

## ✔ Congratulations! You passed!

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1. Select the characteristic polynomial for the given matrix.

1 / 1 point

$$\begin{bmatrix} 2 & 1 \\ -3 & 6 \end{bmatrix}$$

- ☒  $\lambda^2 - 8\lambda + 15$
- ☐  $\lambda^2 - 8\lambda - 1$
- ☐  $\lambda^3 - 8\lambda + 15$
- ☐  $\lambda^2 + 8\lambda + 15$

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Correct

Correct!  $\lambda^2 - (2 + 6)\lambda + (2 * 6 - 1(-3)) = 0$

2. Select the eigenvectors for the previous matrix in Q1, as given below:

1 / 1 point

$$\begin{bmatrix} 2 & 1 \\ -3 & 6 \end{bmatrix}$$

- ☐  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \end{pmatrix}$
- ☒  $\begin{pmatrix} 1 \\ 3 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \end{pmatrix}$
- ☐  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \end{pmatrix}$
- ☐  $\begin{pmatrix} 1 \\ 3 \end{pmatrix}, \begin{pmatrix} 1 \\ 3 \end{pmatrix}$

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Correct

Correct! You first find the eigenvalues for the given matrix:  $\lambda = 5, \lambda = 3$ . Now you solve the equations using each of the eigenvalues.

For  $\lambda = 5$ , you have  $\begin{cases} 2x + y = 5x \\ -3x + 6y = 5y \end{cases}$ , which has solutions for  $x = 1, y = 3$ . Your eigenvector is  $\begin{pmatrix} 1 \\ 3 \end{pmatrix}$ .

For  $\lambda = 3$ , you have  $\begin{cases} 2x + y = 3x \\ -3x + 6y = 3y \end{cases}$ , which has solutions for  $x = 1, y = 1$ . Your eigenvector is  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ .

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3. Which of the following is an eigenvalue for the given identity matrix.

1 / 1 point

$$ID = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

- ☐  $\lambda = -1$
- ☒  $\lambda = 1$
- ☐  $\lambda = 2$

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✓ **Correct**

Correct! The eigenvalue for the identity matrix is always 1.

4. Find the eigenvalues of matrix  $A \cdot B$  where:

1 / 1 point

$$A = \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

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Hint: What type of matrix is  $B$ ? Does it change the output when multiplied with  $A$ ? If not, focus only on one of the matrices to find the eigenvalues.

- ☐  $\lambda_1 = 3, \lambda_2 = 1$
- ☐ Eigenvalues cannot be determined.
- ☐  $\lambda_1 = 4, \lambda_2 = 2$
- ☒  $\lambda_1 = 4, \lambda_2 = 1$

✓ **Correct**

Correct!  $A \cdot B = \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 \cdot 1 + 2 \cdot 0 & 1 \cdot 0 + 2 \cdot 1 \\ 0 \cdot 1 + 4 \cdot 0 & 0 \cdot 0 + 4 \cdot 1 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix}$

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Since the second matrix is an identity matrix, you wouldn't need to solve the above multiplication since identity matrix does not change the result.

The eigenvalues of  $A$  are the roots of the characteristic equation  $\det(A - \lambda I) = 0$ .

By solving  $\lambda^2 - 5\lambda + 4 = 0$ , you get  $\lambda_1 = 4, \lambda_2 = 1$ .

5. Select the eigenvectors, using the eigenvalues you found for the above matrix  $A \cdot B$  in Q4.

1 / 1 point

- ☐  $\vec{v}_1 = (1, 3); \vec{v}_2 = (1, 0)$
- ☒  $\vec{v}_1 = (2, 3); \vec{v}_2 = (1, 0)$
- ☐  $\vec{v}_1 = (2, 0); \vec{v}_2 = (1, 0)$
- ☐  $\vec{v}_1 = (2, 3); \vec{v}_2 = (2, 3)$

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✓ **Correct**

Correct!

For  $\lambda = 4$ , you have  $\begin{cases} x + 2y = 4x \\ 0x + 4y = 4y \end{cases}$ , which has solutions for  $x = 2, y = 3$ . Your eigenvector  $\vec{v}_1$  is  $\begin{pmatrix} 2 \\ 3 \end{pmatrix}$ .

For  $\lambda = 1$ , you have  $\begin{cases} x + 2y = x \\ 0x + 4y = y \end{cases}$ , which has solutions for  $x = 1, y = 0$ . Your eigenvector  $\vec{v}_2$  is  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$ .

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1 / 1 point

6. Which of the vectors span the matrix  $W = \begin{bmatrix} 2 & 3 & 0 \\ 1 & 2 & 5 \\ 3 & -2 & -1 \end{bmatrix}$ ?

☒  $\vec{V}_1 = \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}, \vec{V}_2 = \begin{bmatrix} 3 \\ 2 \\ -2 \end{bmatrix}, \vec{V}_3 = \begin{bmatrix} 0 \\ 5 \\ -1 \end{bmatrix}$

☐  $V_1 = \begin{bmatrix} 2 \\ 3 \\ 0 \end{bmatrix}, V_2 = \begin{bmatrix} 1 \\ 2 \\ 5 \end{bmatrix}, V_3 = \begin{bmatrix} 3 \\ -2 \\ -1 \end{bmatrix}$

✓ Correct

Correct! There are linearly independent columns that span the matrix, which individually form three vectors  $\vec{V}_1, \vec{V}_2, \vec{V}_3$ . These vectors span the matrix  $W$ .

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7. Given matrix  $P$  select the answer with the correct eigenbasis.

$$P = \begin{bmatrix} 2 & 0 & 0 \\ 1 & 2 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

Hint: First compute the eigenvalues, eigenvectors and contrast the eigenbasis matrix with the spanning eigenvectors.

☒  $Eigenbasis = \begin{bmatrix} 0 & 0 & -1 \\ -1 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$

☐  $Eigenbasis = \begin{bmatrix} 0 & -1 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix}$

☐  $Eigenbasis = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$

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✓ Correct

Correct! After solving the characteristic equations to find the eigenvalues, you should get  $\lambda_1 = 1$  and  $\lambda_2 = 2$ .

The eigenvector for  $\lambda_1 = 1$  is  $\vec{V}_1 = \begin{pmatrix} 0 \\ -1 \\ 1 \end{pmatrix}$ .

The eigenvectors for  $\lambda_2 = 2$  are  $\vec{V}_2 = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \vec{V}_3 = \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}$ .

The eigenvectors form the eigenbasis:  $\begin{bmatrix} 0 & 0 & -1 \\ -1 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$

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8. Select the characteristic polynomial for the given matrix.

1 / 1 point

$$\begin{bmatrix} 3 & 1 & -2 \\ 4 & 0 & 1 \\ 2 & 1 & -1 \end{bmatrix}$$



$$\lambda^3 + 2\lambda^2 + 4\lambda - 5$$



$$-\lambda^3 + 2\lambda^2 + 4\lambda - 5$$



$$-\lambda^3 + 2\lambda^2 + 9$$



$$-\lambda^2 + 2\lambda^3 + 4\lambda - 5$$

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**Correct**

Correct! The characteristic polynomial of a matrix A is given by  $f(\lambda) = \det(A - \lambda I)$ .

First, you find the following:

$$\begin{bmatrix} 3 & 1 & -2 \\ 4 & 0 & 1 \\ 2 & 1 & -1 \end{bmatrix} \cdot \lambda \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Now you compute the determinant of the result:

$$\det \begin{pmatrix} 3 - \lambda & 1 & -2 \\ 4 & -\lambda & 1 \\ 2 & 1 & -1 - \lambda \end{pmatrix} = -\lambda^3 + 2\lambda^2 + 4\lambda - 5$$

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9. You are given a non-singular matrix A with real entries and eigenvalue  $i$ .

1 / 1 point

Which of the following statements is correct?



$i$  is an eigenvalue of  $A^{-1} + A$ .



$i$  is an eigenvalue of  $A^{-1} \cdot A \cdot I$ .



$1/i$  is an eigenvalue of  $A^{-1}$ .



**Correct**

Correct! You know that the eigenvalues of a matrix A are the solutions of its characteristic polynomial equation  $\det(A - \lambda I) = 0$ .