

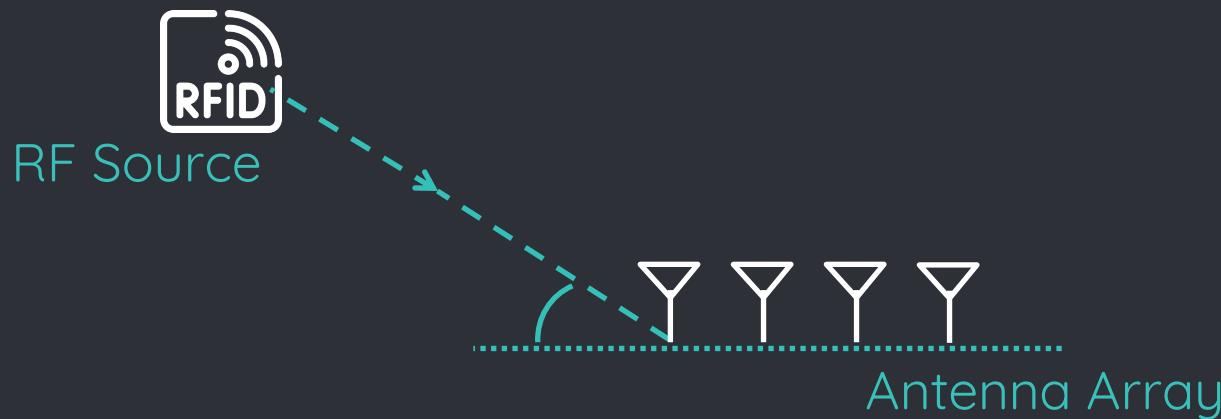


# **LSAB: Enhancing Spatio-Temporal Efficiency of AoA Tracking Systems**

Qingrui Pan, Zhenlin An, Qiongzheng Lin, and Lei Yang

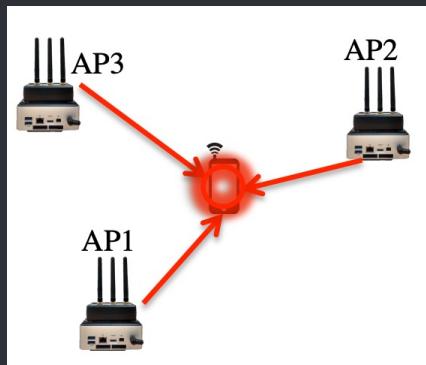
- ## AoA tracking System

- **Angle of arrival (AoA)** of a signal is the **direction** from which an RF signal is propagated.

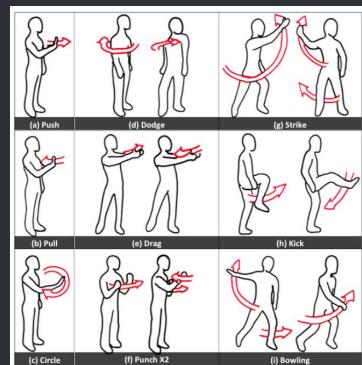


# • AoA tracking System

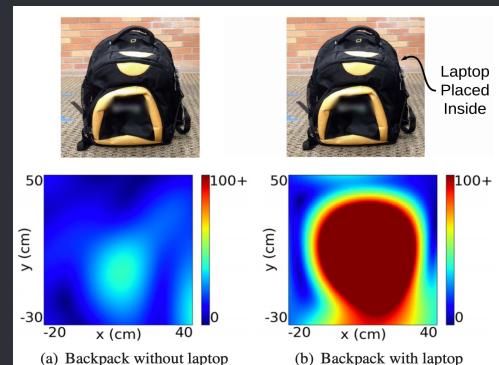
- AoA Systems facilitate a wide range of **wireless** applications like **localization** and **sensing**.



Localization and tracking



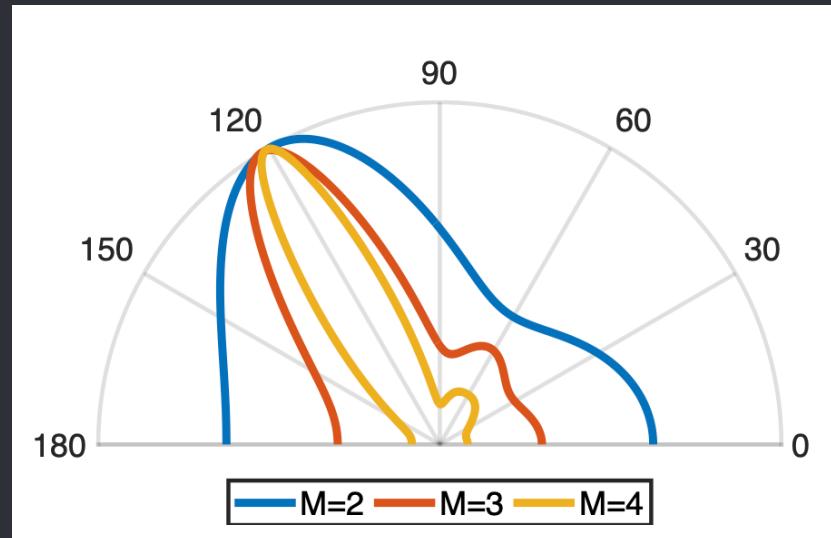
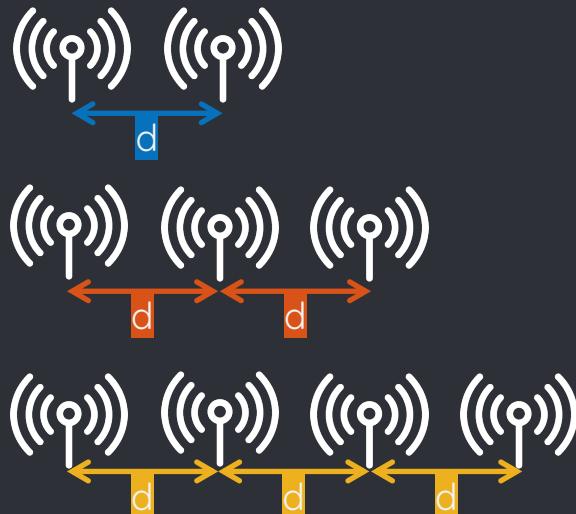
Activity Recognition



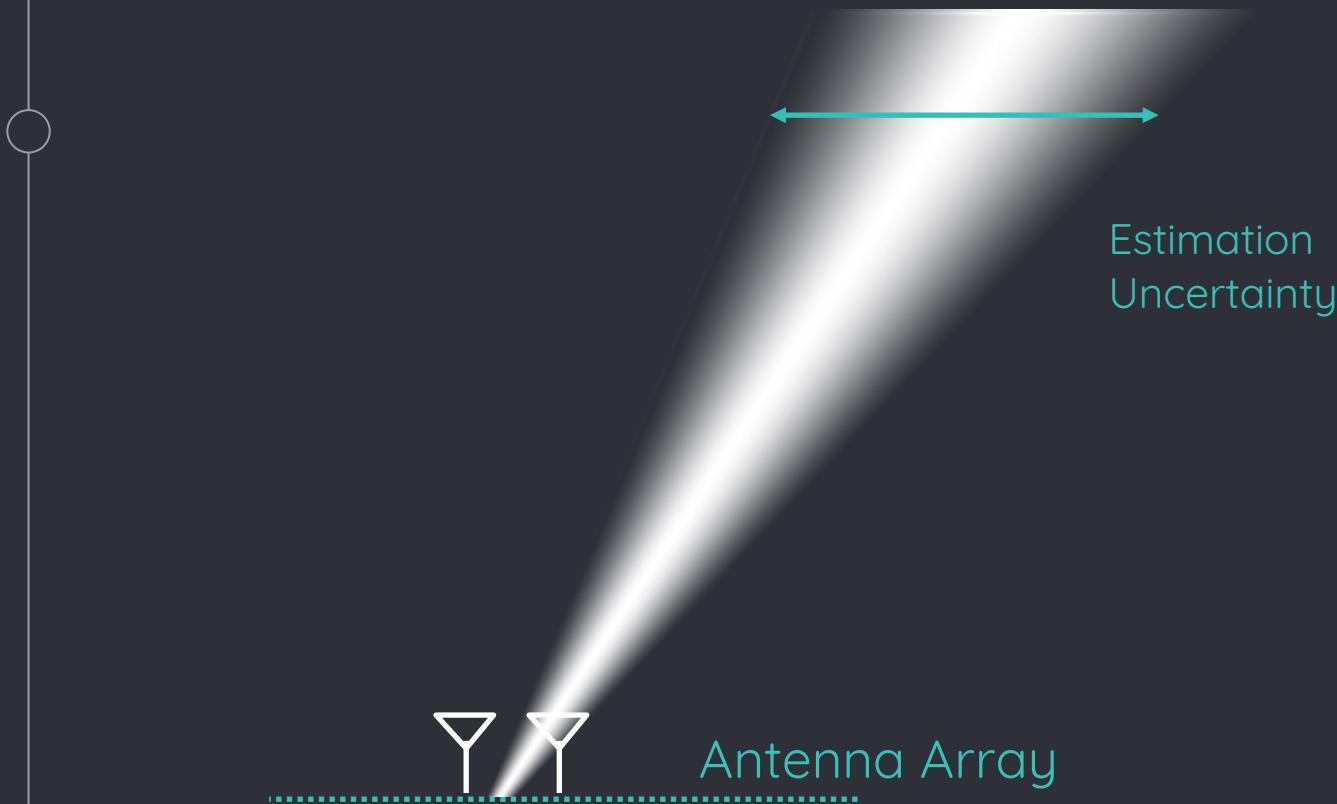
Wi-Fi Imaging

## • AoA tracking System

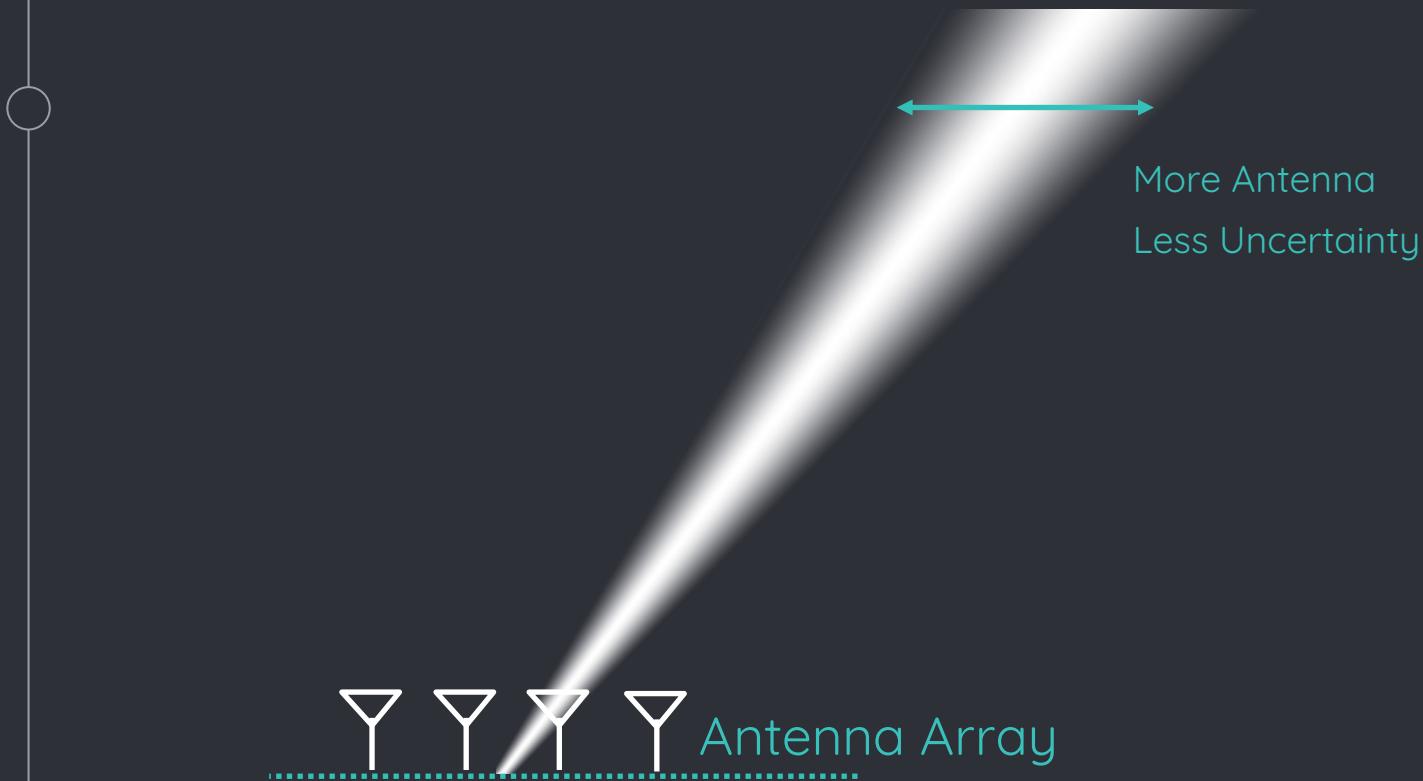
Number of antenna elements in a AoA System determine the **resolution** and **accuracy**.



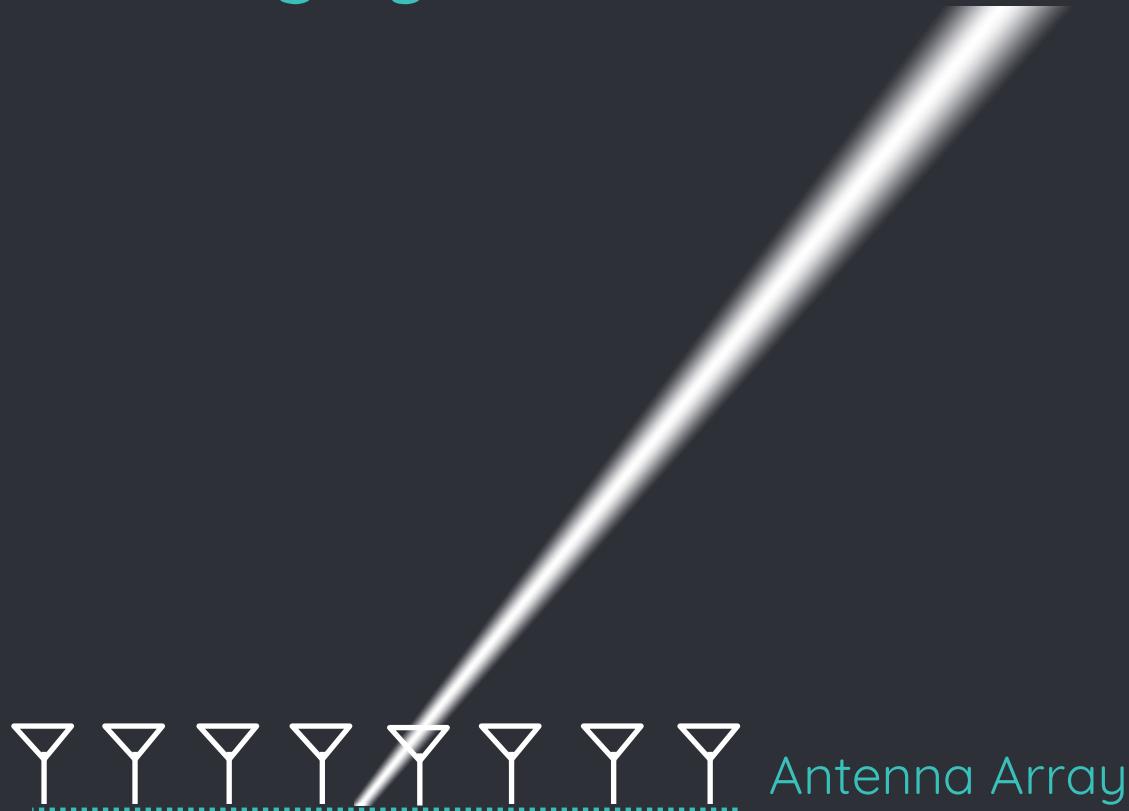
- **AoA tracking System**



- **AoA tracking System**



- **AoA tracking System**



- **AoA tracking System**

Not Practical!

Antenna Array



“

*Challenge:*

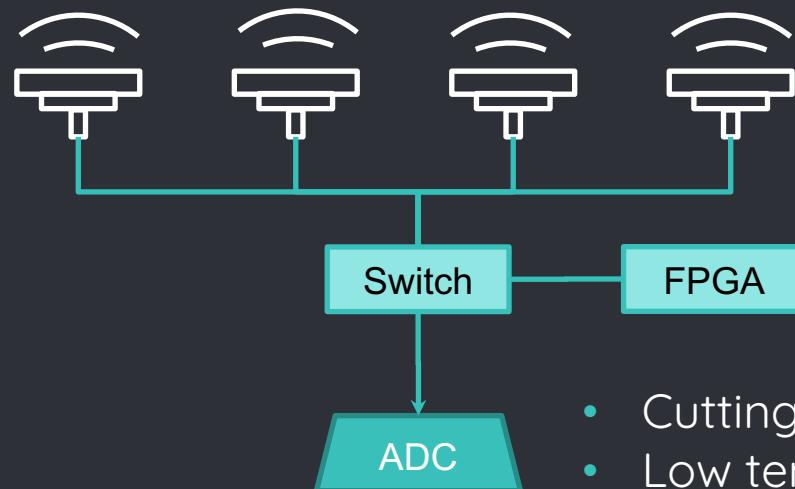
*How to cut the number of antenna array  
but keep the performance?*

- **State-of-the-art Solutions**

- RF Switches
- Virtual Linear/Circular Array
- Sparse Array

- ## State-of-the-art Solutions

- RF Switches



- Cutting the cost of frontend and ADC
- Low temporal efficiency

- ## State-of-the-art Solutions

- Virtual Linear/Circular Array
  - Cutting the cost of more components
  - Low temporal efficiency and movement error



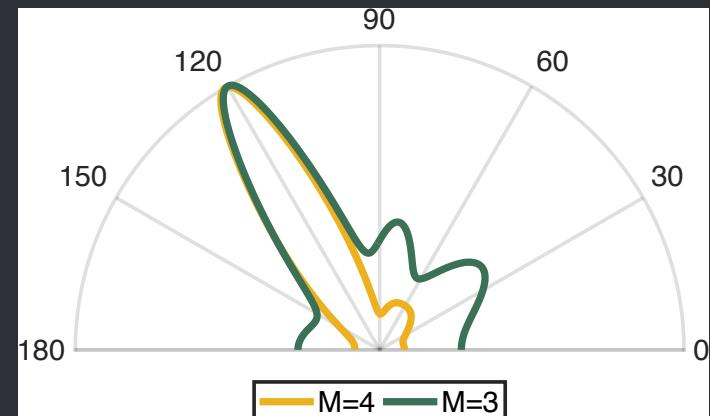
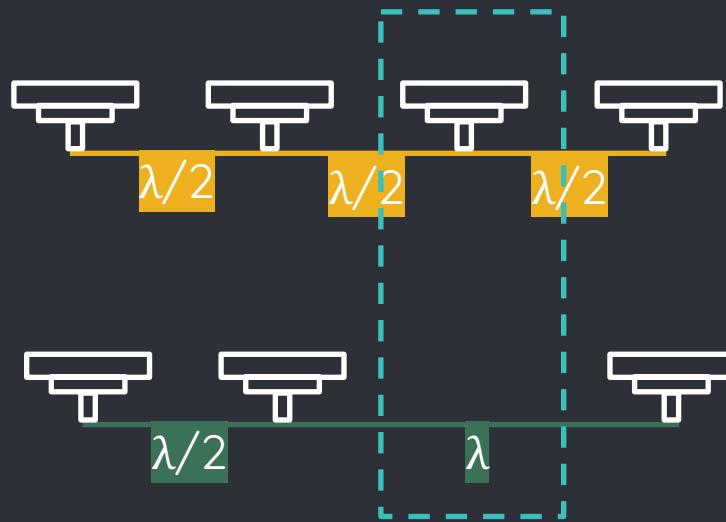
Moving at  $v$   
 $Rx/Tx$  at interval  $t$



Virtual Antenna Array spaced  $vt$

- # State-of-the-art Solutions

- Sparse Array



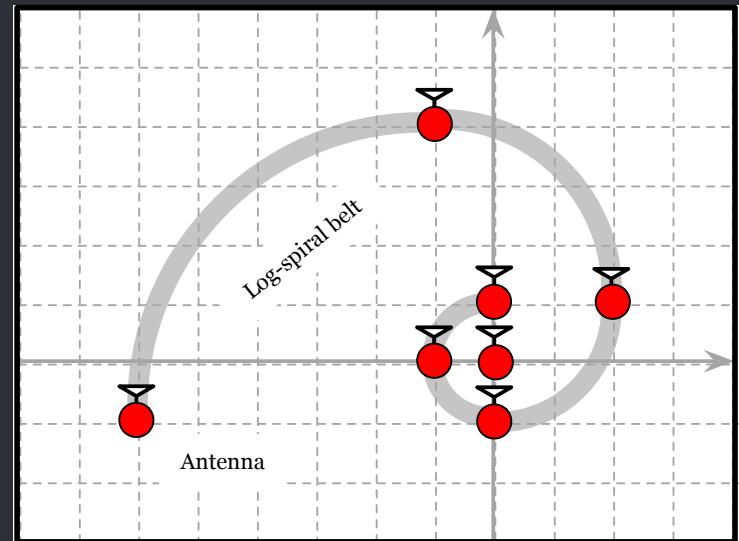
- ## State-of-the-art Solutions

	Advantage	Disadvantage
RF Switches	Cutting the cost of frontend and ADC	Low temporal efficiency and high cost on antenna elements
Virtual Linear/Circular Array	Cutting the cost of all other components	Low temporal efficiency and movement error
<b>Sparse Array</b>	<b>Cutting cost with high temporal efficiency</b>	<b>Lack of research in 2-D aspects</b>

## • Our Solution

### Log-Spiral Antenna Belt

- 2D sparse array
- Decrease antenna number
- Keep high accuracy and temporal efficiency

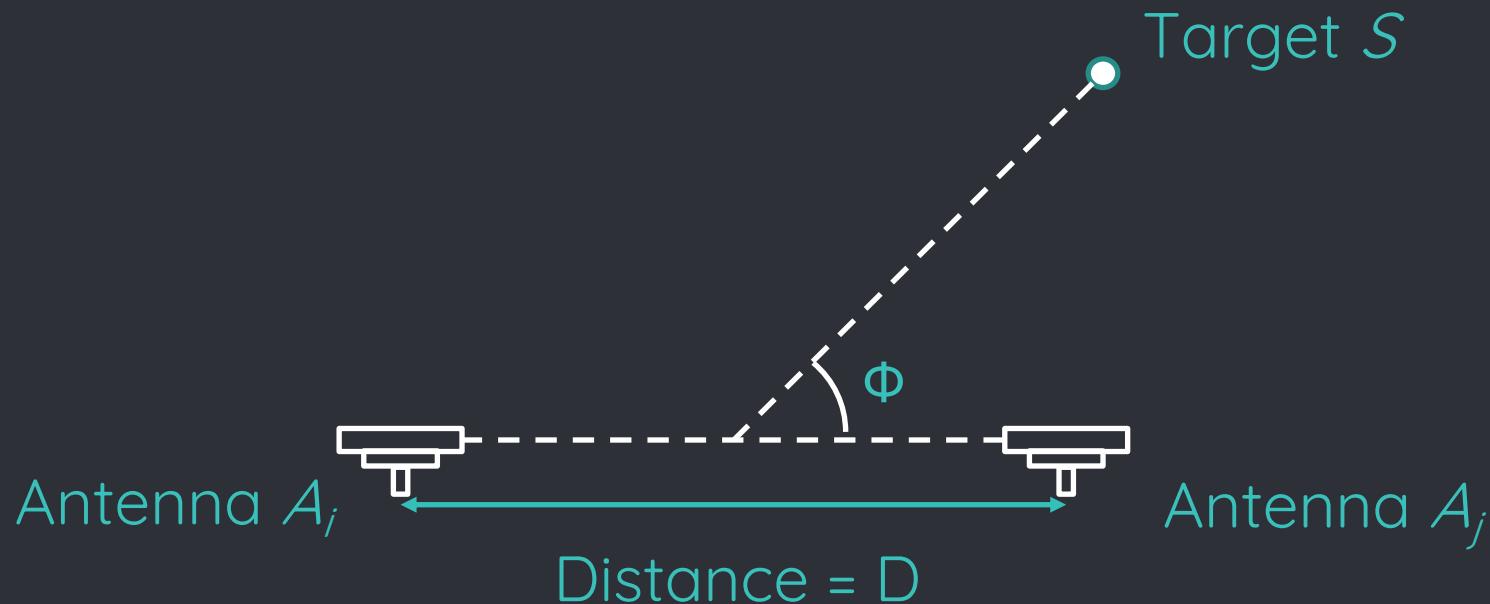


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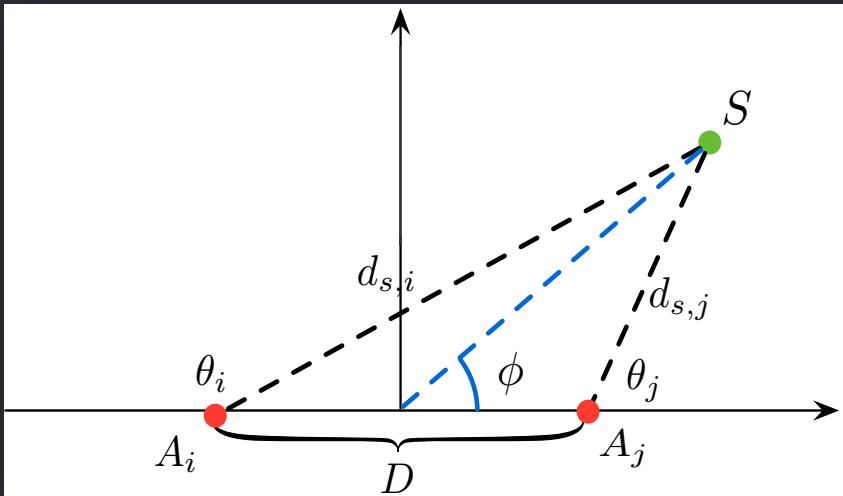
*Key Idea:*

*To evaluate redundancy in an antenna array  
by the placements of antenna elements*

- **Example: Antenna Array of two elements**



- ## AoA Estimation Model



$$\Delta d_{i,j} = d_{s,i} - d_{s,j}$$

$$\Delta \theta_{i,j} = \theta_{s,i} - \theta_{s,j}$$

$$\Delta \theta_{i,j} = 2\pi \Delta d_{i,j} / \lambda \bmod 2\pi$$

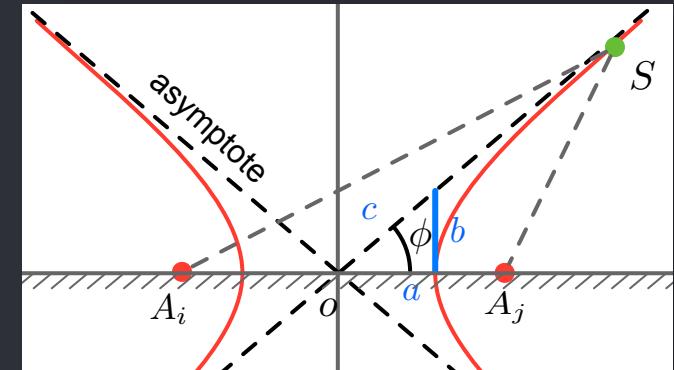


$$\Delta d_{i,j} = \lambda \Delta \theta_{i,j} / 2\pi + k\lambda$$

## • K and Estimation Ambiguity

Considering  $-D \leq \Delta d_{i,j} \leq D$

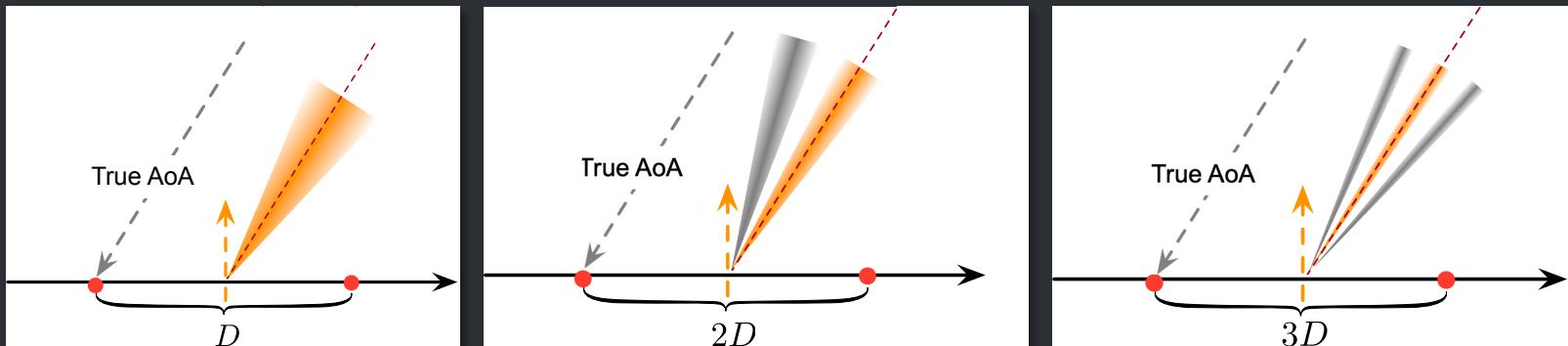
If  $D = K \cdot \lambda/2$  then:



$$\phi \approx \arccos\left(\frac{a}{c}\right) = \arccos\left(\frac{\Delta d_{i,j}}{c}\right) = \arccos\left(\frac{\lambda}{c} \Delta \theta_{i,j} \right) \quad k\lambda$$

Distance  $K \cdot \lambda/2$  results in K possible results,  
denoted as **K Ambiguity**

- ## K and Resolution Degree

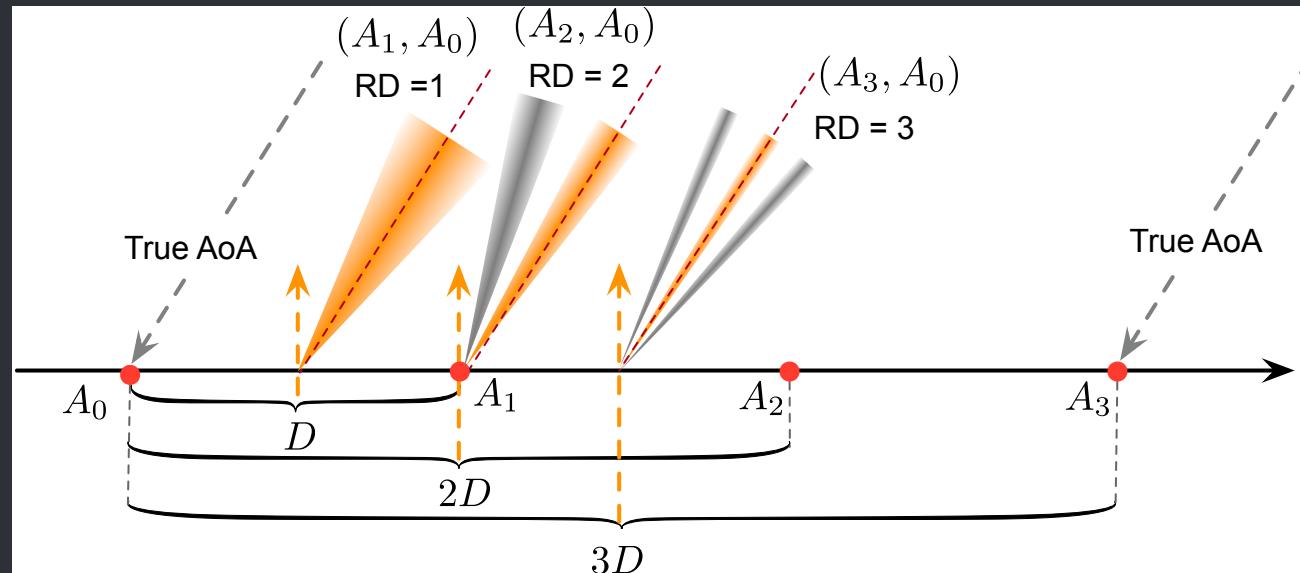


If we consider a phase noise in AoA estimation:

$\phi = \text{Distance } K \cdot \lambda/2$  decreases phase noise by  $K$  times,  
Denoted as **K Resolution Degree**

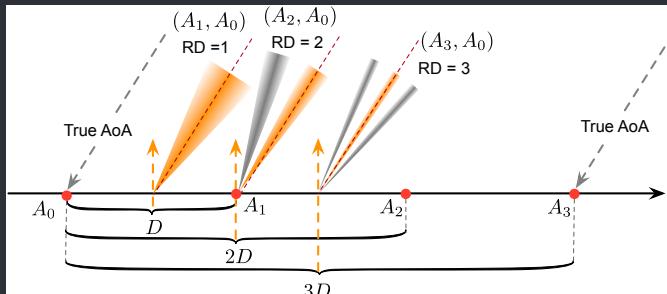
## • K and Antenna Array

Different element **pairs** in an antenna array cover different **Ambiguities** and **Resolution degrees**.

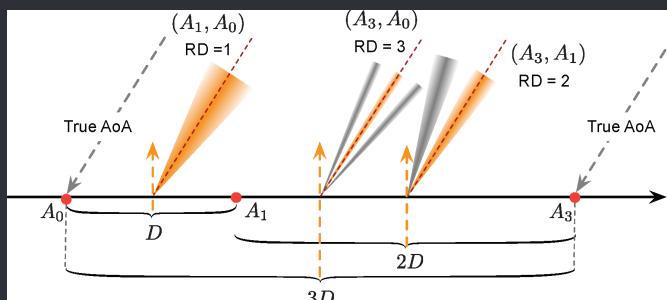


# Minimal-resolution-redundancy and Sparse Linear Array

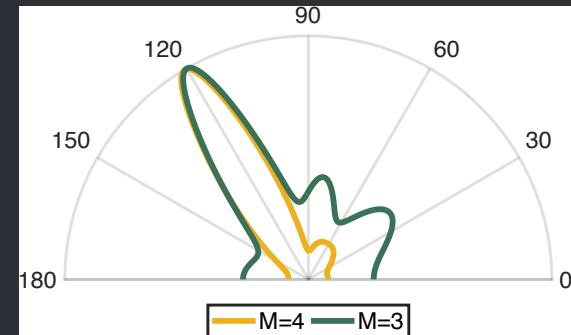
Covering all Ambiguity and Resolution Degree,  
Antenna Array share similar estimation results.



Uniform Linear Array  
(4 elements)

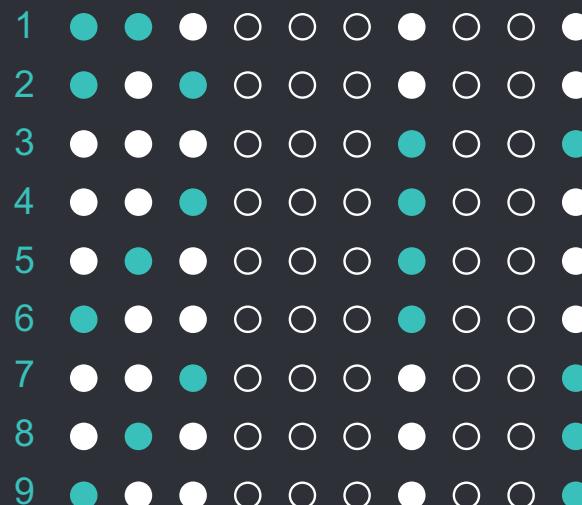


Sparse Linear Array  
(3 elements)



# • Other Sparse Antenna Arrays

## Sparse Linear Arrays

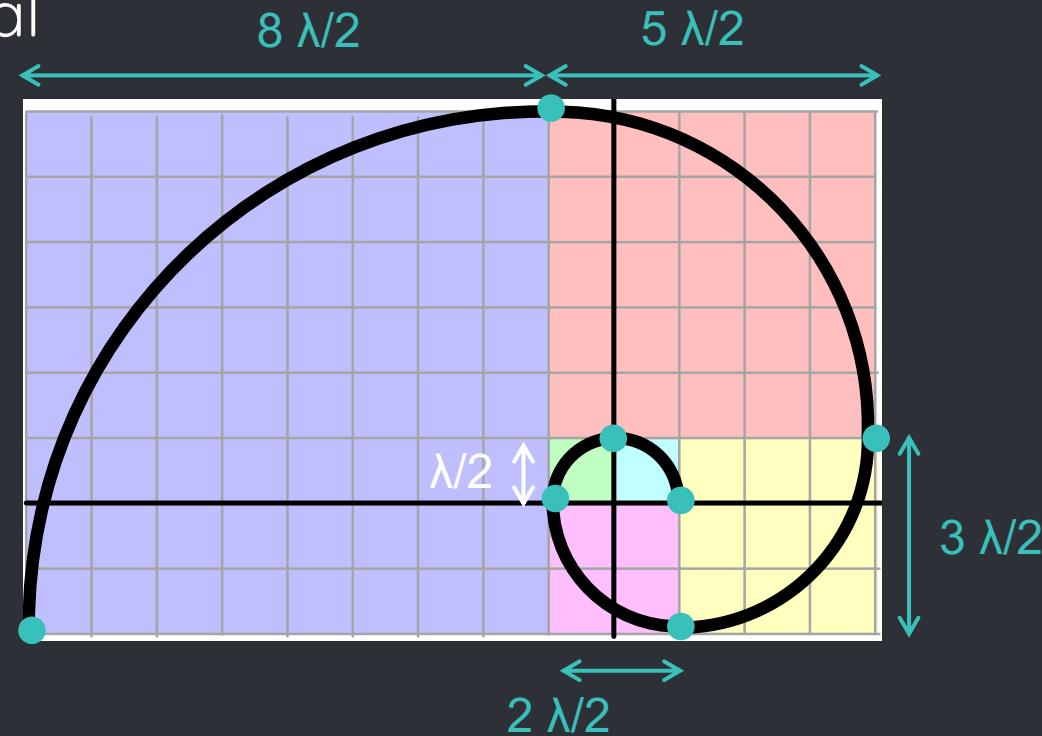


● denote antenna elements  
○ denotes empty space

M	Deployment	N	Degrees
2	●●	2	(1,2)
3	●●○●	3	(1,2,3)
4	●●○●●	5	(1,2,3,4)
5	●●●○○○○●○●	10	(1,2,3,...,8,9)
6	●●●●○○○○○○●●	14	(1,2,3,...,13)
7	●●●●●○○○○●○●●	18	(1,2,3,...,17)

- # Sparse Linear Array to LSAB

Fibonacci Spiral

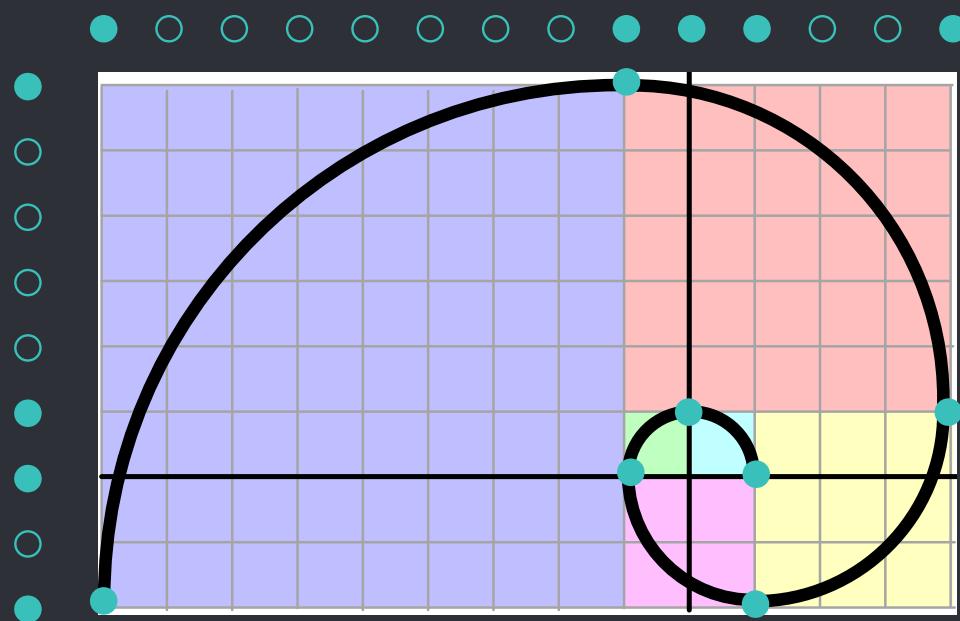


- # Sparse Linear Array to LSAB

- ## Fibonacci Spiral

$K=(1,2,3, ,5,6, ,8)$

$K=(1,2,3,4,5, , ,8,9,10, , ,13)$

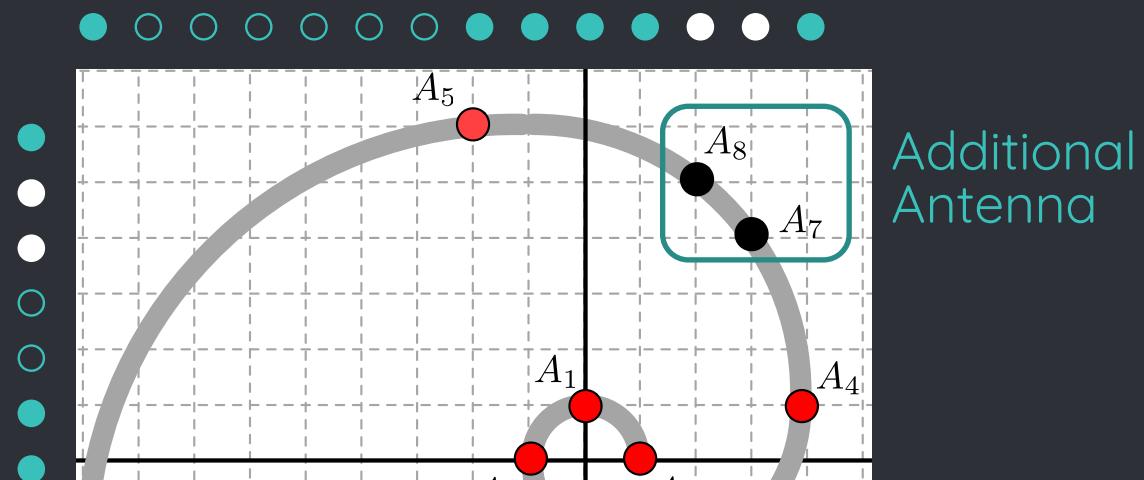


- # Sparse Linear Array to LSAB

Log-Spiral Antenna Belt

$K=(1,2,3,4,5,6,7,8,9,10,11,12,13)$

$K=$   
 $(1,2,3,4,5,6,7,8)$



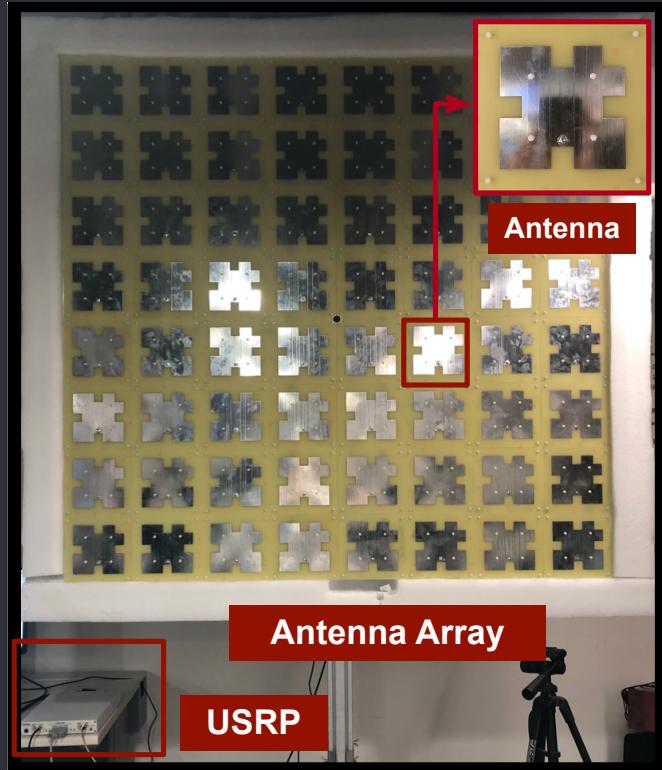
Ambiguity and Resolution degree K is fully covered



## Implementation and Evaluation

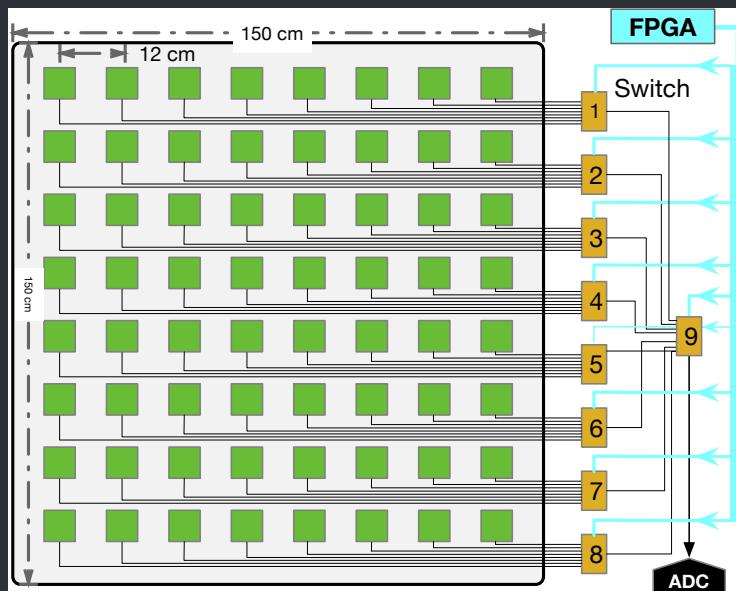
## Implementation

- 8 x 8 Antenna Array:
  - Substrate of RT/duroid 5880
  - High-speed RF switches BGS18GA14
- NI USRP 2950 software-defined radio (SDR)
- PC equipped with Intel CPU Xeon E5-2620

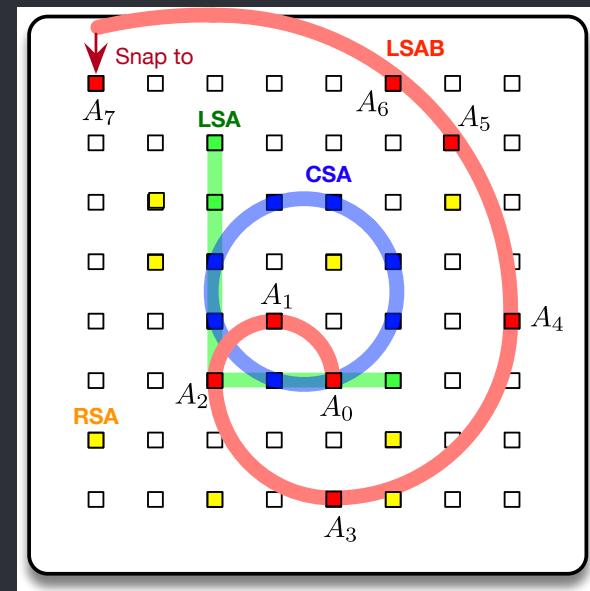


# Evaluation

Schematic of the UPA

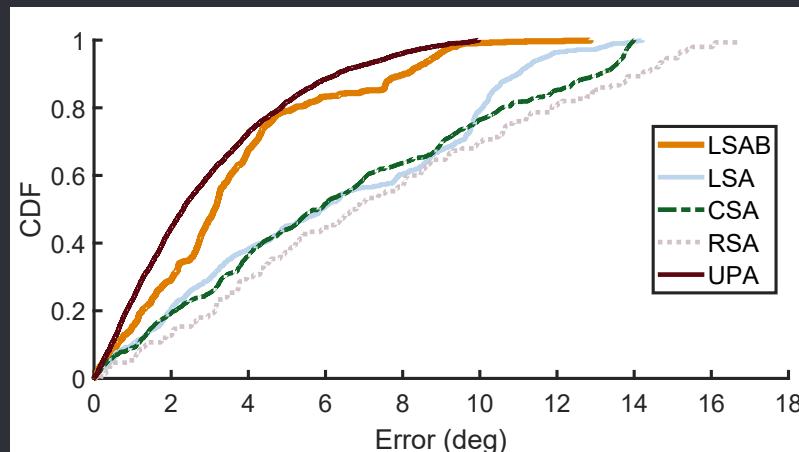


Logical SPAs

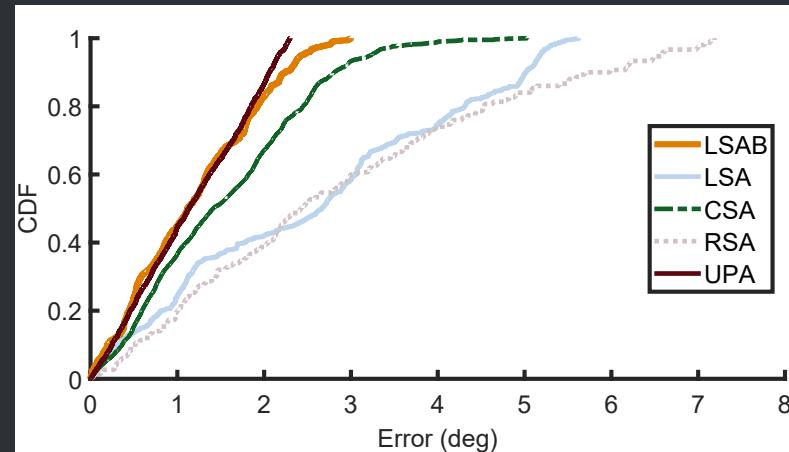


- Accuracy of angle estimation

Azimuthal Angle



Elevation Angle



LSAB can achieve median errors of  $3.12^\circ$  and  $1.11^\circ$ , and the 90th percentiles of  $8.04^\circ$  and  $2.24^\circ$  in the two angles.

Close to UPA and better than other SPAs.

- **Conclusion**

- Estimating the direction of an RF source as accurately as a conventional UPA
- Enhancing the spatio-temporal efficiency of AoA based systems



Thank you!