

"PALLAB GANGULY" # "LE DUC TOAN"

TEAMHOTEL

$M_{mass} := 8830 \text{ kg}$ mass of the machine

$V_{TOP} := 6.95 \frac{m}{s}$ Top Speed

$F_{max} := 32600 \text{ N}$ Max Transtion Force

$L_{hoses} := 1.5 \text{ m}$ Length of hoses

$R_{wheel} := 0.6 \text{ m}$ Radius of wheel

$I_{wheel} := 23.32 \text{ kg} \cdot \text{m}^2$ Interia wheel $1 \text{ rpm} = 0.105 \frac{1}{s}$

$P_{diesel} := 80000 \text{ W}$ Power of diesel engine

$n_p := 33.33 \frac{1}{s}$ Constant speed

$eff_{vp} := .97$ vol eff of pump

$eff_{vm} := .95$ vol eff of motor

$eff_{hmp} := .96$ hyd mech eff of pump

$eff_{hmm} := .95$ hyd mech eff of motor

$eff_g := .98$ tot eff of gear

$i_g := 15.5$ gear ratio (assumption)

$\Delta P_{max} := 400 \text{ bar}$ max pressure (assumption) $eff_{tm} := .931$

Hydrostatic transmission power $eff_{tp} := .931$

"Boost Pump"

"LINK 1: [https://www.boschrexroth.com/ics/cat/?language=en&id=&cat=Mobile-Hydraulics-](https://www.boschrexroth.com/ics/cat/?language=en&id=&cat=Mobile-Hydraulics)
"According to data sheet as in link 1"

$p_{boost} := 22 \text{ bar}$ "pressure of boost pump"

$$n_{boost} := 2000 \text{ rpm} \quad \text{"speed of the pump"}$$

$$V_{boost} := 32 \frac{\text{cm}^3}{\text{rev}} \quad \text{"volumetric displacement of the pump"}$$

$$Q_{boost} := V_{boost} \cdot n_{boost} \cdot \text{eff}_{vp} = 62.08 \frac{\text{l}}{\text{min}}$$

$$P_{boost} := \frac{Q_{boost} \cdot p_{boost}}{\text{eff}_{tm}} = 2.445 \text{ kW}$$

$$P_{hsm} := P_{diesel} - P_{boost} = (7.756 \cdot 10^4) \text{ W}$$

CONVERSION RATIO

$$R := \frac{V_{TOP} \cdot F_{max}}{P_{hsm} \cdot \text{eff}_g \cdot \text{eff}_{tp} \cdot \text{eff}_{tm}} = 3.439$$

$$R_m := \sqrt{R} = 1.855$$

$$V_{gp0} := \frac{V_{TOP} \cdot F_{max}}{n_p \cdot \Delta P_{max} \cdot \text{eff}_g \cdot \text{eff}_{tp} \cdot \text{eff}_{tm} \cdot R_m} = 107.882 \text{ cm}^3$$

$$\text{Volumetric Displacement of pump} := 115 \text{ cm}^3 \quad V_{gp} := 115 \text{ cm}^3 \quad (\text{assumed})$$

"LINK 1: <https://www.boschrexroth.com/ics/cat/?language=en&id=&cat=Mobile-Hydraulics-Catal>

$$V_{gm0} := \frac{F_{max} \cdot 2 \cdot \pi \cdot R_{wheel}}{\Delta P_{max} \cdot \text{eff}_{hmm} \cdot i_g \cdot \text{eff}_g} = 212.916 \text{ cm}^3$$

$$\text{Volumetric Displacement of motor} := 215 \text{ cm}^3 \quad V_{gm} := 215 \text{ cm}^3$$

"LINK 2: <https://www.boschrexroth.com/ics/cat/?language=en&id=&cat=Mobile-Hydraulics-Ca>

Velocity and $\omega_{p1} = \frac{V_{p1}}{r_{p1}}$

$$Q_{p1} := \frac{P_{hsm} \cdot \text{eff}_{tp}}{\Delta P_{max}} = 0.002 \frac{\text{m}^3}{\text{s}}$$

$$V_{gp1} := \frac{Q_{p1}}{n_p \cdot \text{eff}_{vp}} = 55.833 \text{ cm}^3$$

$$T_{m1} := \frac{V_{gm} \cdot \Delta P_{max} \cdot eff_{hmm}}{2 \cdot \pi} = (1.3 \cdot 10^3) \text{ N} \cdot \text{m}$$

$$n_{m1} := \frac{Q_{p1} \cdot eff_{vm}}{V_{gm}} = 7.976 \frac{1}{s}$$

$$F_1 := \frac{T_{m1} \cdot i_g \cdot eff_g}{R_{wheel}} = 32.919 \text{ kN}$$

$$p_1 := \frac{P_{hsm} \cdot eff_{tp}}{Q_{p1}} = 400 \text{ bar}$$

$$v_1 := \frac{2 \cdot \pi \cdot n_{m1} \cdot R_{wheel}}{i_g} = 6.984 \frac{\text{km}}{\text{hr}}$$

$$F_1 \cdot v_1 = 63.861 \text{ kW} \quad \text{"Power at point 1"}$$

Velocity and Transtion force at point2

$$Q_{p2} := V_{gp} \cdot n_p \cdot eff_{vp} = 0.004 \frac{\text{m}^3}{s}$$

$$p_2 := \frac{P_{hsm} \cdot eff_{tp}}{Q_{p2}} = 194.202 \text{ bar}$$

$$n_{mmax} := \frac{V_{TOP} \cdot i_g}{R_{wheel} \cdot \pi \cdot 2} = 28.575 \frac{1}{s}$$

$$V_{gm1} := \frac{Q_{p2} \cdot eff_{vm}}{n_{mmax}} = 123.607 \text{ cm}^3$$

$$T_{m2} := \frac{V_{gm1} \cdot p_2 \cdot eff_{hmm}}{2 \cdot \pi} = 362.946 \text{ J}$$

$$F_2 := \frac{T_{m2} \cdot i_g \cdot eff_g}{R_{wheel}} = 9.189 \text{ kN}$$

$$v_2 := \frac{2 \cdot \pi \cdot n_{mmax} \cdot R_{wheel}}{i_g} = 25.02 \frac{\text{km}}{\text{hr}} \quad (\text{same}) \quad n_{p2} := 12566.3706 \frac{\text{rad}}{s}$$

$$F_2 \cdot v_2 = 63.861 \text{ kW} \quad \text{"power at point 2"}$$

DYNAMIC CHARACTERISTIC OF HST

D_{m1} displacement volume of motor

$$D_{m1} := \frac{V_{gm}}{2 \cdot \pi} = (3.422 \cdot 10^{-5}) \frac{m^3}{s}$$

C_t leakage coefficient of HST

$$C_{t0} := eff_{vp} \cdot (1 - eff_{vm}) \cdot n_p \cdot V_{gp1} + (1 - eff_{vp}) \cdot n_p \cdot V_{gp1} = (1.461 \cdot 10^{-4}) \frac{m^3}{s}$$

$$C_t := \frac{C_{t0}}{\Delta P_{max}} = (3.652 \cdot 10^{-12}) \frac{m^4 \cdot s}{kg}$$

$$B_e := 400 \text{ MPa}$$

V_1 dead volume under pressure between pump & motor
(assumed)

Corner Power

$$P_{cp} := V_{TOP} \cdot F_1 = 228.788 \text{ kW}$$

$$v := \left(0 \frac{m}{s}, 0.2 \frac{m}{s} \dots 6 \frac{m}{s} \right) = \begin{bmatrix} 0 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.8 \\ 1 \\ 1.2 \\ 1.4 \\ 1.6 \\ 1.8 \\ 2 \\ 2.2 \\ \vdots \end{bmatrix} \frac{m}{s}$$

$$v_{ao} := v + 1.5 \frac{m}{s}$$

$$F(v) := \frac{Q_{p2} \cdot eff_{vm} \cdot p_2 \cdot eff_{hmm} \cdot eff_g}{v_{ao}} = \begin{bmatrix} 4.257 \cdot 10^4 \\ 3.757 \cdot 10^4 \\ 3.361 \cdot 10^4 \\ 3.041 \cdot 10^4 \\ 2.777 \cdot 10^4 \\ 2.554 \cdot 10^4 \\ 2.365 \cdot 10^4 \\ 2.202 \cdot 10^4 \\ 2.06 \cdot 10^4 \\ 1.935 \cdot 10^4 \\ 1.825 \cdot 10^4 \\ 1.726 \cdot 10^4 \\ \vdots \end{bmatrix} N$$

“Reynolds number/hoses, laminar flow”

$$v_n := 100 \frac{mm^2}{s} = (1 \cdot 10^{-4}) \frac{m^2}{s} \quad \text{“kinematic oil viscosity at temperature } 15^\circ C \text{”}$$

$$R_e := 2450$$

$$\rho_n := 0.876 \frac{kg}{L} = 876 \frac{kg}{m^3}$$

“oil density at $15^\circ C$ ”

“LINK 3: <http://www.hydroscand.co.uk/storage/ma/a3e942dd69f04b0c8f47c5e13db78355/3faa6b2/>

“Dynamic viscosity”

$$\mu_n := v_n \cdot \rho_n = 0.088 \frac{kg}{m \cdot s}$$

$$A_n := \frac{R_e \cdot \mu_n}{\rho_n} = 0.245 \frac{m^2}{s}$$

$$Q_{max} := .004 \frac{m^3}{s}$$

$$v_{ao} := \frac{A_n^2 \cdot \pi}{Q_{max} \cdot 4} = 11.786 \frac{m}{s}$$

$$A := \left(\frac{A_n}{2 \cdot v_{ao}} \right)^2 \cdot \pi = (3.394 \cdot 10^{-4}) m^2$$

$$D_{hoses1} := \frac{A_n}{v_{ao}} = 0.021 m$$

LINK3 “<http://www.gates.com/~media/files/gates/industrial/>

$$D_{hoses} := 0.0254 m$$

“from link 3”

$$V_1 := \frac{\pi}{4} \cdot D_{hoses}^2 \cdot L_{hoses} = (7.601 \cdot 10^{-4}) \text{ m}^3$$

J_L Moment of Inertia

$$J_L := M_{mass} \cdot R_{wheel}^2 = (3.179 \cdot 10^3) \text{ kg} \cdot \text{m}^2$$

$$J_{red} := \frac{J_L}{i_g^2} = 13.231 \text{ kg} \cdot \text{m}^2$$

B_t velocity dependent dynamic damping

$$\omega_1 := \frac{v_2}{R_{wheel}} = 11.583 \frac{1}{s}$$

$$B_t := \frac{0.5 \cdot T_{m2}}{\omega_1 \cdot i_g} = 1.011 \frac{N \cdot m \cdot s}{rad}$$

C_1 Hydraulic Capacitance of dead volume

$$C_1 := \frac{V_1}{B_e} = (1.9 \cdot 10^{-12}) \frac{\text{m}^3}{Pa}$$

$$\omega_h := \sqrt{\frac{D_{m1}^2 \cdot i_g^2 + C_t \cdot B_t}{J_L \cdot C_1}} = 6.824 \frac{rad}{s}$$

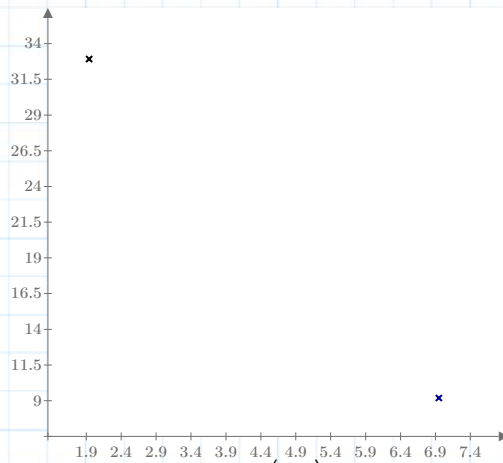
$$\delta_g := \frac{C_t}{2} \cdot \sqrt{\frac{J_L}{C_1 \cdot (D_{m1}^2 \cdot i_g^2 + C_t \cdot B_t)}} + \frac{B_t}{2} \cdot \sqrt{\frac{C_1}{J_L \cdot (D_{m1}^2 \cdot i_g^2 + C_t \cdot B_t)}} = 0.141$$

“natural frequency obtained from simulation”

$$T_1 := 26.62 \text{ s} - 25.7 \text{ s} = 0.92 \text{ s}$$

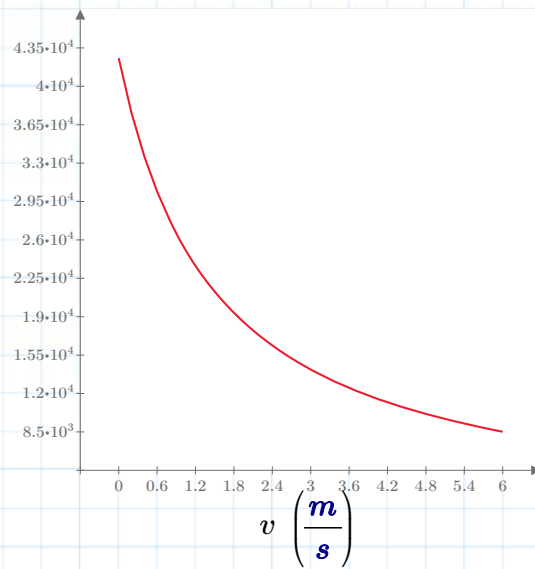
$$f_{sim} := \frac{1}{T_1} = 1.087 \frac{1}{\text{s}}$$

$$f_{sim1} := 2 \cdot \pi \cdot f_{sim} = 6.83 \frac{\text{rad}}{\text{s}}$$



$$\frac{F_2 \text{ (kN)}}{F_1 \text{ (kN)}}$$

$$\frac{v_2 \left(\frac{\text{m}}{\text{s}} \right)}{v_1 \left(\frac{\text{m}}{\text{s}} \right)}$$



$$\underline{F(v) \text{ (N)}}$$

“Heat Exchanger of the machine”

$$Q_{leakagep\ell m} := C_{t0} = (1.461 \cdot 10^{-4}) \frac{m^3}{s}$$

$$P_{leak} := Q_{leakagep\ell m} \cdot \Delta P_{max} = (5.843 \cdot 10^3) \text{ W}$$

$$T_{oil} := 50 \text{ }^{\circ}\text{C} \quad T_{ambient} := 10 \text{ }^{\circ}\text{C} \quad \Delta T := T_{oil} - T_{ambient} = 40 \text{ K}$$

$$C_{heat} := \frac{P_{leak}}{\Delta T} = 146.082 \frac{W}{K}$$

“Link4:<https://www.hydac.com/de-en/products/heat-exchangers-coolers/show/Download>

“HEAT EXCHANGER” “OK-ELH 3”

“ENGINE BRAKING ”

$$\varepsilon_m := 1$$

$$P_{braking} := 0.1 \cdot P_{hsm} = (7.756 \cdot 10^3) \text{ W}$$

$$P_{valve} := P_{hsm} - P_{braking} = (6.98 \cdot 10^4) \text{ W}$$

“Force exerted by the car in downhill”

$$F_{car} := M_{mass} \cdot g \cdot \sin(7) = 56.89 \text{ kN}$$

$$T_{wheel} := F_{car} \cdot R_{wheel} = (3.413 \cdot 10^4) \text{ J} \quad \text{“Torque at the wheel”}$$

$$T_{motor} := \frac{T_{wheel}}{i_g} = (2.202 \cdot 10^3) \text{ J} \quad \text{“Torque at the motor”}$$

$$\Delta P_{motor} := \frac{T_{motor} \cdot 2 \cdot \pi}{V_{gm} \cdot \varepsilon_m} = 643.575 \text{ bar}$$

“The power lost in the Hydraulic pump is 10% of the Hydrostatic power”