

Exercise 01:

- Find the names of the suppliers who supply some red part:

$$\pi_{\text{Sname}} \left(\pi_{\text{Sid}} \left(\left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'red'}} \text{Parts} \right) \bowtie \text{Catalog} \right) \bowtie \text{Suppliers} \right)$$

- Find the sids of the suppliers who supply some red or green part:

$$\pi_{\text{Sid}} \left(\left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'red'}} \vee \text{color} = \text{'green'}} \text{Parts} \right) \bowtie \text{Catalog} \right)$$

- Find the sids of the suppliers who are red or are at 221 packer street:

$$\rho(R1, \pi_{\text{Sid}} \left(\left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'red'}} \text{Parts} \right) \bowtie \text{Catalog} \right))$$

$$\rho(R2, \left(\pi_{\text{sid}} \sigma_{\text{address} = \text{'221 packer street'}} \text{Suppliers} \right))$$

$$R1 \cup R2$$

- Find the sids of the suppliers who supply some red part and some green part:

$$\rho(R1, \pi_{\text{Sid}} \left(\left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'red'}} \text{Parts} \right) \bowtie \text{Catalog} \right))$$

$$\rho(R2, \pi_{\text{Sid}} \left(\left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'green'}} \text{Parts} \right) \bowtie \text{Catalog} \right))$$

$$R1 \cap R2$$

- Find the sids of the suppliers who supply every part:

$$\left(\pi_{\text{Pid, Sid}} \bowtie \text{Catalog} \right) / \left(\pi_{\text{pid}} \text{Parts} \right)$$

- Find the sids of the suppliers who supply every red part:

$$\left(\pi_{\text{Pid, Sid}} \bowtie \text{Catalog} \right) / \left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'red'}} \text{Parts} \right)$$

- Find the sids of the suppliers who supply every red or green part:

$$\left(\pi_{\text{Pid, Sid}} \bowtie \text{Catalog} \right) / \left(\pi_{\text{pid}} \sigma_{\text{color} = \text{'red'}} \vee \text{color} = \text{'green'}} \text{Parts} \right)$$

- Find the sids of the suppliers who supply every red or supply every green part:

$$\rho(R1, (\pi_{Sid, Pid} \bowtie Catalog) / (\pi_{Pid} \sigma_{color = 'red'} Parts))$$

$$\rho(R2, (\pi_{Sid, Pid} \bowtie Catalog) / (\pi_{Pid} \sigma_{color = 'green'} Parts))$$

$$R1 \cup R2$$

- Find pairs of sids such that the supplier with the first sid charges more for some part than the supplier with the second sid:

$$\rho(R1, Catalog)$$

$$\rho(R2, Catalog)$$

$$\pi_{R1.sid, R2.sid} (\sigma_{R1.sid \neq R2.sid \wedge R1.pid = R2.pid \wedge R1.cost > R2.cost} (R1 \times R2))$$

- Find the pids of parts supplied by at least two different suppliers

$$\pi_{R1.pid} (\sigma_{R1.sid \neq R2.sid \wedge R1.pid = R2.pid} (R1 \times R2))$$