsf{Maximum}(*,\mathsf{NaN}) \to \mathsf{NaN} \\ \mathsf{Maximum}(\mathsf{NaN},*) \to \mathsf{NaN} \\ \mathsf{Maximum}(x,y) \to \mathsf{Encode}_f(\max(X,Y)) & \mathbf{where} \quad X = \mathsf{Decode}_f(x), Y = \mathsf{Decode}_f(y) \end{array}
```

Note

The operations minimumNumber, maximumNumber, defined by IEEE Std 754-2019 are not defined in this document.

4.10.2 Comparisons

Comparison operators take two P3109 operands and return a boolean. Any NaN operand yields the result False.

The below specifications are expressed with the following substitutions for compare Op and Compare Expr:

compare Op	Compare Expr
compareLess	X < Y
compareLessEqual	$X \leq Y$
compareEqual	X = Y
compareGreaterEqual	X > Y
compareGreater	$X \ge Y$

Signature

```
\mathsf{compare} \mathit{Op}_{f_x,f_y}(x,y) 	o \mathsf{Boolean}
```

Parameters

```
f_x: format of x
f_y: format of y
```

Operands

```
x:P3109 value, format f_x
y:P3109 value, format f_y
```

Output

b: boolean value

```
\begin{array}{c} \operatorname{compare} Op(\operatorname{NaN},\operatorname{NaN}) \to \operatorname{False} \\ \operatorname{compare} Op(\operatorname{NaN},y) \to \operatorname{False} \\ \operatorname{compare} Op(x,\operatorname{NaN}) \to \operatorname{False} \\ \operatorname{compare} Op(x,y) \to \operatorname{CompareExpr} \\ \mathbf{where} \\ X = \operatorname{Decode}_{f_x}(x) \\ Y = \operatorname{Decode}_{f_y}(y) \end{array}
```

4.10.3 Predicates and classification

Conforming implementations shall provide the classification predicates and the classifier operation defined below.

The classification operations comprise: 1) a set of predicate functions with a boolean return value, taking a single P3109 value as input; 2) a classifier operation class(x) that returns a single value of enumeration type, describing the input value's properties.

```
Signature
```

$$isClass_f(x) \rightarrow b$$

Parameters

f: format of x

Operands

x:P3109 value, format f

 $isCanonical(x) \rightarrow True$

Output

b: boolean value

Behavior

$$\begin{split} & \operatorname{isZero}(\operatorname{NaN}) \to \operatorname{False} \\ & \operatorname{isZero}(x) \to \operatorname{Decode}_f(x) = 0 \\ & \operatorname{isOne}(\operatorname{NaN}) \to \operatorname{False} \\ & \operatorname{isOne}(x) \to \operatorname{Decode}_f(x) = 1 \\ & \operatorname{isNaN}(\operatorname{NaN}) \to \operatorname{True} \\ & \operatorname{isNaN}(x) \to \operatorname{False} \\ & \operatorname{isSignMinus}(\operatorname{NaN}) \to \operatorname{True} \\ & \operatorname{isSignMinus}(x) \to \operatorname{Decode}_f(x) < 0 \\ & \operatorname{isNormal}(x \in \{0, -\operatorname{Inf}, \operatorname{Inf}, \operatorname{NaN}\}) \to \operatorname{False} \\ & \operatorname{isNormal}(x) \to (x \mod 2^{\operatorname{K}_f - 1}) \div 2^{\operatorname{P}_f - 1} > 0 \\ & \operatorname{isSubnormal}(x) \to (x \mod 2^{\operatorname{K}_f - 1}) \div 2^{\operatorname{P}_f - 1} = 0 \\ & \operatorname{isFinite}(x) \to x \notin \{-\operatorname{Inf}, \operatorname{Inf}, \operatorname{NaN}\} \\ & \operatorname{isFinite}(x) \to x \notin \{-\operatorname{Inf}, \operatorname{Inf}, \operatorname{NaN}\} \\ & \operatorname{isInfinite}(x) \to x \in \{-\operatorname{Inf}, \operatorname{Inf}\} \\ & \operatorname{isSignaling}(x) \to \operatorname{False} \\ \end{split}$$

-All P3109 formats have one NaN, which does not signal

—There are no non-canonical P3109 interchange formats

4.10.4 Classifier operation

The Classifier operation class(x) tells which of the eight classes x falls into as defined by Table 4.

Signature

$$\mathsf{class}_f(x) \to c$$

Parameters

f: format of x

Operands

x:P3109 value, format f

Output

c: enumeration

Behavior

 $class(x) \rightarrow ClassEnum$

Table 4: Classifier operation

ClassEnum	Condition
clsNaN clsNegativeInfinity clsNegativeNormal clsNegativeSubnormal clsZero clsPositiveSubnormal clsPositiveNormal clsPositiveInfinity	$\begin{array}{l} isNaN(x) \\ isInfinite(x) \wedge isSignMinus(x) \\ isNormal(x) \wedge isSignMinus(x) \\ isSubnormal(x) \wedge isSignMinus(x) \\ isZero(x) \\ isSubnormal(x) \wedge \neg isSignMinus(x) \\ isNormal(x) \wedge \neg isSignMinus(x) \\ isInfinite(x) \wedge \neg isSignMinus(x) \\ \end{array}$

4.10.5 Total order predicate

The total Order(x, y) predicate provides a total ordering over each P3109 format's value set.

Signature

```
\mathsf{totalOrder}_{f_x,f_y}(x,y) \to b
```

Operands

```
f_x: format of x
f_y: format of y
```

Operands

```
x:P3109 value, format f_x
y:P3109 value, format f_y
```

Output

```
b: boolean value
```

Behavior

```
\begin{split} \mathsf{totalOrder}(\mathsf{NaN},x) &\to \mathsf{True} \\ \mathsf{totalOrder}(x,\mathsf{NaN}) &\to \mathsf{False} \\ \mathsf{totalOrder}(x,y) &\to \mathsf{compareLessEqual}_{f_x,f_y}(x,y) \end{split}
```

Note

The above definition is consistent with the IEEE Std 754-2019 definition of totalOrder. In particular, among P3109 formats, there is a single NaN and it always compares as the most-negative value.

4.10.6 Comparison predicates

Conforming implementations shall provide the comparison predicates defined by Table 5 and the total $\mathsf{Order}(x,y)$ predicate.

Comparison operations are two-argument predicates, and their negations, that return True or False. Comparisons may be ordered or unordered. A comparison is considered unordered iff either argument is NaN. All other comparisons are ordered.

For $\{=,>,\geq,<,\leq,\lessgtr\}$, if any argument is NaN, the result is False.

For $\{\neq, \geqslant, \geq, \not\leq, \not\leq, \not\leq\}$, if any argument is NaN, the result is True.

Otherwise, the result of a comparison shall match the mathematical result.

Table 5: Comparison predicates and negations

Math symbol	Predicate true relations	Math symbol	Negation of predicate true relations
=	compareEqual equal	\neq , NOT =	compareNotEqual less than, greater than, unordered
>	compareGreater greater than	≯, NOT >	compareNotGreater less than, equal, unordered
≥	compareGreaterEqual greater than, equal	$\not\geq, \mathrm{NOT} \geq$	compareLessUnordered less than, unordered
<	compareLess less than	≮, NOT <	compareNotLess greater than, equal, unordered
\leq	compareLessEqual less than, equal	$\not\leq$, not \leq	compareGreaterUnordered greater than, unordered
\$	compareOrdered less than, equal, greater than	≸, NOT ≶	compareUnordered unordered

Appendices

A Rationales

A.1 Use of infinity in computation of attention masks

This section expands the rationale in §3.6. A common use for ∞ is to create masks, for example, in Transformer models in machine learning [5].

These values, assembled in mask matrix M with values $M_{ij} \in \{0, -\infty\}$ are typically added to computed values A, in a computation such as:

$$\log\left(\sum \exp(\tau\times (A+M))\right)$$

where τ is a "temperature" or "base" parameter [6]. This calculation depends on the property $\exp(\tau \times (A_{ij} - \infty)) = 0$.

If a floating-point encoding does not provide infinity, then instead M_{ij} will be replaced by a large float (e.g. 224 is the largest finite binary8p4 value). This is not in itself a difficulty: if all the A values are bounded (e.g. the results of a softmax operation are bounded above by 1.0), then $\exp(1.0 - 224.0)$ is an extremely small number, which will certainly round to zero. Therefore, an explicit representation of infinity is *not* needed in order for this computation to yield its desired value.

However, careful implementations do not execute the calculation as written, and instead fuse the $\log(\sum_i \exp(v_i))$ operation into a single operation logsumexp(v), whose implementation makes use of the identity transformation

$$logsumexp(v) \rightarrow logsumexp(v - max(v)) + max(v)$$

Without the "sticky" properties of Inf, this would produce incorrect answers.

For example, in a format where maxFinite=240 without Inf, and maxFinite=224 with Inf:

$$logsumexp(t * [-224, -\infty]) \rightarrow logsumexp(t * [0, -\infty])$$

while

$$\mathsf{logsumexp}(t*[-224,-240]) \to \mathsf{logsumexp}(t*[0,-16])$$

If t=1 and all calculations are done in 8-bit floating-point, then the answer will be the same, because $\exp(-16) \approx 1.1 \times 10^{-7}$, which will round to zero in all precisions P > 2; but if t is small, or calculations are done in mixed precision, as is common with 8-bit floating-point, the loss of "stickiness" will silently yield unexpected answers. It is not expected that the full calculation shall be done in 8-bit floating-point, but the subtraction of the maximum value (and computation of the maximum) might reasonably be in 8-bit floating-point.

A.2 Eight Bit Formats

Eight bit floating-point representations have received much attention for their usefulness and efficacy in machine learning, especially deep learning. Various 8-bit floating-point formats have been proposed, investigated in research papers, and some have been modeled in software. Four precisions [3, 4, 5, and 6 bit precisions] have become generally accepted as providing greater operational benefits than the others. Overall [there are exceptions], current efforts focus

more on precisions of 3 and 4 bits (exponent fields of 5 and 4 bits, respectively). The specifics of third-party proposals for 8-bit floating-point representations vary and can differ from one precision to another. Regardless, the precisions emphasized in current research and other third-party work do share the same focus.

A.3 Essential Formats

A.3.1 binary8p3

This format has 3 subnormal and 123 normal magnitudes. The subnormal magnitudes cover $[1.0*2^{-17}, 3.0*2^{-17}]$. The normal magnitudes cover $[1.0*2^{-15}, 4195.0]$, There are 31 normal binades with 4 magnitudes per complete binade [binade 2^{15} has 3 magnitudes, the 4^{th} is used for Inf].

A.3.2 binary8p4

This format has 7 subnormal and 119 normal magnitudes. The subnormal magnitudes cover $[1.0 * 2^{-10}, 7.0 * 2^{-10}]$. The normal magnitudes cover $[1.0 * 2^{-7}, 224.0]$. There are 15 normal binades with 8 magnitudes per complete binade [binade 2^7 has 7 magnitudes, the 8^{th} is used for Inf],

A.3.3 binary8p5

This format has 15 subnormal and 111 normal magnitudes. The subnormal magnitudes cover $[1.0*2^{-7}, 15.0*2^{-7}]$. The normal magnitudes cover [0.125, 15.0]. There are 7 normal binades with 16 magnitudes per complete binade [binade 2^3 has 15 magnitudes, the 16^{th} is used for Inf],

A.3.4 binary8p6

This format has 31 subnormal and 95 normal magnitudes. The subnormal magnitudes cover $[1.0*2^{-6}, 31.0*2^{-6}]$. The normal magnitudes cover [0.5, 3.875]. There are 3 normal binades with 32 magnitudes per complete binade [binade 2^1 has 31 magnitudes, the 32^{nd} is used for Inf],

B External Formats

This table summarizes the points of agreement and of difference between the formats proposed in this document and a number of existing formats, some of which have hardware implementations.

OCP: Open Compute Platform [7], describing hardware implementations including nVidia, Intel, and ARM.

AGQ: AMD, Graphcore, Qualcomm[8], implemented in Graphcore's C600 product, and AMD's gfx940.

TSL: Tesla Dojo Technology [9], A Guide to Tesla's Configurable floating-point Formats & Arithmetic

Format	P3109		OCP		AGQ		TSL		
Subformat	P3	P4	P5	E5	E4	E5	E4	E4	E5
Special values shared by all subformats		Y N		1	Y		N		
Exactly one NaN	Y		N		Y		Y		
Positive and negative infinity		Y		Y	N	N	1	N	1
Include negative zero	N		Y		N		N		
Max exponent emax	15	7	3	15	8	15	7	N/A	N/A

C 8-bit Value Tables

Value tables mapping 8-bit strings to value sets are provided in this section.

A typical entry is of the form:

```
HEX = BINARY = BINARY_FLOAT = DECIMAL 0x0b = 0.0001.011 = +0b1.011 \times 2^-7 = 0.0107421875
```

Where the fields are interpreted as follows:

HEX Hexadecimal encoding of the code point

BINARY Binary expansion of the code point, underscores separate

< sign >_< exponent >_< significand >

BINARY_FLOAT The precise float value as a binary fraction followed by 2^e with exponent e

DECIMAL A decimal expansion of the value. If the expansion is not an exact

representation of the precise float value, the equals sign is replaced by

"approximately equals" (\approx).

In addition, entries for subnormal and special values are rendered in color as follows:

 $0x05 = 0.0000_101 = +0b0.101 \times 2^-7 = 0.0048828125$ S

 $0x05 = 0.0000_101 = +000.101 \times 2 - 7 = 0.0048828128$ $0x80 = 1.0000_000 = NaN$ Subnormal value

Special value (NaN, +Inf, -Inf)

C.1 Value Table: P1, emin = -62, emax = 63 (nonsymmetric)

```
0x00 = 0.00000000 = 0.0
                                                                   0x40 = 0.1000000 = +0b1.0 \times 2^1 = 2.0
                                                                                                                                                                                                         0xc0 = 1.1000000 = -0b1.0 \times 2^1 = -2.0
                                                                                                                                     0x80 = 1_00000000_ = NaN
0x01 = 0.0000001 = +0b1.0 \times 2^{-62} \approx 2.1684043E-19
                                                                   0x41 = 0_1000001_ = +0b1.0 \times 2^2 = 4.0
                                                                                                                                     0x81 = 1.0000001. = -0b1.0 \times 2^{-62} \approx -2.1684043E-19
                                                                                                                                                                                                         0xc1 = 1_1000001_1 = -0b1.0 \times 2^2 = -4.0
0x02 = 0.0000010 = +0b1.0 \times 2^{-61} \approx 4.3368087E-19
                                                                   0x42 = 0.1000010 = +0b1.0 \times 2^3 = 8.0
                                                                                                                                     0x82 = 1.0000010. = -0b1.0 \times 2^{-61} \approx -4.3368087E-19
                                                                                                                                                                                                         0xc2 = 1_{-1}000010_{-} = -0b1.0 \times 2^{3} = -8.0
0x03 = 0.0000011. = +0b1.0 \times 2^-60 \approx 8.6736174E-19
                                                                   0x43 = 0.1000011. = +0b1.0 \times 2^4 = 16.0
                                                                                                                                     0x83 = 1.0000011. = -0b1.0 \times 2^-60 \approx -8.6736174E-19
                                                                                                                                                                                                         0xc3 = 1.1000011. = -0b1.0 \times 2^4 = -16.0
0x04 = 0.0000100_{-} = +0b1.0 \times 2^{-}59 \approx 1.7347235E-18
                                                                   0x44 = 0_1000100_1 = +0b1.0 \times 2^5 = 32.0
                                                                                                                                     0x84 = 1_0000100_0 = -0b1.0 \times 2^{-59} \approx -1.7347235E-18
                                                                                                                                                                                                         0xc4 = 1_{-}1000100_{-} = -0b1.0 \times 2^{5} = -32.0
                                                                                                                                     0x85 = 1_0000101_ = -0b1.0 \times 2^-58 \approx -3.469447E-18
                                                                                                                                                                                                         0xc5 = 1_1000101_1 = -0b1.0 \times 2^6 = -64.0
0x05 = 0.0000101 = +0b1.0 \times 2^{-58} \approx 3.469447E-18
                                                                   0x45 = 0_{-}1000101_{-} = +0b1.0 \times 2^{6} = 64.0
0x06 = 0.0000110. = +0b1.0 \times 2^{-57} \approx 6.9388939E-18
                                                                   0x46 = 0.1000110 = +0b1.0 \times 27 = 128.0
                                                                                                                                     0x86 = 1.0000110. = -0b1.0 \times 2^-57 \approx -6.9388939E-18
                                                                                                                                                                                                         0xc6 = 1_{-}1000110_{-} = -0b1.0 \times 27 = -128.0
0 \text{x07} = 0 \text{.0000111} \text{..} = +0 \text{b1.0} \times 2 \text{^--56} \approx 1.3877788 \text{E-17}
                                                                                                                                                                                                         0xc7 = 1_1000111_1 = -0b1.0 \times 2\% = -256.0
                                                                                                                                     0x87 = 1.0000111. = -0b1.0 \times 2^-56 \approx -1.3877788E-17
                                                                   0x47 = 0.1000111. = +0b1.0 \times 2\% = 256.0
0x08 = 0\_0001000\_ = +0b1.0 \times 2^-55 \approx 2.7755576E-17
                                                                                                                                     0x88 = 1_0001000_ = -0b1.0 \times 2^-55 \approx -2.7755576E-17
                                                                                                                                                                                                         0xc8 = 1.1001000_{-} = -0b1.0 \times 2^{9} = -512.0
                                                                   0x48 = 0.1001000 = +0b1.0 \times 2^9 = 512.0
0x09 = 0.0001001 = +0b1.0 \times 2^{-54} \approx 5.5511151E-17
                                                                   0x49 = 0_1001001_ = +0b1.0 \times 2^10 = 1024.0
                                                                                                                                     0x89 = 1_0001001_ = -0b1.0 \times 2^-54 \approx -5.5511151E-17
                                                                                                                                                                                                         0xc9 = 1_1001001_1 = -0b1.0 \times 2^10 = -1024.0
0x0a = 0.0001010. = +0b1.0 \times 2^{-53} \approx 1.110223E-16
                                                                   0x4a = 0.1001010. = +0b1.0 \times 2^11 = 2048.0
                                                                                                                                     0x8a = 1.0001010. = -0b1.0 \times 2^{-53} \approx -1.110223E-16
                                                                                                                                                                                                         0xca = 1_{-}1001010_{-} = -0b1.0 \times 2^{1}1 = -2048.0
0x0b = 0.0001011_{-} = +0b1.0 \times 2^{-52} \approx 2.220446E-16
                                                                   0x4b = 0.1001011. = +0b1.0 \times 2^12 = 4096.0
                                                                                                                                     0x8b = 1.0001011. = -0b1.0 \times 2^{-52} \approx -2.220446E-16
                                                                                                                                                                                                         0xcb = 1_1001011_1 = -0b1.0 \times 2^12 = -4096.0
0x0c = 0.0001100 = +0b1.0 \times 2^{-51} \approx 4.4408921E-16
                                                                                                                                     0x8c = 1.0001100 = -0b1.0 \times 2^{-51} \approx -4.4408921E-16
                                                                                                                                                                                                         0xcc = 1_1001100_1 = -0b1.0 \times 2^13 = -8192.0
                                                                   0x4c = 0.1001100_{-} = +0b1.0 \times 2^{13} = 8192.0
0x0d = 0.0001101. = +0b1.0 \times 2^{-50} \approx 8.8817842E-16
                                                                   0x4d = 0_1001101_ = +0b1.0 \times 2^14 = 16384.0
                                                                                                                                     0x8d = 1_0001101_ = -0b1.0 \times 2^{-50} \approx -8.8817842E-16
                                                                                                                                                                                                         0xcd = 1_1001101_1 = -0b1.0 \times 2^14 = -16384.0
0x0e = 0.0001110. = +0b1.0 \times 2^-49 \approx 1.7763568E-15
                                                                   0x4e = 0_{-}1001110_{-} = +0b1.0 \times 2^{-}15 = 32768.0
                                                                                                                                     0x8e = 1.0001110 = -0b1.0 \times 2^-49 \approx -1.7763568E-15
                                                                                                                                                                                                         0xce = 1.1001110 = -0b1.0 \times 2^{15} = -32768.0
                                                                                                                                     0x8f = 1.0001111. = -0b1.0 \times 2^-48 \approx -3.5527137E-15
                                                                                                                                                                                                         0xcf = 1_1001111_1 = -0b1.0 \times 2^16 = -65536.0
0x0f = 0.0001111_{-} = +0b1.0 \times 2^{-48} \approx 3.5527137E-15
                                                                   0x4f = 0.1001111. = +0b1.0 \times 2^{1}6 = 65536.0
                                                                                                                                     0x90 = 1_0010000_0 = -0b1.0 \times 2^-47 \approx -7.1054274E-15
                                                                                                                                                                                                         0xd0 = 1_1010000_1 = -0b1.0 \times 2^17 = -131072.0
0x10 = 0.0010000 = +0b1.0 \times 2^-47 \approx 7.1054274E-15
                                                                   0x50 = 0_1010000_1 = +0b1.0 \times 2^17 = 131072.0
0x11 = 0.0010001_{-} = +0b1.0 \times 2^{-46} \approx 1.4210855E-14
                                                                   0x51 = 0_1010001_ = +0b1.0 \times 2^18 = 262144.0
                                                                                                                                     0x91 = 1\_0010001\_ = -0b1.0 \times 2^-46 \approx -1.4210855E-14
                                                                                                                                                                                                         0xd1 = 1_1010001_1 = -0b1.0 \times 2^18 = -262144.0
                                                                                                                                                                                                         0xd2 = 1_1010010_1 = -0b1.0 \times 2^19 = -524288.0
0x12 = 0.0010010. = +0b1.0 \times 2^-45 \approx 2.8421709E-14
                                                                   0x52 = 0.1010010. = +0b1.0 \times 2^{19} = 524288.0
                                                                                                                                     0x92 = 1.0010010. = -0b1.0 \times 2^-45 \approx -2.8421709E-14
0x13 = 0.0010011 = +0b1.0 \times 2^{-44} \approx 5.6843419E-14
                                                                   0x53 = 0_1010011_1 = +0b1.0 \times 2^20 = 1048576.0
                                                                                                                                     0x93 = 1.0010011 = -0b1.0 \times 2^{-44} \approx -5.6843419E-14
                                                                                                                                                                                                         0xd3 = 1.1010011. = -0b1.0 \times 2^20 = -1048576.0
0x14 = 0.0010100 = +0b1.0 \times 2^{-43} \approx 1.1368684E-13
                                                                   0x54 = 0_1010100_1 = +0b1.0 \times 2^21 = 2097152.0
                                                                                                                                     0x94 = 1.0010100 = -0b1.0 \times 2^-43 \approx -1.1368684E-13
                                                                                                                                                                                                         0xd4 = 1\ 1010100 = -0b1.0 \times 2^21 = -2097152.0
                                                                                                                                                                                                         0xd5 = 1.1010101. = -0b1.0 \times 2^2 = -4194304.0
0x15 = 0.0010101 = +0b1.0 \times 2^{-42} \approx 2.2737368E-13
                                                                   0x55 = 0.1010101. = +0b1.0 \times 2^2 = 4194304.0
                                                                                                                                     0x95 = 1.0010101. = -0b1.0 \times 2^{-42} \approx -2.2737368E-13
0x16 = 0.0010110 = +0b1.0 \times 2^{-41} \approx 4.5474735E-13
                                                                                                                                     0x96 = 1.0010110 = -0b1.0 \times 2^{-41} \approx -4.5474735E-13
                                                                                                                                                                                                         0xd6 = 1.1010110. = -0b1.0 \times 2^2 = -8388608.0
                                                                   0x56 = 0.1010110. = +0b1.0 \times 2^2 = 8388608.0
0x17 = 0.0010111_{-} = +0b1.0 \times 2^{-40} \approx 9.094947E-13
                                                                   0x57 = 0.1010111_{-} = +0b1.0 \times 2^{2}4 = 16777216.0
                                                                                                                                     0x97 = 1.0010111_{-} = -0b1.0 \times 2^{-40} \approx -9.094947E-13
                                                                                                                                                                                                         0xd7 = 1_{-}1010111_{-} = -0b1.0 \times 2^{2}4 = -16777216.0
0x18 = 0.0011000 = +0b1.0 \times 2^{-39} \approx 1.8189894E-12
                                                                   0x58 = 0.1011000_{-} = +0b1.0 \times 2^{2}5 = 33554432.0
                                                                                                                                     0x98 = 1_0011000_0 = -0b1.0 \times 2^-39 \approx -1.8189894E-12
                                                                                                                                                                                                         0xd8 = 1_1011000_1 = -0b1.0 \times 2^25 = -33554432.0
0x19 = 0.0011001 = +0b1.0 \times 2^{-38} \approx 3.6379788E-12
                                                                   0x59 = 0.1011001_{-} = +0b1.0 \times 2^{2}6 = 67108864.0
                                                                                                                                     0x99 = 1_0011001_ = -0b1.0 \times 2^-38 \approx -3.6379788E-12
                                                                                                                                                                                                         0xd9 = 1_1011001_1 = -0b1.0 \times 2^26 = -67108864.0
0x1a = 0.0011010. = +0b1.0 \times 2^{-37} \approx 7.2759576E-12
                                                                   0x5a = 0.1011010. = +0b1.0 \times 2^2 7 = 134217728.0
                                                                                                                                     0x9a = 1.0011010. = -0b1.0 \times 2^{-37} \approx -7.2759576E-12
                                                                                                                                                                                                         0xda = 1_{-}1011010_{-} = -0b1.0 \times 2^{2}7 = -134217728.0
0x1b = 0.0011011. = +0b1.0 \times 2^-36 \approx 1.4551915E-11
                                                                   0x5b = 0_1011011_1 = +0b1.0 \times 2^28 = 268435456.0
                                                                                                                                     0x9b = 1.0011011. = -0b1.0 \times 2^-36 \approx -1.4551915E-11
                                                                                                                                                                                                         0xdb = 1_{-}1011011_{-} = -0b1.0 \times 2^{2}8 = -268435456.0
0x1c = 0.0011100_{-} = +0b1.0 \times 2^{-35} \approx 2.910383E-11
                                                                                                                                     {\tt 0x9c} = {\tt 1\_0011100\_} = -{\tt 0b1.0 \times 2^-35} \approx -2.910383E\text{--}11
                                                                                                                                                                                                         0xdc = 1.1011100_{-} = -0b1.0 \times 2^{2}9 = -536870912.0
                                                                   0x5c = 0_{-}10111100_{-} = +0b1.0 \times 2^{2}9 = 536870912.0
{\tt 0x1d} = {\tt 0\_0011101\_} = +0{\tt b1.0} \times 2 \hat{\ \ } -34 \approx 5.8207661 E-11
                                                                                                                                     0x9d = 1_0011101_ = -0b1.0 \times 2^-34 \approx -5.8207661E-11
                                                                   0x5d = 0.1011101_{-} = +0b1.0 \times 2^{3}0 = 1073741824.0
                                                                                                                                                                                                         0xdd = 1_1011101_1 = -0b1.0 \times 2^30 = -1073741824.0
                                                                                                                                     0x9e = 1.0011110_{-} = -0b1.0 \times 2^{-33} \approx -1.1641532E-10
0x1e = 0.0011110 = +0b1.0 \times 2^{-33} \approx 1.1641532E-10
                                                                                                                                                                                                         0xde = 1_{-}10111110_{-} = -0b1.0 \times 2^{\circ}31 = -2147483648.0
                                                                   0x5e = 0_{-}10111110_{-} = +0b1.0 \times 2^{3}1 = 2147483648.0
0x1f = 0.0011111_{-} = +0b1.0 \times 2^{-32} \approx 2.3283064E-10
                                                                   0x5f = 0_10111111_1 = +0b1.0 \times 2^32 = 4294967296.0
                                                                                                                                     0x9f = 1.00111111. = -0b1.0 \times 2^{-32} \approx -2.3283064E-10
                                                                                                                                                                                                         0xdf = 1_1011111_1 = -0b1.0 \times 2^32 = -4294967296.0
0x20 = 0.0100000 = +0b1.0 \times 2^{-31} \approx 4.6566129E-10
                                                                   0x60 = 0.1100000 = +0b1.0 \times 2^33 = 8589934592.0
                                                                                                                                     0xa0 = 1.0100000 = -0b1.0 \times 2^{-31} \approx -4.6566129E-10
                                                                                                                                                                                                         0xe0 = 1_1100000_1 = -0b1.0 \times 2^33 = -8589934592.0
0x21 = 0.0100001 = +0b1.0 \times 2^{-30} \approx 9.3132257E-10
                                                                   0x61 = 0_1100001_1 = +0b1.0 \times 2^34 = 17179869184.0
                                                                                                                                     0xa1 = 1_0100001_ = -0b1.0 \times 2^-30 \approx -9.3132257E-10
                                                                                                                                                                                                         0xe1 = 1_1100001_1 = -0b1.0 \times 2^34 = -17179869184.0
0x22 = 0.0100010. = +0b1.0 \times 2^{-29} \approx 1.8626451E-09
                                                                   0x62 = 0_{-}1100010_{-} = +0b1.0 \times 2^{3}5 = 34359738368.0
                                                                                                                                     0xa2 = 1.0100010. = -0b1.0 \times 2^{-29} \approx -1.8626451E-09
                                                                                                                                                                                                         0xe2 = 1_1100010_1 = -0b1.0 \times 2^35 = -34359738368.0
0x23 = 0.0100011_{-} = +0b1.0 \times 2^{-28} \approx 3.7252903E-09
                                                                   0x63 = 0.1100011. = +0b1.0 \times 2^36 = 68719476736.0
                                                                                                                                     0xa3 = 1.0100011. = -0b1.0 \times 2^{-28} \approx -3.7252903E-09
                                                                                                                                                                                                         0xe3 = 1.1100011 = -0b1.0 \times 2^36 = -68719476736.0
                                                                                                                                     0xa4 = 1_0100100_0 = -0b1.0 \times 2^2 - 27 \approx -7.4505806E - 09
                                                                                                                                                                                                         0xe4 = 1_1100100_1 = -0b1.0 \times 2^37 \approx -1.3743895e + 11
0x24 = 0.0100100 = +0b1.0 \times 2^{-27} \approx 7.4505806E-09
                                                                   0x64 = 0_{1100100} = +0b1.0 \times 2^{37} = 137438953472.0
                                                                                                                                                                                                         0xe5 = 1_1100101_2 = -0b1.0 \times 2^38 \approx -2.7487791e + 11
0x25 = 0_0100101_ = +0b1.0 \times 2^-26 \approx 1.4901161E-08
                                                                   0x65 = 0_1100101_ = +0b1.0 \times 2^38 = 274877906944.0
                                                                                                                                     0xa5 = 1_0100101_ = -0b1.0 \times 2^-26 \approx -1.4901161E-08
0x26 = 0.0100110 = +0b1.0 \times 2^{-25} \approx 2.9802322E-08
                                                                                                                                     0xa6 = 1.0100110. = -0b1.0 \times 2^{-25} \approx -2.9802322E-08
                                                                                                                                                                                                         0xe6 = 1_1100110_1 = -0b1.0 \times 2^39 \approx -5.4975581e + 11
                                                                   0x66 = 0.1100110. = +0b1.0 \times 2^39 = 549755813888.0
0x27 = 0.0100111_{-} = +0b1.0 \times 2^{-24} \approx 5.9604645E-08
                                                                                                                                     0xa7 = 1_0100111_ = -0b1.0 \times 2^-24 \approx -5.9604645E-08
                                                                                                                                                                                                         0xe7 = 1.1100111. = -0b1.0 \times 2^40 \approx -1.0995116e + 12
                                                                   0x67 = 0.1100111_{-} = +0b1.0 \times 2^{4}0 \approx 1.0995116e + 12
0x28 = 0.0101000_{-} = +0b1.0 \times 2^{-23} \approx 1.1920929E-07
                                                                   0x68 = 0.1101000_{-} = +0b1.0 \times 2^{4}1 \approx 2.1990233e + 12
                                                                                                                                     0xa8 = 1.0101000 = -0b1.0 \times 2^{-23} \approx -1.1920929E-07
                                                                                                                                                                                                         0xe8 = 1_1101000_1 = -0b1.0 \times 2^41 \approx -2.1990233e + 12
0x29 = 0.0101001 = +0b1.0 \times 2^{-22} \approx 2.3841858E-07
                                                                   0x69 = 0_1101001_ = +0b1.0 \times 2^42 \approx 4.3980465e + 12
                                                                                                                                     0xa9 = 1_0101001_ = -0b1.0 \times 2^-22 \approx -2.3841858E-07
                                                                                                                                                                                                         0xe9 = 1_1101001_1 = -0b1.0 \times 2^42 \approx -4.3980465e + 12
                                                                                                                                                                                                         0 \text{xea} = 1_{-}1101010_{-} = -0 \text{b} 1.0 \times 2^{2} 3 \approx -8.796093 \text{e} + 12
0x2a = 0.0101010. = +0b1.0 \times 2^{-21} \approx 4.7683716E-07
                                                                   0x6a = 0_1101010_1 = +0b1.0 \times 2^43 \approx 8.796093e + 12
                                                                                                                                     0xaa = 1.0101010. = -0b1.0 \times 2^{-21} \approx -4.7683716E-07
0x2b = 0.0101011_{-} = +0b1.0 \times 2^{-20} \approx 9.5367432E-07
                                                                   0x6b = 0.1101011_{-} = +0b1.0 \times 2^{44} \approx 1.7592186e + 13
                                                                                                                                     0xab = 1.0101011. = -0b1.0 \times 2^{-20} \approx -9.5367432E-07
                                                                                                                                                                                                         0xeb = 1.1101011. = -0b1.0 \times 2^44 \approx -1.7592186e + 13
0x2c = 0.0101100 = +0b1.0 \times 2^{-19} \approx 1.9073486E-06
                                                                   0x6c = 0_1101100_1 = +0b1.0 \times 2^45 \approx 3.5184372e + 13
                                                                                                                                     0xac = 1_0101100_{-} = -0b1.0 \times 2^{-19} \approx -1.9073486E-06
                                                                                                                                                                                                         0 \text{xec} = 1_{-}1101100_{-} = -0 \text{b} 1.0 \times 2^{2}45 \approx -3.5184372 \text{e} + 13
0x2d = 0_0101101_ = +0b1.0 \times 2^-18 \approx 3.8146973E-06
                                                                   0x6d = 0_1101101_1 = +0b1.0 \times 2^46 \approx 7.0368744e + 13
                                                                                                                                     0xad = 1_0101101_ = -0b1.0 \times 2^-18 \approx -3.8146973E-06
                                                                                                                                                                                                         0xed = 1_1101101_1 = -0b1.0 \times 2^46 \approx -7.0368744e + 13
0x2e = 0.0101110. = +0b1.0 \times 2^{-17} \approx 7.6293945E-06
                                                                   0x6e = 0_{-}1101110_{-} = +0b1.0 \times 2^{2}47 \approx 1.4073749e + 14
                                                                                                                                     0xae = 1.0101110. = -0b1.0 \times 2^{-17} \approx -7.6293945E-06
                                                                                                                                                                                                         0xee = 1.1101110. = -0b1.0 \times 2^47 \approx -1.4073749e + 14
                                                                                                                                                                                                         0 \text{xef} = 1.11011111. = -0b1.0 \times 2^48 \approx -2.8147498e + 14
0x2f = 0.0101111_{-} = +0b1.0 \times 2^{-1}6 \approx 1.5258789E-05
                                                                   0x6f = 0.1101111. = +0b1.0 \times 2^48 \approx 2.8147498e + 14
                                                                                                                                     0xaf = 1.01011111. = -0b1.0 \times 2^{-1}6 \approx -1.5258789E-05
                                                                                                                                                                                                         0xf0 = 1_1110000_1 = -0b1.0 \times 2^49 \approx -5.6294995e + 14
                                                                                                                                     0xb0 = 1_0110000_{-} = -0b1.0 \times 2^{-15} \approx -3.0517578E-05
0x30 = 0.0110000_{-} = +0b1.0 \times 2^{-15} \approx 3.0517578E-05
                                                                   0x70 = 0.1110000_{-} = +0b1.0 \times 2^{49} \approx 5.6294995e + 14
                                                                                                                                                                                                         0xf1 = 1_1110001_{-} = -0b1.0 \times 2^{5}0 \approx -1.1258999e + 15
0x31 = 0_0110001_ = +0b1.0 \times 2^-14 \approx 6.1035156E-05
                                                                   0x71 = 0_1110001_ = +0b1.0 \times 250 \approx 1.1258999e + 15
                                                                                                                                     0xb1 = 1_0110001_ = -0b1.0 \times 2^-14 \approx -6.1035156E-05
0x32 = 0.0110010 = +0b1.0 \times 2^{-13} \approx 0.00012207031
                                                                   0x72 = 0_{-}1110010_{-} = +0b1.0 \times 2^{5}1 \approx 2.2517998e + 15
                                                                                                                                     0xb2 = 1_0110010_ = -0b1.0 \times 2^-13 \approx -0.00012207031
                                                                                                                                                                                                         0xf2 = 1_1110010_1 = -0b1.0 \times 2^51 \approx -2.2517998e + 15
                                                                                                                                                                                                         0xf3 = 1.1110011. = -0b1.0 \times 2^52 \approx -4.5035996e + 15
0x33 = 0.0110011_{-} = +0b1.0 \times 2^{-12} = 0.000244140625
                                                                   0x73 = 0.1110011_{-} = +0b1.0 \times 2^{2} = 4.5035996e + 15
                                                                                                                                     0xb3 = 1_0110011_ = -0b1.0 \times 2^-12 \approx -0.00024414062
0x34 = 0.0110100_{-} = +0b1.0 \times 2^{-}11 = 0.00048828125
                                                                   0x74 = 0_1110100_1 = +0b1.0 \times 2^53 \approx 9.0071993e + 15
                                                                                                                                     0xb4 = 1_0110100_0 = -0b1.0 \times 2^-11 = -0.00048828125
                                                                                                                                                                                                         0xf4 = 1_1110100_1 = -0b1.0 \times 2^53 \approx -9.0071993e + 15
                                                                                                                                                                                                         0xf5 = 1_1110101_1 = -0b1.0 \times 2^54 \approx -1.8014399e + 16
0x35 = 0.0110101_{-} = +0b1.0 \times 2^{-}10 = 0.0009765625
                                                                   0x75 = 0.1110101 = +0b1.0 \times 254 \approx 1.8014399e + 16
                                                                                                                                     0xb5 = 1.0110101. = -0b1.0 \times 2^{-10} = -0.0009765625
                                                                                                                                                                                                         0xf6 = 1_1110110_1 = -0b1.0 \times 2^55 \approx -3.6028797e + 16
0x36 = 0.0110110. = +0b1.0 \times 2^{-9} = 0.001953125
                                                                   0x76 = 0.1110110. = +0b1.0 \times 255 \approx 3.6028797e + 16
                                                                                                                                     0xb6 = 1.0110110. = -0b1.0 \times 2^{-9} = -0.001953125
0x37 = 0.0110111_{-} = +0b1.0 \times 2^{-8} = 0.00390625
                                                                   0x77 = 0_1110111_1 = +0b1.0 \times 2^56 \approx 7.2057594e + 16
                                                                                                                                     0xb7 = 1_0110111_0 = -0b1.0 \times 2^-8 = -0.00390625
                                                                                                                                                                                                         0xf7 = 1_1110111_1 = -0b1.0 \times 2^56 \approx -7.2057594e + 16
0x38 = 0.0111000_{-} = +0b1.0 \times 2^{-7} = 0.0078125
                                                                   0x78 = 0_1111000_1 = +0b1.0 \times 2^57 \approx 1.4411519e + 17
                                                                                                                                     0xb8 = 1_0111000_ = -0b1.0 \times 2^-7 = -0.0078125
                                                                                                                                                                                                         0xf8 = 1_11111000_{-} = -0b1.0 \times 2^{57} \approx -1.4411519e + 17
0x39 = 0.0111001 = +0b1.0 \times 2^{-6} = 0.015625
                                                                   0x79 = 0_1111001_1 = +0b1.0 \times 2^58 \approx 2.8823038e + 17
                                                                                                                                     0xb9 = 1_0111001_ = -0b1.0 \times 2^-6 = -0.015625
                                                                                                                                                                                                         0xf9 = 1_1111001_1 = -0b1.0 \times 2^58 \approx -2.8823038e + 17
0x3a = 0.0111010_{-} = +0b1.0 \times 2^{-5} = 0.03125
                                                                   0x7a = 0.1111010_{-} = +0b1.0 \times 2^{59} \approx 5.7646075e + 17
                                                                                                                                     0xba = 1.0111010. = -0b1.0 \times 2^-5 = -0.03125
                                                                                                                                                                                                         0xfa = 1_{1111010} = -0b1.0 \times 259 \approx -5.7646075e + 17
0x3b = 0_0111011_ = +0b1.0 \times 2^-4 = 0.0625
                                                                   0x7b = 0_{-}1111011_{-} = +0b1.0 \times 260 \approx 1.1529215e + 18
                                                                                                                                     0xbb = 1_0111011_ = -0b1.0 \times 2^-4 = -0.0625
                                                                                                                                                                                                         0xfb = 1_1111011_1 = -0b1.0 \times 2^{\circ}60 \approx -1.1529215e + 18
0x3c = 0_0111100_ = +0b1.0 \times 2^-3 = 0.125
                                                                   0x7c = 0.11111100_{-} = +0b1.0 \times 2^{\circ}61 \approx 2.305843e + 18
                                                                                                                                     0xbc = 1_01111100_ = -0b1.0 \times 2^-3 = -0.125
                                                                                                                                                                                                         0xfc = 1_11111100_1 = -0b1.0 \times 2^{\circ}61 \approx -2.305843e + 18
0x3d = 0_0111101_ = +0b1.0 \times 2^-2 = 0.25
                                                                   0x7d = 0_11111101_ = +0b1.0 \times 262 \approx 4.611686e + 18
                                                                                                                                     0xbd = 1_0111101_ = -0b1.0 \times 2^2 = -0.25
                                                                                                                                                                                                         0xfd = 1_11111101_1 = -0b1.0 \times 2^{\circ}62 \approx -4.611686e + 18
0x3e = 0.01111110_{-} = +0b1.0 \times 2^{-1} = 0.5
                                                                   0x7e = 0.11111110_{-} = +0b1.0 \times 2^{\circ}63 \approx 9.223372e + 18
                                                                                                                                     0xbe = 1_01111110_0 = -0b1.0 \times 2^{-1} = -0.5
                                                                                                                                                                                                         0xfe = 1.11111110_{-} = -0b1.0 \times 2^{\circ}63 \approx -9.223372e + 18
0x3f = 0.01111111. = +0b1.0 \times 20 = 1.0
                                                                   0x7f = 0_11111111_ = +Inf
                                                                                                                                     0xbf = 1_01111111_0 = -0b1.0 \times 2^0 = -1.0
                                                                                                                                                                                                         0xff = 1_11111111_1 = -Inf
```

C.2 Value Table: P2, emin = -31, emax = 31

$0x00 = 0.000000_0 = 0.0$	$0x40 = 0_100000_0 = +0b1.0 \times 20 = 1.0$	$0x80 = 1_000000_0 = NaN$	$0xc0 = 1_100000_0 = -0b1.0 \times 2^0 = -1.0$
$0x01 = 0_000000_1 = +0b0.1 \times 2^-31 \approx 2.3283064E-10$	$0x41 = 0_100000_1 = +0b1.1 \times 20 = 1.5$	$0x81 = 1_000000_1 = -0b0.1 \times 2^-31 \approx -2.3283064E-10$	$0xc1 = 1_100000_1 = -0b1.1 \times 2^0 = -1.5$
$0x02 = 0.000001.0 = +0b1.0 \times 2^{-31} \approx 4.6566129E-10$	$0x42 = 0.100001.0 = +0b1.0 \times 2^1 = 2.0$	$0x82 = 1.000001.0 = -0b1.0 \times 2^{-31} \approx -4.6566129E-10$	$0xc2 = 1_{-1}00001_{-0} = -0b1.0 \times 2^{1} = -2.0$
$0x03 = 0.000001.1 = +0b1.1 \times 2^{-31} \approx 6.9849193E-10$	$0x43 = 0_100001_1 = +0b1.1 \times 2^1 = 3.0$	$0x83 = 1.000001.1 = -0b1.1 \times 2^{-31} \approx -6.9849193E-10$	$0xc3 = 1_100001_1 = -0b1.1 \times 2^1 = -3.0$
$0x04 = 0.000010_0 = +0b1.0 \times 2^{-30} \approx 9.3132257E-10$	$0x44 = 0_100010_0 = +0b1.0 \times 2^2 = 4.0$	$0x84 = 1.000010.0 = -0b1.0 \times 2^{-30} \approx -9.3132257E-10$	$0xc4 = 1.100010.0 = -0b1.0 \times 2^2 = -4.0$
$0x05 = 0.000010_1 = +0b1.1 \times 2^{-30} \approx 1.3969839E-09$	$0x45 = 0.100010_1 = +0b1.1 \times 2^2 = 6.0$	$0x85 = 1.000010.1 = -0b1.1 \times 2^{-30} \approx -1.3969839E-09$	$0xc5 = 1_100010_1 = -0b1.1 \times 2^2 = -6.0$
$0x06 = 0.000011.0 = +0b1.0 \times 2^{-2}9 \approx 1.8626451E-09$	$0x46 = 0.100011.0 = +0b1.0 \times 2^3 = 8.0$	$0x86 = 1.000011.0 = -0b1.0 \times 2^{-29} \approx -1.8626451E-09$	$0xc6 = 1.100011.0 = -0b1.0 \times 2^3 = -8.0$
$0x07 = 0.000011.0 = +0b1.0 \times 2 - 29 \approx 1.0020451E-09$ $0x07 = 0.000011.1 = +0b1.1 \times 2^{-29} \approx 2.7939677E-09$	$0x40 = 0.100011.0 = +001.0 \times 2.3 = 0.0$ $0x47 = 0.100011.1 = +001.1 \times 2.3 = 12.0$	$0x87 = 1.000011.0 = -0b1.0 \times 2^{-29} \approx -1.0020451E^{-09}$ $0x87 = 1.000011.1 = -0b1.1 \times 2^{-29} \approx -2.7939677E^{-09}$	$0xc7 = 1.100011.0 = -0b1.0 \times 2.3 = -0.0$ $0xc7 = 1.100011.1 = -0b1.1 \times 2^3 = -12.0$
			$0xc7 = 1.100011.1 = -0b1.1 \times 2.3 = -12.0$ $0xc8 = 1.100100.0 = -0b1.0 \times 2^4 = -16.0$
$0x08 = 0.000100.0 = +0b1.0 \times 2^{-2}8 \approx 3.7252903E-09$	$0x48 = 0.100100.0 = +0b1.0 \times 2^4 = 16.0$	$0x88 = 1.000100_0 = -0b1.0 \times 2^2 - 28 \approx -3.7252903E - 09$	
$0x09 = 0.000100_1 = +0b1.1 \times 2^{-28} \approx 5.5879354E-09$	$0x49 = 0_100100_1 = +0b1.1 \times 2^4 = 24.0$	$0x89 = 1.000100_1 = -0b1.1 \times 2^2 - 28 \approx -5.5879354E - 09$	$0xc9 = 1_{-1}00100_{-1} = -0b1.1 \times 2^{2} = -24.0$
$0x0a = 0.000101.0 = +0b1.0 \times 2^{-27} \approx 7.4505806E-09$	$0x4a = 0.100101.0 = +0b1.0 \times 2^5 = 32.0$	$0x8a = 1_000101_0 = -0b1.0 \times 2^2 - 27 \approx -7.4505806E - 09$	$0xca = 1.100101.0 = -0b1.0 \times 2^5 = -32.0$
$0x0b = 0.000101.1 = +0b1.1 \times 2^{-27} \approx 1.1175871E-08$	$0x4b = 0.100101.1 = +0b1.1 \times 2^5 = 48.0$	$0x8b = 1.000101.1 = -0b1.1 \times 2^{-27} \approx -1.1175871E-08$	$0xcb = 1.100101.1 = -0b1.1 \times 2^5 = -48.0$
$0x0c = 0.000110_0 = +0b1.0 \times 2^-26 \approx 1.4901161E-08$	$0x4c = 0_100110_0 = +0b1.0 \times 2\% = 64.0$	$0x8c = 1_000110_0 = -0b1.0 \times 2^-26 \approx -1.4901161E-08$	$0xcc = 1_100110_0 = -0b1.0 \times 2^6 = -64.0$
$0x0d = 0.000110_1 = +0b1.1 \times 2^{-2}6 \approx 2.2351742E-08$	$0x4d = 0_100110_1 = +0b1.1 \times 2^6 = 96.0$	$0x8d = 1_000110_1 = -0b1.1 \times 2^2 - 26 \approx -2.2351742E - 08$	$0xcd = 1_100110_1 = -0b1.1 \times 2^6 = -96.0$
$0x0e = 0.000111.0 = +0b1.0 \times 2^{-25} \approx 2.9802322E-08$	$0x4e = 0.100111.0 = +0b1.0 \times 27 = 128.0$	$0x8e = 1.000111.0 = -0b1.0 \times 2^{-25} \approx -2.9802322E-08$	$0xce = 1.100111.0 = -0b1.0 \times 27 = -128.0$
$0x0f = 0.000111.1 = +0b1.1 \times 2^{-25} \approx 4.4703484E-08$	$0x4f = 0.100111.1 = +0b1.1 \times 27 = 192.0$	$0x8f = 1.000111.1 = -0b1.1 \times 2^{-25} \approx -4.4703484E-08$	$0xcf = 1.100111.1 = -0b1.1 \times 2^7 = -192.0$
$0x10 = 0.001000_0 = +0b1.0 \times 2^{-24} \approx 5.9604645E-08$	$0x50 = 0_101000_0 = +0b1.0 \times 2\% = 256.0$	$0x90 = 1.001000.0 = -0b1.0 \times 2^{-24} \approx -5.9604645E-08$	$0xd0 = 1_101000_0 = -0b1.0 \times 2^8 = -256.0$
$0x11 = 0.001000.1 = +0b1.1 \times 2^{-24} \approx 8.9406967E-08$	$0x51 = 0_101000_1 = +0b1.1 \times 2\% = 384.0$	$0x91 = 1_001000_1 = -0b1.1 \times 2^-24 \approx -8.9406967E-08$	$0xd1 = 1_101000_1 = -0b1.1 \times 2^8 = -384.0$
$0x12 = 0.001001.0 = +0b1.0 \times 2^{2} = 3 \approx 1.1920929E = 07$	$0x52 = 0.101001.0 = +0b1.0 \times 2^{\circ}9 = 512.0$	$0x92 = 1.001001.0 = -0b1.0 \times 2^{-23} \approx -1.1920929E-07$	$0xd2 = 1.101001.0 = -0b1.0 \times 2^9 = -512.0$
$0x13 = 0.001001.1 = +0b1.1 \times 2^{2} = 20 \times 1.7881393E-07$	$0x53 = 0.101001.1 = +0b1.1 \times 29 = 768.0$	$0x93 = 1.001001.1 = -0b1.1 \times 2^{2} - 23 \approx -1.7881393E - 07$	$0xd3 = 1.101001.1 = -0b1.1 \times 2^{\circ}9 = -768.0$
$0x13 = 0.00100111 = +001.1 \times 2 - 23 \approx 1.7601353E - 07$ $0x14 = 0.001010.0 = +001.0 \times 2^{-22} \approx 2.3841858E - 07$	$0x53 = 0.101001.1 = +001.1 \times 2.9 = 700.0$ $0x54 = 0.101010.0 = +001.0 \times 2^{\circ}10 = 1024.0$	$0x94 = 1.001010101 = -0b1.1 \times 2^{-2}3 \approx -1.7661595E = 07$ $0x94 = 1.00101010 = -0b1.0 \times 2^{-2}2 \approx -2.3841858E = 07$	$0xd3 = 1.101001.1 = -001.1 \times 2.9 = -700.0$ $0xd4 = 1.101010.0 = -001.0 \times 2^{\circ}10 = -1024.0$
$0x15 = 0.001010_1 = +0b1.1 \times 2^{-2}2 \approx 3.5762787E-07$	$0x55 = 0_{-}101010_{-}1 = +0b1.1 \times 2^{-}10 = 1536.0$	$0x95 = 1.001010_1 = -0b1.1 \times 2^2 - 22 \approx -3.5762787E - 07$	$0xd5 = 1_{-}101010_{-}1 = -0b1.1 \times 2^{-}10 = -1536.0$
$0x16 = 0.001011.0 = +0b1.0 \times 2^{-21} \approx 4.7683716E-07$	$0x56 = 0.101011.0 = +0b1.0 \times 2^{1}1 = 2048.0$	$0x96 = 1.001011.0 = -0b1.0 \times 2^{2} - 21 \approx -4.7683716E - 07$	$0xd6 = 1.101011.0 = -0b1.0 \times 2^{1}1 = -2048.0$
$0x17 = 0.001011.1 = +0b1.1 \times 2^{-21} \approx 7.1525574E-07$	$0x57 = 0.101011.1 = +0b1.1 \times 2^11 = 3072.0$	$0x97 = 1_001011_1 = -0b1.1 \times 2^-21 \approx -7.1525574E-07$	$0xd7 = 1.101011.1 = -0b1.1 \times 2^11 = -3072.0$
$0x18 = 0.001100_0 = +0b1.0 \times 2^-20 \approx 9.5367432E-07$	$0x58 = 0_101100_0 = +0b1.0 \times 2^12 = 4096.0$	$0x98 = 1_001100_0 = -0b1.0 \times 2^-20 \approx -9.5367432E-07$	$0xd8 = 1_101100_0 = -0b1.0 \times 2^12 = -4096.0$
$0x19 = 0.001100_1 = +0b1.1 \times 2^{-20} \approx 1.4305115E-06$	$0x59 = 0_101100_1 = +0b1.1 \times 2^12 = 6144.0$	$0x99 = 1_001100_1 = -0b1.1 \times 2^2 - 20 \approx -1.4305115E - 06$	$0xd9 = 1_101100_1 = -0b1.1 \times 2^12 = -6144.0$
$0x1a = 0.001101.0 = +0b1.0 \times 2^{-19} \approx 1.9073486E-06$	$0x5a = 0.101101.0 = +0b1.0 \times 2^13 = 8192.0$	$0x9a = 1.001101.0 = -0b1.0 \times 2^{-1}9 \approx -1.9073486E-06$	$0xda = 1.101101.0 = -0b1.0 \times 2^13 = -8192.0$
$0x1b = 0.001101.1 = +0b1.1 \times 2^{-19} \approx 2.8610229E-06$	$0x5b = 0.101101.1 = +0b1.1 \times 2^13 = 12288.0$	$0x9b = 1.001101.1 = -0b1.1 \times 2^{-1}9 \approx -2.8610229E-06$	$0xdb = 1.101101.1 = -0b1.1 \times 2^13 = -12288.0$
$0x1c = 0.001110_0 = +0b1.0 \times 2^{-18} \approx 3.8146973E-06$	$0x5c = 0.101110.0 = +0b1.0 \times 2^14 = 16384.0$	$0x9c = 1_001110_0 = -0b1.0 \times 2^-18 \approx -3.8146973E-06$	$0xdc = 1_101110_0 = -0b1.0 \times 2^14 = -16384.0$
$0x1d = 0.001110_1 = +0b1.1 \times 2^-18 \approx 5.7220459E-06$	$0x5d = 0_101110_1 = +0b1.1 \times 2^14 = 24576.0$	$0x9d = 1_001110_1 = -0b1.1 \times 2^-18 \approx -5.7220459E-06$	$0xdd = 1_101110_1 = -0b1.1 \times 2^14 = -24576.0$
$0x1e = 0.001111.0 = +0b1.0 \times 2^{-17} \approx 7.6293945E-06$	$0x5e = 0.1011111.0 = +0b1.0 \times 2^{1}5 = 32768.0$	$0x9e = 1.001111.0 = -0b1.0 \times 2^{-17} \approx -7.6293945E-06$	$0xde = 1.1011111.0 = -0b1.0 \times 2^{15} = -32768.0$
$0x1f = 0.001111.1 = +0b1.1 \times 2^{-17} \approx 1.1444092E-05$	$0x5f = 0.101111.1 = +0b1.1 \times 2^{\circ}15 = 49152.0$	$0x9f = 1.001111.1 = -0b1.1 \times 2^{-17} \approx -1.1444092E-05$	$0xdf = 1.101111.1 = -0b1.1 \times 2^{\circ}15 = -49152.0$
$0x20 = 0.010000.0 = +0b1.0 \times 2^{-1}6 \approx 1.5258789E-05$	$0x60 = 0.110000.0 = +0b1.0 \times 2^{\circ}16 = 65536.0$	$0xa0 = 1.010000.0 = -0b1.0 \times 2^{-1}6 \approx -1.5258789E-05$	$0xe0 = 1.110000_0 = -0b1.0 \times 2^16 = -65536.0$
$0x20 = 0.01000020 = 001.0 \times 2 10 \approx 1.0250105E 05$ $0x21 = 0.010000_1 = +0b1.1 \times 2^-16 \approx 2.2888184E-05$	$0x60 = 0.11000010 = 001.0 \times 2 10 = 0000010$ $0x61 = 0.110000_1 = +0b1.1 \times 2^{\circ}16 = 98304.0$	$0xa1 = 1.010000.1 = -0b1.1 \times 2^{-1}6 \approx -2.2888184E-05$	$0xe0 = 1.110000.0 = 0b1.0 \times 2.10 = 00000.0$ $0xe1 = 1.110000.1 = -0b1.1 \times 2^{\circ}16 = -98304.0$
$0x22 = 0.010001.0 = +0b1.0 \times 2^{2}-15 \approx 3.0517578E-05$	$0x62 = 0.110001.0 = +0b1.0 \times 2^{\circ}17 = 131072.0$	$0xa2 = 1.010001.0 = -0b1.0 \times 2^{-1}5 \approx -3.0517578E-05$	$0xe2 = 1.110001.0 = -0b1.0 \times 2^{-1}7 = -131072.0$
$0x23 = 0.010001.1 = +0b1.1 \times 2^{-15} \approx 4.5776367E-05$	$0x63 = 0.110001.1 = +0b1.1 \times 2^{17} = 196608.0$	$0xa3 = 1.010001.1 = -0b1.1 \times 2^-15 \approx -4.5776367E-05$	$0xe3 = 1.110001.1 = -0b1.1 \times 2^{-1}7 = -196608.0$
$0x24 = 0.010010.0 = +0b1.0 \times 2^{-14} \approx 6.1035156E-05$	$0x64 = 0_110010_0 = +0b1.0 \times 2^18 = 262144.0$	$0xa4 = 1_010010_0 = -0b1.0 \times 2^-14 \approx -6.1035156E-05$	$0xe4 = 1.110010.0 = -0b1.0 \times 2^{18} = -262144.0$
$0x25 = 0_010010_1 = +0b1.1 \times 2^-14 \approx 9.1552734E-05$	$0x65 = 0_110010_1 = +0b1.1 \times 2^18 = 393216.0$	$0xa5 = 1_010010_1 = -0b1.1 \times 2^-14 \approx -9.1552734E-05$	$0xe5 = 1_110010_1 = -0b1.1 \times 2^18 = -393216.0$
$0x26 = 0.010011.0 = +0b1.0 \times 2^-13 \approx 0.00012207031$	$0x66 = 0_110011_0 = +0b1.0 \times 2^19 = 524288.0$	$0xa6 = 1.010011.0 = -0b1.0 \times 2^-13 \approx -0.00012207031$	$0xe6 = 1.110011.0 = -0b1.0 \times 2^19 = -524288.0$
$0x27 = 0.010011.1 = +0b1.1 \times 2^-13 \approx 0.00018310547$	$0x67 = 0_110011_1 = +0b1.1 \times 2^19 = 786432.0$	$0xa7 = 1_010011_1 = -0b1.1 \times 2^-13 \approx -0.00018310547$	$0xe7 = 1_110011_1 = -0b1.1 \times 2^19 = -786432.0$
$0x28 = 0.010100.0 = +0b1.0 \times 2^{-12} = 0.000244140625$	$0x68 = 0_110100_0 = +0b1.0 \times 2^20 = 1048576.0$	$0xa8 = 1_010100_0 = -0b1.0 \times 2^-12 \approx -0.00024414062$	$0xe8 = 1_110100_0 = -0b1.0 \times 2^20 = -1048576.0$
$0x29 = 0.010100_1 = +0b1.1 \times 2^-12 \approx 0.00036621094$	$0x69 = 0_110100_1 = +0b1.1 \times 2^20 = 1572864.0$	$0xa9 = 1_010100_1 = -0b1.1 \times 2^-12 \approx -0.00036621094$	$0xe9 = 1_110100_1 = -0b1.1 \times 2^20 = -1572864.0$
$0x2a = 0.010101.0 = +0b1.0 \times 2^{-11} = 0.00048828125$	$0x6a = 0.110101.0 = +0b1.0 \times 2^21 = 2097152.0$	$0xaa = 1.010101.0 = -0b1.0 \times 2^{-11} = -0.00048828125$	$0xea = 1_110101_0 = -0b1.0 \times 2^2 = -2097152.0$
$0x2b = 0.010101.1 = +0b1.1 \times 2^{-11} = 0.000732421875$	$0x6b = 0_110101_1 = +0b1.1 \times 2^21 = 3145728.0$	$0xab = 1.010101.1 = -0b1.1 \times 2^{-1}1 \approx -0.00073242188$	$0xeb = 1.110101.1 = -0b1.1 \times 2^2 1 = -3145728.0$
$0x2c = 0.010110_0 = +0b1.0 \times 2^-10 = 0.0009765625$	$0x6c = 0_110110_0 = +0b1.0 \times 2^2 2 = 4194304.0$	$0xac = 1_010110_0 = -0b1.0 \times 2^-10 = -0.0009765625$	$0 \text{xec} = 1.110110.0 = -0 \text{b} 1.0 \times 2^2 2 = -4194304.0$
$0x2d = 0_010110_1 = +0b1.1 \times 2^-10 = 0.00146484375$	$0x6d = 0_110110_1 = +0b1.1 \times 2^2 = 6291456.0$	$0xad = 1_010110_1 = -0b1.1 \times 2^-10 = -0.00146484375$	$0xed = 1_110110_1 = -0b1.1 \times 2^2 = -6291456.0$
$0x2e = 0.010111.0 = +0b1.0 \times 2^{-9} = 0.001953125$	$0x6e = 0.110111.0 = +0b1.0 \times 2^2 = 8388608.0$	$0xae = 1.010111.0 = -0b1.0 \times 2^{-9} = -0.001953125$	$0 \text{xee} = 1.1101111.0 = -0b1.0 \times 2^2 = -8388608.0$
$0x2f = 0.010111.0 = +0b1.0 \times 2 = 0.001303120$ $0x2f = 0.010111.1 = +0b1.1 \times 2^-9 = 0.0029296875$	$0x6f = 0.110111.1 = +0b1.1 \times 2^2 3 = 12582912.0$	$0xaf = 1.010111.1 = -0b1.0 \times 2^{-5} = -0.001333125$ $0xaf = 1.010111.1 = -0b1.1 \times 2^{-9} = -0.0029296875$	$0 \text{xef} = 1.110111.0 = 001.0 \times 2.23 = 0300000.0$ $0 \text{xef} = 1.110111.1 = -001.1 \times 2^{\circ}23 = -12582912.0$
$0x30 = 0.011000_0 = +0b1.0 \times 2^{-8} = 0.00390625$	$0x70 = 0.1110111.1 = +001.1 \times 2.23 = 12362312.0$ $0x70 = 0.111000.0 = +001.0 \times 2^2 = 16777216.0$	$0xb0 = 1.010111.1 = -0b1.1 \times 2^{-9} = -0.0029290873$ $0xb0 = 1.011000_0 = -0b1.0 \times 2^{-8} = -0.00390625$	$0xf0 = 1.110111.1 = -0b1.1 \times 2.23 = -12302912.0$ $0xf0 = 1.111000.0 = -0b1.0 \times 2^24 = -16777216.0$
$0x31 = 0.011000_1 = +0b1.1 \times 2^{-8} = 0.005859375$	$0x71 = 0_111000_1 = +0b1.1 \times 2^24 = 25165824.0$	$0xb1 = 1_011000_1 = -0b1.1 \times 2^-8 = -0.005859375$	$0xf1 = 1_111000_1 = -0b1.1 \times 2^2 = -25165824.0$
$0x32 = 0.011001.0 = +0b1.0 \times 2^{-7} = 0.0078125$	$0x72 = 0.111001.0 = +0b1.0 \times 2^25 = 33554432.0$	$0xb2 = 1.011001.0 = -0b1.0 \times 2^{-7} = -0.0078125$	$0xf2 = 1_111001_0 = -0b1.0 \times 2^2 = -33554432.0$
$0x33 = 0.011001_1 = +0b1.1 \times 2^-7 = 0.01171875$	$0x73 = 0.111001_1 = +0b1.1 \times 2^25 = 50331648.0$	$0xb3 = 1.011001.1 = -0b1.1 \times 2^{-7} = -0.01171875$	$0xf3 = 1.111001.1 = -0b1.1 \times 2^2 = -50331648.0$
$0x34 = 0_011010_0 = +0b1.0 \times 2^-6 = 0.015625$	$0x74 = 0_111010_0 = +0b1.0 \times 2^26 = 67108864.0$	$0xb4 = 1_011010_0 = -0b1.0 \times 2^-6 = -0.015625$	$0xf4 = 1_111010_0 = -0b1.0 \times 2^26 = -67108864.0$
$0x35 = 0_011010_1 = +0b1.1 \times 2^-6 = 0.0234375$	$0x75 = 0_111010_1 = +0b1.1 \times 2^26 = 100663296.0$	$0xb5 = 1_011010_1 = -0b1.1 \times 2^-6 = -0.0234375$	$0xf5 = 1_111010_1 = -0b1.1 \times 2^26 = -100663296.0$
$0x36 = 0.011011.0 = +0b1.0 \times 2^{-5} = 0.03125$	$0x76 = 0.111011.0 = +0b1.0 \times 2^2 7 = 134217728.0$	$0xb6 = 1.011011.0 = -0b1.0 \times 2^{-5} = -0.03125$	$0xf6 = 1.111011.0 = -0b1.0 \times 2^27 = -134217728.0$
$0x37 = 0_011011_1 = +0b1.1 \times 2^5 = 0.046875$	$0x77 = 0_111011_1 = +0b1.1 \times 2^27 = 201326592.0$	$0xb7 = 1_011011_1 = -0b1.1 \times 2^-5 = -0.046875$	$0xf7 = 1_111011_1 = -0b1.1 \times 2^27 = -201326592.0$
$0x38 = 0_011100_0 = +0b1.0 \times 2^-4 = 0.0625$	$0x78 = 0_111100_0 = +0b1.0 \times 2^28 = 268435456.0$	$0xb8 = 1_011100_0 = -0b1.0 \times 2^-4 = -0.0625$	$0xf8 = 1_111100_0 = -0b1.0 \times 2^28 = -268435456.0$
$0x39 = 0.011100_1 = +0b1.1 \times 2^{-4} = 0.09375$	$0x79 = 0_111100_1 = +0b1.1 \times 2^28 = 402653184.0$	$0xb9 = 1_011100_1 = -0b1.1 \times 2^-4 = -0.09375$	$0xf9 = 1_111100_1 = -0b1.1 \times 2^28 = -402653184.0$
$0x3a = 0.011101.0 = +0b1.0 \times 2^{-3} = 0.125$	$0x7a = 0.111101.0 = +0b1.0 \times 2^{\circ}29 = 536870912.0$	$0xba = 1_011101_0 = -0b1.0 \times 2^-3 = -0.125$	$0xfa = 1.111101.0 = -0b1.0 \times 2^29 = -536870912.0$
$0x3b = 0.011101.1 = +0b1.1 \times 2^{-3} = 0.1875$	$0x7b = 0.111101.1 = +0b1.1 \times 2^29 = 805306368.0$	$0xbb = 1.011101.1 = -0b1.1 \times 2^{-3} = -0.1875$	$0xfb = 1.111101.1 = -0b1.1 \times 2^29 = -805306368.0$
$0x3c = 0.011110.0 = +0b1.0 \times 2^{-2} = 0.25$	$0x7c = 0.111110_0 = +0b1.0 \times 2^{\circ}30 = 1073741824.0$	$0xbc = 1.011110.0 = -0b1.0 \times 2^{-2} = -0.25$	$0xfc = 1.111110.0 = -0b1.0 \times 2^30 = -1073741824.0$
$0x3d = 0.011110.1 = +0b1.1 \times 2^{-2} = 0.375$	$0x7d = 0.111110_1 = +0b1.1 \times 2^30 = 1610612736.0$	$0xbd = 1.011110.10 = 001.0 \times 2 \cdot 2 = 0.20$ $0xbd = 1.011110.1 = -0b1.1 \times 2^{-2} = -0.375$	$0xfd = 1_111110_1 = -0b1.1 \times 2^{\circ}30 = -1610612736.0$
		$0xbe = 1.0111111.0 = -0b1.0 \times 2^{-1} = -0.5$	$0xfe - 1 111111 00b1 0 \times 2^312147493649 0$
$0x3e = 0.0111111.0 = +0b1.0 \times 2^{-1} = 0.5$ $0x3f = 0.0111111.1 = +0b1.1 \times 2^{-1} = 0.75$	$0x7e = 0.1111111.0 = +0b1.0 \times 2^31 = 2147483648.0$ 0x7f = 0.111111.1 = +Inf	$0xbe = 1.011111.0 = -0b1.0 \times 2^{-1} = -0.5$ $0xbf = 1.011111.1 = -0b1.1 \times 2^{-1} = -0.75$	$0xfe = 1.111111.0 = -0b1.0 \times 2^31 = -2147483648.0$ 0xff = 1.111111.1 = -Inf

C.3 Value Table: P3, emin = -15, emax = 15

$0x00 = 0.00000_00 = 0.0$	$0x40 = 0_10000_00 = +0b1.00 \times 2^0 = 1.0$	$0x80 = 1_00000_00 = NaN$	$0xc0 = 1_10000_00 = -0b1.00 \times 2^{\circ} = -1.0$
$0x01 = 0.00000.01 = +0b0.01 \times 2^{-15} \approx 7.6293945E-06$	$0x41 = 0_10000_01 = +0b1.01 \times 2^0 = 1.25$	$0x81 = 1_00000_01 = -0b0.01 \times 2^-15 \approx -7.6293945E-06$	$0xc1 = 1_10000_01 = -0b1.01 \times 2^0 = -1.25$
$0x02 = 0.00000.10 = +0b0.10 \times 2^{-15} \approx 1.5258789E-05$	$0x42 = 0.10000.10 = +0b1.10 \times 2^{\circ}0 = 1.5$	$0x82 = 1.00000.10 = -0b0.10 \times 2^{-15} \approx -1.5258789E-05$	$0xc2 = 1_{-}10000_{-}10 = -0b1.10 \times 2^{\circ}0 = -1.5$
$0x03 = 0.00000.11 = +0b0.11 \times 2^-15 \approx 2.2888184E-05$	$0x43 = 0.10000.11 = +0b1.11 \times 2^{\circ}0 = 1.75$	$0x83 = 1.00000.11 = -0b0.11 \times 2^{-15} \approx -2.2888184E-05$	$0xc3 = 1.10000.11 = -0b1.11 \times 2^{\circ} = -1.75$
$0x04 = 0.00001.00 = +0b1.00 \times 2^{-15} \approx 3.0517578E-05$	$0x44 = 0_10001_00 = +0b1.00 \times 2^1 = 2.0$	$0x84 = 1.00001.00 = -0b1.00 \times 2^{-15} \approx -3.0517578E-05$	$0xc4 = 1_10001_00 = -0b1.00 \times 2^1 = -2.0$
$0x05 = 0.00001.01 = +0b1.01 \times 2^{-15} \approx 3.8146973E-05$	$0x45 = 0_10001_01 = +0b1.01 \times 2^1 = 2.5$	$0x85 = 1_00001_01 = -0b1.01 \times 2^-15 \approx -3.8146973E-05$	$0xc5 = 1_10001_01 = -0b1.01 \times 2^1 = -2.5$
$0x06 = 0.00001.10 = +0b1.10 \times 2^{-1}5 \approx 4.5776367E-05$	$0x46 = 0.10001.10 = +0b1.10 \times 2^1 = 3.0$	$0x86 = 1.00001.10 = -0b1.10 \times 2^{-15} \approx -4.5776367E-05$	$0xc6 = 1.10001.10 = -0b1.10 \times 2^1 = -3.0$
$0x07 = 0.00001.11 = +0b1.11 \times 2^{-15} \approx 5.3405762E-05$	$0x47 = 0.10001.11 = +0b1.11 \times 2^1 = 3.5$	$0x87 = 1.00001.11 = -0b1.11 \times 2^{-15} \approx -5.3405762E-05$	$0xc7 = 1_10001_11 = -0b1.11 \times 2^1 = -3.5$
$0x08 = 0.00010.00 = +0b1.00 \times 2^{-14} \approx 6.1035156E-05$	$0x48 = 0.10010.00 = +0b1.00 \times 2^2 = 4.0$	$0x88 = 1_00010_00 = -0b1.00 \times 2^-14 \approx -6.1035156E-05$	$0xc8 = 1_10010_00 = -0b1.00 \times 2^2 = -4.0$
$0x09 = 0.00010_01 = +0b1.01 \times 2^-14 \approx 7.6293945E-05$	$0x49 = 0.10010.01 = +0b1.01 \times 2^2 = 5.0$	$0x89 = 1_00010_01 = -0b1.01 \times 2^-14 \approx -7.6293945E-05$	$0xc9 = 1_10010_01 = -0b1.01 \times 2^2 = -5.0$
$0x0a = 0.00010.10 = +0b1.10 \times 2^-14 \approx 9.1552734E-05$	$0x4a = 0.10010.10 = +0b1.10 \times 2^2 = 6.0$	$0x8a = 1.00010.10 = -0b1.10 \times 2^-14 \approx -9.1552734E-05$	$0xca = 1.10010.10 = -0b1.10 \times 2^2 = -6.0$
$0x0b = 0.00010.11 = +0b1.11 \times 2^{-14} \approx 0.00010681152$	$0x4b = 0.10010.11 = +0b1.11 \times 2^2 = 7.0$	$0x8b = 1.00010.11 = -0b1.11 \times 2^{-14} \approx -0.00010681152$	$0xcb = 1.10010.11 = -0b1.11 \times 2^2 = -7.0$
$0x0c = 0.00011.00 = +0b1.00 \times 2^{-13} \approx 0.00012207031$	$0x4c = 0_10011_00 = +0b1.00 \times 2^3 = 8.0$	$0x8c = 1_00011_00 = -0b1.00 \times 2^-13 \approx -0.00012207031$	$0xcc = 1.10011.00 = -0b1.00 \times 2^3 = -8.0$
$0x0d = 0.00011.01 = +0b1.01 \times 2^{-13} \approx 0.00015258789$	$0x4d = 0.10011_01 = +0b1.01 \times 2^3 = 10.0$	$0x8d = 1.00011.01 = -0b1.01 \times 2^{-13} \approx -0.00015258789$	$0xcd = 1.10011.01 = -0b1.01 \times 2^3 = -10.0$
·			
$0x0e = 0.00011.10 = +0b1.10 \times 2^{-13} \approx 0.00018310547$	$0x4e = 0.10011.10 = +0b1.10 \times 2^3 = 12.0$	$0x8e = 1.00011.10 = -0b1.10 \times 2^-13 \approx -0.00018310547$	$0xce = 1.10011.10 = -0b1.10 \times 2^3 = -12.0$
$0x0f = 0.00011.11 = +0b1.11 \times 2^{-13} \approx 0.00021362305$	$0x4f = 0.10011.11 = +0b1.11 \times 2^3 = 14.0$	$0x8f = 1.00011.11 = -0b1.11 \times 2^{-13} \approx -0.00021362305$	$0xcf = 1.10011.11 = -0b1.11 \times 2^3 = -14.0$
$0x10 = 0.00100.00 = +0b1.00 \times 2^{-12} = 0.000244140625$	$0x50 = 0_10100_00 = +0b1.00 \times 2^4 = 16.0$	$0x90 = 1.00100.00 = -0b1.00 \times 2^{-12} \approx -0.00024414062$	$0xd0 = 1_10100_00 = -0b1.00 \times 2^4 = -16.0$
$0x11 = 0.00100_01 = +0b1.01 \times 2^-12 \approx 0.00030517578$	$0x51 = 0_10100_01 = +0b1.01 \times 2^4 = 20.0$	$0x91 = 1_00100_01 = -0b1.01 \times 2^-12 \approx -0.00030517578$	$0xd1 = 1_10100_01 = -0b1.01 \times 2^4 = -20.0$
$0x12 = 0.00100.10 = +0b1.10 \times 2^{-12} \approx 0.00036621094$	$0x52 = 0.10100.10 = +0b1.10 \times 2^4 = 24.0$	$0x92 = 1.00100.10 = -0b1.10 \times 2^{-12} \approx -0.00036621094$	$0xd2 = 1.10100.10 = -0b1.10 \times 2^4 = -24.0$
$0x13 = 0.00100.11 = +0b1.11 \times 2^{-12} \approx 0.00042724609$	$0x53 = 0.10100.11 = +0b1.11 \times 2^4 = 28.0$	$0x93 = 1.00100.11 = -0b1.11 \times 2^{-12} \approx -0.00042724609$	$0xd3 = 1.10100.11 = -0b1.11 \times 2^4 = -28.0$
$0x14 = 0.00101.00 = +0b1.00 \times 2^{-11} = 0.00048828125$	$0x54 = 0.10101_00 = +0b1.00 \times 2^5 = 32.0$	$0x94 = 1.00101.00 = -0b1.00 \times 2^{-11} = -0.00048828125$	$0xd4 = 1.10101.00 = -0b1.00 \times 2^5 = -32.0$
$0x15 = 0.00101.01 = +0b1.01 \times 2^{-11} \approx 0.00061035156$	$0x55 = 0_10101_01 = +0b1.01 \times 2^5 = 40.0$	$0x95 = 1_00101_01 = -0b1.01 \times 2^-11 \approx -0.00061035156$	$0xd5 = 1_10101_01 = -0b1.01 \times 2^5 = -40.0$
$0x16 = 0.00101.10 = +0b1.10 \times 2^{-11} = 0.000732421875$	$0x56 = 0.10101.10 = +0b1.10 \times 2^5 = 48.0$	$0x96 = 1.00101.10 = -0b1.10 \times 2^{-11} \approx -0.00073242188$	$0xd6 = 1.10101.10 = -0b1.10 \times 2^5 = -48.0$
$0x17 = 0.00101.11 = +0b1.11 \times 2^{-11} \approx 0.00085449219$	$0x57 = 0.10101.11 = +0b1.11 \times 2^5 = 56.0$	$0x97 = 1.00101.11 = -0b1.11 \times 2^{-1}1 \approx -0.00085449219$	$0xd7 = 1.10101.11 = -0b1.11 \times 2^5 = -56.0$
$0x18 = 0.00110.00 = +0b1.00 \times 2^{-10} = 0.0009765625$	$0x58 = 0_10110_00 = +0b1.00 \times 2^6 = 64.0$	$0x98 = 1_00110_00 = -0b1.00 \times 2^-10 = -0.0009765625$	$0xd8 = 1.10110.00 = -0b1.00 \times 2^6 = -64.0$
$0x19 = 0_00110_01 = +0b1.01 \times 2^-10 = 0.001220703125$	$0x59 = 0_10110_01 = +0b1.01 \times 2^6 = 80.0$	$0x99 = 1_00110_01 = -0b1.01 \times 2^-10 \approx -0.0012207031$	$0xd9 = 1_10110_01 = -0b1.01 \times 2^6 = -80.0$
$0x1a = 0.00110.10 = +0b1.10 \times 2^{-10} = 0.00146484375$	$0x5a = 0.10110.10 = +0b1.10 \times 2^6 = 96.0$	$0x9a = 1.00110.10 = -0b1.10 \times 2^{-10} = -0.00146484375$	$0xda = 1.10110.10 = -0b1.10 \times 2^{6} = -96.0$
$0x1b = 0.00110.11 = +0b1.11 \times 2^{-1}0 = 0.001708984375$	$0x5b = 0.10110_11 = +0b1.11 \times 2^6 = 112.0$	$0x9b = 1.00110.11 = -0b1.11 \times 2^{-1}0 \approx -0.0017089844$	$0xdb = 1.10110.11 = -0b1.11 \times 2^6 = -112.0$
$0x1c = 0.00111.00 = +0b1.00 \times 2^{-9} = 0.001953125$	$0x5c = 0_10111_00 = +0b1.00 \times 27 = 128.0$	$0x9c = 1_00111_00 = -0b1.00 \times 2^-9 = -0.001953125$	$0xdc = 1_10111_00 = -0b1.00 \times 27 = -128.0$
$0x1d = 0_00111_01 = +0b1.01 \times 2^-9 = 0.00244140625$	$0x5d = 0_10111_01 = +0b1.01 \times 2^7 = 160.0$	$0x9d = 1_00111_01 = -0b1.01 \times 2^-9 = -0.00244140625$	$0xdd = 1_10111_01 = -0b1.01 \times 27 = -160.0$
$0x1e = 0.00111.10 = +0b1.10 \times 2^{-9} = 0.0029296875$	$0x5e = 0.10111.10 = +0b1.10 \times 27 = 192.0$	$0x9e = 1.00111.10 = -0b1.10 \times 2^{-9} = -0.0029296875$	$0xde = 1_10111_10 = -0b1.10 \times 27 = -192.0$
$0x1f = 0.00111.11 = +0b1.11 \times 2^-9 = 0.00341796875$	$0x5f = 0.10111.11 = +0b1.11 \times 27 = 224.0$	$0x9f = 1.00111.11 = -0b1.11 \times 2^{-9} = -0.00341796875$	$0xdf = 1.10111.11 = -0b1.11 \times 27 = -224.0$
$0x20 = 0_01000_00 = +0b1.00 \times 2^-8 = 0.00390625$	$0x60 = 0_11000_00 = +0b1.00 \times 2^8 = 256.0$	$0xa0 = 1_01000_00 = -0b1.00 \times 2^-8 = -0.00390625$	$0xe0 = 1_11000_00 = -0b1.00 \times 2^8 = -256.0$
$0x21 = 0.01000.01 = +0b1.01 \times 2^{-8} = 0.0048828125$	$0x61 = 0_11000_01 = +0b1.01 \times 2^8 = 320.0$	$0xa1 = 1_01000_01 = -0b1.01 \times 2^-8 = -0.0048828125$	$0xe1 = 1_11000_01 = -0b1.01 \times 2^8 = -320.0$
$0x22 = 0.01000.10 = +0b1.10 \times 2^{-8} = 0.005859375$	$0x62 = 0.11000.10 = +0b1.10 \times 2^8 = 384.0$	$0xa2 = 1.01000.10 = -0b1.10 \times 2^{-8} = -0.005859375$	$0xe2 = 1.11000.10 = -0b1.10 \times 2^8 = -384.0$
$0x23 = 0.01000_11 = +0b1.11 \times 2^-8 = 0.0068359375$	$0x63 = 0_11000_11 = +0b1.11 \times 2^8 = 448.0$	$0xa3 = 1.01000_11 = -0b1.11 \times 2^-8 = -0.0068359375$	$0 \text{xe3} = 1.11000.11 = -0 \text{b} 1.11 \times 2 \text{\%} = -448.0$
$0x24 = 0_01001_00 = +0b1.00 \times 2^-7 = 0.0078125$	$0x64 = 0_11001_00 = +0b1.00 \times 2^9 = 512.0$	$0xa4 = 1_01001_00 = -0b1.00 \times 2^-7 = -0.0078125$	$0xe4 = 1_11001_00 = -0b1.00 \times 2^9 = -512.0$
$0x25 = 0_01001_01 = +0b1.01 \times 2^-7 = 0.009765625$	$0x65 = 0_11001_01 = +0b1.01 \times 2^9 = 640.0$	$0xa5 = 1_01001_01 = -0b1.01 \times 2^-7 = -0.009765625$	$0xe5 = 1_11001_01 = -0b1.01 \times 2^9 = -640.0$
$0x26 = 0.01001.10 = +0b1.10 \times 2^{-7} = 0.01171875$	$0x66 = 0.11001.10 = +0b1.10 \times 2^9 = 768.0$	$0xa6 = 1.01001.10 = -0b1.10 \times 2^{-7} = -0.01171875$	$0xe6 = 1.11001.10 = -0b1.10 \times 2^9 = -768.0$
$0x27 = 0.01001.11 = +0b1.11 \times 2^{-7} = 0.013671875$	$0x67 = 0_11001_11 = +0b1.11 \times 2^9 = 896.0$	$0xa7 = 1_01001_11 = -0b1.11 \times 2^-7 = -0.013671875$	$0xe7 = 1_11001_11 = -0b1.11 \times 2^9 = -896.0$
$0x28 = 0.01010.00 = +0b1.00 \times 2^{-6} = 0.015625$	$0x68 = 0_11010_00 = +0b1.00 \times 2^10 = 1024.0$	$0xa8 = 1_01010_00 = -0b1.00 \times 2^-6 = -0.015625$	$0xe8 = 1_11010_00 = -0b1.00 \times 2^10 = -1024.0$
$0x29 = 0.01010.01 = +0b1.01 \times 2^{-6} = 0.01953125$	$0x69 = 0_11010_01 = +0b1.01 \times 2^10 = 1280.0$	$0xa9 = 1_01010_01 = -0b1.01 \times 2^-6 = -0.01953125$	$0xe9 = 1_11010_01 = -0b1.01 \times 2^10 = -1280.0$
$0x2a = 0.01010.10 = +0b1.10 \times 2^{-6} = 0.0234375$	$0x6a = 0.11010.10 = +0b1.10 \times 2^10 = 1536.0$	0 xaa = 1_01010_10 = -0 b1.10 \times 2 $^-6$ = -0.0234375	$0xea = 1.11010.10 = -0b1.10 \times 2^{10} = -1536.0$
$0x2b = 0_01010_11 = +0b1.11 \times 2^-6 = 0.02734375$	$0x6b = 0_11010_11 = +0b1.11 \times 2^10 = 1792.0$	$0xab = 1_01010_11 = -0b1.11 \times 2^-6 = -0.02734375$	$0xeb = 1.11010.11 = -0b1.11 \times 2^10 = -1792.0$
$0x2c = 0.01011.00 = +0b1.00 \times 2^{-5} = 0.03125$	$0x6c = 0_11011_00 = +0b1.00 \times 2^11 = 2048.0$	$0xac = 1_01011_00 = -0b1.00 \times 2^5 = -0.03125$	$0 \text{xec} = 1_11011_00 = -0b1.00 \times 2^11 = -2048.0$
$0x2d = 0_01011_01 = +0b1.01 \times 2^-5 = 0.0390625$	$0x6d = 0_11011_01 = +0b1.01 \times 2^11 = 2560.0$	$0xad = 1_01011_01 = -0b1.01 \times 2^-5 = -0.0390625$	$0xed = 1_11011_01 = -0b1.01 \times 2^11 = -2560.0$
$0x2e = 0.01011.10 = +0b1.10 \times 2^-5 = 0.046875$	$0x6e = 0.11011.10 = +0b1.10 \times 2^11 = 3072.0$	$0xae = 1.01011.10 = -0b1.10 \times 2^{-5} = -0.046875$	$0 \text{xee} = 1.11011.10 = -0b1.10 \times 2^11 = -3072.0$
$0x2f = 0_01011_11 = +0b1.11 \times 2^{-5} = 0.0546875$	$0x6f = 0_11011_11 = +0b1.11 \times 2^11 = 3584.0$	$0xaf = 1.01011.11 = -0b1.11 \times 2^{-5} = -0.0546875$	$0xef = 1.11011.11 = -0b1.11 \times 2^11 = -3584.0$
$0x30 = 0.01100.00 = +0b1.00 \times 2^{-4} = 0.0625$	$0x70 = 0_11100_00 = +0b1.00 \times 2^12 = 4096.0$	$0xb0 = 1_01100_00 = -0b1.00 \times 2^4 = -0.0625$	$0xf0 = 1_11100_00 = -0b1.00 \times 2^12 = -4096.0$
$0x31 = 0.01100.01 = +0b1.01 \times 2^{-4} = 0.078125$	$0x71 = 0_11100_01 = +0b1.01 \times 2^12 = 5120.0$	$0xb1 = 1_01100_01 = -0b1.01 \times 2^-4 = -0.078125$	$0xf1 = 1_11100_01 = -0b1.01 \times 2^12 = -5120.0$
$0x32 = 0.01100.10 = +0b1.10 \times 2^-4 = 0.09375$	$0x72 = 0.11100.10 = +0b1.10 \times 2^12 = 6144.0$	$0xb2 = 1_01100_10 = -0b1.10 \times 2^-4 = -0.09375$	$0xf2 = 1.11100.10 = -0b1.10 \times 2^12 = -6144.0$
$0x33 = 0.01100.11 = +0b1.11 \times 2^{-4} = 0.109375$	$0x73 = 0_11100_11 = +0b1.11 \times 2^12 = 7168.0$	$0xb3 = 1_01100_11 = -0b1.11 \times 2^4 = -0.109375$	$0xf3 = 1_11100_11 = -0b1.11 \times 2^12 = -7168.0$
$0x34 = 0.01101.00 = +0b1.00 \times 2^{-3} = 0.125$	$0x74 = 0.11101.00 = +0b1.00 \times 2^13 = 8192.0$	$0xb4 = 1_01101_00 = -0b1.00 \times 2^{-3} = -0.125$	$0xf4 = 1_11101_00 = -0b1.00 \times 2^13 = -8192.0$
$0x35 = 0.01101.01 = +0b1.01 \times 2^{-3} = 0.15625$	$0x75 = 0_11101_01 = +0b1.01 \times 2^13 = 10240.0$	$0xb5 = 1_01101_01 = -0b1.01 \times 2^-3 = -0.15625$	$0xf5 = 1_11101_01 = -0b1.01 \times 2^13 = -10240.0$
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$0x36 = 0.01101.10 = +0b1.10 \times 2^{-3} = 0.1875$	$0x76 = 0_11101_10 = +0b1.10 \times 2^13 = 12288.0$	$0xb6 = 1.01101.10 = -0b1.10 \times 2^{-3} = -0.1875$	$0xf6 = 1.11101.10 = -0b1.10 \times 2^13 = -12288.0$
$0x37 = 0.01101.11 = +0b1.11 \times 2^{-3} = 0.21875$	$0x77 = 0.11101.11 = +0b1.11 \times 2^13 = 14336.0$	$0xb7 = 1_01101_11 = -0b1.11 \times 2^-3 = -0.21875$	$0xf7 = 1_11101_11 = -0b1.11 \times 2^13 = -14336.0$
$0x38 = 0.01110.00 = +0b1.00 \times 2^{-2} = 0.25$	$0x78 = 0.11110.00 = +0b1.00 \times 2^14 = 16384.0$	$0xb8 = 1_01110_00 = -0b1.00 \times 2^2 = -0.25$	$0xf8 = 1_11110_00 = -0b1.00 \times 2^14 = -16384.0$
$0x39 = 0.01110.01 = +0b1.01 \times 2^{-2} = 0.3125$	$0x79 = 0.11110_01 = +0b1.01 \times 2^14 = 20480.0$	$0xb9 = 1_01110_01 = -0b1.01 \times 2^2 = -0.3125$	$0xf9 = 1_11110_01 = -0b1.01 \times 2^14 = -20480.0$
$0x3a = 0.01110.10 = +0b1.10 \times 2^{-2} = 0.375$	$0x7a = 0.11110.10 = +0b1.10 \times 2^14 = 24576.0$	$0xba = 1_01110_10 = -0b1.10 \times 2^2 = -0.375$	$0xfa = 1_11110_10 = -0b1.10 \times 2^14 = -24576.0$
$0x3b = 0_01110_11 = +0b1.11 \times 2^2 - 2 = 0.4375$	$0x7b = 0_11110_11 = +0b1.11 \times 2^14 = 28672.0$	$0xbb = 1_01110_11 = -0b1.11 \times 2^2 = -0.4375$	$0xfb = 1.11110.11 = -0b1.11 \times 2^14 = -28672.0$
$0x3c = 0.01111.00 = +0b1.00 \times 2^{-1} = 0.5$	$0x7c = 0_11111_00 = +0b1.00 \times 2^15 = 32768.0$	$0xbc = 1_01111_00 = -0b1.00 \times 2^-1 = -0.5$	$0xfc = 1_11111_00 = -0b1.00 \times 2^15 = -32768.0$
$0x3d = 0.01111.00 = +0b1.00 \times 2^{-1} = 0.5$ $0x3d = 0.01111.01 = +0b1.01 \times 2^{-1} = 0.625$			551.00 × 2 10 = 52700.0
$0.000 - 0.01111.01 - +001.01 \times 2 - 1 = 0.020$		$0 \times 64 - 1011110106101 \times 2211 - 0625$	$0 = 64 - 1 = 11111 = 01 - 051 = 01 \times 02 = -40000 = 0$
0.0	$0x7d = 0_11111_01 = +0b1.01 \times 2^15 = 40960.0$	$0xbd = 1_01111_01 = -0b1.01 \times 2^-1 = -0.625$	$0xfd = 1_11111_01 = -0b1.01 \times 2^{\circ}15 = -40960.0$
$0x3e = 0.01111.10 = +0b1.10 \times 2^-1 = 0.75$	$0x7d = 0.11111.01 = +0b1.01 \times 2^15 = 40960.0$ $0x7e = 0.11111.10 = +0b1.10 \times 2^15 = 49152.0$	$0xbe = 1.01111.10 = -0b1.10 \times 2^-1 = -0.75$	$0xfe = 1.11111.10 = -0b1.10 \times 2^15 = -49152.0$
$0x3e = 0.01111.10 = +0b1.10 \times 2^{-1} = 0.75$ $0x3f = 0.01111.11 = +0b1.11 \times 2^{-1} = 0.875$	$0x7d = 0_11111_01 = +0b1.01 \times 2^15 = 40960.0$		

C.4 Value Table: P4, emin = -7, emax = 7

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0x00 = 0.0000_000 = 0.0
                                                             0x40 = 0_1000_000 = +0b1.000 \times 2^{\circ} = 1.0
                                                                                                                 0x80 = 1.0000.000 = NaN
                                                                                                                                                                                0xc0 = 1.1000.000 = -0b1.000 \times 2^{\circ}0 = -1.0
0x01 = 0.0000_001 = +0b0.001 \times 2^-7 = 0.0009765625
                                                             0x41 = 0_1000_001 = +0b1.001 \times 2^{\circ} = 1.125
                                                                                                                 0x81 = 1_0000_001 = -0b0.001 \times 2^-7 = -0.0009765625
                                                                                                                                                                               0xc1 = 1_1000_001 = -0b1.001 \times 20 = -1.125
0x02 = 0.0000.010 = +0b0.010 \times 2^{-7} = 0.001953125
                                                             0x42 = 0.1000.010 = +0b1.010 \times 2^{\circ} = 1.25
                                                                                                                 0x82 = 1.0000.010 = -0b0.010 \times 2^{-7} = -0.001953125
                                                                                                                                                                                0xc2 = 1.1000.010 = -0b1.010 \times 2^{\circ} = -1.25
0x03 = 0.0000_011 = +0b0.011 \times 2^-7 = 0.0029296875
                                                             0x43 = 0.1000.011 = +0b1.011 \times 2^{\circ} = 1.375
                                                                                                                 0x83 = 1.0000_011 = -0b0.011 \times 2^-7 = -0.0029296875
                                                                                                                                                                               0xc3 = 1_{-}1000_{-}011 = -0b1.011 \times 2^{\circ} = -1.375
0x04 = 0.0000.100 = +0b0.100 \times 2^{-7} = 0.00390625
                                                             0x44 = 0_1000_100 = +0b1.100 \times 2^{\circ} = 1.5
                                                                                                                 0x84 = 1_0000_100 = -0b0.100 \times 2^{-7} = -0.00390625
                                                                                                                                                                                0xc4 = 1.1000.100 = -0b1.100 \times 2^{\circ} = -1.5
0x05 = 0.0000_101 = +0b0.101 \times 2^{-7} = 0.0048828125
                                                             0x45 = 0.1000.101 = +0b1.101 \times 2^{\circ} = 1.625
                                                                                                                 0x85 = 1.0000_101 = -0b0.101 \times 2^{-7} = -0.0048828125
                                                                                                                                                                               0xc5 = 1_{-}1000_{-}101 = -0b1.101 \times 2^{\circ} = -1.625
0x06 = 0.0000_{-}110 = +0b0.110 \times 2^{-}7 = 0.005859375
                                                             0x46 = 0.1000.110 = +0b1.110 \times 2^{\circ} = 1.75
                                                                                                                 0x86 = 1.0000.110 = -0b0.110 \times 2^{-7} = -0.005859375
                                                                                                                                                                                0xc6 = 1_{-}1000_{-}110 = -0b1.110 \times 2^{\circ}0 = -1.75
0x07 = 0.0000_{-}111 = +0b0.111 \times 2^{-}7 = 0.0068359375
                                                             0x47 = 0.1000.111 = +0b1.111 \times 20 = 1.875
                                                                                                                 0x87 = 1.0000.111 = -0b0.111 \times 2^{-7} = -0.0068359375
                                                                                                                                                                               0xc7 = 1.1000.111 = -0b1.111 \times 2^{\circ} = -1.875
0x08 = 0.0001.000 = +0b1.000 \times 2^{-7} = 0.0078125
                                                                                                                 0x88 = 1.0001.000 = -0b1.000 \times 2^-7 = -0.0078125
                                                                                                                                                                                0xc8 = 1_1001_000 = -0b1.000 \times 2^1 = -2.0
                                                             0x48 = 0_1001_000 = +0b1.000 \times 2^1 = 2.0
                                                             0x49 = 0_1001_001 = +0b1.001 \times 2^1 = 2.25
0x09 = 0.0001.001 = +0b1.001 \times 2^{-7} = 0.0087890625
                                                                                                                 0x89 = 1_0001_001 = -0b1.001 \times 2^-7 = -0.0087890625
                                                                                                                                                                               0xc9 = 1_1001_001 = -0b1.001 \times 2^1 = -2.25
0x0a = 0.0001.010 = +0b1.010 \times 2^{-7} = 0.009765625
                                                             0x4a = 0.1001.010 = +0b1.010 \times 2^1 = 2.5
                                                                                                                 0x8a = 1.0001.010 = -0b1.010 \times 2^{-7} = -0.009765625
                                                                                                                                                                                0xca = 1.1001.010 = -0b1.010 \times 2^1 = -2.5
0x0b = 0.0001.011 = +0b1.011 \times 2^{-7} = 0.0107421875
                                                             0x4b = 0_1001_011 = +0b1.011 \times 2^1 = 2.75
                                                                                                                 0x8b = 1.0001.011 = -0b1.011 \times 2^{-7} = -0.0107421875
                                                                                                                                                                               0xcb = 1_1001_011 = -0b1.011 \times 2^1 = -2.75
0x0c = 0.0001.100 = +0b1.100 \times 2^{-7} = 0.01171875
                                                             0x4c = 0_1001_100 = +0b1.100 \times 2^1 = 3.0
                                                                                                                 0x8c = 1.0001.100 = -0b1.100 \times 2^{-7} = -0.01171875
                                                                                                                                                                                0xcc = 1.1001.100 = -0b1.100 \times 2^1 = -3.0
0x0d = 0.0001.101 = +0b1.101 \times 2^{-7} = 0.0126953125
                                                             0x4d = 0_1001_101 = +0b1.101 \times 2^1 = 3.25
                                                                                                                 0x8d = 1.0001.101 = -0b1.101 \times 2^{-7} = -0.0126953125
                                                                                                                                                                               0xcd = 1_1001_101 = -0b1.101 \times 2^1 = -3.25
0x0e = 0.0001.110 = +0b1.110 \times 2^{-7} = 0.013671875
                                                             0x4e = 0.1001.110 = +0b1.110 \times 2^1 = 3.5
                                                                                                                 0x8e = 1.0001.110 = -0b1.110 \times 2^{-7} = -0.013671875
                                                                                                                                                                                0xce = 1_{-}1001_{-}110 = -0b1.110 \times 2^{-}1 = -3.5
0x0f = 0.0001.111 = +0b1.111 \times 2^{-7} = 0.0146484375
                                                             0x4f = 0_1001_111 = +0b1.111 \times 2^1 = 3.75
                                                                                                                 0x8f = 1.0001.111 = -0b1.111 \times 2^{-7} = -0.0146484375
                                                                                                                                                                               0xcf = 1.1001.111 = -0b1.111 \times 2^1 = -3.75
0x10 = 0.0010.000 = +0b1.000 \times 2^{-6} = 0.015625
                                                             0x50 = 0_1010_000 = +0b1.000 \times 2^2 = 4.0
                                                                                                                 0x90 = 1.0010.000 = -0b1.000 \times 2^{-6} = -0.015625
                                                                                                                                                                                0xd0 = 1_1010_000 = -0b1.000 \times 2^2 = -4.0
0x11 = 0_0010_001 = +0b1.001 \times 2^-6 = 0.017578125
                                                             0x51 = 0.1010.001 = +0b1.001 \times 2^2 = 4.5
                                                                                                                 0x91 = 1_0010_001 = -0b1.001 \times 2^-6 = -0.017578125
                                                                                                                                                                               0xd1 = 1_1010_001 = -0b1.001 \times 2^2 = -4.5
0x12 = 0.0010.010 = +0b1.010 \times 2^{-6} = 0.01953125
                                                             0x52 = 0_{-}1010_{-}010 = +0b1.010 \times 2^{2} = 5.0
                                                                                                                 0x92 = 1.0010.010 = -0b1.010 \times 2^{-6} = -0.01953125
                                                                                                                                                                                0xd2 = 1_{-}1010_{-}010 = -0b1.010 \times 2^2 = -5.0
0x13 = 0.0010.011 = +0b1.011 \times 2^-6 = 0.021484375
                                                             0x53 = 0_1010_011 = +0b1.011 \times 2^2 = 5.5
                                                                                                                 0x93 = 1.0010.011 = -0b1.011 \times 2^{-6} = -0.021484375
                                                                                                                                                                                0xd3 = 1.1010.011 = -0b1.011 \times 2^2 = -5.5
0x14 = 0.0010.100 = +0b1.100 \times 2^{-6} = 0.0234375
                                                             0x54 = 0.1010.100 = +0b1.100 \times 2^2 = 6.0
                                                                                                                 0x94 = 1.0010.100 = -0b1.100 \times 2^{-6} = -0.0234375
                                                                                                                                                                                0xd4 = 1_1010_100 = -0b1.100 \times 2^2 = -6.0
0x15 = 0.0010.101 = +0b1.101 \times 2^-6 = 0.025390625
                                                             0x55 = 0_1010_101 = +0b1.101 \times 2^2 = 6.5
                                                                                                                 0x95 = 1.0010.101 = -0b1.101 \times 2^{-6} = -0.025390625
                                                                                                                                                                               0xd5 = 1_1010_101 = -0b1.101 \times 2^2 = -6.5
0x16 = 0.0010.110 = +0b1.110 \times 2^{-6} = 0.02734375
                                                             0x56 = 0.1010.110 = +0b1.110 \times 2^2 = 7.0
                                                                                                                 0x96 = 1.0010.110 = -0b1.110 \times 2^{-6} = -0.02734375
                                                                                                                                                                                0xd6 = 1.1010.110 = -0b1.110 \times 2^2 = -7.0
0x17 = 0.0010.111 = +0b1.111 \times 2^{-6} = 0.029296875
                                                             0x57 = 0_1010_111 = +0b1.111 \times 2^2 = 7.5
                                                                                                                 0x97 = 1.0010.111 = -0b1.111 \times 2^{-6} = -0.029296875
                                                                                                                                                                                0xd7 = 1.1010.111 = -0b1.111 \times 2^2 = -7.5
0x18 = 0.0011.000 = +0b1.000 \times 2^{-5} = 0.03125
                                                             0x58 = 0_1011_000 = +0b1.000 \times 2^3 = 8.0
                                                                                                                 0x98 = 1.0011.000 = -0b1.000 \times 2^{-5} = -0.03125
                                                                                                                                                                                0xd8 = 1_1011_000 = -0b1.000 \times 2^3 = -8.0
0x19 = 0_0011_001 = +0b1.001 \times 2^5 = 0.03515625
                                                             0x59 = 0_1011_001 = +0b1.001 \times 2^3 = 9.0
                                                                                                                 0x99 = 1_0011_001 = -0b1.001 \times 2^{-5} = -0.03515625
                                                                                                                                                                                0xd9 = 1_1011_001 = -0b1.001 \times 2^3 = -9.0
0x1a = 0.0011.010 = +0b1.010 \times 2^{-5} = 0.0390625
                                                             0x5a = 0.1011.010 = +0b1.010 \times 2^3 = 10.0
                                                                                                                 0x9a = 1.0011.010 = -0b1.010 \times 2^{-5} = -0.0390625
                                                                                                                                                                                0xda = 1.1011.010 = -0b1.010 \times 2^3 = -10.0
0x1b = 0.0011.011 = +0b1.011 \times 2^{-5} = 0.04296875
                                                             0x5b = 0.1011.011 = +0b1.011 \times 2^3 = 11.0
                                                                                                                 0x9b = 1.0011.011 = -0b1.011 \times 2^{-5} = -0.04296875
                                                                                                                                                                               0xdb = 1.1011.011 = -0b1.011 \times 2^3 = -11.0
0x1c = 0.0011.100 = +0b1.100 \times 2^{-5} = 0.046875
                                                             0x5c = 0_1011_100 = +0b1.100 \times 2^3 = 12.0
                                                                                                                 0x9c = 1_0011_100 = -0b1.100 \times 2^5 = -0.046875
                                                                                                                                                                                0xdc = 1_1011_100 = -0b1.100 \times 2^3 = -12.0
0 \texttt{x1d} = 0\_0011\_101 = +0 \texttt{b1.101} \times 2 \texttt{^--5} = 0.05078125
                                                                                                                 0x9d = 1_0011_101 = -0b1.101 \times 2^5 = -0.05078125
                                                                                                                                                                                0xdd = 1_1011_101 = -0b1.101 \times 2^3 = -13.0
                                                             0x5d = 0_1011_101 = +0b1.101 \times 2^3 = 13.0
0x1e = 0.0011.110 = +0b1.110 \times 2^{-5} = 0.0546875
                                                             0x5e = 0.1011.110 = +0b1.110 \times 2^3 = 14.0
                                                                                                                 0x9e = 1.0011.110 = -0b1.110 \times 2^{-5} = -0.0546875
                                                                                                                                                                                0xde = 1_{-}1011_{-}110 = -0b1.110 \times 2^{3} = -14.0
                                                                                                                 0x9f = 1.0011.111 = -0b1.111 \times 2^{-5} = -0.05859375
                                                                                                                                                                                0xdf = 1_1011_111 = -0b1.111 \times 2^3 = -15.0
0x1f = 0.0011.111 = +0b1.111 \times 2^{-5} = 0.05859375
                                                             0x5f = 0.1011.111 = +0b1.111 \times 2^3 = 15.0
0x20 = 0.0100.000 = +0b1.000 \times 2^{-4} = 0.0625
                                                             0x60 = 0_1100_000 = +0b1.000 \times 2^4 = 16.0
                                                                                                                 0xa0 = 1.0100.000 = -0b1.000 \times 2^{-4} = -0.0625
                                                                                                                                                                                0xe0 = 1_1100_000 = -0b1.000 \times 2^4 = -16.0
0x21 = 0_0100_001 = +0b1.001 \times 2^-4 = 0.0703125
                                                             0x61 = 0_1100_001 = +0b1.001 \times 2^4 = 18.0
                                                                                                                 0xa1 = 1_0100_001 = -0b1.001 \times 2^-4 = -0.0703125
                                                                                                                                                                                0xe1 = 1_1100_001 = -0b1.001 \times 2^4 = -18.0
0x22 = 0.0100.010 = +0b1.010 \times 2^{-4} = 0.078125
                                                             0x62 = 0.1100.010 = +0b1.010 \times 2^4 = 20.0
                                                                                                                 0xa2 = 1.0100.010 = -0b1.010 \times 2^{-4} = -0.078125
                                                                                                                                                                                0xe2 = 1_1100_010 = -0b1.010 \times 2^4 = -20.0
0x23 = 0.0100.011 = +0b1.011 \times 2^{-4} = 0.0859375
                                                             0x63 = 0_1100_011 = +0b1.011 \times 2^4 = 22.0
                                                                                                                 0xa3 = 1.0100.011 = -0b1.011 \times 2^{-4} = -0.0859375
                                                                                                                                                                                0xe3 = 1.1100.011 = -0b1.011 \times 2^4 = -22.0
0x24 = 0.0100.100 = +0b1.100 \times 2^{-4} = 0.09375
                                                             0x64 = 0_1100_100 = +0b1.100 \times 2^4 = 24.0
                                                                                                                 0xa4 = 1_0100_100 = -0b1.100 \times 2^-4 = -0.09375
                                                                                                                                                                                0xe4 = 1_1100_100 = -0b1.100 \times 2^4 = -24.0
                                                                                                                 0xa5 = 1_0100_101 = -0b1.101 \times 2^-4 = -0.1015625
                                                                                                                                                                                0xe5 = 1_1100_101 = -0b1.101 \times 2^4 = -26.0
0x25 = 0.0100.101 = +0b1.101 \times 2^{-4} = 0.1015625
                                                             0x65 = 0_1100_101 = +0b1.101 \times 2^4 = 26.0
0x26 = 0.0100.110 = +0b1.110 \times 2^{-4} = 0.109375
                                                             0x66 = 0.1100.110 = +0b1.110 \times 2^4 = 28.0
                                                                                                                 0xa6 = 1.0100.110 = -0b1.110 \times 2^{-4} = -0.109375
                                                                                                                                                                                0xe6 = 1_1100_110 = -0b1.110 \times 2^4 = -28.0
                                                                                                                 0xa7 = 1.0100.111 = -0b1.111 \times 2^{-4} = -0.1171875
0x27 = 0.0100.111 = +0b1.111 \times 2^-4 = 0.1171875
                                                                                                                                                                                0xe7 = 1_1100_111 = -0b1.111 \times 2^4 = -30.0
                                                             0x67 = 0_1100_111 = +0b1.111 \times 2^4 = 30.0
0x28 = 0_0101_000 = +0b1.000 \times 2^{-3} = 0.125
                                                                                                                 0xa8 = 1.0101.000 = -0b1.000 \times 2^{-3} = -0.125
                                                                                                                                                                                0xe8 = 1_1101_000 = -0b1.000 \times 2^5 = -32.0
                                                             0x68 = 0_1101_000 = +0b1.000 \times 2^5 = 32.0
                                                                                                                                                                                0 {\tt xe9} = 1\_1101\_001 = -0 {\tt b1.001} {\times} 2 {\tt \^{T}5} = -36.0
                                                                                                                 0xa9 = 1_0101_001 = -0b1.001 \times 2^{-3} = -0.140625
0x29 = 0_0101_001 = +0b1.001 \times 2^{-3} = 0.140625
                                                             0x69 = 0_1101_001 = +0b1.001 \times 2^5 = 36.0
0x2a = 0.0101.010 = +0b1.010 \times 2^{-3} = 0.15625
                                                             0x6a = 0.1101.010 = +0b1.010 \times 2^5 = 40.0
                                                                                                                 0xaa = 1.0101.010 = -0b1.010 \times 2^{-3} = -0.15625
                                                                                                                                                                                0xea = 1.1101.010 = -0b1.010 \times 2^5 = -40.0
0x2b = 0.0101.011 = +0b1.011 \times 2^{-3} = 0.171875
                                                             0x6b = 0_1101_011 = +0b1.011 \times 2^5 = 44.0
                                                                                                                 0xab = 1.0101.011 = -0b1.011 \times 2^{-3} = -0.171875
                                                                                                                                                                                0xeb = 1.1101.011 = -0b1.011 \times 2^5 = -44.0
0x2c = 0.0101.100 = +0b1.100 \times 2^{-3} = 0.1875
                                                             0x6c = 0_1101_100 = +0b1.100 \times 25 = 48.0
                                                                                                                 0xac = 1.0101.100 = -0b1.100 \times 2^{-3} = -0.1875
                                                                                                                                                                                0 \text{xec} = 1.1101.100 = -0b1.100 \times 2^5 = -48.0
0x2d = 0.0101.101 = +0b1.101 \times 2^{-3} = 0.203125
                                                             0x6d = 0_1101_101 = +0b1.101 \times 2^5 = 52.0
                                                                                                                 0xad = 1_0101_101 = -0b1.101 \times 2^{-3} = -0.203125
                                                                                                                                                                                0xed = 1_1101_101 = -0b1.101 \times 2^5 = -52.0
0x2e = 0.0101.110 = +0b1.110 \times 2^{-3} = 0.21875
                                                             0x6e = 0.1101.110 = +0b1.110 \times 2^5 = 56.0
                                                                                                                 0xae = 1.0101.110 = -0b1.110 \times 2^{-3} = -0.21875
                                                                                                                                                                               0xee = 1.1101.110 = -0b1.110 \times 2^5 = -56.0
0x2f = 0.0101.111 = +0b1.111 \times 2^{-3} = 0.234375
                                                             0x6f = 0_1101_111 = +0b1.111 \times 25 = 60.0
                                                                                                                 0xaf = 1.0101.111 = -0b1.111 \times 2^{-3} = -0.234375
                                                                                                                                                                                0xef = 1.1101.111 = -0b1.111 \times 2^5 = -60.0
0x30 = 0.0110.000 = +0b1.000 \times 2^{-2} = 0.25
                                                             0x70 = 0.1110.000 = +0b1.000 \times 2^{6} = 64.0
                                                                                                                 0xb0 = 1_0110_000 = -0b1.000 \times 2^2 = -0.25
                                                                                                                                                                               0xf0 = 1_1110_000 = -0b1.000 \times 2^6 = -64.0
0x31 = 0_0110_001 = +0b1.001 \times 2^2 = 0.28125
                                                             0x71 = 0_1110_001 = +0b1.001 \times 2\% = 72.0
                                                                                                                 0xb1 = 1_0110_001 = -0b1.001 \times 2^2 = -0.28125
                                                                                                                                                                                0xf1 = 1_1110_001 = -0b1.001 \times 26 = -72.0
0x32 = 0.0110.010 = +0b1.010 \times 2^{-2} = 0.3125
                                                             0x72 = 0_{-}1110_{-}010 = +0b1.010 \times 2\% = 80.0
                                                                                                                 0xb2 = 1_0110_010 = -0b1.010 \times 2^2 = -0.3125
                                                                                                                                                                               0xf2 = 1.1110.010 = -0b1.010 \times 2^6 = -80.0
0x33 = 0.0110.011 = +0b1.011 \times 2^{-2} = 0.34375
                                                             0x73 = 0_1110_011 = +0b1.011 \times 2^6 = 88.0
                                                                                                                 0xb3 = 1.0110.011 = -0b1.011 \times 2^{-2} = -0.34375
                                                                                                                                                                               0xf3 = 1_1110_011 = -0b1.011 \times 26 = -88.0
0x34 = 0.0110.100 = +0b1.100 \times 2^{-2} = 0.375
                                                             0x74 = 0_{1110_{100}} = +0b1.100 \times 2\% = 96.0
                                                                                                                 0xb4 = 1_0110_100 = -0b1.100 \times 2^2 = -0.375
                                                                                                                                                                                0xf4 = 1_1110_100 = -0b1.100 \times 2^6 = -96.0
0x35 = 0.0110.101 = +0b1.101 \times 2^{-2} = 0.40625
                                                             0x75 = 0.1110.101 = +0b1.101 \times 2^6 = 104.0
                                                                                                                 0xb5 = 1.0110.101 = -0b1.101 \times 2^{-2} = -0.40625
                                                                                                                                                                                0xf5 = 1_1110_101 = -0b1.101 \times 26 = -104.0
0x36 = 0.0110.110 = +0b1.110 \times 2^{-2} = 0.4375
                                                             0x76 = 0.1110.110 = +0b1.110 \times 2^6 = 112.0
                                                                                                                 0xb6 = 1.0110.110 = -0b1.110 \times 2^{-2} = -0.4375
                                                                                                                                                                                0xf6 = 1_1110_110 = -0b1.110 \times 26 = -112.0
0x37 = 0.0110.111 = +0b1.111 \times 2^{-2} = 0.46875
                                                             0x77 = 0.1110.111 = +0b1.111 \times 2^6 = 120.0
                                                                                                                 0xb7 = 1_0110_111 = -0b1.111 \times 2^2 = -0.46875
                                                                                                                                                                                0xf7 = 1_1110_111 = -0b1.111 \times 2\% = -120.0
0x38 = 0_0111_000 = +0b1.000 \times 2^-1 = 0.5
                                                             0x78 = 0_1111_000 = +0b1.000 \times 27 = 128.0
                                                                                                                 0xb8 = 1_0111_000 = -0b1.000 \times 2^-1 = -0.5
                                                                                                                                                                                0xf8 = 1_1111_000 = -0b1.000 \times 27 = -128.0
0x39 = 0.0111.001 = +0b1.001 \times 2^{-1} = 0.5625
                                                             0x79 = 0_1111_001 = +0b1.001 \times 27 = 144.0
                                                                                                                 0xb9 = 1_0111_001 = -0b1.001 \times 2^-1 = -0.5625
                                                                                                                                                                                0xf9 = 1_1111_001 = -0b1.001 \times 2^7 = -144.0
0x3a = 0.0111.010 = +0b1.010 \times 2^{-1} = 0.625
                                                             0x7a = 0.1111.010 = +0b1.010 \times 27 = 160.0
                                                                                                                 0xba = 1.0111.010 = -0b1.010 \times 2^{-1} = -0.625
                                                                                                                                                                                0xfa = 1.1111.010 = -0b1.010 \times 27 = -160.0
0x3b = 0.0111.011 = +0b1.011 \times 2^-1 = 0.6875
                                                             0x7b = 0_1111_011 = +0b1.011 \times 27 = 176.0
                                                                                                                 0xbb = 1_0111_011 = -0b1.011 \times 2^-1 = -0.6875
                                                                                                                                                                               0xfb = 1_1111_011 = -0b1.011 \times 2^7 = -176.0
0x3c = 0_0111_100 = +0b1.100 \times 2^{-1} = 0.75
                                                             0x7c = 0_1111_100 = +0b1.100 \times 27 = 192.0
                                                                                                                 0xbc = 1_0111_100 = -0b1.100 \times 2^-1 = -0.75
                                                                                                                                                                               0xfc = 1_1111_100 = -0b1.100 \times 27 = -192.0
0x3d = 0_0111_101 = +0b1.101 \times 2^{-1} = 0.8125
                                                             0x7d = 0_1111_101 = +0b1.101 \times 27 = 208.0
                                                                                                                 0xbd = 1_0111_101 = -0b1.101 \times 2^-1 = -0.8125
                                                                                                                                                                               0xfd = 1_1111_101 = -0b1.101 \times 27 = -208.0
0x3e = 0.0111.110 = +0b1.110 \times 2^-1 = 0.875
                                                             0x7e = 0.1111.110 = +0b1.110 \times 27 = 224.0
                                                                                                                 0xbe = 1.0111.110 = -0b1.110 \times 2^-1 = -0.875
                                                                                                                                                                               0xfe = 1.1111.110 = -0b1.110 \times 27 = -224.0
0x3f = 0_0111_111 = +0b1.111 \times 2^-1 = 0.9375
                                                                                                                 0xbf = 1_0111_111 = -0b1.111 \times 2^-1 = -0.9375
                                                             0x7f = 0_1111_111 = +Inf
                                                                                                                                                                               0xff = 1_1111_111 = -Inf
```

C.5 Value Table: P5, emin = -3, emax = 3

```
0x00 = 0.000_0000 = 0.0
                                                           0x40 = 0.100.0000 = +0b1.0000 \times 2^{\circ} = 1.0
                                                                                                                  0x80 = 1.000.0000 = NaN
                                                                                                                                                                               0xc0 = 1.100.0000 = -0b1.0000 \times 2^{\circ}0 = -1.0
0x01 = 0.000.0001 = +0b0.0001 \times 2^{-3} = 0.0078125
                                                           0x41 = 0.100.0001 = +0b1.0001 \times 2^{\circ} = 1.0625
                                                                                                                  0x81 = 1_000_0001 = -0b0.0001 \times 2^{-3} = -0.0078125
                                                                                                                                                                              0xc1 = 1_100_0001 = -0b1.0001 \times 2^0 = -1.0625
0x02 = 0.000.0010 = +0b0.0010 \times 2^{-3} = 0.015625
                                                           0x42 = 0.100.0010 = +0b1.0010 \times 2^{\circ} = 1.125
                                                                                                                  0x82 = 1.000.0010 = -0b0.0010 \times 2^{-3} = -0.015625
                                                                                                                                                                               0xc2 = 1.100.0010 = -0b1.0010 \times 2^{\circ}0 = -1.125
0x03 = 0.000.0011 = +0b0.0011 \times 2^{-3} = 0.0234375
                                                           0x43 = 0.100.0011 = +0b1.0011 \times 2^{\circ} = 1.1875
                                                                                                                  0x83 = 1.000.0011 = -0b0.0011 \times 2^{-3} = -0.0234375
                                                                                                                                                                              0xc3 = 1.100.0011 = -0b1.0011 \times 2^{\circ}0 = -1.1875
0x04 = 0.000.0100 = +0b0.0100 \times 2^{-3} = 0.03125
                                                           0x44 = 0.100.0100 = +0b1.0100 \times 2^{\circ} = 1.25
                                                                                                                  0x84 = 1.000.0100 = -0b0.0100 \times 2^{-3} = -0.03125
                                                                                                                                                                               0xc4 = 1.100.0100 = -0b1.0100 \times 2^{\circ} = -1.25
0x05 = 0.000.0101 = +0b0.0101 \times 2^{-3} = 0.0390625
                                                           0x45 = 0.100.0101 = +0b1.0101 \times 2^{\circ} = 1.3125
                                                                                                                  0x85 = 1_000_0101 = -0b0.0101 \times 2^{-3} = -0.0390625
                                                                                                                                                                              0xc5 = 1_{-}100_{-}0101 = -0b1.0101 \times 2^{\circ}0 = -1.3125
0x06 = 0.000.0110 = +0b0.0110 \times 2^{-3} = 0.046875
                                                           0x46 = 0.100.0110 = +0b1.0110 \times 2^{\circ} = 1.375
                                                                                                                  0x86 = 1.000.0110 = -0b0.0110 \times 2^{-3} = -0.046875
                                                                                                                                                                               0xc6 = 1.100.0110 = -0b1.0110 \times 2^{\circ} = -1.375
0x07 = 0.000.0111 = +0b0.0111 \times 2^{-3} = 0.0546875
                                                           0x47 = 0.100.0111 = +0b1.0111 \times 2^{\circ} = 1.4375
                                                                                                                  0x87 = 1.000.0111 = -0b0.0111 \times 2^{-3} = -0.0546875
                                                                                                                                                                              0xc7 = 1.100_{-}0111 = -0b1.0111 \times 2^{\circ} = -1.4375
0x08 = 0.000.1000 = +0b0.1000 \times 2^{-3} = 0.0625
                                                                                                                  0x88 = 1.000.1000 = -0b0.1000 \times 2^{-3} = -0.0625
                                                                                                                                                                               0xc8 = 1.100.1000 = -0b1.1000 \times 2^{\circ} = -1.5
                                                           0x48 = 0.100.1000 = +0b1.1000 \times 2^{\circ} = 1.5
0x09 = 0.000_1001 = +0b0.1001 \times 2^{-3} = 0.0703125
                                                           0x49 = 0.100.1001 = +0b1.1001 \times 2^{\circ} = 1.5625
                                                                                                                  0x89 = 1_000_1001 = -0b0.1001 \times 2^{-3} = -0.0703125
                                                                                                                                                                              0xc9 = 1_100_1001 = -0b1.1001 \times 2^{\circ} = -1.5625
0x0a = 0.000_1010 = +0b0.1010 \times 2^{-3} = 0.078125
                                                           0x4a = 0.100.1010 = +0b1.1010 \times 2^{\circ} = 1.625
                                                                                                                  0x8a = 1.000.1010 = -0b0.1010 \times 2^{-3} = -0.078125
                                                                                                                                                                               0xca = 1.100.1010 = -0b1.1010 \times 2^{\circ}0 = -1.625
0x0b = 0.000 \cdot 1011 = +0b0 \cdot 1011 \times 2^{-3} = 0.0859375
                                                           0x4b = 0.100.1011 = +0b1.1011 \times 2^{\circ} = 1.6875
                                                                                                                  0x8b = 1.000 \cdot 1011 = -0b0 \cdot 1011 \times 2^{-3} = -0.0859375
                                                                                                                                                                               0xcb = 1.100.1011 = -0b1.1011 \times 2^{\circ} = -1.6875
0x0c = 0.000_{1100} = +0b0.1100 \times 2^{-3} = 0.09375
                                                           0x4c = 0_{-}100_{-}1100 = +0b1.1100 \times 2^{\circ}0 = 1.75
                                                                                                                  0x8c = 1_000_1100 = -0b0.1100 \times 2^{-3} = -0.09375
                                                                                                                                                                               0xcc = 1.100.1100 = -0b1.1100 \times 2^{\circ} = -1.75
0x0d = 0.000_1101 = +0b0.1101 \times 2^{-3} = 0.1015625
                                                           0x4d = 0.100.1101 = +0b1.1101 \times 20 = 1.8125
                                                                                                                  0x8d = 1_000_1101 = -0b0.1101 \times 2^{-3} = -0.1015625
                                                                                                                                                                              0xcd = 1_100_1101 = -0b1.1101 \times 2^{\circ}0 = -1.8125
                                                                                                                                                                              0xce = 1.100.1110 = -0b1.1110 \times 2^{\circ}0 = -1.875
0x0e = 0.000_{-}1110 = +0b0.1110 \times 2^{-}3 = 0.109375
                                                           0x4e = 0.100.1110 = +0b1.1110 \times 2^{\circ} = 1.875
                                                                                                                  0x8e = 1.000.1110 = -0b0.1110 \times 2^{-3} = -0.109375
0x0f = 0.000.1111 = +0b0.1111 \times 2^{-3} = 0.1171875
                                                           0x4f = 0.100.1111 = +0b1.1111 \times 2^{\circ} = 1.9375
                                                                                                                  0x8f = 1.000_11111 = -0b0.11111 \times 2^{-3} = -0.1171875
                                                                                                                                                                              0xcf = 1.100.1111 = -0b1.1111 \times 2^{\circ} = -1.9375
0x10 = 0.001.0000 = +0b1.0000 \times 2^{-3} = 0.125
                                                                                                                                                                               0xd0 = 1_101_0000 = -0b1.0000 \times 2^1 = -2.0
                                                           0x50 = 0.101.0000 = +0b1.0000 \times 2^1 = 2.0
                                                                                                                  0x90 = 1.001.0000 = -0b1.0000 \times 2^{-3} = -0.125
0x11 = 0.001.0001 = +0b1.0001 \times 2^{-3} = 0.1328125
                                                           0x51 = 0_101_0001 = +0b1.0001 \times 2^1 = 2.125
                                                                                                                  0x91 = 1_001_0001 = -0b1.0001 \times 2^{-3} = -0.1328125
                                                                                                                                                                              0xd1 = 1_101_0001 = -0b1.0001 \times 2^1 = -2.125
0x12 = 0.001.0010 = +0b1.0010 \times 2^{-3} = 0.140625
                                                           0x52 = 0.101.0010 = +0b1.0010 \times 2^1 = 2.25
                                                                                                                  0x92 = 1.001.0010 = -0b1.0010 \times 2^{-3} = -0.140625
                                                                                                                                                                               0xd2 = 1.101.0010 = -0b1.0010 \times 2^1 = -2.25
                                                                                                                  0x93 = 1.001.0011 = -0b1.0011 \times 2^{-3} = -0.1484375
0x13 = 0.001.0011 = +0b1.0011 \times 2^{-3} = 0.1484375
                                                           0x53 = 0.101.0011 = +0b1.0011 \times 2^1 = 2.375
                                                                                                                                                                              0xd3 = 1_101_0011 = -0b1.0011 \times 2^1 = -2.375
0x14 = 0.001.0100 = +0b1.0100 \times 2^{-3} = 0.15625
                                                           0x54 = 0_101_0100 = +0b1.0100 \times 2^1 = 2.5
                                                                                                                  0x94 = 1_001_0100 = -0b1.0100 \times 2^{-3} = -0.15625
                                                                                                                                                                               0xd4 = 1_101_0100 = -0b1.0100 \times 2^1 = -2.5
0x15 = 0.001.0101 = +0b1.0101 \times 2^{-3} = 0.1640625
                                                           0x55 = 0_101_0101 = +0b1.0101 \times 2^1 = 2.625
                                                                                                                  0x95 = 1_001_0101 = -0b1.0101 \times 2^{-3} = -0.1640625
                                                                                                                                                                               0xd5 = 1_{-}101_{-}0101 = -0b1_{-}0101 \times 2^{-}1 = -2.625
0x16 = 0.001.0110 = +0b1.0110 \times 2^{-3} = 0.171875
                                                           0x56 = 0.101.0110 = +0b1.0110 \times 2^1 = 2.75
                                                                                                                  0x96 = 1.001.0110 = -0b1.0110 \times 2^{-3} = -0.171875
                                                                                                                                                                               0xd6 = 1.101.0110 = -0b1.0110 \times 2^1 = -2.75
0x17 = 0.001.0111 = +0b1.0111 \times 2^{-3} = 0.1796875
                                                           0x57 = 0.101.0111 = +0b1.0111 \times 2^1 = 2.875
                                                                                                                  0x97 = 1.001.0111 = -0b1.0111 \times 2^{-3} = -0.1796875
                                                                                                                                                                               0xd7 = 1_101_0111 = -0b1.0111 \times 2^1 = -2.875
0x18 = 0.001.1000 = +0b1.1000 \times 2^{-3} = 0.1875
                                                           0x58 = 0.101.1000 = +0b1.1000 \times 2^1 = 3.0
                                                                                                                  0x98 = 1.001.1000 = -0b1.1000 \times 2^{-3} = -0.1875
                                                                                                                                                                               0xd8 = 1_101_1000 = -0b1.1000 \times 2^1 = -3.0
0x19 = 0.001.1001 = +0b1.1001 \times 2^{-3} = 0.1953125
                                                           0x59 = 0_101_1001 = +0b1.1001 \times 2^1 = 3.125
                                                                                                                  0x99 = 1_001_1001 = -0b1.1001 \times 2^{-3} = -0.1953125
                                                                                                                                                                              0xd9 = 1_101_1001 = -0b1.1001 \times 2^1 = -3.125
0x1a = 0.001.1010 = +0b1.1010 \times 2^{-3} = 0.203125
                                                           0x5a = 0.101.1010 = +0b1.1010 \times 2^1 = 3.25
                                                                                                                  0x9a = 1.001.1010 = -0b1.1010 \times 2^{-3} = -0.203125
                                                                                                                                                                               0xda = 1.101.1010 = -0b1.1010 \times 2^1 = -3.25
0x1b = 0.001.1011 = +0b1.1011 \times 2^{-3} = 0.2109375
                                                           0x5b = 0.101.1011 = +0b1.1011 \times 2^1 = 3.375
                                                                                                                  0x9b = 1.001.1011 = -0b1.1011 \times 2^{-3} = -0.2109375
                                                                                                                                                                              0xdb = 1.101.1011 = -0b1.1011 \times 2^1 = -3.375
0x1c = 0.001.1100 = +0b1.1100 \times 2^{-3} = 0.21875
                                                           0x5c = 0_101_1100 = +0b1.1100 \times 2^1 = 3.5
                                                                                                                  0x9c = 1_001_1100 = -0b1.1100 \times 2^{-3} = -0.21875
                                                                                                                                                                               0xdc = 1_101_1100 = -0b1.1100 \times 2^1 = -3.5
                                                                                                                  0x9d = 1_001_1101 = -0b1.1101 \times 2^{-3} = -0.2265625
0x1d = 0.001_1101 = +0b1.1101 \times 2^{-3} = 0.2265625
                                                           0x5d = 0_101_1101 = +0b1.1101 \times 2^1 = 3.625
                                                                                                                                                                              0xdd = 1_101_1101 = -0b1.1101 \times 2^1 = -3.625
0x1e = 0.001.1110 = +0b1.1110 \times 2^{-3} = 0.234375
                                                                                                                  0x9e = 1.001.1110 = -0b1.1110 \times 2^{-3} = -0.234375
                                                           0x5e = 0.101.1110 = +0b1.1110 \times 2^1 = 3.75
                                                                                                                                                                               0xde = 1.101.1110 = -0b1.1110 \times 2^1 = -3.75
0x1f = 0.001.1111 = +0b1.1111 \times 2^{-3} = 0.2421875
                                                           0x5f = 0.101.1111 = +0b1.1111 \times 2^1 = 3.875
                                                                                                                  0x9f = 1.001.1111 = -0b1.1111 \times 2^{-3} = -0.2421875
                                                                                                                                                                              0xdf = 1.101.1111 = -0b1.1111 \times 2^1 = -3.875
0x20 = 0.010.0000 = +0b1.0000 \times 2^{-2} = 0.25
                                                           0x60 = 0_110_0000 = +0b1.0000 \times 2^2 = 4.0
                                                                                                                  0xa0 = 1.010.0000 = -0b1.0000 \times 2^{-2} = -0.25
                                                                                                                                                                               0xe0 = 1.110.0000 = -0b1.0000 \times 2^2 = -4.0
0x21 = 0_010_0001 = +0b1.0001 \times 2^2 = 0.265625
                                                           0x61 = 0_110_0001 = +0b1.0001 \times 2^2 = 4.25
                                                                                                                  0xa1 = 1_010_0001 = -0b1.0001 \times 2^2 = -0.265625
                                                                                                                                                                               0xe1 = 1_110_0001 = -0b1.0001 \times 2^2 = -4.25
0x22 = 0.010.0010 = +0b1.0010 \times 2^{-2} = 0.28125
                                                           0x62 = 0.110.0010 = +0b1.0010 \times 2^2 = 4.5
                                                                                                                  0xa2 = 1_010_0010 = -0b1.0010 \times 2^2 = -0.28125
                                                                                                                                                                               0xe2 = 1.110.0010 = -0b1.0010 \times 2^2 = -4.5
0x23 = 0.010.0011 = +0b1.0011 \times 2^{-2} = 0.296875
                                                           0x63 = 0.110.0011 = +0b1.0011 \times 2^2 = 4.75
                                                                                                                  0xa3 = 1.010.0011 = -0b1.0011 \times 2^{-2} = -0.296875
                                                                                                                                                                               0xe3 = 1.110.0011 = -0b1.0011 \times 2^2 = -4.75
0x24 = 0_010_0100 = +0b1.0100 \times 2^2 = 0.3125
                                                           0x64 = 0_110_0100 = +0b1.0100 \times 2^2 = 5.0
                                                                                                                  0xa4 = 1_010_0100 = -0b1.0100 \times 2^2 = -0.3125
                                                                                                                                                                               0xe4 = 1_110_0100 = -0b1.0100 \times 2^2 = -5.0
                                                                                                                  0xa5 = 1_010_0101 = -0b1.0101 \times 2^2 = -0.328125
0x25 = 0.010.0101 = +0b1.0101 \times 2^{-2} = 0.328125
                                                           0x65 = 0.110.0101 = +0b1.0101 \times 2^2 = 5.25
                                                                                                                                                                              0xe5 = 1_110_0101 = -0b1.0101 \times 2^2 = -5.25
0x26 = 0.010.0110 = +0b1.0110 \times 2^{-2} = 0.34375
                                                           0x66 = 0.110.0110 = +0b1.0110 \times 2^2 = 5.5
                                                                                                                  0xa6 = 1.010.0110 = -0b1.0110 \times 2^{-2} = -0.34375
                                                                                                                                                                               0xe6 = 1.110.0110 = -0b1.0110 \times 2^2 = -5.5
0x27 = 0_010_0111 = +0b1.0111 \times 2^2 = 0.359375
                                                           0x67 = 0_110_0111 = +0b1.0111 \times 2^2 = 5.75
                                                                                                                  0xa7 = 1.010.0111 = -0b1.0111 \times 2^{-2} = -0.359375
                                                                                                                                                                              0xe7 = 1_110_0111 = -0b1.0111 \times 2^2 = -5.75
0x28 = 0_010_1000 = +0b1.1000 \times 2^-2 = 0.375
                                                           0x68 = 0_110_1000 = +0b1.1000 \times 2^2 = 6.0
                                                                                                                  0xa8 = 1_010_1000 = -0b1.1000 \times 2^2 = -0.375
                                                                                                                                                                               0xe8 = 1_110_1000 = -0b1.1000 \times 2^2 = -6.0
0x29 = 0_010_1001 = +0b1.1001 \times 2^2 = 0.390625
                                                           0x69 = 0_110_1001 = +0b1.1001 \times 2^2 = 6.25
                                                                                                                  0xa9 = 1_010_1001 = -0b1.1001 \times 2^2 = -0.390625
                                                                                                                                                                               0xe9 = 1_110_1001 = -0b1.1001 \times 2^2 = -6.25
                                                           0x6a = 0.110.1010 = +0b1.1010 \times 2^2 = 6.5
0x2a = 0.010.1010 = +0b1.1010 \times 2^{-2} = 0.40625
                                                                                                                  0xaa = 1.010.1010 = -0b1.1010 \times 2^{-2} = -0.40625
                                                                                                                                                                               0xea = 1.110.1010 = -0b1.1010 \times 2^2 = -6.5
0x2b = 0.010.1011 = +0b1.1011 \times 2^{-2} = 0.421875
                                                           0x6b = 0_110_1011 = +0b1.1011 \times 2^2 = 6.75
                                                                                                                  0xab = 1.010.1011 = -0b1.1011 \times 2^{-2} = -0.421875
                                                                                                                                                                               0xeb = 1.110.1011 = -0b1.1011 \times 2^2 = -6.75
0x2c = 0_010_1100 = +0b1.1100 \times 2^2 = 0.4375
                                                           0x6c = 0.110.1100 = +0b1.1100 \times 2^2 = 7.0
                                                                                                                  0xac = 1_010_1100 = -0b1.1100 \times 2^2 = -0.4375
                                                                                                                                                                               0 \text{xec} = 1_110_1100 = -0b1.1100 \times 2^2 = -7.0
0x2d = 0.010.1101 = +0b1.1101 \times 2^{-2} = 0.453125
                                                           0x6d = 0_110_1101 = +0b1.1101 \times 2^2 = 7.25
                                                                                                                  0xad = 1_010_1101 = -0b1.1101 \times 2^2 = -0.453125
                                                                                                                                                                               0xed = 1_110_1101 = -0b1.1101 \times 2^2 = -7.25
0x2e = 0.010.1110 = +0b1.1110 \times 2^{-2} = 0.46875
                                                           0x6e = 0.110.1110 = +0b1.1110 \times 2^2 = 7.5
                                                                                                                  0xae = 1.010.1110 = -0b1.1110 \times 2^{-2} = -0.46875
                                                                                                                                                                               0xee = 1.110.1110 = -0b1.1110 \times 2^2 = -7.5
0x2f = 0_010_1111 = +0b1.1111 \times 2^2 = 0.484375
                                                           0x6f = 0.110.1111 = +0b1.1111 \times 2^2 = 7.75
                                                                                                                  0xaf = 1.010.1111 = -0b1.1111 \times 2^{-2} = -0.484375
                                                                                                                                                                               0xef = 1.110.1111 = -0b1.1111 \times 2^2 = -7.75
0x30 = 0.011.0000 = +0b1.0000 \times 2^{-1} = 0.5
                                                           0x70 = 0.111.0000 = +0b1.0000 \times 2^3 = 8.0
                                                                                                                  0xb0 = 1_011_0000 = -0b1.0000 \times 2^-1 = -0.5
                                                                                                                                                                               0xf0 = 1_111_0000 = -0b1.0000 \times 2^3 = -8.0
0x31 = 0_011_0001 = +0b1.0001 \times 2^-1 = 0.53125
                                                           0x71 = 0_111_0001 = +0b1.0001 \times 2^3 = 8.5
                                                                                                                  0xb1 = 1_011_0001 = -0b1.0001 \times 2^-1 = -0.53125
                                                                                                                                                                               0xf1 = 1_111_0001 = -0b1.0001 \times 2^3 = -8.5
0x32 = 0.011.0010 = +0b1.0010 \times 2^{-1} = 0.5625
                                                           0x72 = 0.111.0010 = +0b1.0010 \times 2^3 = 9.0
                                                                                                                  0xb2 = 1.011.0010 = -0b1.0010 \times 2^{-1} = -0.5625
                                                                                                                                                                               0xf2 = 1_111_0010 = -0b1.0010 \times 2^3 = -9.0
0x33 = 0.011.0011 = +0b1.0011 \times 2^-1 = 0.59375
                                                           0x73 = 0.111.0011 = +0b1.0011 \times 2^3 = 9.5
                                                                                                                  0xb3 = 1_011_0011 = -0b1.0011 \times 2^-1 = -0.59375
                                                                                                                                                                              0xf3 = 1_111_0011 = -0b1.0011 \times 2^3 = -9.5
0x34 = 0.011.0100 = +0b1.0100 \times 2^{-1} = 0.625
                                                           0x74 = 0_111_0100 = +0b1.0100 \times 2^3 = 10.0
                                                                                                                  0xb4 = 1_011_0100 = -0b1.0100 \times 2^-1 = -0.625
                                                                                                                                                                               0xf4 = 1_111_0100 = -0b1.0100 \times 2^3 = -10.0
0x35 = 0.011.0101 = +0b1.0101 \times 2^{-1} = 0.65625
                                                           0x75 = 0.111.0101 = +0b1.0101 \times 2^3 = 10.5
                                                                                                                  0xb5 = 1_011_0101 = -0b1.0101 \times 2^-1 = -0.65625
                                                                                                                                                                               0xf5 = 1_111_0101 = -0b1.0101 \times 2^3 = -10.5
0x36 = 0.011.0110 = +0b1.0110 \times 2^{-1} = 0.6875
                                                           0x76 = 0.111.0110 = +0b1.0110 \times 2^3 = 11.0
                                                                                                                  0xb6 = 1.011.0110 = -0b1.0110 \times 2^{-1} = -0.6875
                                                                                                                                                                               0xf6 = 1.111.0110 = -0b1.0110 \times 2^3 = -11.0
0x37 = 0.011.0111 = +0b1.0111 \times 2^{-1} = 0.71875
                                                           0x77 = 0.111.0111 = +0b1.0111 \times 2^3 = 11.5
                                                                                                                  0xb7 = 1_011_0111 = -0b1.0111 \times 2^-1 = -0.71875
                                                                                                                                                                               0xf7 = 1_111_0111 = -0b1.0111 \times 2^3 = -11.5
0x38 = 0_011_1000 = +0b1.1000 \times 2^-1 = 0.75
                                                           0x78 = 0_111_1000 = +0b1.1000 \times 2^3 = 12.0
                                                                                                                  0xb8 = 1_011_1000 = -0b1.1000 \times 2^{-1} = -0.75
                                                                                                                                                                               0xf8 = 1_111_1000 = -0b1.1000 \times 2^3 = -12.0
0x39 = 0_011_1001 = +0b1.1001 \times 2^-1 = 0.78125
                                                           0x79 = 0_111_1001 = +0b1.1001 \times 2^3 = 12.5
                                                                                                                  0xb9 = 1_011_1001 = -0b1.1001 \times 2^-1 = -0.78125
                                                                                                                                                                               0xf9 = 1_111_1001 = -0b1.1001 \times 2^3 = -12.5
0x3a = 0.011.1010 = +0b1.1010 \times 2^{-1} = 0.8125
                                                           0x7a = 0.111.1010 = +0b1.1010 \times 2^3 = 13.0
                                                                                                                  0xba = 1.011.1010 = -0b1.1010 \times 2^{-1} = -0.8125
                                                                                                                                                                               0xfa = 1.111.1010 = -0b1.1010 \times 2^3 = -13.0
0x3b = 0_011_1011 = +0b1.1011 \times 2^-1 = 0.84375
                                                           0x7b = 0_111_1011 = +0b1.1011 \times 2^3 = 13.5
                                                                                                                  0xbb = 1_011_1011 = -0b1.1011 \times 2^-1 = -0.84375
                                                                                                                                                                              0xfb = 1_111_1011 = -0b1.1011 \times 2^3 = -13.5
                                                                                                                  0xbc = 1_011_1100 = -0b1.1100 \times 2^-1 = -0.875
0x3c = 0_011_1100 = +0b1.1100 \times 2^{-1} = 0.875
                                                           0x7c = 0_111_1100 = +0b1.1100 \times 2^3 = 14.0
                                                                                                                                                                               0xfc = 1_111_1100 = -0b1.1100 \times 2^3 = -14.0
0 x 3 d = 0\_011\_1101 = +0 b1.1101 \times 2 \hat{\ } -1 = 0.90625
                                                           \mathtt{0x7d} = \mathtt{0\_111\_1101} = +\mathtt{0b1.1101} {\times} \mathtt{2\^{-}3} = \mathtt{14.5}
                                                                                                                  0xbd = 1_011_1101 = -0b1.1101 \times 2^-1 = -0.90625
                                                                                                                                                                              0xfd = 1_111_1101 = -0b1.1101 \times 2^3 = -14.5
0x3e = 0.011.1110 = +0b1.1110 \times 2^{-1} = 0.9375
                                                           0x7e = 0.111.1110 = +0b1.1110 \times 2^3 = 15.0
                                                                                                                  0xbe = 1.011.1110 = -0b1.1110 \times 2^{-1} = -0.9375
                                                                                                                                                                               0xfe = 1.111.1110 = -0b1.1110 \times 2^3 = -15.0
0x3f = 0_011_1111 = +0b1.1111 \times 2^-1 = 0.96875
                                                           0x7f = 0_111_1111 = +Inf
                                                                                                                  0xbf = 1_011_1111 = -0b1.1111 \times 2^-1 = -0.96875
                                                                                                                                                                              0xff = 1_111_1111 = -Inf
```

C.6 Value Table: P6, emin = -1, emax = 1

```
0x00 = 0.000000 = 0.0
                                                           0x40 = 0.10.00000 = +0b1.00000 \times 2^{\circ} = 1.0
                                                                                                                    0x80 = 1_00_00000 = NaN
                                                                                                                                                                                 0xc0 = 1.10.00000 = -0b1.00000 \times 2^{\circ}0 = -1.0
0x01 = 0.00.00001 = +0b0.00001 \times 2^{-1} = 0.015625
                                                                                                                    0x81 = 1_00_00001 = -0b0.00001 \times 2^-1 = -0.015625
                                                           0x41 = 0.10.00001 = +0b1.00001 \times 2^{\circ} = 1.03125
                                                                                                                                                                                0xc1 = 1_10_00001 = -0b1.00001 \times 2^0 = -1.03125
0x02 = 0.00.00010 = +0b0.00010 \times 2^{-1} = 0.03125
                                                           0x42 = 0.10.00010 = +0b1.00010 \times 2^{\circ}0 = 1.0625
                                                                                                                    0x82 = 1.00.00010 = -0b0.00010 \times 2^{-1} = -0.03125
                                                                                                                                                                                 0xc2 = 1_{-}10_{-}00010 = -0b1_{-}00010 \times 2^{\circ}0 = -1_{-}0625
0x03 = 0.00.00011 = +0b0.00011 \times 2^{-1} = 0.046875
                                                           0x43 = 0.10.00011 = +0b1.00011 \times 2^{\circ} = 1.09375
                                                                                                                    0x83 = 1.00.00011 = -0b0.00011 \times 2^{-1} = -0.046875
                                                                                                                                                                                0xc3 = 1.10.00011 = -0b1.00011 \times 2^{\circ}0 = -1.09375
0x04 = 0.00.00100 = +0b0.00100 \times 2^{-1} = 0.0625
                                                           0x44 = 0.10.00100 = +0b1.00100 \times 2^{\circ} = 1.125
                                                                                                                    0x84 = 1_00_00100 = -0b0.00100 \times 2^-1 = -0.0625
                                                                                                                                                                                 0xc4 = 1_10_00100 = -0b1.00100 \times 2^0 = -1.125
                                                                                                                    0x85 = 1_00_00101 = -0b0.00101 \times 2^-1 = -0.078125
0x05 = 0.00.00101 = +0b0.00101 \times 2^{-1} = 0.078125
                                                           0x45 = 0.10.00101 = +0b1.00101 \times 2^{\circ} = 1.15625
                                                                                                                                                                                0xc5 = 1_10_00101 = -0b1.00101 \times 2^0 = -1.15625
0x06 = 0.00.00110 = +0b0.00110 \times 2^{-1} = 0.09375
                                                           0x46 = 0.10.00110 = +0b1.00110 \times 2^{\circ} = 1.1875
                                                                                                                    0x86 = 1.00.00110 = -0b0.00110 \times 2^{-1} = -0.09375
                                                                                                                                                                                0xc6 = 1.10.00110 = -0b1.00110 \times 2^{\circ}0 = -1.1875
0x07 = 0.00.00111 = +0b0.00111 \times 2^{-1} = 0.109375
                                                           0x47 = 0.10.00111 = +0b1.00111 \times 2^{\circ} = 1.21875
                                                                                                                    0x87 = 1.00.00111 = -0b0.00111 \times 2^{-1} = -0.109375
                                                                                                                                                                                0xc7 = 1.10.00111 = -0b1.00111 \times 2^{\circ}0 = -1.21875
0x08 = 0.00.01000 = +0b0.01000 \times 2^{-1} = 0.125
                                                                                                                    0x88 = 1_00_01000 = -0b0.01000 \times 2^-1 = -0.125
                                                                                                                                                                                0xc8 = 1_10_01000 = -0b1.01000 \times 2^0 = -1.25
                                                           0x48 = 0.10.01000 = +0b1.01000 \times 2^{\circ} = 1.25
0 x 0 9 = 0\_00\_01001 = +0 b 0.01001 \times 2^-1 = 0.140625
                                                                                                                    0x89 = 1_00_01001 = -0b0.01001 \times 2^-1 = -0.140625
                                                           0x49 = 0.10.01001 = +0b1.01001 \times 2^{\circ} = 1.28125
                                                                                                                                                                                0xc9 = 1_10_01001 = -0b1.01001 \times 2^0 = -1.28125
0x0a = 0.00.01010 = +0b0.01010 \times 2^{-1} = 0.15625
                                                           0x4a = 0.10.01010 = +0b1.01010 \times 2^{\circ} = 1.3125
                                                                                                                    0x8a = 1.00.01010 = -0b0.01010 \times 2^{-1} = -0.15625
                                                                                                                                                                                 0xca = 1_{-}10_{-}01010 = -0b1.01010 \times 2^{\circ}0 = -1.3125
0x0b = 0.00.01011 = +0b0.01011 \times 2^{-1} = 0.171875
                                                           0x4b = 0.10.01011 = +0b1.01011 \times 2^{\circ} = 1.34375
                                                                                                                    0x8b = 1.00.01011 = -0b0.01011 \times 2^{-1} = -0.171875
                                                                                                                                                                                0xcb = 1.10.01011 = -0b1.01011 \times 2^{\circ}0 = -1.34375
0x0c = 0.00.01100 = +0b0.01100 \times 2^{-1} = 0.1875
                                                           0x4c = 0_10_01100 = +0b1.01100 \times 2^{\circ} = 1.375
                                                                                                                    0x8c = 1_00_01100 = -0b0.01100 \times 2^-1 = -0.1875
                                                                                                                                                                                 0xcc = 1_{-}10_{-}01100 = -0b1.01100 \times 2^{\circ}0 = -1.375
0x0d = 0_00_01101 = +0b0.01101 \times 2^-1 = 0.203125
                                                           0x4d = 0.10.01101 = +0b1.01101 \times 20 = 1.40625
                                                                                                                    0x8d = 1.00.01101 = -0b0.01101 \times 2^{-1} = -0.203125
                                                                                                                                                                                0xcd = 1_10_01101 = -0b1.01101 \times 2^0 = -1.40625
0x0e = 0.00.01110 = +0b0.01110 \times 2^{-1} = 0.21875
                                                           0x4e = 0.10.01110 = +0b1.01110 \times 2^{\circ} = 1.4375
                                                                                                                    0x8e = 1.00.01110 = -0b0.01110 \times 2^{-1} = -0.21875
                                                                                                                                                                                0xce = 1.10.01110 = -0b1.01110 \times 2^{\circ} = -1.4375
0x0f = 0.00.01111 = +0b0.01111 \times 2^{-1} = 0.234375
                                                           0x4f = 0.10.01111 = +0b1.01111 \times 2^{\circ} = 1.46875
                                                                                                                    0x8f = 1.00.01111 = -0b0.01111 \times 2^{-1} = -0.234375
                                                                                                                                                                                0xcf = 1_10_01111 = -0b1.01111 \times 2^0 = -1.46875
0x10 = 0.00.10000 = +0b0.10000 \times 2^{-1} = 0.25
                                                           0x50 = 0.10.10000 = +0b1.10000 \times 2^{\circ} = 1.5
                                                                                                                    0x90 = 1.00.10000 = -0b0.10000 \times 2^{-1} = -0.25
                                                                                                                                                                                 0xd0 = 1.10.10000 = -0b1.10000 \times 2^{\circ}0 = -1.5
0x11 = 0_00_10001 = +0b0.10001 \times 2^-1 = 0.265625
                                                           0x51 = 0.10.10001 = +0b1.10001 \times 20 = 1.53125
                                                                                                                    0x91 = 1_00_10001 = -0b0.10001 \times 2^-1 = -0.265625
                                                                                                                                                                                0xd1 = 1_10_10001 = -0b1.10001 \times 2^0 = -1.53125
0x12 = 0.00.10010 = +0b0.10010 \times 2^{-1} = 0.28125
                                                           0x52 = 0.10.10010 = +0b1.10010 \times 2^{\circ} = 1.5625
                                                                                                                    0x92 = 1.00.10010 = -0b0.10010 \times 2^{-1} = -0.28125
                                                                                                                                                                                0xd2 = 1_{-}10_{-}10010 = -0b1.10010 \times 2^{\circ}0 = -1.5625
                                                           0x53 = 0.10.10011 = +0b1.10011 \times 20 = 1.59375
                                                                                                                                                                                0xd3 = 1.10.10011 = -0b1.10011 \times 2^{\circ}0 = -1.59375
0x13 = 0.00_{-}10011 = +0b0.10011 \times 2^{-1} = 0.296875
                                                                                                                    0x93 = 1.00.10011 = -0b0.10011 \times 2^{-1} = -0.296875
0x14 = 0.00_{-}10100 = +0b0.10100 \times 2^{-}1 = 0.3125
                                                           0x54 = 0_10_10100 = +0b1.10100 \times 20 = 1.625
                                                                                                                    0x94 = 1.00.10100 = -0b0.10100 \times 2^{-1} = -0.3125
                                                                                                                                                                                 0xd4 = 1.10.10100 = -0b1.10100 \times 2^{\circ}0 = -1.625
0x15 = 0.00_{-}10101 = +0b0.10101 \times 2^{-1} = 0.328125
                                                           0x55 = 0.10.10101 = +0b1.10101 \times 20 = 1.65625
                                                                                                                    0x95 = 1.00.10101 = -0b0.10101 \times 2^{-1} = -0.328125
                                                                                                                                                                                0xd5 = 1_10_10101 = -0b1.10101 \times 2^0 = -1.65625
0x16 = 0.00.10110 = +0b0.10110 \times 2^{-1} = 0.34375
                                                           0x56 = 0.10.10110 = +0b1.10110 \times 2^{\circ}0 = 1.6875
                                                                                                                    0x96 = 1.00.10110 = -0b0.10110 \times 2^{-1} = -0.34375
                                                                                                                                                                                0xd6 = 1.10.10110 = -0b1.10110 \times 2^{\circ} = -1.6875
0x17 = 0.00_10111 = +0b0.10111 \times 2^{-1} = 0.359375
                                                           0x57 = 0.10.10111 = +0b1.10111 \times 2^{\circ} = 1.71875
                                                                                                                    0x97 = 1.00.10111 = -0b0.10111 \times 2^{-1} = -0.359375
                                                                                                                                                                                0xd7 = 1.10.10111 = -0b1.10111 \times 2^{\circ}0 = -1.71875
0x18 = 0.00_{11000} = +0b0.11000 \times 2^{-1} = 0.375
                                                           0x58 = 0.10.11000 = +0b1.11000 \times 2^{\circ} = 1.75
                                                                                                                    0x98 = 1_00_11000 = -0b0.11000 \times 2^-1 = -0.375
                                                                                                                                                                                 0xd8 = 1_10_11000 = -0b1.11000 \times 2^0 = -1.75
0x19 = 0.00_11001 = +0b0.11001 \times 2^-1 = 0.390625
                                                           0x59 = 0.10.11001 = +0b1.11001 \times 2^{\circ} = 1.78125
                                                                                                                    0x99 = 1_00_11001 = -0b0.11001 \times 2^-1 = -0.390625
                                                                                                                                                                                0xd9 = 1_10_11001 = -0b1.11001 \times 2^0 = -1.78125
0x1a = 0.00.11010 = +0b0.11010 \times 2^{-1} = 0.40625
                                                           0x5a = 0.10.11010 = +0b1.11010 \times 2^{\circ} = 1.8125
                                                                                                                    0x9a = 1.00.11010 = -0b0.11010 \times 2^{-1} = -0.40625
                                                                                                                                                                                0xda = 1.10.11010 = -0b1.11010 \times 2^{\circ} = -1.8125
0x1b = 0.00.11011 = +0b0.11011 \times 2^{-1} = 0.421875
                                                           0x5b = 0.10.11011 = +0b1.11011 \times 2^{\circ} = 1.84375
                                                                                                                    0x9b = 1.00.11011 = -0b0.11011 \times 2^{-1} = -0.421875
                                                                                                                                                                                0xdb = 1.10.11011 = -0b1.11011 \times 2^{\circ}0 = -1.84375
0x1c = 0.00_111100 = +0b0.11100 \times 2^{-1} = 0.4375
                                                           0x5c = 0_10_11100 = +0b1.11100 \times 2\% = 1.875
                                                                                                                    0x9c = 1_00_11100 = -0b0.11100 \times 2^-1 = -0.4375
                                                                                                                                                                                0xdc = 1.10.11100 = -0b1.11100 \times 2^{\circ}0 = -1.875
                                                                                                                    0x9d = 1_00_11101 = -0b0.11101 \times 2^-1 = -0.453125
0x1d = 0.00_111101 = +0b0.11101 \times 2^-1 = 0.453125
                                                                                                                                                                                0xdd = 1_10_11101 = -0b1.11101 \times 2^0 = -1.90625
                                                           0x5d = 0.10.11101 = +0b1.11101 \times 2^{\circ} = 1.90625
0x1e = 0.00.11110 = +0b0.11110 \times 2^{-1} = 0.46875
                                                           0x5e = 0.10.11110 = +0b1.11110 \times 2^{\circ} = 1.9375
                                                                                                                    0x9e = 1.00.111110 = -0b0.111110 \times 2^{-1} = -0.46875
                                                                                                                                                                                0xde = 1.10.11110 = -0b1.11110 \times 2^{\circ}0 = -1.9375
0x1f = 0.00_111111 = +0b0.111111 \times 2^{-1} = 0.484375
                                                                                                                    0x9f = 1.00.111111 = -0b0.111111 \times 2^{-1} = -0.484375
                                                           0x5f = 0.10.111111 = +0b1.111111 \times 2^{\circ} = 1.96875
                                                                                                                                                                                0xdf = 1_10_111111 = -0b1.111111 \times 2^0 = -1.96875
0x20 = 0.01.00000 = +0b1.00000 \times 2^{-1} = 0.5
                                                           0x60 = 0.11.00000 = +0b1.00000 \times 2^1 = 2.0
                                                                                                                    0xa0 = 1_01_00000 = -0b1.00000 \times 2^{-1} = -0.5
                                                                                                                                                                                 0xe0 = 1.11.00000 = -0b1.00000 \times 2^1 = -2.0
0x21 = 0.01.00001 = +0b1.00001 \times 2^{-1} = 0.515625
                                                           0x61 = 0_11_00001 = +0b1.00001 \times 2^1 = 2.0625
                                                                                                                    0xa1 = 1_01_00001 = -0b1.00001 \times 2^-1 = -0.515625
                                                                                                                                                                                0xe1 = 1_11_00001 = -0b1.00001 \times 2^1 = -2.0625
0x22 = 0.01.00010 = +0b1.00010 \times 2^{-1} = 0.53125
                                                           0x62 = 0.11.00010 = +0b1.00010 \times 2^1 = 2.125
                                                                                                                    0xa2 = 1.01.00010 = -0b1.00010 \times 2^{-1} = -0.53125
                                                                                                                                                                                 0xe2 = 1_11_00010 = -0b1.00010 \times 2^1 = -2.125
0x23 = 0.01.00011 = +0b1.00011 \times 2^{-1} = 0.546875
                                                           0x63 = 0_11_00011 = +0b1.00011 \times 2^1 = 2.1875
                                                                                                                    0xa3 = 1.01.00011 = -0b1.00011 \times 2^{-1} = -0.546875
                                                                                                                                                                                0xe3 = 1.11.00011 = -0b1.00011 \times 2^1 = -2.1875
0x24 = 0_01_00100 = +0b1.00100 \times 2^{-1} = 0.5625
                                                           0x64 = 0_11_00100 = +0b1.00100 \times 2^1 = 2.25
                                                                                                                    0xa4 = 1_01_00100 = -0b1.00100 \times 2^-1 = -0.5625
                                                                                                                                                                                 0xe4 = 1_11_00100 = -0b1.00100 \times 2^1 = -2.25
0x25 = 0.01.00101 = +0b1.00101 \times 2^{-1} = 0.578125
                                                                                                                    0xa5 = 1_01_00101 = -0b1.00101 \times 2^-1 = -0.578125
                                                                                                                                                                                0xe5 = 1_11_00101 = -0b1.00101 \times 2^1 = -2.3125
                                                           0x65 = 0_11_00101 = +0b1.00101 \times 2^1 = 2.3125
0x26 = 0.01.00110 = +0b1.00110 \times 2^{-1} = 0.59375
                                                           0x66 = 0.11.00110 = +0b1.00110 \times 2^1 = 2.375
                                                                                                                    0xa6 = 1_01_00110 = -0b1.00110 \times 2^-1 = -0.59375
                                                                                                                                                                                0xe6 = 1_11_00110 = -0b1.00110 \times 2^1 = -2.375
0x27 = 0.01.00111 = +0b1.00111 \times 2^-1 = 0.609375
                                                           0x67 = 0.11.00111 = +0b1.00111 \times 2^1 = 2.4375
                                                                                                                    0xa7 = 1_01_00111 = -0b1.00111 \times 2^-1 = -0.609375
                                                                                                                                                                                0xe7 = 1.11.00111 = -0b1.00111 \times 2^1 = -2.4375
0x28 = 0_01_01000 = +0b1.01000 \times 2^-1 = 0.625
                                                                                                                    0xa8 = 1_01_01000 = -0b1.01000 \times 2^-1 = -0.625
                                                                                                                                                                                 0xe8 = 1_11_01000 = -0b1.01000 \times 2^1 = -2.5
                                                           0x68 = 0_11_01000 = +0b1.01000 \times 2^1 = 2.5
                                                                                                                    0xa9 = 1_01_01001 = -0b1.01001 \times 2^-1 = -0.640625
                                                                                                                                                                                0xe9 = 1_11_01001 = -0b1.01001 \times 2^1 = -2.5625
0x29 = 0_01_01001 = +0b1.01001 \times 2^-1 = 0.640625
                                                           0x69 = 0_11_01001 = +0b1.01001 \times 2^1 = 2.5625
0x2a = 0.01.01010 = +0b1.01010 \times 2^{-1} = 0.65625
                                                           0x6a = 0.11.01010 = +0b1.01010 \times 2^1 = 2.625
                                                                                                                    0xaa = 1.01.01010 = -0b1.01010 \times 2^{-1} = -0.65625
                                                                                                                                                                                 0xea = 1.11.01010 = -0b1.01010 \times 2^1 = -2.625
0x2b = 0.01.01011 = +0b1.01011 \times 2^{-1} = 0.671875
                                                           0x6b = 0_11_01011 = +0b1.01011 \times 2^1 = 2.6875
                                                                                                                    0xab = 1.01.01011 = -0b1.01011 \times 2^{-1} = -0.671875
                                                                                                                                                                                0xeb = 1_11_01011 = -0b1.01011 \times 2^1 = -2.6875
0x2c = 0_01_01100 = +0b1.01100 \times 2^-1 = 0.6875
                                                           0x6c = 0_11_01100 = +0b1.01100 \times 2^1 = 2.75
                                                                                                                    0xac = 1_01_01100 = -0b1.01100 \times 2^-1 = -0.6875
                                                                                                                                                                                 0 \text{xec} = 1_11_01100 = -0b1.01100 \times 2^1 = -2.75
0x2d = 0_01_01101 = +0b1.01101 \times 2^-1 = 0.703125
                                                           0x6d = 0_11_01101 = +0b1.01101 \times 2^1 = 2.8125
                                                                                                                    0xad = 1_01_01101 = -0b1.01101 \times 2^-1 = -0.703125
                                                                                                                                                                                0xed = 1_11_01101 = -0b1.01101 \times 2^1 = -2.8125
0x2e = 0.01.01110 = +0b1.01110 \times 2^{-1} = 0.71875
                                                           0x6e = 0.11.01110 = +0b1.01110 \times 2^1 = 2.875
                                                                                                                    0xae = 1_01_01110 = -0b1.01110 \times 2^-1 = -0.71875
                                                                                                                                                                                0xee = 1.11.01110 = -0b1.01110 \times 2^1 = -2.875
0x2f = 0_01_01111 = +0b1.01111 \times 2^-1 = 0.734375
                                                           0x6f = 0_11_01111 = +0b1.01111 \times 2^1 = 2.9375
                                                                                                                    0xaf = 1.01.01111 = -0b1.01111 \times 2^{-1} = -0.734375
                                                                                                                                                                                0xef = 1.11.01111 = -0b1.01111 \times 2^1 = -2.9375
0x30 = 0.01.10000 = +0b1.10000 \times 2^{-1} = 0.75
                                                           0x70 = 0.11.10000 = +0b1.10000 \times 2^1 = 3.0
                                                                                                                    0xb0 = 1_01_10000 = -0b1.10000 \times 2^-1 = -0.75
                                                                                                                                                                                0xf0 = 1_11_10000 = -0b1.10000 \times 2^1 = -3.0
0x31 = 0_01_10001 = +0b1.10001 \times 2^-1 = 0.765625
                                                           0x71 = 0_11_10001 = +0b1.10001 \times 2^1 = 3.0625
                                                                                                                    0xb1 = 1_01_10001 = -0b1.10001 \times 2^-1 = -0.765625
                                                                                                                                                                                0xf1 = 1_11_10001 = -0b1.10001 \times 2^1 = -3.0625
0x32 = 0.01.10010 = +0b1.10010 \times 2^{-1} = 0.78125
                                                           0x72 = 0.11.10010 = +0b1.10010 \times 2^1 = 3.125
                                                                                                                    0xb2 = 1_01_10010 = -0b1.10010 \times 2^-1 = -0.78125
                                                                                                                                                                                0xf2 = 1.11.10010 = -0b1.10010 \times 2^1 = -3.125
0x33 = 0.01.10011 = +0b1.10011 \times 2^{-1} = 0.796875
                                                           0x73 = 0_11_10011 = +0b1.10011 \times 2^1 = 3.1875
                                                                                                                    0xb3 = 1_01_10011 = -0b1.10011 \times 2^-1 = -0.796875
                                                                                                                                                                                0xf3 = 1.11.10011 = -0b1.10011 \times 2^1 = -3.1875
0x34 = 0_01_10100 = +0b1.10100 \times 2^-1 = 0.8125
                                                           0x74 = 0_11_10100 = +0b1.10100 \times 2^1 = 3.25
                                                                                                                    0xb4 = 1_01_10100 = -0b1.10100 \times 2^{-1} = -0.8125
                                                                                                                                                                                 0xf4 = 1_11_10100 = -0b1.10100 \times 2^1 = -3.25
0x35 = 0.01.10101 = +0b1.10101 \times 2^{-1} = 0.828125
                                                           0x75 = 0.11.10101 = +0b1.10101 \times 2^{2} = 3.3125
                                                                                                                    0xb5 = 1_01_10101 = -0b1.10101 \times 2^{-1} = -0.828125
                                                                                                                                                                                0xf5 = 1.11.10101 = -0b1.10101 \times 2^1 = -3.3125
0x36 = 0.01.10110 = +0b1.10110 \times 2^{-1} = 0.84375
                                                           0x76 = 0.11.10110 = +0b1.10110 \times 2^1 = 3.375
                                                                                                                    0xb6 = 1.01.10110 = -0b1.10110 \times 2^{-1} = -0.84375
                                                                                                                                                                                0xf6 = 1_11_10110 = -0b1.10110 \times 2^1 = -3.375
0x37 = 0.01.10111 = +0b1.10111 \times 2^{-1} = 0.859375
                                                           0x77 = 0_11_10111 = +0b1.10111 \times 2^1 = 3.4375
                                                                                                                    0xb7 = 1.01.10111 = -0b1.10111 \times 2^{-1} = -0.859375
                                                                                                                                                                                0xf7 = 1.11.10111 = -0b1.10111 \times 2^1 = -3.4375
0x38 = 0_01_11000 = +0b1.11000 \times 2^-1 = 0.875
                                                           0x78 = 0_11_11000 = +0b1.11000 \times 2^1 = 3.5
                                                                                                                    0xb8 = 1_01_11000 = -0b1.11000 \times 2^{-1} = -0.875
                                                                                                                                                                                 0xf8 = 1_11_1000 = -0b1.11000 \times 2^1 = -3.5
0x39 = 0_01_11001 = +0b1.11001 \times 2^-1 = 0.890625
                                                           0x79 = 0_11_11001 = +0b1.11001 \times 2^1 = 3.5625
                                                                                                                    0xb9 = 1_01_11001 = -0b1.11001 \times 2^-1 = -0.890625
                                                                                                                                                                                0xf9 = 1_11_1001 = -0b1.11001 \times 2^1 = -3.5625
0x3a = 0.01.11010 = +0b1.11010 \times 2^-1 = 0.90625
                                                           0x7a = 0.11.11010 = +0b1.11010 \times 2^1 = 3.625
                                                                                                                    0xba = 1.01.11010 = -0b1.11010 \times 2^{-1} = -0.90625
                                                                                                                                                                                 0xfa = 1_11_1010 = -0b1.11010 \times 2^1 = -3.625
0x3b = 0_01_11011 = +0b1.11011 \times 2^-1 = 0.921875
                                                           0x7b = 0.11.11011 = +0b1.11011 \times 2^1 = 3.6875
                                                                                                                    0xbb = 1_01_11011 = -0b1.11011 \times 2^-1 = -0.921875
                                                                                                                                                                                0xfb = 1.11.11011 = -0b1.11011 \times 2^1 = -3.6875
                                                                                                                                                                                 0xfc = 1_11_11100 = -0b1.11100 \times 2^1 = -3.75
0x3c = 0_01_11100 = +0b1.11100 \times 2^-1 = 0.9375
                                                           0x7c = 0_11_11100 = +0b1.11100 \times 2^1 = 3.75
                                                                                                                    0xbc = 1_01_11100 = -0b1.11100 \times 2^-1 = -0.9375
0 \texttt{x3d} = 0\_01\_11101 = +0 \texttt{b1}.11101 \times 2 \hat{} -1 = 0.953125
                                                           0x7d = 0_11_11101 = +0b1.11101 \times 2^1 = 3.8125
                                                                                                                    0xbd = 1_01_11101 = -0b1.11101 \times 2^-1 = -0.953125
                                                                                                                                                                                0xfd = 1_11_11101 = -0b1.11101 \times 2^1 = -3.8125
0x3e = 0.01.11110 = +0b1.111110 \times 2^{-1} = 0.96875
                                                           0x7e = 0.11.11110 = +0b1.11110 \times 2^1 = 3.875
                                                                                                                    0xbe = 1_01_11110 = -0b1.11110 \times 2^-1 = -0.96875
                                                                                                                                                                                0xfe = 1.11.11110 = -0b1.11110 \times 2^1 = -3.875
0x3f = 0_01_111111 = +0b1.111111 \times 2^{-1} = 0.984375
                                                                                                                    0xbf = 1_01_11111 = -0b1.111111 \times 2^-1 = -0.984375
                                                          0x7f = 0_11_11111 = +Inf
                                                                                                                                                                                0xff = 1_11_11111 = -Inf
```

C.7 Value Table: P7, emin = 0, emax = 0 (linear)

```
0x40 = 0_1.000000 = +0b1.000000 \times 20 = 1.0
0x00 = 0_0000000 = 0.0
                                                                                                                            0x80 = 1_0_0000000 = NaN
                                                                                                                                                                                            0xc0 = 1_1000000 = -0b1.000000 \times 20 = -1.0
0x01 = 0_0000001 = +0b0.000001 \times 2^0 = 0.015625
                                                                                                                            0x81 = 1_0000001 = -0b0.000001 \times 2^{\circ}0 = -0.015625
                                                              0x41 = 0_1.000001 = +0b1.000001 \times 2^{\circ} = 1.015625
                                                                                                                                                                                           0xc1 = 1_1_000001 = -0b1.000001 \times 2^0 = -1.015625
0x02 = 0.0.000010 = +0b0.000010 \times 20 = 0.03125
                                                              0x42 = 0_{-1} - 000010 = +0b1.000010 \times 2^{\circ} = 1.03125
                                                                                                                            0x82 = 1_{-}0_{-}000010 = -0b0.000010 \times 2^{\circ}0 = -0.03125
                                                                                                                                                                                           0xc2 = 1_{-1} - 000010 = -0b1.000010 \times 2^{\circ}0 = -1.03125
0x03 = 0.0.000011 = +0b0.000011 \times 2^{\circ}0 = 0.046875
                                                              0x43 = 0_1.000011 = +0b1.000011 \times 2^{\circ} = 1.046875
                                                                                                                            0x83 = 1.0.000011 = -0b0.000011 \times 2^{\circ}0 = -0.046875
                                                                                                                                                                                           0xc3 = 1_1.000011 = -0b1.000011 \times 2^{\circ}0 = -1.046875
0x04 = 0_0000100 = +0b0.000100 \times 2^0 = 0.0625
                                                              0x44 = 0_1.000100 = +0b1.000100 \times 2^{\circ} = 1.0625
                                                                                                                            0x84 = 1_0.000100 = -0b0.000100 \times 2^0 = -0.0625
                                                                                                                                                                                           0xc4 = 1_1.000100 = -0b1.000100 \times 2^{\circ} = -1.0625
0x05 = 0_0000101 = +0b0.000101 \times 2^{\circ} = 0.078125
                                                                                                                            0x85 = 1_0000101 = -0b0.000101 \times 2^{\circ}0 = -0.078125
                                                              0x45 = 0_1.000101 = +0b1.000101 \times 2^{\circ} = 1.078125
                                                                                                                                                                                           0xc5 = 1_1_000101 = -0b1.000101 \times 2^{\circ} = -1.078125
0x06 = 0.0.000110 = +0b0.000110 \times 2^{\circ}0 = 0.09375
                                                              0x46 = 0_{-1}.000110 = +0b1.000110 \times 2^{\circ} = 1.09375
                                                                                                                            0x86 = 1.0.000110 = -0b0.000110 \times 2^{\circ}0 = -0.09375
                                                                                                                                                                                           0xc6 = 1_{-}1_{-}000110 = -0b1.000110 \times 2^{\circ}0 = -1.09375
0x07 = 0_0000111 = +0b0.000111 \times 2^0 = 0.109375
                                                              0x47 = 0_{-1}.000111 = +0b1.000111 \times 2^{\circ} = 1.109375
                                                                                                                            0x87 = 1.0.000111 = -0b0.000111 \times 2^{\circ} = -0.109375
                                                                                                                                                                                           0xc7 = 1_{-1}.000111 = -0b1.000111 \times 2^{\circ} = -1.109375
0x08 = 0_0001000 = +0b0.001000 \times 2^0 = 0.125
                                                                                                                            0x88 = 1.0.001000 = -0b0.001000 \times 2^{\circ} = -0.125
                                                              0x48 = 0_1.001000 = +0b1.001000 \times 2^{\circ} = 1.125
                                                                                                                                                                                           0xc8 = 1_1_001000 = -0b1.001000 \times 2^{\circ} = -1.125
0x09 = 0_0001001 = +0b0.001001 \times 2^{\circ} = 0.140625
                                                                                                                            0x89 = 1_0.001001 = -0b0.001001 \times 2^{\circ}0 = -0.140625
                                                              0x49 = 0_1.001001 = +0b1.001001 \times 2^{\circ} = 1.140625
                                                                                                                                                                                           0xc9 = 1_1_001001 = -0b1.001001 \times 2^{\circ} = -1.140625
0x0a = 0.0.001010 = +0b0.001010 \times 20 = 0.15625
                                                              0x4a = 0_{-1}.001010 = +0b1.001010 \times 2^{\circ}0 = 1.15625
                                                                                                                            0x8a = 1.0.001010 = -0b0.001010 \times 2^{\circ}0 = -0.15625
                                                                                                                                                                                           0xca = 1_{-1}.001010 = -0b1.001010 \times 2^{\circ}0 = -1.15625
0x0b = 0.0.001011 = +0b0.001011 \times 2^{\circ}0 = 0.171875
                                                              0x4b = 0_1.001011 = +0b1.001011 \times 2^{\circ}0 = 1.171875
                                                                                                                            0x8b = 1.0.001011 = -0b0.001011 \times 2^{\circ}0 = -0.171875
                                                                                                                                                                                           0xcb = 1_1_001011 = -0b1.001011 \times 2^{\circ} = -1.171875
0x0c = 0_0.001100 = +0b0.001100 \times 2^{\circ} = 0.1875
                                                              0x4c = 0_1.001100 = +0b1.001100 \times 2^{\circ} = 1.1875
                                                                                                                            0x8c = 1_0_001100 = -0b0.001100 \times 2^0 = -0.1875
                                                                                                                                                                                            0xcc = 1_{-1} - 001100 = -0b1.001100 \times 2^{\circ} = -1.1875
0x0d = 0_001101 = +0b0.001101 \times 20 = 0.203125
                                                              0x4d = 0_1.001101 = +0b1.001101 \times 2^0 = 1.203125
                                                                                                                            0x8d = 1_0.001101 = -0b0.001101 \times 2^{\circ} = -0.203125
                                                                                                                                                                                           0xcd = 1_1 - 001101 = -0b1.001101 \times 20 = -1.203125
0x0e = 0.0.001110 = +0b0.001110 \times 20 = 0.21875
                                                              0x4e = 0_{-1}.001110 = +0b1.001110 \times 2^{\circ} = 1.21875
                                                                                                                            0x8e = 1.0.001110 = -0b0.001110 \times 2^{\circ} = -0.21875
                                                                                                                                                                                           0xce = 1_{-1}_{-001110} = -0b1.001110 \times 2^{\circ}0 = -1.21875
0x0f = 0.0.001111 = +0b0.001111 \times 2^{\circ} = 0.234375
                                                              0x4f = 0.1.001111 = +0b1.001111 \times 2^{\circ} = 1.234375
                                                                                                                            0x8f = 1_0.001111 = -0b0.001111 \times 2^0 = -0.234375
                                                                                                                                                                                           0xcf = 1_1_001111 = -0b1.001111 \times 2^0 = -1.234375
0x10 = 0_0010000 = +0b0.010000 \times 2^0 = 0.25
                                                              0x50 = 0_1_010000 = +0b1.010000 \times 20 = 1.25
                                                                                                                            0x90 = 1_0_010000 = -0b0.010000 \times 2^0 = -0.25
                                                                                                                                                                                           0xd0 = 1_1_010000 = -0b1.010000 \times 2^0 = -1.25
0x11 = 0_0_010001 = +0b0.010001 \times 2^0 = 0.265625
                                                                                                                            0x91 = 1_0_010001 = -0b0.010001 \times 2^0 = -0.265625
                                                              0x51 = 0_1.010001 = +0b1.010001 \times 20 = 1.265625
                                                                                                                                                                                           0xd1 = 1_1010001 = -0b1.010001 \times 2^0 = -1.265625
0x12 = 0_0010010 = +0b0.010010 \times 20 = 0.28125
                                                              0x52 = 0_{-1}.010010 = +0b1.010010 \times 2^{\circ}0 = 1.28125
                                                                                                                            0x92 = 1.0.010010 = -0b0.010010 \times 2^{\circ}0 = -0.28125
                                                                                                                                                                                           0xd2 = 1_{-}1_{-}010010 = -0b1.010010 \times 2^{\circ}0 = -1.28125
0x13 = 0.0.010011 = +0b0.010011 \times 2^{\circ}0 = 0.296875
                                                              0x53 = 0_1.010011 = +0b1.010011 \times 2^{\circ} = 1.296875
                                                                                                                            0x93 = 1.0.010011 = -0b0.010011 \times 2^{\circ}0 = -0.296875
                                                                                                                                                                                           0xd3 = 1_1_010011 = -0b1.010011 \times 2^0 = -1.296875
0x14 = 0_00_010100 = +0b0.010100 \times 20 = 0.3125
                                                              0x54 = 0_1.010100 = +0b1.010100 \times 20 = 1.3125
                                                                                                                            0x94 = 1 \ 0 \ 010100 = -0b0.010100 \times 2^{\circ} = -0.3125
                                                                                                                                                                                            0xd4 = 1_1010100 = -0b1.010100 \times 2^{\circ}0 = -1.3125
0x15 = 0.0.010101 = +0b0.010101 \times 2^{\circ}0 = 0.328125
                                                              0x55 = 0_1.010101 = +0b1.010101 \times 2^{\circ}0 = 1.328125
                                                                                                                            0x95 = 1_0.010101 = -0b0.010101 \times 2^{\circ} = -0.328125
                                                                                                                                                                                           0xd5 = 1_1010101 = -0b1.010101 \times 20 = -1.328125
0x16 = 0.0.010110 = +0b0.010110 \times 20 = 0.34375
                                                              0x56 = 0_{-1} \cdot 010110 = +0b1.010110 \times 2^{\circ} = 1.34375
                                                                                                                            0x96 = 1.0.010110 = -0b0.010110 \times 2^{\circ}0 = -0.34375
                                                                                                                                                                                            0xd6 = 1_{-1} \cdot 010110 = -0b1.010110 \times 2^{\circ}0 = -1.34375
0x17 = 0.0.010111 = +0b0.010111 \times 20 = 0.359375
                                                                                                                            0x97 = 1.0.010111 = -0b0.010111 \times 2^{\circ} = -0.359375
                                                              0x57 = 0_1.010111 = +0b1.010111 \times 2^{\circ} = 1.359375
                                                                                                                                                                                           0xd7 = 1_1010111 = -0b1.010111 \times 2^{\circ} = -1.359375
0x18 = 0_0011000 = +0b0.011000 \times 2^0 = 0.375
                                                              0x58 = 0_1_011000 = +0b1.011000 \times 2^0 = 1.375
                                                                                                                            0x98 = 1_0_011000 = -0b0.011000 \times 2^0 = -0.375
                                                                                                                                                                                           0xd8 = 1_1_011000 = -0b1.011000 \times 2^{\circ} = -1.375
0x19 = 0_0011001 = +0b0.011001 \times 2^{\circ} = 0.390625
                                                              0x59 = 0_1_011001 = +0b1.011001 \times 2^0 = 1.390625
                                                                                                                            0x99 = 1_0_011001 = -0b0.011001 \times 2^0 = -0.390625
                                                                                                                                                                                           0xd9 = 1_1011001 = -0b1.011001 \times 2^{\circ} = -1.390625
0x1a = 0.0.011010 = +0b0.011010 \times 2^{\circ} = 0.40625
                                                              0x5a = 0_1.011010 = +0b1.011010 \times 2^{\circ} = 1.40625
                                                                                                                            0x9a = 1_0.011010 = -0b0.011010 \times 2^{\circ} = -0.40625
                                                                                                                                                                                           0xda = 1_1 - 011010 = -0b1.011010 \times 2^0 = -1.40625
0x1b = 0.0.011011 = +0b0.011011 \times 2^{\circ} = 0.421875
                                                              0x5b = 0_1.011011 = +0b1.011011 \times 2^{\circ} = 1.421875
                                                                                                                            0x9b = 1.0.011011 = -0b0.011011 \times 2^{\circ}0 = -0.421875
                                                                                                                                                                                           0xdb = 1_1011011 = -0b1.011011 \times 2^0 = -1.421875
                                                                                                                                                                                           0xdc = 1_1_011100 = -0b1.011100 \times 2^0 = -1.4375
0x1c = 0_00_111100 = +0b0.011100 \times 2^0 = 0.4375
                                                              0x5c = 0_1.011100 = +0b1.011100 \times 2^{\circ} = 1.4375
                                                                                                                            0x9c = 1_0_011100 = -0b0.011100 \times 2^{\circ} = -0.4375
                                                                                                                                                                                           0xdd = 1\_1\_011101 = -0b1.011101 \times 2 \ 0 = -1.453125
0x1d = 0_0011101 = +0b0.011101 \times 2^0 = 0.453125
                                                                                                                            0x9d = 1_0.011101 = -0b0.011101 \times 2^{\circ} = -0.453125
                                                              0x5d = 0_1.011101 = +0b1.011101 \times 2^{\circ} = 1.453125
0x1e = 0_0.011110 = +0b0.011110 \times 2^{\circ} = 0.46875
                                                              0x5e = 0_1.011110 = +0b1.011110 \times 2^{\circ} = 1.46875
                                                                                                                            0x9e = 1.0.011110 = -0b0.011110 \times 2^{\circ} = -0.46875
                                                                                                                                                                                           0xde = 1_{-}1_{-}011110 = -0b1.011110 \times 2^{\circ}0 = -1.46875
0x1f = 0.0.011111 = +0b0.0111111 \times 2^{\circ} = 0.484375
                                                                                                                            0x9f = 1.0.011111 = -0b0.011111 \times 2^{\circ} = -0.484375
                                                              0x5f = 0.1.011111 = +0b1.0111111 \times 2^{\circ} = 1.484375
                                                                                                                                                                                           0xdf = 1_1_011111 = -0b1.0111111 \times 2^{\circ} = -1.484375
0x20 = 0.0100000 = +0b0.100000 \times 2^{\circ} = 0.5
                                                              0x60 = 0_1100000 = +0b1.100000 \times 2^{\circ}0 = 1.5
                                                                                                                            0xa0 = 1_0100000 = -0b0.100000 \times 2^0 = -0.5
                                                                                                                                                                                            0xe0 = 1_1100000 = -0b1.100000 \times 2^{\circ} = -1.5
0x21 = 0_0100001 = +0b0.100001 \times 2^{\circ} = 0.515625
                                                              0x61 = 0_1100001 = +0b1.100001 \times 2^{\circ} = 1.515625
                                                                                                                            0xa1 = 1_0_100001 = -0b0.100001 \times 2^0 = -0.515625
                                                                                                                                                                                            0xe1 = 1_1100001 = -0b1.100001 \times 2^{\circ} = -1.515625
0x22 = 0.0.100010 = +0b0.100010 \times 2^{\circ}0 = 0.53125
                                                              0x62 = 0_{-1}100010 = +0b1.100010 \times 2^{\circ}0 = 1.53125
                                                                                                                            0xa2 = 1.0.100010 = -0b0.100010 \times 2^{\circ}0 = -0.53125
                                                                                                                                                                                            0xe2 = 1_1100010 = -0b1.100010 \times 2^{\circ}0 = -1.53125
0x23 = 0.0.100011 = +0b0.100011 \times 2^{\circ}0 = 0.546875
                                                              0x63 = 0_1100011 = +0b1.100011 \times 2^{\circ} = 1.546875
                                                                                                                            0xa3 = 1_0100011 = -0b0.100011 \times 2^0 = -0.546875
                                                                                                                                                                                           0xe3 = 1_1100011 = -0b1.100011 \times 20 = -1.546875
0x24 = 0_0100100 = +060.100100 \times 2^{\circ} = 0.5625
                                                              0x64 = 0_1100100 = +0b1.100100 \times 2^{\circ} = 1.5625
                                                                                                                            0xa4 = 1_0_100100 = -0b0.100100 \times 2^0 = -0.5625
                                                                                                                                                                                           0xe4 = 1_1100100 = -0b1.100100 \times 2^{\circ} = -1.5625
0x25 = 0_0100101 = +0b0.100101 \times 2^{\circ} = 0.578125
                                                              0x65 = 0_1100101 = +0b1.100101 \times 2^{\circ} = 1.578125
                                                                                                                            0xa5 = 1_0_100101 = -0b0.100101 \times 2^{\circ} = -0.578125
                                                                                                                                                                                           0xe5 = 1_1100101 = -0b1.100101 \times 2^{\circ} = -1.578125
                                                                                                                            0xa6 = 1.0.100110 = -0b0.100110 \times 2^{\circ} = -0.59375
0x26 = 0_0100110 = +0b0.100110 \times 2^{\circ} = 0.59375
                                                              0x66 = 0_{-1}100110 = +0b1.100110 \times 2^{\circ} = 1.59375
                                                                                                                                                                                           0xe6 = 1_{-}1_{-}100110 = -0b1.100110 \times 2^{\circ}0 = -1.59375
0x27 = 0_0100111 = +0b0.100111 \times 2^0 = 0.609375
                                                              0x67 = 0.1.100111 = +0b1.100111 \times 2^{\circ} = 1.609375
                                                                                                                            0xa7 = 1_0100111 = -0b0.100111 \times 2^0 = -0.609375
                                                                                                                                                                                           0xe7 = 1_1100111 = -0b1.100111 \times 2^{\circ} = -1.609375
0x28 = 0_0_101000 = +0b0.101000 \times 20 = 0.625
                                                              0x68 = 0_1101000 = +0b1.101000 \times 2^{\circ} = 1.625
                                                                                                                            0xa8 = 1.0.101000 = -0b0.101000 \times 2^{\circ} = -0.625
                                                                                                                                                                                           0xe8 = 1_1101000 = -0b1.101000 \times 2^{\circ} = -1.625
0\texttt{x29} = 0\_0\_101001 = +0\texttt{b}0.101001 \times 2 \\ \texttt{?0} = 0.640625
                                                              0 x 69 = 0\_1\_101001 = +0 b1.101001 \times 2 \ 0 = 1.640625
                                                                                                                            0xa9 = 1_0_101001 = -0b0.101001 \times 2^{\circ}0 = -0.640625
                                                                                                                                                                                           0xe9 = 1_1101001 = -0b1.101001 \times 2^{\circ}0 = -1.640625
0x2a = 0.0.101010 = +0b0.101010 \times 2^{\circ}0 = 0.65625
                                                              0x6a = 0_{-1}101010 = +0b1.101010 \times 2^{\circ}0 = 1.65625
                                                                                                                            0xaa = 1.0.101010 = -0b0.101010 \times 2^{\circ}0 = -0.65625
                                                                                                                                                                                            0xea = 1_1101010 = -0b1.101010 \times 20 = -1.65625
0x2b = 0.0.101011 = +0b0.101011 \times 2^{\circ}0 = 0.671875
                                                              0x6b = 0_1101011 = +0b1.101011 \times 2^{\circ}0 = 1.671875
                                                                                                                            0xab = 1_0 101011 = -0b0.101011 \times 2^{\circ} = -0.671875
                                                                                                                                                                                           0xeb = 1_11_01011 = -0b1_101011 \times 2^{\circ} = -1.671875
                                                                                                                            0xac = 1_0_101100 = -0b0.101100 \times 2^{\circ} = -0.6875
0x2c = 0_0101100 = +0b0.101100 \times 2^{\circ} = 0.6875
                                                              0x6c = 0_1101100 = +0b1.101100 \times 2^{\circ} = 1.6875
                                                                                                                                                                                            0xec = 1_1101100 = -0b1.101100 \times 2^{\circ} = -1.6875
0x2d = 0_0_101101 = +0b0.101101 \times 2^{\circ} = 0.703125
                                                              0x6d = 0_1101101 = +0b1.101101 \times 2^{\circ} = 1.703125
                                                                                                                            0xad = 1_0_101101 = -0b0.101101 \times 2^{\circ} = -0.703125
                                                                                                                                                                                           0xed = 1_1101101 = -0b1.101101 \times 2^{\circ} = -1.703125
0x2e = 0_0101110 = +0b0.101110 \times 2^{\circ} = 0.71875
                                                              0x6e = 0_{-1}101110 = +0b1.101110 \times 2^{\circ} = 1.71875
                                                                                                                            0xae = 1_0_101110 = -0b0.101110 \times 2^0 = -0.71875
                                                                                                                                                                                           0xee = 1_{-1}.101110 = -0b1.101110 \times 2^{\circ}0 = -1.71875
0x2f = 0_0101111 = +0b0.101111 \times 2^{\circ} = 0.734375
                                                              0x6f = 0_1.101111 = +0b1.1011111 \times 2^{\circ} = 1.734375
                                                                                                                            0xaf = 1_0 - 1011111 = -0b0.1011111 \times 2^0 = -0.734375
                                                                                                                                                                                           0xef = 1_11_011111 = -0b1.1011111 \times 2^{\circ}0 = -1.734375
0x30 = 0_0110000 = +0b0.110000 \times 2^{\circ} = 0.75
                                                                                                                            0xb0 = 1_0_110000 = -0b0.110000 \times 2^0 = -0.75
                                                              0x70 = 0_1110000 = +0b1.110000 \times 2^{\circ} = 1.75
                                                                                                                                                                                           0xf0 = 1_1110000 = -0b1.110000 \times 2^{\circ} = -1.75
0x31 = 0_0110001 = +0b0.110001 \times 2^{\circ} = 0.765625
                                                              0x71 = 0_1110001 = +0b1.110001 \times 20 = 1.765625
                                                                                                                            0xb1 = 1_0_110001 = -0b0.110001 \times 2^{\circ} = -0.765625
                                                                                                                                                                                           0xf1 = 1_110001 = -0b1.110001 \times 2^{\circ} = -1.765625
0x32 = 0_0110010 = +0b0.110010 \times 2^0 = 0.78125
                                                              0x72 = 0_{-1}10010 = +0b1.110010 \times 2^{\circ} = 1.78125
                                                                                                                            0xb2 = 1_0-110010 = -0b0.110010 \times 2^{\circ} = -0.78125
                                                                                                                                                                                           0xf2 = 1_{-1}10010 = -0b1.110010 \times 2^{\circ} = -1.78125
0x33 = 0_0110011 = +0b0.110011 \times 2^{\circ} = 0.796875
                                                              0x73 = 0_1110011 = +0b1.110011 \times 2^{\circ} = 1.796875
                                                                                                                            0xb3 = 1_0_110011 = -0b0.110011 \times 2^{\circ} = -0.796875
                                                                                                                                                                                           0xf3 = 1_110011 = -0b1.110011 \times 2^0 = -1.796875
0x34 = 0_0110100 = +0b0.110100 \times 2^{\circ} = 0.8125
                                                                                                                            0xb4 = 1_0_110100 = -0b0.110100 \times 2^{\circ} = -0.8125
                                                              0x74 = 0_1110100 = +0b1.110100 \times 2^{\circ} = 1.8125
                                                                                                                                                                                            0xf4 = 1_110100 = -0b1.110100 \times 2^{\circ} = -1.8125
0x35 = 0.0.110101 = +0b0.110101 \times 2^{\circ}0 = 0.828125
                                                              0x75 = 0_1110101 = +0b1.110101 \times 2^{\circ}0 = 1.828125
                                                                                                                            0xb5 = 1_0_110101 = -0b0.110101 \times 2^{\circ} = -0.828125
                                                                                                                                                                                           0xf5 = 1_110101 = -0b1.110101 \times 2^{\circ} = -1.828125
0x36 = 0.0.110110 = +0b0.110110 \times 20 = 0.84375
                                                              0x76 = 0_{-1}110110 = +0b1.110110 \times 2^{\circ} = 1.84375
                                                                                                                            0xb6 = 1_0_110110 = -0b0.110110 \times 2^{\circ} = -0.84375
                                                                                                                                                                                            0xf6 = 1_1110110 = -0b1.110110 \times 2^{\circ}0 = -1.84375
0x37 = 0.0.110111 = +0b0.110111 \times 2^{\circ} = 0.859375
                                                              0x77 = 0_1110111 = +0b1.110111 \times 2^{\circ} = 1.859375
                                                                                                                            0xb7 = 1_0_110111 = -0b0.110111 \times 2^{\circ} = -0.859375
                                                                                                                                                                                           0xf7 = 1_110111 = -0b1.110111 \times 2^{\circ} = -1.859375
0x38 = 0_0_111000 = +0b0.111000 \times 2^0 = 0.875
                                                              0x78 = 0_1111000 = +0b1.111000 \times 2^{\circ} = 1.875
                                                                                                                            0xb8 = 1_0_111000 = -0b0.111000 \times 2^0 = -0.875
                                                                                                                                                                                           0xf8 = 1_1111000 = -0b1.111000 \times 2^{\circ}0 = -1.875
0x39 = 0_0111001 = +0b0.111001 \times 2^{\circ} = 0.890625
                                                              0x79 = 0_1111001 = +0b1.111001 \times 2^{\circ} = 1.890625
                                                                                                                            0xb9 = 1_0_111001 = -0b0.111001 \times 2^{\circ} = -0.890625
                                                                                                                                                                                           0xf9 = 1_1111001 = -0b1.111001 \times 2^{\circ} = -1.890625
0x3a = 0.0.111010 = +0b0.111010 \times 2^{\circ} = 0.90625
                                                              0x7a = 0_1111010 = +0b1.111010 \times 2^{\circ} = 1.90625
                                                                                                                            0xba = 1_0.111010 = -0b0.111010 \times 2^{\circ} = -0.90625
                                                                                                                                                                                           0xfa = 1_1111010 = -0b1.111010 \times 2^{\circ} = -1.90625
0x3b = 0_0111011 = +0b0.111011 \times 2^0 = 0.921875
                                                              0x7b = 0_1111011 = +0b1.111011 \times 2^{\circ} = 1.921875
                                                                                                                            0xbb = 1_0_111011 = -0b0.111011 \times 2^{\circ} = -0.921875
                                                                                                                                                                                           0xfb = 1_1111011 = -0b1.111011 \times 2^{\circ}0 = -1.921875
0x3c = 0_0111100 = +0b0.111100 \times 2^{\circ} = 0.9375
                                                              0x7c = 0_1111100 = +0b1.1111100 \times 2^{\circ} = 1.9375
                                                                                                                            0xbc = 1_0_1111100 = -0b0.1111100 \times 2^0 = -0.9375
                                                                                                                                                                                           0xfc = 1_1111100 = -0b1.1111100 \times 2^{\circ}0 = -1.9375
0 \texttt{x3d} = 0\_0\_1111101 = +0 \texttt{b} 0.111101 \times 2 \texttt{?0} = 0.953125
                                                              0x7d = 0_1111101 = +0b1.111101 \times 2^{\circ} = 1.953125
                                                                                                                            0xbd = 1_0_1111101 = -0b0.1111101 \times 2^{\circ} = -0.953125
                                                                                                                                                                                           0xfd = 1_1111101 = -0b1.111101 \times 2^{\circ} = -1.953125
0x3e = 0_0.1111110 = +0b0.1111110 \times 20 = 0.96875
                                                                                                                                                                                           0 \texttt{xfe} = 1 \text{-} 1 \text{-} 1111110 = -0 \texttt{b} 1.1111110 \times 2 \text{``0} = -1.96875
                                                              0x7e = 0_11111110 = +0b1.1111110 \times 2^{\circ} = 1.96875
                                                                                                                            0xbe = 1.0.1111110 = -0b0.1111110 \times 2^{\circ}0 = -0.96875
0x3f = 0_01111111 = +0b0.1111111 \times 2^0 = 0.984375
                                                                                                                            0xbf = 1_0_1111111 = -0b0.1111111 \times 2^{\circ} = -0.984375
                                                              0x7f = 0_1_1111111 = +Inf
                                                                                                                                                                                           0xff = 1_11111111 = -Inf
```

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