

# Paul Breiding | Curriculum Vitae

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born 12th of May 1988 in Witzenhausen, Germany, german citizenship



## University of Kassel

*Substitute Professor for Computeralgebra*

11/2020 – 03/2021

## Akademie der Wissenschaften und der Literatur Mainz

*Member of the Junge Akademie*

04/2020 – 03/2024

## Technische Universität Berlin

*Postdoc in the algorithmic algebra research group*

Since 04/2019

## Max-Planck-Institute for Mathematics in the Sciences Leipzig

*Postdoc in the nonlinear algebra research group*

10/2017 – 03/2019

## Technische Universität Berlin

*PhD student with Prof. Dr. Bürgisser*

12/2013 – 09/2017

Date of thesis defense: July 25, 2017. Evaluation 'summa cum laude'.

## Scuola Internazionale Superiore di Studi Avanzati (SISSA)

*Regular research visits*

Since 01/2017

## Simons Institute for the Theory of Computing

*Visiting Graduate Student*

08/2014 – 10/2014

Algorithms and Complexity in Algebraic Geometry

## Education

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### Georg-August-Universität Göttingen

*Master of Science, Grade: 1,1.*

10/2011 – 11/2013

Evaluation: 'excellent'.

### Universidad de Sevilla

*Undergraduate studies, part of the Erasmus exchange program*

02/2011 – 09/2011

### Georg-August Universität Göttingen

*Bachelor of Science, Grade: Sehr Gut (1,5)*

10/2008 – 09/2011

### Otto-Hahn-Gymnasium Göttingen

*Abitur, Grade: Sehr Gut (1,4)*

06/2007

Languages.....

**German:** *fluent, native*

**English:** *fluent*

## Grants

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### Emmy Noether Research Group Grant

*Granted by the Deutsche Forschungsgemeinschaft*

2021

## Publications

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Journal articles.....

- [1] C. Beltrán, P. Breiding, and N. Vannieuwenhoven. Pencil-based algorithms for tensor rank decomposition are not stable. *SIAM J. Matrix Anal. and Appl.* 40(2), 739–773 (2019).
- [2] P. Breiding. An algebraic geometry perspective on topological data analysis. *SIAM News* 53(1) (2020).
- [3] P. Breiding. The expected number of eigenvalues of a real gaussian tensor. *SIAM J. Appl. Algebra Geometry*, 1(1), 254–271 (2017).
- [4] P. Breiding. How many eigenvalues of a random symmetric tensor are real? *Trans. Amer. Math. Soc.* 372,

7857–7887 (2019).

- [5] P. Breiding and P. Bürgisser. Distribution of the eigenvalues of a random system of homogeneous polynomials. *Linear Algebra and its Applications*, 497, 88–107 (2016).
- [6] P. Breiding, H. Keneshlou, and A. Lerario. Quantitative singularity theory for random polynomials. *International Mathematical Research Notices*, to appear.
- [7] P. Breiding, K. Kozhasov, and A. Lerario. On the geometry of the set of symmetric matrices with repeated eigenvalues. *Arnold Math J.* 1(4), 423–443 (2018).
- [8] P. Breiding, K. Kozhasov, and A. Lerario. Random spectrahedra. *SIAM J. Optim.* 29(4), 2608–2624 (2019).
- [9] P. Breiding and O. Marigliano. Random points on an algebraic manifold. *SIAM J. Mathematics of Data Science*, to appear.
- [10] P. Breiding, B. Sturmfels, S. Kalisnik Verovsek, and M. Weinstein. Learning algebraic varieties from samples. *Revista Matemática Complutense*, 31, 545–593 (2018).
- [11] P. Breiding, B. Sturmfels, and S. Timme. 3264 conics in a second. *Not. Amer. Math. Soc.* 67, 30–37 (2020). Article is featured on the title page.
- [12] P. Breiding and N. Vannieuwenhoven. The condition number of join decompositions. *SIAM J. Matrix Anal. and Appl.*, 39(1), 287–309 (2018).
- [13] P. Breiding and N. Vannieuwenhoven. Convergence analysis of Riemannian Gauss-Newton methods and its connection with the geometric condition number. *Applied Mathematics Letters*, 78, 42–50 (2018).
- [14] P. Breiding and N. Vannieuwenhoven. On the average condition number of tensor rank decompositions. *IMA J. Num. Anal.* (2019).
- [15] P. Breiding and N. Vannieuwenhoven. A Riemannian trust region method for the canonical tensor rank approximation problem. *SIAM J. Optim.*, 28, 2435–2465 (2018). Source code for the MATLAB implementation available at <https://arxiv.org/src/1709.00033v2/anc>.

#### Preprints

- [16] C. Beltrán, P. Breiding, and N. Vannieuwenhoven. The average condition number of most tensor rank decomposition problems is infinite. *arXiv1903.05527*.
- [17] P. Breiding. An efficient randomized homotopy method to approximate eigenpairs of tensors. *arXiv1512.03284*.
- [18] P. Breiding and N. Vannieuwenhoven. The condition number of Riemannian approximation problems. *arXiv:1909.12186*.

#### Book projects

- [19] P. Breiding and A. Lerario. *Lectures on Random Algebraic Geometry*. Unpublished work in progress. Available at [page.math.tu-berlin.de/~breiding/rag.html](http://page.math.tu-berlin.de/~breiding/rag.html).

#### Software projects

- [20] P. Breiding and S. Timme. Homotopycontinuation.jl: A package for homotopy continuation in julia. Website: [juliahomotopycontinuation.org](http://juliahomotopycontinuation.org). GitHub: [github.com/JuliaHomotopyContinuation](https://github.com/JuliaHomotopyContinuation). Published in: Mathematical Software – ICMS 2018. Lecture Notes in Computer Science. Open Source software, source code freely available on [github.com](https://github.com).

### Homotopy Continuation.jl

#### Internet publications

- [21] P. Breiding, B. Sturmfels, and S. Timme. [juliahomotopycontinuation.org/do-it-yourself/](http://juliahomotopycontinuation.org/do-it-yourself/). A website, where the user can compute and plot the conics which are tangent to their 5 own conics.
- [22] P. Breiding and S. Timme. [juliahomotopycontinuation.org/examples/](http://juliahomotopycontinuation.org/examples/). An ongoing list of examples where polynomial systems are solved numerically.

#### Theses

- [23] P. Breiding. Zyklotomische Körper und die Fermat–Gleichung zum Exponent  $p^2$ , 2011. Grade: 1.0. First supervisor: Preda Mihailescu. Second supervisor: Maarten Solleveld.
- [24] P. Breiding. On a p-adic newton method. Master’s thesis, Georg-August Universität Göttingen, 2013. Grade: 1.0. First supervisor: Preda Mihailescu. Second supervisor: Peter Bürgisser.
- [25] P. Breiding. *Numerical and Statistical Aspects of Tensor Decompositions*. PhD thesis, TU Berlin, 2017. Grade: summa cum laude. First supervisor: Peter Bürgisser. Second supervisor: Felipe Cucker.

## Teaching experience

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<b>Numerical Algebraic Geometry with Julia</b> <i>Freie Universität Berlin</i>	<b>Lecturer</b> 09/2019–03/2020
<b>Seminar: Numerical Nonlinear Algebra</b> <i>Technische Universität Berlin</i>	<b>Lecturer</b> 04/2019–07/2019
<b>Lecture: Condition – the geometry of numerical algorithms</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	<b>Lecturer</b> 10/2018–01/2019
<b>Mathematik für unbegleitete minderjährige Flüchtlinge</b> <i>Stiftung SPI Berlin</i>	<b>Teacher</b> 03/2016–11/2016
<b>Gewöhnliche Differentialgleichungen</b> <i>TU Berlin</i> Undergraduate course for students in Engineering	<b>Teaching Assistant</b> 04/2017 – 09/2017
<b>Algebra, Multivariate Polynomials</b> <i>TU Berlin</i> Undergraduate courses for students in Mathematics	<b>Teaching Assistant</b> 12/2013 – 04/2017
<b>Analysis, Lineare algebra</b> <i>TU Berlin</i> Undergraduate courses for students in Engineering	<b>Tutor</b> 12/2013 – 04/2017
<b>Statistische Beratung</b> <i>Institut für medizinische Statistik, UMG Göttingen</i>	<b>Tutor</b> 06/2013 – 09/2013
<b>Lineare Algebra 1 &amp; 2, Mikroökonomik 1 &amp; 2</b> <i>Georg-August-Universität Göttingen</i>	<b>Tutor</b> 10/2010 – 03/2013

## Organizational experience

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<b>Minisymposium on Random Geometry and Topology</b> <i>SIAM Conference on Applied Algebraic Geometry</i>	<b>Organizer</b> 07/2019
<b>Minisymposium on Numerical Methods in Algebraic Geometry</b> <i>SIAM Conference on Applied Algebraic Geometry</i>	<b>Organizer</b> 07/2019
<b>Summer School on Randomness and Learning in Nonlinear Algebra</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	<b>Organizer</b> 07/2019
<b>Workshop on Random Algebraic Geometry</b> <i>SISSA</i>	<b>Organizer</b> 11/2018
<b>Max-Planck Day</b> <i>Munich</i> Presentation of MPI MiS to a general audience	<b>Organizer</b> 09/2018
<b>Summer School on Numerical Computing in Algebraic Geometry</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	<b>Organizer</b> 08/2018
<b>Berlin-Leipzig Seminar on Algebra, Geometry and Combinatorics</b> <i>MPI for Mathematics in the Sciences/TU Berlin/FU Berlin</i>	<b>Organizer</b> 10/2017 – 12/2017

## Peer reviewing

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for the following journals: SIAM Journal on Applied Algebra and Geometry, Linear Algebra and its Applications, Journal Foundations of Computational Mathematics, Proceedings of the Royal Society A, Journal of the American Mathematical Society, Mathematics of Computation

## Invited talks

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<b>Symmetry, Randomness, and Computations in Real Algebraic Geometry</b> <i>ICERM</i>	08/2020
<b>Mathematics for Complex Data</b> <i>KTH Stockholm</i>	06/2020

<b>Mathematical Software Day</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	12/2019
<b>Complexity of Numerical Computation</b> <i>Berlin-Brandenburgische Akademie der Wissenschaften</i> Conference in honor of Felipe Cucker	08/2019
<b>SIAM Conference on Applied Algebraic Geometry</b> <i>University of Bern</i> Minisymposium on the algebra and geometry of tensors	07/2019
<b>Workshop on Geometry, Topology, and Computation</b> <i>Mathematikon, Universität Heidelberg</i>	06/2019
<b>Computeralgebra Tagung</b> <i>Universität Kassel</i>	05/2019
<b>Low-Rank Optimization and Applications</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	04/2019
<b>Complexity Reduction in Algebraic Statistics</b> <i>OvGU Magdeburg</i>	11/2018
<b>Workshop on Random Real Geometry</b> <i>SISSA</i>	10/2018
<b>Seminar za Numeričku Matematiku i Znan. Računanje</b> <i>University of Zagreb</i>	10/2018
<b>TENSORS</b> <i>University of Torino</i>	09/2018
<b>International Symposium on Mathematical Programming (ISMP)</b> <i>University of Bordeaux</i>	07/2018
<b>Numerical Methods for Curves</b> <i>University of Rennes</i>	02/2018
<b>9th polymake conference and developer meeting</b> <i>TU Berlin</i>	02/2018
<b>Seminar Numerische Lineare Algebra</b> <i>University of Osnabrück</i>	01/2018
<b>Open Source Computer Algebra Research (OSCAR)</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	12/2017
<b>2nd Algebraic Statistics Day</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	11/2017
<b>Algebra meets Numerics: Condition and Complexity</b> <i>TU Berlin</i>	11/2017
<b>SIAM Conference on Applied Algebraic Geometry</b> <i>Georgia Tech, Atlanta.</i> Minisymposium on Random Algebraic Geometry	07/2017
<b>Reading Group on Real Algebraic Geometry</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	07/2017
<b>Foundations of Computational Mathematics Conference</b> <i>University of Barcelona</i> Real Number Complexity workshop	07/2017
<b>"What is ...?" seminar</b> <i>TU Berlin</i> Live recording available at <a href="https://vimeo.com/256622174">vimeo.com/256622174</a>	07/2017
<b>Tensors: Algebra meets Numerics</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	12/2016
<b>Algorithms and Complexity in Algebraic Geometry reunion meeting</b> <i>Simons Institute for the Theory of Computing, Berkeley</i>	12/2015