

CE310 – Evolutionary Algorithm

Assignment part 2

Problem 1:

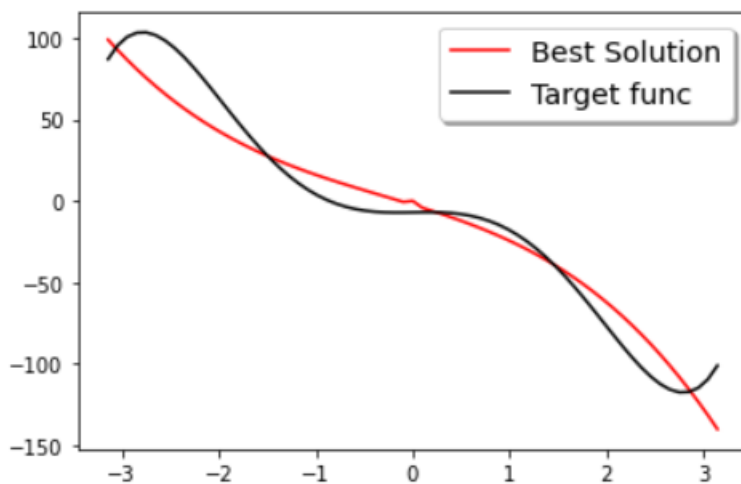
$$p_1(x) = x^5 - 13 \cdot x^3 + x - 7$$

Experiment 1:

Parameters:

Population size = 500, Tournament size = 2

(Usual result)

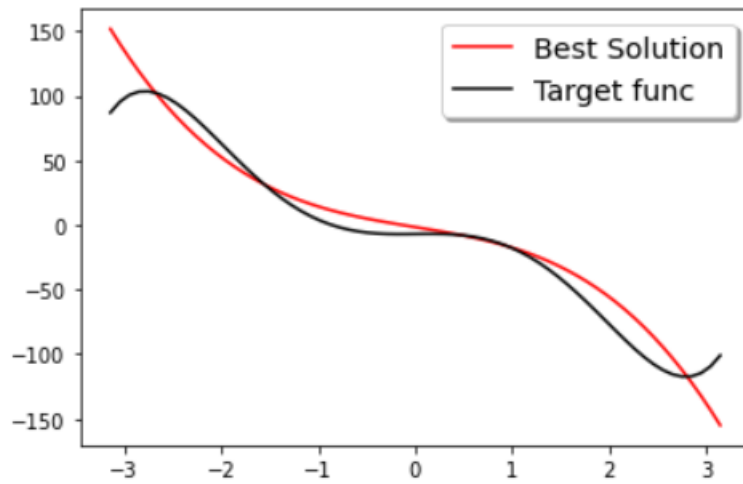


Experiment 2:

Parameters:

Population size = 2000, Tournament size = 2

(Usual result)

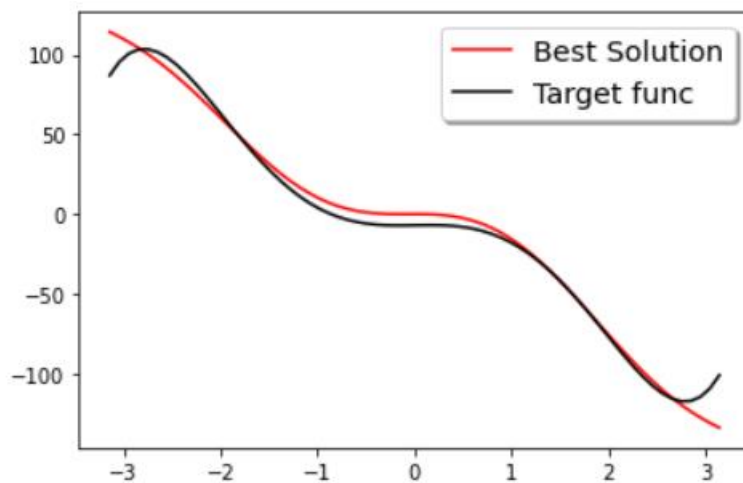


Experiment 3:

Parameters:

Population size = 500, Tournament size = 5

(Usual result)

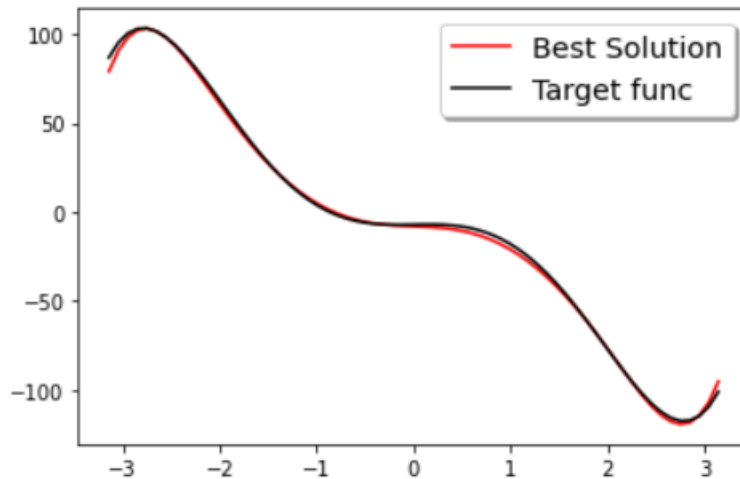


Experiment 4:

Parameters:

Population size = 2000, Tournament size = 5

(Usual result)



The GA seems to minimise fitness, hence indicating that the fitness function measures the area or distance (squared) between the curves, and a lower fitness value represents the result being closer to the original problem (equation) - difference between each value of x (for GP and actual equation).

The plot showing normalised fitness and size shows a general decrease in fitness and an increase in size, however different Hyper Parameters influence convergence (of fitness) and the growth of the program, such that the generated program will reflect the original problem much more accurately (optimal performance) through the generations.

(All chosen statistics for each run are the same: minimum and maximum from the mean and median fitness and size of the individual, as well as the average size in the first and last generation)

It is expected that the GP with a higher population size will produce a better solution (program) as this parameter has a significant impact on performance in GAs, and much like GAs, it will explore and sample more of the search space (more likely to find an optimal solution).

Run (N)	Experiment 1	Experiment 2	Experiment 3	Experiment 4
1	Fitness: (min, max) 3027.960744969552 , 4209.121486537739 Mean Fitness: Gen 0: 4.10322e+27 Gen 15: 4.79136e+27 Gen 30: 7.36063e+28 Median Fitness: Gen 0: 4209.12 Gen 15: 3979.02 Gen 30: 3027.96 Evaluations: 12339	Fitness: (min, max) 3067.431286301585 , 4209.121486537739 Mean Fitness: Gen 0: 3.47436e+28 Gen 15: 2.53776e+28 Gen 30: 1.91681e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 3967.81 Gen 30: 3067.43 Evaluations: 49230	Fitness: (min, max) 116.3140600227790 5, 4203.066755640003 Mean Fitness: Gen 0: 1.58421e+29 Gen 15: 3.25717e+31 Gen 30: 3.97979e+31 Median Fitness: Gen 0: 4203.07 Gen 15: 333.408 Gen 30: 116.314 Evaluations: 12477	Fitness: (min, max) 115.8619714728973 , 4209.121486537739 Mean Fitness: Gen 0: 3.35841e+28 Gen 15: 5.6502e+31 Gen 30: 8.06935e+31 Median Fitness: Gen 0: 4209.12 Gen 15: 886.282 Gen 30: 115.862 Evaluations: 49491

2	Fitness: (min, max) 2733.653415848689 ', 4209.121486537739 Mean Fitness: Gen 0: 4213.98 Gen 15: 3900.27 Gen 30: 3286.93 Median Fitness: Gen 0: 4209.12 Gen 15: 3949.9 Gen 30: 2733.65 Evaluations: 12342	Fitness: (min, max) 1913.732416961233 4, 4201.988404596935 Mean Fitness: Gen 0: 1.23097e+28 Gen 15: 1.06589e+29 Gen 30: 1.11501e+28 Median Fitness: Gen 0: 4201.99 Gen 15: 3942.84 Gen 30: 1913.73 Evaluations: 49323	Fitness: (min, max) 220.3948119287469 2, 4209.121486537739 Mean Fitness: Gen 0: 1.05614e+29 Gen 15: 80581.5 Gen 30: 87151.8 Median Fitness: Gen 0: 4209.12 Gen 15: 941.616 Gen 30: 225.187 Evaluations: 12441	Fitness: (min, max) 122.0263021286373 5, 4209.121486537739 Mean Fitness: Gen 0: 3.33228e+28 Gen 15: 1.91232e+32 Gen 30: 1.57488e+32 Median Fitness: Gen 0: 4209.12 Gen 15: 807.618 Gen 30: 122.026 Evaluations: 49295
	Fitness: (min, max) 3250.203134153122 ', 4209.121486537739 Mean Fitness: Gen 0: 3.28258e+28 Gen 15: 3946.64 Gen 30: 3230.9 Median Fitness: Gen 0: 4209.12 Gen 15: 3960.9 Gen 30: 3250.2 Evaluations: 12390	Fitness: (min, max) 2777.021050776826 ', 4208.73146377518 Mean Fitness: Gen 0: 4.16185e+28 Gen 15: 2.7563e+28 Gen 30: 6.56727e+29 Median Fitness: Gen 0: 4208.73 Gen 15: 3949.9 Gen 30: 2777.02 Evaluations: 49331	Fitness: (min, max) 184.1438697551839 ', 4202.74913496607 Mean Fitness: Gen 0: 1.64129e+28 Gen 15: 4.37797e+29 Gen 30: 1848.68 Median Fitness: Gen 0: 4202.75 Gen 15: 1890.62 Gen 30: 184.144 Evaluations: 12351	Fitness: (min, max) 264.4946758304673 ', 4201.988404596935 Mean Fitness: Gen 0: 1.17062e+29 Gen 15: 3.79241e+31 Gen 30: 9.99228e+28 Median Fitness: Gen 0: 4201.99 Gen 15: 981.616 Gen 30: 264.495 Evaluations: 49280
4	Fitness: (min, max) 3125.209598890105 ', 4209.121486537739 Mean Fitness: Gen 0: 4223.66 Gen 15: 9.90772e+29 Gen 30: 1.48499e+30 Median Fitness:	Fitness: (min, max) 49332 Mean Fitness: Gen 0: 7.31892e+28 Gen 15: 4.30553e+28 Gen 30: 7.3279e+28 Median Fitness: Gen 0: 4209.12	Fitness: (min, max) 498.7967379176175 ', 4201.557635366166 Mean Fitness: Gen 0: 4205.49 Gen 15: 3.46892e+30 Gen 30: 31827.9 Median Fitness:	Fitness: (min, max) 388.9261335259753 ', 4201.557635366166 Mean Fitness: Gen 0: 2.84168e+28 Gen 15: 4.02264e+28 Gen 30: 2.59882e+31 Median Fitness:

	Gen 0: 4209.12 Gen 15: 3973.9 Gen 30: 3125.21 Evaluations: 12395	Gen 15: 3971.75 Gen 30: 2853.34 Evaluations: 2853.3414754845544, 4209.121486537739	Gen 15: 2125.81 Gen 30: 518.793 Evaluations: 12430	Gen 0: 4201.56 Gen 15: 1460.76 Gen 30: 388.926 Evaluations: 49240
5	Fitness: (min, max) 2937.8809080751785, 4209.121486537739 Mean Fitness: Gen 0: 1.16215e+28 Gen 15: 3921.56 Gen 30: 4214.34 Median Fitness: Gen 0: 4209.12 Gen 15: 3955.3 Gen 30: 2937.88 Evaluations: 12294	Fitness: (min, max) 2989.8270739602244, 4208.73146377518 Mean Fitness: Gen 0: 1.22117e+29 Gen 15: 1.07108e+29 Gen 30: 1.23189e+30 Median Fitness: Gen 0: 4208.73 Gen 15: 3973.9 Gen 30: 2989.83 Evaluations: 49484	Fitness: (min, max) 218.2536008394273, 4208.73146377518 Mean Fitness: Gen 0: 1.64129e+28 Gen 15: 1.64129e+28 Gen 30: 4629.57 Median Fitness: Gen 0: 4208.73 Gen 15: 295.112 Gen 30: 218.254 Evaluations: 12407	Fitness: (min, max) 215.5741290869868, 4209.121486537739 Mean Fitness: Gen 0: 3.5075e+28 Gen 15: 8.70091e+29 Gen 30: 1.03019e+28 Median Fitness: Gen 0: 4209.12 Gen 15: 791.132 Gen 30: 215.574 Evaluations: 49340
6	Fitness: (min, max) 2959.914826220891, 4209.121486537739 Mean Fitness: Gen 0: 4.1695e+28 Gen 15: 6.12967e+28 Gen 30: 1.09541e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 3974.31 Gen 30: 2959.91 Evaluations: 12404	Fitness: (min, max) 2989.8270739602244, 4208.73146377518 Mean Fitness: Gen 0: 2.2606e+28 Gen 15: 4.55581e+29 Gen 30: 2.79164e+28 Median Fitness: Gen 0: 4208.73 Gen 15: 3962.82 Gen 30: 2608.09 Evaluations: 49484	Fitness: (min, max) 96.10946424798601, 4202.874080105195 Mean Fitness: Gen 0: 1.64129e+28 Gen 15: 6.56515e+28 Gen 30: 1626.41 Median Fitness: Gen 0: 4202.87 Gen 15: 722.488 Gen 30: 97.8533 Evaluations: 12447	Fitness: (min, max) 201.3213063144171, 4208.73146377518 Mean Fitness: Gen 0: 2.58045e+28 Gen 15: 2.51549e+30 Gen 30: 7.95467e+30 Median Fitness: Gen 0: 4208.73 Gen 15: 808.281 Gen 30: 201.321 Evaluations: 49331
7	Fitness: (min, max) 2623.2971469283375, 4209.121486537739 Mean Fitness:	Fitness: (min, max) 2548.8146597057703, 4209.121486537739 Mean Fitness:	Fitness: (min, max) 98.95583670322767, 4201.557635366166 Mean Fitness:	Fitness: (min, max) 144.93090989056884, 4208.623395724519 Mean Fitness:

	Gen 0: 4.10322e+27 Gen 15: 6.10133e+28 Gen 30: 2.12206e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 3973.9 Gen 30: 2623.3 Evaluations: 12447	Gen 0: 4.72573e+28 Gen 15: 1.96759e+28 Gen 30: 1.2812e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 3905.59 Gen 30: 2548.81 Evaluations: 49264	Gen 0: 3.28258e+28 Gen 15: 3.12042e+30 Gen 30: 11495.5 Median Fitness: Gen 0: 4201.56 Gen 15: 1809.34 Gen 30: 98.9558 Evaluations: 12479	Gen 0: 6.83723e+28 Gen 15: 1.86709e+30 Gen 30: 6.69029e+29 Median Fitness: Gen 0: 4208.62 Gen 15: 1210.39 Gen 30: 144.931 Evaluations: 49426
8	Fitness: (min, max) 3368.848398043906 4, 4209.121486537739 Mean Fitness: Gen 0: 7.0086e+27 Gen 15: 4.10322e+27 Gen 30: 356959 Median Fitness: Gen 0: 4209.12 Gen 15: 3973.9 Gen 30: 3368.85 Evaluations: 12363	Fitness: (min, max) 2041.035863486703 2, 4208.623395724519 Mean Fitness: Gen 0: 2.73018e+28 Gen 15: 7.90765e+28 Gen 30: 4.3841e+29 Median Fitness: Gen 0: 4208.62 Gen 15: 3960.9 Gen 30: 2041.04 Evaluations: 49519	Fitness: (min, max) 266.9140147122643 6, 4201.557635366166 Mean Fitness: Gen 0: 5.81079e+28 Gen 15: 3096.91 Gen 30: 8.80471e+30 Median Fitness: Gen 0: 4201.56 Gen 15: 837.58 Gen 30: 291.884 Evaluations: 12339	Fitness: (min, max) 115.5006798304723 6, 4209.121486537739 Mean Fitness: Gen 0: 3.57631e+28 Gen 15: 8.28092e+29 Gen 30: 7.12734e+28 Median Fitness: Gen 0: 4209.12 Gen 15: 788.858 Gen 30: 115.501 Evaluations: 49414
9	Fitness: (min, max) 1344.591559830749 2, 4201.557635366166 Mean Fitness: Gen 0: 1.0151e+29 Gen 15: 1.37512e+28 Gen 30: 4.10322e+27 Median Fitness: Gen 0: 4201.56 Gen 15: 3884.38 Gen 30: 1344.59 Evaluations:	Fitness: (min, max) 2543.223590181326 5, 4209.121486537739 Mean Fitness: Gen 0: 4.58554e+28 Gen 15: 5.39873e+28 Gen 30: 5.89392e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 3960.9 Gen 30: 2543.22	Fitness: (min, max) 158.0736534606831 , 4209.121486537739 Mean Fitness: Gen 0: 4212.66 Gen 15: 1.0323e+30 Gen 30: 1.61989e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 420.252 Gen 30: 158.074 Evaluations:	Fitness: (min, max) 141.4452942687726 7, 4209.121486537739 Mean Fitness: Gen 0: 5.07552e+28 Gen 15: 9.34734e+30 Gen 30: 1.52943e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 648.188 Gen 30: 141.445

	12261	Evaluations: 49623	12324	Evaluations: 49344
10	Fitness: (min, max) 2954.480081247207 6, 4209.121486537739 Mean Fitness: Gen 0: 2.90538e+27 Gen 15: 4.10322e+27 Gen 30: 3539.58 Median Fitness: Gen 0: 4209.12 Gen 15: 3960.9 Gen 30: 2954.48 Evaluations: 12246	Fitness: (min, max) 1972.912877948857 2, 4208.73146377518 Mean Fitness: Gen 0: 3.04684e+28 Gen 15: 8.04689e+28 Gen 30: 1.25604e+29 Median Fitness: Gen 0: 4208.73 Gen 15: 3755.66 Gen 30: 1972.91 Evaluations: 49307	Fitness: (min, max) 197.7015595379879 2, 4209.121486537739 Mean Fitness: Gen 0: 1.64129e+28 Gen 15: 43472.1 Gen 30: 10265.2 Median Fitness: Gen 0: 4209.12 Gen 15: 1126.96 Gen 30: 197.702 Evaluations: 12413	Fitness: (min, max) 211.1363418786587 8, 4209.121486537739 Mean Fitness: Gen 0: 2.55114e+28 Gen 15: 1.82485e+30 Gen 30: 1.23055e+29 Median Fitness: Gen 0: 4209.12 Gen 15: 792.227 Gen 30: 211.136 Evaluations: 49310

Problem 2:

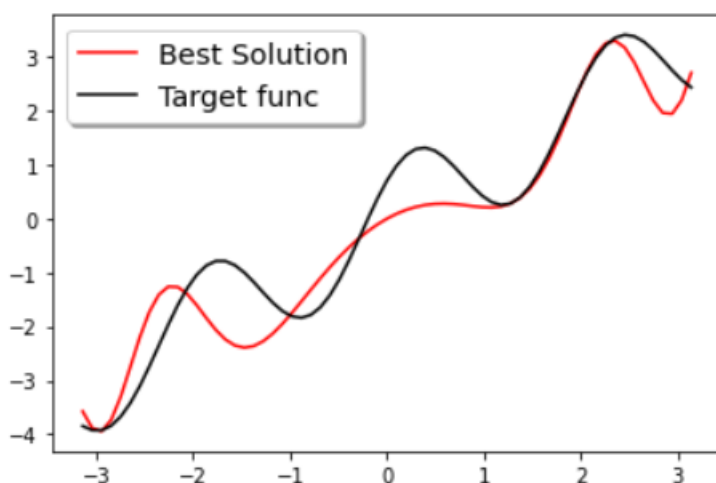
$$p_2(x) = \sin\left(\frac{\pi}{4} + 3 \cdot x\right) + x$$

Experiment 1:

Parameters:

Population size = 500, Tournament size = 2

(Usual result)

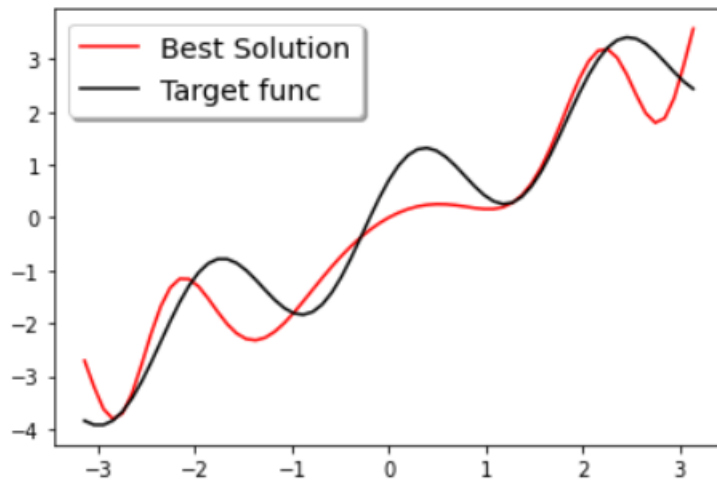
**Experiment 2:**

Student ID: 1804900

Parameters:

Population size = 2000, Tournament size = 2

(Usual result)

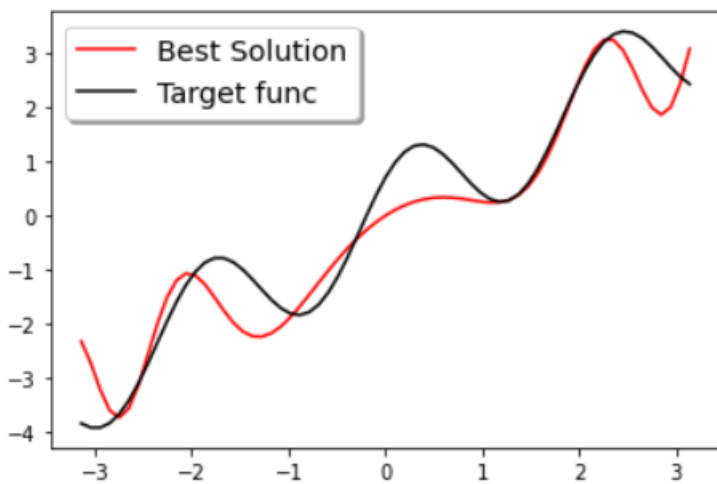


Experiment 3:

Parameters:

Population size = 500, Tournament size = 5

(Usual result)

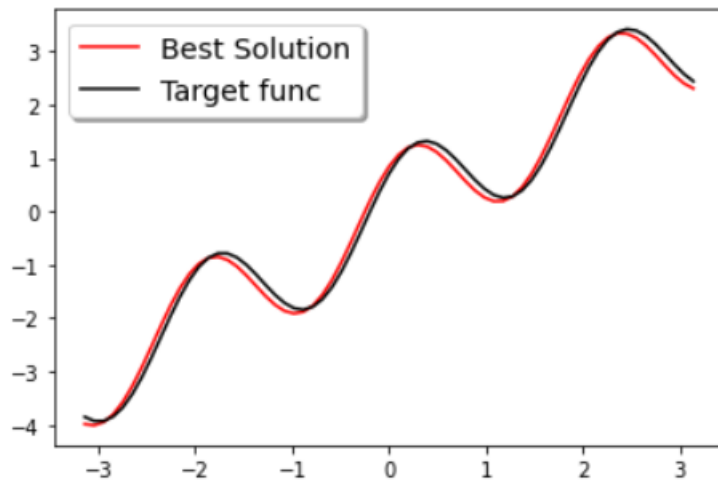


Experiment 4:

Parameters:

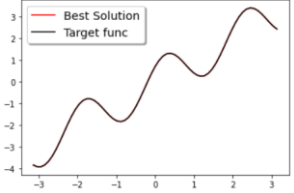
Population size = 2000, Tournament size = 5

(Usual result)



Run (N)	Experiment 1	Experiment 2	Experiment 3	Experiment 4
1	Fitness: (min, max) 0.5000000000000000 1, 5.043233995630595	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548
	Mean Fitness: Gen 0: 1.64129e+28 Gen 15: 4.10322e+27 Gen 30: 1.06149e+29	Mean Fitness: Gen 0: 1.20993e+29 Gen 15: 5.12903e+27 Gen 30: 4.97454e+27	Mean Fitness: Gen 0: 5.12523e+28 Gen 15: 4.87036e+28 Gen 30: 7.44961	Mean Fitness: Gen 0: 3.51642e+28 Gen 15: 2.47708 Gen 30: 1.11799e+29
	Median Fitness: Gen 0: 5.21666 Gen 15: 0.5 Gen 30: 0.5	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.860604	Median Fitness: Gen 0: 5.07985 Gen 15: 0.816615 Gen 30: 0.670642
	Evaluations: 12457	Evaluations: 49420	Evaluations: 12371	Evaluations: 49566
2	Fitness: (min, max) 0.478632368511468 4, 5.07984998575548	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.444085056771500 34, 5.043233995630595	Fitness: (min, max) 0.493627483655798 67, 5.07984998575548
	Mean Fitness: Gen 0: 5.21187e+28 Gen 15: 4.04972e+28 Gen 30: 5.69101e+28	Mean Fitness: Gen 0: 4.70533e+28 Gen 15: 7.0086e+27 Gen 30: 7.90765e+28	Mean Fitness: Gen 0: 4.79136e+27 Gen 15: 26.262 Gen 30: 0.890222	Mean Fitness: Gen 0: 1.69609e+28 Gen 15: 1.37507e+30 Gen 30: 8.05807e+60
	Median Fitness:	Median Fitness:	Median Fitness: Gen 0: 5.04323	Median Fitness:

	Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 12358	Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 49292	Gen 15: 0.992308 Gen 30: 0.444085 Evaluations: 12369	Gen 0: 5.07985 Gen 15: 0.493627 Gen 30: 0.493627 Evaluations: 49352
3	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548 Mean Fitness: Gen 0: 4.04972e+28 Gen 15: 1.39872e+27 Gen 30: 5.62219e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.484901 Gen 30: 0.492585 Evaluations: 12340	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548 Mean Fitness: Gen 0: 3.33675e+28 Gen 15: 2.55353 Gen 30: 5.18193e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 49464	Fitness: (min, max) 0.456372728063965 , 5.07984998575548 Mean Fitness: Gen 0: 4.28928e+28 Gen 15: 2.29125 Gen 30: 0.922137 Median Fitness: Gen 0: 5.07985 Gen 15: 0.946356 Gen 30: 0.456373 Evaluations: 12295	Fitness: (min, max) 0.407410576959953 3, 5.07984998575548 Mean Fitness: Gen 0: 3.47819e+28 Gen 15: 1.51753e+29 Gen 30: 2.35626e+30 Median Fitness: Gen 0: 5.07985 Gen 15: 1.42877 Gen 30: 0.407411 Evaluations: 49496
4	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548 Mean Fitness: Gen 0: 4.46004e+28 Gen 15: 4.1695e+28 Gen 30: 1.9865 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 12312	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548 Mean Fitness: Gen 0: 6.73019e+28 Gen 15: 6.27974e+28 Gen 30: 1.94983e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 49465	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548 Mean Fitness: Gen 0: 3.28258e+28 Gen 15: 1.93379 Gen 30: 1.35782 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.609894 Evaluations: 12381	Fitness: (min, max) 0.203909206064839 8, 5.07984998575548 Mean Fitness: Gen 0: 3.44378e+28 Gen 15: 3.53462e+29 Gen 30: 0.720065 Median Fitness: Gen 0: 5.07985 Gen 15: 0.566918 Gen 30: 0.203909 Evaluations: 49418

				 <p>Perfect Solution!</p>
5	Fitness: (min, max) 0.5000000000000000 1, 5.309954308961832	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.492330516723973 54, 5.043233995630595	Fitness: (min, max) 0.255446046725775 87, 5.07984998575548
	Mean Fitness: Gen 0: 3.28258e+28 Gen 15: 9.57061e+28 Gen 30: 4.62048e+29	Mean Fitness: Gen 0: 2.55114e+28 Gen 15: 2.05161e+27 Gen 30: 1.01604e+28	Mean Fitness: Gen 0: 6.30882 Gen 15: 1.07836e+28 Gen 30: 6.23028	Mean Fitness: Gen 0: 2.55114e+28 Gen 15: 6.42789 Gen 30: 1.01243e+28
	Median Fitness: Gen 0: 5.30995 Gen 15: 0.5 Gen 30: 0.5	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5	Median Fitness: Gen 0: 5.04323 Gen 15: 0.5 Gen 30: 0.493627	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.255446
	Evaluations: 12336	Evaluations: 49243	Evaluations: 12362	Evaluations: 49463
6	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.301677979887848 6, 5.07984998575548	Fitness: (min, max) 0.451170923751723 8, 5.07984998575548
	Mean Fitness: Gen 0: 1.93183e+28 Gen 15: 1.64129e+28 Gen 30: 1.18446e+28	Mean Fitness: Gen 0: 4.48999e+28 Gen 15: 1.83307e+28 Gen 30: 3.35405e+28	Mean Fitness: Gen 0: 7.74262e+28 Gen 15: 2.96992 Gen 30: 0.591947	Mean Fitness: Gen 0: 5.99492e+28 Gen 15: 1.41057e+60 Gen 30: 2.52673e+91
	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5	Median Fitness: Gen 0: 5.07985 Gen 15: 0.655457 Gen 30: 0.301678	Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.451171
	Evaluations: 12387	Evaluations: 49328	Evaluations: 12346	Evaluations: 49412
7	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.5000000000000000 1, 5.07984998575548	Fitness: (min, max) 0.5000000000000000 1, 5.288197177233015	Fitness: (min, max) 0.404162583777748 44, 5.07984998575548

	Mean Fitness: Gen 0: 7.09492 Gen 15: 2.36559 Gen 30: 1.28327e+28 Median Fitness: Gen 0: 0.5 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 12362	Mean Fitness: Gen 0: 3.26302e+28 Gen 15: 2.09749e+28 Gen 30: 4.74529e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 49456	Mean Fitness: Gen 0: 6.38604 Gen 15: 4.04972e+28 Gen 30: 8.04212e+29 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 5.2882 Evaluations: 12442	Mean Fitness: Gen 0: 2.56834e+28 Gen 15: 5.72289e+28 Gen 30: 9.58817e+27 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.404163 Evaluations: 49391
8	Fitness: (min, max) Mean Fitness: Gen 0: 1.16215e+28 Gen 15: 2.21578 Gen 30: 4.04972e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 12286	Fitness: (min, max) 0.49362748365579867, 5.07984998575548 Mean Fitness: Gen 0: 4.04972e+28 Gen 15: 1.74387e+28 Gen 30: 4.63226e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.493627 Evaluations: 49249	Fitness: (min, max) 0.4962927210708832, 5.07984998575548 Mean Fitness: Gen 0: 6.10133e+28 Gen 15: 7.4084e+27 Gen 30: 1.24624 Median Fitness: Gen 0: 5.07985 Gen 15: 0.992308 Gen 30: 0.496293 Evaluations: 12286	Fitness: (min, max) 0.4553641008437071, 5.043233995630595 Mean Fitness: Gen 0: 1.55293e+28 Gen 15: 11.2825 Gen 30: 1.18222e+28 Median Fitness: Gen 0: 5.04323 Gen 15: 1.52034 Gen 30: 0.455364 Evaluations: 49401
9	Fitness: (min, max) 0.50000000000000001, 5.107523988709597 Mean Fitness: Gen 0: 6.10133e+28 Gen 15: 5.37531 Gen 30: 2.57192 Median Fitness: Gen 0: 5.10752 Gen 15: 0.5 Gen 30: 0.5 Evaluations:	Fitness: (min, max) 0.50000000000000001, 5.051989430488548 Mean Fitness: Gen 0: 2.20899e+28 Gen 15: 1.42275e+28 Gen 30: 2.01597e+28 Median Fitness: Gen 0: 5.05199 Gen 15: 0.5 Gen 30: 0.5	Fitness: (min, max) 0.48725496731159723, 5.07984998575548 Mean Fitness: Gen 0: 4.57982e+28 Gen 15: 4.04972e+29 Gen 30: 1.89793e+29 Median Fitness: Gen 0: 5.07985 Gen 15: 0.510574 Gen 30: 0.426697	Fitness: (min, max) 0.44100515334044743, 5.07984998575548 Mean Fitness: Gen 0: 4.38804e+28 Gen 15: 1.41054e+29 Gen 30: 3.13815 Median Fitness: Gen 0: 5.07985 Gen 15: 1.52176 Gen 30: 0.441005

	12447			
		Evaluations: 49323	Evaluations: 12376	Evaluations: 49318
10	Fitness: (min, max) 0.49362748365579867, 5.07984998575548 Mean Fitness: Gen 0: 1.64129e+28 Gen 15: 4.46004e+28 Gen 30: 8.32755e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.493627 Evaluations: 12311	Fitness: (min, max) 0.50000000000000001, 5.07984998575548 Mean Fitness: Gen 0: 2.7563e+28 Gen 15: 2.27717e+28 Gen 30: 5.64439e+28 Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.5 Evaluations: 49407	Fitness: (min, max) 0.49362748365579867, 5.07984998575548 Mean Fitness: Gen 0: 6.49314 Gen 15: 1.64129e+28 Gen 30: 4.85662 Median Fitness: Gen 0: 5.07985 Gen 15: 0.493627 Gen 30: 1.27929 Evaluations: 12311	Fitness: (min, max) 0.4211721498665185, 5.07984998575548 Mean Fitness: Gen 0: 2.02549e+28 Gen 15: 1.02581e+27 Gen 30: 1.47361 Median Fitness: Gen 0: 5.07985 Gen 15: 0.794008 Gen 30: 0.421172 Evaluations: 49421

The general correlation between all experiments shows that the most effective hyper parameter for the fitness of a program is **population size**. This is due to the search space being explored more deeply with a higher population, therefore an optimal solution is more likely to be explored, as opposed to a smaller population, which would likely result in a less optimal solution (less than ideal fitness).

In terms of **tournament** size, it is also a very prominent parameter that goes hand in hand with the population size. With a higher population, and a bigger tournament size of 5, there is more of a chance of picking fitter individuals as they are compared to a higher number of other individuals within the tournament. 2 individuals could both have a low fitness, in which case the individual with only a slightly better fitness is chosen - the average fitness increases slightly. A size of 5 individuals increases the probability of an individual with a significantly higher fitness being chosen – the optimal tournament size depends on the population size, but the average fitness will be much better.

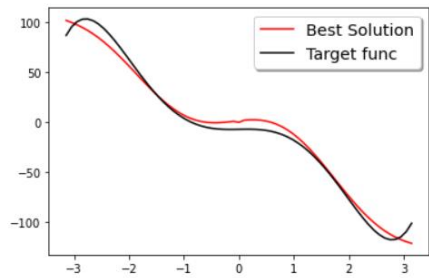
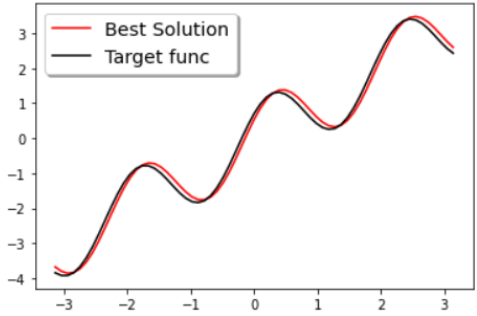
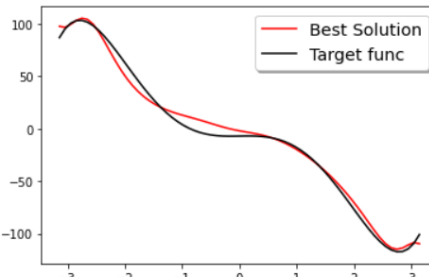
In this case, the larger population size proves to be more effective than a lower one, as there is more likely to be individuals with a higher fitness (a higher probability) selected to be in the tournament.

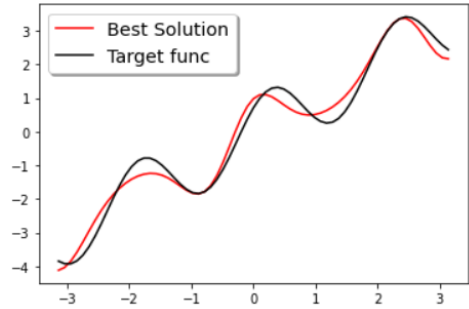
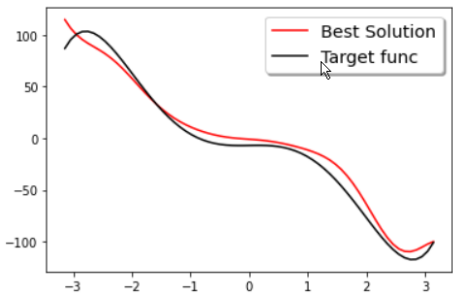
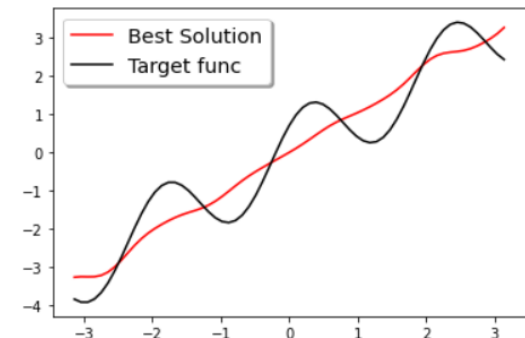
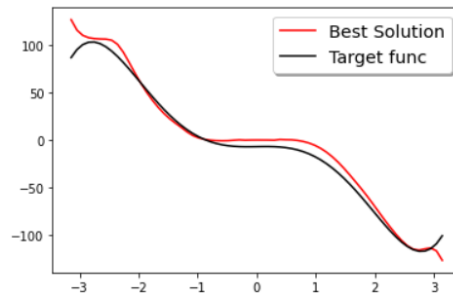
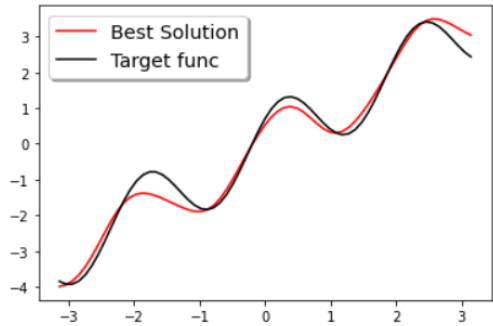
As every program in the population is randomly generated, there were inevitable variations based around the typical result shown for each experiment, and in some tests the variations between the fittest programs were ample – the fittest individuals for each run would vary but usually have a similarly shaped function, however there would be the exception where the shape of the solution is very different to the perfect solution – this was especially seen in experiments 1, 2 and 3. Experiment 4, which used the best combination of parameters for generating the (most accurate) fittest individual, had more variations based on the function produced (visual representation), but not enough to say they were ample – only on a rare occasion would the GP produce a clearly unfit program. This is likely because more randomly generated programs are produced (higher

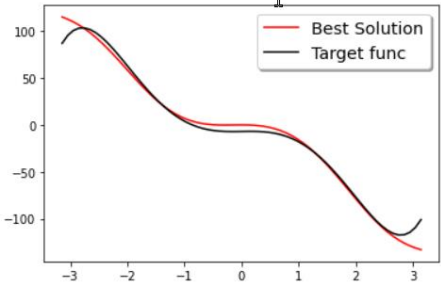
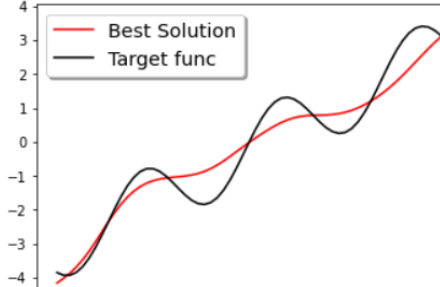
population) – as each new individual is generated via reproduction, crossover, mutation, or architecture altering operation (all mutually exclusive), a higher population is likely to have more mutated individuals, which can cause more of these varied results (fluctuation of fitness).

As shown by the table below, the next 10 runs (5 runs for each problem) show consistent results with the first batch.

Chosen optimal configuration (tournament size: 5, population size: 2000)

Run (N)	Experiment 4 - Batch 2 (Problem 1)	Experiment 4 – Batch 2 (Problem 2)
1	<p>Fitness: (min, max) 77.70481229401409, 4208.926475156459</p> <p>Mean Fitness: Gen 0: 5.92229e+28 Gen 15: 6.43256e+28 Gen 30: 4.34448e+30</p> <p>Median Fitness: Gen 0: 4208.93 Gen 15: 974.716 Gen 30: 77.7048</p> <p>Evaluations: 49300</p> 	<p>Fitness: (min, max) 0.331951084272608, 5.07984998575548</p> <p>Mean Fitness: Gen 0: 3.2692e+28 Gen 15: 5544.7 Gen 30: 2.50416e+27</p> <p>Median Fitness: Gen 0: 5.07985 Gen 15: 0.493627 Gen 30: 0.331951</p> <p>Evaluations: 49531</p> 
2	<p>Fitness: (min, max) 122.3946813017185, 4209.121486537739</p> <p>Mean Fitness: Gen 0: 2.03823e+28 Gen 15: 4.93917e+28 Gen 30: 3058.48</p> <p>Median Fitness: Gen 0: 4209.12 Gen 15: 373.811 Gen 30: 122.395</p> <p>Evaluations: 49546</p> 	<p>Fitness: (min, max) 0.4386016516407071, 5.07984998575548</p> <p>Mean Fitness: Gen 0: 2.7563e+28 Gen 15: 1.02581e+27 Gen 30: 1.02581e+27</p> <p>Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.438602</p> <p>Evaluations: 49501</p>

		
3	<p>Fitness: (min, max) 277.4425697063118, 4209.121486537739</p> <p>Mean Fitness: Gen 0: 1.74387e+28 Gen 15: 2.48569e+28 Gen 30: 5.21661e+30</p> <p>Median Fitness: Gen 0: 4209.12 Gen 15: 846.895 Gen 30: 277.443 Evaluations: 49360</p> 	<p>Fitness: (min, max) 0.4398736331590296, 5.07984998575548</p> <p>Mean Fitness: Gen 0: 8.43393e+28 Gen 15: 1.91876e+29 Gen 30: 9.40742e+28</p> <p>Median Fitness: Gen 0: 5.07985 Gen 15: 1.24145 Gen 30: 0.439874 Evaluations: 49466</p> 
4	<p>Fitness: (min, max) 113.51705923459308, 4209.121486537739</p> <p>Mean Fitness: Gen 0: 4.55879e+28 Gen 15: 5.86994e+31 Gen 30: 4.44499e+30</p> <p>Median Fitness: Gen 0: 4209.12 Gen 15: 788.163 Gen 30: 113.517 Evaluations: 49319</p> 	<p>Fitness: (min, max) 0.18202754167865454, 5.07984998575548</p> <p>Mean Fitness: Gen 0: 2.81556e+28 Gen 15: 2.9447e+29 Gen 30: 1.05316e+28</p> <p>Median Fitness: Gen 0: 5.07985 Gen 15: 0.487793 Gen 30: 0.182028 Evaluations: 49428</p> 

5	<p>Fitness: (min, max) 142.89707367971545, 4208.73146377518</p> <p>Mean Fitness: Gen 0: 1.11372e+29 Gen 15: 2.09812e+31 Gen 30: 9.97889e+29</p> <p>Median Fitness: Gen 0: 4208.73 Gen 15: 1040.7 Gen 30: 232.326</p> <p>Evaluations: 49552</p> 	<p>Fitness: (min, max) 0.4030478300419816, 5.07984998575548</p> <p>Mean Fitness: Gen 0: 6.75768 Gen 15: 4.83956e+29 Gen 30: 7.12622e+28</p> <p>Median Fitness: Gen 0: 5.07985 Gen 15: 0.5 Gen 30: 0.403048</p> <p>Evaluations: 49072</p> 
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To conclude, by using the correct parameters, such as the optimal combination concluded in this experiment, GP is a very good method of finding an accurate solution (at least an **almost perfect** solution).