## Assn2\_Parth\_Dethaliya\_24-27-29

## October 8, 2024

```
[1]: # Name: Parth Jilubhai Dethaliya
     # Reg No: 24-27-29
     # Programme: M. Tech. Data Science
     # Assignment Number: 2
[2]: import numpy as np
     def print_var_info(var):
        print(f"values : \n{var}")
        print(f"Shape
                          : {var.shape}")
        print(f"Dimension : {var.ndim}")
[3]: ## Q1
     # a
     var1 = np.arange(31) # including 0 and 30 as well, total 31 values
    print_var_info(var1)
    values
    [ 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
     24 25 26 27 28 29 30]
    Shape
             : (31,)
    Dimension: 1
[4]: # b
     # Since 31 values are present in var1 (5,6) or (6,5) shapes may not work so,
     var2 = var1.reshape(31,1)
    print_var_info(var2)
    values
    [[ 0]]
     [ 1]
     Γ 21
     [ 3]
     Γ 41
     [5]
     [ 6]
     [7]
     [8]
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[ 9]
     [10]
     [11]
     [12]
     [13]
     [14]
     [15]
     [16]
     [17]
     [18]
     [19]
     [20]
     [21]
     [22]
     [23]
     [24]
     [25]
     [26]
     [27]
     [28]
     [29]
     [30]]
             : (31, 1)
    Shape
    Dimension: 2
[5]: # c
     # Similarly 3d shape
     var3 = var2.reshape(1,31,1) # or var1.reshape() both would result in same
     print_var_info(var3)
    values
    [[ 0]]
      [ 1]
      [ 2]
      [ 3]
      [ 4]
      [5]
      [ 6]
      [7]
      [8]
      [ 9]
      [10]
      [11]
      [12]
      [13]
      [14]
      [15]
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[16]
       [17]
       [18]
       [19]
       [20]
       [21]
       [22]
       [23]
       [24]
       [25]
       [26]
       [27]
       [28]
       [29]
       [30]]]
     Shape
               : (1, 31, 1)
     Dimension: 3
[6]: # d
      var2[1,0] = -1
      print(var1)
      print(var3)
     [ \ 0 \ -1 \ \ 2 \ \ 3 \ \ 4 \ \ 5 \ \ 6 \ \ 7 \ \ 8 \ \ 9 \ 10 \ 11 \ 12 \ 13 \ 14 \ 15 \ 16 \ 17 \ 18 \ 19 \ 20 \ 21 \ 22 \ 23
      24 25 26 27 28 29 30]
     [[ 0]]
       [-1]
       [ 2]
       [ 3]
       [ 4]
       [ 5]
       [ 6]
       [7]
       [8]
       [ 9]
       [10]
       [11]
       [12]
       [13]
       [14]
       [15]
       [16]
       [17]
       [18]
       [19]
       [20]
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[21]
[22]
[23]
[24]
[25]
[26]
[27]
[28]
[29]
[30]]]
```

The values in var1 as well as var3 changes because reshapes doesn't returns copy rather it returns view (in most of the cases).

```
[7]: # e i) Sum var3 over its second dimension
     print(f"Shape
                    : {var3.shape}")
     sum_var3_ax1 = np.sum(var3, axis=1)
     print("Sum over second dimension:", sum_var3_ax1) # Second dimension contains ∪
      ⇔all the 31 values so it sums over it
     # e ii) Sum var3 over its 3rd dimension
     sum var3 ax2 = np.sum(var3, axis=2)
     print("Sum over third dimension:", sum_var3_ax2) # it will sum between columns_
      ⇔but since we only have 31 rows and
     \# single column so it will be same thing but with dimension 2 (as it has \sqcup
      ⇒reduced that 2nd axis by summin over it)
     # e iii) Sum var3 over its 1st & 3rd dimension
     sum_var3_ax1_3 = np.sum(var3, axis=(0,2))
     print("Sum over first, third dimension:", sum_var3_ax1_3) # it willfirst sum_u
      →over axis 0 which is between the depth, but since
     # there exists only one depth so the output information may not change, only |
      \hookrightarrowaxis 0 will be reduces
     # then it sums over axis 2, again same thing will happen as mention in "e (ii)"_{	t L}
      →and the dimension will be 1 now
             : (1, 31, 1)
    Shape
    Sum over second dimension: [[463]]
    Sum over third dimension: [[ 0 -1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
    17 18 19 20 21 22 23
```

```
Snape : (1, 31, 1)
Sum over second dimension: [[463]]
Sum over third dimension: [[0-1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
24 25 26 27 28 29 30]]
Sum over first, third dimension: [0-1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
24 25 26 27 28 29 30]
```

Conclusion regarding output shape: if an array is of shape (a,b,c), any\_operation(axis=0) returns (b,c) (eliminates the given axis) example: i) any\_operation(axis=1) returns (a,c) ii) any\_operation(axis=(0,1) returns (b) likewise...

```
[8]: # f i)
     print("Second row")
     print(var2[1,:])
     # f ii)
     print("\nLast column")
     print(var2[:,-1]) # Only 1 column exists so the output will with full data but |
     # f iii) Top right 2x2
     # Since it's not possible with shape (31,1) so creating new variable with (5,6)_{\sqcup}
     ⇔shape to do this
     var4 = np.arange(30).reshape(5,6)
     print("\nvar4: ")
     print_var_info(var4)
     print("\n")
     print("Top right 2x2: \n")
    print(var4[:2,-2:])
    Second row
    [-1]
    Last column
    [ 0 -1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
     24 25 26 27 28 29 30]
    var4:
    values
    [[0 1 2 3 4 5]
     [67891011]
     [12 13 14 15 16 17]
     [18 19 20 21 22 23]
     [24 25 26 27 28 29]]
             : (5, 6)
    Shape
    Dimension: 2
    Top right 2x2:
    [[ 4 5]
     [10 11]]
```

```
[9]: # 02
     # a
     arr = np.arange(10)
     print("original array : ", arr)
     arr2 = arr + 1
     print("Broadcasted + 1 : ",arr2)
     original array : [0 1 2 3 4 5 6 7 8 9]
     Broadcasted + 1 : [ 1 2 3 4 5 6 7 8 9 10]
[10]: # b 10x10 matrix
     column vector = arr2.reshape(10,1)
     arr3 = column_vector + arr2
[11]: arr3
                         5, 6, 7, 8, 9, 10, 11],
[11]: array([[ 2,
                  3,
                     4,
                         6,
            [ 3,
                  4,
                     5,
                             7, 8, 9, 10, 11, 12],
                     6, 7, 8, 9, 10, 11, 12, 13],
            [4,
                     7, 8, 9, 10, 11, 12, 13, 14],
            [6, 7, 8, 9, 10, 11, 12, 13, 14, 15],
            [7, 8, 9, 10, 11, 12, 13, 14, 15, 16],
            [8, 9, 10, 11, 12, 13, 14, 15, 16, 17],
            [ 9, 10, 11, 12, 13, 14, 15, 16, 17, 18],
            [10, 11, 12, 13, 14, 15, 16, 17, 18, 19],
            [11, 12, 13, 14, 15, 16, 17, 18, 19, 20]])
[12]: # c
     import numpy.random as npr
     data = np.exp(npr.randn ( 50 , 5 ) )
     print(data)
     [[ 0.13229182  0.39721069
                               8.3678117
                                                      0.78534795]
                                          0.88091519
      [ 1.1196919
                   1.47960031
                               1.69209521
                                          0.25459477
                                                      0.5030388 ]
      [ 2.4487117
                   2.33291236
                               0.60274116
                                          3.25405418
                                                      8.158569027
      [ 1.04600821  3.45910292
                               1.20869025
                                          0.52069193 1.95885277]
      [ 1.43256151  0.60955491
                               2.47809694
                                          1.99690595 0.491371857
      [ 0.53065645 2.73139153 1.11948245
                                          0.4632505
                                                      4.51046351]
      [ 0.91598094  0.39871461
                               0.44057713 0.90685407
                                                      1.25208093]
      [ 5.6727857
                   2.24761558
                               0.5714233
                                          0.15712224 2.42640908]
      1.88657776
                                                     1.2082491 ]
      [ 1.55886364  1.29158243
                               1.01839507
                                          0.23227627
                                                      1.27863051]
      [ 0.49530623  0.29778728
                               0.52356885
                                          0.42079815
                                                      7.99480334]
      [ 0.48306008  0.74142276
                               0.98438274
                                          0.51874428
                                                      2.32025173]
      [ 0.98226191 2.58905789
                               0.66329924
                                          0.11886209
                                                      0.56154774]
      [ 2.74573058  0.86371696
                                          0.18878987
                               0.91360364
                                                      1.10784177]
      [ 2.8059662
                   0.36201195
                               1.41655453
                                          0.11922446 4.38202385]
```

```
[ 0.29265948
                     0.7753107
                                  0.16264586
                                              1.67239303
                                                           0.13733294]
      [ 0.36638882
                     0.69623991
                                 0.24693859
                                              0.55146543
                                                           7.78035216]
      [ 0.22266936
                     1.02379112 11.96526992
                                              2.44759177
                                                           2.3850377 ]
                     1.16655125
      [ 8.35267772
                                  0.62134689
                                              6.19670375
                                                           4.04417533]
      [27.44357743
                     0.31247982
                                 0.81454733
                                              0.15266395
                                                           1.31835454]
      [ 0.84686158
                     0.55745581
                                  2.83680902
                                              0.74399516
                                                           0.66352456]
      [ 0.44012025
                     2.24633017
                                  0.7029408
                                              0.22626505
                                                           0.58068104]
      [ 1.01884628
                     0.33523397
                                  0.62453713
                                              1.84481719
                                                           1.86398793]
                                                           2.53443318]
      [ 0.41026182
                     2.50439289
                                 0.24908101
                                              0.95095174
      [ 0.58272083
                                                           0.90553543]
                     0.5895959
                                  0.70301295
                                              0.38228042
      [ 3.34962561
                     5.7408649
                                  0.5831893
                                              0.33659583
                                                           1.89905087]
      [ 2.93818512
                     0.33643166
                                 0.89982054
                                              0.64358729
                                                           0.30207579]
      [ 1.05546278
                     2.03189243
                                  0.74591055
                                              1.25600447
                                                           0.56667275]
      [ 2.33202607
                     0.1729393
                                  5.49859471
                                              9.01744217
                                                           2.54580476]
      [ 1.10312158
                     1.18132481
                                  1.52844569
                                              1.18225154
                                                           4.89123294]
      [ 0.52451822
                     1.45098809
                                  0.9188544
                                              0.84564303
                                                           0.38161375]
                     0.21977817
      [ 0.4155313
                                  0.65223202
                                              0.4130988
                                                           6.51447277]
      [ 0.87154053
                     2.44160611
                                  0.85575953
                                              2.20387769
                                                           3.40729262]
      T 0.14688363
                     0.56069502
                                 0.77558375 10.82876143
                                                           1.30979827]
      [ 0.40901795
                     0.33704482
                                  0.31477298
                                              2.51190632
                                                           1.02359118]
      [ 1.38988314
                     2.27221406
                                  1.07926439
                                              1.02963811
                                                           2.86029646]
      [ 0.92445086
                     0.65752098
                                 0.88948291
                                              0.70300029
                                                           0.04598369]
      [ 0.70950143
                     0.65942511
                                  0.20892291
                                              1.6108211
                                                           0.12547167]
      [ 0.51210691
                     2.76010361
                                  0.2756458
                                                           0.22903389]
                                              0.75028278
      [ 0.75180298
                     1.30699762
                                                           1.33900009]
                                  2.45793774
                                              2.72082362
      [ 2.25838547
                     0.34063229
                                 0.18487967
                                              0.20314186
                                                           2.13930735]
      [ 1.41296851
                     0.09692474
                                  2.09958656
                                              0.34618667
                                                           0.35905557]
      [ 0.56638609
                     3.69980926
                                 7.54261557
                                              2.67675264
                                                           0.34610111]
      [ 1.09382417
                     1.20078371
                                  0.59713914
                                              0.74868553
                                                           8.05346451]
      [ 3.64050935
                     0.59130831
                                  0.34719952
                                              0.47317292
                                                           2.26084248]
      [ 0.55844141
                     0.62052054
                                              2.88865532
                                                           1.62031351]
                                  0.06156567
      [ 2.87954124
                     0.55451959
                                  0.56316166
                                              2.31115225
                                                           1.20441798]
      [ 1.30395797
                     4.57793524
                                 2.27537411
                                              0.84132928
                                                           0.83165199]
      [ 0.1489721
                     2.06007317
                                 0.18535706
                                              2.46888701
                                                           0.75611431]]
[13]: std = np.std(data,axis=0)# for each column that means we have to compute_
       ⇔between rows
      mean = np.mean(data,axis=0)
      print(std)
      print(mean)
      [4.02330743 1.20473127 2.22624715 2.05294962 2.19348308]
     [2.05117208 1.38328025 1.46143417 1.53706826 2.14912957]
[14]: normalized = (data-mean)/std
      print(normalized)
     [[-4.76940996e-01 -8.18497522e-01 3.10225104e+00 -3.19614794e-01]
```

0.28906948

0.7529258

1.29092123]

[ 0.85204655 2.12333447

- -6.21742485e-01]
- [-2.31521005e-01 7.99514880e-02 1.03609807e-01 -6.24697983e-01
- -7.50446075e-01]
- [ 9.88091589e-02 7.88252235e-01 -3.85713243e-01 8.36350736e-01
  - 2.73967897e+00]
- -8.67464157e-02]
- [-1.53756723e-01 -6.42238949e-01 4.56671116e-01 2.23988787e-01
- -7.55764992e-01]
- $[-3.77926782e-01 \quad 1.11901411e+00 \quad -1.53600073e-01 \quad -5.23060940e-01 \quad -5.23060940e-01 \quad -5.23060940e-01 \quad -6.23060940e-01 \quad -6.2306094$ 
  - 1.07652253e+00]
- [-2.82153716e-01 -8.17249177e-01 -4.58555128e-01 -3.06979859e-01
- -4.08960821e-01]
- [ 9.00158310e-01 7.17450736e-01 -3.99780805e-01 -6.72177247e-01
  - 1.26410603e-01]
- [ 1.49431297e+00 -1.85933254e-01 -5.15640389e-01 1.70247483e-01
- -4.28943574e-01]
- [-1.22364111e-01 -7.61147511e-02 -1.99007150e-01 -6.35569416e-01
- -3.96856975e-01]
- $[-3.86713140e-01 \ -9.01024981e-01 \ -4.21276373e-01 \ -5.43739653e-01$ 
  - 2.66501886e+00]
- $\hbox{ $[-3.89756941e-01\ -5.32780634e-01\ -2.14285028e-01\ -4.96029699e-01] }$ 
  - 7.80138971e-02]
- [-2.65679466e-01 1.00086856e+00 -3.58511377e-01 -6.90813916e-01
- -7.23772088e-01]
- [ 1.72633713e-01 -4.31269031e-01 -2.46078038e-01 -6.56751816e-01
- -4.74718863e-01]
- [ 1.87605380e-01 -8.47714608e-01 -2.01593243e-02 -6.90637408e-01
  - 1.01796741e+00]
- [-2.98044717e-01 6.14289880e-01 -5.26610308e-01 -3.81958940e-01
- -3.91253683e-01]
- [-4.37081338e-01 -5.04651590e-01 -5.83398080e-01 6.59172409e-02
- -9.17169887e-01]
- [-4.18755784e-01 -5.70285141e-01 -5.45534928e-01 -4.80091096e-01
  - 2.56725144e+00]
- [-4.54477503e-01 -2.98397770e-01 4.71818044e+00 4.43519658e-01
  - 1.07549556e-01]
- [ 1.56625009e+00 -1.79898211e-01 -3.77355803e-01 2.26972715e+00
  - 8.63943646e-01]
- [ 6.31132613e+00 -8.88829279e-01 -2.90572790e-01 -6.74348898e-01
- -3.78746950e-01]
- [-2.99333451e-01 -6.85484357e-01 6.17799713e-01 -3.86309090e-01
- -6.77281272e-01]
- $[-4.00429711e-01 \quad 7.16383762e-01 \quad -3.40704926e-01 \quad -6.38497504e-01$
- -7.15049295e-01]
- [-2.56586358e-01 -8.69941958e-01 -3.75922794e-01 1.49905742e-01
- -1.29994909e-01]
- $[-4.07851074e-01 \quad 9.30591473e-01 \quad -5.44572584e-01 \quad -2.85499710e-01$

- 1.75658350e-01]
- $[-3.64986090e-01 \ -6.58806133e-01 \ -3.40672521e-01 \ -5.62501793e-01$
- -5.66949502e-01]
- $[3.22732865e-01\ 3.61705948e+00\ -3.94495675e-01\ -5.84754941e-01$
- -1.14009859e-01]
- [ 2.20468621e-01 -8.68947805e-01 -2.52269221e-01 -4.35218165e-01
- -8.42064293e-01]
- [-2.47485263e-01 5.38387443e-01 -3.21403501e-01 -1.36907301e-01
- -7.21435618e-01]
- [ 6.98067441e-02 -1.00465638e+00 1.81343771e+00 3.64372016e+00
  - 1.80842605e-01]
- [-2.35639587e-01 -1.67635259e-01 3.01006645e-02 -1.72832650e-01
  - 1.25011376e+00]
- [-3.79452450e-01 5.62016180e-02 -2.43719467e-01 -3.36796003e-01
- -8.05803263e-01]
- [-4.06541335e-01 -9.65777274e-01 -3.63482623e-01 -5.47490033e-01]
  - 1.99014219e+00]
- [-2.93199456e-01 8.78474633e-01 -2.72060828e-01 3.24805552e-01
  - 5.73591411e-01]
- [-4.73314177e-01 -6.82795612e-01 -3.08074698e-01 4.52602104e+00]
- -3.82647718e-01]
- [-4.08160241e-01 -8.68438844e-01 -5.15064643e-01 4.74847532e-01
- -5.13128367e-01]
- $\begin{bmatrix} -1.64364506\text{e}-01 & 7.37868963\text{e}-01 & -1.71665477\text{e}-01 & -2.47171262\text{e}-01 \end{bmatrix}$ 
  - 3.24218091e-01]
- [-2.80048502e-01 -6.02424199e-01 -2.56912743e-01 -4.06277856e-01]
- -9.58815639e-01]
- [-3.33474554e-01 -6.00843654e-01 -5.62611056e-01 3.59253046e-02
- -9.22577390e-01]
- [-3.82537303e-01 1.14284688e+00 -5.32640042e-01 -3.83246367e-01
- -8.75363800e-01]
- [-3.22960431e-01 -6.33192100e-02 4.47615878e-01 5.76611987e-01
- -3.69334728e-01]
- [ 5.15032465e-02 -8.65461028e-01 -5.73410956e-01 -6.49760902e-01
- -4.47790823e-03]
- [-1.58626598e-01 -1.06775307e+00 2.86649389e-01 -5.80083200e-01
- -8.16087444e-01]
- [-3.69046117e-01 1.92285954e+00 2.73158414e+00 5.55144836e-01
- -8.21993329e-01]
- [-2.37950473e-01 -1.51483188e-01 -3.88229597e-01 -3.84024393e-01
  - 2.69176225e+00]
- [ 3.95032519e-01 -6.57384730e-01 -5.00499081e-01 -5.18227690e-01
  - 5.09294632e-02]
- [-3.71020781e-01 -6.33136806e-01 -6.28801929e-01 6.58363482e-01
- -2.41085086e-01]
- [ 2.05892584e-01 -6.87921593e-01 -4.03491819e-01 3.77059418e-01
- -4.30690166e-01]
- [-1.85721356e-01 2.65175735e+00 3.65610771e-01 -3.38897248e-01

```
-6.00632662e-01]
      [-4.72795086e-01 5.61779159e-01 -5.73196518e-01 4.53892654e-01
       -6.35069981e-01]]
[15]: std = np.std(normalized,axis=0)
     mean = np.mean(normalized,axis=0)
     print("Standard Deviation : ",std)
     print("Mean
                              : ",mean)
     # Mean O, Std = 1
     Standard Deviation: [1. 1. 1. 1.]
                       : [-3.17523785e-16 -7.32747196e-17 -1.19904087e-16
     Mean
     -3.88578059e-17
       4.04121181e-16]
[16]: # 3 Vandermonde matrix
     N = 12
     def vandermonde(N):
         vec = np.arange (N) +1
         vector = np.arange(N) + 1
         v2 = np.arange(N) # Power Vector
         output = vector.reshape(N,1)**v2
         return output
     def printMat(Mat):
         for row in Mat:
             print(" ".join(f"{elem}" for elem in row))
     Vector = vandermonde(N)
     printMat(Vector)
     1 1 1 1 1 1 1 1 1 1 1 1
     1 2 4 8 16 32 64 128 256 512 1024 2048
     1 3 9 27 81 243 729 2187 6561 19683 59049 177147
     1 4 16 64 256 1024 4096 16384 65536 262144 1048576 4194304
     1 5 25 125 625 3125 15625 78125 390625 1953125 9765625 48828125
     1 6 36 216 1296 7776 46656 279936 1679616 10077696 60466176 362797056
     1 7 49 343 2401 16807 117649 823543 5764801 40353607 282475249 1977326743
     1 8 64 512 4096 32768 262144 2097152 16777216 134217728 1073741824 0
     1 9 81 729 6561 59049 531441 4782969 43046721 387420489 -808182895 1316288537
     1215752192
     1 11 121 1331 14641 161051 1771561 19487171 214358881 -1937019605 167620825
     1843829075
     1 12 144 1728 20736 248832 2985984 35831808 429981696 864813056 1787822080
     -20971520
```

```
[17]: # b
      x = np.ones(12)
      b = np.dot(Vector,x)
      print(b)
     [1.20000000e+01 4.09500000e+03 2.65720000e+05 5.59240500e+06
      6.10351560e+07 4.35356467e+08 2.30688120e+09 1.22713351e+09
      9.43953692e+08 3.73692871e+09 3.10225064e+08 3.10073456e+09]
[18]: # c naive solution
      Vector_inv = np.linalg.inv(Vector)
      Sol = np.dot(Vector_inv,b)
      print(Sol)
      # The result is almost ones(12) with slight variation maybe due to floating \Box
       ⇔points instability while inversing Vector
     [1.00158882 0.99722672 1.00127029 0.99991608 1.00000095 0.99999905
      1.00000018 0.99999999 1.
                                       1.
                                                   1.
                                                              1.
                                                                        1
[19]: # d solve using numpy
      Sol_inbuilt = np.linalg.solve(Vector,b)
      print(Sol_inbuilt)
     [1.0000114 0.99997033 1.00002961 0.99998507 1.00000423 0.9999993
      1.00000007 1.
                            1.
                                       1.
                                                   1.
                                                              1.
                                                                        ]
[20]: # The solution using .solve() seems more accurate but let's verify that using
       ⇔some statistics
      Diff solve = x - Sol
      Diff_solve_inbuilt = x - Sol_inbuilt
      print(np.std(Diff_solve) , np.std(Diff_solve_inbuilt) )
      # clearly the inbuilt function method's solution is more closer to ones(12)
     0.0009931496457600455 1.3316958977450673e-05
[21]: #https://qithub.com/PARTH1D/Parth_24-27-29/blob/main/
       →Assn2_Parth_Dethaliya_24-27-29.ipynb
 []:
```