# Paul Breiding | Curriculum Vitae

Universität Osnabrück, FB Mathematik/Informatik, Albrechtstr. 28a, D-49076 Osnabrück

□ pbreiding@uni-osnabrueck.de • □ paulbreiding.org • □ PBrdng
□ Paul Breiding • □ □ pbrdng • born 12th of May 1988, german citizenship

Universität Osnabrück		
Professor for Mathematical Methods in Data Science		$Since \ 04/2022 \ on$
Max-Plack-Institute for Mathematics in the Sciences Leipzig  Head of Emmy Noether Research Group:  Numerical and Probabilistic Nonlinear Algebra		04/2021 - 03/2022
University of Kassel Substitute Professor for Computeralgebra		11/2020 - 03/2021
Akademie der Wissenschaften und der Literatur Mainz Speaker of the Junge Akademie   Mainz		02/2022 - 02/2023
Akademie der Wissenschaften und der Literatur Mainz Member of the Junge Akademie   Mainz		04/2020 - 03/2024
Parental leave 7 months in total	10/2019 - 11/2019 and	04/2020 - 10/2020
<b>Technische Universität Berlin</b> Postdoctoral researcher in the algorithmic algebra research group		04/2019 - 10/2020
Max-Plack-Institute for Mathematics in the Sciences Leipzig  Postdoctoral researcher in the nonlinear algebra research group		10/2017 - 03/2019
<b>Technische Universität Berlin</b> PhD student with Prof. Dr. Bürgisser Date of thesis defense: July 25, 2017. Evaluation 'summa cum laude'.		12/2013 - 09/2017
Simons Institute for the Theory of Computing Visiting graduate student Algorithms and Complexity in Algebraic Geometry		08/2014 - 10/2014
Education		
Georg-August-Universität Göttingen  Master of Science  Evaluation: excellent.  Universidad de Sevilla		10/2011 - 11/2013
Undergraduate studies, part of the Erasmus exchange program		02/2011 - 09/2011
Georg-August Universität Göttingen Bachelor of Science		10/2008 - 09/2011
Languages		
German: fluent, native		
English: fluent		

### **External Funding**

Emmy Noether Research Group Grant

Granted by the Deutsche Forschungsgemeinschaft

Total amount: €1.132.600

2020

Project title: Numerical and Probabilistic Nonlinear Algebra

### Awards

### SIAG/AG Early Career Prize

Awarded by the SIAM Activity Group on Algebraic Geometry

2021

### Service

**Peer reviewing** for the following journals: SIAM Journal on Applied Algebra and Geometry, Linear Algebra and its Applications, Journal Foundations of Computational Mathematics, Proceedings of the Royal Society A, Journal of the American Mathematical Society, Mathematics of Computation.

Editorial board member of Numerical Algebra, Control and Optimization.

## Teaching experience

Lecture: Analysis 1 Universität Osnabrück	Lecturer 10/2022-02/2023
Lecture: Elemente der Datenanalyse Universität Osnabrück	<b>Lecturer</b> 10/2022-02/2023
Lecture: Mathematische Grundlagen der Datenanalyse Universität Osnabrück	$ \begin{array}{c} \textbf{Lecturer} \\ \textit{04/2022-07/2022} \end{array} $
Lecture: Random Algebraic Geometry Universität Leipzig	$ \frac{ \mathbf{Lecturer} }{ 10/2021 - 03/2022 } $
IMPRS Ringvorlesung Max-Planck Institute for Mathematics in the Sciences	<b>Lecturer</b> 04/2021-06/2021
Lecture: Statistics for engineers Universität Kassel	<b>Lecturer</b> 11/2020-03/2021
All lectures and exercises are available on and Computeralgebra  Universität Kassel	$\frac{\textbf{Lecturer}}{11/2020-03/2021}$
All lectures are available on and $\Omega$ ; lecture for high school teachers  Seminar: Mathematics for primary school teachers  Universität Kassel	<b>Lecturer</b> 11/2020-03/2021
Lecture: Numerical algebraic geometry with Julia Freie Universität Berlin	$\begin{array}{c} \textbf{Lecturer} \\ 09/2019 – 03/2020 \end{array}$
Seminar: Numerical nonlinear algebra Technische Universität Berlin	<b>Lecturer</b> 04/2019-07/2019
Lecture: Condition – the geometry of numerical algorithms  Max-Planck Institute for Mathematics in the Sciences	<b>Lecturer</b> 10/2018-01/2019
Mathematik für unbegleitete minderjährige Flüchtlinge $Stiftung\ SPI\ Berlin$	<b>Teacher</b> 03/2016-11/2016
Statistische Beratung Institut für medizinische Statistik, UMG Göttingen	<b>Tutor</b> 06/2013 - 09/2013

### Organizational experience

Random Algebraic Geometry BIRS Workshop	$\begin{array}{c} \textbf{Organizer} \\ 04/2023 \end{array}$
Stochastic Geometry Universität Osnabrück	$\begin{array}{c} \textbf{Organizer} \\ 11/2023 \end{array}$
Geometry in Complexity and Computations $Universit\ddot{a}t\ Konstanz$	$\begin{array}{c} \textbf{Organizer} \\ \textit{09/2022} \end{array}$
The 1st and 2nd East German Tensor Day One-day workshop	<b>Organizer</b> 09/2021 and 12/2021

Workshop on Software and Applications of Numerical Nonlinear Algebra $Online\ workshop$	$\begin{array}{c} \textbf{Organizer} \\ 06/2021 \end{array}$
Workshop Computational Algebra 2020 Online workshop	$\begin{array}{c} \textbf{Organizer} \\ 11/2020 \end{array}$
Minisymposium on Random Geometry and Topology SIAM Conference on Applied Algebraic Geometry	$\begin{array}{c} \textbf{Organizer} \\ 07/2019 \end{array}$
Minisymposium on Numerical Methods in Algebraic Geometry SIAM Conference on Applied Algebraic Geometry	$\begin{array}{c} \textbf{Organizer} \\ 07/2019 \end{array}$
Summer School on Randomness and Learning in Nonlinear Algebra Max-Planck Institute for Mathematics in the Sciences	$\begin{array}{c} \textbf{Organizer} \\ 07/2019 \end{array}$
Workshop on Random Algebraic Geometry $SISSA$	Organizer $11/2018$
Max-Planck Day (presentation of MPI MiS to a general audience) $Munich$	$\begin{array}{c} \textbf{Organizer} \\ 09/2018 \end{array}$
Summer School on Numerical Computing in Algebraic Geometry Max-Planck Institute for Mathematics in the Sciences	Organizer $08/2018$
EROC - European Roller Derby Organizational Conference International conference with $\sim 150$ participants; topics included diversity and inclusion	<b>Organizer</b> 2016 and 2017

#### **Publications**

Journal articles....

- [1] C. Beltrán, P. Breiding, and N. Vannieuwenhoven. Pencil-based algorithms for tensor rank decomposition are not stable. SIAM J. Matrix Anal. and Appl. 40(2), 739–773 (2019).
- [2] C. Beltrán, P. Breiding, and N. Vannieuwenhoven. The average condition number of most tensor rank decomposition problems is infinite. *Foundations of Computational Mathematics.*, 2022.
- [3] P. Breiding. An algebraic geometry perspective on topological data analysis. SIAM News 53(1) (2020).
- [4] P. Breiding. The expected number of eigenvalues of a real gaussian tensor. SIAM J. Appl. Algebra Geometry, 1(1), 254–271 (2017).
- [5] P. Breiding. How many eigenvalues of a random symmetric tensor are real? Trans. Amer. Math. Soc. 372, 7857–7887 (2019).
- [6] P. Breiding and P. Bürgisser. Distribution of the eigenvalues of a random system of homogeneous polynomials. *Linear Algebra and its Applications*, 497, 88–107 (2016).
- [7] P. Breiding, P. Bürgisser, A. Lerario, and L. Mathis. The zonoid algebra, generalized mixed volumes, and random determinants. *Adv. in Math. (to appear)*.
- [8] P. Breiding, T. Çelik, T. Duff, A. Heaton, A. Maraj, A. Sattelberger, L. Venturello, and O. Yürük. Nonlinear algebra and applications. *Numerical Algebra, Optimization and Control.*, 2021.
- [9] P. Breiding, R. Hodges, C. Ikenmeyer, and M. Michalek. Equations for GL invariant families of polynomials. *Vietnam Journal of Mathematics.*, 2022.
- [10] P. Breiding, H. Keneshlou, and A. Lerario. Quantitative singularity theory for random polynomials. *International Mathematical Research Notices* (2020).
- [11] P. Breiding, K. Kozhasov, and A. Lerario. On the geometry of the set of symmetric matrices with repeated eigenvalues. *Arnold Math J.* 1(4), 423–443 (2018).
- [12] P. Breiding, K. Kozhasov, and A. Lerario. Random spectrahedra. SIAM J. Optim. 29(4), 2608–2624 (2019).
- [13] P. Breiding and O. Marigliano. Random points on an algebraic manifold. SIAM J. Mathematics of Data Science 2(3), 683–704 (2020).
- [14] P. Breiding, F. Sottile, and J. Woodcock. Euclidean distance degree and mixed volume. Foundations of Computational Mathematics, 2021.
- [15] P. Breiding, B. Sturmfels, S. Kalisnik Verovsek, and M. Weinstein. Learning algebraic varieties from samples. *Revista Matemática Complutense*, 31, 545–593 (2018).
- [16] P. Breiding, B. Sturmfels, and S. Timme. 3264 conics in a second. Not. Amer. Math. Soc. 67, 30–37 (2020). Article is featured on the title page.
- [17] P. Breiding and N. Vannieuwenhoven. The condition number of join decompositions. SIAM J. Matrix Anal. and Appl., 39(1), 287–309 (2018).

- [18] P. Breiding and N. Vannieuwenhoven. The condition number of Riemannian approximation problems. SIAM J. Optim. 31(1), 1049–1077 (2021).
- [19] P. Breiding and N. Vannieuwenhoven. Convergence analysis of Riemannian Gauss-Newton methods and its connection with the geometric condition number. *Applied Mathematics Letters*, 78, 42–50 (2018).
- [20] P. Breiding and N. Vannieuwenhoven. On the average condition number of tensor rank decompositions. *IMA J. Num. Anal.* (2019).
- [21] P. Breiding and N. Vannieuwenhoven. A Riemannian trust region method for the canonical tensor rank approximation problem. SIAM J. Optim., 28, 2435-2465 (2018).
- [22] N. Dewaele, P. Breiding, and N. Vannieuwenhoven. The condition number of many tensor decompositions is invariant under Tucker compression. *Numerical Algorithms (to appear)*.

Preprints.....

- [23] P. Blagojević, P. Breiding, and A. Heaton. Facet volumes of polytopes. arXiv:2112.08437.
- [24] Michałek M. Monin L Breiding, P. and S. Telen. The algebraic degree of coupled oscillators. arXiv:2208.08179.
- [25] P. Breiding. An efficient randomized homotopy method to approximate eigenpairs of tensors. arXiv1512.03284.
- [26] P. Breiding, F. Gesmundo, M. Michalek, and N. Vannieuwenhoven. Algebraic compressed sensing. arXiv2108.13208.
- [27] P. Breiding, K. Ranestad, and M. Weinstein. Enumerative geometry of curvature of algebraic hypersurfaces. arXiv:2206.09130.
- [28] P. Breiding, K. Rose, and S. Timme. Certifying zeros of polynomial systems using interval arithmetic. arXiv:2011.05000.
- [29] P. Breiding, F. Rydell, E. Shehu, and A. Torres. Line multiview varieties. arXiv:2203.01694.
- [30] P. Breiding and N. Vannieuwenhoven. Sensitivity of low-rank matrix recovery. arXiv:2103.00531.
- [31] N. Dewaele, P. Breiding, and N. Vannieuwenhoven. Three decompositions of symmetric tensors have similar condition numbers. *arXiv:2110.04172*.

Software projects.....

[32] P. Breiding and S. Timme. Homotopycontinuation.jl: A package for homotopy continuation in Julia. 

§ juliahomotopycontinuation.org. 

§ github.com/JuliaHomotopyContinuation. Open Source software. 

Homotopy

#### Homotopy Continuation.jl

Lecture notes.

- [33] P. Breiding and S. Fairchild. *Mathematical Methods in Data Science*. Unpublished work in progress. Available at https://pbrdng.github.io/MathData.pdf.
- [34] P. Breiding and A. Lerario. Lectures on Random Algebraic Geometry. Unpublished work in progress. Available at https://pbrdng.github.io/rag.html.

Wahsites

[35] P. Breiding, B. Sturmfels, and S. Timme. juliahomotopycontinuation.org/do-it-yourself/. A website, where the user can compute and plot the conics which are tangent to their 5 own conics.

Theses

- [36] P. Breiding. Zyklotomische Körper und die Fermat-Gleichung zum Exponent  $p^2$ ., 2011. Grade: 1.0. First supervisor: Preda Mihailescu. Second supervisor: Maarten Solleveld.
- [37] P. Breiding. On a p-adic newton method. Master's thesis, Georg-August Universität Göttingen, 2013. Grade: 1.0. First supervisor: Preda Mihailescu. Second supervisor: Peter Bürgisser.
- [38] P. Breiding. Numerical and Statistical Aspects of Tensor Decompositions. PhD thesis, TU Berlin, 2017. Grade: summa cum laude. First supervisor: Peter Bürgisser. Second supervisor: Felipe Cucker.

#### References

Carlos Beltrán: beltranc@unican.es

Universidad de Santander, Av. de los Castros, 39005 Santander, Spain

Peter Bürgisser: pbuerg@math.tu-berlin.de

Technische Universität Berlin, Straße des 17. Juni 136, 10623 Berlin, Germany.

Antonio Lerario: lerario@sissa.it

SISSA, Via Bonomea 265 Trieste, Italy. **Bernd Sturmfels**: bernd@mis.mpg.de

MPI für Mathematik in den Naturwissenschaften, Inselstraße 22, 04103 Leipzig, Germany

**Nick Vannieuwenhoven**: nick.vannieuwenhoven@cs.kuleuven.be KU Leuven, Celestijnenlaan 200 A, B-3001 Heverlee, Belgium.