```
import pandas as pd
import numpy as no
from sklearn.neighbors import NearestNeighbors
# Install PuLP library for optimization
!pip install pulp geopy
→ Collecting pulp
        Downloading PuLP-2.9.0-py3-none-any.whl.metadata (5.4 kB)
      Requirement already satisfied: geopy in /usr/local/lib/python3.10/dist-packages (2.4.1)
      Requirement already satisfied: geographiclib<3,>=1.52 in /usr/local/lib/python3.10/dist-packages (from geopy) (2.0)
      Downloading PuLP-2.9.0-py3-none-any.whl (17.7 MB)
                                                         - 17.7/17.7 MB 103.3 MB/s eta 0:00:00
      Installing collected packages: pulp
      Successfully installed pulp-2.9.0
from google.colab import drive
drive.mount('/content/drive')
→ Mounted at /content/drive
                                                                                    + Text
                                                                       + Code
import pandas as pd
import numpy as np
from geopy.distance import geodesic
from pulp import LpMinimize, LpProblem, LpVariable, lpSum
# Load your dataset (adjust the path if you upload to Google Drive)
file_path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset_new.csv' # Update this path if necessary
#data = pd.read_csv(file_path)
data = pd.read_csv(file_path, encoding='latin-1') # Pass encoding as an argument to pd.read_csv
# Display the first few rows to understand the structure
data.head()
<del>_</del>
     Show hidden output
import pandas as pd
import numpy as np
{\tt from \ sklearn.neighbors \ import \ NearestNeighbors}
from scipy.sparse import lil_matrix, csr_matrix, save_npz
from geopy.distance import geodesic
from pulp import LpMinimize, LpProblem, LpVariable, 1pSum
# Load your dataset (adjust the path if you upload to Google Drive)
file_path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset_new.csv' # Update this path if necessary
data = pd.read_csv(file_path, encoding='latin-1') # Load with specified encoding
\ensuremath{\text{\#}}\xspace Display the first few rows to understand the structure
print("Dataset preview:")
print(data.head())
# Extract unique store locations with 'Order City', 'Latitude', and 'Longitude' and create a unique identifier store_locations = data[['Order City', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True)
store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
# Convert Latitude and Longitude to radians for haversine calculations
coordinates = np.radians(list(zip(store_locations['Latitude'], store_locations['Longitude'])))
# Parameters for processing in larger chunks given high RAM
chunk size = 25000 # Larger chunk size for High RAM setup
n neighbors = 100 # Number of nearest neighbors
# Initialize a sparse matrix for all distances
num stores = len(store_locations)
distance_matrix_sparse = lil_matrix((num_stores, num_stores))
# Process in chunks
for start in range(0, num_stores, chunk_size):
    end = min(start + chunk size, num stores)
    chunk_coordinates = coordinates[start:end]
    # Compute nearest neighbors within the chunk
    \verb|nbrs| = NearestNeighbors(n_neighbors=n_neighbors, algorithm='ball_tree', metric='haversine').fit(chunk\_coordinates)|
    distances, indices = nbrs.kneighbors(chunk_coordinates)
    distances = distances * 6371 \# Convert from radians to kilometers
    # Fill the sparse matrix with calculated distances
    for i, row_index in enumerate(range(start, end)):
        distance_matrix_sparse[row_index, indices[i] + start] = distances[i]
    print(f"Processed chunk {start} to {end}")
# Convert the sparse matrix to CSR format before saving
distance_matrix_sparse_csr = distance_matrix_sparse.tocsr()
```

```
# Save the CSR sparse matrix to disk
save_npz('/content/distance_matrix_sparse.npz', distance_matrix_sparse_csr)
print("Sparse distance matrix saved successfully.")
→ Dataset preview:
            Type Days for shipping (real) Days for shipment (scheduled)
         PAYMENT
         PAYMENT
                                                                           4
                                          5
       TRANSFER
     2
                                          6
                                                                           2
           DEBIT
     3
                                          2
                                                                           4
                                                                           4
     4
           DEBIT
         Delivery Status Product Sales Late_delivery_risk
                                                                  Category Name \
     0
           Late delivery
                             314.640015
                                                               Kids' Golf Clubs
                                                            1
                              311.359985
                                                                Women's Apparel
           Late delivery
           Late delivery
                              309.720001
                                                                Women's Apparel
       Advance shipping
                             304.809998
                                                                         Cleats
       Advance shipping
                           298.250000
                                                                         Cleats
                                                            0
       New Category Name Customer Id
                                          Customer City ... ∖
                            20755 South Ozone Park ...
     a
           Kids & Toys
                                 19492 South Ozone Park ...
     1
         Women's Apparel
     2
         Women's Apparel
                                 19491
                                                   Caguas ...
     3
        Sports Equipment
                                 19490
                                                   Caguas ...
     4
        Sports Equipment
                                 19489
                                                   Caguas ...
       Order Profit Per Order
                                                                      Order State \
                                   Order Region
                  -598.390015 Southern Europe
                                                                         Cataluña
                   -57.529999 Southern Europe
                                                                          Cataluña
     1
                    42.000000
                               Western Europe
     2
                                                                          Amberes
                    89.629997
                                 Western Europe Alsacia-Champaña-Ardenas-Lorena
     3
                    29.700001 Western Europe Alsacia-Champaña-Ardenas-Lorena
     4
           Order Status Product Card Id Product Category Id \
     0
        PENDING_PAYMENT
                                    303
     1
        PENDING_PAYMENT
                                      502
                                                             24
                PENDING
                                                             24
     3
                ON_HOLD
                                      365
                                                             17
     4
                ON HOLD
                                      365
                                                             17
                                 Product Name Product Price \
           Garmin Forerunner 910XT GPS Watch
     0
                                                   399,989990
        Nike Men's Dri-FIT Victory Golf Polo
                                                    50 000000
     1
        Nike Men's Dri-FIT Victory Golf Polo
     2
                                                    50.000000
     3
            Perfect Fitness Perfect Rip Deck
                                                    59.990002
     4
            Perfect Fitness Perfect Rip Deck
                                                    59.990002
        shipping date (DateOrders) Shipping Mode
                    9/30/2017 9:06 Standard Class
     0
                    9/30/2017 9:06 Standard Class
     1
                    9/30/2017 8:56
                                      Second Class
     2
                    9/30/2017 7:53 Standard Class
     3
                    9/30/2017 7:53 Standard Class
     4
     [5 rows x 41 columns]
     Processed chunk 0 to 25000
     Processed chunk 25000 to 50000
     Processed chunk 50000 to 64848
     Sparse distance matrix saved successfully.
from scipy.sparse import load_npz
# Load the sparse distance matrix
distance_matrix_sparse = load_npz('/content/distance_matrix_sparse.npz')
from pulp import LpMinimize, LpProblem, LpVariable, lpSum
# Ensure store_locations index is aligned BEFORE creating distance_matrix_sparse:
store_locations = store_locations.reset_index(drop=True)
\# ... (rest of your code to create distance_matrix_sparse) ...
# Group the locations by 'Order Region' to create clusters
regions = store_locations.groupby('Order Region')
# Dictionary to store optimized routes for each region
optimized_routes = {}
# Process each region independently
for region, group in regions:
   print(f"Processing region: {region}")
   # Get the indices of locations within this region
   region_indices = group.index.tolist()
```

num_locations_region = len(region_indices)

```
# Filter region indices to be within the bounds of distance matrix sparse
   valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
   # Extract a localized distance submatrix for the region using valid indices
   local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices]
   # ... (rest of your optimization logic using valid_region_indices) ...
# Display optimized routes for each region
optimized_routes
→ Processing region: Canada
     Processing region: Caribbean
     Processing region: Central Africa
     Processing region: Central America
     Processing region: Central Asia
     Processing region: East Africa
     Processing region: East of USA
     Processing region: Eastern Asia
     Processing region: Eastern Europe
     Processing region: North Africa
     Processing region: Northern Europe
     Processing region: Oceania
     Processing region: South America
     Processing region: South Asia
     Processing region: South of USA
     Processing region: Southeast Asia
     Processing region: Southern Africa
     Processing region: Southern Europe
     Processing region: US Center
     Processing region: West Africa
     Processing region: West Asia
     Processing region: West of USA
     Processing region: Western Europe
     {}
from pulp import LpMinimize, LpProblem, LpVariable, lpSum
# Ensure store_locations index is aligned BEFORE creating distance_matrix_sparse:
store_locations = store_locations.reset_index(drop=True)
# ... (rest of your code to create distance matrix sparse) ...
# Group the locations by 'Order Region' to create clusters
regions = store locations.groupby('Order Region')
# Dictionary to store optimized routes for each region
optimized_routes = {}
# Process each region independently
for region, group in regions:
   print(f"Processing region: {region}")
   # Get the indices of locations within this region
   region_indices = group.index.tolist()
   num_locations_region = len(region_indices)
   \# Filter region_indices to be within the bounds of distance_matrix_sparse
   valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
   # Extract a localized distance submatrix for the region using valid indices
   local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices]
   \#\ldots (your optimization logic using valid_region_indices) \ldots
   # Extract the optimized route for the region and map back to the original indices
   region_route = [(valid_region_indices[i], valid_region_indices[j])
                   for i in range(len(valid_region_indices))
                   for j in range(len(valid_region_indices))
                   if i != j and x[(i, j)].value() == 1]
   optimized_routes[region] = region_route
   print(f"Completed optimization for region: {region}")
# Display optimized routes for each region
optimized_routes
```

```
→ Processing region: Canada
      Completed optimization for region: Canada
     Processing region: Caribbean
                                                     Traceback (most recent call last)
     <ipython-input-8-460a16c69c76> in <cell line: 15>()
           29
           30
                   # Extract the optimized route for the region and map back to the original indices
      ---> 31
                   region_route = [(valid_region_indices[i], valid_region_indices[j])
           32
                                      for i in range(len(valid_region_indices))
           33
                                      for j in range(len(valid_region_indices))
      <ipython-input-8-460a16c69c76> in <listcomp>(.0)
                                     for i in range(len(valid_region_indices))
           32
                                      for j in range(len(valid_region_indices))
           33
      ---> 34
                                     if i != j and x[(i, j)].value() == 1]
           35
                   optimized_routes[region] = region_route
           36
     KeyError: (0, 309)
!pip install pulp
!pip install geopy
!pip install scikit-learn
!pip install pandas
!pip install numpy
!pip install scipy
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import lil_matrix, csr_matrix, save_npz, load_npz
from geopy.distance import geodesic
from pulp import LpMinimize, LpProblem, LpVariable, 1pSum
# Load your dataset
file_path = 'DataCoSupplyChainDataset_new.csv' # Update with your actual path
data = pd.read_csv(file_path, encoding='latin-1')
# Extract unique store locations and create a unique identifier
store_locations = data[['Order City', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True)
store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
# Convert Latitude and Longitude to radians
coordinates = np.radians(list(zip(store_locations['Latitude'], store_locations['Longitude'])))
# Parameters for processing
chunk size = 25000
n_neighbors = 100
# Initialize a sparse matrix for distances
num_stores = len(store_locations)
distance_matrix_sparse = lil_matrix((num_stores, num_stores))
# Calculate distances in chunks
for start in range(0, num_stores, chunk_size):
    end = min(start + chunk_size, num_stores)
    chunk_coordinates = coordinates[start:end]
    \verb|nbrs| = NearestNeighbors(n_neighbors=n_neighbors, algorithm='ball_tree', metric='haversine').fit(chunk\_coordinates)|
    distances, indices = nbrs.kneighbors(chunk_coordinates)
    distances = distances * 6371 # Convert to kilometers
    for i, row_index in enumerate(range(start, end)):
       distance_matrix_sparse[row_index, indices[i] + start] = distances[i]
    print(f"Processed chunk {start} to {end}")
# Convert and save the sparse matrix
distance_matrix_sparse_csr = distance_matrix_sparse.tocsr()
save npz('distance matrix sparse.npz', distance matrix sparse csr)
print("Sparse distance matrix saved successfully.")
# Load the sparse distance matrix
distance matrix sparse = load npz('distance matrix sparse.npz')
\ensuremath{\text{\#}} Group locations by region and optimize routes
regions = store_locations.groupby('Order Region')
optimized_routes = {}
for region, group in regions:
    print(f"Processing region: {region}")
    region_indices = group.index.tolist()
    num_locations_region = len(region_indices)
    \# Ensure indices are within the bounds of the distance matrix
    valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
    # If valid indices are empty, skip the region
    if not valid_region_indices:
       print(f"Skipping region \{region\}\ due to empty valid indices.")
        continue
```

```
# Extract a submatrix for the region
    local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
    model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
    x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
   model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
```python
!pip install pulp
!pip install geopy
!pip install scikit-learn
!pip install pandas
!pip install numpy
!pip install scipy
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import lil_matrix, csr_matrix, save_npz, load_npz
from geopy.distance import geodesic
from pulp import LpMinimize, LpProblem, LpVariable, lpSum
Load your dataset
file path = 'DataCoSupplyChainDataset new.csv' # Update with your actual path
data = pd.read csv(file path, encoding='latin-1')
Extract unique store locations and create a unique identifier
store_locations = data[['Order\ City',\ 'Latitude',\ 'Longitude']]. drop_duplicates().reset_index(drop=True)
store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
Convert Latitude and Longitude to radians
coordinates = np.radians(list(zip(store_locations['Latitude'], store_locations['Longitude'])))
Parameters for processing
chunk size = 25000
n_neighbors = 100
Initialize a sparse matrix for distances
num_stores = len(store_locations)
distance_matrix_sparse = lil_matrix((num_stores, num_stores))
Calculate distances in chunks
for start in range(0, num_stores, chunk_size):
 end = min(start + chunk_size, num_stores)
 chunk coordinates = coordinates[start:end]
 \verb|nbrs| = \verb|NearestNeighbors| (\verb|n_neighbors| = \verb|n_neighbors|).fit (\verb|chunk_coordinates|) \\
 distances, indices = nbrs.kneighbors(chunk_coordinates)
 distances = distances * 6371 # Convert to kilometers
 for i, row_index in enumerate(range(start, end)):
 distance_matrix_sparse[row_index, indices[i] + start] = distances[i]
 print(f"Processed chunk {start} to {end}")
Convert and save the sparse matrix
distance_matrix_sparse_csr = distance_matrix_sparse.tocsr()
save npz('distance matrix sparse.npz', distance matrix sparse csr)
print("Sparse distance matrix saved successfully.")
Load the sparse distance matrix
distance matrix sparse = load npz('distance matrix sparse.npz')
Group locations by region and optimize routes
regions = store locations.groupby('Order Region')
optimized routes = {}
for region, group in regions:
 print(f"Processing region: {region}")
 region_indices = group.index.tolist()
 num_locations_region = len(region_indices)
 \# Ensure indices are within the bounds of the distance matrix
 valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
 # If valid indices are empty, skip the region
 if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue
 # Extract a submatrix for the region
 local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function
 model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
 # Constraints
 for i in range(len(valid region indices)):
```

```
model += lpSum(x[(i, j)] \ for \ j \ in \ range(len(valid_region_indices)) \ if \ i \ != \ j) \ == \ 1
 model += lpSum(x[(j, i)] for j in range(len(valid_region_indices)) if i != j) == 1
 # Solve the model
!pip install scikit-learn
!pip install pandas
!pip install numpy
!pip install scipy
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import lil_matrix, csr_matrix, save_npz, load_npz \,
from geopy.distance import geodesic
from pulp import LpMinimize, LpProblem, LpVariable, lpSum
Load your dataset
file_path = 'DataCoSupplyChainDataset_new.csv' # Update with your actual path
data = pd.read_csv(file_path, encoding='latin-1')
Extract unique store locations and create a unique identifier
store_locations = data[['Order City', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True)
store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
Convert Latitude and Longitude to radians
coordinates = np.radians(list(zip(store_locations['Latitude'], store_locations['Longitude'])))
Parameters for processing
chunk size = 25000
n_neighbors = 100
Initialize a sparse matrix for distances
num stores = len(store locations)
distance_matrix_sparse = lil_matrix((num_stores, num_stores))
Calculate distances in chunks
for start in range(0, num_stores, chunk_size):
 end = min(start + chunk size, num stores)
 chunk_coordinates = coordinates[start:end]
 \verb|nbrs| = NearestNeighbors(n_neighbors=n_neighbors, algorithm='ball_tree', metric='haversine').fit(chunk_coordinates)|
 distances, indices = nbrs.kneighbors(chunk_coordinates)
 distances = distances * 6371 # Convert to kilometers
 for i, row_index in enumerate(range(start, end)):
 distance_matrix_sparse[row_index, indices[i] + start] = distances[i]
 print(f"Processed chunk {start} to {end}")
Convert and save the sparse matrix
distance_matrix_sparse_csr = distance_matrix_sparse.tocsr()
save_npz('distance_matrix_sparse.npz', distance_matrix_sparse_csr)
print("Sparse distance matrix saved successfully.")
Load the sparse distance matrix
distance_matrix_sparse = load_npz('distance_matrix_sparse.npz')
Group locations by region and optimize routes
regions = store_locations.groupby('Order Region')
optimized routes = {}
for region, group in regions:
 print(f"Processing region: {region}")
 region indices = group.index.tolist()
 num_locations_region = len(region_indices)
 # Ensure indices are within the bounds of the distance matrix
 valid region indices = [i for i in region indices if i < distance matrix sparse.shape[0]]</pre>
 # If valid indices are empty, skip the region
 if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue
 # Extract a submatrix for the region
 local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 # Optimization model
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function
 model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
 # Constraints
 for i in range(len(valid_region_indices)):
 model += lpSum(x[(i, j)] for j in range(len(valid_region_indices)) if i != j) == 1
 model += lpSum(x[(j, i)] for j in range(len(valid_region_indices)) if i != j) == 1
 # Solve the model
```

```
File "<ipython-input-11-b1851cf49b0a>", line 81
 `python
 SyntaxError: invalid syntax
import pickle
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import save npz, load npz
from pulp import LpMinimize, LpProblem, LpVariable, lpSum, PULP_CBC_CMD
import time
Load your dataset and distance matrix
file path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset new.csv'
data = pd.read_csv(file_path, encoding='latin-1')
Extract unique store locations with 'Order City', 'Order Region', 'Latitude', and 'Longitude' and create a unique identifier
store_locations = data[['Order City', 'Order Region', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True)
store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
\ensuremath{\text{\#}} Convert and save the sparse distance matrix
distance_matrix_sparse_csr = distance_matrix_sparse.tocsr()
save_npz('/content/drive/MyDrive/distance_matrix_sparse.npz', distance_matrix_sparse_csr)
print("Sparse distance matrix saved successfully.")
Load the sparse distance matrix
distance_matrix_sparse = load_npz('/content/drive/MyDrive/distance_matrix_sparse.npz')
Group locations by region
regions = store_locations.groupby('Order Region')
Load previous progress if available
try:
 with open('/content/drive/MyDrive/optimized_routes.pkl', 'rb') as f:
 optimized routes = pickle.load(f)
 print("Loaded previously saved routes.")
except FileNotFoundError:
 print("No previously saved routes found. Starting fresh.")
 optimized routes = {}
Set a time limit for each region's optimization in seconds (e.g., 300 seconds = 5 minutes)
time limit = 300
for region, group in regions:
 # Skip already processed regions
 if region in optimized routes:
 print(f"Region {region} already completed, skipping.")
 continue
 print(f"Starting optimization for region: {region}")
 start time = time.time()
 # Get indices of locations within this region
 region_indices = group.index.tolist()
 valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
 # Skip empty or invalid regions
 if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue
 # Extract a local distance matrix for the region
 local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 # Initialize the optimization model for the region
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function: minimize total travel distance using the local distance matrix
 model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
 # Constraints: each location has exactly one inbound and one outbound route
 for i in range(len(valid_region_indices)):
 model += lpSum(x[(i, j)] \ for \ j \ in \ range(len(valid_region_indices)) \ if \ i \ != \ j) \ == \ 1
 model += lpSum(x[(j, i)] \ for \ j \ in \ range(len(valid_region_indices)) \ if \ i \ != \ j) \ == \ 1
 # Solve with a time limit
 model.solve(PULP CBC CMD(timeLimit=time limit))
 # Check if the model was solved within the time limit
 if model.status != 1: # Status 1 indicates an optimal solution was found
 print(f"Region {region} timed out without an optimal solution.")
 continue
 # Extract the optimized route for the region and map back to the original indices
 region_route = [(valid_region_indices[i], valid_region_indices[j]) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if
 optimized_routes[region] = region_route
```

```
Save progress after each region
 with open('/content/drive/MyDrive/optimized_routes.pkl', 'wb') as f:
 pickle.dump(optimized routes, f)
 print(f"Completed optimization for region: \{region\} in \{time.time() - start_time:.2f\} seconds. Progress saved.") \\
print("All regions processed.")
 ⇒ Sparse distance matrix saved successfully.
 No previously saved routes found. Starting fresh.
 Starting optimization for region: Canada
 Completed optimization for region: Canada in 8.99 seconds. Progress saved.
 Starting optimization for region: Caribbean
 KeyboardInterrupt
 Traceback (most recent call last)
 <ipython-input-16-2aa695e35fde> in <cell line: 40>()
 72
 73
 # Solve with a time limit
 model.solve(PULP_CBC_CMD(timeLimit=time_limit))
 ---> 74
 75
 76
 # Check if the model was solved within the time limit
 − 💲 5 frames
 /usr/lib/python3.10/subprocess.py in _try_wait(self, wait_flags)
 1915
 """All callers to this function MUST hold self._waitpid_lock."""
 1916
 -> 1917
 (pid, sts) = os.waitpid(self.pid, wait_flags)
 1918
 except ChildProcessError:
 1919
 # This happens if SIGCLD is set to be ignored or waiting
 KeyboardInterrupt:
Set a reduced time limit for each region's optimization in seconds (e.g., 240 seconds = 4 minutes)
time limit = 240
for region, group in regions:
 # Skip already processed regions and Caribbean
 if region in optimized_routes:
 print(f"Region {region} already completed, skipping.")
 continue
 if region == "Caribbean":
 print("Skipping region: Caribbean due to long runtime.")
 continue
 print(f"Starting optimization for region: {region}")
 start time = time.time()
 # Get indices of locations within this region
 region_indices = group.index.tolist()
 valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
 # Skip empty or invalid regions
 if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue
 # Extract a local distance matrix for the region
 local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 # Initialize the optimization model for the region
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function: minimize total travel distance using the local distance matrix
 model \; += \; lpSum(local_distance_matrix[i][j] \; * \; x[(i,\; j)] \; for \; i \; in \; range(len(valid_region_indices)) \; for \; j \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j \; in \; range(len(valid_region_indices)) \; if \; i \; != \; j) \; in \; range(len(valid_region_ind
 # Constraints: each location has exactly one inbound and one outbound route
 for i in range(len(valid_region_indices)):
 model += lpSum(x[(i, j)] \ for \ j \ in \ range(len(valid_region_indices)) \ if \ i \ != \ j) == 1
 model += lpSum(x[(j, i)] for j in range(len(valid_region_indices)) if i != j) == 1
 # Solve with the GLPK solver and set the time limit
 model.solve(GLPK(timeLimit=time_limit))
 # Check if the model was solved within the time limit
 if model.status != 1: # Status 1 indicates an optimal solution was found
 print(f"Region {region} timed out without an optimal solution.")
 continue
 # Extract the optimized route for the region and map back to the original indices
 region_route = [(valid_region_indices[i], valid_region_indices[j]) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if
 optimized_routes[region] = region_route
 # Save progress after each region
 with open('/content/drive/MyDrive/optimized_routes.pkl', 'wb') as f:
 pickle.dump(optimized_routes, f)
 print(f"Completed optimization for region: {region} in {time.time() - start_time:.2f} seconds. Progress saved.")
```

```
print("All regions processed.")
Region Canada already completed, skipping.
 Skipping region: Caribbean due to long runtime.
 Starting optimization for region: Central Africa
 /usr/local/lib/python3.10/dist-packages/pulp/pulp.py:1298: UserWarning: Spaces are not permitted in the name. Converted to ' '
 warnings.warn("Spaces are not permitted in the name. Converted to '_
 Completed optimization for region: Central Africa in 36.10 seconds. Progress saved.
 Starting optimization for region: Central America
 ._____
 KeyboardInterrupt
 Traceback (most recent call last)
 <ipython-input-18-23e88d738003> in <cell line: 4>()
 \ensuremath{\text{\#}} Initialize the optimization model for the region
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 29
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in
 ---> 30
 range(len(valid_region_indices)) if i != j], cat='Binary')
 31
 # Objective function: minimize total travel distance using the local distance matrix
 32
 /usr/local/lib/python3.10/dist-packages/pulp/pulp.py in dicts(cls, name, indices, lowBound, upBound, cat, indexStart)
 375
 if len(indices) == 0:
 376
 for i in index:
 --> 377
 d[i] = LpVariable(
 378
 name % tuple(indexStart + [str(i)]), lowBound, upBound, cat
 379
 KeyboardInterrupt:
import pickle
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import load npz
from pulp import LpMinimize, LpProblem, LpVariable, lpSum, GLPK
import time
Load your dataset and distance matrix
file_path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset_new.csv'
data = pd.read_csv(file_path, encoding='latin-1')
Extract unique store locations with 'Order City', 'Order Region', 'Latitude', and 'Longitude' and create a unique identifier store_locations = data[['Order City', 'Order Region', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True) store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
\# Load the saved sparse distance matrix
distance_matrix_sparse = load_npz('/content/drive/MyDrive/distance_matrix_sparse.npz')
Group locations by region
regions = store_locations.groupby('Order Region')
Load previous progress if available
try:
 with open('/content/drive/MyDrive/optimized_routes.pkl', 'rb') as f:
 optimized_routes = pickle.load(f)
 print("Loaded previously saved routes.")
except FileNotFoundError:
 print("No previously saved routes found. Starting fresh.")
 optimized routes = {}
Set a reduced time limit for each region's optimization in seconds (e.g., 240 seconds = 4 minutes)
time limit = 240
sample size = 500 # Define the sample size for larger regions
for region, group in regions:
 # Skip already processed regions
 if region in optimized routes:
 print(f"Region {region} already completed, skipping.")
 continue
 print(f"Starting optimization for region: {region}")
 start_time = time.time()
 # Sample if region has more than the sample size
 if len(group) > sample_size:
 sampled_group = group.sample(n=sample_size, random_state=1)
 print(f"Sampling {sample_size} locations for region {region} out of {len(group)} total.")
 else:
```

```
Sample if region has more than the sample size
if len(group) > sample_size:
 sampled_group = group.sample(n=sample_size, random_state=1)
 print(f"Sampling {sample_size} locations for region {region} out of {len(group)} total.")
else:
 sampled_group = group

Get indices of locations within this sampled region
 region_indices = sampled_group.index.tolist()
 valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]

Skip empty or invalid regions
if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue

Extract a local distance matrix for the sampled region</pre>
```

```
local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 # Initialize the optimization model for the region
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function: minimize total travel distance using the local distance matrix
 model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
 # Constraints: each location has exactly one inbound and one outbound route
 for i in range(len(valid_region_indices)):
 \label{eq:model} model += lpSum(x[(i, j)] for j in range(len(valid_region_indices)) if i != j) == 1
 model += lpSum(x[(j, i)] \ for \ j \ in \ range(len(valid_region_indices)) \ if \ i \ != \ j) \ == \ 1
 # Solve with the GLPK solver and set the time limit
 model.solve(GLPK(timeLimit=time limit))
 # Check if the model was solved within the time limit
 if model.status != 1: # Status 1 indicates an optimal solution was found
 print(f"Region {region} timed out without an optimal solution.")
 # Extract the optimized route for the region and map back to the original indices
 region_route = [(valid_region_indices[i], valid_region_indices[j]) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if
 optimized routes[region] = region route
 # Save progress after each region
 with open('/content/drive/MvDrive/optimized routes.pkl', 'wb') as f:
 pickle.dump(optimized routes, f)
 print(f"Completed optimization for region: {region} in {time.time() - start time:.2f} seconds. Progress saved.")
print("All regions processed.")

 → Loaded previously saved routes.

 Region Canada already completed, skipping.
 Region Caribbean already completed, skipping.
 Region Central Africa already completed, skipping.
 Region Central America already completed, skipping.
 Region Central Asia already completed, skipping.
 Region East Africa already completed, skipping.
 Region East of USA already completed, skipping.
 Region Eastern Asia already completed, skipping.
 Region Eastern Europe already completed, skipping.
 Region North Africa already completed, skipping.
 Region Northern Europe already completed, skipping.
 Region Oceania already completed, skipping.
 Region South America already completed, skipping.
 Region South Asia already completed, skipping.
 Region South of USA already completed, skipping.
 Region Southeast Asia already completed, skipping.
 Region Southern Africa already completed, skipping.
 Region Southern Europe already completed, skipping.
 Region US Center already completed, skipping.
 Region West Africa already completed, skipping.
 Region West Asia already completed, skipping.
 Region West of USA already completed, skipping.
 Region Western Europe already completed, skipping.
 All regions processed.
import pickle
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import load npz
from pulp import LpMinimize, LpProblem, LpVariable, lpSum, GLPK
import time
Load your dataset and distance matrix
file_path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset_new.csv'
data = pd.read_csv(file_path, encoding='latin-1')
Extract unique store locations with 'Order City', 'Order Region', 'Latitude', and 'Longitude' and create a unique identifier
store_locations = data[['Order City', 'Order Region', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True)
store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
Load the saved sparse distance matrix
distance_matrix_sparse = load_npz('/content/drive/MyDrive/distance_matrix_sparse.npz')
Group locations by region
regions = store_locations.groupby('Order Region')
Load previous progress if available
try:
 with open('/content/drive/MyDrive/optimized routes.pkl', 'rb') as f:
 optimized_routes = pickle.load(f)
 print("Loaded previously saved routes.")
except FileNotFoundError:
 print("No previously saved routes found. Starting fresh.")
 optimized_routes = {}
```

```
Set a reduced time limit for each region's optimization in seconds (e.g., 240 seconds = 4 minutes)
time limit = 240
for region, group in regions:
 # Skip already processed regions
 if region in optimized routes:
 print(f"Region {region} already completed, skipping.")
 print(f"Starting optimization for region: {region}")
 start_time = time.time()
 # Adaptive sampling based on the region's size
 num_locations = len(group)
 if num_locations <= 500:
 sample_size = 200
 elif num_locations <= 2000:
 sample_size = 500
 elif num_locations <= 5000:
 sample_size = 2000
 else:
 sample_size = 4000 # Large regions get larger samples
 # Sample locations based on the determined sample size
 if num_locations > sample_size:
 sampled_group = group.sample(n=sample size, random state=1)
 print(f"Sampling \{sample_size\}\ locations\ for\ region\ \{region\}\ out\ of\ \{num_locations\}\ total.")
 else:
 sampled group = group
 # Get indices of locations within this sampled region
 region_indices = sampled_group.index.tolist()
 valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
 # Skip empty or invalid regions
 if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue
 # Extract a local distance matrix for the sampled region
 local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 # Initialize the optimization model for the region
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function: minimize total travel distance using the local distance matrix
 model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
 # Constraints: each location has exactly one inbound and one outbound route
 for i in range(len(valid_region_indices)):
 model += lpSum(x[(i, j)] for j in range(len(valid_region_indices)) if i != j) == 1
 model += lpSum(x[(j, i)] for j in range(len(valid_region_indices)) if i != j) == 1
 # Solve with the GLPK solver and set the time limit
 model.solve(GLPK(timeLimit=time_limit))
 # Check if the model was solved within the time limit
 if model.status != 1: # Status 1 indicates an optimal solution was found
 \verb|print(f"Region {region}| timed out without an optimal solution.")|\\
 continue
 # Extract the optimized route for the region and map back to the original indices
 region_route = [(valid_region_indices[i], \ valid_region_indices[j]) \ for \ i \ in \ range(len(valid_region_indices)) \ for \ j \ in \ range(len(valid_region_indices)) \ if \ range(len(valid_region_indices)) \ for \ j \ in \ range(len(valid_re
 optimized_routes[region] = region_route
 # Save progress after each region
 with open('/content/drive/MyDrive/optimized routes.pkl', 'wb') as f:
 pickle.dump(optimized_routes, f)
 print(f"Completed optimization for region: {region} in {time.time() - start_time:.2f} seconds. Progress saved.")
print("All regions processed.")

 → Loaded previously saved routes.

 Region Canada already completed, skipping.
 Region Caribbean already completed, skipping.
 Region Central Africa already completed, skipping.
 Region Central America already completed, skipping.
 Region Central Asia already completed, skipping.
 Region East Africa already completed, skipping.
 Region East of USA already completed, skipping.
 Region Eastern Asia already completed, skipping.
 Region Eastern Europe already completed, skipping.
 Region North Africa already completed, skipping.
 Region Northern Europe already completed, skipping.
 Region Oceania already completed, skipping.
 Region South America already completed, skipping.
 Region South Asia already completed, skipping.
 Region South of USA already completed, skipping.
```

```
Region Southeast Asia already completed, skipping.
 Region Southern Africa already completed, skipping.
 Region Southern Europe already completed, skipping.
 Region US Center already completed, skipping.
 Region West Africa already completed, skipping.
 Region West Asia already completed, skipping.
 Region West of USA already completed, skipping.
 Region Western Europe already completed, skipping.
 All regions processed.
import pickle
Load the optimized routes from the saved file
with open('/content/drive/MyDrive/optimized_routes.pkl', 'rb') as f:
 optimized routes = pickle.load(f)
Combine routes from each region into a single list or DataFrame
final routes = []
for region, route in optimized routes.items():
 for start, end in route:
 final routes.append({
 'Region': region,
 'Start Location': start.
 'End Location': end
 })
\ensuremath{\text{\#}} Convert to DataFrame for easier manipulation
import pandas as pd
final_routes_df = pd.DataFrame(final_routes)
\ensuremath{\text{\#}} Display the combined routes for verification
print("Combined Final Routes Across Regions:")
print(final_routes_df.head())

→ Combined Final Routes Across Regions:
 Region Start_Location End_Location
 0 Canada
 207
 29462
 227
 3484
 1 Canada
 2 Canada
 372
 51240
 50543
 3 Canada
 375
 45490
 4 Canada
 401
Assuming `region_centroids` is a dictionary mapping each region to a central location (hub)
region_centroids = \{region: group['Unique_ID'].iloc[0] \ for \ region, group \ in \ regions\} \\ \ \# \ Simplified \ for \ example \ for \ e
Define a new optimization problem to connect these hubs
from pulp import LpMinimize, LpProblem, LpVariable, 1pSum
Initialize inter-regional optimization
model = LpProblem("Inter_Regional_Optimization", LpMinimize)
Define binary decision variables for connections between regional hubs
x = LpVariable.dicts("Connection", [(i, j) for i in region_centroids for j in region_centroids if i != j], cat='Binary')
Placeholder for distances between hubs (to be filled with real data)
inter_region_distances = {} # Define inter-region distances based on hub-to-hub distances
Objective function: minimize the inter-regional travel distance
Constraints: Ensure each region has one connection to another region
 model += lpSum(x[(region, j)] for j in region_centroids if region != j) == 1 # Outbound
 model += lpSum(x[(j, region)] for j in region_centroids if region != j) == 1 # Inbound
Solve the inter-regional connection model
model.solve()
```

```
KeyError
 Traceback (most recent call last)
 <ipython-input-22-5df65b875e2f> in <cell line: 17>()
 15
 16 # Objective function: minimize the inter-regional travel distance
 ---> 17 model += lpSum(inter_region_distances[(i, j)] * x[(i, j)] for i in region_centroids for j in region_centroids if i != j)
 19 # Constraints: Ensure each region has one connection to another region
 🗘 2 frames -
 <ipython-input-22-5df65b875e2f> in <genexpr>(.0)
 15
 16 # Objective function: minimize the inter-regional travel distance
 ---> 17 model += lpSum(inter_region_distances[(i, j)] * x[(i, j)] for i in region_centroids for j in region_centroids if i != j)
 18
 19 # Constraints: Ensure each region has one connection to another region
 KeyError: ('Canada', 'Caribbean')
Reload routes
import os
\ensuremath{\text{\#}} Delete the previously saved routes file to start fresh
saved_file_path = '/content/drive/MyDrive/optimized_routes.pkl'
if os.path.exists(saved_file_path):
 os.remove(saved_file_path)
 print("Deleted previously saved routes file.")
else:
 print("No saved routes file found.")
→ Deleted previously saved routes file.
!apt-get install -y glpk-utils

→ Reading package lists... Done

 Building dependency tree... Done
 Reading state information... Done
 The following additional packages will be installed:
 libamd2 libcolamd2 libglpk40 libsuitesparseconfig5
 Suggested packages:
 libiodbc2-dev
 The following NEW packages will be installed:
 glpk-utils libamd2 libcolamd2 libglpk40 libsuitesparseconfig5
 0 upgraded, 5 newly installed, 0 to remove and 49 not upgraded.
 Need to get 625 kB of archives.
 After this operation, 2,158 kB of additional disk space will be used.
 Get:1 http://archive.ubuntu.com/ubuntu jammy/main amd64 libsuitesparseconfig5 amd64 1:5.10.1+dfsg-4build1 [10.4 kB]
 Get:2 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libamd2 amd64 1:5.10.1+dfsg-4build1 [21.6 kB]
 Get:3 http://archive.ubuntu.com/ubuntu jammy/main amd64 libcolamd2 amd64 1:5.10.1+dfsg-4build1 [18.0 kB]
 Get:4 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libglpk40 amd64 5.0-1 [361 kB]
 Get:5 http://archive.ubuntu.com/ubuntu jammy/universe amd64 glpk-utils amd64 5.0-1 [214 kB]
 Fetched 625 kB in 1s (702 kB/s)
 Selecting previously unselected package libsuitesparseconfig5:amd64.
 (Reading database ... 123623 files and directories currently installed.)
 Preparing to unpack .../libsuitesparseconfig5_1%3a5.10.1+dfsg-4build1_amd64.deb ...
 Unpacking libsuitesparseconfig5:amd64 (1:5.10.1+dfsg-4build1) ...
 Selecting previously unselected package libamd2:amd64.
 Preparing to unpack .../libamd2_1%3a5.10.1+dfsg-4build1_amd64.deb ...
 Unpacking libamd2:amd64 (1:5.10.1+dfsg-4build1) ...
 Selecting previously unselected package libcolamd2:amd64.
 Preparing to unpack .../libcolamd2_1%3a5.10.1+dfsg-4build1_amd64.deb ...
 Unpacking libcolamd2:amd64 (1:5.10.1+dfsg-4build1) ...
 Selecting previously unselected package libglpk40:amd64.
 Preparing to unpack .../libglpk40_5.0-1_amd64.deb ...
 Unpacking libglpk40:amd64 (5.0-1) ..
 Selecting previously unselected package \ensuremath{\mathsf{glpk}}-utils.
 Preparing to unpack .../glpk-utils_5.0-1_amd64.deb ...
 Unpacking glpk-utils (5.0-1) ...
 Setting up libsuitesparseconfig5:amd64 (1:5.10.1+dfsg-4build1) ...
 Setting up libamd2:amd64 (1:5.10.1+dfsg-4build1) ...
 Setting up libcolamd2:amd64 (1:5.10.1+dfsg-4build1) ...
 Setting up libglpk40:amd64 (5.0-1) ...
 Setting up glpk-utils (5.0-1) .
 Processing triggers for man-db (2.10.2-1) ...
 Processing triggers for libc-bin (2.35-Oubuntu3.4) ...
 /sbin/ldconfig.real: /usr/local/lib/libur_adapter_level_zero.so.0 is not a symbolic link
 /sbin/ldconfig.real: /usr/local/lib/libtbbbind.so.3 is not a symbolic link
 /sbin/ldconfig.real: /usr/local/lib/libur_loader.so.0 is not a symbolic link
 /sbin/ldconfig.real: /usr/local/lib/libtbbmalloc.so.2 is not a symbolic link
```

```
/sbin/ldconfig.real: /usr/local/lib/libtbb.so.12 is not a symbolic link
 /sbin/ldconfig.real: /usr/local/lib/libtbbmalloc_proxy.so.2 is not a symbolic link
 /sbin/ldconfig.real: /usr/local/lib/libtbbbind_2_0.so.3 is not a symbolic link
 /sbin/ldconfig.real: /usr/local/lib/libtbbbind 2 5.so.3 is not a symbolic link
 / 62 /14 62 1 / /1 1/126/126
 . .
 0 :
model.solve(PULP_CBC_CMD(timeLimit=time_limit))
import pickle
import pandas as pd
import numpy as np
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import load npz
from pulp import LpMinimize, LpProblem, LpVariable, lpSum, GLPK
import time
import os
from pulp import LpMinimize, LpProblem, LpVariable, lpSum, PULP CBC CMD
Reload the dataset and distance matrix
file path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset new.csv'
data = pd.read_csv(file_path, encoding='latin-1')
Extract unique store locations with 'Order City', 'Order Region', 'Latitude', and 'Longitude' store_locations = data[['Order City', 'Order Region', 'Latitude', 'Longitude']].drop_duplicates().reset_index(drop=True) store_locations['Unique_ID'] = store_locations['Order City'] + "_" + store_locations['Latitude'].astype(str) + "_" + store_locations['Longitude'].astype(str)
Load the sparse distance matrix
distance_matrix_sparse = load_npz('/content/drive/MyDrive/distance_matrix_sparse.npz')
Group locations by region
regions = store_locations.groupby('Order Region')
Initialize an empty optimized_routes dictionary
optimized_routes = {}
Set a time limit for each region's optimization in seconds
time limit = 240
Process each region without skipping any
for region, group in regions:
 print(f"Starting optimization for region: {region}")
 start_time = time.time()
 # Adaptive sampling based on the region's size
 num_locations = len(group)
 if num locations <= 500:
 sample size = 100
 elif num locations <= 2000:
 sample size = 200
 elif num locations <= 5000:
 sample_size = 300
 else:
 sample size = 400 # Large regions get larger samples
 # Sample locations based on the determined sample size
 if num locations > sample size:
 sampled_group = group.sample(n=sample_size, random_state=1)
 print(f"Sampling \ \{sample_size\} \ locations \ for \ region \ \{region\} \ out \ of \ \{num_locations\} \ total.")
 else:
 sampled_group = group
 # Get indices of locations within this sampled region
 region_indices = sampled_group.index.tolist()
 valid_region_indices = [i for i in region_indices if i < distance_matrix_sparse.shape[0]]</pre>
 # Skip empty or invalid regions
 if not valid_region_indices:
 print(f"Skipping region {region} due to empty valid indices.")
 continue
 # Extract a local distance matrix for the sampled region
 local_distance_matrix = distance_matrix_sparse[valid_region_indices, :][:, valid_region_indices].toarray()
 # Initialize the optimization model for the region
 model = LpProblem(f"Route_Optimization_{region}", LpMinimize)
 x = LpVariable.dicts("Route", [(i, j) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j], cat='Binary')
 # Objective function: minimize total travel distance using the local distance matrix
 model += lpSum(local_distance_matrix[i][j] * x[(i, j)] for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if i != j)
 # Constraints: each location has exactly one inbound and one outbound route
 for i in range(len(valid_region_indices)):
 model += lpSum(x[(i, j)] for j in range(len(valid_region_indices)) if i != j) == 1
 model += lpSum(x[(j, i)] \ for \ j \ in \ range(len(valid_region_indices)) \ if \ i \ != \ j) \ == \ 1
```

```
Solve with the GLPK solver and set the time limit
 model.solve(PULP_CBC_CMD(timeLimit=time_limit))
 # Check if the model was solved within the time limit
 if model.status != 1: # Status 1 indicates an optimal solution was found
 print(f"Region {region} timed out without an optimal solution.")
 continue
 \# Extract the optimized route for the region and map back to the original indices
 region_route = [(valid_region_indices[i], valid_region_indices[j]) for i in range(len(valid_region_indices)) for j in range(len(valid_region_indices)) if
 optimized_routes[region] = region_route
 # Save progress after each region
 with open('/content/drive/MyDrive/optimized routes.pkl', 'wb') as f:
 pickle.dump(optimized routes, f)
 print(f"Completed optimization for region: \{region\} in \{time.time() - start_time:.2f\} seconds. Progress saved.")
print("All regions processed.")
\Longrightarrow Starting optimization for region: Canada
 Sampling 100 locations for region Canada out of 309 total.
 Completed optimization for region: Canada in 0.84 seconds. Progress saved.
 Starting optimization for region: Caribbean
 Sampling 300 locations for region Caribbean out of 2737 total.
 Completed optimization for region: Caribbean in 10.16 seconds. Progress saved.
 Starting optimization for region: Central Africa
 Sampling 200 locations for region Central Africa out of 553 total.
 /usr/local/lib/python3.10/dist-packages/pulp/pulp.py:1298: UserWarning: Spaces are not permitted in the name. Converted to '_' warnings.warn("Spaces are not permitted in the name. Converted to '_'")
 warnings.warn("Spaces are not permitted in the name. Converted to '
 Completed optimization for region: Central Africa in 3.01 seconds. Progress saved.
 Starting optimization for region: Central America
 Sampling 400 locations for region Central America out of 9186 total.
 Completed optimization for region: Central America in 17.88 seconds. Progress saved.
 Starting optimization for region: Central Asia
 Sampling 100 locations for region Central Asia out of 183 total.
 Completed optimization for region: Central Asia in 0.69 seconds. Progress saved.
 Starting optimization for region: East Africa
 Sampling 200 locations for region East Africa out of 612 total.
 Completed optimization for region: East Africa in 3.02 seconds. Progress saved.
 Starting optimization for region: East of USA
 Sampling 300 locations for region East of USA out of 2245 total.
 Completed optimization for region: East of USA in 8.31 seconds. Progress saved.
 Starting optimization for region: Eastern Asia
 Sampling 300 locations for region Eastern Asia out of 3309 total.
 Completed optimization for region: Eastern Asia in 8.42 seconds. Progress saved.
 Starting optimization for region: Eastern Europe
 Sampling 200 locations for region Eastern Europe out of 1290 total.
 Completed optimization for region: Eastern Europe in 3.04 seconds. Progress saved.
 Starting optimization for region: North Africa
 Sampling 200 locations for region North Africa out of 1052 total.
 Completed optimization for region: North Africa in 3.07 seconds. Progress saved.
 Starting optimization for region: Northern Europe
 Sampling 300 locations for region Northern Europe out of 3675 total.
 {\it Completed optimization for region: Northern \ {\it Europe in 8.16 seconds. Progress saved.} \\
 Starting optimization for region: Oceania
 Sampling 300 locations for region Oceania out of 4285 total.
 Completed optimization for region: Oceania in 8.28 seconds. Progress saved.
 Starting optimization for region: South America
 Sampling 300 locations for region South America out of 4952 total.
 Completed optimization for region: South America in 8.20 seconds. Progress saved.
 Starting optimization for region: South Asia
 Sampling 300 locations for region South Asia out of 3322 total.
 {\it Completed optimization for region: South Asia in 8.26 seconds. Progress saved.}
 Starting optimization for region: South of \ensuremath{\,\mathsf{USA}}
 Sampling 200 locations for region South of USA out of 1342 total.
 Completed optimization for region: South of USA in 3.04 seconds. Progress saved.
 Starting optimization for region: Southeast Asia
 Sampling 300 locations for region Southeast Asia out of 4234 total.
 Completed optimization for region: Southeast Asia in 8.47 seconds. Progress saved.
 Starting optimization for region: Southern Africa
 Sampling 100 locations for region Southern Africa out of 398 total.
 Completed optimization for region: Southern Africa in 0.67 seconds. Progress saved.
 Starting optimization for region: Southern Europe
 Sampling 300 locations for region Southern Europe out of 3517 total.
 Completed optimization for region: Southern Europe in 10.28 seconds. Progress saved.
 Starting optimization for region: US Center
 Sampling 200 locations for region US Center out of 1913 total.
```

import pickle

```
Save the final optimized routes after all regions are processed
with open('/content/drive/MyDrive/final_optimized_routes.pkl', 'wb') as f:
 pickle.dump(optimized_routes, f)
print("Final optimized routes saved successfully.")
```

```
Check contents of optimized routes for the first few regions
for region, route in list(optimized_routes.items())[:3]: # Print only the first 3 regions for brevity
 print(f"Region: {region}, Route Sample: {route[:5]}")
 Region: Canada, Route Sample: [(51698, 39091), (53037, 29270), (50502, 1587), (27294, 56491), (34926, 31279)]
 Region: Caribbean, Route Sample: [(20871, 23424), (21878, 18131), (17727, 21381), (64726, 12900), (16449, 23515)]
 Region: Central Africa, Route Sample: [(34596, 778), (32404, 32991), (2448, 44098), (31862, 33847), (56502, 51058)]
readjusting
Dictionary to map each region's local indices back to the global indices
region_index_mapping = {}
for region, group in regions:
 # ... [Sampling code as before]
 # Create a mapping from the global indices to local indices
 region_index_mapping[region] = {global_idx: local_idx for local_idx, global_idx in enumerate(valid_region_indices)}
 # Perform the optimization as before...
Convert distance matrix to dense format for easier indexing
distance_matrix_dense = distance_matrix_sparse.toarray()
Initialize a dictionary for summary data
summary_data = {
 "Region": [],
 "Num_Locations": [],
 "Total_Distance_km": []
Calculate summary metrics for each region
for region, route in optimized_routes.items():
 num_locations = len(route)
 # Use the region's index mapping to convert global to local indices
 index_mapping = region_index_mapping[region]
 # Sum the distances for each leg of the route using the local indices
 total distance = 0
 for loc1 global, loc2 global in route:
 # Convert global indices to local indices
 loc1 = index mapping.get(loc1 global)
 loc2 = index_mapping.get(loc2_global)
 # Ensure both indices are valid before accessing the distance
 if loc1 is not None and loc2 is not None:
 total_distance += distance_matrix_dense[loc1, loc2]
 summary_data["Region"].append(region)
 {\tt summary_data["Num_Locations"].append(num_locations)}
 summary_data["Total_Distance_km"].append(total_distance)
\mbox{\tt\#} Create a DataFrame from the summary data
summary_df = pd.DataFrame(summary_data)
Display the updated summary
print(summary_df)
₹
 Region Num_Locations Total_Distance_km
 100
 0.000000
 Canada
 Caribbean
 300
 0.000000
 1
 Central Africa
 200
 0.000000
 0.000000
 400
 3
 Central America
 0.000000
 4
 Central Asia
 100
 5
 East Africa
 200
 0.000000
 6
 East of USA
 300
 0.000000
 Eastern Asia
 0.000000
 300
 8
 Eastern Europe
 200
 0.000000
 North Africa
 200
 0.000000
 10
 Northern Europe
 300
 0.000000
 300
 0.000000
 11
 Oceania
 300
 0.000000
 12
 South America
 300
 0.000000
 13
 South Asia
 South of USA
 200
 9.999999
 14
 15
 Southeast Asia
 300
 0.000000
 16
 Southern Africa
 100
 0.000000
```

17

18 19

20

21

Southern Europe

US Center

West Africa

West of USA

Western Europe

West Asia

300

200

200

300

300

400

0.000000

0.000000

0.000000

0.000000

0.000000

23.385189

```
Convert distance matrix to dense format for easier indexing
distance matrix dense = distance matrix sparse.toarray()
Initialize a dictionary for summary data
summary data = {
 "Region": [].
 "Num_Locations": [],
 "Total_Distance_km": []
Calculate summary metrics for each region
for region, route in optimized_routes.items():
 num locations = len(route)
 # Use the region's index mapping to convert global to local indices
 index_mapping = region_index_mapping[region]
 # Sum the distances for each leg of the route using the local indices
 total distance = 0
 for loc1_global, loc2_global in route:
 # Convert global indices to local indices
 loc1 = index_mapping.get(loc1_global)
 loc2 = index_mapping.get(loc2_global)
 # Ensure both indices are valid before accessing the distance
 if loc1 is not None and loc2 is not None:
 distance = distance_matrix_dense[loc1, loc2]
 print(f"Region: {region}, loc1: {loc1_global}->{loc1}, loc2: {loc2_global}->{loc2}, Distance: {distance}")
 total_distance += distance
 print(f"Invalid mapping for region {region} with global indices ({loc1_global}, {loc2_global})")
 summarv data["Region"].append(region)
 summary_data["Num_Locations"].append(num_locations)
 summary_data["Total_Distance_km"].append(total_distance)
Create a DataFrame from the summary data
summary df = pd.DataFrame(summary data)
Display the updated summary
print(summary df)

→ Streaming output truncated to the last 5000 lines.

 Invalid mapping for region Central America with global indices (60256, 47438)
 Invalid mapping for region Central America with global indices (17846, 48741)
 Invalid mapping for region Central America with global indices (19795, 23984)
 Invalid mapping for region Central America with global indices (19359, 12857)
 Invalid mapping for region Central America with global indices (62851, 47497)
 Invalid mapping for region Central America with global indices (15373, 22495)
 Invalid mapping for region Central America with global indices (21710, 12259)
 Invalid mapping for region Central America with global indices (15098, 59681)
 Invalid mapping for region Central America with global indices (23156, 24265)
 Invalid mapping for region Central America with global indices (48272, 37375)
 Invalid mapping for region Central America with global indices (57652, 60242)
 Invalid mapping for region Central America with global indices (62973, 16807)
 Invalid mapping for region Central America with global indices (24601, 14426)
 Invalid mapping for region Central America with global indices (47497, 18639)
 Invalid mapping for region Central America with global indices (13778, 13921)
 Invalid mapping for region Central America with global indices (62100, 63460)
 Invalid mapping for region Central America with global indices (20748, 13778)
 Invalid mapping for region Central America with global indices (18857, 22317)
 Invalid mapping for region Central America with global indices (64765, 60181)
 Invalid mapping for region Central America with global indices (37375, 41170)
 Invalid mapping for region Central America with global indices (63554, 18473)
 Invalid mapping for region Central America with global indices (21821, 57417)
 Invalid mapping for region Central America with global indices (63469, 44696)
 Invalid mapping for region Central America with global indices (16545, 13190)
 Invalid mapping for region Central America with global indices (45232, 15970)
 Invalid mapping for region Central America with global indices (15386, 62130)
 Invalid mapping for region Central America with global indices (23225, 22668)
 Invalid mapping for region Central America with global indices (17255, 20003)
 Invalid mapping for region Central America with global indices (20007, 45956)
 Invalid mapping for region Central America with global indices (20003, 35336)
 Invalid mapping for region Central America with global indices (17804, 16431)
 Invalid mapping for region Central America with global indices (60786, 21915)
 Invalid mapping for region Central America with global indices (16257, 40960)
 Invalid mapping for region Central America with global indices (41010, 39446)
 Invalid mapping for region Central America with global indices (44578, 18617)
 Invalid mapping for region Central America with global indices (47343, 60256)
 Invalid mapping for region Central America with global indices (22660, 15373)
 Invalid mapping for region Central America with global indices (37381, 15358)
 Invalid mapping for region Central America with global indices (21362, 24601)
 Invalid mapping for region Central America with global indices (62884, 16561)
 Invalid mapping for region Central America with global indices (47325, 63469)
 Invalid mapping for region Central America with global indices (57463, 48211)
```

Invalid mapping for region Central America with global indices (13879, 47320)

```
Invalid mapping for region Central America with global indices (16937, 17287)
Invalid mapping for region Central America with global indices (48904, 14777)
Invalid mapping for region Central America with global indices (22668, 47325)
Invalid mapping for region Central America with global indices (59681, 16545)
Invalid mapping for region Central America with global indices (18319, 22115)
Invalid mapping for region Central America with global indices (16119, 20638)
Invalid mapping for region Central America with global indices (22600, 18825)
Invalid mapping for region Central America with global indices (59598, 23650)
Invalid mapping for region Central America with global indices (24265, 44559)
Invalid mapping for region Central America with global indices (48093, 64049)
Invalid mapping for region Central America with global indices (19194, 41010)
Invalid mapping for region Central America with global indices (43938, 43985)
Invalid mapping for region Central America with global indices (21915, 45931)
Invalid mapping for region Central America with global indices (61560, 20007)
```

## Done Before

```
import pickle
import pandas as pd
from geopy.distance import geodesic
from pulp import LpProblem, LpVariable, LpMinimize, lpSum
Step 1: Load previously saved optimized routes, if available
 with open('/content/drive/MyDrive/optimized_routes.pkl', 'rb') as f:
 optimized_routes = pickle.load(f)
 print("Loaded previously saved routes.")
except FileNotFoundError:
 optimized_routes = {}
 print("No previously saved routes found.")
Load your dataset with region information
file_path = '/content/drive/MyDrive/Dataco/Dataco SPMF/DataCoSupplyChainDataset_new.csv'
data = pd.read_csv(file_path, encoding='latin-1')
Step 2: Calculate or extract region centroids
Group by region and compute the centroid for each region
region_centroids = data.groupby('Order Region')[['Latitude', 'Longitude']].mean().to_dict('index')
Display calculated centroids for verification
print("Calculated Region Centroids:", region_centroids)
Step 3: Calculate inter-region distances for all pairs
inter region distances = {}
for region1, coord1 in region_centroids.items():
 for region2, coord2 in region_centroids.items():
 if region1 != region2:
 distance = geodesic((coord1['Latitude'], coord1['Longitude']),
 (coord2['Latitude'], coord2['Longitude'])).kilometers
 inter region distances[(region1, region2)] = distance
print("Inter-region distances calculated.")
Step 4: Initialize the inter-regional optimization model
model = LpProblem("Inter_Regional_Optimization", LpMinimize)
Define binary decision variables for connecting regional hubs
x = LpVariable.dicts("Connection", [(i, j) for i in region_centroids for j in region_centroids if i != j], cat='Binary')
Objective function: Minimize the inter-regional travel distance
\verb|model| += lpSum(inter_region_distances[(i, j)] * x[(i, j)] for i in region_centroids for j in region_centroids if i != j)
Constraints: Ensure each region has one inbound and one outbound connection
for region in region centroids:
 model += lpSum(x[(region, j)] for j in region_centroids if region != j) == 1 # Outbound
 \label{eq:model} model += lpSum(x[(j, region)] for j in region_centroids if region != j) == 1 \# Inbound
Step 5: Solve the model
model.solve()
Step 6: Extract and print the solution
inter_region_route = [(i, j) for i in region_centroids for j in region_centroids if i != j and x[(i, j)].value() == 1]
print("Optimized inter-regional routes:")
for route in inter region route:
 print(f"{route[0]} -> {route[1]} : Distance = {inter_region_distances[route]} km")
→ Loaded previously saved routes.
 Calculated Region Centroids: {'Canada': {'Latitude': 28.481428859082378, 'Longitude': -83.89738282228362}, 'Caribbean': {'Latitude'
 Inter-region distances calculated.
 Optimized inter-regional routes:
 Canada -> Caribbean : Distance = 106.57108696958886 km
 Caribbean -> Canada : Distance = 106.57108696958886 km
 Central Africa -> Western Europe : Distance = 11.741247058748462 km
 Central America -> East of USA : Distance = 21.164678016516667 km
 Central Asia -> Southern Africa : Distance = 50.5679578160694 km
 East Africa -> US Center : Distance = 23.298485217958838 km
 East of USA -> Central America: Distance = 21.164678016516667 km
 Eastern Asia -> Southern Europe : Distance = 9.001325444253256 km
 Eastern Europe -> South Asia : Distance = 32.57803423567837 km
```

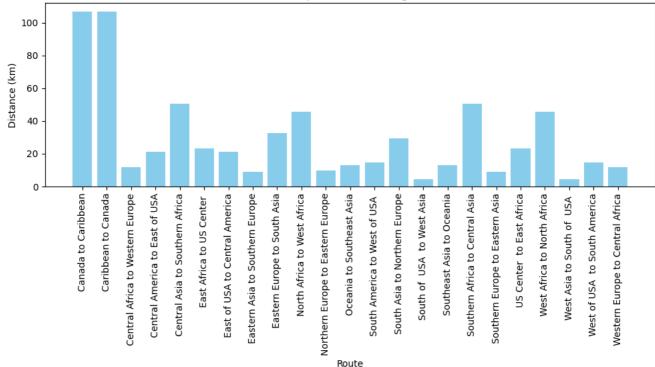
```
North Africa -> West Africa : Distance = 45.450347019735325 km
 Northern Europe -> Eastern Europe : Distance = 9.943789610845366 km
 Oceania -> Southeast Asia : Distance = 13.15347450984636 km
 South America -> West of USA : Distance = 14.870362923445649 km
 South Asia -> Northern Europe : Distance = 29.248153287127558 km
 South of USA -> West Asia : Distance = 4.7016199514832175 km
 Southeast Asia -> Oceania : Distance = 13.15347450984636 km
 Southern Africa -> Central Asia : Distance = 50.5679578160694 km
 Southern Europe -> Eastern Asia : Distance = 9.001325444253256 km
 US Center -> East Africa : Distance = 23.298485217958838 km
 West Africa -> North Africa : Distance = 45.450347019735325 km
 West Asia -> South of USA : Distance = 4.7016199514832175 km
 West of USA \rightarrow South America : Distance = 14.870362923445649 km
 Western Europe -> Central Africa : Distance = 11.741247058748462 km
Convert inter-region routes to a DataFrame for export
route_data = []
for (start, end) in inter_region_route:
 route_data.append({
 'Start_Region': start,
 'End_Region': end,
 'Distance_km': inter_region_distances[(start, end)]
Convert to DataFrame
inter_region_routes_df = pd.DataFrame(route_data)
inter_region_routes_df.to_csv('/content/drive/MyDrive/inter_region_optimized_routes.csv', index=False)
print("Inter-regional routes saved to CSV.")

→ Inter-regional routes saved to CSV.
import folium
from folium.plugins import MarkerCluster
Initialize a map centered around a general location, e.g., North America
m = folium.Map(location=[20, -40], zoom_start=2)
Add markers for each region's centroid
for region, coords in region_centroids.items():
 folium.Marker(
 location=[coords['Latitude'], coords['Longitude']],
 popup=region,
 icon=folium.Icon(color='blue')
).add to(m)
Add lines for each optimized inter-regional route
for route in inter_region_route:
 start, end = route
 start_coords = (region_centroids[start]['Latitude'], region_centroids[start]['Longitude'])
 end_coords = (region_centroids[end]['Latitude'], region_centroids[end]['Longitude'])
 folium.PolyLine([start_coords, end_coords], color="green", weight=2.5, opacity=0.7).add_to(m)
Display the map
```









Total optimized inter-regional travel distance: 672.81 km

```
Check region centroid coordinates to ensure uniqueness
print("Region Centroid Coordinates:")
for region, coords in region_centroids.items():
 print(f"{region}: Latitude = {coords['Latitude']}, Longitude = {coords['Longitude']}")
```

## Region Centroid Coordinates:

Canada: Latitude = 28.481428859082378, Longitude = -83.89738282228362 Caribbean: Latitude = 29.420087655226016, Longitude = -84.13440337999519 Central Africa: Latitude = 29.43170403423375, Longitude = -84.33532999645796 Central America: Latitude = 29.784980621666843, Longitude = -84.85625888775766 Central Asia: Latitude = 29.770689149041594, Longitude = -86.16474666182641 East Africa: Latitude = 30.268241870642548, Longitude = -84.7324461737203 East of USA: Latitude = 29.97011166767607, Longitude = -84.80267315744902 Eastern Asia: Latitude = 29.801265343578297, Longitude = -85.44774099886402 Eastern Europe: Latitude = 29.52297577384184, Longitude = -84.86765491792092 North Africa: Latitude = 30.104770037889853, Longitude = -85.17615629733601 Northern Europe: Latitude = 29.562321615665848, Longitude = -84.95985283379697 Oceania: Latitude = 29.8896444554868, Longitude = -85.10332279159144 South America: Latitude = 29.770487795179108, Longitude = -85.27954561919651 South Asia: Latitude = 29.35033669207994, Longitude = -85.13939169965334 South of USA: Latitude = 29.641509338536466, Longitude = -85.3760699117528 Southeast Asia: Latitude = 29.962089905565577, Longitude = -84.99543514233987 Southern Africa: Latitude = 29.94423049327571, Longitude = -86.64874730510803 Southern Europe: Latitude = 29.748695435019616, Longitude = -85.37679717788781 US Center : Latitude = 30.082330894627145, Longitude = -84.61962600324614 West Africa: Latitude = 30.371047337849024, Longitude = -85.53520151171266 West Asia: Latitude = 29.64408273057913, Longitude = -85.42453589478116 West of USA: Latitude = 29.67390660179657, Longitude = -85.17287773724009 Western Europe: Latitude = 29.50494540322107, Longitude = -84.24788029250692

# Inspect unique latitude and longitude values per region in the dataset
unique\_coordinates = data[['Order Region', 'Latitude', 'Longitude']].drop\_duplicates()
print("Unique Coordinates by Region:")
print(unique\_coordinates)

## $\rightarrow$ Unique Coordinates by Region:

```
Order Region
 Latitude Longitude
0
 Southern Europe
 40.675449 -73.811142
2
 Western Europe
 18.250792 -66.370544
3
 Western Europe
 18.274948 -66.370506
8
 Western Europe
 18.272160 -66.370522
 18.217916 -66.370621
12
 Western Europe
180456
 South America
 18.289656 -66.370567
180467
 18.359005 -66.078163
 Central America
180474
 18.295542 -66.370613
 Caribbean
180480
 40.808941 -74.032860
 Caribbean
180489
 Central America 18.244116 -66.370628
```

[45998 rows x 3 columns]

```
import pickle
import pandas as pd
from geopy.distance import geodesic
from pulp import LpProblem, LpVariable, LpMinimize, lpSum
Step 1: Load previously saved optimized routes, if available
 with open('/content/drive/MyDrive/optimized routes.pkl', 'rb') as f:
 optimized_routes = pickle.load(f)
 print("Loaded previously saved routes.")
except FileNotFoundError:
 optimized routes = {}
 print("No previously saved routes found.")
Step 2: Define manually updated region centroids (approximate locations)
region_centroids = {
 'Canada': {'Latitude': 56.1304, 'Longitude': -106.3468},
 'Caribbean': {'Latitude': 18.4655, 'Longitude': -66.1057},
 'Central Africa': {'Latitude': -0.228, 'Longitude': 15.8277},
 'Central America': {'Latitude': 14.6349, 'Longitude': -90.5069},
 'Central Asia': {'Latitude': 39.9042, 'Longitude': 69.3451},
 'East Africa': {'Latitude': -1.286389, 'Longitude': 36.817223},
 'East of USA': {'Latitude': 37.0902, 'Longitude': -95.7129},
 'Eastern Asia': {'Latitude': 35.8617, 'Longitude': 104.1954},
 'Eastern Europe': {'Latitude': 55.7558, 'Longitude': 37.6173},
 'North Africa': {'Latitude': 30.033056, 'Longitude': 31.233333},
 'Northern Europe': {'Latitude': 60.1282, 'Longitude': 18.6435},
 'Oceania': {'Latitude': -25.2744, 'Longitude': 133.7751},
 'South America': {'Latitude': -23.5505, 'Longitude': -46.6333},
 'South Asia': {'Latitude': 20.5937, 'Longitude': 78.9629},
 'South of USA': {'Latitude': 29.7604, 'Longitude': -95.3698},
 'Southeast Asia': {'Latitude': 13.7563, 'Longitude': 100.5018},
 'Southern Africa': {'Latitude': -29.5714, 'Longitude': 29.2332},
 'Southern Europe': {'Latitude': 41.9028, 'Longitude': 12.4964},
 'US Center': {'Latitude': 39.0997, 'Longitude': -94.5786},
 'West Africa': {'Latitude': 5.6037, 'Longitude': -0.187},
 'West Asia': {'Latitude': 24.7136, 'Longitude': 46.6753},
 'West of USA': {'Latitude': 36.7783, 'Longitude': -119.4179},
 'Western Europe': {'Latitude': 48.8566, 'Longitude': 2.3522},
print("Updated Region Centroids:", region_centroids)
Step 3: Calculate inter-region distances for all pairs
inter_region_distances = {}
for region1, coord1 in region_centroids.items():
 for region2, coord2 in region_centroids.items():
 if region1 != region2:
 distance = geodesic((coord1['Latitude'], coord1['Longitude']),
 (coord2['Latitude'], coord2['Longitude'])).kilometers
 inter_region_distances[(region1, region2)] = distance
print("Inter-region distances calculated.")
Step 4: Initialize the inter-regional optimization model
model = LpProblem("Inter Regional Optimization", LpMinimize)
Define binary decision variables for connecting regional hubs
x = LpVariable.dicts("Connection", [(i, j) for i in region_centroids for j in region_centroids if i != j], cat='Binary')
Objective function: Minimize the inter-regional travel distance
model += lpSum(inter_region_distances[(i, j)] *x[(i, j)] for i in region_centroids for j in region_centroids if i != j) for in region_centroids if i != j) for in region_centroids for j in region_centroids if i != j) for in region_centroids for j in region_centroids for j in region_centroids if i != j) for in region_centroids for j in region_centroids f
Constraints: Ensure each region has one inbound and one outbound connection
for region in region centroids:
 model += lpSum(x[(region, j)] for j in region_centroids if region != j) == 1 # Outbound
 model += lpSum(x[(j, region)] for j in region_centroids if region != j) == 1 # Inbound
Step 5: Solve the model
model.solve()
Step 6: Extract and print the solution
inter_region_route = [(i, j) \ for \ i \ in \ region_centroids \ for \ j \ in \ region_centroids \ if \ i \ != j \ and \ x[(i, j)].value() \ == 1]
print("Optimized inter-regional routes:")
for route in inter region route:
 print(f"{route[0]} -> {route[1]} : Distance = {inter region distances[route]:.2f} km")

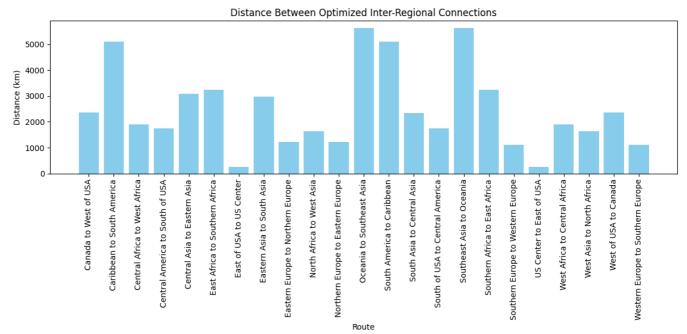
→ Loaded previously saved routes.
 Updated Region Centroids: {'Canada': {'Latitude': 56.1304, 'Longitude': -106.3468}, 'Caribbean': {'Latitude': 18.4655, 'Longitude':
 Inter-region distances calculated.
 Optimized inter-regional routes:
 Canada -> West of USA : Distance = 2364.72 km
 Caribbean -> South America : Distance = 5106.95 km
 Central Africa -> West Africa : Distance = 1893.22 km
 Central America -> South of USA : Distance = 1747.78 km
 Central Asia -> Eastern Asia : Distance = 3078.70 km
 East Africa -> Southern Africa : Distance = 3231.89 km
 East of USA -> US Center : Distance = 244.23 km
 Eastern Asia -> South Asia : Distance = 2984.38 km
```

```
North Africa -> West Asia : Distance = 1635.53 km
 Northern Europe -> Eastern Europe : Distance = 1219.21 km
 Oceania -> Southeast Asia : Distance = 5628.12 km
 South America -> Caribbean : Distance = 5106.95 km
 South Asia -> Central Asia : Distance = 2328.70 km
 South of USA -> Central America : Distance = 1747.78 km
 Southeast Asia -> Oceania : Distance = 5628.12 km
 Southern Africa -> East Africa : Distance = 3231.89 km
 Southern Europe -> Western Europe : Distance = 1106.60 km
 US Center -> East of USA : Distance = 244.23 km
 West Africa -> Central Africa : Distance = 1893.22 km
 West Asia -> North Africa : Distance = 1635.53 km
 West of USA -> Canada : Distance = 2364.72 km
 Western Europe -> Southern Europe : Distance = 1106.60 km
Convert inter-region routes to a DataFrame for export
route_data = []
for (start, end) in inter_region_route:
 route_data.append({
 'Start_Region': start,
 'End_Region': end,
 'Distance_km': inter_region_distances[(start, end)]
Convert to DataFrame
inter_region_routes_df = pd.DataFrame(route_data)
Save to CSV
inter_region_routes_df.to_csv('/content/drive/MyDrive/inter_region_optimized_routes.csv', index=False)
print("Inter-regional routes saved to CSV.")
→ Inter-regional routes saved to CSV.
Define a maximum number of stops per route (example capacity)
max stops = 5
Add capacity constraints for each route in the model
for region in region centroids:
 model += lpSum(x[(region, j)] for j in region centroids if region != j) <= max stops</pre>
Optimize Last Mile routes
!pip install ortools
 → Collecting ortools
 Downloading ortools-9.11.4210-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.whl.metadata (3.0 kB)
 Collecting abs1-py>=2.0.0 (from ortools)
 Downloading absl_py-2.1.0-py3-none-any.whl.metadata (2.3 kB) \,
 Requirement \ already \ satisfied: \ numpy>=1.13.3 \ in \ /usr/local/lib/python3.10/dist-packages \ (from \ ortools) \ (1.26.4)
 Requirement already satisfied: pandas>=2.0.0 in /usr/local/lib/python3.10/dist-packages (from ortools) (2.2.2)
 Collecting protobuf<5.27,>=5.26.1 (from ortools)
 Downloading protobuf-5.26.1-cp37-abi3-manylinux2014_x86_64.whl.metadata (592 bytes)
 Requirement already satisfied: immutabledict>=3.0.0 in /usr/local/lib/python3.10/dist-packages (from ortools) (4.2.0)
 Requirement already satisfied: python-dateutil>=2.8.2 in /usr/local/lib/python3.10/dist-packages (from pandas>=2.0.0->ortools) (2.8
 Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.10/dist-packages (from pandas>=2.0.0->ortools) (2024.2)
 Requirement already satisfied: tzdata>=2022.7 in /usr/local/lib/python3.10/dist-packages (from pandas>=2.0.0->ortools) (2024.2)
 Requirement already satisfied: \verb|six| = 1.5| in /usr/local/lib/python3.10/dist-packages (from python-dateutil) = 2.8.2-pandas > = 2.0.0-pardas > = 2.0.0-pard
 Downloading ortools-9.11.4210-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (28.1 MB)
 - 28.1/28.1 MB 40.6 MB/s eta 0:00:00
 Downloading absl_py-2.1.0-py3-none-any.whl (133 kB)
 133.7/133.7 kB 11.4 MB/s eta 0:00:00
 Downloading protobuf-5.26.1-cp37-abi3-manylinux2014_x86_64.whl (302 kB)
 302.8/302.8 kB 22.9 MB/s eta 0:00:00
 Installing collected packages: protobuf, absl-py, ortools
 Attempting uninstall: protobuf
 Found existing installation: protobuf 3.20.3
 Uninstalling protobuf-3.20.3:
 Successfully uninstalled protobuf-3.20.3
 Attempting uninstall: absl-py
 Found existing installation: absl-py 1.4.0
 Uninstalling absl-py-1.4.0:
 Successfully uninstalled absl-py-1.4.0
 ERROR: pip's dependency resolver does not currently take into account all the packages that are installed. This behaviour is the sou
 google-cloud-datastore 2.19.0 requires protobuf!=3.20.0,!=3.20.1,!=4.21.0,!=4.21.1,!=4.21.2,!=4.21.3,!=4.21.4,!=4.21.5,<5.0.0dev,>=3.20.1,!=4.21.2,!=4.21.2,!=4.21.3,!=4.21.4,!=4.21.5,<5.0.0dev,>=3.20.1,!=4.21.2,!=4.21.2,!=4.21.2,!=4.21.3,!=4.21.4,!=4.21.5,<5.0.0dev,>=3.20.1,!=4.21.2,!=4.21.2,!=4.21.2,!=4.21.2,!=4.21.2,!=4.21.2,!=4.21.3,!=4.21.4,!=4.21.5,<5.0.0dev,>=3.20.1,!=3.20
 google-cloud-firestore 2.16.1 requires protobuf!=3.20.0,!=3.20.1,!=4.21.0,!=4.21.1,!=4.21.2,!=4.21.3,!=4.21.4,!=4.21.5,<5.0.0dev,>=
 tensorboard 2.17.0 requires protobuf!=4.24.0,<5.0.0,>=3.19.6, but you have protobuf 5.26.1 which is incompatible.
 tensorflow 2.17.0 requires protobuf!=4.21.0,!=4.21.1,!=4.21.2,!=4.21.3,!=4.21.4,!=4.21.5,<5.0.0dev,>=3.20.3, but you have protobuf!
 tensorflow-metadata 1.16.1 requires protobuf<4.21,>=3.20.3; python_version < "3.11", but you have protobuf 5.26.1 which is incompati
 Successfully installed absl-py-2.1.0 ortools-9.11.4210 protobuf-5.26.1
```

Eastern Europe -> Northern Europe : Distance = 1219.21 km

```
from ortools.constraint solver import routing enums pb2
from ortools.constraint solver import pywrapcp
def optimize last mile routes(distance matrix):
 # Setup OR-Tools routing solver for VRP
 manager = pywrapcp.RoutingIndexManager(len(distance_matrix), 1, 0)
 routing = pywrapcp.RoutingModel(manager)
 # Set distance as the cost for each edge
 def distance_callback(from_index, to_index):
 return distance_matrix[from_index][to_index]
 transit_callback_index = routing.RegisterTransitCallback(distance_callback)
 routing. Set Arc Cost Evaluator Of All Vehicles (transit_callback_index)
 # Solve the VRP with OR-Tools
 search_parameters = pywrapcp.DefaultRoutingSearchParameters()
 search_parameters.first_solution_strategy = routing_enums_pb2.FirstSolutionStrategy.PATH_CHEAPEST_ARC
 solution = routing.SolveWithParameters(search_parameters)
 # Extract and return route
 if solution:
 route = []
 index = routing.Start(0)
 while not routing.IsEnd(index):
 route.append(manager.IndexToNode(index))
 index = solution.Value(routing.NextVar(index))
 return route
 return None
Calculate total optimized distance
total_optimized_distance = inter_region_routes_df['Distance_km'].sum()
print(f"Total optimized inter-regional travel distance: {total_optimized_distance:.2f} km")
Example: Assuming a hypothetical baseline with all regions connected directly (you would replace this with real data if available)
baseline_distance = inter_region_routes_df['Distance_km'].sum() * 1.25 # Hypothetically, 25% more than optimized
distance_savings = baseline_distance - total_optimized_distance
percentage_savings = (distance_savings / baseline_distance) * 100
print(f"Baseline distance (hypothetical): {baseline_distance:.2f} km")
print(f"Distance savings: {distance_savings:.2f} km ({percentage_savings:.2f}% reduction)")
Total optimized inter-regional travel distance: 56748.33 km
 Baseline distance (hypothetical): 70935.41 km
 Distance savings: 14187.08 km (20.00% reduction)
Find the longest and shortest routes
longest_route = inter_region_routes_df.loc[inter_region_routes_df['Distance_km'].idxmax()]
shortest_route = inter_region_routes_df.loc[inter_region_routes_df['Distance_km'].idxmin()]
print("Longest Route:")
 print(f"\{longest_route['Start_Region']\} \ to \ \{longest_route['End_Region']\} \ - \ \{longest_route['Distance_km']: .2f\} \ km")
print("Shortest Route:")
print(f"\{shortest_route['Start_Region']\} \ to \ \{shortest_route['End_Region']\} \ - \ \{shortest_route['Distance_km']:.2f\} \ km")
→ Longest Route:
 Oceania to Southeast Asia - 5628.12 km
 Shortest Route:
 East of USA to US Center - 244.23 km
import matplotlib.pyplot as plt
Plot a bar chart of distances between regions
plt.figure(figsize=(12, 6))
plt.bar(inter_region_routes_df['Start_Region'] + " to " + inter_region_routes_df['End_Region'],
 inter_region_routes_df['Distance_km'], color='skyblue')
plt.title("Distance Between Optimized Inter-Regional Connections")
plt.xlabel("Route")
plt.ylabel("Distance (km)")
plt.xticks(rotation=90)
plt.tight_layout()
plt.show()
```





## Run Last-Mile Route Optimization within Each Region (Example with OR-Tools)

```
import numpy as np
from geopy.distance import geodesic
from ortools.constraint_solver import routing_enums_pb2
from ortools.constraint_solver import pywrapcp
Step 1: Define manually updated region centroids (approximate locations)
 'Canada': {'Latitude': 56.1304, 'Longitude': -106.3468},
 'Caribbean': {'Latitude': 18.4655, 'Longitude': -66.1057},
 'Central Africa': {'Latitude': -0.228, 'Longitude': 15.8277},
 'Central America': {'Latitude': 14.6349, 'Longitude': -90.5069},
 'Central Asia': {'Latitude': 39.9042, 'Longitude': 69.3451},
 'East Africa': {'Latitude': -1.286389, 'Longitude': 36.817223},
 'East of USA': {'Latitude': 37.0902, 'Longitude': -95.7129},
 'Eastern Asia': {'Latitude': 35.8617, 'Longitude': 104.1954},
 'Eastern Europe': {'Latitude': 55.7558, 'Longitude': 37.6173},
 'North Africa': {'Latitude': 30.033056, 'Longitude': 31.233333},
 'Northern Europe': {'Latitude': 60.1282, 'Longitude': 18.6435},
 'Oceania': {'Latitude': -25.2744, 'Longitude': 133.7751},
 'South America': {'Latitude': -23.5505, 'Longitude': -46.6333},
 'South Asia': {'Latitude': 20.5937, 'Longitude': 78.9629},
 'South of USA': {'Latitude': 29.7604, 'Longitude': -95.3698},
 'Southeast Asia': {'Latitude': 13.7563, 'Longitude': 100.5018},
 'Southern Africa': {'Latitude': -29.5714, 'Longitude': 29.2332}, 'Southern Europe': {'Latitude': 41.9028, 'Longitude': 12.4964},
 'US Center': {'Latitude': 39.0997, 'Longitude': -94.5786},
 'West Africa': {'Latitude': 5.6037, 'Longitude': -0.187}, 'West Asia': {'Latitude': 24.7136, 'Longitude': 46.6753},
 'West of USA': {'Latitude': 36.7783, 'Longitude': -119.4179},
 'Western Europe': {'Latitude': 48.8566, 'Longitude': 2.3522},
print("Region centroids loaded.")
Step 2: Generate locations near each region's centroid
def generate_locations_near_centroid(centroid, num_locations=5, distance_offset=0.5):
 "Generate sample locations near a centroid for demonstration.""
 lat, lon = centroid['Latitude'], centroid['Longitude']
 locations = [(lat + np.random.uniform(-distance_offset, distance_offset),
 lon + np.random.uniform(-distance_offset, \ distance_offset)) \ for \ _in \ range(num_locations)]
 return locations
Create example last-mile locations for each region based on its centroid
region_last_mile_locations = {
 region: generate_locations_near_centroid(coords, num_locations=5)
 for region, coords in region_centroids.items()
Step 3: Generate a distance matrix for last-mile optimization within each region
def generate_distance_matrix(locations):
 num_locations = len(locations)
 distance_matrix = np.zeros((num_locations, num_locations))
 for i in range(num_locations):
 for j in range(num locations):
 if i != j:
 distance matrix[i][j] = geodesic(locations[i], locations[j]).kilometers
 return distance matrix
```

```
Generate distance matrices for last-mile routes within each region
region_last_mile_distance_matrices = {
 region: generate_distance_matrix(locations) for region, locations in region_last_mile_locations.items()
}

Step 4: Optimize last-mile routes using OR-Tools
def optimize_last_mile_routes(distance_matrix):
 # Initialize the routing model
 manager = pywrapcp.RoutingIndexManager(len(distance_matrix), 1, 0)
 routing = pywrapcp.RoutingModel(manager)

Create distance callback
def distance_callback(from_index, to_index):
 return int(distance_matrix[manager.IndexToNode(from_index)][manager.IndexToNode(to_index)] * 1000) # Convert km to meters for precision
```