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P6492

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SEAT No.: [Total No. of Pages: 4

First Year Engineering **ENGINEERING MATHEMATICS-II**

(2019 Pattern) (Semester - I & III) (107008)

Time: 2½ Hours]

[Max. Marks: 70

Instructions to the candidates:

- Q.No. 1 is compulsory.
- Solve Q.2 or Q.3, C,4 or Q.5, Q.6 or Q.7, Q.8, or Q.9. *2*)
- Neat diagrams must be drawn whenever necessary. 3)
- Figures to the right indicate full marks. 4)
- Use of electronic pocket calculator is allowed. *5)*
- Assume suitable data if necessary.

Q1) Write the correct option for the following multiple choice questions.

a)
$$\int_{0}^{\frac{\pi}{2}} \cos^{6} x =$$
ii)
$$\frac{5}{16}$$
iii)
$$\frac{16\pi}{10}$$
iv)
$$\frac{5\pi}{48}$$
b) The curve $y^{2}(x-a) = x^{2}(2a-x)$ is
i) Symmetric about X - axis and net passing through origin
ii) Symmetric about Y - axis and passing through origin
iii) Symmetric about Y - axis and passing through origin
iv) Symmetric about Y - axis and passing through origin
iv) Symmetric about Y - axis and passing through origin
iv) Symmetric about Y - axis and passing through origin
iv) The value of double integral
$$\int_{0}^{1} \int_{0}^{1} \frac{1}{\sqrt{1-x^{2}}} dx \, dy \text{ is}$$
 [2]

- b)
 - Symmetric about X axis and net passing through origin
 - Symmetric about Y axis and net passing through origin
 - Symmetric about X axis and passing through origin
 - Symmetric about Y axis and passing through origin

c) The value of double integral
$$\int_{0}^{1} \int_{0}^{1} \frac{1}{\sqrt{1-x^2}\sqrt{1-y^2}} dx dy \text{ is}$$
 [2]

i)

iii)

P.T.O.

d) The Centre (C) and radius (r) of the sphere
$$x^2 + y^2 + z^2 - 2y - 4z - 11 = 0$$
 are

i)
$$C = (0,1,2); r = 4$$

i)
$$C \equiv (0,-1,-2); r = 2$$

i)
$$C \equiv (0,1,2); r = 4$$

iii) $C \equiv (0,2,4); r = 4$

iv)
$$C \equiv (0,1,2); r = 2$$

e) The number of loops in the rose curve
$$r = a \cos 4\theta$$
 are [1]

f)
$$\iint_{\mathbb{R}} dxdy$$
 represents [1]

- ii) Centre of gravity
- Moment of inertia
- iv) Area of region R

Q2) a) If
$$I_n = \int_{\pi/4}^{\pi/2} \cot^n \theta \ d\theta$$
 prove that $I_n = \frac{1}{1 - 1} - I_{n-2}$. [5]

b) Show that
$$\int_{0}^{1} x^{m-1} (1-x^{2})^{n-1} dx = \frac{1}{2} \beta \binom{m}{2}, n$$
. [5]

b) Show that
$$\int_{0}^{1} x^{m-1} (1-x^{2})^{n-1} dx = \frac{1}{2} \beta \left(\frac{m}{2}, n\right)$$
. [5]

c) Prove that $\int_{0}^{1} \frac{x^{a}-1}{\log x} dx = \log(b+a), a \ge 0$.

OR

Q3) a) If
$$I_n = \int_0^{\pi/2} x^n \sin x \, dx$$
 then prove that $I_n = n \left(\frac{\pi}{2}\right)^{n-1} - n(n-1) I_{n-2}$. [5]

b) Show that
$$\int_{0}^{\infty} e^{-h^2 x^2} dx = \frac{\sqrt{\pi}}{2h}.$$
 [5]

$$\int_{a}^{b} e^{-x^{2}} dx = \frac{\sqrt{\pi}}{2} \left[erf(b) - erf(a) \right]$$

OR

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Q4) a) Trace the curve
$$x^2y^2 = a^2(y^2 - x^2)$$
 [5]

b) Trace the curve
$$r = a(1 - \sin \theta)$$
 [5]

c) Find the whole length of the loop of the curve
$$3y^2 = x(x-1)^2$$
. [5]

Q5) a) Trace the curve
$$y^2(2a-x)=x^3$$
. [5]
b) Trace the curve $r = a\cos 2\theta$.

b) Trace the curve
$$r = a\cos 2\theta$$
. [5]

c) Trace the curve
$$x^{2/3} + y^{2/3} = a^{2/3}$$
. [5]

- Prove that the two spheres $x^2 + y^2 + z^2 = 2x + 4y 4z = 0$ **Q6)** a) $x^2 + y^2 + z^2 + 10x + 2z + 10 = 0$ touch each other and find the co-ordinates of the point of contact. [5]
 - Find the equation of right circular cone whose vertex is (1,-1,2), axis is b) the line $\frac{x-1}{2} = \frac{y+1}{1} = \frac{z-2}{2}$ and the semi-vertical angle 45°. [5]
 - Find the equation of right circular cylinder of radius a whose axis passes c) through the origin and makes equal angles with the co-ordinate axes [5]

- Show that the plane x-2y-2z-7=0 touches the sphere **Q7**) a) $x^{2} + y^{2} + z^{2} - 10y - 10z - 31 = 0$. Also find the point of contact. [5]
 - Find the equation of right circular cone with vertex at origin, axis the b) Y-axis and semi-vertical angle 30°. [5]
 - Find the equation of right circular cylinder of radius $\sqrt{6}$ whose axis is c) the line $\frac{x}{1} = \frac{y}{-1} = \frac{z}{1}$. [5]

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Q8) a)	Change the order of integration and evaluate $\int_0^{\pi} \int_x^{\pi} \frac{\sin y}{y} dx dy$.	[5]
b)	Find the area of one loop of $r = a \sin 2\theta$.	[5]
c)	Find the moment of inertia of one loop of the lemniscate $r^2 - a^2$	cos 26

c) Find the moment of inertia of one loop of the lemniscate
$$r^2 = a^2 \cos 2\theta$$
 about initial line. Given that $\rho = \frac{2m}{a^2}$, m is the mass of loop of lemniscate.

Q9) a) Evaluate
$$\iint_1 y dx dy$$
 over the region enclosed by the parabola $x^2 = y$, and the line $y = x + 2$. [5]

Evaluate
$$\iiint x^2 yz dx dy dz$$
, throughout the volume bounded by the plane $x = 0, y = 0, z = 0$ $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$. [5]

Find the y - coordinate of the centre of gravity of the area bounded by by the state of th c) $r = a \sin \theta$ and $r = 2a \sin \theta$. Given that the area bounded by these curves is $\frac{3\pi a^2}{4}$. [5]

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