## Assn2\_Parth\_Dethaliya\_24-27-29

## October 5, 2024

```
[1]: # Name: Parth Jilubhai Dethaliya
     # Reg No: 24-27-29
     # Programme: M. Tech. Data Science
     # Assignment Number: 2
[2]: import numpy as np
     def print_var_info(var):
        print(f"values
                        : \n{var}")
        print(f"Shape
                          : {var.shape}")
        print(f"Dimension : {var.ndim}")
[3]: ## Q1
     # a
     var1 = np.arange(31) # including 0 and 30 as well, total 31 values
    print_var_info(var1)
    values
    [ 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
     24 25 26 27 28 29 30]
    Shape
             : (31,)
    Dimension: 1
[4]: # b
     # Since 31 values are present in var1 (5,6) or (6,5) shapes may not work so,
     var2 = var1.reshape(31,1)
    print_var_info(var2)
    values
    [[ 0]]
     [ 1]
     Γ 21
     [ 3]
     Γ 41
     [5]
     [ 6]
     [7]
     [8]
```

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[ 9]
     [10]
     [11]
     [12]
     [13]
     [14]
     [15]
     [16]
     [17]
     [18]
     [19]
     [20]
     [21]
     [22]
     [23]
     [24]
     [25]
     [26]
     [27]
     [28]
     [29]
     [30]]
             : (31, 1)
    Shape
    Dimension: 2
[5]: # c
     # Similarly 3d shape
     var3 = var2.reshape(1,31,1) # or var1.reshape() both would result in same
     print_var_info(var3)
    values
    [[ 0]]
      [ 1]
      [ 2]
      [ 3]
      [ 4]
      [5]
      [ 6]
      [7]
      [8]
      [ 9]
      [10]
      [11]
      [12]
      [13]
      [14]
      [15]
```

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[16]
       [17]
       [18]
       [19]
       [20]
       [21]
       [22]
       [23]
       [24]
       [25]
       [26]
       [27]
       [28]
       [29]
       [30]]]
     Shape
               : (1, 31, 1)
     Dimension: 3
[6]: # d
      var2[1,0] = -1
      print(var1)
      print(var3)
     [ \ 0 \ -1 \ \ 2 \ \ 3 \ \ 4 \ \ 5 \ \ 6 \ \ 7 \ \ 8 \ \ 9 \ 10 \ 11 \ 12 \ 13 \ 14 \ 15 \ 16 \ 17 \ 18 \ 19 \ 20 \ 21 \ 22 \ 23
      24 25 26 27 28 29 30]
     [[ 0]]
       [-1]
       [ 2]
       [ 3]
       [ 4]
       [ 5]
       [ 6]
       [7]
       [8]
       [ 9]
       [10]
       [11]
       [12]
       [13]
       [14]
       [15]
       [16]
       [17]
       [18]
       [19]
       [20]
```

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[21]
[22]
[23]
[24]
[25]
[26]
[27]
[28]
[29]
[30]]]
```

The values in var1 as well as var3 changes because reshapes doesn't returns copy rather it returns view (in most of the cases).

```
[7]: # e i) Sum var3 over its second dimension
     print(f"Shape
                    : {var3.shape}")
     sum_var3_ax1 = np.sum(var3, axis=1)
     print("Sum over second dimension:", sum_var3_ax1) # Second dimension contains ∪
      ⇔all the 31 values so it sums over it
     # e ii) Sum var3 over its 3rd dimension
     sum var3 ax2 = np.sum(var3, axis=2)
     print("Sum over second dimension:", sum_var3_ax2) # it will sum between columns_
     ⇔but since we only have 31 rows and
     \# single column so it will be same thing but with dimension 2 (as it has \sqcup
      ⇒reduced that 2nd axis by summin over it)
     # e iii) Sum var3 over its 1st & 3rd dimension
     sum_var3_ax1_3 = np.sum(var3, axis=(0,2))
     print("Sum over second dimension:", sum_var3_ax1_3) # it willfirst sum over_
      ⇔axis 0 which is between the depth, but since
     # there exists only one depth so the output information may not change, only |
     ⇔axis 0 will be reduces
     # then it sums over axis 2, again same thing will happen as mention in "e (ii)"_{	t L}
      →and the dimension will be 1 now
             : (1, 31, 1)
    Shape
    Sum over second dimension: [[463]]
    Sum over second dimension: [[ 0 -1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
    17 18 19 20 21 22 23
```

```
Snape : (1, 31, 1)
Sum over second dimension: [[463]]
Sum over second dimension: [[0-1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
24 25 26 27 28 29 30]]
Sum over second dimension: [0-1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
24 25 26 27 28 29 30]
```

Conclusion regarding output shape: if an array is of shape (a,b,c), any\_operation(axis=0) returns (b,c) (eliminates the given axis) example: i) any\_operation(axis=1) returns (a,c) ii) any\_operation(axis=(0,1) returns (b) likewise...

```
[8]: \# f i)
    print("Second row")
    print(var2[2,:])
    # f ii)
    print("\nLast column")
    print(var2[:,-1]) # Only 1 column exists so the output will with full data but |
    # f iii) Top right 2x2
    # Since it's not possible with shape (31,1) so creating new variable with (5,6)_{\sqcup}
     ⇔shape to do this
    var4 = np.arange(30).reshape(5,6)
    print("\nvar4: ")
    print_var_info(var4)
    print("\n")
    print("Top right 2x2: \n")
    print(var4[:4,-4:])
   Second row
    [2]
   Last column
    24 25 26 27 28 29 30]
   var4:
   values
    [[0 1 2 3 4 5]
    [67891011]
    [12 13 14 15 16 17]
    [18 19 20 21 22 23]
    [24 25 26 27 28 29]]
            : (5, 6)
   Shape
   Dimension: 2
   Top right 2x2:
    [[2 3 4 5]
    [8 9 10 11]
    [14 15 16 17]
```

```
[20 21 22 23]]
```

```
[9]: # 02
     # a
     arr = np.arange(10)
     print("original array : ", arr)
     arr2 = arr + 1
     print("Broadcasted + 1 : ",arr2)
     original array : [0 1 2 3 4 5 6 7 8 9]
     Broadcasted + 1 :
                       [1 2 3 4 5 6 7 8 9 10]
\lceil 10 \rceil: # b 10x10 matrix
     column vector = arr2.reshape(10,1)
     arr3 = column_vector + arr2
[11]: arr3
[11]: array([[ 2,
                     4, 5, 6, 7, 8, 9, 10, 11],
                 3,
            [ 3,
                 4,
                     5,
                         6,
                            7, 8, 9, 10, 11, 12],
                         7,
            [4,
                            8, 9, 10, 11, 12, 13],
                 5, 6,
                     7, 8, 9, 10, 11, 12, 13, 14],
            [5,
                     8, 9, 10, 11, 12, 13, 14, 15],
            [6, 7,
            [7, 8, 9, 10, 11, 12, 13, 14, 15, 16],
            [8, 9, 10, 11, 12, 13, 14, 15, 16, 17],
            [ 9, 10, 11, 12, 13, 14, 15, 16, 17, 18],
            [10, 11, 12, 13, 14, 15, 16, 17, 18, 19],
            [11, 12, 13, 14, 15, 16, 17, 18, 19, 20]])
[12]: # c
     import numpy.random as npr
     data = np.exp(npr.randn ( 50 , 5 ) )
     print(data)
     [[ 0.38235034  0.47052197
                              0.53214629 0.40205941
                                                     2.91523004]
      [ 2.09759357
                   6.7715061
                              1.87417993
                                         2.23864297
                                                     1.320715467
      [ 0.87450436  0.32739146
                              1.67193682 1.66378008
                                                     0.62403148]
      [ 0.24493919  0.70024222
                              0.58580026 0.85574078
                                                     1.92754272]
      [ 0.21456058  0.60270527
                              1.0972436
                                          0.79434142
                                                    1.4114013 ]
      [ 0.48448822  0.72102741
                              0.87042439 0.57519546
                                                    0.86214031]
      [ 1.7380417
                   1.36251009
                              3.05740094
                                         7.82942831
                                                     1.01136941]
      [ 1.09660995  0.82763883
                              3.91180426 0.89560132
                                                    1.19201264]
      [ 0.46463446  0.75688305
                              2.30421174
                                         1.37665969
                                                    0.57275142]
      [ 0.17485048    1.049277
                              0.27547992 1.1294214
                                                     1.25206785]
      [ 0.35353941 1.10328982
                              0.68705863
                                         0.4821
                                                     4.88034987]
      [ 1.27380803  0.40903791
                              0.30665223 2.33216675 0.61671796]
      [ 2.46778942  0.86358348
                              0.2519135
                                          0.49389942 0.47557763]
```

```
1.1115445
                                              0.06367931
                                                          2.01671067]
      [ 9.02691775
                     0.58573989
                                                          1.54407345]
                                 1.1673564
                                              5.89537922
      [ 5.04280364
                     1.08837524
                                 1.15437486
                                             0.72243696
                                                          0.40697481]
      [ 0.84990804
                     0.31230545
                                 1.92914941
                                              0.98035944
                                                          2.30270128]
      [ 1.68134421
                     1.61808019
                                 1.22204211
                                              0.59249168
                                                          0.86292201]
      [ 1.10458064
                     1.60106534
                                 5.73051277
                                              4.40731247
                                                          2.21583517]
                                                          0.34600285]
      [ 0.48413142
                     0.84176457
                                 0.8149363
                                              1.80916436
      [ 0.35747069
                     0.7483486
                                 0.7001333
                                              4.80071015
                                                          0.25918724]
      [ 0.27706548
                     0.61372494
                                 0.16333313
                                             1.48792037
                                                          0.41081579]
      [ 1.3685866
                     4.05336671
                                                          3.42932578]
                                 1.23184701
                                              0.23848722
      [ 0.45740037
                     0.89822703
                                 0.25182078
                                              2.30581421
                                                          0.34269687]
                     8.21617173
      [ 0.46983396
                                 4.55730463
                                             0.19743147
                                                          0.86416487]
      [ 0.21656583
                     1.41821823
                                 0.90924882
                                              2.44278065
                                                          0.95401947]
      [12.98801133
                     1.66756708
                                 1.02498594
                                              0.62199627
                                                          0.12466774]
      [ 0.23352828
                                                          0.23006328]
                    1.49689326
                                 1.21756798 13.63536932
      [ 9.65718561
                     0.13178202
                                 1.60640208
                                              2.70827242
                                                          0.14678533]
                    0.27787278
      [ 1.47256576
                                 0.15183198
                                             8.08129085
                                                          1.40715872]
      [ 4.64508427
                                                          0.21599943]
                     1.42864191
                                 0.19686782
                                              0.16315877
      [ 1.11124272
                     2.27035587
                                              1.03521854
                                                          0.59453139]
                                 2.60345896
      [ 0.69408769 10.44493568
                                 0.27796471
                                              1.55845384
                                                          0.7779147 ]
      [ 1.34840899
                     0.73887632
                                 0.98823567
                                              1.00099782
                                                          1.7892939 ]
      [ 1.39881014
                     0.54458281
                                 0.38039964
                                              1.15377251
                                                          1.09535485]
      [ 2.59785481
                     1.12508868
                                 0.15934267
                                              0.72477957
                                                          0.15854823]
      [ 0.34142663
                     1.33605563
                                 0.82568839
                                             0.15709303
                                                          0.32715635]
      [ 0.35862749 14.02454596
                                              0.65457015
                                                          1.2356376 ]
                                 1.66611477
      [ 0.54583687
                     4.603758
                                 0.65128755
                                             0.59922415
                                                          3.24879359]
      [ 4.1059682
                     1.10274585
                                 0.88537284
                                              0.27981202
                                                          2.01558802]
      [ 0.43738869
                     4.38361422
                                 3.39925361
                                              0.71041841
                                                          4.06540601]
      [ 0.5176052
                     1.06473146
                                 0.82508289
                                              1.69731185
                                                          1.95034458]
      [ 0.6003816
                     3.33345797
                                 0.37293915
                                              1.803347
                                                          0.26232508]
      [ 0.20605182
                     0.30892283
                                 0.19303384
                                              2.04201804
                                                          0.43045054]
      [ 0.49921889
                     1.19922506
                                 0.98001505
                                             0.1823939
                                                          0.99863417]
      [ 1.60878768
                     2.37476806
                                 0.32081522
                                              1.13670549
                                                          0.35315203]
      [ 2.96776773
                     0.29138487
                                                          1.08200108]
                                 4.40887413
                                              1.85732645
      [ 0.61845036
                     0.20797488
                                 0.59749474
                                             0.75161403
                                                          0.77548499]]
[13]: std = np.std(data,axis=0) # for each column that means we have to compute_
       ⇒between rows
      mean = np.mean(data,axis=0)
      print(std)
      print(mean)
     [2.53622086 2.69123172 1.24231533 2.4336724
                                                   1.10454843]
     [1.7053151 2.00756827 1.27562354 1.80731343 1.25703347]
[14]: normalized = (data-mean)/std
      print(normalized)
```

0.33476891

1.06642947

0.67491127]

[ 2.43903977 5.22751147

- [[-5.21628371e-01 -5.71131163e-01 -5.98460980e-01 -5.77421193e-01 1.50124388e+00]
- [ 1.54670470e-01 1.77017006e+00 4.81807135e-01 1.77234017e-01 5.76543211e-02]
- [-3.27578227e-01 -6.24315178e-01 3.19011821e-01 -5.89780885e-02 -5.73086685e-01]
- [-5.75807860e-01 -4.85772383e-01 -5.55272289e-01 -3.91002769e-01 6.07043779e-01]
- [-5.87785764e-01 -5.22014878e-01 -1.43586681e-01 -4.16231870e-01 1.39756510e-01]
- [-4.81356689e-01 -4.78049085e-01 -3.26164493e-01 -5.06279307e-01 -3.57515479e-01]
- [ 1.29036863e-02 -2.39688828e-01 1.43423924e+00 2.47449693e+00 -2.22411307e-01]
- [-2.40004788e-01 -4.38434724e-01 2.12199001e+00 -3.74624010e-01 -5.88664352e-02]
- [-4.89184778e-01 -4.64725952e-01 8.27960638e-01 -1.76956331e-01 -6.19512949e-01]
- [-6.03442956e-01 -3.56079065e-01 -8.05064218e-01 -2.78546953e-01 -4.49561139e-03]
- [-5.32988160e-01 -3.36009139e-01 -4.73764503e-01 -5.44532382e-01 3.28035993e+00]
- [-1.70137811e-01 -5.93977228e-01 -7.79972108e-01 2.15663095e-01 -5.79707956e-01]
- [ 3.00634038e-01 -4.25078517e-01 -8.24033971e-01 -5.39683983e-01 -7.07488978e-01]
- [-4.36413402e-01 -1.63370787e-01 -5.34294433e-01 -5.52481805e-01 2.36938353e+00]
- [ 2.89298415e-01 1.19645706e+00 -1.68390472e-01 -6.05070973e-01 -5.27022797e-01]
- [-6.44929405e-01 -2.76211612e-01 -1.32075198e-01 -7.16462136e-01 6.87771746e-01]
- [ 2.88681587e+00 -5.28318827e-01 -8.71494807e-02 1.67979297e+00 2.59870891e-01]
- [ 1.31592977e+00 -3.41551056e-01 -9.75989600e-02 -4.45777530e-01 -7.69598362e-01]
- [-3.37276250e-01 -6.29920792e-01 5.26054740e-01 -3.39796759e-01 9.46692587e-01]
- [-9.45142031e-03 -1.44724840e-01 -4.31302997e-02 -4.99172261e-01 -3.56807774e-01]
- [-2.36862046e-01 -1.51047170e-01 3.58595689e+00 1.06834389e+00 8.68048589e-01]
- [-4.81497369e-01 -4.33185926e-01 -3.70829552e-01 7.60548254e-04 -8.24799165e-01]
- [-5.31438104e-01 -4.67897158e-01 -4.63240067e-01 1.22999164e+00 -9.03397447e-01]
- [-5.63140867e-01 -5.17920222e-01 -8.95336615e-01 -1.31239137e-01 -7.66120941e-01]

- [-1.32767812e-01 7.60171792e-01 -3.52378563e-02 -6.44633274e-01 1.96667910e+00]
- [-4.92037089e-01 -4.12205770e-01 -8.24108611e-01 2.04834792e-01
- -8.27792222e-01]
- [-4.87134681e-01 2.30697468e+00 2.64158463e+00 -6.61503151e-01
- -3.55682551e-01]
- -2.74332927e-01]
- [ 4.44862527e+00 -1.26336649e-01 -2.01750388e-01 -4.87048774e-01
- -1.02518432e+00]
- [-5.80307039e-01 -1.89755127e-01 -4.67317396e-02 4.86016766e+00
- -9.29764751e-01]
- [ 3.13532257e+00 -6.96999161e-01 2.66259722e-01 3.70205534e-01
- -1.00516022e+00]
- [-9.17701385e-02 -6.42715183e-01 -9.04594452e-01 2.57798766e+00
  - 1.35915500e-01]
- [ 1.15911402e+00 -2.15115764e-01 -8.68342918e-01 -6.75585860e-01
- -9.42497423e-01]
- [-2.34235269e-01 9.76458441e-02 1.06883928e+00 -3.17255062e-01
- -5.99794512e-01]
- [-3.98714254e-01 3.13513226e+00 -8.03064088e-01 -1.02256817e-01
- -4.33768912e-01]
- [-1.40723591e-01 -4.71416838e-01 -2.31332464e-01 -3.31316414e-01
  - 4.81880572e-01]
- [-1.20851050e-01 -5.43611851e-01 -7.20609236e-01 -2.68541043e-01
- -1.46375309e-01]
- [ 3.51917189e-01 -3.27909181e-01 -8.98548735e-01 -4.44814949e-01
- -9.94510716e-01]
- [-5.37764075e-01 -2.49518700e-01 -3.62174674e-01 -6.78078283e-01
- -8.41861791e-01]
- [-5.30981991e-01 4.46523336e+00 3.14325375e-01 -4.73664115e-01
- -1.93706973e-02]
- [-4.57167687e-01 9.64684574e-01 -5.02558384e-01 -4.96405875e-01
  - 1.80323476e+00]
- [ 9.46547337e-01 -3.36211266e-01 -3.14131757e-01 -6.27652847e-01
  - 6.86755356e-01]
- [-4.99927442e-01 8.82884194e-01 1.70941307e+00 -4.50715974e-01
  - 2.54255266e+00]
- [-4.68299078e-01 -3.50336539e-01 -3.62662072e-01 -4.51998328e-02
  - 6.27687383e-01]
- [-4.35661387e-01 4.92670210e-01 -7.26614546e-01 -1.62981265e-03
- -9.00556612e-01]
- [-5.91140659e-01 -6.31177697e-01 -8.71429077e-01 9.64405116e-02
- -7.48344678e-01]
- [-4.75548572e-01 -3.00361804e-01 -2.37949646e-01 -6.67682112e-01
- -2.33941125e-01]
- $[-3.80595469e-02 \quad 1.36443021e-01 \quad -7.68571629e-01 \quad -2.75553909e-01 \quad -2.755553909e-01 \quad -2.75553909e-01 \quad -2.75553909e-01 \quad -2.75553909e-01 \quad -2.75553909e-01 \quad -2.75553909e-01 \quad -2.75553909e-01 \quad -2.755553909e-01 \quad -2.75559909e-01 \quad -2.75559909e-01 \quad -2.75559909e-01 \quad -2.75559909e-01 \quad -2.75559909e-01 \quad -2.75559909e-01 \quad -2.75559$
- -8.18326680e-01]

```
[ 4.97769202e-01 -6.37694402e-01 2.52210570e+00 2.05504329e-02
       -1.58465113e-01]
      [-4.28537099e-01 -6.68687642e-01 -5.45858837e-01 -4.33788626e-01
      -4.35968644e-01]]
[15]: std = np.std(normalized,axis=0)
     mean = np.mean(normalized,axis=0)
     print("Standard Deviation : ",std)
     print("Mean
                              : ",mean)
     # Mean 0, Std = 1
     Standard Deviation: [1. 1. 1. 1.]
                       : [ 1.23234756e-16 -1.06581410e-16 -6.66133815e-18
     Mean
     -4.55191440e-17
       3.36397576e-16]
[16]: # 3 Vandermonde matrix
     N = 12
     def vandermonde(N):
         vec = np.arange (N) +1
         vector = np.arange(N) + 1
         v2 = np.arange(N) # Power Vector
         output = vector.reshape(N,1)**v2
         return output
     def printMat(Mat):
         for row in Mat:
             print(" ".join(f"{elem}" for elem in row))
     Vector = vandermonde(N)
     printMat(Vector)
     1 1 1 1 1 1 1 1 1 1 1 1
     1 2 4 8 16 32 64 128 256 512 1024 2048
     1 3 9 27 81 243 729 2187 6561 19683 59049 177147
     1 4 16 64 256 1024 4096 16384 65536 262144 1048576 4194304
     1 5 25 125 625 3125 15625 78125 390625 1953125 9765625 48828125
     1 6 36 216 1296 7776 46656 279936 1679616 10077696 60466176 362797056
     1 7 49 343 2401 16807 117649 823543 5764801 40353607 282475249 1977326743
     1 8 64 512 4096 32768 262144 2097152 16777216 134217728 1073741824 0
     1 9 81 729 6561 59049 531441 4782969 43046721 387420489 -808182895 1316288537
     1215752192
     1 11 121 1331 14641 161051 1771561 19487171 214358881 -1937019605 167620825
     1843829075
     1 12 144 1728 20736 248832 2985984 35831808 429981696 864813056 1787822080
     -20971520
```

```
[17]: # b
      x = np.ones(12)
      b = np.dot(Vector,x)
      print(b)
     [1.20000000e+01 4.09500000e+03 2.65720000e+05 5.59240500e+06
      6.10351560e+07 4.35356467e+08 2.30688120e+09 1.22713351e+09
      9.43953692e+08 3.73692871e+09 3.10225064e+08 3.10073456e+09]
[18]: # c naive solution
      Vector_inv = np.linalg.inv(Vector)
      Sol = np.dot(Vector_inv,b)
      print(Sol)
      # The result is almost ones(12) with slight variation maybe due to floating \Box
       ⇔points instability while inversing Vector
     [1.00158882 0.99722672 1.00127029 0.99991608 1.00000095 0.99999905
      1.00000018 0.99999999 1.
                                       1.
                                                   1.
                                                              1.
                                                                        1
[19]: # d solve using numpy
      Sol_inbuilt = np.linalg.solve(Vector,b)
      print(Sol_inbuilt)
     [1.0000114 0.99997033 1.00002961 0.99998507 1.00000423 0.9999993
      1.00000007 1.
                            1.
                                       1.
                                                   1.
                                                              1.
                                                                        ]
[20]: # The solution using .solve() seems more accurate but let's verify that using
       ⇔some statistics
      Diff solve = x - Sol
      Diff_solve_inbuilt = x - Sol_inbuilt
      print(np.std(Diff_solve) , np.std(Diff_solve_inbuilt) )
      # clearly the inbuilt function method's solution is more closer to ones(12)
     0.0009931496457600455 1.3316958977450673e-05
[21]: #https://qithub.com/PARTH1D/Parth_24-27-29/blob/main/
       →Assn2_Parth_Dethaliya_24-27-29.ipynb
 []:
```