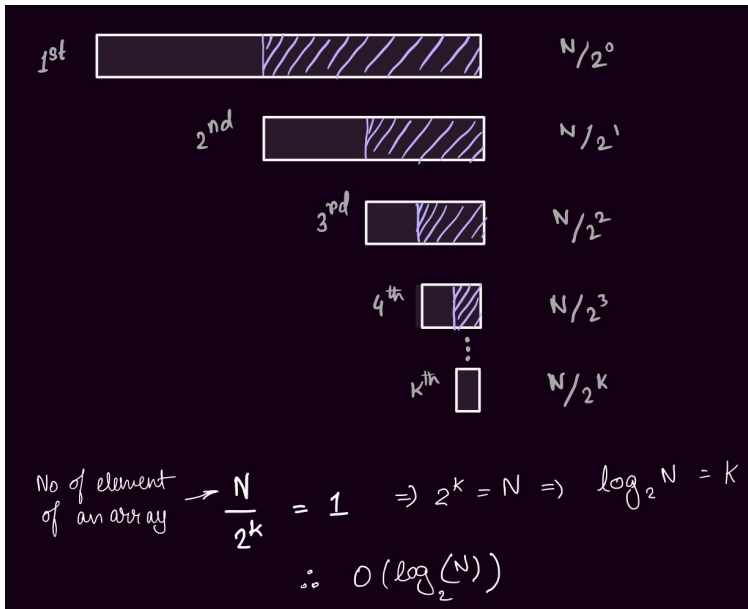


Binary Search

Time Complexity :

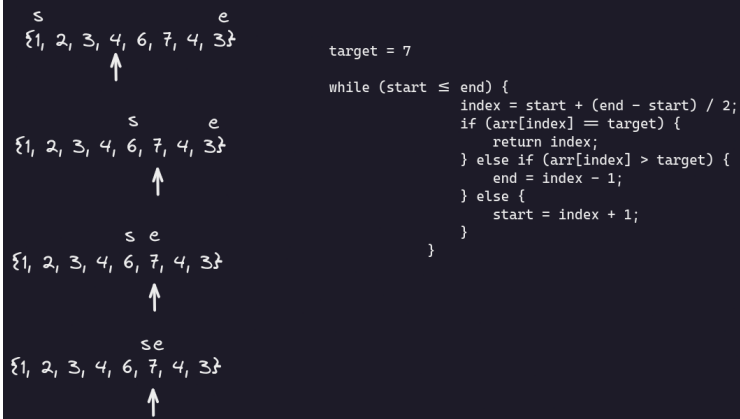
- Best Case : $O(1)$
- Worst Case : $O(\log(n))$ [where n is number of element in the array]



Steps for Binary Search :

1. Find the middle element.
 2. Compare the target element with the middle element :
 - a. if target element > middle element :
 1. if Ascending Array : search in left side of the array.
 2. if Descending Array : search in right side of the array.
 - b. if target element < middle element :
 1. if Ascending Array : search in right side of the array.
 2. if Descending Array : search in left side of the array.
 - c. if target element = middle element :
 1. return element
- Q1. Binary Search

Binary Search



```
package com.inclass;

public class BinarySearch {

    public static void main(String[] args) {
        /*
        Binary Search: (given sorted array (say ascending))
        1. find the middle element
        2. if middle element == target element: ans
        3. if middle element > target: search left
           else middle element < target: search right
        */
        int[] arr = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
        int target = 3;
        // int[] arr = {48, 36, 20, 14, 12, 11, 9, 6, 4, 2};
        // int target = 36;
        if (arr[0] >= arr[arr.length - 1]) {
            System.out.println(binarySearchDes(arr, target));
        } else {
            System.out.println(binarySearchAsc(arr, target));
        }
    }

    // Binary Search for Ascending Sorted Array
    static int binarySearchAsc(int[] arr, int target) {
        int start = 0;
        int end = arr.length - 1;
        int index = 0;
        while (start <= end) {
            index = start + (end - start) / 2;
            if (arr[index] == target) {
                return index;
            } else if (arr[index] > target) {
                end = index - 1;
            } else {
                start = index + 1;
            }
        }
        return -1;
    }

    // Binary Search for Descending Sorted Array
    static int binarySearchDes(int[] arr, int target) {
        int start = 0;
```

```

int end = arr.length - 1;
int index = 0;
while (start ≤ end) {
    index = start + (end - start) / 2;
    if (arr[index] == target) {
        return index;
    } else if (arr[index] < target) {
        end = index - 1;
    } else {
        start = index + 1;
    }
}
return -1;
}
}

```

– Q2. Ceiling Element

```

int[] arr = {2, 3, 5, 9, 14, 16, 18};
int target = 15;

```

```

s      m      e
{2, 3, 5, 9, 14, 16, 18}      start = mid + 1

           s      m      e
{2, 3, 5, 9, 14, 16, 18}      end = mid - 1

           e
           m
           s
{2, 3, 5, 9, 14, 16, 18}      start = mid + 1

           e
           m      s
{2, 3, 5, 9, 14, 16, 18}      return start

```

```

package com.questions;

import java.util.Scanner;

public class Ceiling {
    public static void main(String[] args) {
        int[] arr = {2, 3, 5, 9, 14, 16, 18};
        Scanner in = new Scanner(System.in);
        int target = in.nextInt();
        if (target > arr[arr.length - 1]) {
            System.out.println("No Result Found !");
        } else {
            System.out.println(ceiling(arr, target));
        }
    }

    static int ceiling(int[] arr, int target) {
        int start = 0;
        int end = arr.length - 1;
        int index = 0;
        while (start ≤ end) {
            index = start + (end - start) / 2;
            if (arr[index] == target) {
                return arr[index];
            }
        }
    }
}

```

```

    }
    else if (arr[index] > target) {
        end = index - 1;
    }
    else {
        start = index + 1;
    }
}
return arr[start];
}
}

```

– Q3. Floor Element

```

int[] arr = {2, 3, 5, 9, 14, 16, 18};
int target = 15;

s      m      e      start = mid + 1
{2, 3, 5, 9, 14, 16, 18}

           s      m      e      end = mid - 1
{2, 3, 5, 9, 14, 16, 18}

           e
           m
           s      start = mid + 1
{2, 3, 5, 9, 14, 16, 18}

           e
           m      s      return end
{2, 3, 5, 9, 14, 16, 18}

```

```

package com.questions;

import java.util.Scanner;

public class Floor {

    public static void main(String[] args) {
        int[] arr = {2, 3, 5, 9, 14, 16, 18};
        Scanner in = new Scanner(System.in);
        int target = in.nextInt();
        if (target < arr[0]) {
            System.out.println("No Result Found !");
        }
        else {
            System.out.println(floor(arr, target));
        }
    }

    static int floor(int[] arr, int target) {
        int start = 0;
        int end = arr.length - 1;
        int index;
        while (start ≤ end) {
            index = start + (end - start) / 2;
            if (arr[index] == target) {
                return arr[index];
            }
            else if (arr[index] > target) {
                end = index - 1;
            }
        }
    }
}

```

```

    }
    else {
        start = index + 1;
    }
}
return arr[end];
}
}

```

– Q4. Find First and Last position of element in Sorted Array

```

package com.questions;

import java.util.Arrays;

// <https://leetcode.com/problems/find-first-and-last-position-of-element-in-sorted-array/>

public class FirstLastIndex {

    public static void main(String[] args) {
        System.out.println(Arrays.toString(selfAttempt()));
        System.out.println(Arrays.toString(solution()));
    }

    /* Self Attempt:
    Runtime: 0 ms, faster than 100.00% of Java online submissions for Find First and Last
    Position of Element in Sorted Array.
    Memory Usage: 42.4 MB, less than 54--92% of Java online submissions for Find First and
    Last Position of Element in Sorted Array.
    */
    static int[] selfAttempt() {
        int[] nums = {5, 7, 7, 8, 8, 8, 10};
        int target = 8;
        int index = firstLastIndex(nums, target);
        int first = firstIndex(nums, target, index);
        int last = lastIndex(nums, target, index);
        return new int[]{first, last};
    }

    static int firstLastIndex(int[] nums, int target) {
        int start = 0;
        int end = nums.length - 1;
        int index = 0;
        while (start ≤ end) {
            index = start + (end - start) / 2;
            if (nums[index] < target) {
                start = index + 1;
            } else if (nums[index] > target) {
                end = index - 1;
            } else {
                return index;
            }
        }
        return -1;
    }

    static int firstIndex(int[] nums, int target, int index) {
        int temp = index;
        for (int i = index; i ≥ 0; i--) {
            if (nums[i] ≠ target) {

```

```

        return i + 1;
    }
    else {
        temp = i;
    }
}
return temp;
}

```

```

static int lastIndex(int[] nums, int target, int index) {
    int temp = index;
    for (int i = index; 0 ≤ i && i < nums.length; i++) {
        if (nums[i] ≠ target) {
            return i - 1;
        }
        else{
            temp = i;
        }
    }
    return temp;
}

```

/* Solution:

Runtime: 0 ms, faster than 100.00% of Java online submissions for Find First and Last Position of Element in Sorted Array.

Memory Usage: 44 MB, less than 28.93% of Java online submissions for Find First and Last Position of Element in Sorted Array.

```

*/
static int[] solution() {
    int[] nums = {5, 7, 7, 8, 8, 8, 10};
    int target = 8;
    int start = binarySearch(nums, target, true);
    int end = binarySearch(nums, target, false);
    return new int[] {start, end};
}

static int binarySearch(int[] nums, int target, boolean firstIndex) {
    int index;
    int start = 0;
    int end = nums.length - 1;
    int ans = -1;
    while (start ≤ end) {
        index = start + (end - start) / 2;
        if (nums[index] < target) {
            start = index + 1;
        } else if (nums[index] > target) {
            end = index - 1;
        } else {
            ans = index;
            if (firstIndex) {
                end = index - 1;
            } else {
                start = index + 1;
            }
        }
    }
    return ans;
}
}

```

- Q5. Find position of an element in a sorted array of infinite array

```
package com.questions;

import java.lang.Math;

public class IndexInfiniteArray {

    public static void main(String[] args) {
        System.out.println(solution());
    }

    static int solution() {
        int[] nums = new int[100];
        for (int i = 0; i < 100; i++) {
            nums[i] = i;
        }
        int target = 13;
        return findRange(nums, target);
    }

    static double log2(int num) {
        return Math.log(num)/Math.log(2);
    }

    static int findRange(int[] nums, int target) {
        int start = 0;
        int end = 0;
        int range = (int) log2(nums.length);
        while(start ≤ end) {
            while (range ≥ 0) {
                if ((nums.length - start + 1) - Math.pow(2, range) ≥ 0) {
                    end = start + (int) Math.pow(2, range) - 1;
                    range--;
                    break;
                }
                range--;
            }
            if (target == nums[end]){
                return end;
            } else if (target < nums[end]){
                return binarySearch(nums, target, start, end - 1);
            } else {
                start = end + 1;
            }
        }
        return -1;
    }

    static int binarySearch(int[] nums, int target, int tempstart, int tempend) {
        while (tempstart ≤ tempend) {
            int index = tempstart + (tempend - tempstart) / 2;
            if (target < nums[index]) {
                tempend = index - 1;
            }
            else if (target > nums[index]) {
                tempstart = index + 1;
            }
            else {
                return index;
            }
        }
    }
}
```

```

    }
    }
    return -1;
}
}

```

– Q6. Peak Index in Mountain Array

```

package com.questions;

public class PeakIndexMountainArray {

    // <https://leetcode.com/problems/peak-index-in-a-mountain-array/submissions/>

    public static void main(String[] args) {
        int[] arr = {1, 2, 3, 4, 6, 7, 4, 3, 2, 1};
        System.out.println(solution2(arr));
    }

    /* Solution2 (Error: {1, 2, 2, 3, 1}:
    Runtime: 0 ms, faster than 100.00% of Java online submissions for Peak Index in a Mountain
    Array.
    Memory Usage: 39 MB, less than 89.22% of Java online submissions for Peak Index in a
    Mountain Array.
    */
    // original solution
    static int solution2 (int[] arr) {
        int start = 0;
        int end = arr.length - 1;

        while (start < end) {
            int mid = start + (end - start) / 2;
            if (arr[mid] > arr[mid+1]) {
                end = mid;
            } else {
                start = mid + 1;
            }
        }
        return start;
    }
}

```

– Q7. Search in Rotated Sorted Array

Search in Rotated Sorted Array

{ 2, 4, 5, 7, 8, 9, 10, 12 }

{ 12, 2, 4, 5, 7, 8, 9, 10 }

{ 10, 12, 2, 4, 5, 7, 8, 9 }

Find pivot

$\{ 10, 12, 2, 4, 5, 7, 8, 9 \}$
 asc asc

Finding pivot :

$\{ 10, 12, 2, 4, 5, 7, 8, 9 \}$



Case 1 : $arr[index] > arr[index + 1]$
 return index

$\{ 10, 12, 2, 4, 5, 7, 8, 9 \}$



Case 2 : $arr[index + 1] > arr[index]$
 return index + 1

$\{ 10, 12, 2, 4, 5, 7, 8, 9 \}$



Case 3 : $arr[index] \leq arr[start]$
 end = index - 1

$\{ 10, 12, 2, 4, 5, 7, 8, 9 \}$



Case 4 : else ($arr[index] \geq arr[end]$)
 start = index + 1

For duplicate values (without pivot) :

$\{ 10, 11, 12, 5, 7, 8, 9 \}$
 s e



$\{ 10, 12, 2, 4, 4, 4, 4 \}$
 s e



Right Side
is Sorted

Case 1 : $arr[index] < arr[end] \parallel arr[index] < arr[start]$

Case 1.1 : $arr[index] < target \leq arr[end]$
 start = index + 1

Case 1.2 : else ($arr[start] \leq target < arr[index]$)
 end = index - 1

$\{ 10, 12, 2, 4 \}$
 s e



$\{ 10, 10, 10, 4, 5, 7 \}$
 s e



Case 2 : $arr[index] > arr[end] \parallel arr[index] > arr[start]$

Case 2.1 : $arr[end] \leq target < arr[index]$
 end = index - 1

Case 2.2 : else ($arr[index] < target \leq arr[start]$)
 start = index + 1

Left Side
is Sorted

$\{ 3, 2, 3, 2, 3 \}$

Case 3 : else (arr[start] == arr[index] == arr[end])
end --;

```
package com.questions;

public class TargetRotatedSortedArray {

    // <https://leetcode.com/problems/search-in-rotated-sorted-array/>

    public static void main(String[] args) {
        int[] arr = {1,1,1,1,1,1,1,1,1,1,1,1,2,1,1,1,1,1};
        int target = 2;
        System.out.println(selfAttempt(arr, target));
        System.out.println(solution(arr, target));
        System.out.println(bestSolution(arr, target));
        System.out.println(search(arr, target));
    }

    /* Self Attempt:
    Runtime: 0 ms, faster than 100.00% of Java online submissions for Search in Rotated Sorted
    Array.
    Memory Usage: 39.7 MB, less than 11.53% of Java online submissions for Search in Rotated
    Sorted Array.
    */
    static int selfAttempt(int[] arr, int target) {
        int peak = peak(arr);
        if (target ≥ arr[0]) {
            return binarySearch(arr, target, 0, peak);
        } else {
            return binarySearch(arr, target, peak + 1, arr.length - 1);
        }
    }

    static int peak(int[] arr) {
        int start = 0;
        int end = arr.length - 1;
        if (arr[start] < arr[end]) {
            return end;
        } else {
            while (start < end) {
                int index = start + (end - start) / 2;
                if (arr[index] > arr[start]) {
                    start = index;
                } else {
                    end = index;
                }
            }
            return start;
        }
    }

    static int binarySearch(int[] arr, int target, int start, int end){
        while (start ≤ end) {
            int index = start + (end - start) / 2;
            if (target < arr[index]) {
                end = index - 1;
            }
        }
    }
}
```

```

        } else if (target > arr[index]) {
            start = index + 1;
        } else {
            return index;
        }
    }
    return -1;
}

/* Solution:

*/
static int solution(int[] arr, int target) {
    int pivot = findPivot(arr);
    if (pivot == -1) {
        return binarySearch(arr, target, 0, arr.length - 1);
    } else {
        if (arr[pivot] == target) {
            return pivot;
        } else if (target > arr[0]) {
            return binarySearch(arr, target, 0, pivot);
        } else {
            return binarySearch(arr, target, pivot + 1, arr.length - 1);
        }
    }
}

```

```

static int findPivot(int[] arr) {
    int start = 0;
    int end = arr.length - 1;
    while(start <= end) {
        int index = start + (end - start) / 2;
        if (index < end && arr[index] > arr[index + 1]) {
            return index;
        } else if (index > start && arr[index - 1] > arr[index]) {
            return index - 1;
        } else if (arr[index] == arr[start] && arr[index] == arr[end]) {
            start++;
            end--;
        } else if (arr[index] <= arr[start]) {
            end = index - 1;
        } else if (arr[index] >= arr[end]) {
            start = index + 1;
        } else if (arr[start] == arr[end]) {
            start++;
            end--;
        }
    }
    return -1;
}

```

/* Best Solution (no need to find peak, works with duplicates) :

Runtime: 0 ms, faster than 100.00% of Java online submissions for Search in Rotated Sorted Array.

Memory Usage: 39.2 MB, less than 42.77% of Java online submissions for Search in Rotated Sorted Array.

```

*/
static int bestSolution (int[] arr, int target) {
    int start = 0;
    int end = arr.length - 1;

```

```

while (start ≤ end) {
    int mid = start + (end - start) / 2;
    if (arr[mid] == target) {
        return target;
    } else if (arr[start] > target) {
        if (arr[mid] > target) {
            start = mid + 1;
        } else {
            end = mid - 1;
        }
    } else {
        if (arr[mid] < target) {
            start = mid + 1;
        } else {
            end = mid - 1;
        }
    }
}
return -1;
}

static int search(int[] nums, int target) {
    int pivot = findPivotKunal(nums);
    // if you did not find a pivot, it means the array is not rotated
    if (pivot == -1) {
        // just do normal binary search
        return binarySearch(nums, target, 0, nums.length - 1);
    }
    // if pivot is found, you have found 2 asc sorted arrays
    if (nums[pivot] == target) {
        return pivot;
    }
    if (target ≥ nums[0]) {
        return binarySearch(nums, target, 0, pivot - 1);
    }
    return binarySearch(nums, target, pivot + 1, nums.length - 1);
}

// this will not work in duplicate values
static int findPivotKunal(int[] arr) {
    int start = 0;
    int end = arr.length - 1;
    while (start ≤ end) {
        int mid = start + (end - start) / 2;
        // 4 cases over here
        if (mid < end && arr[mid] > arr[mid + 1]) {
            return mid;
        }
        if (mid > start && arr[mid] < arr[mid - 1]) {
            return mid-1;
        }
        if (arr[mid] ≤ arr[start]) {
            end = mid - 1;
        } else {
            start = mid + 1;
        }
    }
    return -1;
}

```

```

static int findPivotWithDuplicates(int[] arr) {
    int start = 0;
    int end = arr.length - 1;
    while (start ≤ end) {
        int mid = start + (end - start) / 2;
        // 4 cases over here
        if (mid < end && arr[mid] > arr[mid + 1]) {
            return mid;
        }
        if (mid > start && arr[mid] < arr[mid - 1]) {
            return mid-1;
        }
        // if elements at middle, start, end are equal then just skip the duplicates
        if (arr[mid] == arr[start] && arr[mid] == arr[end]) {
            // skip the duplicates
            // NOTE: what if these elements at start and end were the pivot??
            // check if start is pivot
            if (start < end && arr[start] > arr[start + 1]) {
                return start;
            }
            start++;
            // check whether end is pivot
            if (end > start && arr[end] < arr[end - 1]) {
                return end - 1;
            }
            end--;
        }
        // left side is sorted, so pivot should be in right
        else if (arr[start] < arr[mid] || (arr[start] == arr[mid] && arr[mid] > arr[end]))
        {
            start = mid + 1;
        } else {
            end = mid - 1;
        }
    }
    return -1;
}

```

– Q8. Split Array Largest Sum

- Case 1: $m = 1$; \Rightarrow *sum of entire array*
- Case 2: $m = \text{size of array}$; \Rightarrow *maximum element of array*