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# POZNAN UNIVERSITY OF TECHNOLOGY

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FACULTY OF COMPUTING AND TELECOMMUNICATION  
Institute of Computing Science

## LABORATORY 5: LOCAL SEARCH WITH USE OF DELTAS FROM PREVIOUS ITERATIONS

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## 1 Problem Description

The problem description remains the same as in previous labs. The problem is to select exactly 50% of the nodes (from  $n$  available) and build a Hamiltonian cycle through the selected nodes. The objective is to minimize the sum of two components:

1. The total length of the Hamiltonian cycle (calculated as the sum of Euclidean distances between consecutive nodes in the cycle).
2. The total cost of the selected nodes (the sum of the cost attributes for each selected node).

All distances are rounded to the nearest integer.

## 2 Steepest Local Search with Limited Memory (LS with $\Delta$ Reuse)

The goal of this assignment is to improve the time efficiency of the Steepest LS algorithm by implementing a Limited Memory (LM). This approach avoids the  $O(N^2)$  or  $O(N^3)$  computational cost of evaluating the entire neighborhood in every iteration. Instead, we maintain a list (LM) of known improving moves (deltas) and only re-evaluate moves locally around the most recently applied change.

### 2.1 Inter-route Moves (Node Exchange)

An inter-route move involves swapping a node already in the cycle  $i$  with a node outside of it  $k$ . The operation replaces  $i$  in the cycle with  $k$ , effectively modifying the connections between the predecessor and successor of  $i$  to include  $k$  instead. This allows exploration of new solutions by exchanging elements between the cycle and the set of unused nodes.

### 2.2 Intra-route Moves (Edge Exchange)

An intra-route move consists of reversing a subpath within the current cycle. This corresponds to exchanging two non-adjacent edges, effectively reconnecting the affected segment in the opposite direction. Such moves are useful for improving the internal structure of the cycle without changing the set of nodes included.

The full procedure looks following:

```

1 procedure steepestSearch(selected, remaining, inst, move_type)
2
3 LM = steepestSearch_LM
4 n = size(selected)
5
6 // --- 1. Initialize Local Move List if empty ---
7 if LM is empty then
8     // --- Inter-route: Node Exchange ---
9     for i_idx = 0 to n-1 do
10         i_node = selected[i_idx]
11         prev_i = selected[(i_idx - 1 + n) mod n]
12         next_i = selected[(i_idx + 1) mod n]
13         for each k_node in remaining do
14             delta = calculateDeltaInterNode(selected, i_node, k_node, inst)
15             if delta < 0 then
16                 add Move("inter", prev_i, next_i, i_node, k_node, delta) to LM
17
18     // --- Intra-route: Edge Exchange ---
19     for i_idx = 0 to n-1 do
20         for j_idx = i_idx + 1 to n-1 do
21             a = selected[i_idx]
22             next_a = selected[(i_idx + 1) mod n]
23             c = selected[j_idx]
24             next_c = selected[(j_idx + 1) mod n]
25             if next_c = a then continue
26             delta = calculateDeltaIntraEdge(selected, a, c, inst)
27             if delta < 0 then
28                 add Move("intra_edge", a, next_a, c, next_c, delta) to LM
29         end if
30
31 // --- 2. Recheck existing moves ---
32 sort LM by delta ascending
33 for each m in LM do
34     (applyMove, keepMove) = validate(selected, remaining, m)
35     if not keepMove then
36         remove m from LM
37         continue
38     if not applyMove then
39         continue
40
41 // --- 3. Apply the move ---
42 applyMove(selected, remaining, m)
43 remove m from LM
44
45 // --- 4. Update neighborhood ---
46 changed = {m.A, m.B, m.C, m.D}
47 addNewLocalMovesToLM(LM, selected, remaining, inst, changed, m.type)
48 steepestSearch_LM = LM

```

```

49     return true    // improvement found
50
51 return false    // no improving move found
52 end procedure

```

where validate function is:

```

1 procedure validate(succMap, remaining, m)
2     switch m.type
3
4         case "inter":
5             acb = hasEdge(succMap, m.A, m.C) and hasEdge(succMap, m.C, m.B)
6             bca = hasEdge(succMap, m.B, m.C) and hasEdge(succMap, m.C, m.A)
7             d_in_remaining = (m.D in remaining)
8
9             if ( (acb or bca) and d_in_remaining ) then
10                 return (true, true)    // valid and keep move
11             else
12                 return (false, false) // invalid, discard move
13             end if
14
15         case "intra_edge":
16             ab = hasEdge(succMap, m.A, m.B)
17             ba = hasEdge(succMap, m.B, m.A)
18             cd = hasEdge(succMap, m.C, m.D)
19             dc = hasEdge(succMap, m.D, m.C)
20
21             // If either edge pair no longer exists -> invalid
22             if ( (not ab and not ba) or (not cd and not dc) ) then
23                 return (false, false)
24             end if
25
26             // If both original or reversed edges still valid -> keep
27             if ( (ab and cd) or (ba and dc) ) then
28                 return (true, true)
29             end if
30
31             // Otherwise: temporarily invalid but could remain for later
32             return (false, true)
33
34     end switch
35
36     // Default: unknown move type
37     return (false, false)
38 end procedure

```

and adding new moves function is:

```

1 procedure addNewLocalMovesToLM(LM, selected, remaining, inst, changedNodes,
2     move_type)
3     n = size(selected)

```

```

3
4 // --- 1. Inter-route Re-evaluation ---
5 indices_to_check_inter = {}
6 for each node_id in changedNodes do
7     idx = position of node_id in selected
8     if idx != -1 then
9         add (idx - 1) mod n to indices_to_check_inter
10        add idx to indices_to_check_inter
11        add (idx + 1) mod n to indices_to_check_inter
12    end if
13 end for
14
15 // (A) Re-evaluate neighbors of affected positions with all remaining nodes
16 for each i_idx in indices_to_check_inter do
17     node_i = selected[i_idx]
18     for each node_k in remaining do
19         delta = calculateDeltaInterNode(selected, node_i, node_k, inst)
20         if delta < 0 then
21             prev = selected[(i_idx - 1 + n) mod n]
22             next = selected[(i_idx + 1) mod n]
23             add Move("inter", prev, next, node_i, node_k, delta) to LM
24         end if
25     end for
26 end for
27
28 // (B) If last move was "inter", re-evaluate possible reintroduction of the
29 // removed node
30 if move_type = "inter" then
31     node_c_old = first node in changedNodes such that node in remaining (or -1
32     if none)
33     if node_c_old != -1 then
34         for i_idx = 0 to n-1 do
35             node_i = selected[i_idx]
36             delta = calculateDeltaInterNode(selected, node_i, node_c_old, inst
37         )
38         if delta < 0 then
39             prev = selected[(i_idx - 1 + n) mod n]
40             next = selected[(i_idx + 1) mod n]
41             add Move("inter", prev, next, node_i, node_c_old, delta) to LM
42         end if
43     end for
44 end if
45
46 // --- 2. Intra-route Re-evaluation ---
47 nodes_to_check = copy of changedNodes
48 for each a_node in nodes_to_check do

```

```

49     i_idx = position of a_node in selected
50     if i_idx = -1 then continue
51
52     for j_idx = 0 to n-1 do
53         if i_idx = j_idx then continue
54
55         // Ensure proper ordering
56         if i_idx > j_idx then
57             swap(i_idx, j_idx)
58         end if
59
60         // Skip adjacent edges
61         if (j_idx = i_idx + 1) or (i_idx = 0 and j_idx = n - 1) then continue
62
63         a = selected[i_idx]
64         c = selected[j_idx]
65         delta = calculateDeltaIntraEdge(selected, a, c, inst)
66
67         if delta < 0 then
68             next_a = selected[(i_idx + 1) mod n]
69             next_c = selected[(j_idx + 1) mod n]
70             add Move("intra_edge", a, next_a, c, next_c, delta) to LM
71         end if
72     end for
73 end for
74
75 // --- 3. Sort updated LM by best improvement ---
76 sort LM by delta ascending
77 end procedure

```

### 3 Experimental Results

#### 3.1 TSPA: steepestLM

**Results:** min: 71499 max: 78454 avg: 74278

**Best path:** [177, 10, 190, 4, 112, 84, 35, 131, 149, 47, 65, 116, 43, 42, 115, 59, 51, 176, 80, 79, 133, 151, 162, 123, 127, 70, 135, 154, 180, 53, 63, 94, 124, 152, 97, 1, 101, 86, 75, 2, 120, 44, 25, 16, 171, 175, 113, 56, 31, 38, 157, 196, 81, 90, 165, 119, 40, 185, 179, 145, 78, 92, 57, 55, 52, 106, 178, 3, 49, 102, 14, 144, 62, 9, 148, 137, 23, 89, 183, 143, 0, 117, 93, 140, 68, 46, 139, 41, 193, 159, 69, 108, 18, 22, 181, 160, 34, 54, 48, 184]

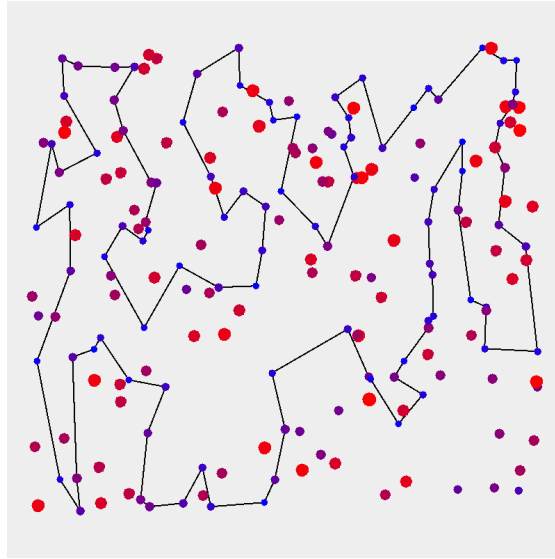


FIGURE 1: Best solution for steepestLM, TSPA.

### 3.2 TSPB: steepestLM

**Results:** min: 46213 max: 52112 avg: 48723

**Best path:** [18, 62, 128, 124, 106, 159, 143, 111, 8, 104, 138, 139, 11, 33, 160, 29, 0, 35, 109, 189, 155, 3, 70, 145, 168, 195, 13, 132, 169, 188, 6, 147, 178, 10, 133, 122, 90, 191, 51, 98, 118, 121, 131, 135, 107, 40, 63, 1, 24, 156, 198, 117, 193, 31, 54, 73, 136, 190, 80, 175, 78, 5, 177, 21, 61, 36, 141, 77, 81, 153, 146, 187, 163, 89, 127, 103, 113, 180, 176, 194, 166, 86, 95, 130, 185, 179, 66, 94, 47, 148, 20, 28, 149, 4, 140, 183, 152, 170, 34, 55]

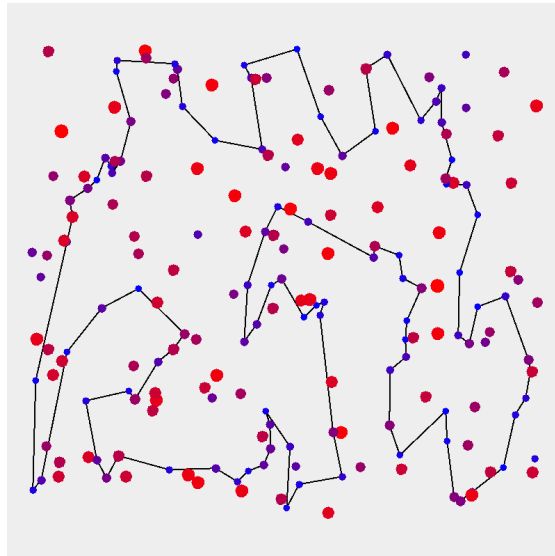


FIGURE 2: Best solution for steepestLM, TSPB.

TABLE 1: Results summary.

TSPA				TSPB			
Method	Average (Avg)	Min	Max	Method	Average (Avg)	Min	Max
<i>Lab 3: LS (Start: Random)</i>				<i>Lab 3: LS (Start: Random)</i>			
R: Steepest+Node	88109	80805	95207	R: Steepest+Node	62972	55302	70406
R: Steepest+Edge	75098	72746	79436	R: Steepest+Edge	49275	46671	52022
<i>Lab 5: LS with LM (Start: Random)</i>				<i>Lab 5: LS with LM (Start: Random)</i>			
R: Steepest+Edge+LM	74278	71499	78454	R: Steepest+Edge+LM	48723	46213	52112

TABLE 2: Execution times (in milliseconds) summary.

TSPA				TSPB			
Method	Average (Avg)	Min	Max	Method	Average (Avg)	Min	Max
<i>Lab 3: LS (Start: Random)</i>				<i>Lab 3: LS (Start: Random)</i>			
R: Steepest+Node	75,49	55,15	352,30	R: Steepest+Node	85,70	55,29	287,95
R: Steepest+Edge	55,12	44,83	115,60	R: Steepest+Edge	65,75	45,59	187,54
<i>Lab 5: LS with LM (Start: Random)</i>				<i>Lab 5: LS with LM (Start: Random)</i>			
R: Steepest+Edge+LM	42,90	30,78	218,94	R: Steepest+Edge+LM	44,79	27,35	207,19

## 4 Conclusions

Based on the results for TSPA and TSPB, the introduction of the Limited Memory (LM) strategy to the Steepest Local Search (LS) proved highly effective. The LS with LM consistently achieved better average and minimum solution costs compared to the standard full steepest search (R: Steepest+Edge) across both problem instances (TSPA: 74278 vs 75098; TSPB: 48723 vs 49275). This improvement suggests that the LM heuristic, by guiding the search with a focused list of high-impact moves, navigated the solution space more effectively, often leading to the discovery of deeper local optima. Crucially, the LM strategy successfully reduced the execution time, validating the main goal of the assignment. Average running time improved by approximately 22% for TSPA and 32% for TSPB.

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**Solution Checker:** All best solutions obtained were verified using the provided solution checker.

**Source Code:** <https://github.com/PBalewski/EvolutionaryComputation/tree/main/lab5>