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# Chapter 5

# Syntax-Directed Translation

This chapter develops the theme of Section 2.3: the translation of languages guided by context-free grammars. The translation techniques in this chapter will be applied in Chapter 6 to type checking and intermediate-code generation. The techniques are also useful for implementing little languages for specialized tasks; this chapter includes an example from typesetting.

We associate information with a language construct by attaching attributes to the grammar symbol(s) representing the construct, as discussed in Section 2.3.2. A syntax-directed definition specifies the values of attributes by associating semantic rules with the grammar productions. For example, an infix-to-postfix translator might have a production and rule

PRODUCTION SEMANTIC RULE 
$$E \rightarrow E_1 + T \qquad E.code = E_1.code \parallel T.code \parallel '+'$$
 (5.1)

This production has two nonterminals, E and T; the subscript in  $E_1$  distinguishes the occurrence of E in the production body from the occurrence of E as the head. Both E and T have a string-valued attribute code. The semantic rule specifies that the string E.code is formed by concatenating  $E_1.code$ , T.code, and the character '+'. While the rule makes it explicit that the translation of E is built up from the translations of  $E_1$ , T, and '+', it may be inefficient to implement the translation directly by manipulating strings.

From Section 2.3.5, a syntax-directed translation scheme embeds program fragments called semantic actions within production bodies, as in

$$E \to E_1 + T \quad \{ \text{ print }' + ' \}$$
 (5.2)

By convention, semantic actions are enclosed within curly braces. (If curly braces occur as grammar symbols, we enclose them within single quotes, as in

5.1. SYNTAX-DIRECTED DEFINITIONS

'{' and '}'.) The position of a semantic action in a production body determines the order in which the action is executed. In production (5.2), the action occurs at the end, after all the grammar symbols; in general, semantic actions may occur at any position in a production body.

Between the two notations, syntax-directed definitions can be more readable, and hence more useful for specifications. However, translation schemes can be more efficient, and hence more useful for implementations.

The most general approach to syntax-directed translation is to construct a parse tree or a syntax tree, and then to compute the values of attributes at the nodes of the tree by visiting the nodes of the tree. In many cases, translation can be done during parsing, without building an explicit tree. We shall therefore study a class of syntax-directed translations called "L-attributed translations" (L for left-to-right), which encompass virtually all translations that can be performed during parsing. We also study a smaller class, called "S-attributed translations" (S for synthesized), which can be performed easily in connection with a bottom-up parse.

# 5.1 Syntax-Directed Definitions

A syntax-directed definition (SDD) is a context-free grammar together with attributes and rules. Attributes are associated with grammar symbols and rules are associated with productions. If X is a symbol and a is one of its attributes, then we write X.a to denote the value of a at a particular parse-tree node labeled X. If we implement the nodes of the parse tree by records or objects, then the attributes of X can be implemented by data fields in the records that represent the nodes for X. Attributes may be of any kind: numbers, types, table references, or strings, for instance. The strings may even be long sequences of code, say code in the intermediate language used by a compiler.

## 5.1.1 Inherited and Synthesized Attributes

We shall deal with two kinds of attributes for nonterminals:

- 1. A synthesized attribute for a nonterminal A at a parse-tree node N is defined by a semantic rule associated with the production at N. Note that the production must have A as its head. A synthesized attribute at node N is defined only in terms of attribute values at the children of N and at N itself.
- 2. An inherited attribute for a nonterminal B at a parse-tree node N is defined by a semantic rule associated with the production at the parent of N. Note that the production must have B as a symbol in its body. An inherited attribute at node N is defined only in terms of attribute values at N's parent, N itself, and N's siblings.

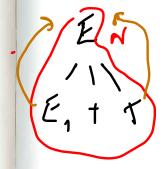
### An Alternative Definition of Inherited Attributes

No additional translations are enabled if we allow an inherited attribute B.c at a node N to be defined in terms of attribute values at the children of N, as well as at N itself, at its parent, and at its siblings. Such rules can be "simulated" by creating additional attributes of B, say  $B.c_1, B.c_2, \ldots$ . These are synthesized attributes that copy the needed attributes of the children of the node labeled B. We then compute B.c as an inherited attribute, using the attributes  $B.c_1, B.c_2, \ldots$  in place of attributes at the children. Such attributes are rarely needed in practice.

While we do not allow an inherited attribute at node N to be defined in terms of attribute values at the children of node N, we do allow a synthesized attribute at node N to be defined in terms of inherited attribute values at node N itself.

Terminals can have synthesized attributes, but not inherited attributes. Attributes for terminals have lexical values that are supplied by the lexical analyzer; there are no semantic rules in the SDD itself for computing the value of an attribute for a terminal.

**Example 5.1:** The SDD in Fig. 5.1 is based on our familiar grammar for arithmetic expressions with operators + and \*. It evaluates expressions terminated by an endmarker **n**. In the SDD, each of the nonterminals has a single synthesized attribute, called *val*. We also suppose that the terminal **digit** has a synthesized attribute *lexval*, which is an integer value returned by the lexical analyzer.



	PRODUCTION	SEMANTIC RULES
1)	L  o En .	L.val = E.val
2)	$E \rightarrow E_1 + T \cdot$	$E.val = E_1.val + T.val$
3)	$E \to T$	E.val = T.val
4)	$T \rightarrow T_1 * F \cdot$	$T.val = T_1.val \times F.val$
5)	T  o F .	T.val = F.val
6)	$F \rightarrow (E)$	F.val = E.val
7)	$F \to \mathbf{digit}$ •	$F.val = \mathbf{digit}.lexval$

Figure 5.1: Syntax-directed definition of a simple desk calculator

The rule for production 1,  $L \to E$  n, sets L.val to E.val, which we shall see is the numerical value of the entire expression.

Production 2,  $E \to E_1 + T$ , also has one rule, which computes the *val* attribute for the head E as the sum of the values at  $E_1$  and T. At any parse-

5.1. SYNTAX-DIRECTED DEFINITIONS

tree node N labeled E, the value of val for E is the sum of the values of val at the children of node N labeled E and T.

Production 3,  $E \to T$ , has a single rule that defines the value of val for E to be the same as the value of val at the child for T. Production 4 is similar to the second production; its rule multiplies the values at the children instead of adding them. The rules for productions 5 and 6 copy values at a child, like that for the third production. Production 7 gives F.val the value of a digit, that is, the numerical value of the token **digit** that the lexical analyzer returned.  $\Box$ 

An SDD that involves only synthesized attributes is called *S-attributed*; the SDD in Fig. 5.1 has this property. In an S-attributed SDD, each rule computes an attribute for the nonterminal at the head of a production from attributes taken from the body of the production.

For simplicity, the examples in this section have semantic rules without side effects. In practice, it is convenient to allow SDD's to have limited side effects, such as printing the result computed by a desk calculator or interacting with a symbol table. Once the order of evaluation of attributes is discussed in Section 5.2, we shall allow semantic rules to compute arbitrary functions, possibly involving side effects.

An S-attributed SDD can be implemented naturally in conjunction with an LR parser. In fact, the SDD in Fig. 5.1 mirrors the Yacc program of Fig. 4.58, which illustrates translation during LR parsing. The difference is that, in the rule for production 1, the Yacc program prints the value E.val as a side effect, instead of defining the attribute L.val.

An SDD without side effects is sometimes called an *attribute grammar*. The rules in an attribute grammar define the value of an attribute purely in terms of the values of other attributes and constants.

## 5.1.2 Evaluating an SDD at the Nodes of a Parse Tree

To visualize the translation specified by an SDD, it helps to work with parse trees, even though a translator need not actually build a parse tree. Imagine therefore that the rules of an SDD are applied by first constructing a parse tree and then using the rules to evaluate all of the attributes at each of the nodes of the parse tree. A parse tree, showing the value(s) of its attribute(s) is called an annotated parse tree.

How do we construct an annotated parse tree? In what order do we evaluate attributes? Before we can evaluate an attribute at a node of a parse tree, we must evaluate all the attributes upon which its value depends. For example, if all attributes are synthesized, as in Example 5.1, then we must evaluate the val attributes at all of the children of a node before we can evaluate the val attribute at the node itself.

With synthesized attributes, we can evaluate attributes in any bottom-up order, such as that of a postorder traversal of the parse tree; the evaluation of S-attributed definitions is discussed in Section 5.2.3.

For SDD's with both inherited and synthesized attributes, there is no guarantee that there is even one order in which to evaluate attributes at nodes. For instance, consider nonterminals A and B, with synthesized and inherited attributes A.s and B.i, respectively, along with the production and rules

PRODUCTION SEMANTIC RULES  $A \rightarrow B$  A.s = B.i; B.i = A.s + 1

These rules are circular; it is impossible to evaluate either A.s at a node N or B.i at the child of N without first evaluating the other. The circular dependency of A.s and B.i at some pair of nodes in a parse tree is suggested by Fig. 5.2.

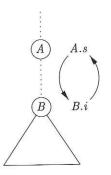


Figure 5.2: The circular dependency of A.s and B.i on one another

It is computationally difficult to determine whether or not there exist any circularities in any of the parse trees that a given SDD could have to translate. Fortunately, there are useful subclasses of SDD's that are sufficient to guarantee that an order of evaluation exists, as we shall see in Section 5.2.

**Example 5.2:** Figure 5.3 shows an annotated parse tree for the input string 3\*5+4 n, constructed using the grammar and rules of Fig. 5.1. The values of *lexval* are presumed supplied by the lexical analyzer. Each of the nodes for the nonterminals has attribute val computed in a bottom-up order, and we see the resulting values associated with each node. For instance, at the node with a child labeled \*, after computing T.val = 3 and F.val = 5 at its first and third children, we apply the rule that says T.val is the product of these two values, or 15.  $\Box$ 

Inherited attributes are useful when the structure of a parse tree does not "match" the abstract syntax of the source code. The next example shows how inherited attributes can be used to overcome such a mismatch due to a grammar designed for parsing rather than translation.

<sup>&</sup>lt;sup>1</sup>Without going into details, while the problem is decidable, it cannot be solved by a polynomial-time algorithm, even if  $\mathcal{P} = \mathcal{NP}$ , since it has exponential time complexity.

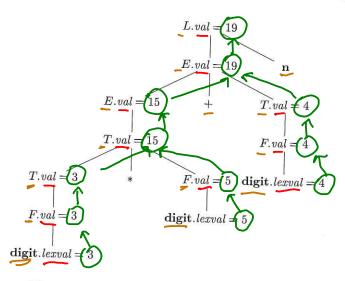


Figure 5.3: Annotated parse tree for 3\*5+4 n

**Example 5.3:** The SDD in Fig. 5.4 computes terms like 3\*5 and 3\*5\*7. The top-down parse of input 3\*5 begins with the production  $T \to FT'$ . Here, F generates the digit 3, but the operator \* is generated by T'. Thus, the left operand 3 appears in a different subtree of the parse tree from \*. An inherited attribute will therefore be used to pass the operand to the operator.

The grammar in this example is an excerpt from a non-left-recursive version of the familiar expression grammar; we used such a grammar as a running example to illustrate top-down parsing in Section 4.4.

PRODUCTION	SEMANTIC RULES
1) $T \rightarrow F T'$	T'.inh = F.val T.val = T'.syn
$2)  T' \to *F T_1'$	$T'_1.inh = T'.inh \times F.val$ $T'.syn = T'_1.syn$
3) $T' \to \epsilon$	T'.syn = T'.inh
4) $F \to \mathbf{digit}$	$F.val = \mathbf{digit}.lexval$

L-ATTAIB

Figure 5.4: An SDD based on a grammar suitable for top-down parsing

Each of the nonterminals T and F has a synthesized attribute val; the terminal **digit** has a synthesized attribute lexval. The nonterminal T' has two attributes: an inherited attribute inh and a synthesized attribute syn.

The semantic rules are based on the idea that the left operand of the operator \* is inherited. More precisely, the head T' of the production  $T' \to *F T'_1$  inherits the left operand of \* in the production body. Given a term x\*y\*z, the root of the subtree for \*y\*z inherits x. Then, the root of the subtree for \*z inherits the value of x\*y, and so on, if there are more factors in the term. Once all the factors have been accumulated, the result is passed back up the tree using synthesized attributes.

To see how the semantic rules are used, consider the annotated parse tree for 3\*5 in Fig. 5.5. The leftmost leaf in the parse tree, labeled **digit**, has attribute value lexval=3, where the 3 is supplied by the lexical analyzer. Its parent is for production 4,  $F \to \mathbf{digit}$ . The only semantic rule associated with this production defines  $F.val = \mathbf{digit}.lexval$ , which equals 3.

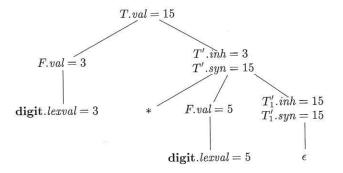


Figure 5.5: Annotated parse tree for 3\*5

At the second child of the root, the inherited attribute T'.inh is defined by the semantic rule T'.inh = F.val associated with production 1. Thus, the left operand, 3, for the \* operator is passed from left to right across the children of the root.

The production at the node for T' is  $T' \to *FT'_1$ . (We retain the subscript 1 in the annotated parse tree to distinguish between the two nodes for T'.) The inherited attribute  $T'_1.inh$  is defined by the semantic rule  $T'_1.inh = T'.inh \times F.val$  associated with production 2.

With T'.inh = 3 and F.val = 5, we get  $T'_1.inh = 15$ . At the lower node for  $T'_1$ , the production is  $T' \to \epsilon$ . The semantic rule T'.syn = T'.inh defines  $T'_1.syn = 15$ . The syn attributes at the nodes for T' pass the value 15 up the tree to the node for T, where T.val = 15.  $\Box$ 

#### 5.1.3 Exercises for Section 5.1

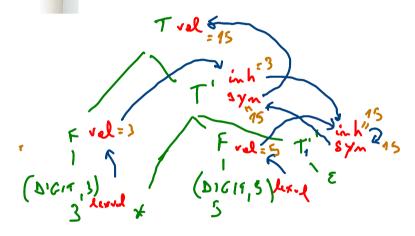
Exercise 5.1.1: For the SDD of Fig. 5.1, give annotated parse trees for the following expressions:

a) 
$$(3+4)*(5+6)$$
 n.

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	PRODUCTION	SEMANTIC RULES	L-ATTAIB
1)	$T \to F T'$	T'.inh = F.val T.val = T'.syn	
2)	$T' \to *FT'_1$	$T'_{1}.inh = T'_{1}.inh \times F_{1}.val$ $T'_{1}.syn = T'_{1}.syn$	
3)	$T' \to \epsilon$	T'.syn = T'.inh	
4)	$F  o \mathbf{digit}$	$F.val = \mathbf{digit}.lexval$	

Figure 5.4: An SDD based on a grammar suitable for top-down parsing



Gli archi in blu sono gli archi del grafo delle dipendenze sugli attributi. L'albero di parsing è in verde. Gli attributi in rosso.



\$ c. 6.1

- b) 1\*2\*3\*(4+5) n.
- c) (9+8\*(7+6)+5)\*4 n.

**Exercise 5.1.2:** Extend the SDD of Fig. 5.4 to handle expressions as in Fig. 5.1.

Exercise 5.1.3: Repeat Exercise 5.1.1, using your SDD from Exercise 5.1.2.

# 5.2 Evaluation Orders for SDD's

"Dependency graphs" are a useful tool for determining an evaluation order for the attribute instances in a given parse tree. While an annotated parse tree shows the values of attributes, a dependency graph helps us determine how those values can be computed.

In this section, in addition to dependency graphs, we define two important classes of SDD's: the "S-attributed" and the more general "L-attributed" SDD's. The translations specified by these two classes fit well with the parsing methods we have studied, and most translations encountered in practice can be written to conform to the requirements of at least one of these classes.

## 5.2.1 Dependency Graphs

A dependency graph depicts the flow of information among the attribute instances in a particular parse tree; an edge from one attribute instance to another means that the value of the first is needed to compute the second. Edges express constraints implied by the semantic rules. In more detail:

- ullet For each parse-tree node, say a node labeled by grammar symbol X, the dependency graph has a node for each attribute associated with X.
- Suppose that a semantic rule associated with a production p defines the value of synthesized attribute A.b in terms of the value of X.c (the rule may define A.b in terms of other attributes in addition to X.c). Then, the dependency graph has an edge from X.c to A.b. More precisely, at every node N labeled A where production p is applied, create an edge to attribute b at N, from the attribute c at the child of N corresponding to this instance of the symbol X in the body of the production.
- Suppose that a semantic rule associated with a production p defines the value of inherited attribute B.c in terms of the value of X.a. Then, the dependency graph has an edge from X.a to B.c. For each node N labeled B that corresponds to an occurrence of this B in the body of production p, create an edge to attribute c at N from the attribute a at the node M

that corresponds to this occurrence of X. Note that M could be either the parent or a sibling of N.

Example 5.4: Consider the following production and rule:

PRODUCTION SEMANTIC RULE  $E \rightarrow E_1 + T$   $E.val = E_1.val + T.val$ 

At every node N labeled E, with children corresponding to the body of this production, the synthesized attribute val at N is computed using the values of val at the two children, labeled E and T. Thus, a portion of the dependency graph for every parse tree in which this production is used looks like Fig. 5.6. As a convention, we shall show the parse tree edges as dotted lines, while the edges of the dependency graph are solid.  $\square$ 

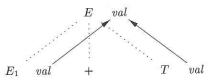


Figure 5.6: E.val is synthesized from  $E_1.val$  and  $E_2.val$ 

Example 5.5: An example of a complete dependency graph appears in Fig. 5.7. The nodes of the dependency graph, represented by the numbers 1 through 9, correspond to the attributes in the annotated parse tree in Fig. 5.5.

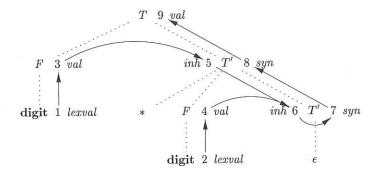


Figure 5.7: Dependency graph for the annotated parse tree of Fig. 5.5

Nodes 1 and 2 represent the attribute lexval associated with the two leaves labeled **digit**. Nodes 3 and 4 represent the attribute val associated with the two nodes labeled F. The edges to node 3 from 1 and to node 4 from 2 result

<sup>&</sup>lt;sup>2</sup>Since a node N can have several children labeled X, we again assume that subscripts distinguish among uses of the same symbol at different places in the production.

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from the semantic rule that defines F.val in terms of  $\mathbf{digit}.lexval$ . In fact, F.val equals  $\mathbf{digit}.lexval$ , but the edge represents dependence, not equality.

Nodes 5 and 6 represent the inherited attribute T'.inh associated with each of the occurrences of nonterminal T'. The edge to 5 from 3 is due to the rule T'.inh = F.val, which defines T'.inh at the right child of the root from F.val at the left child. We see edges to 6 from node 5 for T'.inh and from node 4 for F.val, because these values are multiplied to evaluate the attribute inh at node 6.

Nodes 7 and 8 represent the synthesized attribute syn associated with the occurrences of T'. The edge to node 7 from 6 is due to the semantic rule T'.syn = T'.inh associated with production 3 in Fig. 5.4. The edge to node 8 from 7 is due to a semantic rule associated with production 2.

Finally, node 9 represents the attribute T.val. The edge to 9 from 8 is due to the semantic rule, T.val = T'.syn, associated with production 1.  $\Box$ 

## 5.2.2 Ordering the Evaluation of Attributes

The dependency graph characterizes the possible orders in which we can evaluate the attributes at the various nodes of a parse tree. If the dependency graph has an edge from node M to node N, then the attribute corresponding to M must be evaluated before the attribute of N. Thus, the only allowable orders of evaluation are those sequences of nodes  $N_1, N_2, \ldots, N_k$  such that if there is an edge of the dependency graph from  $N_i$  to  $N_j$ , then i < j. Such an ordering embeds a directed graph into a linear order, and is called a topological sort of the graph.

If there is any cycle in the graph, then there are no topological sorts; that is, there is no way to evaluate the SDD on this parse tree. If there are no cycles, however, then there is always at least one topological sort. To see why, since there are no cycles, we can surely find a node with no edge entering. For if there were no such node, we could proceed from predecessor to predecessor until we came back to some node we had already seen, yielding a cycle. Make this node the first in the topological order, remove it from the dependency graph, and repeat the process on the remaining nodes.

**Example 5.6:** The dependency graph of Fig. 5.7 has no cycles. One topological sort is the order in which the nodes have already been numbered:  $1, 2, \ldots, 9$ . Notice that every edge of the graph goes from a node to a higher-numbered node, so this order is surely a topological sort. There are other topological sorts as well, such as 1, 3, 5, 2, 4, 6, 7, 8, 9.  $\square$ 

## 5.2.3 S-Attributed Definitions

As mentioned earlier, given an SDD, it is very hard to tell whether there exist any parse trees whose dependency graphs have cycles. In practice, translations can be implemented using classes of SDD's that guarantee an evaluation order,

since they do not permit dependency graphs with cycles. Moreover, the two classes introduced in this section can be implemented efficiently in connection with top-down or bottom-up parsing.

The first class is defined as follows:

• An SDD is S-attributed if every attribute is synthesized.

**Example 5.7:** The SDD of Fig. 5.1 is an example of an S-attributed definition. Each attribute, L.val, E.val, T.val, and T.val is synthesized.  $\Box$ 

When an SDD is S-attributed, we can evaluate its attributes in any bottomup order of the nodes of the parse tree. It is often especially simple to evaluate the attributes by performing a postorder traversal of the parse tree and evaluating the attributes at a node N when the traversal leaves N for the last time. That is, we apply the function *postorder*, defined below, to the root of the parse tree (see also the box "Preorder and Postorder Traversals" in Section 2.3.4):

```
\begin{array}{c} postorder(N) \; \{\\ & \textbf{for} \; ( \; \text{each child} \; C \; \text{of} \; N, \; \text{from the left} \; ) \; postorder(C);\\ & \text{evaluate the attributes associated with node} \; N;\\ \} \end{array}
```

S-attributed definitions can be implemented during bottom-up parsing, since a bottom-up parse corresponds to a postorder traversal. Specifically, postorder corresponds exactly to the order in which an LR parser reduces a production body to its head. This fact will be used in Section 5.4.2 to evaluate synthesized attributes and store them on the stack during LR parsing, without creating the tree nodes explicitly.

### 5.2.4 L-Attributed Definitions

The second class of SDD's is called *L-attributed definitions*. The idea behind this class is that, between the attributes associated with a production body, dependency-graph edges can go from left to right, but not from right to left (hence "L-attributed"). More precisely, each attribute must be either

- 1. Synthesized, or
- 2. Inherited, but with the rules limited as follows. Suppose that there is a production  $A \to X_1 X_2 \cdots X_n$ , and that there is an inherited attribute  $X_i.a$  computed by a rule associated with this production. Then the rule may use only:
  - (a) Inherited attributes associated with the head A.
  - (b) Either inherited or synthesized attributes associated with the occurrences of symbols  $X_1, X_2, \ldots, X_{i-1}$  located to the left of  $X_i$ .

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(c) Inherited or synthesized attributes associated with this occurrence of  $X_i$  itself, but only in such a way that there are no cycles in a dependency graph formed by the attributes of this  $X_i$ .

**Example 5.8:** The SDD in Fig. 5.4 is L-attributed. To see why, consider the semantic rules for inherited attributes, which are repeated here for convenience:

 $\begin{array}{ll} \text{Production} & \text{Semantic Rule} \\ T \rightarrow F \ T' & T'.inh = F.val \\ T' \rightarrow * F \ T'_1 & T'_1.inh = T'.inh \times F.val \end{array}$ 

The first of these rules defines the inherited attribute T'.inh using only F.val, and F appears to the left of T' in the production body, as required. The second rule defines  $T'_1.inh$  using the inherited attribute T'.inh associated with the head, and F.val, where F appears to the left of  $T'_1$  in the production body.

In each of these cases, the rules use information "from above or from the left," as required by the class. The remaining attributes are synthesized. Hence, the SDD is L-attributed.  $\Box$ 

**Example 5.9:** Any SDD containing the following production and rules cannot be L-attributed:

PRODUCTION SEMANTIC RULES  $A \rightarrow B \ C$  A.s = B.b; B.i = f(C.c. A.s)

The first rule, A.s = B.b, is a legitimate rule in either an S-attributed or L-attributed SDD. It defines a synthesized attribute A.s in terms of an attribute at a child (that is, a symbol within the production body).

The second rule defines an inherited attribute B.i, so the entire SDD cannot be S-attributed. Further, although the rule is legal, the SDD cannot be L-attributed, because the attribute C.c is used to help define B.i, and C is to the right of B in the production body. While attributes at siblings in a parse tree may be used in L-attributed SDD's, they must be to the left of the symbol whose attribute is being defined.  $\Box$ 

## 5.2.5 Semantic Rules with Controlled Side Effects

In practice, translations involve side effects: a desk calculator might print a result; a code generator might enter the type of an identifier into a symbol table. With SDD's, we strike a balance between attribute grammars and translation schemes. Attribute grammars have no side effects and allow any evaluation order consistent with the dependency graph. Translation schemes impose left-to-right evaluation and allow semantic actions to contain any program fragment; translation schemes are discussed in Section 5.4.

We shall control side effects in SDD's in one of the following ways:

- Permit incidental side effects that do not constrain attribute evaluation. In other words, permit side effects when attribute evaluation based on any topological sort of the dependency graph produces a "correct" translation, where "correct" depends on the application.
- Constrain the allowable evaluation orders, so that the same translation is produced for any allowable order. The constraints can be thought of as implicit edges added to the dependency graph.

As an example of an incidental side effect, let us modify the desk calculator of Example 5.1 to print a result. Instead of the rule L.val = E.val, which saves the result in the synthesized attribute L.val, consider:

PRODUCTION SEMANTIC RULE 1)  $L \to E \mathbf{n}$  print(E.val)

Semantic rules that are executed for their side effects, such as print(E.val), will be treated as the definitions of dummy synthesized attributes associated with the head of the production. The modified SDD produces the same translation under any topological sort, since the print statement is executed at the end, after the result is computed into E.val.

**Example 5.10:** The SDD in Fig. 5.8 takes a simple declaration D consisting of a basic type T followed by a list L of identifiers. T can be **int** or **float**. For each identifier on the list, the type is entered into the symbol-table entry for the identifier. We assume that entering the type for one identifier does not affect the symbol-table entry for any other identifier. Thus, entries can be updated in any order. This SDD does not check whether an identifier is declared more than once; it can be modified to do so.

	PRODUCTION	SEMANTIC RULES
1)	$D \to T \; L$	L.inh = T.type
2)	$T  o \mathbf{int}$	T.type = integer
3)	$T \to \mathbf{float}$	T.type = float
4)	$L \to L_1$ , id	$L_1.inh = L.inh$
		$addType(\mathbf{id}.entry, L.inh)$
5)	$L \to \mathbf{id}$	$addType(\mathbf{id}.entry, L.inh)$

Figure 5.8: Syntax-directed definition for simple type declarations

Nonterminal D represents a declaration, which, from production 1, consists of a type T followed by a list L of identifiers. T has one attribute, T.type, which is the type in the declaration D. Nonterminal L also has one attribute, which we call inh to emphasize that it is an inherited attribute. The purpose of L.inh

is to pass the declared type down the list of identifiers, so that it can be added to the appropriate symbol-table entries.

Productions 2 and 3 each evaluate the synthesized attribute T.type, giving it the appropriate value, integer or float. This type is passed to the attribute L.inh in the rule for production 1. Production 4 passes L.inh down the parse tree. That is, the value  $L_1.inh$  is computed at a parse-tree node by copying the value of L.inh from the parent of that node; the parent corresponds to the head of the production.

Productions 4 and 5 also have a rule in which a function addType is called with two arguments:

- 1. id. entry, a lexical value that points to a symbol-table object, and
- 2. L.inh, the type being assigned to every identifier on the list.

We suppose that function addType properly installs the type L.inh as the type of the represented identifier.

A dependency graph for the input string float  $id_1$ ,  $id_2$ ,  $id_3$  appears in Fig. 5.9. Numbers 1 through 10 represent the nodes of the dependency graph. Nodes 1, 2, and 3 represent the attribute *entry* associated with each of the leaves labeled id. Nodes 6, 8, and 10 are the dummy attributes that represent the application of the function addType to a type and one of these *entry* values.

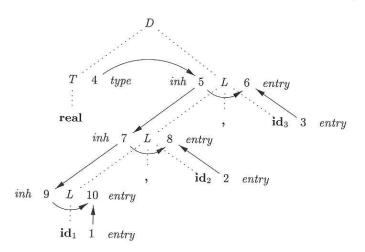


Figure 5.9: Dependency graph for a declaration  $\mathbf{float}\ \mathbf{id}_1\,,\,\mathbf{id}_2\,,\,\mathbf{id}_3$ 

Node 4 represents the attribute T.type, and is actually where attribute evaluation begins. This type is then passed to nodes 5, 7, and 9 representing L.inh associated with each of the occurrences of the nonterminal L.

### 5.2.6 Exercises for Section 5.2

Exercise 5.2.1: What are all the topological sorts for the dependency graph of Fig. 5.7?

Exercise 5.2.2: For the SDD of Fig. 5.8, give annotated parse trees for the following expressions:

- a) int a, b, c.
- b) float w, x, y, z.

Exercise 5.2.3: Suppose that we have a production  $A \to BCD$ . Each of the four nonterminals A, B, C, and D have two attributes: s is a synthesized attribute, and i is an inherited attribute. For each of the sets of rules below, tell whether (i) the rules are consistent with an S-attributed definition (ii) the rules are consistent with an L-attributed definition, and (iii) whether the rules are consistent with any evaluation order at all?

- a) A.s = B.i + C.s.
- b) A.s = B.i + C.s and D.i = A.i + B.s.
- c) A.s = B.s + D.s.
- ! d) A.s = D.i, B.i = A.s + C.s, C.i = B.s, and D.i = B.i + C.i.
- ! Exercise 5.2.4: This grammar generates binary numbers with a "decimal" point:

$$S \rightarrow L . L \mid L$$
  

$$L \rightarrow L B \mid B$$
  

$$B \rightarrow 0 \mid 1$$

Design an L-attributed SDD to compute S.val, the decimal-number value of an input string. For example, the translation of string 101.101 should be the decimal number 5.625. Hint: use an inherited attribute L.side that tells which side of the decimal point a bit is on.

- !! Exercise 5.2.5: Design an S-attributed SDD for the grammar and translation described in Exercise 5.2.4.
- !! Exercise 5.2.6: Implement Algorithm 3.23, which converts a regular expression into a nondeterministic finite automaton, by an L-attributed SDD on a top-down parsable grammar. Assume that there is a token **char** representing any character, and that **char**.lexval is the character it represents. You may also assume the existence of a function new() that returns a new state, that is, a state never before returned by this function. Use any convenient notation to specify the transitions of the NFA.