

# Regiones de decision

## Regiones de decision

Tags: Reconocimiento de Patrones, Clasificación, funciones discriminantes y superficies de decision

$$P(x|w_i) \approx N(\mu_i, \Sigma_i) \quad (2.3.15)$$

$$P(x|w_1) \approx N(0, I) \rightarrow \text{Lubina}$$

$$P(x|w_2) \approx N\left(\begin{pmatrix} 1 \\ 1 \end{pmatrix}, I\right)$$

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- $P(x|w_2) \approx N\left(\begin{pmatrix} 1 \\ 1 \end{pmatrix}, I\right)$

Paso 1:

$$x = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

$$g_1(x) = (-1/2) \left[ \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \end{pmatrix} \right]^t \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \left( \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \end{pmatrix} \right) - (1/2) \ln(1) + \ln(1/2)$$

$$g_1(x) = (-1/2) \left[ \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} \right]^t \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \ln(1/2)$$

$$g_1(x) = (-1/2) [x_1^2 + x_2^2] + \ln(1/2)$$

$$g_1(x) = -1/2 x_1^2 - 1/2 x_2^2 + \ln(1/2)$$

$$g_2(x) = (-1/2) \left[ \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - \begin{pmatrix} 1 \\ 1 \end{pmatrix} \right]^t \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \left( \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - \begin{pmatrix} 1 \\ 1 \end{pmatrix} \right) - (1/2) \ln(1) + \ln(1/2)$$

$$g_2(x) = (-1/2) \left[ \begin{pmatrix} x_1 - 1 \\ x_2 - 1 \end{pmatrix} \right]^t \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x_1 - 1 \\ x_2 - 1 \end{pmatrix} + \ln(1/2)$$

$$g_2(x) = (-1/2) [x_1^2 - 2x_1 + 1 + x_2^2 - 2x_2 + 1] + \ln(1/2)$$

$$g_2(x) = -1/2 x_1^2 + x_1 - 1 - 1/2 x_2^2 + x_2 + \ln(1/2)$$

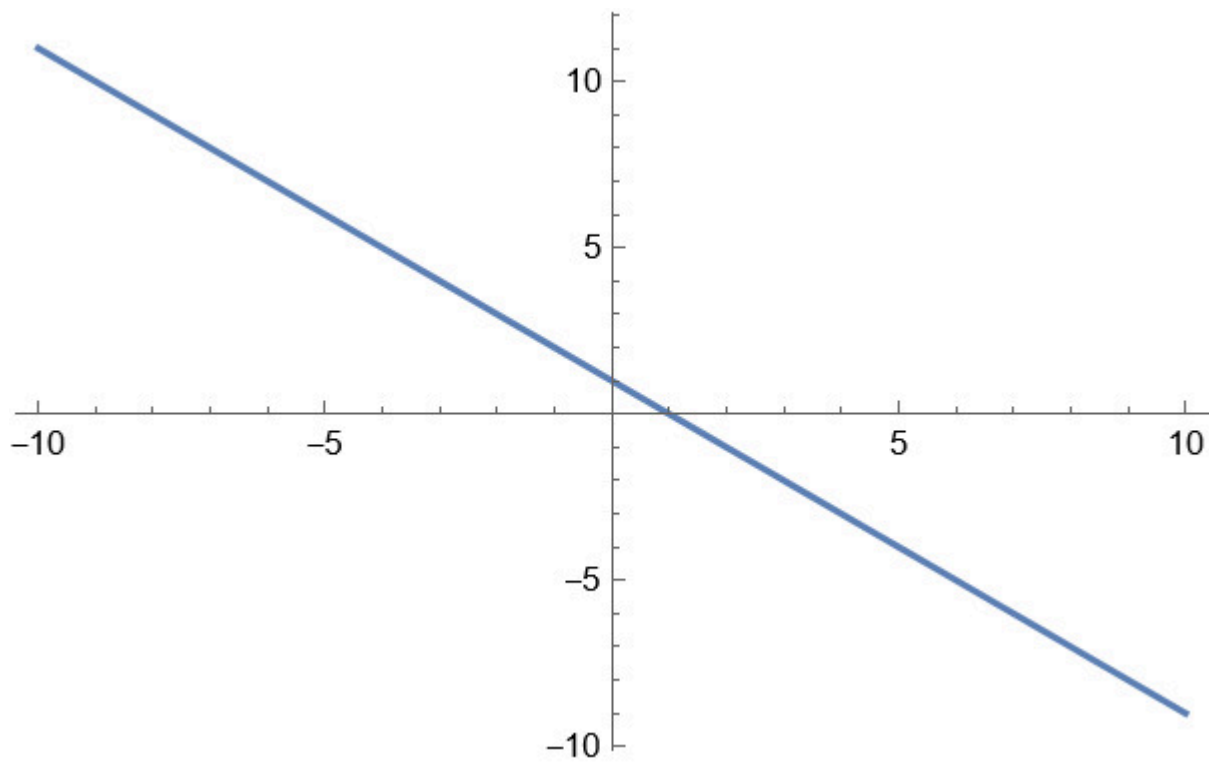
Paso 2: Igualar ecuaciones

$$g_1(x) = g_2(x) \text{ para toda } i \neq j$$

$$-1/2x_1^2 - 1/2x_2^2 + \ln(1/2) = -1/2x_1^2 + x_1 - 1 - 1/2x_2^2 + x_2 + \ln(1/2)$$

$$0 = x_1 - 1 + x_2$$

$$x_1 = 1 - x_2$$



## References

Tarea 4 - RDC