

<In the Name of God>

Numerical Analysis Fall 2012, Dec 20th

Instructor: Dr. Hamed Masnadi-Shirazi

$$\begin{bmatrix} a_{11} & a_{12} & \dots & a_{1k} & \dots & a_{1n} \\ 0 & a_{22} & \dots & a_{2k} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & a_{kk} & \dots & a_{kn} \\ 0 & 0 & \dots & a_{k+1,k} & \dots & a_{k+1,n} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & a_{nk} & \dots & a_{nn} \end{bmatrix},$$

HW #3

Due Date: Dec 30, 2012 (Late HWs will get a zero grade.)

(Note: getting help or helping others on this HW is **NOT allowed!**)

- 1) **Linear System of Equations:** (A) Use the algorithm presented on pg-374 of the textbook to write the Gaussian elimination with partial pivoting algorithm for solving a linear system of equations. The input to your algorithm should be the augmented matrix. Use your algorithm to solve the following problems:

a) $0.003x_1 + 59.14x_2 = 59.17$
 $5.291x_1 - 6.130x_2 = 46.78$

b) $x_1 + x_2 + 3x_4 = 4$
 $2x_1 + x_2 - x_3 + x_4 = 1$
 $3x_1 - x_2 - x_3 + 2x_4 = -3$
 $-x_1 + 2x_2 + 3x_3 - x_4 = 4$

Your program should show the final upper triangle matrix along with the solutions.

(B) Compare your result with Matlabs solutions. By performing $x = A \backslash b$;

(C) Create some linear systems with $A = \text{gallery}('orthog', n)$ for $n=40$ by picking a random solution x and computing the right-hand side b from it, and compare the quality of your solution to the exact solution.

Submission Guide: submit your Matlab program. Submit the output of your program. Failing to follow the above guidelines will result in a ZERO grade!