Exercises of SVM classifier

Eva Cernadas FMLCV Course

CITIUS: Centro de Tecnoloxías Intelixentes da USC Universidade de Santiago de Compostela

14 de diciembre de 2021

We practice the use of Support Vector Machine (SVM) classifier on the datasets wine.data (with 2 classes) and hepatitis.data (with 3 classes). We use the functionality provided by several libraries:

- 1. LibSVM library¹, accessible from C++, Octave/Matlab, Python, Weka/Java.
- 2. Class SVC in the svm module of Python scikit-learn².
- 3. Function ksvm in the kernlab package in programming language R³

The tasks can be done using some of these programming languages (R, octave, Matlab, C++ or Python). To use the LibSVM from octave or matlab, do the following steps: 1) download the library from the web page or TEAMS; 2) uncompress the file using the command tar zxvf libsvm-3.24.tar.gz or unzip libsvm-3.24.zip; and 3) compile the library using the command make. If you use octave, go to the folder matlab, enter in octave and run make. Then, exit octave. The main functions of libsvm are:

- 1. svm= svmtrain(c, x, opt), where the input argument x is the matrix with the patterns of the training set, c is the desired output of the patterns of the training set and opt is a string with the configuration options of the SVM (see the libsvm README file). This function returns the SVM trained.
- 2. z=svmpredict(tc, tx, svm), where the input argument tx is the matrix with the test patterns, tc is a vector with the desired output of the test patterns and svm is the trained SVM. This function returns the predicted output for the test patterns.

¹https://www.csie.ntu.edu.tw/~cjlin/libsvm/

²https://scikit-learn.org/stable/modules/generated/sklearn.svm.SVC.html

³https://www.rdocumentation.org/packages/kernlab/versions/0.9-29/topics/ksvm

The code to apply linear and radial SVM to a classification dataset using the whole set to train and test the SVM (this evaluation methodology is not normally used due to provide very optimistic results, but it is only to know the use of the functions symtrain() and sympredict()). Note that the data must be pre-processed to be with mean 0 and standard desviation 1.

```
1 clear all;
  warning off all
  addpath ("libsvm -3.24/matlab")
  %3 classes
  %dataset='wine'; x=load('wine.data');
  \% 2 classes
  dataset='hepatitis'; x=load('hepatitis.data');
  c=x(:,1); x(:,1) = []; [N,I] = size(x);
  cl=unique(c);C=numel(cl);
  % preprocessing: mean 0, desviation 1
  mx = mean(x); stdx = std(x);
  x=bsxfun(@rdivide, bsxfun(@minus,x,mx),stdx);
  \% x = (x - mean(x)) . / std(x);
                              #matlab
  %SVM with linear kernel
  %s is the SVM type (0 for classification)
  %t is the kernel type (0 for linear and 2 for radial)
  %c is the tuned parameter lambda
  %g is the tuned parameter kernel spread
18
  opt = sprintf('-s \ 0 \ -t \ 0 \ -c \ \%g \ -q', 100);
19
  svm = svmtrain(c, x, opt);
  y=svmpredict(c, x, svm);
21
  [kappa, accu, cm] = evaluate(c, y, C);
22
  disp ('Confusion matrix='); disp (cm);
  fprintf('SVM lineal: dataset %: accuracy=%.2f % %n', dataset, accu)
24
  fprintf('SVM lineal: dataset %: kappa=%.2f%%n', dataset, kappa)
25
  %SVM with radial base (Gaussian) kernel
26
  opt = sprintf('-s \ 0 \ -t \ 2 \ -c \ \%g \ -g \ \%g \ -q', 100, 1/I);
27
  svm=svmtrain(c,x,opt);
  y=sympredict(c,x,sym);
  [kappa, accu, cm] = evaluate(c, y, C);
  disp ('Confusion matrix='); disp (cm);
  fprintf('SVM radial: dataset %: accuracy=%.2f % %n', dataset, accu)
  fprintf('SVM radial: dataset %: kappa=%.2f % %n', dataset, kappa)
```

Use the linear SVM using cross-validation with 4 folds. In this case, the lambda parameter must be tuned using the validation set. The functions standarized() and normalize() are used to standarized the data to be mean zero and standard desviation 1:

1 % standarized: return the mean, standard desviation of data x and

```
% the data x with mean 0 and standard desviation 1.
  %x: a matrix of number of patterns by number of inputs
  function [mx, stdx, x] = standarized(x)
     % preprocessing: mean 0, desviation 1
     mx = mean(x); stdx = std(x);
     x=bsxfun (@rdivide, bsxfun (@minus, x, mx), stdx);
     \% x = (x - mean(x)) . / std(x); \#matlab
  end
  % normalize: return the data x normalized
  % inputs: the data x and the mean and std to normalize
  function x=normalize(x, meant, stdt)
     x=bsxfun(@rdivide, bsxfun(@minus,x,meant), stdt);
     \% x = (x - meant) . / stdt; #matlab
6 end
     The code to apply linear SVM using cross-validation is provided:
1 clear all; more off
2 warning off all
3 addpath ("libsvm -3.24/matlab")
  %3 classes
  % dataset='wine'; x=load('wine.data'); % first column is the
      output
  %2 classes
  dataset='hepatitis'; x=load('hepatitis.data'); % first column is
      the output
  c=x(:,1); x(:,1) = []; [N, I] = size(x);
  cl=unique(c);C=numel(cl);
  K=4 % number of folds
  [tx, tc, vx, vc, sx, sc] = createFolds(x, c, K);
  vL= 2.^{(-5:2:15)}; nL=length(vL); \% lambda values
  best_kappa = -100; best_k=100;
  for l=1:nL
     L=vL(1);
15
     for i=1:K
16
       opt=sprintf('-s \ 0 \ -t \ 0 \ -c \ \%g \ -q', L);
17
       [mx, stdx, x] = standarized(tx{i});
18
       svm=svmtrain(tc\{i\},x,opt);
19
       xv = normalize(vx\{i\}, mx, stdx);
       y=svmpredict(vc\{i\},xv,svm);
21
       [\text{kappa}(i), \text{acc}(i)] = \text{evaluate}(\text{vc}\{i\}, \text{y}, \text{C});
22
23
     kappa_mean=mean(kappa); acc_mean=mean(acc);
24
```

```
fprintf('lambda=%.1g:',L);
25
     fprintf ('kappa=%.1f % %accuracy=%.1f % %n', kappa_mean, acc_mean)
26
     if kappa_mean>best_kappa
27
       best_kappa=kappa_mean;
28
       bestL=L;
     end
30
31
  printf('best_config='); fprintf('Lambda= \%\n', bestL);
32
  cmt=zeros(C); % confusion matrix
  kappa=zeros(1,K); acc=zeros(1,K);
34
  for i=1:K
35
     opt=sprintf('-s \ 0 \ -t \ 0 \ -c \ \% \ -q \ -b \ 1', bestL);
36
     [mx, stdx, x] = standarized([tx{i}; vx{i}]);
37
    svm=svmtrain([tc{i}; vc{i}], x, opt);
38
    xv = normalize(sx\{i\}, mx, stdx);
39
    y=svmpredict(sc\{i\},xv,svm);
40
     [\text{kappa}(i), \text{acc}(i), \text{cm}] = \text{evaluate}(\text{sc}\{i\}, y, C);
41
     fprintf('fold %: kappa=%.1f%%accuracy=%.1f%%p',i,kappa(i),
42
        acc(i))
    cmt = cmt + cm;
43
44
  kappa_mean=mean(kappa); acc_mean=mean(acc); cmt=cmt/K;
  disp('Final confusion matrix='); disp(cmt);
  fprintf('dataset %: kappa=%.1f%%accuracy=%.1f%%n',dataset,
     kappa_mean, acc_mean)
```

The code to apply radial SVM using cross-validation is also provided. In this case the tuned parameters are the regularization parameter λ and the kernel spread σ :

```
clear all; more off
warning off all
addpath("libsvm -3.24/matlab")

% 3 classes
dataset='wine'; x=load('wine.data'); % first column is the output
% 2 classes
% dataset='hepatitis'; x=load('hepatitis.data'); % first column is
the output
c=x(:,1);x(:,1)=[];[N,I]=size(x);
cl=unique(c);C=numel(cl);
K=4 % number of folds
[tx,tc,vx,vc,sx,sc]=createFolds(x, c, K);
vL= 2.^(-5:2:15);nL=length(vL); % lambda values
vG=2.^(-7:2:7);nG=length(vG); % kernel spread values
best_kappa=-100;bestL=100; bestG=0;
```

```
for l=1:nL
15
    L=vL(1);
16
     for j=1:nG
17
       G=vG(j);
18
       for i=1:K
19
         opt=sprintf('-s \ 0 \ -t \ 2 \ -c \ \%g \ -g \ \%g \ -q', L,G);
20
         [mx, stdx, x] = standarized(tx{i});
21
         svm=svmtrain(tc\{i\},x,opt);
22
         xv = normalize(vx\{i\}, mx, stdx);
23
         y=svmpredict(vc\{i\},xv,svm);
24
         [kappa(i), acc(i)]=evaluate(vc{i}, y, C);
25
       end
26
       kappa_mean=mean(kappa); acc_mean=mean(acc);
27
       fprintf('lambda=%.1g, radial=%.1g: ',L,G);
28
       fprintf('kappa=%.1f%%accuracy=%.1f%%p',kappa_mean,acc_mean)
29
       if kappa_mean>best_kappa
30
         best_kappa=kappa_mean;
31
         bestL=L; bestG=G;
32
       end
33
     end
34
35
  printf('best_config='); fprintf('Lambda= \%g, Radial spread=\%g\n',
36
     bestL, bestG);
  cmt=zeros(C); % confusion matrix
37
  kappa=zeros(1,K); acc=zeros(1,K);
  for i=1:K
39
     opt=sprintf('-s 0 -t 2 -c %g -g %g -q', bestL, bestG);
40
     [mx, stdx, x] = standarized([tx{i}; vx{i}]);
41
    svm=svmtrain([tc{i}; vc{i}], x, opt);
42
    xv=normalize(sx{i}, mx, stdx);
43
    y=svmpredict(sc\{i\},xv,svm);
44
     [\text{kappa}(i), \text{acc}(i), \text{cm}] = \text{evaluate}(\text{sc}\{i\}, y, C);
45
     fprintf('fold %: kappa=%.1f%%accuracy=%.1f%%n',i,kappa(i),
46
        acc(i))
    cmt = cmt + cm;
47
48
  kappa_mean=mean(kappa); acc_mean=mean(acc); cmt=cmt/K;
  disp('Final confusion matrix='); disp(cmt);
  fprintf('dataset %: kappa=%.1f%%accuracy=%.1f%%n',dataset,
     kappa_mean, acc_mean)
```

1. Programas en Python

1. Use the following code to create a program svc.py that implements SVC using the object SVC of sklearn.svm, tuning the λ and $\gamma = 1/2\sigma^2$ hyper-parameters using 4-fold cross-validation with the createFolds() function used with ANN:

```
model=SVC(C=L, kernel='rbf', gamma=G, verbose=False). fit (tx[k],
      ty [k])
z=model.predict(vx[k])
  The whole program is:
1 # NN sintonizando o no. V de vecinhos con validacion cruzada
      K-fold e particions de entrenamento, validación e teste
  from numpy import *
  from sklearn.svm import *
  from sklearn.metrics import *
  dataset='wine'; # hepatitis (2 clases), wine (3 clases)
  nf='%.data'%dataset;x=loadtxt(nf)
  y=x[:,0]-1; x=delete(x,0,1); C=len(unique(y))
  print ('SVC dataset %' %dataset)
10
11
  def createFolds(x,y,K):
12
     from numpy.random import shuffle, seed
13
     seed (100)
14
     [N, n] = x \cdot shape; C = len(unique(y)); ntf = K-2; nvf = 1
     ti = [[]] *K; vi = [[]] *K; si = [[]] *K
16
     for i in range (C):
17
       t=where (y=i) [0]; npc=len(t); shuffle(t)
18
       npf = int (npc/K); ntp = npf * ntf
19
       nvp = npf * nvf ; nsp = npc - ntp - nvp ; start = 0
20
       for k in range(K):
         p=start; u=[]
22
         for 1 in range (ntp):
23
            u.append(t[p]); p=(p+1)\%npc
24
          ti [k] = ti [k] + u; u = []
25
          for l in range(nvp):
26
            u. append (t[p]); p=(p+1)% npc
27
         vi[k] = vi[k] + u; u = []
         for l in range (nsp):
            u.append(t[p]); p=(p+1) \%apc
30
          si[k]=si[k]+u; start=start+npf
31
     tx = []; ty = []; vx = []; vy = []; sx = []; sy = []
32
```

```
for k in range(K):
33
       i=ti[k];tx.append(x[i,:]);ty.append(y[i])
34
       i=vi[k]; vx.append(x[i],:]); vy.append(y[i])
35
       i=si[k]; sx.append(x[i,:]); sy.append(y[i])
36
     return [tx, ty, vx, vy, sx, sy]
38
  K=4:
39
  tx, ty, vx, vy, sx, sy = createFolds(x, y, K)
40
41
  # preprocesamento: media 0, desviacion
42
  for k in range(K):
43
    med=mean(tx[k],0); dev=std(tx[k],0)
44
     tx[k]=(tx[k]-med)/dev
45
    vx[k] = (vx[k] - med)/dev
46
    sx[k]=(sx[k]-med)/dev
47
  # sintonizacion de hiper-parametros
  kappa_mellor = -100; kappa = zeros([1,K]);
  vL=2.**arange(-5,16,2);nL=len(vL); \# regularization (lambda)
  vG=2.**arange(-10,11,2);nG=len(vG); \# ancho cerne gausiano (
51
  vkappa=zeros ([nL,nG]); kappa=zeros (K); kappa_mellor=-inf;
52
  print ('%10s %15s %10s %10s '%('Lambda', 'Gamma', 'Kappa', 'Best')
  for i in range(nL):
       L=vL [ i ]
55
       for j in range (nG):
56
           G=vG [ j ]
57
           for k in range(K):
58
                modelo=SVC(C=L, kernel='rbf', gamma=G, verbose=False
59
                   ). fit (tx[k], ty[k])
                z=modelo.predict(vx[k])
60
                kappa[k]=100*cohen_kappa_score(vy[k],z)
61
           kappa_med=mean(kappa); vkappa[i,j]=kappa_med
62
           if kappa_med>kappa_mellor:
63
                kappa_mellor=kappa_med; L_mellor=L; G_mellor=G
64
           print ('%10i %15g %10.1f %10.1f' %(L,G,kappa_med,
65
               kappa_mellor))
  print ('L_mellor=% G_mellor=% kappa=%.1f%%%(L_mellor,
     G_mellor, kappa_mellor))
  from pylab import *
  # grafica coa sintonizacion dos hiper-parametros L,G-
```

```
figure (1); clf (); u=ravel (vkappa); plot (u); grid (True)
   axis([1, len(u), -5, 100])
   xlabel('Configuracion'); ylabel('Kappa (%)')
   title ('Kappa (%%) sintonizacion de SVC %' %dataset)
   savefig ('sintonizacion_svc_ % .eps' %dataset); show()
  #grafica 3D-
   from mpl_toolkits.mplot3d import Axes3D
   fig=figure(2); clf(); ax=Axes3D(fig)
   [X,Y]=meshgrid(log2(vL),log2(vG)); ax.plot_surface(X,Y,vkappa,
      rstride = 1, cstride = 1, cmap = 'hot'
   xlabel('$log_2 \lambda$'); ylabel('$log_2 \gamma$')
   title ('Kappa (%%) sintonizacion SVC 3D %' dataset); colorbar
80
   show()
81
  # mapa de calor-
  figure (3); clf(); imshow(vkappa); colorbar()
   xlabel('Regularizacion ($log_2 \lambda$)'); ylabel('Ancho do
      cerne gausiano ($log_2 \gamma$)')
   title ('Sintonizacion SVC mapa calor %' 'Adataset)
   show()
86
  # test-
87
  mc=zeros([C,C])
   if C==2:
89
     pre=zeros (K); re=zeros (K); f1=zeros (K)
90
   for k in range (K):
91
     x=vstack((tx[k],vx[k])); y=concatenate((ty[k],vy[k]))
     modelo=SVC(C=L_mellor, kernel='rbf', gamma=G_mellor, verbose=
93
        False). fit(x,y)
     z=modelo.predict(sx[k]);y=sy[k]
94
     kappa [k]=100*cohen_kappa_score(y,z)
95
     mc + = confusion_m atrix(y, z)
96
     if C==2:
97
       pre[k] = precision\_score(y, z)
98
       re[k] = recall_score(y, z)
99
       f1 [k] = f1 \_score(y, z)
100
   kappa_med=mean(kappa);mc/=K
101
   print ('SVC dataset= % I= % G= % kappa= %.1f % %% (dataset,
102
      L_mellor, G_mellor, kappa_med))
   print('matriz de confusion:'); print(mc)
```

2. Exercises to do by the students

The lab work for the students is:

- 1. Download the datasets wine.data and hepatitis.data from the TEAMS.
- 2. Calculate the accuracy, Cohen kappa and confusion matrix for both datasets using the SVM classifier with linear kernel using the whole dataset as training and test set.
- 3. Calculate the accuracy, Cohen kappa and confusion matrix for both datasets using the SVM classifier with Gaussian kernel using the whole dataset as training and test set and using the default configuration for the hyper-parameters ($\lambda = 100$ and $\sigma = 1/n$, which n is the number of inputs). Compare the performance with the SVM classifier with linear kernel.
- 4. Repeat the process using cross-validation with 4 and 10 folds. In this case, we must tune the hyper-parameters for the SVM with Gaussian kernel: the regularization parameter λ with values $\lambda = 2^{-5}.,2^{15}$ and the kernel spread σ of the Gaussian kernel, $\sigma = 2^{-7}.,2^{7}$. For the SVM with linear kernel, it is only need to tune the λ parameter. So, you must use the validation set to tune the hyper-parameters and select the best configuration to train the SVM with the training and validation sets and test the SVM over the test set.
- 5. Use the SVM classifier to the classification of the textures dataset. Compare the results using the SVM classifier with linear and Gaussian kernel. For the SVM classifier with Gaussian kernel, compare the results using the OVO (one-versus-one) and OVA (one-versus-all) approaches. The LibSVM implements the OVO approach and the OVA approach must be programmed. To implement the OVA approach, you need to create C (number of classes) two-class SVMs, each one to discriminate between the patterns of class i, i = 1, ..., C and the patterns of the remaining classes j, j = 1, ..., C and $j \neq i$.

Submit before 22 January by TEAMS the results and dificulties found. It can be done individually or by groups.