Floating Point Formats for Machine Learning

IEEE Working Group P3109 interim report on 8-bit binary floating-point formats.

24 September 2023

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1. Introduction

This document represents the results of discussions and decisions made by IEEE working group P3109, "Standard for Arithmetic Formats for Machine Learning". The Project Authorization Request (PAR) for P3109 defines the scope, need, and stakeholders as follows:

Scope of proposed standard: This standard defines a binary arithmetic and data format for machine learning-optimized domains. It also specifies the default handling of exceptions occurring in this arithmetic. This standard provides a consistent and flexible arithmetic framework optimized for Machine Learning Systems (MLS) in hardware and/or software implementations to minimize the work required to make MLS interoperable with each other as well as other dependent systems. This standard is aligned with the IEEE Std 754-2019 for Floating-Point Arithmetic.

Need for the Project: Machine Learning Systems have different arithmetic requirements from most other domains. Precisions tend to be lower, and accuracy is measured in dimensions other than just numerical (e.g. inference accuracy). Furthermore, Machine Learning Systems often are integrated into mission-critical and safety-critical systems. With no standards specifically addressing these needs, Machine Learning Systems are built with inconsistent expectations and assumptions that hinder the compatibility and reuse of machine learning hardware, software, and training data.

Stakeholders for the Standard: System developers, vendors, and users of machine learning applications across many industries and interests including but not limited to compute, storage, medical, telecommunications, e-commerce, fleet-management, automotive, robotics, and security.

The scope of this interim release is interchange formats only. The working group continues to deliberate on the specification of operations.

2. Typographical conventions and notation

Bold text describes the decisions and specifications of this document.

Non-bold text is non-normative background material, typically providing rationale and arguments representing the discussions of the WG leading to a decision and specification.

This document specifies 8-bit floating-point interchange formats (binary formats) and associated operations. Binary formats are parameterized by their width, the number of bits spanned in memory (here, 8); and their precision (p), the number of bits spanned by the true significand (one more than the number of explicit "mantissa" bits).

The formats defined herein shall be referred to as "binary8" formats, and further parametrized by precision p yielding names "binary8p".

For example, "binary8p3" is a format with 3 bits of precision, hence a 2-bit mantissa and a 5-bit exponent field.

3. Values

This section describes the set of values that a binary8 format shall represent. The universe of values in existing floating point usage encompasses some finite real numerical values, the nonfinite numerical values positive and negative infinity (-Inf, +Inf), the non-numeric not-a-number values $(NaN, NaN_1, ...)$, and negative zero (-0). The value set for each binary8 format specifies the set of values that are available in that format.

Each binary format shall be associated with a unique encoding. An 8-bit binary encoding is a mapping from 8-bit strings to values. Some of these mappings are included as an Appendix.

The four special values (0, +Inf, -Inf, NaN) have encodings that are shared by all binary8 formats.

Value	Hexadecimal Encoding	Bit Sequence
Zero	0x00	0000 0000
Positive Infinity (+Inf)	0x7F	0111 1111
Negative Infinity (-Inf)	0xFF	1111 1111
Not a Number (NaN)	0x80	1000 0000

Table 1 – Encoding Special Values

The set of finite floating-point numbers representable with a binary format is determined by two parameters:

- Precision p, the number of digits in the significand including the implicit leading bit
- Maximum exponent *emax*, the exponent of the largest finite value

IEEE-754 2019 includes the radix b and emin in the list of format parameters. This document covers binary (radix 2) formats only. The parameter emin is determinable from other parameters, so is not a format-defining parameter.

P3109 formats shall define emax = $2^{8-p-1} - 1$. In IEEE-754, *emax* was consistently chosen across formats to be $2^{w-1} - 1$, where w is the exponent field width in bits. This choice has the consequence that the binary8pp value sets are subsets of the IEEE-754 binary16 value set for p > 2, and a near-symmetric distribution of values below and above the value 1.

Parameter	binary8p p	binary8p5	binary8p4	binary8p3	binary16	binary32	binary64
k, storage width in bits	8	8	8	8	16	32	64
p, precision in bits	р	5	4	3	11	24	53
emax, max exponent	$2^{8-p-1}-1$	3	7	15	15	127	1023
						1	
w, exponent field width	8 - p	3	4	5	5	8	11
bias, E - e	emax + 1	4	8	16	15	127	1023
sign bit	1	1	1	1	1	1	1
t, trailing significand field width in bits	p-1	4	3	2	10	23	52

Table 2 – Parameters for Binary Formats*

 $^{^{}st}$ Adapted from table 3.5 of IEEE-754 (2019), and extended to include proposed binary8 formats.

4. Subnormals

Binary8 value sets shall include subnormals.

The IEEE-754 value sets include subnormals. A value with trailing significand field m and exponent e is interpreted as $1.m \times 2^{e-b}$ except when all bits of the exponent bitfield are 0, in which case, the value is $0.m \times 2^{e-b+1}$.

When training models, it is common to represent near-zero values for gradients. Subnormal numbers induce equal quantization steps around zero; this expands the reach of binary8 trainable models. In statistical applications, the subnormal range is useful for uniform-like distributions, being uniform around zero. This also supports working with Gaussian-like distributions where numbers around zero are more probable.

5. Not a number (NaN)

Binary8 value sets shall include exactly one NaN, which shall not signal.

Other floating point formats define several NaN values, denoted (NaN, NaN1, ...). NaNs are returned from operations with results outside the set of values. For example, DIV(0,0), or ADD(Inf, -Inf). Multiple NaN encodings are used in other formats to allow different exceptional conditions to be distinguished.

In the context of machine learning systems, uses of NaN include:

- Debugging of code running on the accelerator. In Al accelerators, exceptions may be difficult or expensive
 to convey back to user code, so it is common practice to allow NaN values to propagate through calculations
 in order to indicate that an error has occurred.
- Usage as a "notable value" indicator. In some datasets, for example tabular data, values may be missing. It is useful to use a value outside of the normal numeric range to indicate the position of these values. Particularly where memory usage is a concern, as may be expected in float8 applications, the use of a separate "mask" array, or a list of indices, imposes an extra memory overhead. In some cases, an Inf can be used as a missing value, but given the restricted range of float8, it is likely that infinity shall be used as a separate indicator of "larger/smaller than +/- MaxFloat".
- The use of multiple NaN payloads is not unknown in statistical code (e.g. the R system has NaN and N/A), but it is not widely used, and in the context of float8, multiple NaNs imposes either additional hardware complexity (using only a subset of the significand range), or a large reduction in encoding space (e.g. 8 codes for E5, 16 codes for E4, 32 codes for E3).

6. Zero

Binary8 formats shall have exactly one zero. This zero value is non-negative.

The inclusion of negative zero would incur the cost of an additional code point. Given the decision to encode only a single NaN, placing that NaN at the negative zero code point enables the strictly positive and strictly negative number ranges to be symmetric.

A key rationale for inclusion of -0 in IEEE-754 was the consistent implementation of branch cuts in the atan2 function [Kahan 1987]. Although the atan function is common in deep learning, it is used as an activation function, rather than a trigonometric operation, and the atan2 function is not known in deep learning applications. Furthermore, it is not expected that this standard shall define either atan or atan2.

A secondary rationale for inclusion of -0 is the hardware simplification offered by its presence in the implementation of sign/magnitude arithmetic. However, the existence of in-market implementations is evidence that the small hardware simplification has not been sufficient to balance the loss of one code point.

It might be considered that the use of integer comparisons in sorting would argue against the placing of NaN at the negative zero code point. For example, the JAX machine learning framework is known to sort using integer comparison [link]. However such sorting still requires O(n) preprocessing and postprocessing steps to enable the use of twos-complement integer comparison, and already has special treatment of NaN and -0, so eliminating -0 and placing NaN in the -0 position imposes negligible additional burden. As an aside, it is noted that sorting using comparison operations, as typically defined, is undefined in presence of NaN, however the existing practice is to sort NaN (e.g. using totalOrder) to the end of the array, and this remains permitted, at no additional cost.

7. Infinities

Binary8 formats shall include positive and negative infinities.

This decision causes a reduction in dynamic range (252 values rather than 254), but offers improved numerical robustness in important machine learning use cases. Two generic classes of such usage are:

- mask values, for example, in Transformer models in machine learning, [ref].
- representation of overflow.

As illustrated in Appendix A, both usages are facilitated by the presence of infinity.

8. Extremal Values

It is practical to offer extremal finite values for supported 8-bit binary interchange formats. Following IEEE 754-2019 naming patterns, we adopt: maxNormal(T), minNormal(T), minSubnormal(T) where T is a binary8 format. For example: $maxNormal(binary8p4) == 7/4 * (2^7)$, $minNormal(binary8p5) == 1 / (2^3)$.

	maxNormal	minNormal	minSubnormal
binary8p3	3/2 * (2^15)	1/(2^15)	1/(2^17)
binary8p4	7/4 * (2^7)	1/(2^7)	1/(2^10)
binary8p5	15/8 * (2^3)	1/(2^3)	1/(2^7)
binary8p6	31/16 * (2^1)	1/(2^1)	1/(2^6)

Table 3: Extremal Values

9. Classification Operators

Conforming implementations shall provide these classification predicates and the classifier function. The classification predicates and the classifier function shall not signal exceptions.

predicate	Definition	predicate	definition
isZero	Iff x is 0	isNaN	Iff x is NaN
isInfinite	iff x is infinite	isFinite	Iff x is zero, subnormal or normal
isNormal	Iff x is normal	isSubnormal	Iff x is subnormal
isSignMinus	Iff x has a negative sign 1		
isCanonical	True ²	isSignaling	False ³

Table 4: Classification Predicates

The Classifier function

enum class(x)

NaN

Zero

positiveInfinity
positiveNormal
positiveSubnormal
negativeInfinity
negativeNormal
negativeNormal

end

10. Comparison Operators

Conforming implementations shall provide these comparison operators and the totalOrder(x, y) function.

Comparison operators are two argument predicates and their negations that return { True, False }. Comparisons shall not raise exceptions. Comparisons are either ordered or unordered. A comparison is unordered iff either argument is NaN. All other comparisons are ordered.

For $\{=, >, \ge, <, \le, \lessgtr\}$, if any argument is NaN the result is False. For $\{\ne, \ne, \ne, \notin, \nleq, \lessgtr\}$, if any argument is NaN the result is True. Otherwise, the result of a comparison shall match the mathematical result.

Table 5: Comparison Predicates and Negations

¹ is SignMinus(NaN) is True: all binary8 formats encode NaN as 0x80 (0b10000000).

²There are no non-canonical binary8 interchange formats.

³ All binary8 formats have one NaN; it does not signal.

math symbol	predicate true relations	math symbol	negation true relations
=	CompareEqual	≠, NOT =	CompareNotEqual
	equal		less than, greater than, unordered
>	CompareGreater	≯, NOT >	CompareNotGreater
	greater than		less than, equal, unordered
≥	CompareGreaterEqual	≱, NOT≥	CompareLessUnordered
	equal, greater than		less than, unordered
<	CompareLess	⊄, NOT <	CompareNotLess
	less than		greater than, equal, unordered
≤	CompareLessEqual	≰, NOT ≤	CompareGreaterUnordered
	less than, equal		greater than, unordered
≶	CompareOrdered	≸, NOT ≶	CompareUnordered
	less than, equal, greater than		unordered

The totalOrder predicate

totalOrder(x, y) provides a total ordering over each binary8 format's value set. It shall not raise any exceptions. totalOrder(x, y) shall return { True, False } in accord with the logic given below.

```
boolean totalOrder( x, y )
  if ! ( isNaN(x) || isNaN(y) )
    return compareLessEqual( x, y )
  else
    return isNaN( x )¹
  end
end
```

¹ All binary8 formats encode NaN as 0x80. The most significant bit is set, so, following 754, it is as -NaN.

Logical operations used within totalOrder()

```
! is the logical negation operator: !true == false, !false == true. | | is the short-circuiting, left-associative logical OR. - if a is true, a | | b returns true without evaluating b. - if a evaluates as false, a | | b returns the evaluation of b.
```

-(a||b||c) evaluates as (a||b)||c.

Appendix A: Numerical Examples

Mask Values

A common use for ∞ is to create masks, for example, in Transformer models in machine learning, [ref]. These values, assembled in mask matrix M with values $M_{ij} \in \{0, -\infty\}$ are typically be added to computed values A, in a computation such as:

$$\log \left(\operatorname{sum} \left(\exp \left(\tau * (A + M) \right) \right) \right)$$

where τ is a "temperature" or "base" parameter [ref]. This calculation depends on the property that $\exp(\tau*A_{ij}-\infty)=0$. It is clear that where M_{ij} is a large float (e.g. 480), then $\exp(-480)$ is an extremely small number, clearly much closer to zero than to any other value. However, careful implementations do not execute the calculation as written, and instead fuse the $\log(\sup(\exp(v)))$ operation into a single operation $\log \exp(v)$, whose implementation makes use of the identity

$$logsumexp(v) = logsumexp(v - max(v)) + max(v)$$

Without the "sticky" properties of Inf, this would produce incorrect answers. For example, in a format where MaxFloat=224 without Inf, and MaxFloat=240 with Inf:

$$logsumexp(\tau * [-224, -\infty]) \rightarrow logsumexp(\tau * [0, -\infty])$$

while

$$logsumexp(\tau * [-224, -240]) \rightarrow logsumexp(\tau * [0, -16])$$

If $\tau=1$ and all calculations are done in 8-bit floating point, then the answer will be the same, as $\exp(-16)=0$, but if τ is small, or calculations are done in mixed precision, as is common with 8-bit floating point, the loss of "stickiness" shall silently yield unexpected answers. It is not expected that the full calculation shall be done in 8-bit floating point, but the subtraction of the maximum value (and computation of the maximum) might reasonably be in 8-bit floating point.

Overflow to Infinity

A second use of infinity is to indicate overflow on conversion to the binary8 type. Existing implementations offer several behaviours on overflow: overflow to infinity, saturation to MaxFloat, and overflow to NaN. The existence of a code point for infinity allows any of these options to be implemented in a given instantiation, while removing the code point removes the possibility of implementing the first.

Appendix B: Value Tables

Value tables mapping 8-bit strings to value sets are provided in this section.

A typical entry is of the form:

```
HEX BINARY = BINARY_FLOAT = DECIMAL
0x01 0_00000_01 = +0b0.01*2^-15 = 7.62939453125e-06
```

Where the fields are interpreted as follows:

HEX	Hexadecimal encoding of the code point
BINARY	Binary expansion of the code point, with underscores separating sign_exponent_significand
BINARY_FLOAT	The precise float value as a binary fraction followed by 2^e with decimal exponent e
DECIMAL	The decimal expansion of the value

Value table: binary8p3

```
0 \times 00 = 0 \ 00000 \ 00 = +0 \times 0.00 \times 2^{-15} = 0
                                                        0x40 = 0 \ 10000 \ 00 = +0b1.00*2^0 = 1
                                                                                                                                                               0xc0 = 1\ 10000\ 00 = -0b1.00*2^0 = -1
0x01 = 0\ 00000\ 01 = +0b0.01*2^-15 = 7.62939e-06
                                                        0x41 = 0 \ 10000 \ 01 = +0b1.01*2^0 = 1.25
                                                                                                                                                                0xc1 = 1 10000 01 = -0b1.01*2^0 = -1.25
                                                                                                        0x81 = 1 00000 01 = -0b0.01*2^{-15} = -7.62939e-06
0x02 = 0 00000 10 = +0b0.10*2^-15 = 1.52588e-05
                                                        0x42 = 0 \ 10000 \ 10 = +0b1.10*2^0 = 1.5
                                                                                                        0x82 = 1 00000 10 = -0b0.10*2^-15 = -1.52588e-05
                                                                                                                                                                0xc2 = 1 10000 10 = -0b1.10*2^0 = -1.5
0x03 = 0 \ 00000 \ 11 = +0b0.11*2^-15 = 2.28882e-05
                                                                                                        0x83 = 1 \ 00000 \ 11 = -0b0.11*2^-15 = -2.28882e-05
                                                        0x43 = 0 \ 10000 \ 11 = +0b1.11*2^0 = 1.75
                                                                                                                                                                0xc3 = 1 10000 11 = -0b1.11*2^0 = -1.75
0x04 = 0\ 00001\ 00 = +0b1.00*2^-15 = 3.05176e-05
                                                        0x44 = 0 \ 10001 \ 00 = +0b1.00*2^1 = 2
                                                                                                        0x84 = 1 00001 00 = -0b1.00*2^-15 = -3.05176e-05
                                                                                                                                                                0xc4 = 1 10001 00 = -0b1.00*2^1 = -2
0x05 = 0\ 00001\ 01 = +0b1.01*2^-15 = 3.8147e-05
                                                                                                        0x85 = 1 00001 01 = -0b1.01*2^-15 = -3.8147e-05
                                                                                                                                                                0xc5 = 1 \ 10001 \ 01 = -0b1.01*2^1 = -2.5
                                                        0x45 = 0 \ 10001 \ 01 = +0b1.01*2^1 = 2.5
                                                                                                       0x86 = 1 00001 10 = -0b1.10*2^-15 = -4.57764e-05
                                                                                                                                                                0xc6 = 1 \ 10001 \ 10 = -0b1.10*2^1 = -3
0x06 = 0 \ 00001 \ 10 = +0b1.10*2^-15 = 4.57764e-05
                                                        0x46 = 0 \ 10001 \ 10 = +0b1.10*2^1 = 3
0x07 = 0 \ 00001 \ 11 = +0b1.11*2^-15 = 5.34058e-05
                                                        0x47 = 0 \ 10001 \ 11 = +0b1.11*2^1 = 3.5
                                                                                                        0x87 = 1 00001 11 = -0b1.11*2^-15 = -5.34058e-05
                                                                                                                                                                0xc7 = 1 \ 10001 \ 11 = -0b1.11*2^1 = -3.5
                                                                                                        0x88 = 1_00010_00 = -0b1.00*2^-14 = -6.10352e-05
                                                                                                                                                                0xc8 = 1_10010_00 = -0b1.00*2^2 = -4
0x08 = 0 \ 00010 \ 00 = +0b1.00*2^-14 = 6.10352e-05
                                                        0x48 = 0 \ 10010 \ 00 = +0b1.00*2^2 = 4
0x09 = 0_00010_01 = +0b1.01*2^-14 = 7.62939e-05
                                                                                                        0x89 = 1_00010_01 = -0b1.01*2^-14 = -7.62939e-05
                                                        0x49 = 0 \ 10010 \ 01 = +0b1.01*2^2 = 5
                                                                                                                                                                0xc9 = 1 \ 10010 \ 01 = -0b1.01*2^2 = -5
0x0a = 0_00010_10 = +0b1.10*2^-14 = 9.15527e-05
                                                        0x4a = 0 \ 10010 \ 10 = +0b1.10*2^2 = 6
                                                                                                        0x8a = 1_00010_10 = -0b1.10*2^-14 = -9.15527e-05
                                                                                                                                                                )xca = 1_10010_10 = -0b1.10*2^2 = -6
0x0b = 0_00010_11 = +0b1.11*2^-14 = 0.000106812
                                                        0x4b = 0 \ 10010 \ 11 = +0b1.11*2^2 = 7
                                                                                                        0x8b = 1_00010_11 = -0b1.11*2^-14 = -0.000106812
                                                                                                                                                                x = 1_{10010_{11} = -0b1.11 \times 2^2 = -7}
0 \times 0 = 0_{00011_{00}} = +0 \cdot 1.00 \times 2^{-13} = 0.00012207
                                                        0x4c = 0_10011_00 = +0b1.00*2^3 = 8
                                                                                                        0x8c = 1_00011_00 = -0b1.00*2^-13 = -0.00012207
                                                                                                                                                                0 \times 0 = 1_{0011_{00}} = -0b1.00 \times 2^3 = -8
0x0d = 0_00011_01 = +0b1.01*2^-13 = 0.000152588
                                                        0x4d = 0_10011_01 = +0b1.01*2^3 = 10
                                                                                                        0x8d = 1_{00011_01} = -0b1.01*2^{-13} = -0.000152588
                                                                                                                                                                ext{xcd} = 1_10011_01 = -0b1.01*2^3 = -10
                                                                                                                                                                )xce = 1_10011_10 = -0b1.10*2^3 = -12
0x0e = 0_00011_10 = +0b1.10*2^-13 = 0.000183105
                                                        0x4e = 0_10011_10 = +0b1.10*2^3 = 12
                                                                                                        0x8e = 1_00011_10 = -0b1.10*2^-13 = -0.000183105
0x0f = 0_00011_11 = +0b1.11*2^-13 = 0.000213623
                                                        0x4f = 0_10011_11 = +0b1.11*2^3 = 14
                                                                                                        0x8f = 1_00011_11 = -0b1.11*2^-13 = -0.000213623
                                                                                                                                                                ext{xcf} = 1_10011_11 = -0b1.11*2^3 = -14
0 \times 10 = 0 \ 00100 \ 00 = +0b1.00 \times 2^{-12} = 0.000244141
                                                        0x50 = 0 \ 10100 \ 00 = +0b1.00*2^4 = 16
                                                                                                        0 \times 90 = 1 \ 00100 \ 00 = -0b1.00 \times 2^{-12} = -0.000244141
                                                                                                                                                                0xd0 = 1 \ 10100 \ 00 = -0b1.00*2^4 = -16
0x11 = 0_00100_01 = +0b1.01*2^-12 = 0.000305176
                                                        0x51 = 0_10100_01 = +0b1.01*2^4 = 20
                                                                                                        0x91 = 1_00100_01 = -0b1.01*2^-12 = -0.000305176
                                                                                                                                                                0xd1 = 1_10100_01 = -0b1.01*2^4 = -20
0x12 = 0_00100_10 = +0b1.10*2^-12 = 0.000366211
                                                        0x52 = 0_10100_10 = +0b1.10*2^4 = 24
                                                                                                       0 \times 92 = 1_{00100_{10} = -0b1.10 \times 2^{-12} = -0.000366211}
                                                                                                                                                                xd2 = 1_10100_10 = -0b1.10*2^4 = -24
0x13 = 0_00100_11 = +0b1.11*2^-12 = 0.000427246
                                                        0x53 = 0_10100_11 = +0b1.11*2^4 = 28
                                                                                                        0 \times 93 = 1_00100_11 = -0b1.11 \times 2^{-12} = -0.000427246
                                                                                                                                                                0xd3 = 1_10100_11 = -0b1.11*2^4 = -28
0x14 = 0_00101_00 = +0b1.00*2^-11 = 0.000488281
                                                        0x54 = 0 \ 10101 \ 00 = +0b1.00*2^5 = 32
                                                                                                        0x94 = 1_00101_00 = -0b1.00*2^-11 = -0.000488281
                                                                                                                                                                0xd4 = 1_10101_00 = -0b1.00*2^5 = -32
0x15 = 0_00101_01 = +0b1.01*2^-11 = 0.000610352
                                                        0x55 = 0_10101_01 = +0b1.01*2^5 = 40
                                                                                                        0x95 = 1_00101_01 = -0b1.01*2^-11 = -0.000610352
                                                                                                                                                                xd5 = 1_10101_01 = -0b1.01*2^5 = -40
0 \times 16 = 0_00101_10 = +0b1.10 \times 2^{-11} = 0.000732422
                                                        0x56 = 0_10101_10 = +0b1.10*2^5 = 48
                                                                                                        0x96 = 1_00101_10 = -0b1.10*2^-11 = -0.000732422
                                                                                                                                                                0xd6 = 1_10101_10 = -0b1.10*2^5 = -48
0x17 = 0_00101_11 = +0b1.11*2^-11 = 0.000854492
                                                        0x57 = 0_10101_11 = +0b1.11*2^5 = 56
                                                                                                        0 \times 97 = 1_00101_11 = -0b1.11 \times 2^{-11} = -0.000854492
                                                                                                                                                                xd7 = 1_10101_11 = -0b1.11*2^5 = -56
0x18 = 0_00110_00 = +0b1.00*2^-10 = 0.000976562
                                                        0x58 = 0_10110_00 = +0b1.00*2^6 = 64
                                                                                                        0x98 = 1_00110_00 = -0b1.00*2^-10 = -0.000976562
                                                                                                                                                                xd8 = 1_10110_00 = -0b1.00*2^6 = -64
0x19 = 0_00110_01 = +0b1.01*2^-10 = 0.0012207
                                                        0x59 = 0_10110_01 = +0b1.01*2^6 = 80
                                                                                                        0x99 = 1_00110_01 = -0b1.01*2^-10 = -0.0012207
                                                                                                                                                                xd9 = 1_10110_01 = -0b1.01*2^6 = -80
0x1a = 0_00110_10 = +0b1.10*2^-10 = 0.00146484
                                                        0x5a = 0_10110_10 = +0b1.10*2^6 = 96
                                                                                                        0x9a = 1_00110_10 = -0b1.10*2^-10 = -0.00146484
                                                                                                                                                                xda = 1_10110_10 = -0b1.10*2^6 = -96
                                                                                                        0x9b = 1_00110_11 = -0b1.11*2^-10 = -0.00170898
0 \times 1b = 0_00110_11 = +0b1.11 \times 2^-10 = 0.00170898
                                                        0x5b = 0_10110_11 = +0b1.11*2^6 = 112
                                                                                                                                                                xdb = 1_10110_11 = -0b1.11*2^6 = -112
0 \times 1c = 0 \ 00111 \ 00 = +0b1.00 \times 2^{-9} = 0.00195312
                                                        0x5c = 0_10111_00 = +0b1.00*2^7 = 128
                                                                                                        0x9c = 1_00111_00 = -0b1.00*2^-9 = -0.00195312
                                                                                                                                                                xdc = 1_10111_00 = -0b1.00*2^7 = -128
                                                        0x5d = 0_10111_01 = +0b1.01*2^7 = 160
                                                                                                        0x9d = 1_00111_01 = -0b1.01*2^-9 = -0.00244141
                                                                                                                                                                0xdd = 1_{10111_01} = -0b1.01*2^7 = -160
0x1d = 0_00111_01 = +0b1.01*2^-9 = 0.00244141
                                                                                                        0x9e = 1_00111_10 = -0b1.10*2^-9 = -0.00292969
0 \times 1e = 0_{00111_{10} = +0b1.10 \times 2^{-9} = 0.00292969}
                                                        0x5e = 0_10111_10 = +0b1.10*2^7 = 192
                                                                                                                                                                xde = 1_10111_10 = -0b1.10*2^7 = -192
                                                        x5f = 0_10111_11 = +0b1.11*2^7 = 224
                                                                                                                                                                xdf = 1_10111_11 = -0b1.11*2^7 = -224
0x1f = 0_00111_11 = +0b1.11*2^-9 = 0.00341797
                                                                                                        x9f = 1_00111_11 = -0b1.11*2^-9 = -0.00341797
0x20 = 0_01000_00 = +0b1.00*2^-8 = 0.00390625
                                                        0 \times 60 = 0_11000_00 = +0b1.00 \times 2^8 = 256
                                                                                                        0xa0 = 1_01000_00 = -0b1.00*2^-8 = -0.00390625
                                                                                                                                                               0xe0 = 1_11000_00 = -0b1.00*2*8 = -256
0x21 = 0_01000_01 = +0b1.01*2^-8 = 0.00488281
                                                        0x61 = 0_11000_01 = +0b1.01*2^8 = 320
                                                                                                        0xa1 = 1_01000_01 = -0b1.01*2^-8 = -0.00488281
                                                                                                                                                               0xe1 = 1_11000_01 = -0b1.01*2^8 = -320
0x22 = 0 \ 01000 \ 10 = +0b1.10*2^-8 = 0.00585938
                                                        0x62 = 0_11000_10 = +0b1.10*2^8 = 384
                                                                                                        0xa2 = 1 01000 10 = -0b1.10*2^-8 = -0.00585938
                                                                                                                                                                xe2 = 1_11000_10 = -0b1.10*2^8 = -384
0x23 = 0_01000_11 = +0b1.11*2^-8 = 0.00683594
                                                        0x63 = 0_11000_11 = +0b1.11*2^8 = 448
                                                                                                        0xa3 = 1_01000_11 = -0b1.11*2^-8 = -0.00683594
                                                                                                                                                                xe3 = 1_11000_11 = -0b1.11*2^8 = -448
                                                                                                        0xa4 = 1_01001_00 = -0b1.00*2^-7 = -0.0078125
0x24 = 0 \ 01001 \ 00 = +0b1.00*2^-7 = 0.0078125
                                                        0x64 = 0_11001_00 = +0b1.00*2^9 = 512
                                                                                                                                                                xe4 = 1_11001_00 = -0b1.00*2^9 = -512
0x25 = 0_01001_01 = +0b1.01*2^-7 = 0.00976562
                                                        0x65 = 0_11001_01 = +0b1.01*2^9 = 640
                                                                                                        0xa5 = 1_01001_01 = -0b1.01*2^-7 = -0.00976562
                                                                                                                                                                xe5 = 1_11001_01 = -0b1.01*2^9 = -640
                                                                                                        0xa6 = 1_01001_10 = -0b1.10*2^-7 = -0.0117188
0x26 = 0 \ 01001 \ 10 = +0b1.10*2^-7 = 0.0117188
                                                        0x66 = 0_11001_10 = +0b1.10*2^9 = 768
                                                                                                                                                                xe6 = 1_11001_10 = -0b1.10*2^9 = -768
                                                                                                        0xa7 = 1_01001_11 = -0b1.11*2^-7 = -0.0136719
0x27 = 0_01001_11 = +0b1.11*2^-7 = 0.0136719
                                                        0x67 = 0_11001_11 = +0b1.11*2^9 = 896
                                                                                                                                                                0xe7 = 1 11001 11 = -0b1.11*2^9 = -896
0x28 = 0_01010_00 = +0b1.00*2^-6 = 0.015625
                                                                                                        )xa8 = 1_01010_00 = -0b1.00*2^-6 = -0.015625
                                                        0x68 = 0_11010_00 = +0b1.00*2^10 = 1024
                                                                                                                                                                0xe8 = 1 11010 00 = -0b1.00*2^10 = -1024
0x29 = 0 \ 01010 \ 01 = +0b1.01*2^-6 = 0.0195312
                                                        0x69 = 0 11010 01 = +0b1.01*2^10 = 1280
                                                                                                        0xa9 = 1_01010_01 = -0b1.01*2^-6 = -0.0195312
                                                                                                                                                                0xe9 = 1 11010 01 = -0b1.01*2^10 = -1280
0x2a = 0_01010_10 = +0b1.10*2^-6 = 0.0234375
                                                        0 \times 6a = 0_11010_10 = +0b1.10 \times 2^10 = 1536
                                                                                                         xaa = 1_01010_10 = -0b1.10*2^-6 = -0.0234375
                                                                                                                                                                xea = 1_11010_10 = -0b1.10*2^10 = -1536
                                                                                                        0xab = 1_01010_11 = -0b1.11*2^-6 = -0.0273438
0x2b = 0_01010_11 = +0b1.11*2^-6 = 0.0273438
                                                        0x6b = 0_11010_11 = +0b1.11*2^10 = 1792
                                                                                                                                                                xeb = 1_11010_11 = -0b1.11*2^10 = -1792
0x2c = 0_01011_00 = +0b1.00*2^-5 = 0.03125
                                                        0 \times 6c = 0_{11011_00} = +0b1.00 \times 2^{11} = 2048
                                                                                                         xac = 1_01011_00 = -0b1.00*2^-5 = -0.03125
                                                                                                                                                                xec = 1_11011_00 = -0b1.00*2^11 = -2048
                                                        0x6d = 0_11011_01 = +0b1.01*2^11 = 2560
                                                                                                        0xad = 1_01011_01 = -0b1.01*2^-5 = -0.0390625
                                                                                                                                                                xed = 1_11011_01 = -0b1.01*2^11 = -2560
0x2d = 0_01011_01 = +0b1.01*2^-5 = 0.0390625
0x2e = 0_01011_10 = +0b1.10*2^-5 = 0.046875
                                                        0x6e = 0_11011_10 = +0b1.10*2^11 = 3072
                                                                                                         xae = 1_01011_10 = -0b1.10*2^-5 = -0.046875
                                                                                                                                                                xee = 1_11011_10 = -0b1.10*2^11 = -3072
0x2f = 0_01011_11 = +0b1.11*2^-5 = 0.0546875
                                                        x6f = 0_11011_11 = +0b1.11*2^11 = 3584
                                                                                                        xaf = 1_01011_11 = -0b1.11*2^-5 = -0.0546875
                                                                                                                                                                xef = 1_11011_11 = -0b1.11*2^11 = -3584
0 \times 30 = 0_01100_00 = +0b1.00 \times 2^-4 = 0.0625
                                                        0x70 = 0_11100_00 = +0b1.00*2^12 = 4096
                                                                                                        0xb0 = 1_01100_00 = -0b1.00*2^-4 = -0.0625
                                                                                                                                                               0 \times f0 = 1_{11100_{00}} = -0b1.00 \times 2^{12} = -4096
0x31 = 0_01100_01 = +0b1.01*2^-4 = 0.078125
                                                        0 \times 71 = 0_11100_01 = +0b1.01 \times 2^12 = 5120
                                                                                                        0xb1 = 1_01100_01 = -0b1.01*2^-4 = -0.078125
                                                                                                                                                                xf1 = 1 \ 11100 \ 01 = -0b1.01*2^12 = -5120
0x32 = 0_01100_10 = +0b1.10*2^-4 = 0.09375
                                                        0x72 = 0_11100_10 = +0b1.10*2^12 = 6144
                                                                                                        0xb2 = 1_01100_10 = -0b1.10*2^-4 = -0.09375
                                                                                                                                                                xf2 = 1_11100_10 = -0b1.10*2^12 = -6144
0x33 = 0_01100_11 = +0b1.11*2^-4 = 0.109375
                                                        0 \times 73 = 0_{11100_{11}} = +0b1.11 \times 2^{12} = 7168
                                                                                                         xb3 = 1_01100_11 = -0b1.11*2^-4 = -0.109375
                                                                                                                                                                xf3 = 1_11100_11 = -0b1.11*2^12 = -7168
                                                        0x74 = 0_11101_00 = +0b1.00*2^13 = 8192
0x34 = 0_01101_00 = +0b1.00*2^-3 = 0.125
                                                                                                        0xb4 = 1_01101_00 = -0b1.00*2^-3 = -0.125
                                                                                                                                                                xf4 = 1_11101_00 = -0b1.00*2^13 = -8192
0x35 = 0_01101_01 = +0b1.01*2^-3 = 0.15625
                                                        x75 = 0_11101_01 = +0b1.01*2^13 = 10240
                                                                                                         xb5 = 1_01101_01 = -0b1.01*2^-3 = -0.15625
                                                                                                                                                                xf5 = 1_11101_01 = -0b1.01*2^13 = -10240
0x36 = 0_01101_10 = +0b1.10*2^-3 = 0.1875
                                                        0 \times 76 = 0_11101_10 = +0b1.10 \times 2^13 = 12288
                                                                                                        0xb6 = 1_01101_10 = -0b1.10*2^-3 = -0.1875
                                                                                                                                                                xf6 = 1_11101_10 = -0b1.10*2^13 = -12288
0x37 = 0_01101_11 = +0b1.11*2^-3 = 0.21875
                                                        0 \times 77 = 0_11101_11 = +0b1.11 \times 2^13 = 14336
                                                                                                        xb7 = 1_01101_11 = -0b1.11*2^-3 = -0.21875
                                                                                                                                                                xf7 = 1_11101_11 = -0b1.11*2^13 = -14336
0x38 = 0_01110_00 = +0b1.00*2^-2 = 0.25
                                                        0x78 = 0_11110_00 = +0b1.00*2^14 = 16384
                                                                                                        0xb8 = 1_01110_00 = -0b1.00*2^-2 = -0.25
                                                                                                                                                                xf8 = 1_11110_00 = -0b1.00*2^14 = -16384
                                                                                                        0x39 = 0_01110_01 = +0b1.01*2^-2 = 0.3125
                                                        0 \times 79 = 0_11110_01 = +0b1.01 \times 2^14 = 20480
                                                                                                                                                                0xf9 = 1_11110_01 = -0b1.01*2^14 = -20480
0x3a = 0_01110_10 = +0b1.10*2^-2 = 0.375
                                                        0x7a = 0_11110_10 = +0b1.10*2^14 = 24576
                                                                                                         xba = 1_01110_10 = -0b1.10*2^-2 = -0.375
                                                                                                                                                                xfa = 1_11110_10 = -0b1.10*2^14 = -24576
                                                                                                        )xbb = 1_01110_11 = -0b1.11*2^-2 = -0.4375
0x3b = 0_01110_11 = +0b1.11*2^-2 = 0.4375
                                                        0 \times 7b = 0_11110_11 = +0b1.11 \times 2^14 = 28672
                                                                                                                                                                xfb = 1_11110_11 = -0b1.11*2^14 = -28672
0x3c = 0_01111_00 = +0b1.00*2^-1 = 0.5
                                                        0x7c = 0_11111_00 = +0b1.00*2^15 = 32768
                                                                                                        0 \times bc = 1_01111_00 = -0b1.00 \times 2^-1 = -0.5
                                                                                                                                                                xfc = 1_11111_00 = -0b1.00*2^15 = -32768
                                                                                                        )xbd = 1_01111_01 = -0b1.01*2^-1 = -0.625
                                                                                                                                                                xfd = 1_11111_01 = -0b1.01*2^15 = -40960
0x3d = 0_01111_01 = +0b1.01*2^-1 = 0.625
                                                        0x7d = 0_11111_01 = +0b1.01*2^15 = 40960
0x3e = 0_01111_10 = +0b1.10*2^-1 = 0.75
                                                        0x7e = 0_11111_10 = +0b1.10*2^15 = 49152
                                                                                                        0xbe = 1_01111_10 = -0b1.10*2^{-1} = -0.75

0xbf = 1_01111_11 = -0b1.11*2^{-1} = -0.875
                                                                                                                                                               0xfe = 1_11111_10 = -0b1.10*2^15 = -49152
0x3f = 0_01111_11 = +0b1.11*2^-1 = 0.875
                                                        )x7f = 0_11111_11 = +Inf
                                                                                                                                                                0xff = 1_11111_11 = -Inf
```

Value table: binary8p4

```
0 \times 0.0 = 0.0000 \times 0.00 = +0.00 \times 0.00 \times 2^{-7} = 0.0000 \times 0.00000 \times 0.0000 \times 0.0000 \times 0.0000 \times 0.0000 \times 0.0000 \times 0.0000 \times 0.00000 \times 0.0000 \times 0.00000 \times 0.0000 \times 0.
                                                                   0x40 = 0.1000 000 = +0b1 000*2^0 = 1
                                                                                                                                  N80 = 1 0000 000 = NaN
                                                                                                                                                                                                        0xc0 = 1 1000 000 = -0b1 000*2^0 = -1
0 \times 01 = 0 \ 0000 \ 001 = +0b0.001 \times 2^{-7} = 0.000976562
                                                                   0x41 = 0 \ 1000 \ 001 = +0b1.001*2^0 = 1.125
                                                                                                                                 0x81 = 1 0000 001 = -0b0.001*2^-7 = -0.000976562
                                                                                                                                                                                                        0xc1 = 1 \ 1000 \ 001 = -0b1.001*2^0 = -1.125
0 \times 02 = 0 \ 0000 \ 010 = +0 \times 0.010 \times 2^{-7} = 0.00195312
                                                                   0x42 = 0\ 1000\ 010 = +0b1.010*2^0 = 1.25
                                                                                                                                 0x82 = 1 0000 010 = -0b0.010*2^-7 = -0.00195312
                                                                                                                                                                                                        0xc2 = 1 \ 1000 \ 010 = -0b1.010*2^0 = -1.25
                                                                                                                                 0x83 = 1_0000_011 = -0b0.011*2^-7 = -0.00292969
0 \times 03 = 0 \ 0000 \ 011 = +0 \times 0.011 \times 2^{-7} = 0.00292969
                                                                                                                                                                                                        0xc3 = 1 \ 1000 \ 011 = -0b1.011*2^0 = -1.375
                                                                   0x43 = 0 \ 1000 \ 011 = +0b1.011*2^0 = 1.375
                                                                                                                                 0x84 = 1 0000 100 = -0b0.100*2^-7 = -0.00390625
                                                                                                                                                                                                        0xc4 = 1\ 1000\ 100 = -0b1.100*2^0 = -1.5
0 \times 04 = 0 0000 100 = +0 \times 0.100 \times 2^{-7} = 0.00390625
                                                                   0x44 = 0\ 1000\ 100 = +0b1.100*2^0 = 1.5
0x05 = 0_0000_101 = +0b0.101*2^-7 = 0.00488281
                                                                                                                                 0x85 = 1_0000_101 = -0b0.101*2^-7 = -0.00488281
                                                                   0x45 = 0\ 1000\ 101 = +0b1.101*2^0 = 1.625
                                                                                                                                                                                                        0xc5 = 1 \ 1000 \ 101 = -0b1.101*2^0 = -1.625
0 \times 06 = 0 \ 0000 \ 110 = +0 \times 0.110 \times 2^{-7} = 0.00585938
                                                                                                                                 0x86 = 1 0000 110 = -0b0.110*2^-7 = -0.00585938
                                                                                                                                                                                                        0xc6 = 1 \ 1000 \ 110 = -0b1.110*2^0 = -1.75
                                                                   0x46 = 0 \ 1000 \ 110 = +0b1.110*2^0 = 1.75
0 \times 07 = 0_0000_111 = +0 \times 0.111 \times 2^-7 = 0.00683594
                                                                                                                                 0x87 = 1_0000_111 = -0b0.111*2^-7 = -0.00683594
                                                                                                                                                                                                        0xc7 = 1_1000_111 = -0b1.111*2^0 = -1.875
                                                                   0x47 = 0\ 1000\ 111 = +0b1.111*2^0 = 1.875
0 \times 08 = 0_0001_000 = +0b1.000 \times 2^-7 = 0.0078125
                                                                                                                                 0x88 = 1_0001_000 = -0b1.000*2^-7 = -0.0078125
                                                                                                                                                                                                        0xc8 = 1_1001_000 = -0b1.000*2^1 = -2
                                                                   0x48 = 0 \ 1001 \ 000 = +0b1.000*2^1 = 2
0x09 = 0_0001_001 = +0b1.001*2^-7 = 0.00878906
                                                                   0x49 = 0_1001_001 = +0b1.001*2^1 = 2.25
                                                                                                                                 0x89 = 1_0001_001 = -0b1.001*2^-7 = -0.00878906
                                                                                                                                                                                                        0xc9 = 1_1001_001 = -0b1.001*2^1 = -2.25
0x0a = 0_0001_010 = +0b1.010*2^-7 = 0.00976562
                                                                   0x4a = 0_1001_010 = +0b1.010*2^1 = 2.5
                                                                                                                                 0x8a = 1_0001_010 = -0b1.010*2^-7 = -0.00976562
                                                                                                                                                                                                        0xca = 1_1001_010 = -0b1.010*2^1 = -2.5
0 \times 0 = 0_{0001_{011}} = +0 \cdot 1.011 \times 2^{-7} = 0.0107422
                                                                   0x4b = 0_1001_011 = +0b1.011*2^1 = 2.75
                                                                                                                                 0x8b = 1_0001_011 = -0b1.011*2^-7 = -0.0107422
                                                                                                                                                                                                        0xcb = 1_1001_011 = -0b1.011*2^1 = -2.75
0 \times 0 = 0_{0001} = 0 = +0 \times 1.100 \times 2^{-7} = 0.0117188
                                                                   0x4c = 0_1001_100 = +0b1.100*2^1 = 3
                                                                                                                                 0x8c = 1_0001_100 = -0b1.100*2^-7 = -0.0117188
                                                                                                                                                                                                        0 \times cc = 1_{1001_{100}} = -0b1.100 \times 2^1 = -3
0x0d = 0_0001_101 = +0b1.101*2^-7 = 0.0126953
                                                                   0x4d = 0_1001_101 = +0b1.101*2^1 = 3.25
                                                                                                                                 0x8d = 1_0001_101 = -0b1.101*2^-7 = -0.0126953
                                                                                                                                                                                                        0xcd = 1_1001_101 = -0b1.101*2^1 = -3.25
                                                                                                                                 0x8e = 1_0001_110 = -0b1.110*2^-7 = -0.0136719
                                                                                                                                                                                                        0xce = 1_1001_110 = -0b1.110*2^1 = -3.5
0x0e = 0 0001 110 = +0b1.110*2^-7 = 0.0136719
                                                                   0x4e = 0 \ 1001 \ 110 = +0b1.110*2^1 = 3.5
0x0f = 0_0001_111 = +0b1.111*2^-7 = 0.0146484
                                                                   0x4f = 0_1001_111 = +0b1.111*2^1 = 3.75
                                                                                                                                 0x8f = 1_0001_111 = -0b1.111*2^-7 = -0.0146484
                                                                                                                                                                                                        0xcf = 1_1001_111 = -0b1.111*2^1 = -3.75
0 \times 10 = 0_0010_000 = +0b1.000 \times 2^-6 = 0.015625
                                                                                                                                 0x90 = 1_0010_000 = -0b1.000*2^-6 = -0.015625
                                                                                                                                                                                                        0xd0 = 1_1010_000 = -0b1.000*2^2 = -4
                                                                   0x50 = 0 \ 1010 \ 000 = +0b1.000*2^2 = 4
0x11 = 0_0010_001 = +0b1.001*2^-6 = 0.0175781
                                                                   0x51 = 0_1010_001 = +0b1.001*2^2 = 4.5
                                                                                                                                 0x91 = 1_0010_001 = -0b1.001*2^-6 = -0.0175781
                                                                                                                                                                                                        0xd1 = 1_1010_001 = -0b1.001*2^2 = -4.5
0x12 = 0_0010_010 = +0b1.010*2^-6 = 0.0195312
                                                                   0x52 = 0_1010_010 = +0b1.010*2^2 = 5
                                                                                                                                 0 \times 92 = 1_{0010_{010}} = -0 \times 1.010 \times 2^{-6} = -0.0195312
                                                                                                                                                                                                        0xd2 = 1_1010_010 = -0b1.010*2^2 = -5
0x13 = 0_0010_011 = +0b1.011*2^-6 = 0.0214844
                                                                   0x53 = 0_1010_011 = +0b1.011*2^2 = 5.5
                                                                                                                                 0x93 = 1_0010_011 = -0b1.011*2^-6 = -0.0214844
                                                                                                                                                                                                        0xd3 = 1_1010_011 = -0b1.011*2^2 = -5.5
0x14 = 0_0010_100 = +0b1.100*2^-6 = 0.0234375
                                                                   0x54 = 0_1010_100 = +0b1.100*2^2 = 6
                                                                                                                                 0x94 = 1_0010_100 = -0b1.100*2^-6 = -0.0234375
                                                                                                                                                                                                        0xd4 = 1_1010_100 = -0b1.100*2^2 = -6
0x15 = 0_0010_101 = +0b1.101*2^-6 = 0.0253906
                                                                   0x55 = 0_1010_101 = +0b1.101*2^2 = 6.5
                                                                                                                                 0x95 = 1_0010_101 = -0b1.101*2^-6 = -0.0253906
                                                                                                                                                                                                        0xd5 = 1_1010_101 = -0b1.101*2^2 = -6.5
0x16 = 0_0010_110 = +0b1.110*2^-6 = 0.0273438
                                                                   0x56 = 0_1010_110 = +0b1.110*2^2 = 7
                                                                                                                                 0x96 = 1_0010_110 = -0b1.110*2^-6 = -0.0273438
                                                                                                                                                                                                        0xd6 = 1_1010_110 = -0b1.110*2^2 = -7
0x17 = 0_0010_111 = +0b1.111*2^-6 = 0.0292969
                                                                   0x57 = 0_1010_111 = +0b1.111*2^2 = 7.5
                                                                                                                                 0x97 = 1_0010_111 = -0b1.111*2^-6 = -0.0292969
                                                                                                                                                                                                        0xd7 = 1_1010_111 = -0b1.111*2^2 = -7.5
0x18 = 0_0011_000 = +0b1.000*2^-5 = 0.03125
                                                                   0x58 = 0_1011_000 = +0b1.000*2^3 = 8
                                                                                                                                 0x98 = 1_0011_000 = -0b1.000*2^-5 = -0.03125
                                                                                                                                                                                                        0xd8 = 1_1011_000 = -0b1.000*2^3 = -8
0x19 = 0 0011 001 = +0b1.001*2^-5 = 0.0351562
                                                                   0x59 = 0_1011_001 = +0b1.001*2^3 = 9
                                                                                                                                 0x99 = 1 \ 0011 \ 001 = -0b1.001*2^{-5} = -0.0351562
                                                                                                                                                                                                         0xd9 = 1_1011_001 = -0b1.001*2^3 = -9
                                                                                                                                 0x9a = 1_0011_010 = -0b1.010*2^-5 = -0.0390625
                                                                                                                                                                                                        0xda = 1_1011_010 = -0b1.010*2^3 = -10
0x1a = 0 \ 0011 \ 010 = +0b1.010*2^-5 = 0.0390625
                                                                   0x5a = 0 \ 1011 \ 010 = +0b1.010*2^3 = 10
                                                                                                                                  0x9b = 1 0011 011 = -0b1.011*2^{-5} = -0.0429688
0x1b = 0 \ 0011 \ 011 = +0b1.011*2^-5 = 0.0429688
                                                                   0x5b = 0 \ 1011 \ 011 = +0b1.011*2^3 = 11
                                                                                                                                                                                                         0xdb = 1_1011_011 = -0b1.011*2^3 = -11
                                                                                                                                 0x9c = 1_0011_100 = -0b1.100*2^-5 = -0.046875
                                                                                                                                                                                                        0xdc = 1_1011_100 = -0b1.100*2^3 = -12
0x1c = 0 \ 0011 \ 100 = +0b1.100*2^{-5} = 0.046875
                                                                   0x5c = 0 \ 1011 \ 100 = +0b1.100*2^3 = 12
0x1d = 0_0011_101 = +0b1.101*2^-5 = 0.0507812
                                                                   0x5d = 0_1011_101 = +0b1.101*2^3 = 13
                                                                                                                                 0x9d = 1_0011_101 = -0b1.101*2^-5 = -0.0507812
                                                                                                                                                                                                         0xdd = 1_1011_101 = -0b1.101*2^3 = -13
0x1e = 0_0011_110 = +0b1.110*2^-5 = 0.0546875
                                                                   0x5e = 0_1011_110 = +0b1.110*2^3 = 14
                                                                                                                                 0x9e = 1_0011_110 = -0b1.110*2^-5 = -0.0546875
                                                                                                                                                                                                        0xde = 1_1011_110 = -0b1.110*2^3 = -14
0x1f = 0_0011_111 = +0b1.111*2^-5 = 0.0585938
                                                                   0x5f = 0_1011_111 = +0b1.111*2^3 = 15
                                                                                                                                 0x9f = 1_0011_111 = -0b1.111*2^-5 = -0.0585938
                                                                                                                                                                                                         0xdf = 1_1011_111 = -0b1.111*2^3 = -15
0x20 = 0 \ 0100 \ 000 = +0b1.000*2^-4 = 0.0625
                                                                   0 \times 60 = 0 \ 1100 \ 000 = +0 \times 1.000 \times 2^4 = 16
                                                                                                                                 0xa0 = 1 \ 0100 \ 000 = -0b1.000*2^{4} = -0.0625
                                                                                                                                                                                                        0xe0 = 1 \ 1100 \ 000 = -0b1.000*2^4 = -16
0x21 = 0 \ 0100 \ 001 = +0b1.001*2^-4 = 0.0703125
                                                                   0 \times 61 = 0 \ 1100 \ 001 = +0 \cdot 1.001 \times 2^4 = 18
                                                                                                                                 0xa1 = 1_0100_001 = -0b1.001*2^-4 = -0.0703125
                                                                                                                                                                                                        0xe1 = 1 \ 1100 \ 001 = -0b1.001*2^4 = -18
0x22 = 0 0100 010 = +0b1.010*2^-4 = 0.078125
                                                                   0x62 = 0 1100 010 = +0b1.010*2^4 = 20
                                                                                                                                 0xa2 = 1 0100 010 = -0b1.010*2^-4 = -0.078125
                                                                                                                                                                                                        0xe2 = 1 1100 010 = -0b1.010*2^4 = -20
0x23 = 0 \ 0100 \ 011 = +0b1.011*2^-4 = 0.0859375
                                                                   0x63 = 0_1100_011 = +0b1.011*2^4 = 22
                                                                                                                                 0xa3 = 1 \ 0100 \ 011 = -0b1.011*2^-4 = -0.0859375
                                                                                                                                                                                                        0xe3 = 1_1100_011 = -0b1.011*2^4 = -22
                                                                                                                                  0xa4 = 1_0100_100 = -0b1.100*2^-4 = -0.09375
                                                                                                                                                                                                        0xe4 = 1 \ 1100 \ 100 = -0b1.100*2^4 = -24
0x24 = 0 \ 0100 \ 100 = +0b1.100*2^-4 = 0.09375
                                                                   0 \times 64 = 0 \ 1100 \ 100 = +0b1.100 \times 2^4 = 24
                                                                                                                                 0xa5 = 1_0100_101 = -0b1.101*2^-4 = -0.101562
                                                                                                                                                                                                        0xe5 = 1_1100_101 = -0b1.101*2^4 = -26
0x25 = 0 \ 0100 \ 101 = +0b1.101*2^-4 = 0.101562
                                                                   0 \times 65 = 0 \ 1100 \ 101 = +0 \cdot 1.101 \times 2^4 = 26
0x26 = 0_0100_110 = +0b1.110*2^-4 = 0.109375
                                                                   0 \times 66 = 0_1100_110 = +0b1.110 \times 2^4 = 28
                                                                                                                                  0xa6 = 1_0100_110 = -0b1.110*2^-4 = -0.109375
                                                                                                                                                                                                        0xe6 = 1_1100_110 = -0b1.110*2^4 = -28
0x27 = 0 \ 0100 \ 111 = +0b1.111*2^-4 = 0.117188
                                                                   0 \times 67 = 0 \ 1100 \ 111 = +0 \cdot 1.111 \times 2^4 = 30
                                                                                                                                 0xa7 = 1_0100_111 = -0b1.111*2^-4 = -0.117188
                                                                                                                                                                                                        0xe7 = 1_1100_111 = -0b1.111*2^4 = -30
0x28 = 0_0101_000 = +0b1.000*2^-3 = 0.125
                                                                   0x68 = 0_1101_000 = +0b1.000*2^5 = 32
                                                                                                                                  0xa8 = 1_0101_000 = -0b1.000*2^-3 = -0.125
                                                                                                                                                                                                        0xe8 = 1_1101_000 = -0b1.000*2^5 = -32
0x29 = 0_0101_001 = +0b1.001*2^-3 = 0.140625
                                                                   0x69 = 0_1101_001 = +0b1.001*2^5 = 36
                                                                                                                                  0xa9 = 1_0101_001 = -0b1.001*2^-3 = -0.140625
                                                                                                                                                                                                         0xe9 = 1_1101_001 = -0b1.001*2^5 = -36
0x2a = 0_0101_010 = +0b1.010*2^-3 = 0.15625
                                                                   0x6a = 0_1101_010 = +0b1.010*2^5 = 40
                                                                                                                                  0xaa = 1_0101_010 = -0b1.010*2^-3 = -0.15625
                                                                                                                                                                                                        0xea = 1_1101_010 = -0b1.010*2^5 = -40
0x2b = 0_0101_011 = +0b1.011*2^-3 = 0.171875
                                                                   0 \times 6b = 0_{1101_{011}} = +0b1.011 \times 2^5 = 44
                                                                                                                                  0xab = 1_0101_011 = -0b1.011*2^-3 = -0.171875
                                                                                                                                                                                                        0xeb = 1_1101_011 = -0b1.011*2^5 = -44
0x2c = 0_0101_100 = +0b1.100*2^-3 = 0.1875
                                                                   0x6c = 0_1101_100 = +0b1.100*2^5 = 48
                                                                                                                                 0 \times ac = 1_0101_100 = -0b1.100 \times 2^{-3} = -0.1875
                                                                                                                                                                                                        0xec = 1_1101_100 = -0b1.100*2^5 = -48
0x2d = 0_0101_101 = +0b1.101*2^-3 = 0.203125
                                                                   0x6d = 0_1101_101 = +0b1.101*2^5 = 52
                                                                                                                                  0xad = 1_0101_101 = -0b1.101*2^-3 = -0.203125
                                                                                                                                                                                                        0xed = 1_1101_101 = -0b1.101*2^5 = -52
0x2e = 0 0101 110 = +0b1.110*2^{-3} = 0.21875
                                                                   0x6e = 0_1101_110 = +0b1.110*2^5 = 56
                                                                                                                                 0xae = 1 0101 110 = -0b1.110*2^-3 = -0.21875
                                                                                                                                                                                                        0xee = 1 1101 110 = -0b1.110*2^5 = -56
0x2f = 0_0101_111 = +0b1.111*2^-3 = 0.234375
                                                                   0x6f = 0_1101_111 = +0b1.111*2^5 = 60
                                                                                                                                  0xaf = 1_0101_111 = -0b1.111*2^-3 = -0.234375
                                                                                                                                                                                                        0xef = 1_1101_111 = -0b1.111*2^5 = -60
0x30 = 0 \ 0110 \ 000 = +0b1.000*2^-2 = 0.25
                                                                   0x70 = 0 1110 000 = +0b1.000*2^6 = 64
                                                                                                                                 0xb0 = 1 \ 0110 \ 000 = -0b1.000*2^-2 = -0.25
                                                                                                                                                                                                        0xf0 = 1 \ 1110 \ 000 = -0b1.000*2^6 = -64
0x31 = 0_0110_001 = +0b1.001*2^-2 = 0.28125
                                                                   0x71 = 0_1110_001 = +0b1.001*2^6 = 72
                                                                                                                                  0xb1 = 1_0110_001 = -0b1.001*2^-2 = -0.28125
                                                                                                                                                                                                        0xf1 = 1_1110_001 = -0b1.001*2^6 = -72
0x32 = 0_0110_010 = +0b1.010*2^-2 = 0.3125
                                                                   0x72 = 0_1110_010 = +0b1.010*2^6 = 80
                                                                                                                                  0xb2 = 1_0110_010 = -0b1.010*2^-2 = -0.3125
                                                                                                                                                                                                        0xf2 = 1_1110_010 = -0b1.010*2^6 = -80
0x33 = 0_0110_011 = +0b1.011*2^-2 = 0.34375
                                                                   0x73 = 0_1110_011 = +0b1.011*2^6 = 88
                                                                                                                                  0xb3 = 1_0110_011 = -0b1.011*2^-2 = -0.34375
                                                                                                                                                                                                        0xf3 = 1_1110_011 = -0b1.011*2^6 = -88
0x34 = 0_0110_100 = +0b1.100*2^-2 = 0.375
                                                                   0x74 = 0_1110_100 = +0b1.100*2^6 = 96
                                                                                                                                  xb4 = 1_0110_100 = -0b1.100*2^-2 = -0.375
                                                                                                                                                                                                        0xf4 = 1_1110_100 = -0b1.100*2^6 = -96
0x35 = 0_0110_101 = +0b1.101*2^-2 = 0.40625
                                                                   0x75 = 0_1110_101 = +0b1.101*2^6 = 104
                                                                                                                                  0xb5 = 1_0110_101 = -0b1.101*2^-2 = -0.40625
                                                                                                                                                                                                        0xf5 = 1_1110_101 = -0b1.101*2^6 = -104
0x36 = 0_0110_110 = +0b1.110*2^-2 = 0.4375
                                                                   0x76 = 0_1110_110 = +0b1.110*2^6 = 112
                                                                                                                                  0xb6 = 1_0110_110 = -0b1.110*2^-2 = -0.4375
                                                                                                                                                                                                        0xf6 = 1_1110_110 = -0b1.110*2^6 = -112
0x37 = 0_0110_111 = +0b1.111*2^-2 = 0.46875
                                                                   0x77 = 0_1110_111 = +0b1.111*2^6 = 120
                                                                                                                                 0xb7 = 1_0110_111 = -0b1.111*2^-2 = -0.46875
                                                                                                                                                                                                        0xf7 = 1_1110_111 = -0b1.111*2^6 = -120
0x38 = 0_0111_000 = +0b1.000*2^-1 = 0.5
                                                                   0x78 = 0_1111_000 = +0b1.000*2^7 = 128
                                                                                                                                 0xb8 = 1_0111_000 = -0b1.000*2^-1 = -0.5
                                                                                                                                                                                                        0xf8 = 1_1111_000 = -0b1.000*2^7 = -128
0x39 = 0 \ 0111 \ 001 = +0b1.001*2^-1 = 0.5625
                                                                   0x79 = 0_1111_001 = +0b1.001*2^7 = 144
                                                                                                                                 0xb9 = 1_0111_001 = -0b1.001*2^-1 = -0.5625
                                                                                                                                                                                                        0xf9 = 1_1111_001 = -0b1.001*2^7 = -144
0x3a = 0 \ 0111 \ 010 = +0b1.010*2^-1 = 0.625
                                                                   0x7a = 0_1111_010 = +0b1.010*2^7 = 160
                                                                                                                                  0xba = 1_0111_010 = -0b1.010*2^-1 = -0.625
                                                                                                                                                                                                        0xfa = 1_1111_010 = -0b1.010*2^7 = -160
                                                                   0x7b = 0_1111_011 = +0b1.011*2^7 = 176
0x3b = 0 \ 0111 \ 011 = +0b1.011*2^-1 = 0.6875
                                                                                                                                  0xbb = 1_0111_011 = -0b1.011*2^-1 = -0.6875
                                                                                                                                                                                                        0xfb = 1_1111_011 = -0b1.011*2^7 = -176
0x3c = 0 \ 0111 \ 100 = +0b1.100*2^{-1} = 0.75
                                                                   0x7c = 0_1111_100 = +0b1.100*2^7 = 192
                                                                                                                                 0xbc = 1 \ 0111 \ 100 = -0b1.100*2^{-1} = -0.75
                                                                                                                                                                                                        0xfc = 1_1111_100 = -0b1.100*2^7 = -192
                                                                                                                                  0xbd = 1_0111_101 = -0b1.101*2^-1 = -0.8125
0x3d = 0 \ 0111 \ 101 = +0b1.101*2^-1 = 0.8125
                                                                   0x7d = 0 1111 101 = +0b1.101*2^7 = 208
                                                                                                                                                                                                        0xfd = 1_1111_101 = -0b1.101*2^7 = -208
0x3e = 0 \ 0111 \ 110 = +0b1.110*2^-1 = 0.875
                                                                   0x7e = 0_1111_110 = +0b1.110*2^7 = 224
                                                                                                                                 0xbe = 1 \ 0111 \ 110 = -0b1.110*2^-1 = -0.875
                                                                                                                                                                                                        0xfe = 1_1111_110 = -0b1.110*2^7 = -224
                                                                                                                                 0xbf = 1_0111_111 = -0b1.111*2^-1 = -0.9375
0x3f = 0 0111 111 = +0b1.111*2^-1 = 0.9375
                                                                   0x7f = 0_1111_111 = +Inf
                                                                                                                                                                                                        0xff = 1_1111_111 = -Inf
```

Value table: binary8p5

```
0 \times 0.0 = 0.000 \ 0.000 = +0 \times 0.000 \times 2^{-3} = 0
                                                     0x40 = 0.100 0000 = +0b1 0000*2^0 = 1
                                                                                                                                                                0xc0 = 1 100 0000 = -0b1 0000*2^0 = -1
0x01 = 0_000_0001 = +0b0.0001*2^{-3} = 0.0078125
                                                     0x41 = 0 \ 100 \ 0001 = +0b1.0001*2^0 = 1.0625
                                                                                                           0x81 = 1_000_0001 = -0b0.0001*2^{-3} = -0.0078125
                                                                                                                                                                0xc1 = 1_100_0001 = -0b1.0001*2^0 = -1.0625
0x02 = 0_000_0010 = +0b0.0010*2^-3 = 0.015625
                                                     0x42 = 0_100_0010 = +0b1.0010*2^0 = 1.125
                                                                                                           0x82 = 1_000_0010 = -0b0.0010*2^-3 = -0.015625
                                                                                                                                                                0xc2 = 1_100_0010 = -0b1.0010*2^0 = -1.125
0 \times 03 = 0_000_0011 = +0b0.0011 \times 2^{-3} = 0.0234375
                                                     0x43 = 0_100_0011 = +0b1.0011*2^0 = 1.1875
                                                                                                           0x83 = 1_000_0011 = -0b0.0011*2^-3 = -0.0234375
                                                                                                                                                                0xc3 = 1_100_0011 = -0b1.0011*2^0 = -1.1875
                                                                                                                                                                0xc4 = 1_100_0100 = -0b1.0100*2^0 = -1.25
0x04 = 0_000_0100 = +0b0.0100*2^-3 = 0.03125
                                                     0x44 = 0_100_0100 = +0b1.0100*2^0 = 1.25
                                                                                                           0x84 = 1_000_0100 = -0b0.0100*2^-3 = -0.03125
                                                                                                           0x85 = 1_000_0101 = -0b0.0101*2^-3 = -0.0390625
0 \times 05 = 0 000 0101 = +0b0.0101*2^-3 = 0.0390625
                                                     0x45 = 0_100_0101 = +0b1.0101*2^0 = 1.3125
                                                                                                                                                                0xc5 = 1 100 0101 = -0b1.0101*2^0 = -1.3125
0 \times 06 = 0_000_0110 = +0b0.0110 \times 2^{-3} = 0.046875
                                                     0x46 = 0_100_0110 = +0b1.0110*2^0 = 1.375
                                                                                                           0x86 = 1_000_0110 = -0b0.0110*2^-3 = -0.046875
                                                                                                                                                                0xc6 = 1_{100_{110}} = -0b1.0110*2^0 = -1.375
0 \times 07 = 0.000 \ 0111 = +0 \times 0.0111 \times 2^{-3} = 0.0546875
                                                     0x47 = 0_100_0111 = +0b1.0111*2^0 = 1.4375
                                                                                                           0 \times 87 = 1_000_0111 = -0 \times 0.0111 \times 2^{-3} = -0.0546875
                                                                                                                                                                0xc7 = 1_100_0111 = -0b1.0111*2^0 = -1.4375
0 \times 08 = 0 000 1000 = +0b0.1000\times 2^{-3} = 0.0625
                                                     0x48 = 0_100_1000 = +0b1.1000*2^0 = 1.5
                                                                                                           0x88 = 1_000_1000 = -0b0.1000*2^-3 = -0.0625
                                                                                                                                                                0xc8 = 1_100_1000 = -0b1.1000*2^0 = -1.5
0 \times 09 = 0.000 \ 1001 = +0b0.1001 \times 2^{-3} = 0.0703125
                                                     0x49 = 0\ 100\ 1001 = +0b1.1001*2^0 = 1.5625
                                                                                                           0 \times 89 = 1 \ 000 \ 1001 = -0b0.1001 \times 2^{-3} = -0.0703125
                                                                                                                                                                0xc9 = 1 \ 100 \ 1001 = -0b1.1001*2^0 = -1.5625
0x0a = 0 000 1010 = +0b0.1010*2^{-3} = 0.078125
                                                     0x4a = 0 100 1010 = +0b1.1010*2^0 = 1.625
                                                                                                           0x8a = 1 000 1010 = -0b0.1010*2^{-3} = -0.078125
                                                                                                                                                                0xca = 1 100 1010 = -0b1.1010*2^0 = -1.625
0 \times 0 = 0 \ 000 \ 1011 = +0 \times 0.1011 \times 2^{-3} = 0.0859375
                                                     0x4b = 0 \ 100 \ 1011 = +0b1.1011*2^0 = 1.6875
                                                                                                            x8b = 1 000 1011 = -0b0.1011*2^{-3} = -0.0859375
                                                                                                                                                                0xcb = 1 100 1011 = -0b1.1011*2^0 = -1.6875
0x0c = 0\ 000\ 1100 = +0b0.1100*2^{-3} = 0.09375
                                                     0x4c = 0 100 1100 = +0b1.1100*2^0 = 1.75
                                                                                                            x8c = 1_000_1100 = -0b0.1100*2^-3 = -0.09375
                                                                                                                                                                0 \times cc = 1_{100_{1100}} = -0b1.1100 \times 2^0 = -1.75
                                                                                                                                                                0 \times cd = 1 \ 100 \ 1101 = -0b1.1101 \times 2^0 = -1.8125
0x0d = 0 000 1101 = +0b0.1101*2^{-3} = 0.101562
                                                     0x4d = 0 \ 100 \ 1101 = +0b1.1101*2^0 = 1.8125
                                                                                                           0x8d = 1 000 1101 = -0b0.1101 \times 2^{-3} = -0.101562
0 \times 0 = 0_000_1110 = +0 \times 0.1110 \times 2^{-3} = 0.109375
                                                     0x4e = 0_100_1110 = +0b1.1110*2^0 = 1.875
                                                                                                           0x8e = 1_000_1110 = -0b0.1110*2^-3 = -0.109375
                                                                                                                                                                0xce = 1_100_1110 = -0b1.1110*2^0 = -1.875
0x0f = 0 000 1111 = +0b0.1111 \times 2^{-3} = 0.117188
                                                     0x4f = 0 100 1111 = +0b1.1111*2^0 = 1.9375
                                                                                                            x8f = 1 000 1111 = -0b0.1111*2^{-3} = -0.117188
                                                                                                                                                                0xcf = 1 100 1111 = -0b1.1111*2^0 = -1.9375
0 \times 10 = 0_001_0000 = +0b1.0000 \times 2^{-3} = 0.125
                                                                                                           0 \times 90 = 1_001_0000 = -0b1.0000 \times 2^{-3} = -0.125
                                                                                                                                                                0xd0 = 1_101_0000 = -0b1.0000*2^1 = -2
                                                     0x50 = 0 \ 101 \ 0000 = +0b1.0000*2^1 = 2
0x11 = 0 \ 001 \ 0001 = +0b1.0001*2^{-3} = 0.132812
                                                     0x51 = 0 \ 101 \ 0001 = +0b1.0001*2^1 = 2.125
                                                                                                           0 \times 91 = 1_001_0001 = -0b1.0001 \times 2^{-3} = -0.132812
                                                                                                                                                                0xd1 = 1_101_0001 = -0b1.0001*2^1 = -2.125
0x12 = 0 \ 001 \ 0010 = +0b1.0010*2^{-3} = 0.140625
                                                     0x52 = 0 \ 101 \ 0010 = +0b1.0010*2^1 = 2.25
                                                                                                           0x92 = 1 001 0010 = -0b1.0010*2^{-3} = -0.140625
                                                                                                                                                                0xd2 = 1 \ 101 \ 0010 = -0b1.0010*2^1 = -2.25
0x13 = 0 \ 001 \ 0011 = +0b1.0011*2^{-3} = 0.148438
                                                     0x53 = 0 \ 101 \ 0011 = +0b1.0011*2^1 = 2.375
                                                                                                           0x93 = 1 \ 001 \ 0011 = -0b1.0011*2^{-3} = -0.148438
                                                                                                                                                                0xd3 = 1 \ 101 \ 0011 = -0b1.0011*2^1 = -2.375
0x14 = 0 \ 001 \ 0100 = +0b1.0100*2^{-3} = 0.15625
                                                     0x54 = 0 \ 101 \ 0100 = +0b1.0100*2^1 = 2.5
                                                                                                           0x94 = 1 001 0100 = -0b1.0100*2^{-3} = -0.15625
                                                                                                                                                                0xd4 = 1 \ 101 \ 0100 = -0b1.0100*2^1 = -2.5
                                                                                                                                                                0 \times d5 = 1_101_0101 = -0b1.0101 \times 2^1 = -2.625
0x15 = 0 \ 001 \ 0101 = +0b1.0101*2^{-3} = 0.164062
                                                     0x55 = 0 \ 101 \ 0101 = +0b1.0101*2^1 = 2.625
                                                                                                           0x95 = 1 \ 001 \ 0101 = -0b1.0101*2^{-3} = -0.164062
0x16 = 0 \ 001 \ 0110 = +0b1.0110*2^{-3} = 0.171875
                                                     0x56 = 0_101_0110 = +0b1.0110*2^1 = 2.75
                                                                                                           0x96 = 1 \ 001 \ 0110 = -0b1.0110*2^{-3} = -0.171875
                                                                                                                                                                0 \times d6 = 1_101_0110 = -0b1.0110 \times 2^1 = -2.75
0x17 = 0 \ 001 \ 0111 = +0b1.0111*2^{-3} = 0.179688
                                                     0x57 = 0_101_0111 = +0b1.0111*2^1 = 2.875
                                                                                                           0 \times 97 = 1_001_0111 = -0b1.0111 \times 2^{-3} = -0.179688
                                                                                                                                                                0 \times d7 = 1_101_0111 = -0b1.0111 \times 2^1 = -2.875
0x18 = 0_001_1000 = +0b1.1000*2^-3 = 0.1875
                                                     0x58 = 0_101_1000 = +0b1.1000*2^1 = 3
                                                                                                           0 \times 98 = 1_001_1000 = -0b1.1000 \times 2^{-3} = -0.1875
                                                                                                                                                                0xd8 = 1_101_1000 = -0b1.1000*2^1 = -3
0x19 = 0_001_1001 = +0b1.1001*2^-3 = 0.195312
                                                     0x59 = 0_101_1001 = +0b1.1001*2^1 = 3.125
                                                                                                           0x99 = 1_001_1001 = -0b1.1001*2^-3 = -0.195312
                                                                                                                                                                0xd9 = 1_101_1001 = -0b1.1001*2^1 = -3.125
0x1a = 0_001_1010 = +0b1.1010*2^-3 = 0.203125
                                                     0x5a = 0_101_1010 = +0b1.1010*2^1 = 3.25
                                                                                                           0x9a = 1_001_1010 = -0b1.1010*2^-3 = -0.203125
                                                                                                                                                                xda = 1_101_1010 = -0b1.1010*2^1 = -3.25
0x1b = 0_001_1011 = +0b1.1011*2^-3 = 0.210938
                                                     0x5b = 0_101_1011 = +0b1.1011*2^1 = 3.375
                                                                                                           0x9b = 1_001_1011 = -0b1.1011*2^-3 = -0.210938
                                                                                                                                                                0xdb = 1_101_1011 = -0b1.1011*2^1 = -3.375
0x1c = 0_001_1100 = +0b1.1100*2^{-3} = 0.21875
                                                     0x5c = 0_101_1100 = +0b1.1100*2^1 = 3.5
                                                                                                                                                                0xdc = 1_101_1100 = -0b1.1100*2^1 = -3.5
                                                                                                           0x9c = 1_001_1100 = -0b1.1100*2^-3 = -0.21875
0x1d = 0_001_1101 = +0b1.1101*2^-3 = 0.226562
                                                     0x5d = 0_101_1101 = +0b1.1101*2^1 = 3.625
                                                                                                           0x9d = 1_001_1101 = -0b1.1101*2^-3 = -0.226562
                                                                                                                                                                0xdd = 1_101_1101 = -0b1.1101*2^1 = -3.625
0 \times 1e = 0_001_1110 = +0b1.1110 \times 2^{-3} = 0.234375
                                                                                                           0x9e = 1_001_1110 = -0b1.1110*2^-3 = -0.234375
                                                     0x5e = 0_101_1110 = +0b1.1110*2^1 = 3.75
                                                                                                                                                                0xde = 1_101_1110 = -0b1.1110*2^1 = -3.75
0x1f = 0_001_1111 = +0b1.1111*2^-3 = 0.242188
                                                     0x5f = 0_101_1111 = +0b1.1111*2^1 = 3.875
                                                                                                           0x9f = 1_001_1111 = -0b1.1111*2^-3 = -0.242188
                                                                                                                                                                0xdf = 1_101_1111 = -0b1.1111*2^1 = -3.875
0x20 = 0 \ 010 \ 0000 = +0b1.0000*2^{-2} = 0.25
                                                     0 \times 60 = 0 \ 110 \ 0000 = +0b1.0000 \times 2^2 = 4
                                                                                                           0xa0 = 1 \ 010 \ 0000 = -0b1.0000*2^{-2} = -0.25
                                                                                                                                                                0xe0 = 1 \ 110 \ 0000 = -0b1.0000*2^2 = -4
0x21 = 0 \ 010 \ 0001 = +0b1.0001*2^-2 = 0.265625
                                                     0 \times 61 = 0 \ 110 \ 0001 = +0b1.0001 \times 2^2 = 4.25
                                                                                                           0xa1 = 1 \ 010 \ 0001 = -0b1.0001*2^{-2} = -0.265625
                                                                                                                                                                0xe1 = 1 \ 110 \ 0001 = -0b1.0001*2^2 = -4.25
0x22 = 0_010_0010 = +0b1.0010*2^-2 = 0.28125
                                                     0x62 = 0_110_0010 = +0b1.0010*2^2 = 4.5
                                                                                                           0xa2 = 1_010_0010 = -0b1.0010*2^-2 = -0.28125
                                                                                                                                                                0xe2 = 1_110_0010 = -0b1.0010*2^2 = -4.5
0x23 = 0_010_0011 = +0b1.0011*2^-2 = 0.296875
                                                     0x63 = 0_110_0011 = +0b1.0011*2^2 = 4.75
                                                                                                           0xa3 = 1_010_0011 = -0b1.0011*2^-2 = -0.296875
                                                                                                                                                                0xe3 = 1_110_0011 = -0b1.0011*2^2 = -4.75
0x24 = 0_010_0100 = +0b1.0100*2^-2 = 0.3125
                                                     0x64 = 0_110_0100 = +0b1.0100*2^2 = 5
                                                                                                           0xa4 = 1_010_0100 = -0b1.0100*2^-2 = -0.3125
                                                                                                                                                                0xe4 = 1_110_0100 = -0b1.0100*2^2 = -5
0x25 = 0_010_0101 = +0b1.0101*2^-2 = 0.328125
                                                     0x65 = 0_110_0101 = +0b1.0101*2^2 = 5.25
                                                                                                           )xa5 = 1_010_0101 = -0b1.0101*2^-2 = -0.328125
                                                                                                                                                                0xe5 = 1_110_0101 = -0b1.0101*2^2 = -5.25
0x26 = 0_010_0110 = +0b1.0110*2^-2 = 0.34375
                                                     0x66 = 0_110_0110 = +0b1.0110*2^2 = 5.5
                                                                                                           0xa6 = 1_010_0110 = -0b1.0110*2^-2 = -0.34375
                                                                                                                                                                0xe6 = 1_110_0110 = -0b1.0110*2^2 = -5.5
                                                                                                           0xa7 = 1_010_0111 = -0b1.0111*2^-2 = -0.359375
0x27 = 0_010_0111 = +0b1.0111*2^-2 = 0.359375
                                                     0x67 = 0_110_0111 = +0b1.0111*2^2 = 5.75
                                                                                                                                                                0xe7 = 1_110_0111 = -0b1.0111*2^2 = -5.75
0x28 = 0_010_1000 = +0b1.1000*2^-2 = 0.375
                                                     0x68 = 0_110_1000 = +0b1.1000*2^2 = 6
                                                                                                           0xa8 = 1_010_1000 = -0b1.1000*2^-2 = -0.375
                                                                                                                                                                0xe8 = 1_110_1000 = -0b1.1000*2^2 = -6
0x29 = 0_010_1001 = +0b1.1001*2^-2 = 0.390625
                                                     0x69 = 0_110_1001 = +0b1.1001*2^2 = 6.25
                                                                                                           0xa9 = 1_010_1001 = -0b1.1001*2^-2 = -0.390625
                                                                                                                                                                0xe9 = 1_110_1001 = -0b1.1001*2^2 = -6.25
0x2a = 0_010_1010 = +0b1.1010*2^-2 = 0.40625
                                                     0x6a = 0_110_1010 = +0b1.1010*2^2 = 6.5
                                                                                                           )xaa = 1_010_1010 = -0b1.1010*2^-2 = -0.40625
                                                                                                                                                                0xea = 1_110_1010 = -0b1.1010*2^2 = -6.5
0x2b = 0_010_1011 = +0b1.1011*2^-2 = 0.421875
                                                     0x6b = 0_110_1011 = +0b1.1011*2^2 = 6.75
                                                                                                           0xab = 1_010_1011 = -0b1.1011*2^-2 = -0.421875
                                                                                                                                                                0xeb = 1_110_1011 = -0b1.1011*2^2 = -6.75
0x2c = 0 \ 010 \ 1100 = +0b1.1100*2^-2 = 0.4375
                                                     0x6c = 0_110_1100 = +0b1.1100*2^2 = 7
                                                                                                           0 \times ac = 1_010_1100 = -0b1.1100 \times 2^{-2} = -0.4375
                                                                                                                                                                0 \times ec = 1_{110_{1100}} = -0b1.1100 \times 2^2 = -7
0x2d = 0 \ 010 \ 1101 = +0b1.1101*2^-2 = 0.453125
                                                     0x6d = 0_110_1101 = +0b1.1101*2^2 = 7.25
                                                                                                           0xad = 1_010_1101 = -0b1.1101*2^-2 = -0.453125
                                                                                                                                                                0xed = 1 \ 110 \ 1101 = -0b1.1101*2^2 = -7.25
0x2e = 0 \ 010 \ 1110 = +0b1.1110*2^-2 = 0.46875
                                                     0x6e = 0 110 1110 = +0b1.1110*2^2 = 7.5
                                                                                                           0xae = 1 010 1110 = -0b1.1110*2^{-2} = -0.46875
                                                                                                                                                                0 \times ee = 1 \ 110 \ 1110 = -0b1.1110 \times 2^2 = -7.5
0x2f = 0 \ 010 \ 1111 = +0b1.1111 + 2^{-2} = 0.484375
                                                     0x6f = 0_110_1111 = +0b1.1111*2^2 = 7.75
                                                                                                           0xaf = 1_010_1111 = -0b1.1111*2^-2 = -0.484375
                                                                                                                                                                0xef = 1_110_1111 = -0b1.1111*2^2 = -7.75
0x30 = 0 \ 011 \ 0000 = +0b1.0000*2^{-1} = 0.5
                                                     0x70 = 0 111 0000 = +0b1.0000*2^3 = 8
                                                                                                           0xb0 = 1 011 0000 = -0b1.0000*2^{-1} = -0.5
                                                                                                                                                                0xf0 = 1 \ 111 \ 0000 = -0b1.0000*2^3 = -8
0x31 = 0_011_0001 = +0b1.0001*2^-1 = 0.53125
                                                     0x71 = 0_111_0001 = +0b1.0001*2^3 = 8.5
                                                                                                           0xb1 = 1_011_0001 = -0b1.0001*2^-1 = -0.53125
                                                                                                                                                                0xf1 = 1_111_0001 = -0b1.0001*2^3 = -8.5
0x32 = 0 \ 011 \ 0010 = +0b1.0010*2^{-1} = 0.5625
                                                     0x72 = 0 111 0010 = +0b1.0010*2^3 = 9
                                                                                                           0xb2 = 1 \ 011 \ 0010 = -0b1.0010*2^{-1} = -0.5625
                                                                                                                                                                0xf2 = 1_111_0010 = -0b1.0010*2^3 = -9
                                                                                                           0xb3 = 1_011_0011 = -0b1.0011*2^-1 = -0.59375
0x33 = 0 \ 011 \ 0011 = +0b1.0011*2^-1 = 0.59375
                                                     0x73 = 0_111_0011 = +0b1.0011*2^3 = 9.5
                                                                                                                                                                0xf3 = 1_111_0011 = -0b1.0011*2^3 = -9.5
0x34 = 0 \ 011 \ 0100 = +0b1.0100*2^{-1} = 0.625
                                                     0x74 = 0_111_0100 = +0b1.0100*2^3 = 10
                                                                                                           0xb4 = 1_011_0100 = -0b1.0100*2^-1 = -0.625
                                                                                                                                                                0xf4 = 1_111_0100 = -0b1.0100*2^3 = -10
0x35 = 0 \ 011 \ 0101 = +0b1.0101*2^-1 = 0.65625
                                                     0x75 = 0 \ 111 \ 0101 = +0b1.0101*2^3 = 10.5
                                                                                                           0xb5 = 1 \ 011 \ 0101 = -0b1.0101*2^{-1} = -0.65625
                                                                                                                                                                0xf5 = 1 111 0101 = -0b1.0101*2^3 = -10.5
0x36 = 0 \ 011 \ 0110 = +0b1.0110*2^-1 = 0.6875
                                                     0x76 = 0 111 0110 = +0b1.0110*2^3 = 11
                                                                                                           0xb6 = 1 \ 011 \ 0110 = -0b1.0110*2^{-1} = -0.6875
                                                                                                                                                                0 \times f6 = 1_111_0110 = -0b1.0110 \times 2^3 = -11
0x37 = 0 \ 011 \ 0111 = +0b1.0111*2^-1 = 0.71875
                                                     0x77 = 0 111 0111 = +0b1.0111*2^3 = 11.5
                                                                                                           0xb7 = 1 \ 011 \ 0111 = -0b1.0111*2^-1 = -0.71875
                                                                                                                                                                0xf7 = 1 \ 111 \ 0111 = -0b1.0111*2^3 = -11.5
                                                                                                                                                                0xf8 = 1_111_1000 = -0b1.1000*2^3 = -12
0x38 = 0 \ 011 \ 1000 = +0b1.1000*2^-1 = 0.75
                                                     0x78 = 0 111 1000 = +0b1.1000*2^3 = 12
                                                                                                           0xb8 = 1 \ 011 \ 1000 = -0b1.1000*2^-1 = -0.75
0x39 = 0_011_1001 = +0b1.1001*2^-1 = 0.78125
                                                     0x79 = 0_111_1001 = +0b1.1001*2^3 = 12.5
                                                                                                           0xb9 = 1_011_1001 = -0b1.1001*2^-1 = -0.78125
                                                                                                                                                                0xf9 = 1_111_1001 = -0b1.1001*2^3 = -12.5
                                                                                                                                                                0xfa = 1 \ 111 \ 1010 = -0b1.1010*2^3 = -13
0x3a = 0 011 1010 = +0b1.1010*2^{-1} = 0.8125
                                                     0x7a = 0 111 1010 = +0b1.1010*2^3 = 13
                                                                                                           0xba = 1 011 1010 = -0b1.1010*2^{-1} = -0.8125
0x3b = 0_011_1011 = +0b1.1011*2^-1 = 0.84375
                                                     0x7b = 0_111_1011 = +0b1.1011*2^3 = 13.5
                                                                                                           0xbb = 1_011_1011 = -0b1.1011*2^{-1} = -0.84375
                                                                                                                                                                0xfb = 1_111_1011 = -0b1.1011*2^3 = -13.5
0x3c = 0.011 1100 = +0b1.1100*2^-1 = 0.875
                                                     0x7c = 0 111 1100 = +0b1.1100*2^3 = 14
                                                                                                           0xbc = 1 011 1100 = -0b1.1100*2^{-1} = -0.875
                                                                                                                                                                0xfc = 1 \ 111 \ 1100 = -0b1.1100*2^3 = -14
                                                     0x7d = 0_111_1101 = +0b1.1101*2^3 = 14.5
                                                                                                           0xbd = 1 \ 011 \ 1101 = -0b1.1101*2^{-1} = -0.90625
                                                                                                                                                                0xfd = 1_111_1101 = -0b1.1101*2^3 = -14.5
0x3d = 0 \ 011 \ 1101 = +0b1.1101*2^-1 = 0.90625
                                                     0x7e = 0 111 1110 = +0b1.1110*2^3 = 15
                                                                                                                                                                0xfe = 1 111 1110 = -0b1.1110*2*3 = -15
0x3e = 0 011 1110 = +0b1.1110*2^{-1} = 0.9375
                                                                                                           0xbe = 1 011 1110 = -0b1.1110*2^{-1} = -0.9375
                                                                                                           0xbf = 1_011_1111 = -0b1.1111*2^-1 = -0.96875
0x3f = 0 \ 011 \ 1111 = +0b1.1111*2^-1 = 0.96875
                                                     0x7f = 0_111_1111 = +Inf
                                                                                                                                                                0xff = 1_111_1111 = -Inf
```