

# Paul Breiding | Curriculum Vitae

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born 12th of May 1988, german citizenship



## Head of Emmy Noether Research Group

*Numerical and Probabilistic Nonlinear Algebra*

04/2021 – 03/2027

## University of Kassel

*Substitute Professor for Computeralgebra*

11/2020 – 03/2021

## Akademie der Wissenschaften und der Literatur Mainz

*Member of the Junge Akademie*

04/2020 – 03/2024

## Parental leave

*7 months in total*

10/2019 – 11/2019 and 04/2020 – 10/2020

## Technische Universität Berlin

*Postdoc in the algorithmic algebra research group*

04/2019 – 10/2020

## Max-Planck-Institute for Mathematics in the Sciences Leipzig

*Postdoc in the nonlinear algebra research group*

10/2017 – 03/2019

## Technische Universität Berlin

*PhD student with Prof. Dr. Bürgisser*

12/2013 – 09/2017

Date of thesis defense: July 25, 2017. Evaluation 'summa cum laude'.

## Simons Institute for the Theory of Computing

*Visiting Graduate Student*

08/2014 – 10/2014

Algorithms and Complexity in Algebraic Geometry

## Education

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### Georg-August-Universität Göttingen

*Master of Science*

10/2011 – 11/2013

Evaluation: excellent.

### Universidad de Sevilla

*Undergraduate studies, part of the Erasmus exchange program*

02/2011 – 09/2011

### Georg-August Universität Göttingen

*Bachelor of Science*

10/2008 – 09/2011

Languages.....

**German:** *fluent, native*

**English:** *fluent*

## Grants

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### Emmy Noether Research Group Grant

Granted by the Deutsche Forschungsgemeinschaft

*Project title: Numerical and Probabilistic Nonlinear Algebra*

2020

Total amount: 1.073.150 €

## Publications

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Journal articles.....

- [1] C. Beltrán, P. Breiding, and N. Vannieuwenhoven. Pencil-based algorithms for tensor rank decomposition are not stable. *SIAM J. Matrix Anal. and Appl.* 40(2), 739–773 (2019).
- [2] P. Breiding. An algebraic geometry perspective on topological data analysis. *SIAM News* 53(1) (2020).
- [3] P. Breiding. The expected number of eigenvalues of a real gaussian tensor. *SIAM J. Appl. Algebra Geometry*, 1(1), 254–271 (2017).

- [4] P. Breiding. How many eigenvalues of a random symmetric tensor are real? *Trans. Amer. Math. Soc.* 372, 7857–7887 (2019).
- [5] P. Breiding and P. Bürgisser. Distribution of the eigenvalues of a random system of homogeneous polynomials. *Linear Algebra and its Applications*, 497, 88–107 (2016).
- [6] P. Breiding, H. Keneshlou, and A. Lerario. Quantitative singularity theory for random polynomials. *International Mathematical Research Notices* (2020).
- [7] P. Breiding, K. Kozhasov, and A. Lerario. On the geometry of the set of symmetric matrices with repeated eigenvalues. *Arnold Math J.* 1(4), 423–443 (2018).
- [8] P. Breiding, K. Kozhasov, and A. Lerario. Random spectrahedra. *SIAM J. Optim.* 29(4), 2608–2624 (2019).
- [9] P. Breiding and O. Marigliano. Random points on an algebraic manifold. *SIAM J. Mathematics of Data Science* 2(3), 683–704 (2020).
- [10] P. Breiding, B. Sturmfels, S. Kalisnik Verovsek, and M. Weinstein. Learning algebraic varieties from samples. *Revista Matemática Complutense*, 31, 545–593 (2018).
- [11] P. Breiding, B. Sturmfels, and S. Timme. 3264 conics in a second. *Not. Amer. Math. Soc.* 67, 30–37 (2020). Article is featured on the title page.
- [12] P. Breiding and N. Vannieuwenhoven. The condition number of join decompositions. *SIAM J. Matrix Anal. and Appl.*, 39(1), 287–309 (2018).
- [13] P. Breiding and N. Vannieuwenhoven. Convergence analysis of Riemannian Gauss-Newton methods and its connection with the geometric condition number. *Applied Mathematics Letters*, 78, 42–50 (2018).
- [14] P. Breiding and N. Vannieuwenhoven. On the average condition number of tensor rank decompositions. *IMA J. Num. Anal.* (2019).
- [15] P. Breiding and N. Vannieuwenhoven. A Riemannian trust region method for the canonical tensor rank approximation problem. *SIAM J. Optim.*, 28, 2435–2465 (2018). Source code for the MATLAB implementation available at <https://arxiv.org/src/1709.00033v2/anc>.

#### Preprints.....

- [16] C. Beltrán, P. Breiding, and N. Vannieuwenhoven. The average condition number of most tensor rank decomposition problems is infinite. *arXiv1903.05527*.
- [17] P. Breiding. An efficient randomized homotopy method to approximate eigenpairs of tensors. *arXiv1512.03284*.
- [18] P. Breiding, C. Ikenmeyer, R. Hodges, and M. Michalek. Equations for  $gl$  invariant families of polynomials. Preprint available at <http://pcwww.liv.ac.uk/~iken/GL-paper/GL-paper.pdf>.
- [19] P. Breiding, K. Rose, and S. Timme. Certifying zeros of polynomial systems using interval arithmetic. *arXiv:2011.05000*.
- [20] P. Breiding, F. Sottile, and J. Woodcock. Euclidean distance degree and mixed volume. *arXiv:2012.06350*.
- [21] P. Breiding and N. Vannieuwenhoven. The condition number of Riemannian approximation problems. *arXiv:1909.12186*.

#### Book projects.....

- [22] P. Breiding and A. Lerario. *Lectures on Random Algebraic Geometry*. Unpublished work in progress. Available at <https://pbrdng.github.io/rag.html>.

#### Software projects.....

- [23] P. Breiding and S. Timme. Homotopycontinuation.jl: A package for homotopy continuation in julia. Website: [juliahomotopycontinuation.org](http://juliahomotopycontinuation.org). GitHub: [github.com/JuliaHomotopyContinuation](https://github.com/JuliaHomotopyContinuation). Published in: Mathematical Software – ICMS 2018. Lecture Notes in Computer Science. Open Source software, source code freely available on [github.com](https://github.com).

**Homotopy  
Continuation.jl**

#### Websites.....

- [24] P. Breiding, B. Sturmfels, and S. Timme. [juliahomotopycontinuation.org/do-it-yourself/](http://juliahomotopycontinuation.org/do-it-yourself/). A website, where the user can compute and plot the conics which are tangent to their 5 own conics.
- [25] P. Breiding and S. Timme. [juliahomotopycontinuation.org/examples/](http://juliahomotopycontinuation.org/examples/). An ongoing list of examples.

- Theses.....
- [26] P. Breiding. Zyklotomische Körper und die Fermat–Gleichung zum Exponent  $p^2$ ., 2011. Grade: 1.0. First supervisor: Preda Mihailescu. Second supervisor: Maarten Solleveld.
- [27] P. Breiding. On a p-adic newton method. Master’s thesis, Georg-August Universität Göttingen, 2013. Grade: 1.0. First supervisor: Preda Mihailescu. Second supervisor: Peter Bürgisser.
- [28] P. Breiding. *Numerical and Statistical Aspects of Tensor Decompositions*. PhD thesis, TU Berlin, 2017. Grade: summa cum laude. First supervisor: Peter Bürgisser. Second supervisor: Felipe Cucker.

## Teaching experience

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<b>Lecture: Statistics for engineers</b> <i>Universität Kassel</i>	<b>Lecturer</b> 11/2020–03/2021
<b>Lecture: Computeralgebra</b> <i>Universität Kassel</i>	<b>Lecturer</b> 11/2020–03/2021
<b>Seminar: Mathematics for primary school teachers</b> <i>Universität Kassel</i>	<b>Lecturer</b> 11/2020–03/2021
<b>Lecture: Numerical algebraic geometry with Julia</b> <i>Freie Universität Berlin</i>	<b>Lecturer</b> 09/2019–03/2020
<b>Seminar: Numerical nonlinear algebra</b> <i>Technische Universität Berlin</i>	<b>Lecturer</b> 04/2019–07/2019
<b>Lecture: Condition – the geometry of numerical algorithms</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	<b>Lecturer</b> 10/2018–01/2019
<b>Mathematik für unbegleitete minderjährige Flüchtlinge</b> <i>Stiftung SPI Berlin</i>	<b>Teacher</b> 03/2016–11/2016
<b>Gewöhnliche Differentialgleichungen, Algebra, Multivariate Polynomials</b> <i>TU Berlin</i> Undergraduate course for students in Engineering and Mathematics	<b>Teaching Assistant</b> 04/2017 – 09/2017
<b>Analysis, Lineare algebra</b> <i>TU Berlin</i> Undergraduate courses for students in Engineering	<b>Tutor</b> 12/2013 – 04/2017
<b>Statistische Beratung</b> <i>Institut für medizinische Statistik, UMG Göttingen</i>	<b>Tutor</b> 06/2013 – 09/2013
<b>Lineare Algebra 1 &amp; 2, Mikroökonomik 1 &amp; 2</b> <i>Georg-August-Universität Göttingen</i>	<b>Tutor</b> 10/2010 – 03/2013

## Organizational experience

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<b>Workshop Computational Algebra 2020</b> <i>Online workshop</i>	<b>Organizer</b> 11/2020
<b>Minisymposium on Random Geometry and Topology</b> <i>SIAM Conference on Applied Algebraic Geometry</i>	<b>Organizer</b> 07/2019
<b>Minisymposium on Numerical Methods in Algebraic Geometry</b> <i>SIAM Conference on Applied Algebraic Geometry</i>	<b>Organizer</b> 07/2019
<b>Summer School on Randomness and Learning in Nonlinear Algebra</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	<b>Organizer</b> 07/2019
<b>Workshop on Random Algebraic Geometry</b> <i>SISSA</i>	<b>Organizer</b> 11/2018
<b>Max-Planck Day</b> <i>Munich</i> Presentation of MPI MiS to a general audience	<b>Organizer</b> 09/2018
<b>Summer School on Numerical Computing in Algebraic Geometry</b> <i>Max-Planck Institute for Mathematics in the Sciences</i>	<b>Organizer</b> 08/2018

## Peer reviewing

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for the following journals: SIAM Journal on Applied Algebra and Geometry, Linear Algebra and its Applications, Journal Foundations of Computational Mathematics, Proceedings of the Royal Society A, Journal of the American Mathematical Society, Mathematics of Computation.

## References

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**Bernd Sturmfels:** bernd@mis.mpg.de

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**Carlos Beltrán:** beltranc@unican.es

Av. de los Castros, 39005 Santander, Spain

**Peter Bürgisser:** pbuerg@math.tu-berlin.de

Technische Universität Berlin, Straße des 17. Juni 136, 10623 Berlin, Germany.

**Antonio Lerario:** lerario@sissa.it

SISSA, Via Bonomea 265 Trieste, Italy.

**Nick Vannieuwenhoven:** nick.vannieuwenhoven@cs.kuleuven.be

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