

# Mecânica 1

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Abstract

## 1 Capítulo 5

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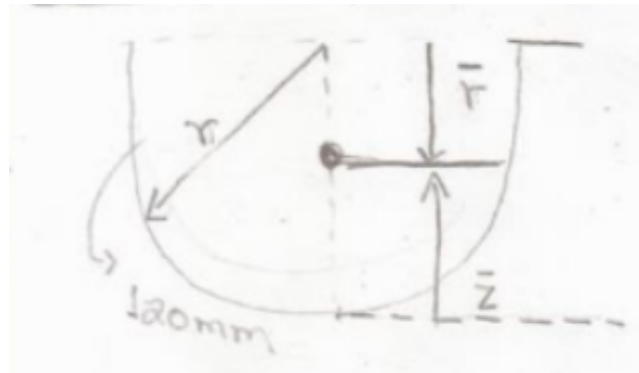


Figure 1:

$$\begin{aligned}\bar{x} &=? \text{ e } \bar{z}=? \\ \bar{r} &= \frac{2*r}{\pi} \Rightarrow \frac{2*120}{\pi} \Rightarrow \bar{r} = 76,4mm \\ \bar{z} &= r - \bar{r} \Rightarrow \bar{z} = 120 - 76,4 \\ \bar{z} &= 43,6mm \\ \bar{x} &= -120mm\end{aligned}$$

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$$yc = \frac{2*r}{\pi} ; dA = \pi * r * dr ; A = \pi * \int_{R/2}^R r * dr \Rightarrow A = \frac{3*\pi*R^2}{8}$$

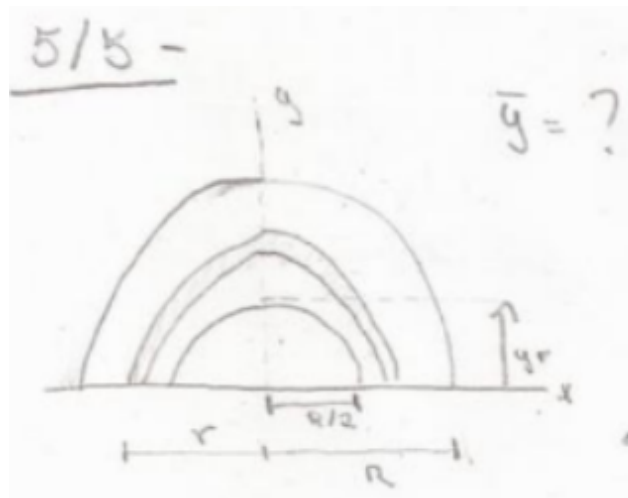


Figure 2:

$$\begin{aligned} \int y * c * dA &=> \int_{R/2}^R \frac{2*r}{\pi} * \pi * r * dr => \frac{2*r^3}{3} \Big| \\ &= \frac{7}{12} * R^3 \\ \bar{y}A &= \int y * c * dA ; \bar{y} = \frac{7}{12} * R^3 \Big| \frac{3*\pi}{12} * R^3 \\ &= \frac{14*R}{9*\pi} \end{aligned}$$

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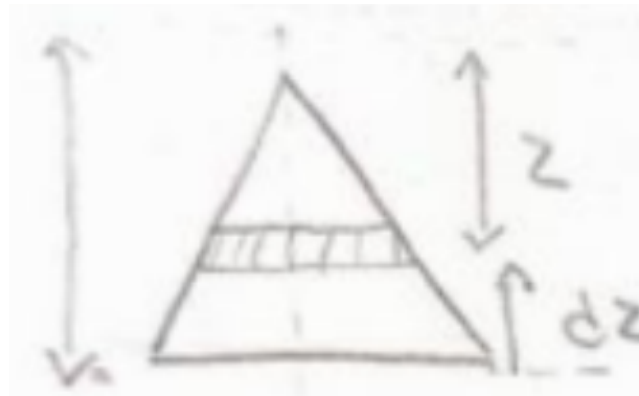


Figure 3:

$\bar{z}$  o vértice ao centróide do seu volume.

$$x = \frac{r}{h} * z$$

$$\begin{aligned}
 dv &= \pi * x^2 * dz = \pi * \left(\frac{r}{h} * z\right)^2 * dz \\
 v &= \frac{\pi * r^2}{h^2} * \int_0^h z * dz = \frac{\pi * r^2 * h}{3} \\
 \int z * dz &= \frac{\pi * r^2}{h} \int_0^h z^3 * dz \Rightarrow \frac{\pi * r^2 * h}{4} \\
 \bar{z} &= \int \frac{z * dv}{v} \Rightarrow \frac{\pi * r^2 * h^2 / 4}{\pi * r^2 * h / 3} \\
 \bar{z} &= \frac{3 * h}{4}
 \end{aligned}$$

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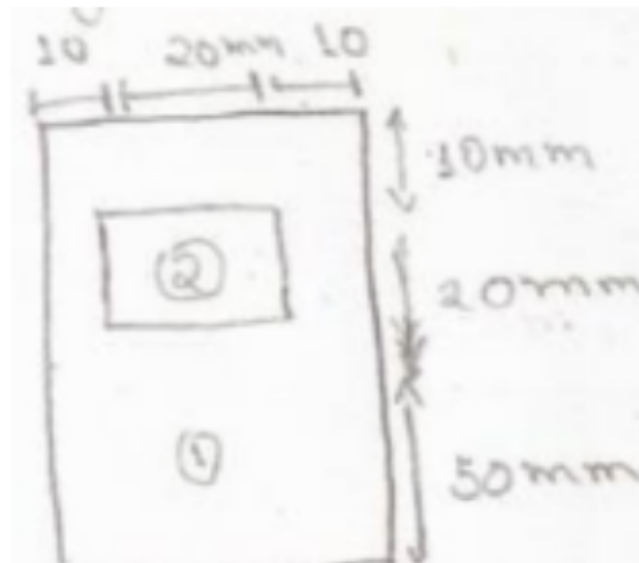


Figure 4:

y do centróide da área sombreada

$$1 - A = 80 * 40 = 3200mm^2$$

$$\bar{y} = 40mm$$

$$\bar{y}A = 3200 * 40 = 12000mm^3$$

$$2 - A = -20 * 20 = -400mm^2$$

$$\bar{y} = 60$$

$$\bar{y}A = -400 * 60 = -2400mm^3$$

$$\sum A = 2800e \sum \bar{y}A = 104000$$

$$\bar{y} = \frac{\sum \bar{y}A}{\sum A} = \frac{104000mm^3}{2800mm^2} = 37,1mm$$

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Volume do sólido gerado por rev=180(graus) em torno do eixo z

$$V = \theta * \bar{r} * A$$

$$V = \pi * (8 + \frac{2}{y} * 12) * \frac{1}{2} * 12 * 12$$

$$V = 3620mm^3$$

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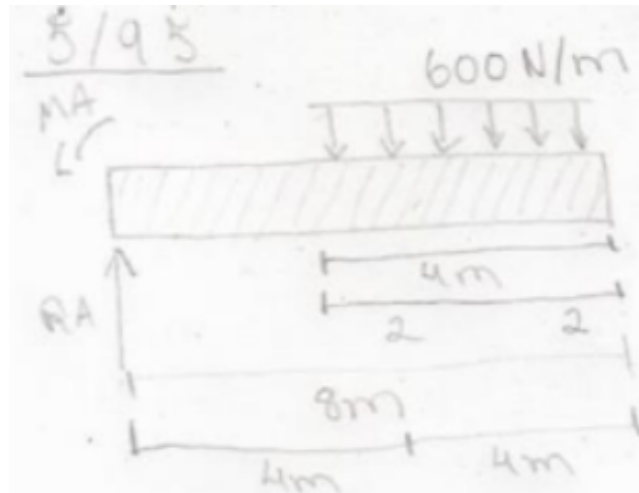


Figure 5:

Força RA e o momento MA em A

$$F = 600 * 4 = 2400N \quad \sum F = 0 : RA - 2400 = 0$$

$$RA = 2400N = 2,4KN$$

$$\sum MA = 0 : MA - 2400 * 4 = 0$$

$$MA = 14 * 400N = 14,4KN$$

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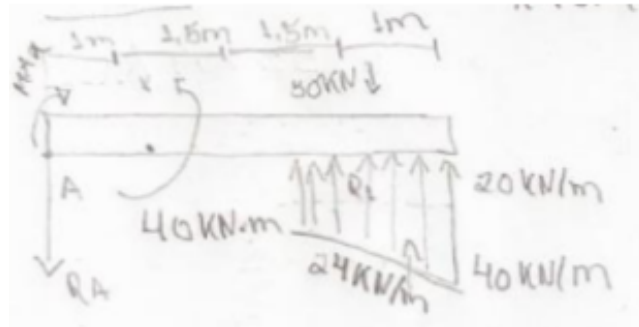


Figure 6:

A força e o momento de reação em A

$$R2 = A2 = 36 * \frac{25}{2} = 45KN$$

$$\sum MX = 0 \text{ portanto, } MA - 40 + 50 * 4 - 60 * 3,75 - 45 * 4,15$$

$$MA = 252,65KN * m$$

$$x \sum F = 0$$

$$-RA - 50 + 60 + 45 = 0$$

$$Ra = 55KN$$

$$\bar{x} = \frac{1,5+1}{3} = 0,833$$

$$R1 = A1 = 24 * 2,5 = 60KN$$

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Força atrativa no meio do vão To

$$L = 1280m$$

$$h = 145m$$

$$w = 310KN * 10^{-3}$$

$$w = 0,3108$$

$$To = \frac{w * L^2}{8 * h} \text{ portanto, } To = \frac{0,3108 * (1280)^2}{8 * 145}$$

$$To = 445,12KN$$

$$c = 2 * Tmax * \sin \theta$$

$$= 2 * \frac{w * L}{2} => w * L$$

$$c = w * L$$

$$c = 0,3108 * 1280$$

$$c = 397,82KN$$

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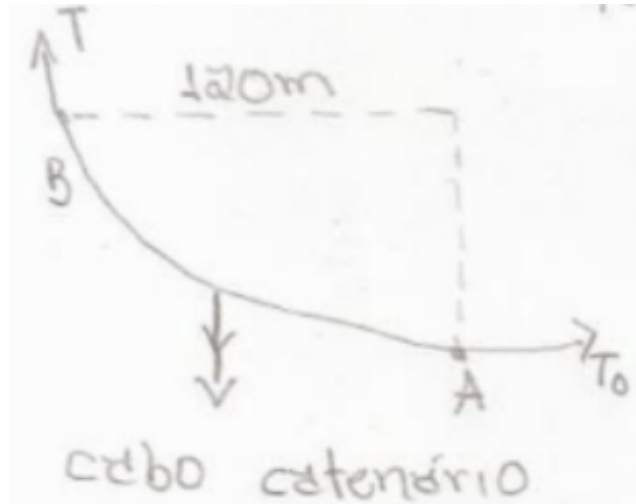


Figure 7:

$T_o = ?$  e  $T_{\text{parabola}} = ?$

$$x = 60m$$

$$y = 30m$$

$$\mu = 0,750 * 8,81 * 10^{-3}$$

$$\mu = 0,00735$$

Cabo Catenário

$$y = \frac{T_o}{\mu} * (\cosh * \frac{\mu * x}{T_o} - 1)$$

$$30 = \frac{T_o}{\mu} * (\cosh * \frac{7,35 * 120}{T_o} - 1)$$

$$T_o = 1801N$$

Cabo Parabólico

$$y = \frac{w * x^2}{2 * T_o}$$

$$\frac{7,35 * (120)^2}{2 * T_o} = 30$$

$$7,35 * 14.400 = 60T_o$$

$$T_o = 1765N$$

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$h_{\text{agua}} = ?$  e  $h_{\text{mercurio}} = ?$

$$P_a Z = 1,0133 * 10^5 Pa$$

$$\rho_{\text{agua}} = 1000 Kg/m^3$$

$$\rho_{\text{mercúrio}} = 13570 \text{ Kg/m}^3$$



Figure 8:

Água:

$$\rho * g * h = PaZ$$

$$1000 * 9,81 * h = 1,0133$$

$$h = 10,33m$$

Mercúrio:

$$\rho * g * h = PaZ$$

$$13570 * 9,81 * h = 1,0133$$

$$h = 0,761$$

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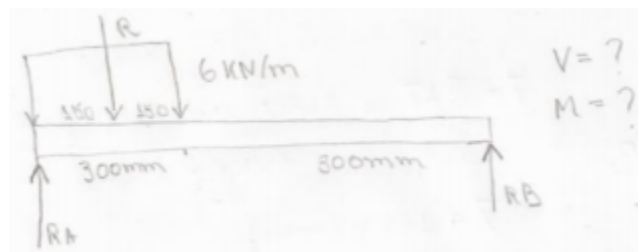


Figure 9:

$$R = 6 * 0,3 = 1,8KN$$

$$\sum MB = 0 \text{ portanto, } 1,8 * (0,3 + 0,015) - 0,6 * RA = 0$$

$$RA = 1,35KN$$

$$R1 = 6 * 0,2 = 1,2KN$$

$$\sum F = 0 \text{ portanto, } 1,35 - 12 - V = 0$$

$$V = 0,15K$$

$$\sum MA = 0$$

$$M - 1,2 * 0,015 - 0,15 * 0,2 = 0$$

$$M = 0,15KN$$

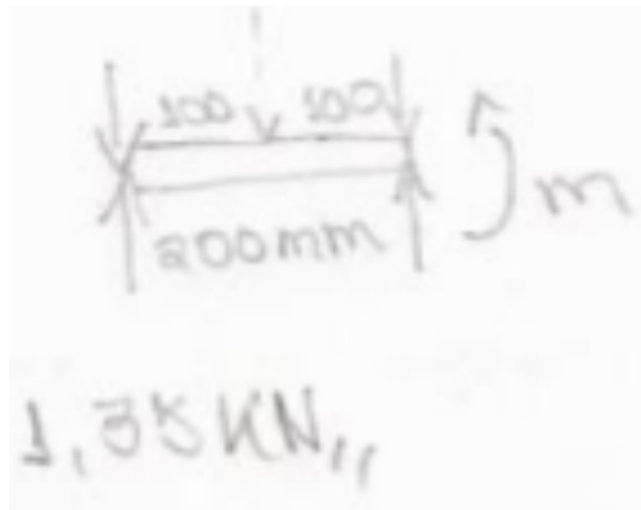


Figure 10: