# Data Project

# Peiran Wang

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# Contents

#### Variable Selection

```
variable_selection1 = function(X, Y) {
    # TODO: fancier variable selection logic
    return(abs(cor(X, Y)) >= 0.35)
    # return a vector of booleans indicating which covariates are selected.
}

variable_selection2 = function(X, Y) {
    # TODO: fancier variable selection logic
    fit = glmnet(X,Y,alpha=0.8,lambda = 5)
    selected = coef(fit)!=0
    return(selected[-1])
    # return a vector of booleans indicating which covariates are selected.
}
```

# Prediction model using one set of covariates

```
prediction_model1 = function(X, Y, X_new) {
    # TODO: fancier prediction model
    cv_model <- cv.glmnet(X, Y, alpha = 0.2)
    best_lambda <- cv_model$lambda.min
    best_model <- glmnet(X, Y, alpha = 0.2, lambda = best_lambda)
    return(predict(best_model, newx = X_new))
}

prediction_model2 = function(X, Y, X_new) {
    # TODO: fancier prediction model
    model = lm(Y ~ 1, data = data.frame(X))
    full_model = lm(Y ~ ., data = data.frame(X))
    step_model = stepAIC(model, scope = list(lower = model, upper = full_model), direction = "forward",tr
    return(predict(step_model, newx=X_new))
}</pre>
```

#### Combined Model

```
combined_model = function(X1, X2, Y, X1_new, X2_new) {
   # TODO: fancier model that combines two sets of covariates
   X0 = X1[,1]*X2
   for (i in 2:dim(X1)[2]) {
      temp = X1[,i]*X2
      X0 = cbind(X0, temp)
   }
   fit = cv.glmnet(X0, Y, nfolds = 10, family = "gaussian", alpha = 0.2)
   best_lambda = fit$lambda.min
   best_fit = glmnet(X0, Y, family = "gaussian", alpha = 0.2, lambda = best_lambda)
   X0_new = X1_new[,1]*X2_new
   for (i in 2:dim(X1_new)[2]) {
      temp = X1_new[,i]*X2_new
      X0_new = cbind(X0_new, temp)
   }
   return(predict(fit, newx = X0_new))
}
```

### Estimate prediction error of the two-stage procedure

For example, using leave-one-out cross validation.

```
Z = Y
predictions = sapply(1:length(Y), function(i) {
    # leave one out
    Xi1 = X1[-i, ]
    Xi2 = X2[-i, ]
    Zi = Z[-i]

# variable selection
s1 = variable_selection1(Xi1, Zi)
s2 = variable_selection2(Xi2, Zi)
```

```
Xi1_s = Xi1[, s1]
  Xi2_s = Xi2[, s2]
  # left out data for testing
  X1_new = X1[i, s1, drop = FALSE]
  X2_{new} = X2[i, s2, drop = FALSE]
  # evaluation of prediction model using first dataset
  pred1 = prediction_model1(Xi1_s, Zi, X1_new)
  # evaluation of prediction model using second dataset
  pred2 = prediction_model2(Xi2_s, Zi, X2_new)
  # evaluation of prediction model using combined dataset
  pred_combined = combined_model(Xi1_s, Xi2_s, Zi, X1_new, X2_new)
  return(rbind(
    pred1,
    pred2,
    pred_combined
  ))
})
# Evaluation
# Model using first dataset
sqrt(mean((predictions[1, ] - Y)^2))
[1] 34.20361
# Model using second dataset
sqrt(mean((predictions[2, ] - Y)^2))
[1] 33.87671
# Model using combined dataset
sqrt(mean((predictions[3, ] - Y)^2))
```

[1] 31.44185