## **Case Study #1: Outsourcing Heart Valves**

Hayward Care, a large healthcare organization, outsources a variety of supplies to efficiently maintain its healthcare processes in the organization's hospitals and outpatient services. One of such supplies is heart valves used in heart operations. Different heart surgeries require valves of different sizes – small, medium, and large. Hayward Care outsources valves from five quality suppliers (wholesale distributors). The cost per valve, which does not depend on the valve size, and proportion of valves of various sizes purchased from each supplier are given in the table below:

Suppliers	Cost per valve	Proportion of Small Valves	Proportion of Medium Valves	Proportion of Large Valves
Supplier 1	\$198	0.40	0.30	0.30
Supplier 2	\$210	0.40	0.40	0.20
Supplier 3	\$205	0.20	0.40	0.40
Supplier 4	\$194	0.30	0.50	0.20
Supplier 5	\$200	0.40	0.40	0.20

Each month, Hayward Care places an order with each supplier. At least 400 small, 400 medium, and 500 large valves must be purchased each month. Because of the limited availability of those valves, at most 600 valves per month can be purchased from each supplier. Due to contractual obligations with Suppliers 1 and 2, Hayward Care needs to purchase at least 150 valves from each of them.

Hayward Care is interested to understand how many heart valves need to be acquired from each supplier to minimize the total monthly cost of the organization's valve purchases.

## Questions.

- Develop an LP model formulation that addresses the issue of minimizing the monthly cost of purchasing heart valves. Briefly explain the model's decision variables, objective function, and constraints.
- Based on the LP model formulation, develop a spreadsheet model, and apply Excel Solver to determine the optimal solution of purchasing the needed heart valves. Present and explain your solution.
- 3. Use the Solver Sensitivity Report from this optimal model in question 2 to explain the following:
  - a. if Hayward Care would like to decrease the maximum purchase from Supplier 3 to 480 units (currently, it is 600 units), how would this change the optimal total cost? Present and briefly explain your results.
  - What should be the cost per valve from Supplier 5, to purchase valves from this supplier?
    Present and briefly explain.
- 4. Hayward Care would like to purchase more from Supplier 4, which the lowest costs per valve. For example, they would like to purchase at least 400 valves from Supplier 4. Present a mathematical

formulation of this constraint. Revise the spreadsheet model in question 2 by adding this constraint, identify and present the optimal solution for the revised model. Compare this optimal solution with the optimal solution in question 2 and briefly explain your results.

5. For the revised model in question 4, apply SolverTable to investigate the effect of changing the maximum number of valves purchased from Supplier 2 from 0 to 600 units (with an increment of 20 units) on the minimum total cost and number of purchased units from each supplier. Present and briefly explain your results.