Python for economists

Ewen Gallic September 2019

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Opening remarks

These notes were produced as part of an introductory course on Python for students in the Econometrics and Big Data course of Aix-Marseille School of Economics / École d'Economie d'Aix-Marseille (AMSE)

0.1 Objectives

The purpose of this book is to introduce you to the Python programming language, to be able to use it efficiently and independently. The reader can and is strongly encouraged to execute all the examples provided. Some chapters are closed with exercises to better assimilate the concepts covered as they are read.

Obviously, Python being a very vast language, these notes cannot and are not intended to be exhaustive of the use of this computer language.

0.2 Who are these notes for?

Initially, this book is intended for beginners who wish to learn the basics of Python. It is intended for AMSE students but may be of interest to individuals with an approach to data through the economic discipline wishing to discover Python.

I would like to thank Adrien Pacifico for his informative comments.

Chapter 1

Introduction

This document is mainly constructed using different references, including:

```
• books: Briggs (2013), Grus (2015), VanderPlas (2016), McKinney (2017);
```

• (excellents) notebooks: Navaro (2018).

1.1 Background information

Python is a multiplatform programming language, written in C, under a free license. It is an interpreted language, *i.e.*, it requires an interpreter to execute commands, and has no compilation phase. Its first public version dates from 1991. The main programmer, Guido van Rossum, had started working on this programming language in the late 1980s. The name given to the Python language comes from the interest of its main creator in a British television series broadcast on the BBC called "Monty Python's Flying Circus".

The popularity of Python has grown strongly in recent years, as confirmed by the survey results provided since 2011 by Stack Overflow. Stack Overflow offers its users the opportunity to complete a survey in which they are asked many questions to describe their experience as a developer. The results of the 2019 survey show a new breakthrough in the use of Python by developers. As shown in Figure 1.1 41.1% of respondents indicate that they develop in Python, *i.e.*, 2.3 percentage points higher than a year earlier.

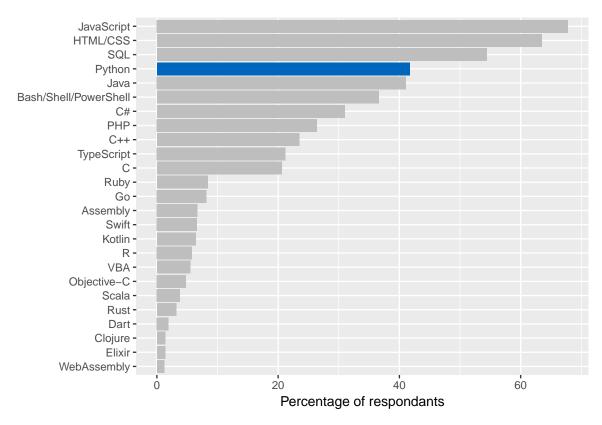


Figure 1.1: Programming, Scripting, and Markup Languages.

1.2. VERSIONS

1.2 Versions

These course notes are intended to provide an introduction to Python, version 3.x. In this sense, the examples provided will correspond to this version, not to the previous ones.

Compared to version 2.7, version 3.0 has made significant changes. It should be noted that Python 2.7 will take "its retirement" on January 1, 2020. After this date, support will no longer be provided.

1.3 Working space

There are many environments in which to program in Python. We will briefly present some of them.

It is assumed here that you have installed [Anaconda] (https://www.anaconda.com/) on your computer. Anaconda is a free and open source distribution of the Python and R programming languages for *data science* and machine learning applications. In addition, when the terminal is mentioned in the notes, it is assumed that the operating system of your machine is either Linux or Mac OS.

1.3.1 Python in a terminal

It is possible to call Python from a terminal, by executing the following command (under Windows: in the start menu, launch the "Python 3.6" software):

python

What can be seen on screen is reproduced in Figure 1.2:

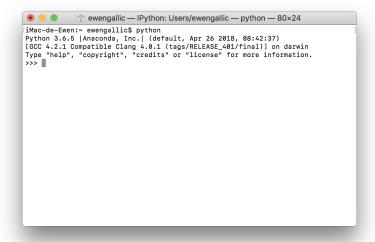


Figure 1.2: Python in a terminal.

We note the presence of the characters >>>> (prompt), which invite the user to enter a command. Expressions are evaluated once they are submitted (using the 'ENTEREE' key) and the result is given, when there is no error in the code.

The presence of the characters >>> (prompt), which invite the user to enter a command can be noticed. Expressions are evaluated once they are submitted (using the 'ENTER' key) and the result is given, when there is no error in the code.

For example, when evaluating 2+1:

```
>>> 2+1
3
>>>
```

The *prompt* at the end can be noted: this tells the user that Python is ready to receive new instructions.

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1.3.2 IPython

There is a slightly more friendly environment than Python in the terminal: IPython. It is also an interactive terminal, but with many more features, including syntax highlighting or auto-completion (using the tab key).

IPython can be opened using a terminal, using the following instruction:

ipython

IPython can also be launched from Anaconda's home window, by clicking on the Launch button of the qtconsole application, visible in the Figure 1.3.

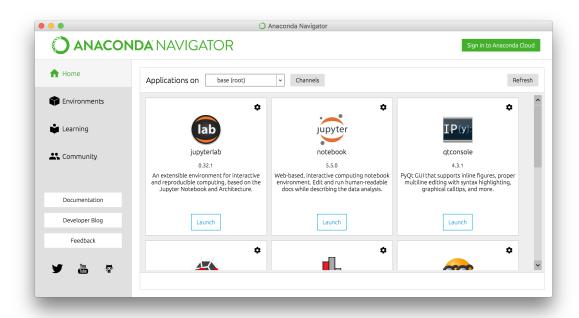


Figure 1.3: Anaconda's home window.

The IPython console, once launched, looks as follows:



Figure 1.4: IPython console.

Let's submit a simple instruction:

```
print("Hello World")
```

The results shows:

```
In [1]: print("Hello World")
Hello World
In [2]:
```

Several things should be noted. First, we note that at the end of the execution of the instruction, IPython indicates that it is ready to receive new instructions, by the presence of the *prompt* In[2]:. The number in brackets refers to the instruction number. We note that it went from 1 to 2 after the execution. We also note that the result of the call to the print() function, with the string of characters (delimited by quotation marks), displays on the screen what was contained between the parentheses.

1.3.3 Spyder

While when using Python in a terminal, it is recommended to have a text editor open next to it (to be able to save instructions), such as, for example, Sublime Text for Linux or Mac OS users, or notepad+++ for Windows.

Another alternative is to use a single integrated development environment (IDE) that includes both an editor and a console. This is what Spyder offers, with many additional features, such as project management, file explorer, command log, debugger, etc.

To launch Spyder, one can open a terminal and simply evaluate Spyder (it is also possible to launch the software using the Start Menu for Windows users). Spyder can also be launched via Anaconda.

The development environment, as shown in Figure 1.5, is divided into several windows:

- on the left: the script editor;
- at the top right: a window to display Python help, the system tree or the variables created;
- bottom right: one or more consoles.

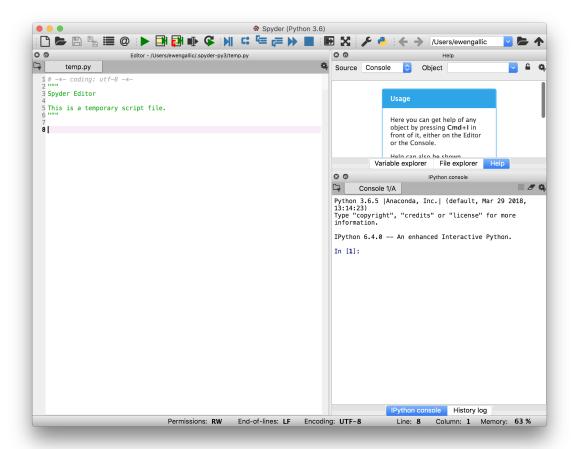


Figure 1.5: Spyder.

1.3.4 Jupyter Notebook

A graphical user interface in a web browser for IPython has gained has gained a strong popularity in the recent years: Jupyter Notebook. It is an open-source application for creating and sharing documents that contain code, equations, graphical representations and text. It is possible to include and execute different language codes in Jupyter notebooks.

Jupyter Notebook can be launched through Anaconda. After clicking on the Launch button of Jupyter Notebook in Anaconda, the default web browser launches and offers a tree structure, as depicted in Figure 1.6. Without realizing it, a local web

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server was launched as well as a Python process (a kernel).

If the browser does not launch automatically, the page that should have been displayed can be accessed at the following address: http://localhost:8890/tree?.

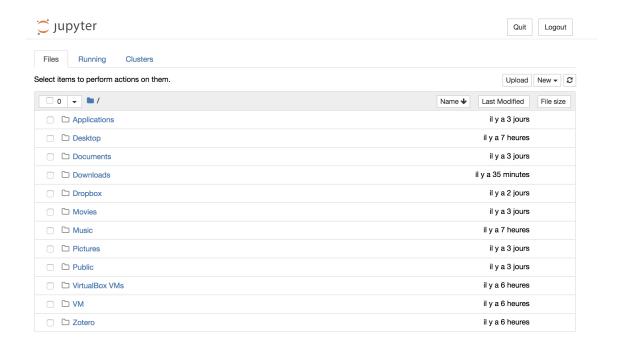


Figure 1.6: Jupyter Notebook.

To address the main functions of Jupyter, create a jupyter folder in a directory of our choice. Once this folder has been created, navigate through the Jupyter tree structure in the web browser.

Once in the folder, create a new Python 3 Notebook (by clicking on the New button at the top left of the window, then on Python 3).

A notebook named Untitled has just been created, the page displays an empty document, as shown in Figure 1.7.

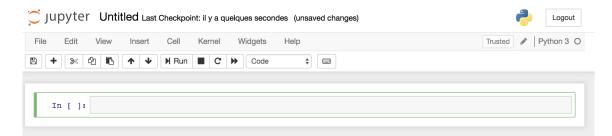


Figure 1.7: An Empty Notebook.

If we look in our file explorer, in the newly created jupyter folder, a new file has appeared: Untitled.ipynb.

1.3.4.1 Evaluation of an instruction

Let us go back to the web browser, to the page displaying your *notebook*.

Below the menu bar, we notice the presence of a framed area, a cell, that starts with IN []:, like what we saw in the console on IPython. On the right, the grey area invites us to submit instructions in Python.

Let us write the following instruction:

```
2+1
```

To submit the instruction for evaluation, there are several ways (make sure you have clicked inside the cell):

- in the menu bar: Cell > Run Cells;
- in the shortcut bar: button Run;
- with the keyboard: hold down the CTRL key and press Enter.

```
In [1]: 2+1
Out[1]: 3
```

Figure 1.8: Evaluated Cell.

1.3.4.2 Text cells

Among the advantages of *notebooks* over traditional scripts is the possibility to add text boxes to accompany the codes and the corresponding output after evaluation.

Let's add a cell below the first one. To do this, one can proceed either:

- using the menu bar: Insert > Insert Cell Below (to insert a cell below; if you want an insertion above, just choose Insert Cell Above);
- by clicking in the frame of the cell from which you want to add (anywhere except in the grayed out code area, so that you can switch to command' mode), then pressing the Bkey on the keyboard (A' for insertion above).

The new cell calls for a Python instruction to be entered. To indicate that the content should be interpreted as text, it is necessary to specify it. Again, there are several ways to do this:

- using the menu bar: Cell > Cell Type > Markdown;
- using the shortcut bar: in the drop-down menu where Code is written, by selecting Markdown;
- in command mode (after clicking inside the cell frame, but not in the code area), by pressing the M key on the keyboard.

The cell is then ready to receive text, written in markdown. For more information on writing in Markdown, you can refer to this [cheat sheet] (https://github.com/adam-p/markdown-here/wiki/Markdown-Cheatsheet).

Let's enter a few lines of text to see very briefly how the cells written in Markdown work.

```
# A Level 1 Title

I will write *text in italics* and also **in bold**.

## A Level 2 Title

I can write lists:

- with an item
- a second one
- and a third nesting a new list:
    - with a subitem
    - and a second one
```

```
- a fourth one including a numbered nested list:
    1. with a subitem
    1. and another.

## Another Level 2 Title

I can even put equations in $LaTeX$.
Like $X \sim \mathcal{N}(0.1)$.

To learn more about $\LaTeX$, we can refer to this:
    [Wikipedia page](https://en.wikibooks.org/wiki/LaTeX/Mathematics).
```

Which gives, in Jupyter:

Figure 1.9: Text cell not evaluated.

Then, the cell still has to be evaluated, as if it were a cell containing a Python instruction, to switch to a Markdown display (CTRL and ENTER).

To **edit the text** once we have switched to markdown, a simple double-click in the cell text box does the trick.

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To change the cell type so that it becomes code:

- using the menu bar: Cell > Cell Type > Code;
- using the shortcut bar: in the drop-down menu where Code is written, by selecting Code;
- in command mode, press the key on the Y keyboard.

1.3.4.3 Deleting a cell

To delete a cell:

- using the menu bar: Edit > Delete Cells
- using the shortcut bar: scissor icon
- in command mode, press the D keyboard key twice.

1.4 Variables

1.4.1 Assignment and deletion

When we evaluated the 2+1 instructions earlier, the result was displayed in the console, but it was not saved. In many cases, it is useful to keep the content of the result in an object, so that it can be reused later. To do this, *variables* are used. To create a variable, we use the equality sign (=), followed by what we want to save (text, a number, several numbers, etc.) and preceded by the name we will use to designate this variable.

For example, if we want to store the result of the calculation 2+1 in a variable that we will name x, we write:

```
x = 2+1
```

To display the value of our variable x, we can use the function print():

```
print(x)
```

3

To change the value of the variable, a new assignment can be made:

```
x = 4
print(x)
## 4
```

It is also possible to give more than one name to the same content (a copy of x is made):

```
x = 4;
y = x;
print(y)
## 4
```

If the copy is modified, the original will not be affected:

```
y = 0
print(y)
```

0

```
print(x)
```

4

A variable can be **deleted** with the instruction **del**:

```
del y
```

The display of the content of 'y' returns an error:

```
print(y)
```

```
## Error in py_call_impl(callable, dots$args, dots$keywords):
    NameError: name 'y' is not defined
##
## Detailed traceback:
```

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```
## File "<string>", line 1, in <module>
```

But we note that the variable x has not been deleted:

```
print(x)
## 4
```

1.4.2 Naming Conventions

The name of a variable can be composed of alphanumeric characters as well as the underscore (_) (there is no limit on the length of the name). It is forbidden to start the name of the variable with a number. It is also prohibited to include a space in the name of a variable.

To increase the readability of the variable names, several methods exist. We will adopt the following:

- all letters in lowercase;
- the separation of terms by an underscore (_).

For example, for a variable containing the value of a user's identifier: id user.

It should be noted that the variable names are case sensitive:

```
x = "toto"
print(x)
## toto
```

```
print(X)
```

```
## Error in py_call_impl(callable, dots$args, dots$keywords):
    NameError: name 'X' is not defined
##
## Detailed traceback:
## File "<string>", line 1, in <module>
```

1.5 Comments

There are several ways to add comments in python.

One way is to use the number sign (#) to make a **comment on a single line**. Everything that follows the number sign to the end of the line will not be evaluated by Python. On the other hand, what comes before the number sign will be.

```
# Un commentaire print("Bonjour")
print("Hello") # Un autre commentaire
## Hello
```

The introduction of a **block of comments** (comments on several lines) is done by surrounding what is to be commented with a delimiter: three single or double quotation marks:

```
A comment that starts on a line and continues on to another and stops at the third""
```

1.6 Modules and packages

Some basic functions in Python are loaded by default. Others require a **module** to be loaded. These modules are files that contain **definitions** as well as **instructions**.

Package are defined as a combination of modules that offer a set of functions.

Among the packages that will be used in these notes are:

- NumPy, a fundamental package for scientific calculations
- pandas, a package allowing easy data manipulation and analysis
- Matplotlib, a package allowing us to create graphics.

To load a module (or a *package*), we use the command **import**. For example, to load the *package* pandas:

import pandas

This allows us to use functions contained in the module or package. For example, here we can use the function Series(), contained in the *package* pandas, to create an array of data indexed to a dimension:

```
x = pandas.Series([1, 5, 4])
print(x)

## 0   1
## 1   5
```

2 4 ## dtype: int64

It is possible to give an alias to the module or package that is imported, by specifying it using the following syntax:

```
import module as alias
```

This is common practice to shorten the names of modules that will be used a lot. For example, for pandas, the name is usually shortened to pd:

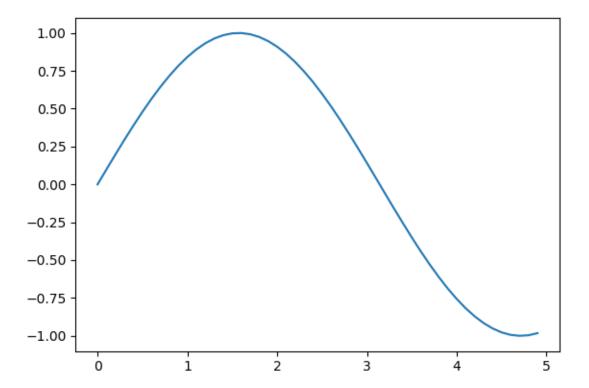
```
import pandas as pd
x = pd.Series([1, 5, 4])
print(x)

## 0    1
## 1    5
## 2    4
## dtype: int64
```

A single function can also be imported from a module, and an alias can be assigned to it (optionally). For example, with the pyplot() function of the package matplotlib, we usually do the following:

```
import matplotlib
import matplotlib.pyplot as plt
import numpy as np
x = np.arange(0, 5, 0.1);
```

```
y = np.sin(x)
plt.plot(x, y)
```



1.7 The Help System

To conclude this introduction, it seems important to mention the presence of **help** and **documentation** in Python.

For information on functions, it is possible to refer to the [online documentation] (https://docs.python.org/3/). It is also possible to get help inside the environment we are using, using the question mark (?).

For example, when using IPython (which, let's remember, is the case when working

with Jupyter Notebook), the help can be accessed using different syntaxes:

- ? : fournitprovides an introduction and an overview of the features offered in Python (you leave it with the ESC key for example)
- object? : provides details about object (for example x? or plt.plot?)
- object??: more details about object
- %quickref: short reference on Python syntaxes
- help(): access to the Python help system.

Note: the **tabulation** key on the keyboard allows not only **autocompletion**, but also an **exploration of the content** of an object or module.

In addition, when it comes to finding help on a more complex problem, the right thing to do is not hesitate to search on a search engine, in mailing lists and of course on the many questions on Stack Overflow.

Chapter 2

Types of Data

Many types of data are integrated into Python. In this section we will discuss strings, numerical values, booleans (TRUE/FALSE), the null value, dates and times.

2.1 Strings

A **string** is a collection of characters such as letters, numbers, spaces, punctuation marks, etc.

Strings are marked with single, double, or triple quotation marks.

Here is an example:

```
x = "Hello World"
```

To display the content of our variable x containing the string in the console, the function print() can be used:

```
print(x)
```

```
## Hello World
```

As indicated just before, single quotation marks can be used to create a string:

```
y = 'How are you?'
print(y)

## How are you?
```

To include apostrophes in a character string created using single quotation marks, one must use an escape character: a backslash (\):

```
z = 'I\'m fine'
print(z)

## I'm fine
```

Note that if the string is created using double quotation marks, it is not necessary to use the escape character:

```
z = "I'm \"fine\""
print(z)
## I'm "fine"
```

To specify a line break, we use the following string: \n.

```
x = "Hello, \nWorld"
print(x)

## Hello,
## World
```

In the case of character strings on **multiple lines**, using single or double quotation marks will return an error (*EOL while scanning trial literal*, *i.e.*, detection of a syntax error, Python was expecting something else at the end of the line). To write a string on several lines, Python suggests using quotation marks (single or double) at the beginning and end of the string three times:

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```
x = """Hello,
World"""
print(x)

## Hello,
## World
```

Remark 2.1.1

The character \ (backslash) is the escape character. It allows to display certain characters, such as quotation marks in a string defined by quotation marks, or control characters, such as tabulation, line breaks, etc. Here are some common examples:

Code	Description	Code	Description
\n	New line	\r	Line break
\t	Tabulation	\b	Backspace
\\	Backslash	\'	Quotation mark
\"	Double quotation mark	\`	Grave accent

To obtain the **length of a string**, Python offers the function len():

```
x = "Hello World !"
print(len(x))
```

```
## 13
```

```
print(x, len(x))
## Hello World ! 13
```

2.1.1 Concatenation of Strings

To concatenate strings, i.e., to put them end to end, Python offers to use the operator +:

```
print("Hello" + " World")
## Hello World
```

The * operator allows us to repeat a string several times:

```
print( 3 * "Go Habs Go! " + "Woo Hoo!")
## Go Habs Go! Go Habs Go! Woo Hoo!
```

When two literals of strings are side by side, Python concatenates them:

```
x = ('You shall ' 'not ' "pass!")
print(x)
```

```
## You shall not pass!
```

It is also possible to add the content of a variable to a string, using brackets ({}) and the method format():

```
x = "I like to code in {}"
langage_1 = "R"
langage_2 = "Python"
preference_1 = x.format(langage_1)
print(preference_1)
```

```
## I like to code in R
```

```
preference_2 = x.format(langage_2)
print(preference_2)
```

```
## I like to code in Python
```

It is possible to add more than one variable content in a string, always with brackets and the method format():

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```
x = "I like to code in {} and in {}"
preference_3 = x.format(langage_1, langage_2)
print(preference_3)
```

```
## I like to code in R and in Python
```

2.1.2 Indexing and Extraction

Strings can be indexed. Be careful, the index of the first character starts at 0.

To obtain the ith character of a string, brackets can be used. The syntax is as follows:

```
x[i-1]
```

For example, to display the first character, then the fifth of the Hello string:

```
x = "Hello"
print(x[0])
```

H

```
print(x[4])
```

0

The extraction can be done starting at the end of the chain, by preceding the value of the index with the minus sign (-).

For example, to display the penultimate character of our string \mathbf{x} :

```
print(x[-2])
```

1

The extraction of a substring by specifying its start and end position (implicitly or not) is also done with the brackets. We just need to specify the two index values: [start:end] as in the following example:

```
x = "You shall not pass!"

# From the fourth character (not included) to the ninth (included)
print(x[4:9])

## shall
```

When the first value is not specified, the beginning of the string is taken by default; when the second value is not specified, the end of the string is taken by default.

```
# From the 4th character (non included) to the end of the string
print(x[4:])
# From the beginning of the string to the penultimate (included)
print(x[:-1])
# From the 3rd character before the end (included) to the end
print(x[-5:])
## shall not pass!
## You shall not pass
```

It is possible to add a third argument in the brackets: the step.

```
# From the 4th character (not included),
# to the end of the string, in steps of 3
print(x[4::3])
```

sln s

To obtain the chain in the opposite direction:

2.1. STRINGS 43

```
print(x[::-1])
## !ssap ton llahs uoY
```

2.1.3 Available Methods with Strings

Many methods are available for strings. By adding a dot (.) after the name of an object designating a string and then pressing the tab key, the available methods are displayed in a drop-down menu.

For example, the count() method allows us to count the number of occurrences of a pattern in the string. To count the number of occurrences of in in the following string:

```
x = "le train de tes injures roule sur le rail de mon indifférence"
print(x.count("in"))
## 3
```

Remark 2.1.2

Once the method call has been written, by placing the cursor at the end of the line and pressing the Shift and Tabulation keys, explanations can be displayed.

2.1.3.1 Conversion to upper or lower case

The lower() and upper() methods allow us to pass a string in lowercase and uppercase characters, respectively.

```
x = "le train de tes injures roule sur le rail de mon indifférence"
print(x.lower())
print(x.upper())
```

```
## le train de tes injures roule sur le rail de mon indiffé
rence

## LE TRAIN DE TES INJURES ROULE SUR LE RAIL DE MON INDIFFÉ
RENCE
```

2.1.3.2 Seach Pattern for Strings

When we wish to find a pattern in a string, we can use the method find(). A pattern to be searched is provided in arguments. The find() method returns the smallest index in the string where the pattern is found. If the pattern is not found, the returned value is -1.

```
print(x.find("in"))
print(x.find("hello"))
## 6
```

It is possible to add as an option an indication allowing to **restrict the search on a substring**, by specifying the start and end index:

```
print(x.find("in", 7, 20))
## 16
```

Note: the end index can be omitted; in this case, the end of the string is used:

```
print(x.find("in", 20))
```

49

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Remark 2.1.3

If one does not want to know the position of the sub-chain, but only its presence or absence, one can use the operator in: print("train" in x)

To perform a search without regard to case, the method capitalize() can be used:

```
x = "Mademoiselle Deray, il est interdit de manger de la choucroute ici."
print(x.find("deray"))

## -1

print(x.capitalize().find("deray"))

## 13
```

2.1.3.3 Splitting Strings

To **split a string into substrings**, based on a pattern used to delimit the substrings (e.g., a comma or a space), the method **split()** can be used:

```
print(x.split(" "))

## ['Mademoiselle', 'Deray,', 'il', 'est', 'interdit', 'de', '
    manger', 'de', 'la', 'choucroute', 'ici.']
```

By indicating a numerical value as arguments, it is possible to limit the number of substrings returned:

The splitlines() method also allows us to separate a string of characters according to a pattern, this pattern being an end of line character, such as a line break or a carriage return for example.

```
x = '''"No, I am your Father!
- No... No. It's not true! That's impossible!
- Search your feelings. You know it to be true.
- Noooooooo! Noooo!"'''
print(x.splitlines())
```

```
## ['"No, I am your Father!', "- No... No. It's not true! That
's impossible!", '- Search your feelings. You know it to be
true.', '- Noooooooo! Noooo!"']
```

2.1.3.4 Cleaning, completion

To remove blank characters (e.g., spaces, line breaks, quadratins, etc.) at the beginning and end of a string, we can use the strip() method, which is sometimes very useful for cleaning strings.

```
x = "\n\n Pardon, du sucre ? \n \n"
print(x.strip())
```

```
## Pardon, du sucre ?
```

It is possible to specify in arguments which characters to remove at the beginning and end of the string:

```
x = "www.egallic.fr"
print(x.strip("wrf."))
## egallic
```

Sometimes we have to make sure to obtain a **string of a given length** (when we have to provide a file with fixed widths for each column for example). The rjust() method is then a great help. By entering a string length and a fill character, it returns

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the string with a possible completion (if the length of the returned string is not long enough with respect to the requested value), repeating the fill character as many times as necessary.

For example, to have a longitude coordinate stored in a string of characters of length 7, adding spaces may be necessary:

```
longitude = "48.11"
print(longitude.rjust(7," "))
## 48.11
```

2.1.3.5 Replacements

The replace() method allows to perform replacement of patterns in a character string:

```
x = "Criquette ! Vous, ici ? Dans votre propre salle de bain ? Quelle surprise !"
print(x.replace("Criquette", "Ridge"))

## Ridge ! Vous, ici ? Dans votre propre salle de bain ?
Quelle surprise !
```

This method is very convenient for **removing spaces** for example:

```
print(x.replace(" ", ""))

## Criquette! Vous, ici? Dansvotrepropresalledebain?
   Quellesurprise!
```

Here is a table listing some of the available methods ([exhaustive list in the documentation] (https://docs.python.org/3/library/stdtypes.html#string-methods)):

Method	Description
<pre>capitalize() casefold()</pre>	Capitalization of the first character and lowercase of the rest Removes case distinctions (useful for comparing strings without
	regard to case)

Method	Description
count()	Counts the number of occurrences (without overlap) of a pattern
encode()	Encodes a string of characters in a specific encoding
find()	Returns the smallest element where a substring is found
lower()	Returns the string having passed each alphabetical character in
	lower case
replace()	Replaces one pattern with another
split()	Separates the chain into substring according to a pattern
title()	Returns the string after passing each first letter of a word through a
	capital letter
upper()	Returns the string having passed each alphabetical character in
	upper case

2.1.4 Conversion to character strings

When we want to concatenate a string with a number, Python returns an error.

```
nb_followers = 0
message = "He has " + nb_followers + "followers."

## Error in py_call_impl(callable, dots$args, dots$keywords):
    TypeError: must be str, not int

##
## Detailed traceback:
## File "<string>", line 1, in <module>
```

print(message)

```
## Error in py_call_impl(callable, dots$args, dots$keywords):
   NameError: name 'message' is not defined
##
## Detailed traceback:
## File "<string>", line 1, in <module>
```

We should then convert the object that is not a string into a string beforehand. To do this, Python offers the function str():

```
message = "He has " + str(nb_followers) + " followers."
print(message)
```

```
## He has 0 followers.
```

2.1.5 Exercise

- 1. Create two variables named a and b so that they contain the following strings respectively: 23 to 0 and C'est la piquette, Jack!.
- 2. Display the number of characters from a, then b.
- 3. Concatenate a and b in a single string, adding a comma as a separating character.
- 4. Same question by choosing the separation line as the separator character.
- 5. Using the appropriate method, capitalize a and b.
- 6. Using the appropriate method, lowercase a and b.
- 7. Extract the word la and Jack from the string b, using indexes.
- 8. Look for the sub-chain piqu in b, then do the same with the sub-chain mauvais.
- 9. Return the position (index) of the first character a found in the string b, then try with the character w.
- 10. Replace the occurrences of the pattern a by the pattern Z in the substring b.
- 11. Separate the string b using the comma as a sub-chain separator.
- 12. (Bonus) Remove all punctuation characters from string b, then use an appropriate method to remove white characters at the beginning and end of the string. (Use the 'regex' library).

2.2 Numerical values

There are four categories of numbers in Python: integers, floating point numbers and complexes.

2.2.1 Integers

Integers (ints), in Python, are signed integers.

Remark 2.2.1

The type of an object is accessed using the type() function in Python.

```
x = 2
y = -2
print(type(x))

## <class 'int'>

print(type(y))

## <class 'int'>
```

2.2.2 Floating Point Numbers

Floats are real numbers. They are written using a dot to distinguish the integer part from the decimal part of the number.

```
x = 2.0
y = 48.15162342
print(type(x))

## <class 'float'>

print(type(y))

## <class 'float'>
```

Scientific notations can also be used, using E or e to indicate a power of 10. For example, to write 3.2^{12} :

```
x = 3.2E12
y = 3.2e12
print(x)
```

3200000000000.0

```
print(y)
```

```
## 3200000000000.0
```

In addition, when the number is equal to a fraction of 1, it is possible to avoid writing the zero:

```
print(0.35)
```

```
## 0.35
```

```
print(.35)
```

```
## 0.35
```

2.2.3 Complex numbers

Python allows us to natively manipulate complex numbers, of the form z = a + ib, where a and b are floating point numbers, and such that $i^2 = (-i)^2 = 1$. The real part of the number, $\Re(z)$, is a while its imaginary part, $\Im(z)$, is b.

In python, the imaginary unit i is denoted by the letter j.

```
z = 1+3j
print(z)
## (1+3j)
```

```
print(type(z))
```

```
## <class 'complex'>
```

It is also possible to use the complex() function, which requires two arguments (the real part and the imaginary part):

```
z = complex(1, 3)
print(z)
## (1+3j)
```

```
print(type(z))
## <class 'complex'>
```

Several methods are available with complex numbers. For example, to access the conjugate, Python provides the method conjugate():

```
print(z.conjugate())
## (1-3j)
```

Access to the real part of a complex or its imaginary part is done calling the real and imag elements, respectively.

```
z = complex(1, 3)
print(z.real)

## 1.0

print(z.imag)
```

3.0

2.2.4 Conversions

To convert a number to another digital format, Python has a few functions.

2.2.4.1 Conversion to Integer

The **conversion of an integer or string** is done using the function **int()**:

```
x = "3"
x_int = int(x)
print(type(x_int))

## <class 'int'>

print(type(x))

## <class 'str'>
```

Note that the conversion of a floating point number truncates the number to keep only the integer part:

```
x = 3.6
x_int = int(x)
print(x_int)
## 3
```

2.2.4.2 Conversion to Floating Point Number

To convert a number or string to a floating point number or string (if possible), Python suggests using the function float().

```
x = "3.6"
x_float = float(x)
print(type(x_float))
## <class 'float'>
```

With an integer:

```
x = 3
x_float = float(x)
print(x_float)
## 3.0
```

2.2.4.3 Conversion to Complex

The conversion of a number or a string of characters into a complex number is done with the function complex():

```
x = "2"
x_complex = complex(x)
print(x_complex)

## (2+0j)

With a float:
x = 2.4
x_complex = complex(x)
print(x_complex)

## (2.4+0j)
```

2.3 Booleans

Logical data can have two values: True or False. They correspond to a logical condition. Care must be taken to ensure that the case is well respected.

```
x = True
y = False
print(x, y)
```

```
## True False
```

True can be automatically converted to 1; False to 0. This can be very convenient, for example, when counting true or false values in the columns of a data table.

```
res = True + True + False + True*True
print(res)
## 3
```

2.4 Empty Object

The empty object, commonly called null, has an equivalent in Python: None. To assign it to a variable, one should be careful with case:

```
x = None
print(x)
## None
```

```
print(type(x))
## <class 'NoneType'>
```

The None object is a neutral variable, with "null" behavior.

To test if an object is the None object, we proceed as follows (the result is a Boolean):

```
x = 1
y = None
print(x is None)
```

```
## False
```

print(y is None)

True

2.5 Dates and Times

There are several modules to manage dates and time in Python. We will explore part of the datetime module.

2.5.1 Module Datetime

Python has a module called **datetime** which offers the possibility to manipulate dates and durations (*dates* and *times*).

There are several types of objects designating dates:

- date: a date according to the Gregorian calendar, indicating the year, month and day
- time: a given time, without taking into account a particular day, indicating the hour, minute, second (possibly the microsecond and time zone as well)
- datetime: a date combining date and time;
- timedelta: a time between two objects of the type dates, time or datetime;
- tzinfo: an abstract basic type, providing information about time zones;
- timezone: a type using the tzinfo type as a fixed offset from UTC.

2.5.1.1 Date

Objects of type date refer to dates in the Gregorian calendar, for which the following characteristics are mentioned: year, month and day.

To create a date object, the syntax is as follows:

```
date(year, month, day)
```

For example, to create the date of April 23, 2013:

```
from datetime import date
debut = date(year = 2013, month = 4, day = 23)
print(debut)

## 2013-04-23

print(type(debut))
```

<class 'datetime.date'>

Remark 2.5.1

It is not mandatory to specify the name of the arguments in the call to the date function. However, the order of priority should be as follows: year, month, day.

The attributes of the created date can then be accessed (they are integers):

```
print(debut.year) # Extract the year
```

2013

```
print(debut.month) # Extract the month
## 4
```

```
print(debut.day) # Extract the day
## 23
```

Some methods are available for objects of the type date. We will review some of them.

2.5.1.1.1 ctime()

The ctime() method returns the date as a string.

```
print(debut.ctime())
```

```
## Tue Apr 23 00:00:00 2013
```

2.5.1.1.2 weekday()

The weekday() method returns the position of the day of the week (Monday being 0, Sunday 6)

```
print(debut.weekday())
```

1

Remark 2.5.2

This method can be very handy when analyzing data to explore aspects of weekly seasonality.

2.5.1.1.3 isoweekday()

In the same vein as weekday(), the isoweekday() method returns the position of the day of the week, this time assigning the value 1 to Monday and 7 to Sunday.

```
print(debut.isoweekday())
```

2

2.5.1.1.4 toordinal()

The toordinal() method returns the day number, taking as a reference the value 1 for the first day of year 1.

print(debut.toordinal())

734981

2.5.1.1.5 isoformat()

The isoformat() method returns the date in ISO numbering, as a string.

```
print(debut.isoformat())
```

2013-04-23

2.5.1.1.6 isocalendar()

The isocalendar() method returns a nuplet (c.f. Section ??) with three elements: year, week number and day of week (all three in ISO numbering).

```
print(debut.isocalendar())
```

```
## (2013, 17, 2)
```

2.5.1.1.7 replace()

The replace() method returns the date after making a modification.

```
x = debut.replace(year=2014)
y = debut.replace(month=5)
z = debut.replace(day=24)
print(x, y, z)
```

```
## 2014-04-23 2013-05-23 2013-04-24
```

This has no impact on the original object:

print(debut)

```
## 2013-04-23
```

It is possible to modify several elements at the same time:

```
x = debut.replace(day=24, month=5)
print(x)
```

```
## 2013-05-24
```

2.5.1.1.8 strftime()

The strftime() method returns, as a string, a representation of the date, depending on a mask used.

For example, to have the date represented as DD-MM-YYYY (two-digit day, two-digit month and four-digit year):

```
print(debut.strftime("%d-%m-%Y"))
```

```
## 23-04-2013
```

In the previous example, two things are noteworthy: the presence of formatting instructions (which begin with the percentage symbol) and the presence of other characters (here, hyphens). It can be noted that characters can be replaced by others, this is a choice to represent the date by separating its elements with dashes. It is possible to adopt another type of writing, for example with slashes, or even other character strings:

```
print(debut.strftime("%d/%m/%Y"))
```

```
## 23/04/2013
```

```
print(debut.strftime("Jour : %d, Mois : %m, Annee : %Y"))
## Jour : 23, Mois : 04, Annee : 2013
```

As for the formatting guidelines, they correspond to the codes required by the C standard (c.f. the Python documentation). Here are some of them:

Table 2.3: Formatting codes

Code	Description	Example
%a	Abbreviation of the day of the week (depends on Tu	
	the location)	
%A	Full weekday (depends on location)	Tuesday
%b	Abbreviation of the month (depends on the Ap	
	location)	
%В	Name of the full month (depends on location)	April
%с	Date and time (depends on location) in format %a	Tue Apr 23
	%e %b %H:%M:%S:%Y	00:00:00 2013
%C	Century (00-99) (integer part of the year's division	20
	by 100)	
%d	Day of the month (01–31)	23
%D	Date in format $\%m/\%d/\%y$	04/23/13
%e	Day of the month in decimal number (1–31)	23
%F	Date in format %Y-%m-%d	2013-04-23
%h	Same as %b	Apr
%H	Hour (00–24)	00
%I	Hour (01–12)	12
%j	Day of the year (001–366)	113
%m	Month (01–12)	04
%M	Minute (00-59)	00
%n	Line break in output, white character in input	\n
%p	AM/PM PM	AM
%r	Hour in format 12 AM/PM	12:00:00 AM
%R	Same as %H:%M	00:00
%S	Second (00-61)	00
%t	Tabulation in output, white character in input	\t
%Т	Same as %H:%M:%S	00:00:00

Example	Description	Code
2	Day of the week (1–7), starts on Monday	
16	Week of the year (00–53), Sunday as the beginning	%U
	of the week, and the first Sunday of the year defines	
17	the week Week of the year (00.52). If the week (which begins	0/37
17	Week of the year (00-53). If the week (which begins on a Monday) that contains January 1 has four or	%V
	more days in the New Year, then it is considered	
	Week 1. Otherwise, it is considered as the last of	
	the previous year, and the following week is	
	considered as week 1 (ISO 8601 standard)	
2	Day of the week (0–6), Sunday being equal to 0	%w
16	Week of the year (00–53), Monday being the first	%W
	day of the week, and typically, the first Monday of	
	the year defines week 1 (U.K. convention)	
04/23/13	Date (depends on location)	%x
00:00:00'	Hour (depends on location)	%X
13	Year without the "century" (00–99)	%у
2013	Year (in input, only from 0 to 9999)	%Y
	Offset in hours and minutes with respect to UTC	%z
	time	
	Abbreviation of the time zone (output only) CEST	%Z

2.5.1.2 Time

Time objects refer to specific times without taking into account a particular day. They provide information on the hour, minute, second (possibly the microsecond and time zone as well).

To create a time object, the syntax is as follows:

```
time(hour, minute, second)
```

For example, to create the moment 23:04:59 (twenty-three hours, four minutes and fifty-nine seconds):

```
from datetime import time
moment = time(hour = 23, minute = 4, second = 59)
```

print(moment)

```
## 23:04:59
```

print(type(moment))

```
## <class 'datetime.time'>
```

We can add information about the microsecond. Its value must be between zero and one million.

```
moment = time(hour = 23, minute = 4, second = 59, microsecond = 230)
print(moment)
```

```
## 23:04:59.000230
```

print(type(moment))

```
## <class 'datetime.time'>
```

The attributes of the created date (they are integers) can then be accessed, including the following:

```
print(moment.hour) # Extract the hour
```

23

```
print(moment.minute) # Extract the minute
```

4

```
print(moment.second) # Extract the second
```

59

```
print(moment.microsecond) # Extract the microsecond
## 230
```

Some methods for time objects are available. Their use is similar to objects of the date class (refer to Section 2.5.1.1).

2.5.1.3 Datetime

The datetime objects combine the elements of the date and time objects. They provide the day in the Gregorian calendar as well as the hour, minute, second (possibly the microsecond and time zone).

To create a datetime object, the syntax is as follows:

```
datetime(year, month, day, hour, minute, second, microsecond)
```

For example, to create the date 23-04-2013 at 17:10:00:

```
from datetime import datetime
x = datetime(year = 2013, month = 4, day = 23,
  hour = 23, minute = 4, second = 59)
print(x)
```

```
## 2013-04-23 23:04:59
```

```
print(type(x))
```

```
## <class 'datetime.datetime'>
```

The datetime objects have the attributes of the date objects (c.f. Section 2.5.1.1) and time type (c.f. Section 2.5.1.2).

As for methods, relatively more are available. We will comment on some of them.

2.5.1.3.1 today() et now()

The today() and now() methods return the current datetime, the one at the time the instruction is evaluated:

```
print(x.today())
```

```
## 2019-10-08 17:53:08.259629
```

print(datetime.today())

```
## 2019-10-08 17:53:08.263955
```

The distinction between the two lies in the time zone. With today(), the attribute tzinfo is set to None, while with now(), the attribute tzinfo, if specified, is taken into account.

2.5.1.3.2 timestamp()

The timestamp() method returns, as a floating point number, the *timestamp* POSIX corresponding to the datetime object. The *timestamp* POSIX corresponds to the Posix time, equivalent to the number of seconds elapsed since January 1, 1970, at 00:00:00 UTC.

print(x.timestamp())

```
## 1366751099.0
```

2.5.1.3.3 date()

The date() method returns a date type object whose year, month and day attributes are identical to those of the object:

```
x_date = x.date()
print(x_date)
```

```
## 2013-04-23
```

```
print(type(x_date))
```

```
## <class 'datetime.date'>
```

2.5.1.3.4 time()

The time() method returns an object of type time whose hour, minute, second, microsecond attributes are identical to those of the object:

```
x_time = x.time()
print(x_time)
```

```
## 23:04:59
```

print(type(x_time))

```
## <class 'datetime.time'>
```

2.5.1.4 Timedelta

The objects of type timedelta represent times between two dates or times.

To create an object of type timedelta, the syntax is as follows:

```
timedelta(days, hours, minutes, seconds, microseconds)
```

It is not mandatory to provide a value for each argument. When an argument does not receive a value, its default value is 0.

For example, to create an object indicating a duration of 1 day and 30 seconds:

```
from datetime import timedelta
duree = timedelta(days = 1, seconds = 30)
duree
```

```
## datetime.timedelta(1, 30)
```

```
datetime.timedelta(1, 30)
```

The attributes (having been defined) can then be accessed. For example, to access the number of days represented by the duration:

```
duree.days
```

1

```
1
```

The total_seconds() method is used to obtain the duration expressed in seconds:

```
duree = timedelta(days = 1, seconds = 30, hours = 20)
duree.total_seconds()
158430.0
```

2.5.1.4.1 Time Between Two Objects date or datetime.

When subtracting two objects of type date, the number of days between these two dates is obtained, in the form of an object of type timedelta:

```
from datetime import timedelta
beginning = date(2018, 1, 1)
end = date(2018, 1, 2)
nb_days = end-beginning
print(type(nb_days))
```

```
## <class 'datetime.timedelta'>
```

```
print(nb_days)
```

```
## 1 day, 0:00:00
```

When subtracting two objects of type datetime, we obtain the number of days, seconds (and microseconds, if entered) separating these two dates, in the form of an object of type timedelta:

```
beginning = datetime(2018, 1, 1, 12, 26, 30, 230)
end = datetime(2018, 1, 2, 11, 14, 31)
duration = end-beginning
print(type(duration))
```

```
## <class 'datetime.timedelta'>
```

print(duration)

```
## 22:48:00.999770
```

It can be noted that the durations given take into account leap years. Let us first look at the number of days between February 28 and March 1 for a non-leap year:

```
beginning = date(2021, 2,28)
end = date(2021, 3, 1)
duration = end - beginning
duration
```

```
datetime.timedelta(1)
```

Now let's look at the same thing, but in the case of a leap year:

```
beginning_leap = date(2020, 2,28)
end_leap = date(2020, 3, 1)
beginning_leap = end_leap - beginning_leap
beginning_leap
```

```
datetime.timedelta(2)
```

It is also possible to add durations to a date:

```
debut = datetime(2018, 12, 31, 23, 59, 59)
print(debut + timedelta(seconds = 1))
```

```
## 2019-01-01 00:00:00
```

2.5.2 pytz Module

If date management is of particular importance, a library proposes to go a little further, especially with regard to time zone management. This library is called pytz. Many examples are available on[the project web page] (https://pypi.org/project/pytz/).

2.5.3 Exercices

- 1. Using the appropriate function, store the date of August 29, 2019 in an object called d then display the type of the object.
- 2. Using the appropriate function, display the current date.
- 3. Store the next date in an object named d2: "2019-08-29 20:30:56". Then, display in the console with the print() function the year, minute and second attributes of d2.
- 4. Add 2 days, 3 hours and 4 minutes to d2, and store the result in an object called d3.
- 5. Display the difference in seconds between d3 and d2.
- 6. From the object d2, display the date of d2 as a string so that it follows the following syntax: "Month Day, Year", with "Month" the name of the month (August), "Day" the two-digit day number (29) and "Year" the year of the date (2019).

Chapter 3

Structures

Python features several different basic integrated structures. In this section we will discuss some of them: lists, tuplets, sets and dictionaries.

3.1 Lists

One of the most flexible structures in Python is the list. It is a grouping of values. The creation of a list is done by writing the values by separating them with a comma and surrounding them by square brackets ([and]).

```
x = ["Pascaline", "Gauthier", "Xuan", "Jimmy"]
print(x)
## ['Pascaline', 'Gauthier', 'Xuan', 'Jimmy']
```

The content of a list is not necessarily text:

```
y = [1, 2, 3, 4, 5]
print(y)
## [1, 2, 3, 4, 5]
```

It is even possible to include elements of different types in a list:

```
z = ["Piketty", "Thomas", 1971]
print(z)
## ['Piketty', 'Thomas', 1971]
```

A list can contain another list:

```
tweets = ["aaa", "bbb"]
followers = ["Anne", "Bob", "Irma", "John"]
compte = [tweets, followers]
print(compte)
```

```
## [['aaa', 'bbb'], ['Anne', 'Bob', 'Irma', 'John']]
```

3.1.1 Extraction of the Elements

Access to the elements is made thanks to its indexation (be careful, the index of the first element is 0):

```
print(x[0]) # The first element of x

## Pascaline

print(x[1]) # The second element of x

## Gauthier
```

Access to an element can also be done by starting from the end, by putting the minus sign (-) in front of the index:

```
print(x[-1]) # The last element of x
## Jimmy
```

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```
print(x[-2]) # The penultimate element of x

## Xuan

Splitting a list so as to obtain a subset of the list is done with the colon (:):
print(x[1:2]) # The first and second elements of x

## ['Gauthier']

print(x[2:]) # From the second element (not included) to the end of x

## ['Xuan', 'Jimmy']

print(x[:-2]) # From the first to the penultimate (not included)

## ['Pascaline', 'Gauthier']
```

Remark 3.1.1

The extraction from a list using the brackets returns a list.

When extracting items from the list using the brackets, it is possible to add a third argument, the step:

```
print(x[::2]) # Every other element
## ['Pascaline', 'Xuan']
```

Access to nested lists is done by using the brackets several times:

```
tweets = ["aaa", "bbb"]
followers = ["Anne", "Bob", "Irma", "John"]
conuts = [tweets, followers]
res = conuts[1][3] # The 4th item of the 2nd item on the list counts
```

The number of elements in a list is obtained with the function len():

```
print(len(conuts))
## 2

print(len(conuts[1]))
## 4
```

3.1.2 Modification

Lists are mutable, *i.e.*, their content can be modified once the object has been created.

3.1.2.1 Replacement

To **modify** an element in a list, the indexes can be used:

```
x = [1, 3, 5, 6, 9]
x[3] = 7 # Replacing the 4th element
print(x)
## [1, 3, 5, 7, 9]
```

3.1.2.2 Adding Elements

To add items to a list, the method append() can be used:

```
x.append(11) # Add value 11 at the end of the list
print(x)
```

```
## [1, 3, 5, 7, 9, 11]
```

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It is also possible to use the extend() method, to concatenate lists:

```
y = [13, 15]
x.extend(y)
print(x)
```

```
## [1, 3, 5, 7, 9, 11, 13, 15]
```

3.1.2.3 Deleting Elements

To removing an item from a list, the method remove() can be used:

```
x.remove(3) # Remove the fourth element
print(x)
```

```
## [1, 5, 7, 9, 11, 13, 15]
```

The del command can also be used:

```
x = [1, 3, 5, 6, 9]
del x[3] # Remove the fourth element
print(x)
```

```
## [1, 3, 5, 9]
```

3.1.2.4 Multiple assignments

Several values can be modified at the same time:

```
x = [1, 3, 5, 6, 10]
x[3:5] = [7, 9] # Replaces 4th and 5th values
print(x)
```

```
## [1, 3, 5, 7, 9]
```

The modification can increase the size of the list:

```
x = [1, 2, 3, 4, 5]
x[2:3] = ['a', 'b', 'c', 'd'] # Replaces the 3rd value
print(x)
```

```
## [1, 2, 'a', 'b', 'c', 'd', 4, 5]
```

Several values can be deleted at the same time:

```
x = [1, 2, 3, 4, 5]
x[3:5] = [] # Removes the 4th and 5th values
print(x)
```

```
## [1, 2, 3]
```

3.1.3 Verifying if a Value is Present

By using the operator in, it is possible to test the belonging of an object to a list:

```
x = [1, 2, 3, 4, 5]
print(1 in x)
## True
```

3.1.4 Copy of List

Be careful, copying a list is not trivial in Python. Let's take an example.

```
x = [1, 2, 3]

y = x
```

Let's modify the first element of y, and look at the content of y and x:

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```
y[0] = 0
print(y)

## [0, 2, 3]

print(x)

## [0, 2, 3]
```

As can be seen, using the equal sign simply created a reference and not a copy.

To copy a list, there are several ways to do so. Among them, the use of the list() function:

```
x = [1, 2, 3]
y = list(x)
y[0] = 0
print("x : ", x)

## x : [1, 2, 3]
print("y : ", y)
```

It can be noted that when a splitting is done, a new object is created, not a reference:

```
x = [1, 2, 3, 4]
y = x[:2]
y[0] = 0
print("x : ", x)
```

```
## x : [1, 2, 3, 4]
```

y : [0, 2, 3]

```
print("y : ", y)
## y : [0, 2]
```

3.1.5 Sorting

To sort the objects in the list (without creating a new one), Python offers the method sort():

```
x = [2, 1, 4, 3]
x.sort()
print(x)
```

```
## [1, 2, 3, 4]
```

It also works with text values, sorting in alphabetical order:

```
x = ["c", "b", "a", "a"]
x.sort()
print(x)
## ['a', 'a', 'b', 'c']
```

It is possible to provide the **sort()** method with arguments. Among these arguments, there is one, **key**, which provides a function for sorting. This function must return a value for each object in the list, on which the sorting will be performed. For example, with the **len()** function, which, when applied to text, returns the number of characters:

```
x = ["aa", "a", "aaaaa", "aa"]
x.sort(key=len)
print(x)
```

```
## ['a', 'aa', 'aa', 'aaaaa']
```

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3.2 Tuples

The tuples are sequences of Python objects.

To create a tuple, one lists the values, separated by commas:

```
x = 1, 4, 9, 16, 25
print(x)
## (1, 4, 9, 16, 25)
```

It should be noted that tuplets are identified by a series of values, surrounded in two brackets.

3.2.1 Extraction of the Elements

The elements of a tuple are extracted in the same way as those in the lists (see Section 3.1.1).

```
print(x[0])
## 1
```

3.2.2 Modification

Unlike lists, tuplets are **inalterable** (i.e. cannot be modified after they have been created):

```
x[0] = 1

## Error in py_call_impl(callable, dots$args, dots$keywords):
    TypeError: 'tuple' object does not support item assignment

##

## Detailed traceback:
## File "<string>", line 1, in <module>
```

It is possible to **nest tuplets** inside another tuple. To do this, parentheses are used:

```
x = ((1, 4, 9, 16), (1, 8, 26, 64))
print(x)
```

```
## ((1, 4, 9, 16), (1, 8, 26, 64))
```

3.3 Sets

Sets are unordered collections of unique elements. The sets are unalterable, not indexed.

To create a set, Python provides the **set()** function. One or more elements constituting the set are provided, separated by commas and surrounded by braces ({}):

Equivalently, rather than using the set() function, the set can only be defined using the brackets:

```
new_set = {"Marseille", "Aix-en-Provence", "Nice", "Rennes"}
print(new_set)

## {'Nice', 'Aix-en-Provence', 'Marseille', 'Rennes'}
```

On the other hand, if the set is empty, Python returns an error if the set() function is not used: il est nécessaire d'utiliser la fonction set:

```
empty_set = {}
type(empty_set)
```

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```
## <class 'dict'>
```

The type of the object we have just created is not set but dict (i.e. Section 3.4). Also, to create the empty set, we use set():

```
empty_set = set()
print(type(empty_set))
## <class 'set'>
```

During the creation of a set, if there are duplicates in the values provided, these will be deleted to keep only one value:

```
new_set = set({"Marseille", "Aix-en-Provence", "Nice", "Marseille", "Rennes"})
print(new_set)
## {'Nice', 'Aix-en-Provence', 'Marseille', 'Rennes'}
```

The length of a set is obtained using the len() function:

```
print(len(new_set))
```

4

3.3.1 Modifications

3.3.1.1 Adding Elements

To add an element to a set, Python offers the add() method:

```
new_set.add("Toulon")
print(new_set)

## {'Toulon', 'Rennes', 'Aix-en-Provence', 'Nice', 'Marseille
```

If the element is already present, it will not be added:

```
new_set.add("Toulon")
print(new_set)

## {'Toulon', 'Rennes', 'Aix-en-Provence', 'Nice', 'Marseille
    '}
```

3.3.1.2 Deletion

To remove a value from a set, Python offers the method remove():

```
new_set.remove("Toulon")
print(new_set)
## {'Rennes', 'Aix-en-Provence', 'Nice', 'Marseille'}
```

If the value is not present in the set, Python returns an error message:

```
new_set.remove("Toulon")

## Error in py_call_impl(callable, dots$args, dots$keywords):
    KeyError: 'Toulon'

##

## Detailed traceback:
## File "<string>", line 1, in <module>

print(new_set)

## {'Rennes', 'Aix-en-Provence', 'Nice', 'Marseille'}
```

3.3.2 Belonging test

One of the advantages of sets is the quick search for presence or absence of values (faster than in a list). As with the lists, the belonging tests are performed using the

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operator in:

```
print("Marseille" in new_set)

## True

print("Paris" in new_set)

## False
```

3.3.3 Copying a Set

To copy a set, as for lists (c.f. Section ??), the equality sign should not be used. Copying a set is done using the copy() method:

```
new_set = set({"Marseille", "Aix-en-Provence", "Nice"})
y = new_set.copy()
y.add("Toulon")
print("y : ", y)

## y : {'Nice', 'Toulon', 'Aix-en-Provence', 'Marseille'}

print("set : ", new_set)

## set : {'Nice', 'Aix-en-Provence', 'Marseille'}
```

3.3.4 Conversion to a List

One of the interests of sets is that they contain unique elements. Also, when you want to obtain the distinct elements of a list, it is possible to convert it into a set (with the set() function), then to convert the set into a list (with the list() function):

```
my_list = ["Marseille", "Aix-en-Provence", "Marseille", "Marseille"]
print(my_list)

## ['Marseille', 'Aix-en-Provence', 'Marseille', 'Marseille']

my_set = set(my_list)
print(my_set)

## {'Aix-en-Provence', 'Marseille'}

my_new_list = list(my_set)
print(my_new_list)

## ['Aix-en-Provence', 'Marseille']
```

3.4 Dictionaries

Python dictionaries are an implementation of key-value objects, the keys being indexed.

Keys are often text, values can be of different types and structures.

To create a dictionary, you can proceed by using braces ({}). As encountered in the Section 3.3, if we evaluate the following code, we get a dictionary:

```
empty_dict = {}
print(type(empty_dict))

## <class 'dict'>
```

To create a dictionary with entries, the braces can be used. Each entry is separated by commas, and the key is distinguished from the associated value by two points (:):

```
my_dict = { "nom": "Kyrie",
    "prenom": "John",
    "naissance": 1992,
    "equipes": ["Cleveland", "Boston"]}
print(my_dict)

## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
    equipes': ['Cleveland', 'Boston']}
```

It is also possible to create a dictionary using the dict() function, by providing a sequence of key-values:

```
x = dict([("Julien-Yacine", "Data-scientist"),
   ("Sonia", "Director")])
print(x)
```

```
## {'Julien-Yacine': 'Data-scientist', 'Sonia': 'Director'}
```

3.4.1 Extraction of the Elements

Extraction from dictionaries is based on the same principle as for lists and tuples (see Section @ref(#structure-liste-extraction)). However, the extraction of an element from a dictionary is not based on its position in the dictionary, but by its key:

```
print(my_dict["prenom"])
## John
```

```
print(my_dict["equipes"])
## ['Cleveland', 'Boston']
```

If the extraction is done by a key not present in the dictionary, an error will be returned:

```
print(my_dict["age"])

## Error in py_call_impl(callable, dots$args, dots$keywords):
    KeyError: 'age'

##

## Detailed traceback:
## File "<string>", line 1, in <module>
```

You can test the presence of a key with the operator in:

```
print("prenom" in my_dict)

## True

print("age" in my_dict)

## False
```

The extraction of values can also be done using the get() method, which returns a None value if the key is not present:

```
print(my_dict.get("prenom"))

## John

print(my_dict.get("age"))

## None
```

3.4.2 Keys and values

Using the key() method, the keys of the dictionary can be accessed:

print(the items)

```
the_keys = my_dict.keys()
print(the keys)
## dict_keys(['nom', 'prenom', 'naissance', 'equipes'])
print(type(the_keys))
## <class 'dict_keys'>
It is then possible to transform this key enumeration into a list:
the keys list = list(the keys)
print(the_keys_list)
## ['nom', 'prenom', 'naissance', 'equipes']
The values() method provides the dictionary values:
the_values = my_dict.values()
print(the_values)
## dict_values(['Kyrie', 'John', 1992, ['Cleveland', 'Boston
    ']])
print(type(the_values))
## <class 'dict_values'>
The items() method provides keys and values in the form of tuples:
the items = my dict.items()
```

dict_items([('nom', 'Kyrie'), ('prenom', 'John'), ('

naissance', 1992), ('equipes', ['Cleveland', 'Boston'])])

```
print(type(the_items))
## <class 'dict_items'>
```

3.4.3 Search for Belonging

Thanks to the methods keys(), values() and items(), it is easy to search for the presence of objects in a dictionary.

```
print("age" in the_keys)
## False

print("nom" in the_keys)
## True

print(['Cleveland', 'Boston'] in the_values)
## True
```

3.4.4 Modification

3.4.4.1 Replacement

To replace the value associated with a key, the brackets ([]) and the equality sign (=) can be used.

For example, to replace the values associated with the team key:

```
## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
    equipes': ['Montclair Kimberley Academy', 'Cleveland
    Cavaliers', 'Boston Celtics']}
```

3.4.4.2 Adding Elements

Adding an element to a dictionary can be done with brackets ([]) and the equality sign (=):

```
my_dict["taille_cm"] = 191
print(my_dict)

## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
    equipes': ['Montclair Kimberley Academy', 'Cleveland
    Cavaliers', 'Boston Celtics'], 'taille_cm': 191}
```

To add the content of another dictionary to a dictionary, Python offers the update() method.

Let's create a second dictionary first:

```
second_dict = {"masse_kg" : 88, "debut_nba" : 2011}
print(second_dict)

## {'masse_kg': 88, 'debut_nba': 2011}
```

Let's add the content of this second dictionary to the first:

```
my_dict.update(second_dict)
print(my_dict)
```

```
## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
    equipes': ['Montclair Kimberley Academy', 'Cleveland
    Cavaliers', 'Boston Celtics'], 'taille_cm': 191, 'masse_kg
    ': 88, 'debut_nba': 2011}
```

If the second dictionary is subsequently modified, it will not affect the first:

```
second_dict["poste"] = "PG"
print(second_dict)
```

```
## {'masse_kg': 88, 'debut_nba': 2011, 'poste': 'PG'}
```

```
print(my dict)
```

```
## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
    equipes': ['Montclair Kimberley Academy', 'Cleveland
    Cavaliers', 'Boston Celtics'], 'taille_cm': 191, 'masse_kg
    ': 88, 'debut_nba': 2011}
```

3.4.4.3 Deleting elements

There are several ways to delete an element in a dictionary. For example, with the operator del:

```
del my_dict["debut_nba"]
print(my_dict)
```

```
## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
    equipes': ['Montclair Kimberley Academy', 'Cleveland
    Cavaliers', 'Boston Celtics'], 'taille_cm': 191, 'masse_kg
    ': 88}
```

It is also possible to use the pop() method:

```
res = my_dict.pop("masse_kg")
print(my_dict)
```

```
## {'nom': 'Kyrie', 'prenom': 'John', 'naissance': 1992, '
equipes': ['Montclair Kimberley Academy', 'Cleveland
Cavaliers', 'Boston Celtics'], 'taille_cm': 191}
```

In the previous instruction, we added an assignment of the result of applying the pop() method to a variable named res. As can be seen, the pop() method, in addition to deleting the key, returned the associated value:

```
print(res)
```

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3.4.5 Copy of a Dictionary

To copy a dictionary, and not create a reference (which is the case if you use the equality sign), Python provides, as for sets, a copy() method:

```
d = {"Marseille": 13, "Rennes" : 35}
d2 = d.copy()
d2["Paris"] = 75
print("d: ", d)

## d: {'Marseille': 13, 'Rennes': 35}

print("d2: ", d2)

## d2: {'Marseille': 13, 'Rennes': 35, 'Paris': 75}
```

3.4.6 Exercise

- 1. Create a dictionary named photo, including the following key-value pairs:
 - 1. key: id, value: 1,
 - 2. key: description, value: A photo of the Old Port of Marseille,
 - 3. key: loc, value: a list in which the following coordinates are given 5.3772133, 43.302424.

- 2. add the following key-value pair to the photo dictionary: key: user, value: bob.
- 3. Look for an entry with a key that is worth description in the photo dictionary. If this is the case, display the corresponding entry (key and value).
- 4. Delete the entry in photo whose key is user.
- 5. Modify the value of the entry loc in the photo dictionary, to propose a new list, whose coordinates are as follows: 5.3692712 and 43.2949627.

Chapter 4

Operators

Python includes different operators, allowing operations to be performed between operands, *i.e.*, between variables, literals or expressions.

4.1 Arithmetic Operators

The basic arithmetic operators are integrated in Python.

We have already used some of them in the previous chapters to perform operations on integers or floating point numbers (addition, subtraction, etc.). Let's take a quick look at the most common arithmetic operators used to perform operations on numbers.

4.1.1 Addition

An addition between two numbers is made using the + symbol:

```
print(1+1) # Addition
```

2

4.1.2 Subtraction

A subtraction between two numbers is performed using the - symbol:

```
print(1-1) # Subtraction
## 0
```

4.1.3 Multiplication

A multiplication between two numbers is performed using the * symbol:

```
print(2*2) # Multiplication
## 4
```

4.1.4 Division

A (real) division between two numbers is made using the symbol /:

```
print(3/2) # Division
## 1.5
```

To perform a Euclidean division (or division with remainder), slash is doubled:

```
print(3//2) # Euclidean division
```

```
## 1
```

4.1.5 Modulo

The modulo (remainder of the Euclidean division) is obtained using the symbol %:

```
print(12%10) # Modulo
## 2
```

4.1.6 Power

To raise a number to a given power, we use two stars (**):

```
print(2**3) # 2^3
## 8
```

4.1.7 Order

The order of operations follows the PEMDAS rule (Parentheses, Exponents, Multiplication and Division, Adition and Subtraction).

For example, the following instruction first performs the calculation 2×2 , then adds 1:

```
print(2*2+1)
## 5
```

The following instruction, using brackets, first calculates 2 + 1, then multiplies the result with 2:

```
print(2*(2+1))
## 6
```

4.1.8 Mathematical Operators on Strings

Some mathematical operators presented in Section 4.1 can be applied to strings.

When using the symbol + between two strings, Python concatenates these two strings (see Section 2.1.1):

```
a = "euro"
b = "dollar"
print(a+b)
## eurodollar
```

When a string is "multiplied" by a scalar n, Python repeats this string n times:

```
2*a
## 'euroeuro'
```

4.1.9 Mathematical Operators on Lists or tuples

Some mathematical operators can also be applied to lists.

When using the symbol + between two lists, Python concatenates them into one:

```
l_1 = [1, "apple", 5, 7]
l_2 = [9, 11]
print(l_1 + l_2)
## [1, 'apple', 5, 7, 9, 11]
```

Same with tuples:

```
t_1 = (1, "apple", 5, 7)
t_2 = (9, 11)
print(t_1 + t_2)
```

```
## (1, 'apple', 5, 7, 9, 11)
```

By "multiplying" a list by a scalar n, Python repeats this list n times:

```
print(3*l_1)
```

```
## [1, 'apple', 5, 7, 1, 'apple', 5, 7, 1, 'apple', 5, 7]
```

Same with tuples:

```
print(3*t_1)
## (1, 'apple', 5, 7, 1, 'apple', 5, 7, 1, 'apple', 5, 7)
```

4.2 Comparison Operators

Comparison operators allow objects of all basic types to be compared with each other. The result of a comparison test produces Boolean values.

Table 4.1: Comparison operators

Operator	Python Operator	Description
=	==	Equal to
\neq	!= (or <>)	Different from
>	>	Greater than
\geq	>=	& Greater than or equal to
<	<	Lower than
\leq	<=	Less than or equal to
\in	in	In
∉	not in	Not it

True

4.2.1 Equality, Inequality

To test the content equality between two objects:

```
a = "Hello"
b = "World"
c = "World"

print(a == c)

## False

print(b == c)

## True

The inequality between two objects:

x = [1,2,3]
y = [1,2,3]
z = [1,3,4]

print(x != y)

## False

print(x != z)
```

4.2.2 Inferiority and Superiority, Strict or Broad

To know if an object is inferior (strictly or not) or inferior (strictly or not) to another:

```
x = 1
y = 1
z = 2
print(x < y)</pre>
## False
print(x <= y)</pre>
## True
print(x > z)
## False
print(x \ge z)
## False
It is also possible to compare two strings. The comparison is carried out according to
the lexicographical order:
m_1 = "eat"
m_2 = "eating"
m_3 = "drinking"
```

```
## True

print(m_3 > m_1) # drinking after eat?

## False
```

print(m_1 < m_2) # eat before eating?</pre>

When comparing two lists together, Python works step by step. Let's look through an example to see how this comparison is done.

Let's create two lists:

```
x = [1, 3, 5, 7]

y = [9, 11]
```

Python will start by comparing the first elements of each list (here, it is possible, the two elements are comparable; otherwise, an error would be returned):

```
print(x < y)
## True</pre>
```

As 1<9, Python returns True.

Let's change x so that the first element is greater than the first element of y.

```
x = [10, 3, 5, 7]
y = [9, 11]
print(x < y)
## False</pre>
```

This time, as \$10>\$9, Python returns False.

Now let's change the first element of x so that it is equal to y:

```
x = [10, 3, 5, 7]
y = [10, 11]
print(x < y)</pre>
```

```
## True
```

This time, Python compares the first element of \mathbf{x} with that of \mathbf{y} . As the two are identical, the second elements are compared. This can be demonstrated by evaluating the following code:

False

```
x = [10, 12, 5, 7]
y = [10, 11]
print(x < y)</pre>
```

4.2.3 Inclusion and exclusion

As encountered several times in Chapter 3, the inclusion tests are performed using the operator in.

```
the operator in.
print(3 in [1,2, 3])

## True

To test if an item is excluded from a list, tuple, dictionary, etc., we use not in:
print(4 not in [1,2, 3])

## True

print(4 not in [1,2, 3, 4])

## False

With a dictionary:
dictionnaire = {"nom": "Rockwell", "prenom": "Criquette"}
```

"age" not in dictionnaire.keys()

True

4.3 Logical operators

Logical operators operate on one or more logical objects (Boolean).

4.3.1 And logical

The and operator allows logical "AND" comparisons to be made. We compare two objects, x and y (these objects can result from a previous comparison, for this both only need to be Boolean).

If one of the two objects x and y is true, the logical "AND" comparison returns true:

```
x = True
y = True
print(x and y)
## True
```

If at least one of them is false, the logical "AND" comparison returns false:

```
x = True
y = False
print(x and y)
## False

print(y and y)
## False
```

If one of the two compared objects is equal to the empty value (None), then the logical "AND" comparison returns :

- the value None if the other object is worth True or None
- the value False if the other object is worth False.

```
x = True
y = False
z = None
print(x and z)

## None

print(y and z)

## False

print(z and z)

## None
```

4.3.2 Logical OR

The operator or allows logical "OR" comparisons to be made. Again, we compare two Booleans, x and y.

If at least one of the two objects ${\tt x}$ and ${\tt y}$ is true, the logical "OR" comparison returns true:

```
x = True
y = False
print(x or y)
## True
```

If both are false, the logical "OR" comparison returns false:

```
x = False
y = False
print(x or y)
```

```
## False
```

If one of the two objects is None, the logical "OR" comparison returns :

- True if the other object is worth True
- None if the other object is worth False or None.

```
x = True
y = False
z = None
print(x or z)

## True

print(y or z)

## None

## None
```

4.3.3 Logical Not

The operator not, when applied to a Boolean, evaluates the latter at its opposite value:

```
x = True
y = False
print(not x)
## False
```

```
print(not y)
## True
```

When using the operator not on an empty value (None), Python returns True:

```
x = None
not x
## True
```

4.4 Some Functions

Python has many useful functions for manipulating structures and data. Table 4.2 lists some of them. Some require the loading of the math library, others require the statistics library. We will see other functions specific to the NumPy library in Chapter 9.

Table 4.2: Some numerical functions

Function	Description
math.ceil(x)	Smallest integer greater than or equal to x
<pre>math.copysign(x,</pre>	Absolute value of x but with the sign of y
у)	
math.floor(x)	Smallest integer less than or equal to x
math.round(x,	Rounded from x to ndigits decimal places
ndigits)	
math.fabs(x)	Absolute value of x
math.exp(x)	Exponential of x
math.log(x)	Natural logarithm of x (based on e)
<pre>math.log(x, b)</pre>	Logarithm based on ${\tt b}$ of ${\tt x}$
math.log10(x)	Logarithm in base 10 of x
math.pow(x,y)	x high to the power y
math.sqrt(x)	Square root of x
<pre>math.fsum()</pre>	Sum of the values of x

Function	Description
math.sin(x)	Sine of x
$\mathtt{math.cos}(\mathtt{x})$	Cosine of x
math.tan(x)	Tangent of x
math.asin(x)	Arc-sineus of x
math.acos(x)	Arc-cosinus of x
math.atan(x)	Arc-tangent of x
math.sinh(x)	Hyperbolic sine of x
math.cosh(x)	Hyperbolic cosine of x
math.tanh(x)	Hyperbolic tangent of x
<pre>math.asinh(x)</pre>	Hyperbolic arc-sine of ${\tt x}$
math.acosh(x)	Hyperbolic arc-cosine of ${\tt x}$
math.atanh(x)	Hyperbolic arc-tangent of ${\tt x}$
math.degree(x)	Conversion of radians \mathbf{x} to degrees
math.radians(x)	Conversion of \mathbf{x} from degrees to radians
<pre>math.factorial()</pre>	Factory of x
<pre>math.gcd(x, y)</pre>	Largest common divisor of \mathbf{x} and \mathbf{y}
<pre>math.isclose(x, y,</pre>	Compare x and y and returns if they are close to the
rel_tol=1e-09,	tolerance level rel_tol (abs_tol is the absolute
abs_tol=0.0)	minimum tolerance)
<pre>math.isfinite(x)</pre>	Returns True if x is either infinite, or NaN
<pre>math.isinf(x)</pre>	Returns $True$ if x is infinite, $False$ otherwise
<pre>math.isnan(x)</pre>	Returns True if x is NaN, False if not
<pre>statistics.mean(x)</pre>	Average of x
statistics.median(x)	Median of x
statistics.mode(x)	Mode of x
statistics.stdev(x)	Standard deviation of x
<pre>statistics.variance(x)</pre>	Variance of x

4.5 Some Constants

The \mathtt{math} library offers some constants, as shown in Table 4.3.

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Table 4.3: Some constants integrated in Python

Function	Description
'math.pi	The number Pi (π)
math.e	The constant e
$\mathtt{math.tau}$	The constant τ , equal to 2π
${\tt math.inf}$	The infinite (∞)
-math.inf	Minus infinity $(-\infty)$
${\tt math.nan}$	Floating point number $not\ to\ number$

4.6 Exercise

- 1. Calculate the remainder of the Euclidean division of 10 by 3.
- 2. Display the largest common divisor between 6209 and 4435.
- 3. Let us consider two objects: a = 18 and b = -4. Test it if:
- a is strictly less than b,
- a is greater than or equal to b,
- a is different from b.
- 4. Let x be the list such as x = [1, 1, 1, 2, 3, 5, 8]. Check whether:
- 1 is in x;
- 0 is in x;
- 1 and 0 are in x;
- 1 or 0 are in x;
- 1 or 0 is not present in x.

Chapter 5

Loading and Saving Data

To explore data and/or perform statistical or econometric analyses, it is important to know how to import and export data.

First of all, it is important to mention the notion of a working directory. In computer science, the current directory of a process refers to a directory of the file system associated with that process.

When we launch Jupyter Notebook, a tree structure is displayed, and we navigate inside it to create or open a *notebook*. The directory containing the *notebook* is the current directory. When Python is told to import data (or export objects), the origin (or destination) will be indicated **relatively** in the current directory, unless absolute paths (*i.e.*, a path from the root /) are used.

If a Python program is started from a terminal, the current directory is the directory in which the terminal is located at the time the program is started.

To display the current directory in Python, the following code can be used:

```
import os
cwd = os.getcwd()
print(cwd)
```

```
## /Users/ewengallic/Dropbox/Universite_Aix_Marseille/
   Magistere_2_Programming_for_big_data/Cours/chapters/python/
   Python_for_economists
```

Remark 5.0.1

The listdir() function of the os library is very useful: it allows to list all the documents and directories contained in the current directory, or in any directory if the argument path informs the path (absolute or relative). After importing the function (from os import getcwd), it can be called: os.listdir().

5.1 Load Data

Depending on the data format, data import techniques differ.

Remark 5.1.1

Chapter 10 provides other ways to import data, with the pandas library.

5.1.1 Fichiers textes

When the data is present in a text file (ASCII), Python offers the open() function.

The (simplified) syntax of the open() function is as follows:

```
open(file, mode='r', buffering=-1,
  encoding=None, errors=None, newline=None)
```

Here is what the arguments correspond to (there are others):

- file: a string indicating the path and name of the file to be opened;
- mode: specifies the way the file is opened (see the lines below for possible values);
- buffering: specifies using an integer the behavior to be adopted for buffering (1 to buffering per line; an integer > 1 to indicate the size in bytes of the chunks to be buffered);
- encoding: specifies the encoding of the file;
- errors: specifies how to handle encoding and decoding errors (e.g., strict returns an exception error, ignore ignores errors, replace replaces them, backslashreplace replaces malformed data with escape sequences);
- newline : controls the end of the lines (\n, \r, etc.).

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Table 5.1: Main Values for How to Open Files.

Value	Description
r	Opening to read (default)
W	Opening to write
x	Opening to create a document, fails if the file already exists
a	Opening to write, adding at the end of the file if it already exists
+	Opening for update (read and write)
b	To be added to an opening mode for binary files (rb or wb)
t	Text mode (automatic decoding of bytes in Unicode). Default if not
	specified (adds to the mode, like b)

It is important to remember to **close the file** once we have finished using it. To do this, we use the close() method.

In the fichiers_exemples folder is a file called text_file.txt which contains three lines of text. Let's open this file, and use the .read() method to display its content:

```
my_file.close()
```

A common practice in Python is to open a file in a with block. The reason for this choice is that a file opened in such a block is automatically closed at the end of the block.

The syntax is as follows:

```
# Opening in read-only mode (default)
with open(path, "r") as mon_fichier:
  data = function_to_get_data_from_my_file()
```

For example, to retrieve each line as an element of a list, a loop running through each line of the file can be used. At each iteration, the line is retrieved:

```
# Opening in read-only mode (default)
with open(path, "r") as my_file:
   data = [x for x in my_file]
print(data)
```

```
## ['Bonjour, je suis un fichier au format txt.\n', "Je
contiens plusieurs lignes, l'idée étant de montrer comment
fonctionne l'importation d'un tel fichier dans Python.\n",
   'Trois lignes devraient suffir.']
```

Note: at each iteration, the strip() method can be applied. It returns the character string of the line, by removing any white characters at the beginning of the string:

```
# Opening in read-only mode (default)
with open(path, "r") as my_file:
   data = [x.strip() for x in my_file]
print(data)
```

```
## ['Bonjour, je suis un fichier au format txt.', "Je contiens
   plusieurs lignes, l'idée étant de montrer comment
   fonctionne l'importation d'un tel fichier dans Python.", '
   Trois lignes devraient suffir.']
```

The readlines() method can also be used to import lines into a list:

```
with open(path, "r") as my_file:
    data = my_file.readlines()
print(data)
```

```
## ['Bonjour, je suis un fichier au format txt.\n', "Je
contiens plusieurs lignes, l'idée étant de montrer comment
```

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```
fonctionne l'importation d'un tel fichier dans Python.\n", 'Trois lignes devraient suffir.']
```

Character encoding may be a problem during import. In this case, it may be a good idea to change the value of the **encoding** argument of the **open()** function. The available encodings depend on the locale. The available values are obtained using the following method (code not executed in these notes):

```
import locale
locale_alias
```

5.1.1.1 Import from the Internet

To import a text file from the Internet, methods from the urllib library can be used:

```
import urllib
from urllib.request import urlopen
url = "http://egallic.fr/Enseignement/Python/fichiers_exemples/fichier_texte.txt"
with urllib.request.urlopen(url) as my_file:
    data = my_file.read()
print(data)
```

b"Bonjour, je suis un fichier au format txt.\nJe contiens
plusieurs lignes, l'id\xc3\xa9e \xc3\xa9tant de montrer
comment fonctionne l'importation d'un tel fichier dans
Python.\nTrois lignes devraient suffir."

As can be seen, the encoding of characters is a concern here. We can apply the method decode():

```
print(data.decode())
```

```
## Bonjour, je suis un fichier au format txt.
## Je contiens plusieurs lignes, l'idée étant de montrer
   comment fonctionne l'importation d'un tel fichier dans
   Python.
## Trois lignes devraient suffir.
```

5.1.2 CSV Files

CSV files (comma separated value) are very common. Many databases export their data to CSV (e.g., World Bank, FAO, Eurostat, etc.). To import them into Python, you can use the csv module.

Again, we use the open() function, with the arguments described in Section 5.1.1. Then, we use the reader() method of the csv module:

```
import csv
with open('./fichiers_exemples/fichier_csv.csv') as my_file:
    my_file_reader = csv.reader(my_file, delimiter=',', quotechar='"')
    data = [x for x in my_file_reader]

print(data)

## [['nom', 'prénom', 'équipe'], ['Irving', ' "Kyrie"', ' "
    Celtics"'], ['James', ' "Lebron"', ' "Lakers"', ''], ['
    Curry', ' "Stephen"', ' "Golden State Warriors"']]
```

The reader() method can take several arguments, described in Table 5.2.

Table 5.2: Arguments of the reader() Function

Argument	Description
csvfile	The object opened with open()
dialect	Argument specifying the "dialect" of the CSV file (e.g.,
	<pre>excel, excel-tab, unix)</pre>
delimiter	The character delimiting the fields (i.e., the values of the
	variables)
quotechar	Character used to surround fields containing special
	characters
escapechar	Escape character
doublequote	Controls how the <i>quotechar</i> appear inside a field: when
	True, the character is doubled, when False, the escape
	character is used as a prefix to the quotechar
lineterminator	String of characters used to end a line
skipinitialspace	When True, the white character located just after the
	field separation character is ignored

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nt Description	Argument
t When True, returns an exception error if there is a ba	strict
input of CS	

A CSV file can also be imported as a dictionary, using the csv.DictReader() method of the CSV module:

```
import csv
path = "./fichiers_exemples/fichier_csv.csv"
with open(path) as my_file:
    my_file_csv = csv.DictReader(my_file)
    data = [ligne for ligne in my_file_csv]
print(data)

## [OrderedDict([('nom', 'Irving'), ('prénom', ' "Kyrie"'), ('équipe', ' "Celtics"')]), OrderedDict([('nom', 'James'), ('prénom', ' "Lebron"'), ('équipe', ' "Lakers"'), (None, [''])]), OrderedDict([('nom', 'Curry'), ('prénom', ' "Stephen"'), ('équipe', ' "Golden State Warriors"')])]
```

5.1.2.1 Import From the Internet

As with txt files, a CSV file hosted on the Internet can be loaded:

```
import csv
import urllib.request
import codecs

url = "http://egallic.fr/Enseignement/Python/fichiers_exemples/fichier_csv.csv"
with urllib.request.urlopen(url) as my_file:
    my_file_csv = csv.reader(codecs.iterdecode(my_file, 'utf-8'))
    data = [ligne for ligne in my_file_csv]
print(data)

## [['nom', 'prénom', 'équipe'], ['Irving', ' "Kyrie"', ' "
    Celtics"'], ['James', ' "Lebron"', ' "Lakers"', ''], ['
```

```
Curry', ' "Stephen"', ' "Golden State Warriors"']]
```

5.1.3 JSON Files

To import files in JSON format (JavaScript Object Notation), which are widely used when communicating with an API, you can use the json library, and its load() method:

```
import json
url = './fichiers_exemples/tweets.json'
with open(url) as my_file_json:
    data = json.load(my_file_json)
```

Then, you can display the imported content using the pprint() function:

```
from pprint import pprint
pprint(data)
```

5.1.3.1 Import from the Internet

Once again, it is possible to import JSON files from the Internet:

```
import urllib
from urllib.request import urlopen
url = "http://egallic.fr/Enseignement/Python/fichiers_exemples/tweets.json"
with urllib.request.urlopen(url) as my_file:
```

```
data = json.load(my_file)
pprint(data)
```

5.1.4 Excel Files

Excel files (xls or xlsx) are also widely used in economics. The reader is referred to Section 10.16.2 for a method of importing Excel data with the pandas library.

5.2 Exporting data

It is not uncommon to have to export data, for instance to share it. Again, the function open() is used, by playing with the value of the argument mode (see Table 5.1).

5.2.1 Text Files

Let's say we need to export lines of text to a file. Before giving an example with the open() function, let's look at two important functions to convert the contents of some objects to text.

The first, str(), returns a string version of an object. We have already applied it to numbers that we wanted to concatenate in Section 2.1.4.

```
x = ["pomme", 1, 3]
str(x)
```

```
## "['pomme', 1, 3]"
```

The result of this instruction returns the list as a string: "['pomme', 1, 3]".

The second function that seems important to address is repr(). This function returns a string containing a printable representation on an object screen. In addition, this channel can be read by the interpreter.

```
y = "Fromage, tu veux du fromage ?\n"
repr(y)
```

```
## "'Fromage, tu veux du fromage ?\\n'"
```

The result writes: "'Fromage, tu veux du fromage ?\\n'".

Let's say we want to export two lines:

- the first, a text that indicates a title ("Kyrie Irving Characteristics");
- the second, a dictionary containing information about Kyrie Irving (see below).

Let's define this dictionary:

```
z = { "name": "Kyrie",
   "surname": "Irving",
   "date_of_birth": 1992,
   "teams": ["Cleveland", "Boston", "Nets"]}
```

One of the syntaxes for exporting data in txt format is:

```
# Ouverture en mode lecture (par défaut)
path = "path/to/file.txt"
with open(path, "w") as my_file:
  function_to_export()
```

We create a variable indicating the path to the file. Then we open the file in writing mode by specifying the argument mode = "w". Then, we still have to write our lines in the file.

```
path = "./fichiers_exemples/Irving.txt"
with open(path, mode = "w") as my_file:
```

```
my_file.write("Characteristics of Kyrie Irving\n")
my_file.writelines(repr(z))
## 32
```

If the file is already existing, having used mode="w", the old file will be overwritten by the new one. If we want to add lines to the existing file, we will use mode="a" for example:

```
with open(path, mode = "a") as my_file:
   my_file.writelines("\nAnother line\n")
```

If we want to be warned if the file already exists, and to make the writing fail if this is the case, we can use mode="x":

```
with open(path, mode = "x") as my_file:
    my_file.writelines("A new line that will not be added\n")

## Error in py_call_impl(callable, dots$args, dots$keywords):
    FileExistsError: [Errno 17] File exists: './
    fichiers_exemples/Irving.txt'

##

## Detailed traceback:
## File "<string>", line 1, in <module>
```

5.2.2 CSV Files

As economists, we are more likely to have to export data in CSV format rather than text, due to the rectangular structure of the data we are handling. As for the import of CSV (c.f. Section 5.1.2), on utilise le module csv. we use the module csv. To write to the file, we use the writer() method. The formatting arguments of this function are the same as those of the reader() function (see Table 5.2).

Example of creating a CSV file:

```
import csv
path = "./fichiers_exemples/ffile_export.csv"
```

Of course, most of the time, we do not write each entry by hand. We export the data contained in a structure. Section 10.16.2 provides examples of this type of export, when the data are contained in two-dimensional tables created with the pandas library.

5.2.3 JSON Files

It may be necessary to save structured data in JSON format, for example when an API (e.g., the Twitter API) has been used that returns objects in JSON format.

To do this, we will use the json library, and its dump() method. This method allows to serialize an object (for example a list, like what you get with the Twitter API queried with the twitter-python library) in JSON.

```
import json
x = [1, "apple", ["seed", "red"]]
y = { "name": "Kyrie",
    "surname": "John",
    "year_of_birth": 1992,
    "teams": ["Cleveland", "Boston", "Nets"]}
x_json = json.dumps(x)
y_json = json.dumps(y)

print("x_json: ", x_json)
```

```
## x_json: [1, "apple", ["seed", "red"]]
```

As can be seen, there are some minor problems with accentuated character rendering. We can specify, using the argument ensure_ascii evaluated at False that we do not want to make sure that non-ascii characters are escaped by sequences of type \uXXXX.

```
\uxxxx.
x_json = json.dumps(x, ensure_ascii=False)
y_json = json.dumps(y, ensure_ascii=False)

print("x_json: ", x_json)

## x_json: [1, "apple", ["seed", "red"]]

print("y_json: ", y_json)

## y_json: {"name": "Kyrie", "surname": "John", "
    year_of_birth": 1992, "teams": ["Cleveland", "Boston", "
    Nets"]}

path = "./fichiers_exemples/export_json.json"

with open(path, 'w') as f:
    json.dump(json.dumps(x, ensure_ascii=False), f)
    f.write('\n')
    json.dump(json.dumps(y, ensure_ascii=False), f)
```

1

If we want to re-import in Python the content of the file export_json.json:

```
path = "./fichiers_exemples/export_json.json"
with open(path, "r") as f:
    data = []
    for line in f:
        data.append(json.loads(line, encoding="utf-8"))

print(data)

## ['[1, "apple", ["seed", "red"]]', '{"name": "Kyrie", "
    surname": "John", "year_of_birth": 1992, "teams": ["
```

```
5.2.4 Exercise
```

- 1. Create a list named a containing information on the unemployment rate in France in the second quarter of 2018. This list must contain three elements:
 - the year;
 - the quarter;
 - the value of the unemployment rate (9.1%).

Cleveland", "Boston", "Nets"]}']

- 2. Export the contents of the list a in CSV format, preceded by a line specifying the names of the fields. Use the semicolon (;) as a field separator.
- 3. Import the file created in the previous question into Python.

Chapter 6

Conditions

Often, depending on the evaluation of an expression, one wants to perform one operation rather than another. For example, when a new variable is created in a statistical analysis, and this variable takes its values according to another, it may be necessary to use **conditional instructions**: "if the value is less than x, then... otherwise, ...".

In this short chapter, we look at how to write conditional instructions.

6.1 Conditional if Instructions

The simplest conditional instruction that can be found is if. If and only if an expression is evaluated at True, then an instruction will be evaluated.

The syntax is as follows:

```
if expression:
  instruction
```

The lines after the colon (:) must be placed in a block, using a tab stop.

Remark 6.1.1

A code block is a grouping of statements. Nested codes indented at the same position are part of the same block:

```
block 1 line
block 2 line
block2 line
block line1
```

In the code below, we define a variable, x, that contains the integer 2. The following instruction evaluates the expression x == 2 (see Section @ref(#operateurs-comparaison) for reminders on comparison operators). If the result of this expression is True, then the content of the block is evaluated.

```
x = 2
if x == 2:
  print("Hello")
```

Hello

If we change the value of x so that the expression x == 2 returns False:

```
x = 3
if x == 2:
  print("Hello")
```

Inside the block, several instructions can be written that will be evaluated if the expression is True:

```
x = 2
if x == 2:
    y = "Hello"
    print(y + ", x vaut : " + str(x))
```

```
## Hello, x vaut : 2
```

Remark 6.1.2

When writing a code, it may be practical to use 'if' conditional instructions to evaluate or not certain parts of the code. For example, when we write a script, there are times when we have to re-evaluate the beginning, but some parts don't need to be re-evaluated every time, like graphical outputs (which takes time). Of course, it is possible to comment on these parts of codes that do not require a new evaluation. But we can also put the instructions in a conditional block:

- at the beginning of the script, we create a variable graph = False;
- before creating a graph, it is placed in a block if graph:

When executing the script, it is then possible to choose to create and export the graphs of the if graph: blocks by modifying the graph variable as desired.

6.2 if-else Conditional Instructions

If the condition is not verified, other instructions can be evaluated using the 'if-else' instructions.

The syntax is as follows:

```
if expression:
  instructions
else:
  other_instructions
```

For example, suppose we want to create a variable related to temperature, taking the value warm if the value of the variable temperature exceeds 28 degrees C, otherwise cold. Let's say the temperature is 26 degrees C:

```
temperature = 26
heat = ""

if temperature > 28:
   heat = "hot"
else:
   heat = "cold"

print("It is " + heat + " out there")
```

```
## It is cold out there
```

If the temperature is now 32 degrees C:

```
temperature = 32
heat = ""

if temperature > 28:
   heat = "hot"
else:
   heat = "cold"

print("It is " + heat + " out there")

## It is hot out there
```

6.3 if-elif Conditional Instructions

If the condition is not verified, another one can be tested and then other instructions evaluated if the second one is verified. Otherwise, another one can be tested, and so on. Instructions may also be evaluated if none of the conditions have been assessed at True. To do this, conditional 'if-elif' instructions can be used.

The syntax is as follows:

```
if expression:
   instructions
elif expression_2:
   instructions_2
elif expression_3:
   instructions_3
else:
   other_instruction
```

The previous example lacks some common sense. Can we say that the fact that it is 28 degrees C or less it is cold? Let's add a few nuances:

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```
temperature = -4
heat = ""

if temperature > 28:
   heat = "hot"
elif temperature <= 28 and temperature > 15:
   heat = "not too hot"
elif temperature <= 15 and temperature > 0:
   heat = "cold"
else:
   heat = "very cold"

print("It is " + heat + " out there")
```

It is very cold out there

Remark 6.3.1

The advantage of using if-elif' conditional instructions over writing severalif' conditional instructions in succession is that with the first way of doing things, comparisons stop as soon as one is completed, which is more efficient.

6.4 Exercise

Let us consider a list named europe containing the following values, as strings: "Germany", "France" and "Spain".

Let us consider a second list, named asia, containing in the form of strings: "Vietnam", "China" and "India".

The objective will be to create a continent variable that will indicate either Europe, Asia or other at the end of the code execution.

Using conditional instructions of the if-elif' type, write a code that checks the value of a variable namedcountry. Another variable, namedcontinent' will take values depending on the content of the former one, such that:

- if the country value is present in the europe list, the variable continent should be set to Europe
- if the country value is present in the asia list, the variable continent should be set to Asia
- if the country value is not present in europe or asia, the variable continent will be set to Other.

To do this:

- 1. Create the two lists europe and asia as well as the variable country (setting the value to Spain) and the variable continent (initiated with an empty character string).
- 2. Write the code to achieve the explained objective, and display the content of the continent variable at the end of the execution.
- 3. Change the initial value of country to China then Brazil and in each case, execute the code written in the previous question.

Chapter 7

Loops

When the same operation has to be repeated several times, for a given number of times or as long as a condition is verified (or as long as it is not verified), loops can be used, which is much less painful than evaluating by hand or by copying and pasting the same instruction.

We will discuss two types of loops in this chapter:

- those for which we do not know a priori the number of iterations (the number of repetitions) to be performed: while() loops
- those for which we know a priori how many iterations are necessary: for() loops

Remark 7.0.1

It is possible to stop a for() loop before a predefined number of iterations; in the same way, it is possible to use a while() loop by knowing in advance how many iterations to perform.

7.1 Loops with while()

The principle of a while() loop is that instructions inside the loop will be repeated as long as a condition is met. The idea is to make this condition depend on one or more objects that will be modified during the iterations (otherwise, the loop would turn infinitely).

The syntax is as follows:

```
while condition:
instructions
```

As for conditional instructions (see Section 6), the instructions are placed inside a block.

Let's look at an example of a while() loop:

In this loop, at each iteration, the value of x divided by 3 is displayed, then the value of x is replaced by a third of its current value. This operation is repeated as long as the expression x/3 > 1 returns True.

7.2 Loops with for()

When we know the number of iterations in advance, we can use a for() loop. The syntax is as follows:

```
for object in possible_values:
  instructions
```

with object the name of a local variable at the function for(), possible_values an object comprising n elements defining the values that object will take for each of the n turns, and instructions the instructions that will be executed at each iteration.

In the following example, we will calculate the square of the first n integers. The values that our object variable (which we will call i) will take will be integers from 1 to n. To obtain a sequence of integers in Python, we can use the range() function, which takes the following arguments:

- start: (optional, default, 0) start value for the sequence (included);
- stop: end value of the sequence (not included);
- step: (optional, default 1) the step.

Before calculating the sequence of the n first squares, let's look at an example of how the range() function works:

```
print(list(range(0, 4))) # Les entiers de 0 à 3

## [0, 1, 2, 3]

print(list(range(4))) # Les entiers de 0 à 3

## [0, 1, 2, 3]

print(list(range(2, 10))) # Les entiers de 2 à 9

## [2, 3, 4, 5, 6, 7, 8, 9]

print(list(range(2, 10, 3))) # Les entiers de 2 à 9 par pas de 3

## [2, 5, 8]
```

To display the sequence of the first 10 first squares, we can write:

```
message = "The squared value of {} is {}"
n=10
for i in range(0, n+1):
    print(message.format(i,i**2))

## The squared value of 0 is 0
## The squared value of 1 is 1
## The squared value of 2 is 4
## The squared value of 3 is 9
## The squared value of 4 is 16
## The squared value of 5 is 25
## The squared value of 6 is 36
## The squared value of 7 is 49
## The squared value of 8 is 64
## The squared value of 9 is 81
## The squared value of 10 is 100
```

During the first iteration, i is 0. In the second case, i is 1. In the third, i is 2, etc.

If we want to store the result in a list:

```
n=10
n_squares = []
for i in range(0, n+1):
    n_squares.append(i**2)

print(n_squares)

## [0, 1, 4, 9, 16, 25, 36, 49, 64, 81, 100]
```

It is not mandatory to use the range() function in a for() loop, you can define the values "by hand":

```
message = "The squared value of {} is {}"
for i in [0, 1, 2, 8, 9, 10]:
   print(message.format(i,i**2))

## The squared value of 0 is 0
## The squared value of 1 is 1
```

```
## The squared value of 2 is 4
## The squared value of 8 is 64
## The squared value of 9 is 81
## The squared value of 10 is 100
```

In the same spirit, it is not mandatory to iterate on numerical values:

```
message = "There is(are) {} letter(s) in the name: {}"
for first_name in ["Pascaline", "Gauthier", "Xuan", "Jimmy"]:
    print(message.format(len(first_name), first_name))

## There is(are) 9 letter(s) in the name: Pascaline
## There is(are) 8 letter(s) in the name: Gauthier
## There is(are) 4 letter(s) in the name: Xuan
## There is(are) 5 letter(s) in the name: Jimmy
```

Nothing prevents loops from being made inside loops:

```
message = "i equals {} and j equals {}"
for i in range(0,3):
    for j in range(0,3):
        print(message.format(i, j))

## i equals 0 and j equals 0
## i equals 0 and j equals 1
## i equals 0 and j equals 2
## i equals 1 and j equals 0
## i equals 1 and j equals 0
## i equals 1 and j equals 1
## i equals 2 and j equals 0
## i equals 2 and j equals 0
## i equals 2 and j equals 0
## i equals 2 and j equals 1
## i equals 2 and j equals 1
```

As can be seen, iteration is done for each value of i, and for each of these values, a second iteration is performed on the values of j.

Remark 7.2.1

The letters i and j are often used to designate a counter in a for() loop, but this is obviously not a requirement.

In a loop, if we want to increment a counter, we can use the symbol += rather than writing 'counter = counter $+ \dots$ ":

```
message = "New value for j: {}"
j = 10
for i in range(0, 4):
    j += 5
    print(message.format(j))

## New value for j: 15
## New value for j: 20
## New value for j: 25
## New value for j: 30
```

```
print(j)
```

30

7.3 Exercise

- 1. Write a very naive program to determine if a number is prime or not. To do this:
 - 1. define a number variable containing a natural integer of your choice (not too large),
 - 2. using a loop, check if each integer up to the square root of your number, is a divisor of your number (stop if ever it is the case)
 - 3. at the loop output, write a conditional instruction indicating whether or not the number is a prime one.

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2. Choose a 'mystery' number between 1 and 100, and store it in an object called mystery_number. Then, create a loop that at each iteration performs a random draw of an integer between 1 and 100. As long as the number drawn is different from the mystery number, the loop must continue. At the output of the loop, a variable called nb_drawings will contain the number of draws made to obtain the mystery number.

Note: to draw a random number between 1 and 100, the method randint() of the module random may help).

- 3. Use a loop to scan integers from 1 to 20 using a for loop, displaying in the console at each iteration if the current number is even.
- 4. Use a for() loop to repeat the Fibonacci sequence until its tenth term (the F_n sequence is defined by the following recurrence relationship: $F_n = F_{n-1} + F_{n-2}$; the initial values are $F_0 = 0$ and $F_1 = 1$).

Chapter 8

Functions

Most of the time, we use the basic functions or those contained in modules. However, when retrieving data online or formatting data imported from various sources, it may be necessary to create our own functions. The advantage of creating one's functions is revealed when one has to carry out a series of instructions repeatedly, with some slight differences (we can then apply the functions within a loop, as we discussed in Chapter 7).

8.1 Definition

A function is declared using the keyword **def**. What it returns is returned using the keyword **return**.

La syntaxe est la suivante :

```
def name_function(arguments):
  body of the function
```

Once the function is defined, it is called by referring to its name:

```
name_function()
```

So, all we need to do is add parentheses to the name of the function to call it. Indeed, function_name refers to the object that contains the function that is called using the

expression function_name(). For example, if we want to define the function that calculates the square of a number, here is what we can write:

```
def square(x):
    return x**2

It can then be called:
print(square(2))
## 4

print(square(-3))
## 9
```

8.1.1 Adding a Description

It is possible (and strongly recommended) to add a description of what the function does, by adopting some conventions (see https://www.python.org/dev/peps/pep-0257/) =

```
def square(x):
    """returns the squared value of x"""
    return x**2
```

When the next instruction is then evaluated, the description of the function is displayed:

```
`?`(square)
```

In Jupyter Notebook, after writing the name of the function, the description can also be displayed by pressing the Shift and Tabulation keys on the keyboard.

8.1.2 Arguments of a Function

In the example of the square() function we created, we filled in only one argument, called x. If the function we wish to create requires several argument, they must be

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separated by a comma.

Let us consider, for example, the following problem. We have a production function Y(L, K, M), which depends on the number of workers L and the amount of capital K, and the equipment M, such that $Y(L, K, M) = L^{0.3}K^{0.5}M^2$. This function can be written in Python as follows:

```
def production(1, k, m):
    """

Returns the value of the production according to
    labour, capital and materials

Keyword arguments:
    l -- labour (float)
    k -- capital (float)
    m -- materials (float)
    """

return 1**0.3 * k**0.5 * m**(0.2)
```

8.1.2.1 Call Without Argument Names

Using the previous example, if we are given L=60 and K=42 and M=40, we can deduce the production:

```
prod_val = production(60, 42, 40)
print(prod_val)
## 46.289449781254994
```

It should be noted that the name of the arguments has not been mentioned here. When the function was called, the value of the first argument was assigned to the first argument (1), the second to the second argument (k) and finally the third to the third argument (m).

8.1.2.2 Positional Arguments, Arguments by Keywords

There are two types of arguments that can be given to a function in Python:

- the positional arguments;
- arguments by keywords.

Unlike positional arguments, keyword arguments have a default value assigned by default. We speak of a formal argument to designate the arguments of the function (the variables used in the body of the function) and an effective argument to designate the value that we wish to give to the formal argument To define the value to be given to a formal argument, we use the equality symbol. When calling the function, if the user does not explicitly define a value, the default value will be assigned. Thus, it is not necessarily necessary to specify the arguments by keywords when calling the function.

It is important to note that positional arguments (those that do not have a default value) must appear first in the argument list.

Let's take an example with two positional arguments (1 and m) and one argument per keyword (k):

```
def production_2(1, m, k=42):
    """

Returns the value of the production according to
    labour, capital and materials

Keyword arguments:
    l -- labour (float)
    m -- materials (float)
    k -- capital (float) (default 42)
    """

return 1**0.3 * k**0.5 * m**(0.2)
```

The production_2() function can be called, to give the same result, in the following three ways:

```
# By naming all argument, by ommitting k
prod_val_1 = production_2(1 = 42, m = 40)
# By naming all argument and specifying k
prod_val_2 = production_2(1 = 42, m = 40, k = 42)
# By naming only the argument k
prod_val_3 = production_2(42, 40, k = 42)
# Without naming any argument
prod_val_4 = production_2(42, 40, 42)
```

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```
res = [prod_val_1, prod_val_2, prod_val_3, prod_val_4]
print(res)
```

```
## [41.59215573604822, 41.59215573604822, 41.59215573604822, 41.59215573604822]
```

Remark 8.1.1

If the function contains several positional arguments; when evaluating:

- or all positional arguments are named by their name;
- or none;
- there are no in-between.

As long as all the positional arguments are named during the evaluation, they can be listed in different orders:

```
def production_3(a, 1, m = 40, k=42):
  11 11 11
  Returns the value of the production according to
  labour, capital and materials
  Keyword arguments:
  a -- total factor productivity (float)
  l -- labour (float)
  m -- materials (float) (default 40)
  k -- capital (float) (default 42)
  return a * 1**0.3 * k**0.5 * m**(0.2)
prod val 1 = production 3(1, 42, m = 38)
prod_val_2 = production_3(a = 1, 1 = 42)
prod val 3 = \text{production } 3(1 = 42, a = 1)
prod val 4 = \text{production } 3(m = 40, 1 = 42, a = 1)
res = [prod_val_1, prod_val_2, prod_val_3, prod_val_4]
print(res)
```

[41.16765711449734, 41.59215573604822, 41.59215573604822,

```
41.59215573604822]
```

8.1.2.3 Function as an Argument to Another Function

A function can be provided as an argument to another function.

```
def square(x):
    """Returns the squared value of x"""
    return x**2

def apply_fun_to_4(fun):
    """Applies the function `fun` to 4"""
    return fun(4)

print(apply_fun_to_4(square))
```

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8.2 Scope of a Function

When a function is called, the body of that function is interpreted. Variables that have been defined in the body of the function are assigned to a local *namespace*. In other words, they live only within this local space, which is created at the moment of the call of the function and destroyed at the end of it. This is referred to as the scope of the variables. Thus, a variable with a local scope (assigned in the local space) can have the same name as a global variable (defined in the global workspace), without designating the same object, or overwrite this object.

Let's look at this through an example.

```
# Definition of a global variable:
value = 1
# Definition of a local variable in function f
```

```
def f(x):
  value = 2
  new_value = 3
  print("value equals: ", value)
  print("new_value equals: ", new_value)
  return x + value
```

Let's call the f() function, then look at the value and new_value values after executing the function.

```
res = f(3)

## value equals: 2
## new_value equals: 3

print("value equals: ", value)

## value equals: 1

print("new_value equals: ", new_value)

## Error in py_call_impl(callable, dots$args, dots$keywords):
    NameError: name 'new_value' is not defined

##
## Detailed traceback:
## File "<string>", line 1, in <module>
```

As can be seen, during the evaluation, the local variable of the name value was 2, which did not refer to the variable of the same name defined in the global environment. After executing the f() function, this local value variable is deleted, and the same applies to the local new_value variable, which does not exist in the global environment (hence the error returned).

Without going into too much detail, it seems important to know some principles about the scope of variables. Variables are defined in environments, which are embedded in each other. If a variable is not defined in the body of a function, Python will search in a parent environment.

```
value = 1
def f(x):
    return x + value

print(f(2))
## 3
```

If we define a function within another function, and call a variable not defined in the body of that function, Python will search in the directly superior environment. If it does not find, it will search in the even higher environment, and so on until ir reaches the global environment.

```
# The value variable is not defined in
# the local environment of g().
# Python will then search in f().
value = 1
def f():
   value = 2
   def g(x):
     return x + value

return g(2)
print(f())
```

```
# The value variable is not defined in g() or f()
# but in the higher environment (here, global)
value = 1
def f():
    def g(x):
        return x + value
return g(2)
```

```
print(f())
## 3
```

If a variable is defined in the body of a function and we want it to be accessible in the global environment, we can use the keyword global:

```
def f(x):
    global y
    y = x+1

f(3)
print(y)
## 4
```

Remark 8.2.1

The variable that we want to define globally from a local space of the function must not have the same name of one of the arguments.

8.3 Lambda Functions

Python offers what are called lambdas functions, or anonymous functions. A lambda function has only one instruction whose result is that of the function.

They are defined using the keyword lambda. The syntax is as follows:

```
name_function = lambda arguments : result
```

The arguments are to be separated by commas.

Let's take the function square() created previously:

```
def square(x):
    return x**2
```

The equivalent lambda function is written:

```
square_2 = lambda x: x**2
print(square_2(4))
## 16
```

With several arguments, let's look at the lambda function equivalent to the production() function:

```
def production(1, k, m):
    """
    Returns the value of the production according to
    labour, capital and materials.

    Keyword arguments:
    l -- labour (float)
    k -- capital (float)
    m -- materials (float)
    """
    return 1**0.3 * k**0.5 * m**(0.2)

production_2 = lambda 1,k,m : 1**0.3 * k**0.5 * m**(0.2)

print(production(42, 40, 42))

## 40.987803063838406

## 40.987803063838406
```

8.4 Returning Several Values

It can sometimes be convenient to return several elements in return for a function. Although the list is a candidate for this feature, it may be better to use a dictionary, to be able to access the values with their key!

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```
import statistics
def desc_stats(x):
    """Returns the mean and standard deviation of `x`"""
    return {"mean": statistics.mean(x),
        "std_dev": statistics.stdev(x)}

x = [1,3,2,6,4,1,8,9,3,2]
res = desc_stats(x)
print(res)

## {'mean': 3.9, 'std_dev': 2.8460498941515415}

message = "The average value equals {} and the standard deviation is {}"
print(message.format(res["mean"], res["std_dev"]))

## The average value equals 3.9 and the standard deviation is
        2.8460498941515415
```

8.5 Exercise

- 1. Create a function named $sum_n_integers$ which returns the sum of the first integer n. Its only argument will be n.
- 2. Using a loop, display the sum of the first 2 integers, then 3 first integers, then 4 first integers, etc. up to 10.
- 3. Create a function that from two points represented by pairs of coordinates (x_1, y_1) and (x_2, y_2) returns the Euclidean distance between these two points. Propose a second solution using a lambda function.

Chapter 9

Introduction to Numpy

This chapter is devoted to an important library for numerical calculations: NumPy (abbreviation of *Numerical Python*).

It is common practice to import NumPy by assigning it the alias np:

import numpy as np

9.1 Arrays

NumPy offers a popular data structure, arrays, on which calculations can be performed efficiently. Arrays are a useful structure for performing basic statistical operations as well as pseudo-random number generation.

The structure of the tables is similar to that of the lists, but the latter are slower to process and use more memory. The gain in processing speed of the 'NumPy' arrays comes from the fact that the data is stored in contiguous memory blocks, thus facilitating read access.

To be convinced, we can use the example of Pierre Navaro given in his *notebook* on NumPy.. Let's create two lists of 1000 length each, with numbers drawn randomly using the random() function of the random module. Let's divide each element in the first list by the element at the same position in the second line, then calculate the sum of these 1000 divisions. Then let's look at the execution time using the magic function %timeit:

```
from random import random
from operator import truediv

11 = [random() for i in range(1000)]

12 = [random() for i in range(1000)]
# %timeit s = sum(map(truediv, l1, l2))
```

(uncomment the last line and test on a Jupyter Notebook)

Now, let's transform the two lists into NumPy tables with the array() method, and do the same calculation with a NumPy method:

```
a1 = np.array(11)
a2 = np.array(12)
# %timeit s = np.sum(a1/a2)
```

As can be seen by executing these codes in an IPython environment, the execution time is much faster with the NumPy methods for this calculation.

9.1.1 Creation

The creation of an array can be done with the array() method, from a list, as we just did:

```
list = [1,2,4]
table = np.array(list)
print(table)
## [1 2 4]
```

```
print(type(table))
## <class 'numpy.ndarray'>
```

If array() is provided with a list of nested lists of the same length, a multidimensional array will be created:

```
list_2 = [ [1,2,3], [4,5,6] ]
table_2 = np.array(list_2)
print(table_2)

## [[1 2 3]
## [4 5 6]]
```

```
print(type(table_2))
```

```
## <class 'numpy.ndarray'>
```

Tables can also be created from tuples:

```
tup = (1, 2, 3)
table = np.array(tup)
print(table)
```

```
## [1 2 3]
```

print(type(table))

```
## <class 'numpy.ndarray'>
```

An 1-dimension array can be casted to a 2-dimension array (if possible), by changing its shape attribute:

```
table = np.array([3, 2, 5, 1, 6, 5])
table.shape = (3,2)
print(table)
```

```
## [[3 2]
## [5 1]
## [6 5]]
```

print(y, y.dtype)

9.1.1.1 Some Functions Generating array Objects

Some of the functions in NumPy produce pre-filled arrays. This is the case of the zeros() function. When given an integer value n, the zeros() function creates a one-dimensional array, with n 0:

```
print( np.zeros(4) )
## [0. 0. 0. 0.]
```

The type of zeros (e. g. int, int32, int64, int64, float, float32, float64, etc.) can be specified using the dtype argument:

```
print( np.zeros(4, dtype = "int") )
## [0 0 0 0]
```

More explanations on the types of data with NumPy are available on the online documentation.

The type of the elements of an array is indicated via the argument dtype:

```
x = np.zeros(4, dtype = "int")
print(x, x.dtype)
## [0 0 0 0] int64
```

It is also possible to convert the type of elements into another type, using the astype() method:

```
y = x.astype("float")
print(x, x.dtype)
## [0 0 0 0] int64
```

```
## [0. 0. 0.] float64
```

When provided with a tuple longer than 1, zeros() creates a multidimensional array:

```
print( np.zeros((2, 3)) )

## [[0. 0. 0.]
## [0. 0. 0.]]
```

```
print( np.zeros((2, 3, 4)) )
```

```
## [[[0. 0. 0. 0.]

## [0. 0. 0. 0.]

## [0. 0. 0. 0.]]

##

## [[0. 0. 0. 0.]

## [0. 0. 0. 0.]
```

The empty() function of Numpy also returns an array on the same principle as zeros(), but without initializing the values inside.

```
print( np.empty((2, 3), dtype = "int") )
## [[0 0 0]
## [0 0 0]]
```

The ones() function of Numpy returns the same kind of arrays, with 1s in initialized values:

```
print( np.ones((2, 3), dtype = "float") )

## [[1. 1. 1.]
## [1. 1. 1.]]
```

To choose a specific value for initialization, you can use the full() function of Numpy:

```
print( np.full((2, 3), 10, dtype = "float") )

## [[10. 10. 10.]
## [10. 10. 10.]]

print( np.full((2, 3), np.inf) )

## [[inf inf inf]
## [inf inf inf]]
```

The eye() function of Numpy creates a two-dimensional array in which all elements are initialized to zero, except those of the diagonal initialized to 1:

```
print( np.eye(2, dtype="int64") )
## [[1 0]
## [0 1]]
```

By modifying the keyword argument k, the diagonal can be shifted:

```
print( np.eye(3, k=-1) )

## [[0. 0. 0.]
## [1. 0. 0.]
## [0. 1. 0.]]
```

The identity() function of Numpy creates an identity matrix in the form of an array:

```
print( np.identity(3, dtype = "int") )

## [[1 0 0]
## [0 1 0]
## [0 0 1]]
```

The arange() function of Numpy allows to generate a sequence of numbers separated by a fixed interval, all stored in an array. The syntax is as follows:

```
np.arange( start, stop, step, dtype )
```

with start the start value, stop the finish value, step the step, i.e., the spacing between the numbers in the sequence and type the type of numbers:

```
print( np.arange(5) )

## [0 1 2 3 4]

print( np.arange(2, 5) )

## [2 3 4]

print( np.arange(2, 10, 2) )

## [2 4 6 8]
```

9.1.2 Dimensions

To know the size of an array, the value of the attribute ndim can be displayed:

```
print("ndim tableau : ", table.ndim)

## ndim tableau : 2

print("ndim table_2 : ", table_2.ndim)

## ndim table_2 : 2
```

The number of elements in the array can be obtained by the size attribute or by the size() function of Numpy:

```
print("size table : ", table.size)

## size table : 6

print("size table_2: ", table_2.size)

## size table_2: 6

print("np.size(table):", np.size(table))

## np.size(table): 6
```

The **shape** attribute returns a tuple indicating the length for each dimension of the array:

```
print("size table: ", table.shape)

## size table: (3, 2)

print("size table_2: ", table_2.shape)

## size table_2: (2, 3)
```

9.1.3 Extracting Elements from an Array

Access to the elements of an array is done in the same way as for lists (see Section 3.1.1), using indexes. The syntax is as follows:

```
array[lower:upper:step]
```

with lower the lower boundary of the index range, upper the upper range, and step the spacing between the values.

• When lower is not specified, the first element (indexed 0) is considered as the value assigned to lower.

- When upper' is not specified, the last element is considered as the value assigned toupper'.
- When step is not specified, a step of 1 is assigned by default.

Let's take a quick look at some examples, using two objects: an array of dimension 1, and a second of dimension 2.

```
table_1 = np.arange(1,13)
table_2 = [ [1, 2, 3], [4, 5, 6], [7, 8, 9], [10, 11, 12]]
table_2 = np.array(table_2)
```

Access to the first element:

```
message = "table_{}[0] : {} (type : {})"
print(message.format(0, table_1[0], type(table_1[0])))
## table_0[0] : 1 (type : <class 'numpy.int64'>)
```

```
print(message.format(1, table_2[0], type(table_2[0])))
## table_1[0] : [1 2 3] (type : <class 'numpy.ndarray'>)
```

Access to the elements can be done from the end:

print("table_1[-1] : ", table_1[-1]) # last element

```
## table_1[-1] : 12

print("table_2[-1] : ", table_2[-1]) # last element

## table_2[-1] : [10 11 12]
```

Slicing is possible:

```
# the elements from the 2nd (not included) to the 4th
print("Slice Table 1 : \n", table_1[2:4])
## Slice Table 1 :
## [3 4]
print("Sclie Table 2 : \n", table_2[2:4])
## Sclie Table 2 :
   [[7 8 9]
   [10 11 12]]
##
For two-dimensional arrays, the elements can be accessed in the following ways:
# Within the 3rd element, access the 1st element
print(table_2[2][0])
## 7
print(table_2[2,0])
## 7
To extract columns from an array with two entries:
print("Second column: \n", table_2[:, [1]])
## Second column:
##
   [[ 2]
##
   [ 5]
## [8]
## [11]]
```

```
print("Second and third columns: \n", table_2[:, [1,2]])
```

```
## Second and third columns:
## [[ 2 3]
## [ 5 6]
## [ 8 9]
## [11 12]]
```

For this last instruction, we specify with the first argument not filled in (before the two points) that we want all the elements of the first dimension, then, with the comma, we indicate that we look inside each element of the first dimension, and that we want the values at positions 1 and 2 (therefore the elements of columns 2 and 3).

To extract only some elements from a 1-dimensional array, we can specify the indices of the elements to be recovered:

```
print("2nd and 4th elements: \n", table_2[[1,3]])

## 2nd and 4th elements:
## [[ 4 5 6]
## [10 11 12]]
```

9.1.3.1 Extraction Using Boolean

To extract or not elements from a table, you can use Boolean tables as masks. The idea is to provide a boolean array (a mask) of the same size as the one for which you want to extract elements under certain conditions. When the value of the Boolean in the mask is set to True, the corresponding element of the array is returned; otherwise, it is not.

```
table = np.array([0, 3, 2, 5, 1, 4])
res = table[[True, False, True, False, True, True]]
print(res)
```

```
## [0 2 1 4]
```

Only the elements in positions 1, 3, 5 and 6 were returned.

In practice, the mask is only very rarely created by the user, but rather comes from a logical instruction applied to the interest table. For example, in our table, we can first create a mask to identify even elements:

```
mask = table % 2 == 0
print(mask)

## [ True False True False False True]

print(type(mask))
```

```
## <class 'numpy.ndarray'>
```

Once this mask is created, it can be applied to the array to extract only those elements for which the corresponding value in the mask is True:

```
print(table[mask])
## [0 2 4]
```

9.1.4 Modification

To replace the values in an array, equal sign (=) can be used:

```
table = np.array([ [1, 2, 3], [4, 5, 6], [7, 8, 9], [10, 11, 12]])
table[0] = [11, 22, 33]
print(table)
```

```
## [[11 22 33]
## [ 4 5 6]
## [ 7 8 9]
## [10 11 12]]
```

If a scalar is provided during replacement, the value will be repeated for all elements of the dimension:

```
table[0] = 100
print(table)

## [[100 100 100]
## [ 4 5 6]
## [ 7 8 9]
## [ 10 11 12]]
```

Same idea with a slicing:

```
table[0:2] = 100
print(table)

## [[100 100 100]
## [100 100 100]
## [ 7 8 9]
## [ 10 11 12]]
```

In fact, a breakdown with just the two points without specifying the start and end arguments of the breakdown followed by an equal sign and a number replaces all the values in the table with this number:

```
table[:] = 0
print(table)

## [[0 0 0]
## [0 0 0]
## [0 0 0]
## [0 0 0]]
```

9.1.4.1 Insterting Elements

To add elements, we use the append() function of NumPy. Note that calling this function does not change the object to which the values are added. If we want the

changes to be made to this object, we must overwrite it:

```
t 1 = np.array([1,3,5])
print("t_1 : ", t_1)
## t<sub>1</sub>: [1 3 5]
t_1 = np.append(t_1, 1)
print("t 1 after the insertion: ", t_1)
## t_1 after the insertion: [1 3 5 1]
To add a column to a two-dimensional table:
t_2 = np.array([[1,2,3], [5,6,7]])
print("t 2 : \n", t 2)
## t_2 :
## [[1 2 3]
## [5 6 7]]
add col t 2 = np.array([[4], [8]])
t_2 = np.append(t_2,add_col_t_2, axis = 1)
print("t_2 after the insertion: \n", t 2)
## t_2 after the insertion:
## [[1 2 3 4]
## [5 6 7 8]]
To add a line, we use the vstack() function of Numpy:
ajout_ligne_t_2 = np.array([10, 11, 12, 13])
t 2 = np.vstack([t 2,ajout ligne t 2])
print("t_2 après ajout ligne : \n", t_2)
## t_2 après ajout ligne :
## [[ 1 2 3 4]
```

```
## [ 5 6 7 8]
## [10 11 12 13]]
```

9.1.4.2 Deleting / Removing Elements

To delete elements, we can use the delete() function of NumPy:

```
print("t_1 : ", t_1)
# Remove the last element

## t_1 : [1 3 5 1]

np.delete(t_1, (-1))
## array([1, 3, 5])
```

Note: for the deletion to be effective, the result of np.delete() is assigned to the object.

To delete multiple items:

```
print("t_1 : ", t_1)
# Remove the first and second elements:

## t_1 : [1 3 5 1]

t_1 = np.delete(t_1, ([0, 2]))
print(t_1)

## [3 1]
```

To delete a column from a two-dimensional table:

[10 11 12 13]]

```
print("t_2 : ", t_2)
# Remove the last column:
## t 2 : [[ 1 2 3 4]
## [5 6 7 8]
## [10 11 12 13]]
np.delete(t 2, (0), axis=1)
## array([[ 2, 3, 4],
      [6,7,8],
##
##
        [11, 12, 13]])
Delete multiple columns:
print("t 2 : ", t 2)
# Remove the first and third columns:
## t_2 : [[ 1 2 3 4]
## [5 6 7 8]
## [10 11 12 13]]
np.delete(t 2, ([0,2]), axis=1)
## array([[ 2, 4],
##
        [6,8],
         [11, 13]])
##
And to delete a row:
print("t 2 : ", t 2)
# Remove the first line:
## t_2 : [[ 1 2 3 4]
## [5 6 7 8]
```

```
np.delete(t_2, (0), axis=0)
```

```
## array([[ 5, 6, 7, 8],
## [10, 11, 12, 13]])
```

Delete multiple lines:

```
print("t_2 : ", t_2)
# Remove the first and third lines:
```

```
## t_2 : [[ 1 2 3 4]
## [ 5 6 7 8]
## [10 11 12 13]]
```

```
np.delete(t_2, ([0,2]), axis=0)
```

```
## array([[5, 6, 7, 8]])
```

9.1.5 Copyi of an Array

Copying an array, as with lists (c.f. Section 3.1.4), should not be done with the equal symbol (=). Let's see why.

```
table_1 = np.array([1, 2, 3])
table_2 = table_1
```

Let's modify the first element of table_2, and observe the content of table_2 and table_1:

```
table_2[0] = 0
print("Table 1: \n", table_1)

## Table 1:
## [0 2 3]
```

```
print("Table 2: \n", table_2)

## Table 2:
## [0 2 3]
```

As can be seen, using the equal sign simply created a reference and not a copy.

There are several ways to copy an array. Among them, the use of the np.array() function:

```
table_1 = np.array([1, 2, 3])
table_2 = np.array(table_1)
table_2[0] = 0
print("table_1 : ", table_1)

## table_1 : [1 2 3]

print("table_2 : ", table_2)

## table_2 : [0 2 3]
```

The copy() method can also be used:

```
table_1 = np.array([1, 2, 3])
table_2 = table_1.copy()
table_2[0] = 0
print("table_1 : ", table_1)

## table_1 : [1 2 3]

print("table_2 : ", table_2)

## table_2 : [0 2 3]
```

It can be noted that when a slicing is made, a new object is created, not a reference:

```
table_1 = np.array([1, 2, 3, 4])
table_2 = table_1[:2]
table_2[0] = 0
print("table_1 : ", table_1)

## table_1 : [0 2 3 4]

print("table_2 : ", table_2)

## table_2 : [0 2]
```

9.1.6 Sorting

The NumPy library provides a function to sort the tables, sort():

```
table = np.array([3, 2, 5, 1, 6, 5])
print("Sorted Table: ", np.sort(table))

## Sorted Table: [1 2 3 5 5 6]

print("Table: ", table)

## Table: [3 2 5 1 6 5]
```

As we can see, the sort() function of NumPy offers a view: the table is not modified, which is not the case if we use the sort() method:

```
table = np.array([3, 2, 5, 1, 6, 5])
table.sort()
print("The array was modified: ", table)

## The array was modified: [1 2 3 5 5 6]
```

9.1.7 Transposition

To obtain the transposition of an array, the attribute T can be used. It should be noted that you get a view of the object: the object is not changed.

```
table = np.array([3, 2, 5, 1, 6, 5])
table.shape = (3,2)
print("Array: \n", table)

## Array:
## [[3 2]
## [5 1]
## [6 5]]
```

```
print("Transposed Array: \n", table.T)
```

```
## Transposed Array:
## [[3 5 6]
## [2 1 5]]
```

The transpose() function of NumPy can also be used:

```
print(np.transpose(table))
```

```
## [[3 5 6]
## [2 1 5]]
```

Be careful, if a name is assigned to the transpose, either by using the attribute T or the method np.transpose(), it creates a reference, not a copy of an element...

```
table_transpose = np.transpose(table)
table_transpose[0,0] = 99
print("Array: \n", table)
```

```
## Array:
## [[99 2]
## [5 1]
```

```
## [ 6 5]]
```

```
print("Transpose of the Array: \n", table_transpose)
```

```
## Transpose of the Array:
## [[99 5 6]
## [ 2 1 5]]
```

To know if an array is a view or not, we can display the base attribute, which returns None if it is not the case:

```
print("table: ", table.base)

## table: None

print("table_transpose : ", table_transpose.base)

## table_transpose : [[99 2]

## [ 5 1]

## [ 6 5]]
```

9.1.8 Operations on Arrays

It is possible to use operators on the tables. Their effect requires some explanation.

9.1.8.1 + and - Operators

When the operator + (-) is used between two tables of the same size, an addition (subtraction) is performed:

```
t_1 = np.array([1, 2, 3, 4])
t_2 = np.array([5, 6, 7, 8])
t_3 = np.array([[1, 2, 3, 4], [5, 6, 7, 8], [9, 10, 11, 12]])
```

[12 13 14 15]]

```
t_4 = np.array([[13, 14, 15, 16], [17, 18, 19, 20], [21, 22, 23, 24]])
t 1 + t 2
## array([ 6, 8, 10, 12])
t_3 + t_4
## array([[14, 16, 18, 20],
           [22, 24, 26, 28],
##
           [30, 32, 34, 36]])
##
t_1 - t_2
## array([-4, -4, -4, -4])
When the operator + (-) is used between a scalar and an array, the scalar is added
(subtracted) to all elements of the array:
print("t_1 + 3 : \n", t_1 + 3)
## t_1 + 3 :
## [4 5 6 7]
print("t_1 + 3. : \n", t_1 + 3.)
## t_1 + 3. :
## [4. 5. 6. 7.]
print("t_3 + 3 : \n", t_3 + 3)
## t_3 + 3 :
## [[ 4 5 6 7]
## [ 8 9 10 11]
```

```
print("t_3 - 3 : \n", t_3 - 3)

## t_3 - 3 :
## [[-2 -1 0 1]
## [ 2 3 4 5]
## [ 6 7 8 9]]
```

9.1.8.2 * and / Operators

When the operator * (/) is used between two tables of the same size, a multiplication (division) forward term is performed:

```
t_1 * t_2

## array([ 5, 12, 21, 32])

t_3 * t_4
```

```
## array([[ 13, 28, 45, 64],
## [ 85, 108, 133, 160],
## [189, 220, 253, 288]])
```

```
t_3 / t_4

## array([[0.07692308, 0.14285714, 0.2 , 0.25 ],
## [0.29411765, 0.33333333, 0.36842105, 0.4 ],
## [0.42857143, 0.45454545, 0.47826087, 0.5 ]])
```

When the operator * (/) is used between a scalar and an array, all the elements of the array are multiplied (divided) by this scalar :

```
print("t_1 * 3 : \n", t_1 * 3)
## t_1 * 3 :
## [ 3 6 9 12]
```

```
print("t_1 / 3 : \n", t_1 / 3)

## t_1 / 3 :
## [0.33333333 0.66666667 1. 1.33333333]
```

9.1.8.3 Power

It is also possible to raise each number in a table to a given power:

```
print("t_1 ** 3 : \n", t_1 ** 3)

## t_1 ** 3 :
## [ 1 8 27 64]
```

9.1.8.4 Operations on Matrices

In addition to the term-by-term operations/subtraction/multiplication/division (or on a scalar), it is possible to perform some calculations on two-dimensional tables (matrices).

We've already seen the transposition of a matrix in Section 9.1.7.

To perform a matrix product, NumPy provides the function dot():

```
np.dot(t_3, t_4.T)
```

```
## array([[150, 190, 230],
## [382, 486, 590],
## [614, 782, 950]])
```

We have to make sure that the matrices are compatible, otherwise, an error will be returned:

```
np.dot(t_3, t_4)
```

```
## Error in py_call_impl(callable, dots$args, dots$keywords):
    ValueError: shapes (3,4) and (3,4) not aligned: 4 (dim 1)
    != 3 (dim 0)
##
## Detailed traceback:
## File "<string>", line 1, in <module>
```

The matrix product can also be obtained using the operator **Q**:

```
t_3 0 t_4.T

## array([[150, 190, 230],
## [382, 486, 590],
```

The product of a vector with a matrix is also possible:

[614, 782, 950]])

```
np.dot(t_1, t_3.T)
## array([ 30, 70, 110])
```

9.1.9 Logical Operators

##

To perform logical tests on the elements of a table, NumPy offers functions, listed in Table 9.1. The result returned by applying these functions is a Boolean array.

Table 9.1: Logical Functions

Description	Code
Greater than	greater()
Greater than or equal to	<pre>greater_equal()</pre>
Lower than	less()
Lower than or equal to	<pre>less_equal()</pre>
Equal to	equal()
Different from	<pre>not_equal()</pre>

Description
Logical And
Logical Or
Logical XOR

For example, to obtain the elements of t between 10 and 20 (included):

9.1.10 Some Constants

NumPy provides some constants, some of which are shown in Table 9.2.

Table 9.2: Formatting Codes

Code	Description
np.inf	Infinity (we get $-\infty$ by writing $-np.inf$ or $np.NINF$)
np.nan	Representation as a floating point number of Not a Number
np.e	Euler constant (e)
np.euler_gamma	Euler-Mascheroni constant (γ)
np.pi	$Pi(\pi)$

We can note the presence of the value NaN, which is a special value among the floating point numbers. The behavior of this constant is special.

When we add, subtract, multiply or divide a number by this NaN value, we obtain NaN:

```
print("Addition : ", np.nan + 1)

## Addition : nan

print("Substraction : ", np.nan - 1)

## Substraction : nan

print("Multiplication : ", np.nan + 1)

## Multiplication : nan

print("Division : ", np.nan / 1)

## Division : nan
```

9.1.11 Universal functions

Universal functions (*ufunc* for *universal functions*) are functions that can be applied term-by-term to the elements of an array. There are two types of universal functions: uannic functions, which perform an operation on a single operand, and binary functions, which perform an operation on two operands.

Among the *ufuncs* are arithmetic operations (addition, multiplication, power, absolute value, etc.) and common mathematical functions (trigonometric, exponential, logarithmic functions, etc.). Table 9.3 lists some universal functions, while Table 9.4 lists some universal binary functions.

Table 9.3: Unary Universal Function

Code	Description
negative(x)	Opposite elements of elements of x
absolute(x)	Absolute values of the elements of x
sign(x)	Signs of the elements of x (0, 1 or -1)
rint(x)	Ronded value of x to the nearest integer
floor(x)	Truncated value of x to the next smaller integer
<pre>ceil(x)</pre>	Truncated value of x to the next larger integer
sqrt(x)	Square root of x
square(x)	Squared value of x
sin(x),	Sine (cosine, and tangent) of the elements of x
cos(x), tan(x)	
sinh(x),	Hyperbolic sine (cosine, and tangent) of the elements of x
cosh(x),	
tanh(x)	
arcsin(x),	Arc-sine (arc-cosine, and arc-tangent) de x
arccos(x),	
arctan(x)	
arcsinh(x),	Hyperbolic arc-sinus (arc-cosine, and arc-tangent) of the
arccosh(x),	elements of x
arctanh(x)	
hypoth(x,y)	Hypotenuse $\sqrt{x^2 + y^2}$
degrees(x)	Conversion of the angles values of ${\tt x}$ from radians to degrees
radians(x)	Conversion of the angles values of \mathbf{x} from degrees to radians
exp(x)	Exponential of the values of x
expm1(x)	$e^x - 1$
log(x)	Natural logarithm of the elements of x
log10(x)	Logatithm of the elements of x in base 10
log2(x)	Logarithm of the elements of x in base 2
log1p(x)	ln(1+x)
exp2(x)	2^x
isnan(x)	Boolean table indicating True for the elements NaN
<pre>isfinite(x)</pre>	Boolean table indicating True for non-infinite and non-NaN elements
isinf(x)	Boolean array indicating True for infinite elements

Table 9.4: Binary Universal Functions

Code	Description
add(x,y)	Term by term addition of the elements of x and y
subtract(x,y)	Term by term substraction of the elements of \mathbf{x} and \mathbf{y}
<pre>multiply(x,y)</pre>	Term by term multiplication of the elements of \mathbf{x} and \mathbf{y}
<pre>divide(x,y)</pre>	Term by term division of the elements of x and y
floor_divide(x	, y Largest integer smaller or equal to the division of the elements
	of x and y
<pre>power(x,y)</pre>	Elements of x to the power of the elements of y
mod(x,y)	Remainder of Euclidean term by term divisions of the eleemnts
	of x by the elements of y
round(x,n)	Rounded value of the elements of x up to n digits
<pre>arctan2(x,y)</pre>	Polar angles of x and y

To use these functions, proceed as in the following example:

[-12, -12, -12, -12]

##

9.1.12 Mathematical and Statistical Methods and Functions

NumPy provides many methods to calculate statistics on all array values, or on one of the array axes (for example on the equivalent of rows or columns in two-dimensional arrays). Some of them are reported in Table 9.5.

Code	Description
sum()	Returns the sum of the elements
<pre>prod()</pre>	Returns the product of the elements
cumsum()	Returns the cumulative sum of the elements
<pre>cumprod()</pre>	Returns the cumulative product of the elements
mean()	Returns the average
<pre>var()</pre>	Returns the variance
std()	Returns the standard error
min()	Returns the minnimum value
max()	Returns the maximum value
argmin()	Returns the index of the first element with the lowest value
argmax()	Returns the index of the first element with the largest value

Table 9.5: Mathematical and Statistical Methods

Let's give an example of the use of these methods:

```
t_1 = np.array([[1, 2, 3, 4], [-1, 6, 7, 8], [9, -1, 11, 12]])
print("t_1 : \n", t_1)

## t_1 :
## [[ 1 2 3 4]
## [-1 6 7 8]
## [ 9 -1 11 12]]

print("Sum of the elements: ", t_1.sum())

## Sum of the elements: 61

print("Covariance of the elements: ", t_1.var())

## Covariance of the elements: 18.0763888888889
```

To apply these functions to a given axis, we modify the value of the argument axis:

```
print("Sum per column: ", t_1.sum(axis=0))

## Sum per column: [ 9  7  21  24]

print("Sum per row: ", t_1.sum(axis=1))

## Sum per row: [10  20  31]
```

 ${\tt NumPy}$ also offers some statistically specific functions, some of which are listed in Table 9.6.

Table 9.6: Statistical Functions

Code	Description
sum(x),	Sum of the elements of x (nansum(x) does not take into
nansum(x)	account NaN values)
mean(x),	Average of x
nanmean()	
median(x),	Median of x
nanmedian()	
average(x)	Average of x (possibility to use weights using the weight
	argument)
min(x), nanmin()	Mininum of x
max(x), nanmax()	Maximum of x
<pre>percentile(x,p),</pre>	P-th percentile of x
nanpercentile(n,p)	
var(x),	Variance of x
nanvar(x)	
<pre>std(x), nanstd()</pre>	Standard-deviation of x
cov(x)	Covariance of x
<pre>corrcoef(x)</pre>	Correlation coefficient

To use the statistical functions:

```
t_1 = np.array([[1, 2, 3, 4], [-1, 6, 7, 8], [9, -1, 11, 12]])
print("t_1 : \n", t_1)

## t_1 :
## [[ 1 2 3 4]
## [-1 6 7 8]
## [ 9 -1 11 12]]
```

```
print("Variance: ", np.var(t_1))
```

```
## Variance: 18.07638888888889
```

If the array has NaN values, for example, to calculate the sum, if sum() is used, the result will be NaN. To ignore the values NaN, we use a specific function (here, nansum()):

```
t_1 = np.array([[1, 2, np.NaN, 4], [-1, 6, 7, 8], [9, -1, 11, 12]])
print("Sum: ", np.sum(t_1))
```

```
## Sum: nan
```

```
print("Sum ignoring NaN values: ", np.nansum(t_1))
## Sum ignoring NaN values: 58.0
```

To calculate a weighted average (let's consider a vector):

```
v_1 = np.array([1, 1, 4, 2])
w = np.array([1, 1, .5, 1])
print("Weighted average: ", np.average(v_1, weights=w))
```

```
## Weighted average: 1.7142857142857142
```

9.2 Generation of Pseudo-random Numbers

The generation of pseudo-random numbers is allowed by the random module of Numpy. The reader interested in the more statistical aspects will be able to find more concepts covered in the stats sub-module of SciPy.

```
from numpy import random
```

Table 9.7 lists some functions that allow to draw numbers in a pseudo-random way with the random module of Numpy (by evaluating random, we get an exhaustive list).

Table 9.7: Some Functions for Pseudo-random Number Generation

Code	Description
rand(size)	Drawing size obs. from a Uniform distribution [0,1]
uniform(a,b,size	TDrawing size obs. from a Uniform distribution $[a; b]$
randint(a,b,size	Drawing size obs. from a Uniform distribution $[a; b[$
<pre>randn(size)</pre>	Drawing size obs. from a Normal distribution $\mathcal{N}(0,1)$
normal(mu,	Drawing size obs. from a Normal distribution with mu mean
std, size)	and standard error std
<pre>binomial(size,</pre>	Drawing size obs. from a Binomial distribution $\mathcal{B}in(n,p)$
n, p)	
beta(alpha,	Drawing size obs. from a Beta distribution $Beta(\alpha, \beta)$
beta, size)	
poisson(lambda,	Drawing size obs. from a Poisson distribution $\mathcal{P}(\lambda)$
size)	
standard_t(df,	Drawing size obs. from a Student distribution $\mathcal{S}t(\mathrm{df})$
size)	

Here is an example of generating pseudo random numbers according to a Gaussian distribution:

A multidimensional array can be generated. For example, a two-dimensional array, in which the first dimension contains 10 elements, each containing 4 random draws according to a $\mathcal{N}(0.1)$:

```
[[ 0.30802506
              1.11662112 -2.08762678 -0.52793389]
   [-0.07997368 0.52742341
                        1.03289108 1.13246365]
##
   ##
   [-0.13972581 \ -1.79977333 \ -2.13167746 \ -0.58245566]
##
   [-0.60448707 1.18512919 0.94176895 -0.6211865 ]
##
##
   [-0.04806523 \quad 0.64177182 \quad 1.39752478 \quad -0.94884771]
   [ 1.49388632 -0.1832472
                         0.50866272 0.77952575]
##
   [-2.34890576 0.54460348
                         0.32012378 1.2872278 ]
##
##
   [0.25163866 - 0.19595951 - 0.14274807 0.71915014]]
```

The generation of numbers is based on a *seed*, i.e. a number that initiates the generator of pseudo random numbers. It is possible to fix this seed, so that reproducible results can be obtained, for example. To do this, we can use the <code>seed()</code> method, to which we indicate a value as an argument:

By fixing the seed again, one will obtain exactly the same draft:

```
np.random.seed(1234)
x = np.random.normal(size=10)
print(x)
```

```
## [ 0.47143516 -1.19097569 1.43270697 -0.3126519 -0.72058873 0.88716294
```

```
## 0.85958841 -0.6365235 0.01569637 -2.24268495]
```

To avoid affecting the global environment by the random seed, the RandomState method of the random sub-module of NumPy can be used:

```
from numpy.random import RandomState
rs = RandomState(123)
x = rs.normal(10)
print(x)
```

```
## 8.914369396699438
```

In addition, the switching() function of the random sub-module allows a random switch:

```
x = np.arange(10)
y = np.random.permutation(x)
print("x : ", x)

## x : [0 1 2 3 4 5 6 7 8 9]

print("y : ", y)

## y : [9 7 4 3 8 2 6 1 0 5]
```

The shuffle() function of the random submodule allows to perform a random permutation of the elements:

```
x = np.arange(10)
print("x avant permutation : ", x)

## x avant permutation : [0 1 2 3 4 5 6 7 8 9]
```

np.random.permutation(x)

```
## array([7, 5, 4, 1, 0, 8, 3, 9, 6, 2])
```

```
print("x après permutation : ", x)
```

```
## x après permutation : [0 1 2 3 4 5 6 7 8 9]
```

9.3 Exercise

First exercise

Consider the following vector: $x = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \end{bmatrix}$

- 1. Create this vector using an array called x.
- 2. Display the type of x and its length.
- 3. Extract the first element, then do the same with the last one.
- 4. Extract the first three elements and store them in a vector called a.
- 5. Extract the 1st, 2nd and 5th elements of the vector (be careful with the positions); store them in a vector called b.
- 6. Add the number 10 to the vector x, then multiply the result by 2.
- 7. Add a and b, comment on the result.
- 8. Make the following addition: x+a; comment on the result, then look at the result of a+x.
- 9. Multiply the vector by the scalar 'c' which will be set to 2.
- 10. Multiply a and b; comment on the result.
- 11. Perform the following multiplication: x*a; comment on the results.
- 12. Retrieve the positions of the multiples of 2 and store them in a vector called ind, then store only the multiples of 2 of x in a vector called mult_2.
- 13. Display the elements of x that are multiples of 3 and multiples of 2.
- 14. Display the elements of x that are multiples of 3 or multiples of 2.
- 15. Calculate the sum of the elements of x.
- 16. Replace the first element of x with a 4.
- 17. Replace the first element of x with the value NaN, then calculate the sum of the elements of x. 18 Delete the vector x.

9.3. EXERCISE

Second exercise

- 1. Create the following matrix: $A = \begin{bmatrix} -3 & 5 & 6 \\ -1 & 2 & 2 \\ 1 & -1 & -1 \end{bmatrix}$.
- 2. Display the size of A, its number of columns, its number of rows and its length.

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- 3. Extract the second column from A, then the first row.
- 4. Extract the element in the third position in the first line.
- 5. Extract the submatrix of dimension 2×2 from the lower corner of A, *i. e.*, $\begin{bmatrix} 2 & 2 & -1 & -1 \end{bmatrix}$.
- 6. Calculate the sum of the columns and then the rows of A.
- 7. Display the diagonal of A.
- 8. Add the vector $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}^{\mathsf{T}}$ \$ to the right of the matrix A and store the result in an object called B.
- 9. Remove the fourth vector from B.
- 10. Remove the first and third lines from B.
- 11. Add scalar 10 to A.
- 12. Add the vector $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}^{\top}$ to A.
- 13. Add the identity matrix I_3 to A.
- 14. Divide all the elements of the matrix A by 2.
- 15. Multiply the matrix **A** by the line vector $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}^{\top}$.
- 16. Display the transposition of A.
- 17. Perform the product with transposition $A^{\top}A$.

Chapter 10

Data manipulation with pandas

pandas is an open-source library based on NumPy providing easy-to-use data structures and data analysis tools. The reader familiar with the basic functions of the R language will find many similar features with pandas.

To access the features of pandas, it is common practice to load the library by assigning it the alias pd:

import pandas as pd

We will also use numpy functions (c.f. Section 9). Let's make sure to load this library, if it hasn't already been done:

import numpy as np

10.1 Structures

We will look at two types of structures, series (series') and dataframes (DataFrame').

10.1.1 Series

Series are one-dimensional tables of indexed data.

10.1.1.1 Creating Series from a List

To create one, we can define a list, then apply the function Series of pandas:

```
s = pd.Series([1, 4, -1, np.nan, .5, 1])
print(s)

## 0    1.0
## 1    4.0
## 2    -1.0
## 3    NaN
## 4    0.5
## 5    1.0
## dtype: float64
```

The previous example shows that the **s** series created contains both the data and an associated index. The **values** attribute is used to display the values that are stored in a **numpy** array:

```
print("values of s: ", s.values)

## values of s: [ 1.   4. -1.   nan   0.5   1. ]

print("type of values of s: ", type(s.values))

## type of values of s: <class 'numpy.ndarray'>
```

The index is stored in a specific structure of pandas:

```
print("index of s: ", s.index)

## index of s: RangeIndex(start=0, stop=6, step=1)

print("type of the index of s: ", type(s.index))

## type of the index of s: <class 'pandas.core.indexes.range.
    RangeIndex'>
```

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It is possible to assign a name to the series as well as to the index:

```
s.name = "my serie"
s.name = "name index"
print("name of the Serie: {} , name of the index: {}".format(s.name, s.index.name))
## name of the Serie: name_index , name of the index: None
print("Serie s: \n", s)
## Serie s:
   0
         1.0
## 1
        4.0
## 2
       -1.0
## 3
       NaN
## 4
       0.5
## 5
      1.0
## Name: name_index, dtype: float64
```

10.1.1.2 Definition of the Index

The index can be defined by the user, at the time of creating the series:

The index can also be defined with numerical values, without being forced to follow a specific order:

The index can be modified later, by overwriting the attribute index:

```
s.index = ["o", "d", "i", "l"]
print("Série s : \n", s)

## Série s :
## o   1.0
## d  4.0
## i  -1.0
## l  NaN
## dtype: float64
```

10.1.1.3 Creation of Special Series

A simple trick to creating series with a repeated value consists in providing a scalar to the Series function of NumPy and an index whose length will correspond to the number of times the scalar is repeated:

A series can be created from a dictionary:

```
## King Arthur
## Knight_Round_Table Percival
## Druid Merlin
## dtype: object
```

As noted in the previous output, the dictionary keys were used for the index. When creating the series, specific values can be specified in the key argument: this will result in retrieving only the observations corresponding to these keys:

10.1.2 Dataframes

Dataframes correspond to the data format traditionally found in economics, twodimensional tables, with column variables and observations in rows. The columns and rows of the dataframes are indexed.

10.1.2.1 Creating Dataframes from a Dictionary

To create a dataframe, the DataFrame() function of pandas can be provided with a dictionary that can be transformed into a series. This is the case of a dictionary where the values associated with the keys are all the same length:

```
##
                  weight
        height
## 0
             58
                      115
## 1
             59
                      117
##
  2
             60
                      120
##
             61
                      123
             62
## 4
                      126
## 5
             63
                      129
  6
             64
                      132
##
             65
##
  7
                     135
## 8
             66
                      139
##
  9
             67
                      142
## 10
             68
                      146
## 11
             69
                      150
             70
## 12
                     154
## 13
             71
                      159
## 14
             72
                      164
```

The position of the elements in the dataframe serves as an index. As for the series, the values are accessible in the values attribute and the index in the index attribute. The columns are also indexed:

print(df.columns)

```
## Index(['height', 'weight'], dtype='object')
```

The head() method displays the first few lines (the first 5, by default). You can modify its n arguments to indicate the number of lines to be returned:

df.head(2)

```
## height weight
## 0 58 115
## 1 59 117
```

When creating a dataframe from a dictionary, if the name of the columns to be imported is specified by a list of strings provided in the columns argument of the DataFrame function, it is possible to define not only the columns to be filled but also their order of appearance.

For example, to import only the weight column:

```
df = pd.DataFrame(dict, columns = ["weight"])
print(df.head(2))
```

```
## weight
## 0 115
## 1 117
```

And to define the order in which the columns will appear:

```
df = pd.DataFrame(dict, columns = ["weight", "height"])
print(df.head(2))
```

```
## weight height
## 0 115 58
## 1 117 59
```

i -1.0

If a column name that is missing from the dictionary keys is specified, the resulting dataframe will contain a column with this name but filled with the values NaN:

```
df = pd.DataFrame(dict, columns = ["weight", "height", "age"])
print(df.head(2))

## weight height age
## 0 115 58 NaN
## 1 117 59 NaN
```

10.1.2.2 Creating Dataframes from Series

A dataframe can be created from a series:

If the series is not named, the columns argument of the DataFrame function must not be filled in. But in this case, the column will not have a name, just a numerical index.

```
s = pd.Series([1, 4, -1, np.nan], index = ["o", "d", "i", "l"])
df = pd.DataFrame(s)
print(df)

## 0
## 0 1.0
## d 4.0
```

```
## 1 NaN
```

```
print(df.columns.name)
```

None

10.1.2.3 Creating Dataframes from a Dictionary List

A dataframe can be created from a list of dictionaries:

```
dico_1 = {
    "Name": "Pendragon",
    "Surname": "Arthur",
    "Role": "King of Britain"
}
dico_2 = {
    "Name": "",
    "Surname": "Perceval",
    "Role": "Knight of the Round Table"
}
df = pd.DataFrame([dico_1, dico_2])
print(df)
```

```
## Name Role Surname
## 0 Pendragon King of Britain Arthur
## 1 Knight of the Round Table Perceval
```

If some keys are missing in one or more of the dictionaries in the list, the corresponding values in the dataframe will be NaN:

```
dico_3 = {
    "Surname": "Guinevere",
    "Role": "Queen of Britain"
}
```

```
df = pd.DataFrame([dico_1, dico_2, dico_3])
print(df)

## Name Role Surname
## 0 Pendragon King of Britain Arthur
## 1 Knight of the Round Table Perceval
## 2 NaN Queen of Britain Guinevere
```

10.1.2.4 Création de dataframes à partir d'un dictionnaire de séries

A dataframe can also be created from a series dictionary. To illustrate the method, let's create two dictionaries:

```
# Annual 2017 GDP
# In millions of current dollars
dict_gdp_current = {
    "France": 2582501.31,
    "USA": 19390604.00,
    "UK": 2622433.96
}
# Annual consumer price index
dict_cpi = {
    "France": 0.2,
    "UK": 0.6,
    "USA": 1.3,
    "Germany": 0.5
}
```

From these two dictionaries, let's create two corresponding series:

France 2582501.31 0.2

NaN 0.5

Germany

```
## UK
               2622433.96
## dtype: float64
print("\ns_cpi : \n", s_cpi)
## s_cpi :
## France 0.2
## UK
               0.6
## USA 1.3
## Germany 0.5
## dtype: float64
Then, let's create a dictionary of series:
dict_from_series = {
    "gdp": s_gdp_current,
    "cpi": s_cpi
}
print(dict_from_series)
## {'gdp': France 2582501.31
## USA 19390604.00
## UK 2622433.96
## dtype: float64, 'cpi': France 0.2
## UK
              0.6
               1.3
## USA
## Germany 0.5
## dtype: float64}
Finally, let's create our dataframe:
s = pd.DataFrame(dict_from_series)
print(s)
##
                      gdp cpi
```

```
## UK 2622433.96 0.6
## USA 19390604.00 1.3
```

Remark 10.1.1

The dict_gdp_current dictionary does not contain a Germany key, unlike the dict_cpi dictionary. When the dataframe was created, the GDP value for Germany was therefore assigned as NaN.

10.1.2.5 Creation of Dataframes from a Two-dimensional NumPy Array

A dataframe can also be created from a Numpy array. When creating, with the function DataFrame() of Numpy, it is possible to specify the name of the columns (otherwise, the indication of the columns will be numerical):

```
listing = [
    [1, 2, 3],
    [11, 22, 33],
    [111, 222, 333],
    [1111, 2222, 3333]
٦
array np = np.array(listing)
df = pd.DataFrame(array_np,
                  columns = ["a", "b", "c"])
print(df)
##
                 b
          а
                 2
## 0
          1
                        3
## 1
         11
                22
                       33
## 2
        111
               222
                      333
## 3 1111
              2222
                     3333
```

10.1.2.6 Dimensions

The dimensions of a dataframe are accessed with the attribute shape.

```
print("shape : ", df.shape)
## shape : (4, 3)
```

The number of lines can also be displayed as follows:

```
print("shape : ", len(df))
## shape : 4
```

And the number of columns:

```
print("shape : ", len(df.columns))
## shape : 3
```

10.1.2.7 Modification of the Index

As for the series, the index can be modified once the dataframe has been created, by overwriting the values of the attributes index and columns, for the index of rows and columns, respectively:

```
df.index = ["o", "d", "i", "l"]
df.columns = ["aa", "bb", "cc"]
print(df)
```

```
## aa bb cc
## o 1 2 3
## d 11 22 33
## i 111 222 333
## l 1111 222 3333
```

10.2 Selection

In this section, we look at different ways to select data in series and dataframes. There are two distinct ways to do this:

- a first one based on the use of brackets directly on the object for which we want to select certain parts;
- second based on indexers, accessible as attributes of NumPy objects (loc, at, iat, iat, etc.)

The second method avoids some confusion that may appear in the case of numerical indexes.

10.2.1 For Series

First, let's look at ways to extract values from series.

10.2.1.1 With brackets

The index can be used to extract the data:

```
s = pd.Series([1, 4, -1, np.nan, .5, 1])
s[0] # 1st element of s
## 1.0
```

```
s[1:3] # From the 2nd (included) to the 4th (not included)
```

```
## 1 4.0
## 2 -1.0
## dtype: float64
```

s[[0,4]] # First to 5th element (not included)

```
## 0 1.0
## 4 0.5
```

```
## dtype: float64
```

Note that unlike 'numpy' tables or lists, negative values for the index cannot be used to retrieve data by counting their position relative to the end:

s[-2]

o 1.0

```
## Error in py_call_impl(callable, dots$args, dots$keywords):
   KeyError: −2
##
## Detailed traceback:
    File "<string>", line 1, in <module>
     File "/anaconda3/lib/python3.6/site-packages/pandas/core/
   series.py", line 766, in __getitem__
       result = self.index.get_value(self, key)
##
     File "/anaconda3/lib/python3.6/site-packages/pandas/core/
   indexes/base.py", line 3103, in get_value
       tz=getattr(series.dtype, 'tz', None))
##
     File "pandas/_libs/index.pyx", line 106, in pandas._libs.
   index.IndexEngine.get_value
##
     File "pandas/_libs/index.pyx", line 114, in pandas._libs.
  index.IndexEngine.get_value
    File "pandas/_libs/index.pyx", line 162, in pandas._libs.
##
   index.IndexEngine.get_loc
    File "pandas/_libs/hashtable_class_helper.pxi", line 958,
##
   in pandas._libs.hashtable.Int64HashTable.get_item
    File "pandas/_libs/hashtable_class_helper.pxi", line 964,
##
    in pandas._libs.hashtable.Int64HashTable.get_item
```

In the case of an index composed of strings, it is then possible to refer either to the content of the index (to make it simple, its name) or to its position when extracting the data from the series:

```
## d
        4.0
## i
       -1.0
## 1
       NaN
## dtype: float64
print('s["d"] : \n', s["d"])
## s["d"] :
## 4.0
print('s[1] : \n', s[1])
## s[1] :
## 4.0
print("elements o and i : \n", s[["o", "i"]])
## elements o and i :
## o 1.0
## i -1.0
## dtype: float64
```

On the other hand, in the case where the index is defined with numerical values, to extract the values using the brackets, it will be by the value of the index and not by relying on the position:

4.0

10.2.1.2 With Indexers

Pandas offers two types of multi-axis indication: loc, iloc. The first is mainly based on the use of axis labels, while the second is mainly based on positions using integers.

For the purposes of this section, let's create two series; one with a textual index, the other with a numerical index:

10.2.1.2.1 Extraction of a Single Element

To extract an object with loc, we use the name of the index:

```
print(s_num.loc[5], s_text.loc["c"])
## 1.0 1.0
```

To extract a single element with iloc, simply indicate its position:

```
(s_num.iloc[1], s_text.iloc[1])
## (4.0, 4.0)
```

10.2.1.2.2 Extraction of Several Elements

To extract several elements with loc, we use the names (labels) of the indices, which we provide in a list:

```
print("elements with labels 5 and 4:\n", s_num.loc[[5,4]])

## elements with labels 5 and 4:
## 5    1.0
## 4   -1.0
## dtype: float64
```

```
print("elements with labels c and b: \n", s_text.loc[["c", "b"]])
## elements with labels c and b:
## c 1.0
## b -1.0
## dtype: float64
To extract multiple elements with iloc:
print("elements at positions 0 and 2:\n", s_num.iloc[[0,2]])
## elements at positions 0 and 2:
## 5 1.0
## 4 -1.0
## dtype: float64
print("elements at positions 0 and 2: \n", s_text.iloc[[0,2]])
## elements at positions 0 and 2:
## c 1.0
## b -1.0
## dtype: float64
```

10.2.1.2.3 Slicing

It is possible to perform series slicing, to recover consecutive elements:

```
print("elements with label 5 to 4:\n", s_num.loc[5:4])
```

```
## elements with label 5 to 4:
## 5   1.0
## 0   4.0
## 4  -1.0
## dtype: float64
```

```
print("elements with label c to b: \n", s_text.loc["c":"b"])
## elements with label c to b:
## c 1.0
## a 4.0
## b -1.0
## dtype: float64
To extract multiple elements with iloc:
print("elements at positions 0 and 2:\n", s_num.iloc[0:2])
## elements at positions 0 and 2:
## 5 1.0
## 0
        4.0
## dtype: float64
print("elements at positions 0 and 2: \n", s_text.iloc[0:2])
## elements at positions 0 and 2:
## c 1.0
## a 4.0
## dtype: float64
As we have seen so far, the upper limit value is not included in the breakdown.
```

10.2.1.2.4 Mask

A mask can also be used to extract elements, either using loc or iloc:

```
print("\n",s_num.loc[[True, False, False, True]])
```

```
##
## 5 1.0
## 1 NaN
## dtype: float64
```

```
print("\n", s_text.loc[[True, False, False, True]])
##
##
    С
          1.0
## d
         NaN
## dtype: float64
print("\n", s num.iloc[[True, False, False, True]])
##
##
    5
          1.0
## 1
         NaN
## dtype: float64
print("\n", s text.iloc[[True, False, False, True]])
##
##
          1.0
## d
         NaN
## dtype: float64
```

10.2.1.2.5 What's the Point?

Why introduce such ways of extracting data and not just extract it using the brackets on the objects? Let's look at a simple example. Let's assume that we have the s_num series, with an index composed of integers that is not a sequence ranging from 0 to the number of elements. In this case, if we want to recover the 2nd element, because of the index composed of numerical values, we cannot obtain it by asking s[1]. To extract the 2nd of the series, we must know that its index is 0 and thus ask:

```
print("The element whose index is 0: ", s_num[0])
## The element whose index is 0: 4.0
```

To be able to perform the extraction according to the position, it is very useful to have this attribute iloc:

```
print("The element in 2nd position:", s_num.iloc[1])
## The element in 2nd position: 4.0
```

10.2.2 For dataframes

Now let's look at different ways to extract data from a dataframe. Let's create two dataframes as an example, one with a numerical index; another with a textual index:

```
## df_num :
##
       height
               weight
                        age
                             taille
## 0
         58
                 115
                        28
                               162
## 1
          59
                 117
                        33
                               156
## 2
          60
                 120
                        31
                               172
         61
                        31
## 3
                 123
                               160
         62
## 4
                 126
                        29
                               158
```

```
print("df_text : \n", df_text)

## df_text :
## height weight age taille
```

```
## a
         58
                  115
                         28
                                 162
          59
                                 156
## e
                  117
                         33
          60
                  120
                                 172
## c
                         31
## b
          61
                  123
                         31
                                 160
```

```
## d 62 126 29 158
```

To make it simple, when we want to perform an extraction with the iloc attributes, the syntax is as follows:

```
df.iloc[line_selection, column_selection]
```

with line_selection:

- a single value: 1 (second line);
- a list of values: [2, 1, 3] (3rd line, 2nd line and 4th line);
- a breakdown: [2:4] (from the 3rd line to the 4th line (not included)).

for column selection:

- a single value: 1 (second column);
- a list of values: [2, 1, 3] (3rd column, 2nd column and 4th column);
- a breakdown: [2:4] (from the 3rd column to the 4th column (not included)).

With loc, the syntax is as follows:

```
df.loc[line selection, column selection]
```

with line selection:

- a single value: 'a'' (line nameda');
- a list of names: ["a", "c", "b"] (Rows named "a", "c" and "b");
- a mask: df.['a']<10 (Rows for which the mask values are True).

with column selection:

- a single value: 'a'' (column nameda');
- a list of values: ["a", "c", "b"] (columns named "a", "c" and "b");
- a breakdown: '["a": "c"] (from the column named "a" to the column named "c").

10.2.2.1 Extraction of a Rows

To extract a Rows from a dataframe, the name of the Rows can be used with loc:

```
print("Rows named 'e':\n", df_text.loc["e"])
## Rows named 'e':
## height 59
## weight 117
## age
            33
## taille
           156
## Name: e, dtype: int64
print("\nRows named 'e':\n", df num.loc[1])
## Rows named 'e':
## height 59
## weight 117
## age
            33
## taille 156
## Name: 1, dtype: int64
Or, its position with iloc:
print("Rows in position 0:\n", df_text.iloc[0])
## Rows in position 0:
## height 58
## weight 115
## age
            28
## taille
           162
## Name: a, dtype: int64
print("\nRows in position 0:\n", df_num.iloc[0])
## Rows in position 0:
## height 58
## weight 115
## age
             28
```

```
## taille 162
## Name: 0, dtype: int64
```

10.2.2.2 Extraction of Several Rows

To extract multiple lines from a dataframe, their names can be used with loc (in an array):

```
print("Rows named a and c:\n", df_text.loc[["a", "c"]])

## Rows named a and c:
## height weight age taille
## a 58 115 28 162
## c 60 120 31 172
```

```
print("\nRows named 0 and 2:\n", df_num.loc[[0, 2]])

##

## Rows named 0 and 2:

## height weight age taille

## 0 58 115 28 162

## 2 60 120 31 172
```

Or, their position with iloc:

```
print("Rows at positions 0 and 3:\n", df_text.iloc[[0, 3]])

## Rows at positions 0 and 3:
## height weight age taille
## a 58 115 28 162
## b 61 123 31 160
```

```
print("\nRows at positions 0 and 3:\n", df_num.iloc[[0, 3]])
```

```
##
## Rows at positions 0 and 3:
## height weight age taille
## 0 58 115 28 162
## 3 61 123 31 160
```

10.2.2.3 Slicing of Several Rows

A line sequence can be retrieved by delimiting the first and last line to be retrieved according to their name and using loc:

```
print("Rows from label à to c:\n", df text.loc["a":"c"])
## Rows from label à to c:
##
       height
                weight
                         age
                               taille
           58
## a
                   115
                         28
                                 162
## e
           59
                   117
                         33
                                 156
## c
           60
                   120
                         31
                                 172
```

```
print("\nRows from label 0 to 2:\n", df_num.loc[0:2])
##
## Rows from label 0 to 2:
       height weight
                         age
                              taille
## 0
          58
                  115
                         28
                                162
## 1
           59
                  117
                         33
                                 156
## 2
           60
                  120
                         31
                                 172
```

With the attribute iloc, this is also possible (again, the upper bound is not included):

```
print("Rows at position 0 to 3 (not included):\n", df_text.iloc[0:3])
## Rows at position 0 to 3 (not included):
##
       height weight
                              taille
                         age
           58
                  115
                         28
                                162
## a
                  117
                                156
## e
           59
                         33
```

```
## c 60 120 31 172
```

```
print("\nRows at position 0 to 3 (not included):\n", df_num.iloc[0:3])
##
## Rows at position 0 to 3 (not included):
       height weight
                        age
                            taille
          58
                        28
## 0
                  115
                                162
## 1
          59
                  117
                        33
                                156
## 2
          60
                  120
                        31
                                172
```

10.2.2.4 Mask

A mask can also be used to select certain rows For example, if we want to retrieve the rows for which the variable height has a value greater than 60, we use the following mask:

```
mask = df_text["height"] > 60
print(mask)
```

```
## a False
## e False
## c False
## b True
## d True
## Name: height, dtype: bool
```

To filter:

print(df_text.loc[mask])

```
## height weight age taille
## b 61 123 31 160
## d 62 126 29 158
```

10.2.2.5 Extraction of a Single Column

To extract a column from a dataframe, we can use square brackets and refer to the name of the column (which is indexed by names):

```
print(df_text['weight'].head(2))

## a     115
## e     117
## Name: weight, dtype: int64
```

By selecting a single column, we obtain a series (the dataframe index is kept for the series):

```
print(type(df_text['weight']))
## <class 'pandas.core.series.Series'>
```

A column can also be extracted by referring to the attribute of the dataframe named after this column:

```
print(df_text.weight.head(2))

## a 115
## e 117

## Name: weight, dtype: int64
```

As for the series, we can rely on the attributes loc and iloc:

```
print("Column 2 (loc):\n", df_text.loc[:,"weight"])

## Column 2 (loc):
## a 115
## e 117
## c 120
## b 123
## d 126
## Name: weight, dtype: int64
```

print("Column 2 (iloc):\n", df_text.iloc[:,1]) ## Column 2 (iloc): ## a 115 ## e 117 ## c 120 ## b 123 ## d 126 ## Name: weight, dtype: int64

10.2.2.6 Extraction of Several Columns

To extract several columns, the names of the columns can be placed in a table:

```
print(df_text[["weight", "height"]])
```

```
##
       weight
               height
## a
          115
                     58
## e
          117
                     59
          120
                     60
## c
## b
          123
                     61
## d
          126
                     62
```

The order in which these columns are called corresponds to the order in which they will be returned.

Again, we can use the loc attribute (we use the colon here to specify that we want all the lines):

```
print("Columns from weight to height:\n", df_text.loc[:,["weight", "height"]])
```

```
## Columns from weight to height:
## weight height
## a 115 58
## e 117 59
## c 120 60
## b 123 61
```

```
## d 126 62
```

And the iloc attribute:

```
print("Columns 2 and 1 :\n", df num.iloc[:,[1,0]])
## Columns 2 and 1 :
##
        weight
                 height
## 0
          115
                    58
## 1
          117
                    59
## 2
          120
                    60
## 3
          123
                    61
## 4
          126
                    62
```

10.2.2.7 Slicing Several Columns

To perform a slice, the attributes loc and iloc can be used. We must be careful as the names of the columns used for the breakdown are not placed in a table here:

With loc:

```
print("Columns 2 and 2:\n", df text.loc[:, "height":"age"])
## Columns 2 and 2:
##
        height
                 weight
                          age
## a
           58
                   115
                          28
## e
           59
                   117
                          33
## c
           60
                   120
                          31
           61
                   123
                          31
## b
## d
           62
                   126
                          29
```

And with the iloc attribute:

```
## Columns from position 0 to 2 (not included) :
##
       height weight
## a
          58
                  115
          59
                  117
## e
          60
## c
                  120
          61
## b
                  123
## d
          62
                  126
```

10.2.2.8 Extraction of Rows and Columns

Now that we have reviewed multiple ways to select one or more rows or columns, we can also mention that it is possible to make selections of columns and rows in the same instruction.

For example, with iloc, let's select the rows from position 0 to position 2 (not included) and the columns from position 1 to 3 (not included):

```
print(df_text.iloc[0:2, 1:3])
```

```
## weight age
## a 115 28
## e 117 33
```

With loc, let's select the rows named a and c and the columns from the one named weight to age.

```
df_text.loc[["a", "c"], "weight":"age"]
```

```
## weight age
## a 115 28
## c 120 31
```

4

62

126

29

10.3 Renaming Columns in a Dataframe

To rename a column in a dataframe, pandas offers the method rename(). Let's take an example with our df dataframe:

```
dict = {"height" : [58, 59, 60, 61, 62],
        "weight": [115, 117, 120, 123, 126],
        "age": [28, 33, 31, 31, 29],
        "taille": [162, 156, 172, 160, 158],
df = pd.DataFrame(dict)
print(df)
##
      height
               weight
                         age
                              taille
## 0
           58
                   115
                          28
                                  162
           59
                   117
                          33
                                  156
## 2
           60
                   120
                          31
                                  172
## 3
           61
                   123
                          31
                                  160
```

Let's rename the column taille to height, using a dicionnaire specified in the argument columns, with as key the current name of the column, and value the new name:

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```
df.rename(index=str, columns={"taille": "height"}, inplace=True)
print(df)
##
      height
               weight
                        age
                              height
          58
                   115
                         28
                                 162
## 0
## 1
           59
                   117
                         33
                                  156
## 2
           60
                   120
                          31
                                  172
## 3
           61
                   123
                         31
                                  160
## 4
           62
                   126
                         29
                                  158
```

For the change to be effective, the argument inplace is set to True, otherwise the change is not made to the dataframe.

To rename several columns at the same time, we can provide several pairs of value keys in the dictionary:

```
weight_pounds
##
      height
                                years
                                         height
## 0
           58
                           115
                                    28
                                            162
## 1
           59
                           117
                                    33
                                            156
## 2
           60
                           120
                                    31
                                            172
           61
                           123
## 3
                                    31
                                            160
## 4
           62
                           126
                                    29
                                            158
```

10.4 Filtering

To filter the data in a table, depending on the values encountered for some variables, masks are used, as indicated in Section 10.2.2.4.

Let's look at some examples here, by redefining our dataframe:

```
##
      height
               weight
                        age
                              height_cm
## 0
           58
                   115
                          28
                                     162
## 1
           59
                   117
                          33
                                     156
## 2
           60
                                     172
                   120
                         31
## 3
           61
                   123
                          31
                                     160
## 4
           62
                   126
                          29
                                     158
```

The idea is to create a mask returning a series containing Boolean values, one per line. When the value of the mask line is set to True, the dataframe line on which the

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mask will be applied will be retained, while it will not be retained when the value of the mask line is set to False.

Let's look at a simple example, in which we want to keep observations only for which the value of the age variable is less than 30:

Then, we simply have to apply this mask, with loc. We want all the columns, but only a few rows:

```
print(df.loc[mask])
```

```
## height weight age height_cm
## 0 58 115 28 162
## 4 62 126 29 158
```

Note: it also works without loc:

print(df[mask])

```
## height weight age height_cm
## 0 58 115 28 162
## 4 62 126 29 158
```

More simply, we can use the query() method of pandas. A Boolean expression to be evaluated is provided for this method to filter the data:

```
print(df.query("age<30"))
## height weight age height_cm</pre>
```

```
## 0 58 115 28 162
## 4 62 126 29 158
```

The query can be a little more complex, by combining comparison operators (see Section 4.2) and logical operators (see Section 4.3). For example, suppose that we want to filter the dataframe values to retain only those observations for which the size is less than or equal to 62 and the mass is strictly greater than 120. The request would then be:

```
print(df.query("weight > 120 and height < 62"))

## height weight age height_cm
## 3 61 123 31 160</pre>
```

It can be noted that the following instruction gives the same result:

```
print(df.query("weight > 120").query("height < 62"))

## height weight age height_cm
## 3 61 123 31 160</pre>
```

10.4.1 Checking whether a value belongs to dataframe

To create a mask indicating whether the values of a series or dataframe belong to a set, the isin() method can be used. For example, let's return a mask indicating if the values in the height column of df are in the range [59,60]:

```
df.height.isin(np.arange(59,61))
```

```
## 0 False
## 1 True
## 2 True
## 3 False
## 4 False
## Name: height, dtype: bool
```

10.5 Missing Values

In economics, it is quite common to face incomplete data. The way missing data is managed by pandas is the use of two special values: None and NaN.

The value None can be used in the tables NumPy only when the type of the latter is object.

```
table_none = np.array([1, 4, -1, None])
print(table_none)

## [1 4 -1 None]
```

```
print(type(table_none))
```

```
## <class 'numpy.ndarray'>
```

With an array of type object, operations performed on the data will be less efficient than with a numerical array. (VanderPlas 2016, p 121).

The value NaN is a floating point number value (see Section 9.1.10). NumPy manages it differently from NaN, and does not assign an object pass type from the start in the presence of NaN:

```
table_none = np.array([1, 4, -1, np.nan])
print(table_none)
```

```
## [ 1. 4. -1. nan]
```

print(type(table_none))

```
## <class 'numpy.ndarray'>
```

With pandas, these two values, None and NaN can be present:

```
s = pd.Series([1, None, -1, np.nan])
print(s)

## 0    1.0
## 1    NaN
## 2    -1.0
## 3    NaN
## dtype: float64

print(type(s))

## <class 'pandas.core.series.Series'>
```

This also applies to dataframes:

```
##
     height weight
                  age height_cm
## 0
      58.0
             115
                            162
                  28.0
## 1
      59.0
              117 33.0
                            156
## 2 60.0
              120 31.0
                            172
## 3 61.0
             123 NaN
                            160
## 4 NaN 126 29.0
                            158
```

However, it should be noted that only the type of variables for which missing values exist are passed to float64:

print(df.dtypes)

```
## height float64
## weight int64
```

```
## age float64
## height_cm int64
## dtype: object
```

Remark 10.5.1

Note that the data is recorded on a float64 type. When working on a table with no missing values, whose type is int or bool, if a missing value is entered, pandas will change the data type to float64 and object, respectively.

pandas offers different ways to handle missing values.

10.5.1 Identify Missing Values

With the isnull() method, a boolean mask is returned, indicating True for observations with the value NaN or None:

print(s.isnull())

```
## 0 False
## 1 True
## 2 False
## 3 True
## dtype: bool
```

To know if a value is not zero, the notnull() method can be used:

print(s.notnull())

```
## 0 True
## 1 False
## 2 True
## 3 False
## dtype: bool
```

10.5.2 Remove Observations with Missing Values

The dropna() method allows to remove observations with null values:

print(df.dropna())

##		height	weight	age	height_cm
##	0	58.0	115	28.0	162
##	1	59.0	117	33.0	156
##	2	60.0	120	31.0	172

10.5.3 Removing Missing Values by Other Values

To replace missing values with other values, pandas proposes to use the method fillna():

print(df.fillna(-9999))

##		height	weight	age	height_cm
##	0	58.0	115	28.0	162
##	1	59.0	117	33.0	156
##	2	60.0	120	31.0	172
##	3	61.0	123	-9999.0	160
##	4	-9999.0	126	29.0	158

10.6 Deletions

To delete a value on one of the axes of a series or dataframe, NumPy offers the method drop().

10.6.1 Deleting Elements in a Series

To illustrate how the drop() method works, let's create a series with a numerical index, another with a textual index:

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An element can be deleted from a series by using its name:

```
print("for s_num: \n", s_num.drop(5))

## for s_num:
## 0     4.0
## 4     -1.0
## 1     NaN
## dtype: float64

print("\nfor s_text: \n", s_text.drop("c"))

##
## for s_text:
## a     4.0
## b     -1.0
## d     NaN
## dtype: float64
```

We can also retrieve the name according to the position, by going through a detour using the index() method:

```
print("s_num.index[0]: ", s_num.index[0])

## s_num.index[0]: 5

print("s_text.index[0]: ", s_text.index[0])

## s_text.index[0]: c
```

```
print("for s_num: \n", s_num.drop(s_num.index[0]))

## for s_num:
## 0    4.0
## 4   -1.0
## 1    NaN
## dtype: float64

print("\nfor s_text: \n", s_text.drop(s_text.index[0]))

##
## for s_text:
## a    4.0
## b   -1.0
## d    NaN
## dtype: float64
```

To delete several elements, we can provide several index names in a list using the drop() method:

```
print("for s_num: \n", s_num.drop([5, 4]))

## for s_num:
## 0     4.0

## 1     NaN

## dtype: float64

print("\nfor s_text: \n", s_text.drop(["c", "b"]))

##

## for s_text:
## a     4.0

## d     NaN

## dtype: float64
```

Again, we can retrieve the name according to the position, by going through a detour using the index() method:

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```
print("s_num.index[[0,2]]: ", s_num.index[[0,2]])
## s_num.index[[0,2]]: Int64Index([5, 4], dtype='int64')
print("s_text.index[[0,2]]: ", s_text.index[[0,2]])
## s_text.index[[0,2]]: Index(['c', 'b'], dtype='object')
print("for s_num: \n", s_num.drop(s_num.index[[0,2]]))
## for s_num:
## 0 4.0
## 1
       NaN
## dtype: float64
print("\nfor s text: \n", s text.drop(s text.index[[0,2]]))
##
## for s text:
## a
        4.0
## d
        NaN
## dtype: float64
```

It is also possible to use a slicing to obtain the series without the element(s) (See Section 10.2.1.2.3)

10.6.2 Deleting Elements in a Dataframe

To illustrate how the drop() method works on a dataframe, let's create one:

10.6.2.1 Deleting Rows

To delete a row from a dataframe, we can refer to its name (here, the names are numbers, but they are labels):

```
print("Delete the first row: \n", df.drop(0))
## Delete the first row:
##
       height weight
                        age
                              height_cm
## 1
        59.0
                 117
                       33.0
                                   156
## 2
        60.0
                 120 31.0
                                   172
## 3
        61.0
                 123
                                   160
                       NaN
## 4
        NaN
                 126 29.0
                                   158
```

If the rows have text labels, they can first be retrieved using the index() method:

```
label_pos_0 = df.index[0]
print("Delete the first row: \n", df.drop(label_pos_0))
## Delete the first row:
       height weight
                        age
                              height_cm
## 1
        59.0
                 117
                       33.0
                                   156
## 2
        60.0
                 120
                       31.0
                                   172
## 3
       61.0
                 123
                       NaN
                                   160
                 126
                       29.0
                                   158
## 4
        NaN
```

To delete several rows, the name of these rows in a list is given to the drop() method:

```
print("Delete the 1st and 4th rows: \n", df.drop([0,3]))
```

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```
## Delete the 1st and 4th rows:
       height weight
                         age height_cm
## 1
        59.0
                 117
                       33.0
                                   156
## 2
        60.0
                 120
                       31.0
                                   172
## 4
         NaN
                 126
                       29.0
                                   158
```

Or, by indicating the positions of the lines:

```
label pos = df.index[[0, 3]]
print("Delete the 1st and 4th rows:
                                  \n", df.drop(label pos))
## Delete the 1st and 4th rows:
                               height_cm
       height weight
                          age
        59.0
                  117
                       33.0
## 1
                                    156
## 2
        60.0
                  120
                       31.0
                                    172
## 4
        NaN
                  126 29.0
                                    158
```

It is also possible to use a slicing to obtain the series without the element(s) (See Sections 10.2.2.3 et 10.2.2.7)

10.6.2.2 Deleting Columns

To delete a column from a dataframe, we proceed in the same way as for rows, but by adding the parameter <code>axis=1</code> to the method <code>drop()</code> to specify that we are interested in the columns:

```
print("Delete the first column: \n", df.drop("height", axis=1))
## Delete the first column:
##
       weight
                 age
                     height_cm
## 0
         115
               28.0
                            162
## 1
         117
              33.0
                            156
## 2
         120
              31.0
                            172
## 3
         123
               NaN
                            160
## 4
         126
               29.0
                            158
```

We can first retrieve the labels of the columns according to their position using the method columns():

```
label_pos = df.columns[0]
print("label_pos : ", label_pos)
## label_pos : height
print("Delete the first column: \n", df.drop(label_pos, axis=1))
## Delete the first column:
##
       weight
                     height_cm
                 age
## 0
         115
               28.0
                           162
         117
## 1
              33.0
                           156
## 2
         120 31.0
                           172
## 3
         123 NaN
                           160
## 4
         126 29.0
                           158
```

To delete several columns, the names of these columns are given in a list in the drop() method:

```
print("Delete the 1st and 4th columns: \n",
df.drop(["height", "height_cm"], axis = 1))
## Delete the 1st and 4th columns:
##
       weight
                 age
## 0
         115 28.0
         117 33.0
## 1
## 2
         120
              31.0
## 3
         123
              NaN
## 4
         126
              29.0
```

Or, by indicating the positions of the columns:

```
label_pos = df.columns[[0, 3]]
print("Delete the 1st and 4th columns: \n", df.drop(label_pos, axis=1))
## Delete the 1st and 4th columns:
```

```
##
        weight
                   age
## 0
          115
                28.0
## 1
          117
                33.0
## 2
          120
                31.0
## 3
          123
                 NaN
## 4
          126
                29.0
```

It is also possible to use a slicing to obtain the series without the element(s) (c.f. Sections 10.2.2.3 and 10.2.2.7)

10.7 Replacing Values

We will now look at how to modify one or more values, in the case of a series and then a dataframe.

10.7.1 For a Series

To modify a particular value in a series or dataframe, the equal symbol (=) can be used, having previously targeted the location of the value to be modified, using the extraction techniques explained in Section 10.2.

For example, let's consider the following series:

Let's modify the second element of s num, to give it the value -3:

```
s_num.iloc[1] = -3
print("s_num: ", s_num)

## s_num: 5   1.0
## 0  -3.0
## 4  -1.0
## 1  NaN
## dtype: float64
```

It is of course possible to modify several values at the same time.

Again, all we need to do is target the positions (there are many ways to do this) and provide an object of equivalent dimensions to replace the targeted values. For example, in our s_num series, we will replace the values in position 1 and 3 (2nd and 4th values) with -10 and -9:

```
s_num.iloc[[1,3]] = [-10, -9]
print(s_num)

## 5    1.0
## 0   -10.0
## 4   -1.0
## 1   -9.0
## dtype: float64
```

10.7.2 For a Dataframe

Let's consider the following dataframe:

```
## df:
## city year x y
## 0 Marseille 2019 1 3
## 1 Aix 2019 2 3
## 2 Marseille 2018 2 2
## 3 Aix 2018 2 1
## 4 Paris 2019 0 4
## 5 Paris 2019 0 4
```

10.7.2.1 Changes of a Particular Value

Let's change the value of the first line of df for the column year, so that it is 2020. First, let's retrieve the position of the year column in the dataframe, using the get_loc() method applied to the colnames attribute of the dataframe:

```
pos_year = df.columns.get_loc("year")
print("pos_year: ", pos_year)

## pos_year: 1
```

Then, let's make the modification:

```
df.iloc[0,pos_year] = 2020
print("df: \n", df)

## df:
```

```
## city year x y
## 0 Marseille 2020 1 3
## 1 Aix 2019 2 3
## 2 Marseille 2018 2 2
## 3 Aix 2018 2 1
## 4 Paris 2019 0 4
## 5 Paris 2019 0 4
```

10.7.2.2 Modifications on One or More Columns

To modify all the values in a column to place a particular value, for example a 2 in the x column of df:

```
df.x = 2
print("df: \n", df)
## df:
##
              city
                    year
                            X
                               У
## 0
      Marseille
                    2020
                           2
                              3
                              3
## 1
              Aix
                    2019
                           2
## 2
     Marseille
                    2018
                           2
                              2
## 3
              Aix
                    2018
                              1
                           2
                              4
## 4
           Paris
                    2019
## 5
           Paris
                    2019
                           2
                              4
```

It is also possible to modify the values in the column by providing a list of values:

```
df.x = [2, 3, 4, 2, 1, 0]
print("df: \n", df)
## df:
##
              city
                    year
                              У
## 0
      Marseille
                   2020
                          2
                              3
              Aix
                              3
##
  1
                   2019
                          3
                              2
## 2
      Marseille
                   2018
## 3
                   2018
                          2
                              1
              Aix
## 4
           Paris
                   2019
                          1
                              4
## 5
           Paris
                   2019
                          0
                              4
```

We can therefore imagine modifying the values of a column according to the values that we read in another column. For example, let's assume the following code: if the value of y is 2, then x is a', if the value of yis 1, if the value of xisb', otherwise it is NaN. First, let's build a list containing the values to insert (which we will name nv_val), using a loop. We will go through all the elements of the y' column, and at each iteration add tonv_val' the value obtained by making our comparisons:

```
new_val = []
for i in np.arange(len(df.index)):
    if df.y[i] == 2:
        new_val.append("a")
    elif df.y[i] == 1:
        new_val.append("b")
    else:
        new_val.append(np.nan)
print("new_val: ", new_val)
## new_val: [nan, nan, 'a', 'b', nan, nan]
```

We are ready to modify the content of the x column of df to replace it with new_val:

```
df.x = new_val
print("df: \n", df)

## df:
## city year x y
## 0 Marseille 2020 NaN 3
## 1 Aix 2019 NaN 3
## 2 Marseille 2018 a 2
## 3 Aix 2018 b 1
## 4 Paris 2019 NaN 4
## 5 Paris 2019 NaN 4
```

To replace several columns at the same time:

```
df[["x", "y"]] = [[2, 3, 4, 2, 1, 0], 1]
print("df: \n", df)

## df:
## city year x y
## 0 Marseille 2020 2 1
## 1 Aix 2019 3 1
## 2 Marseille 2018 4 1
## 3 Aix 2018 2 1
## 4 Paris 2019 1 1
```

```
## 5 Paris 2019 0 1
```

In the previous instruction, we replaced the contents of the x and y columns with a vector of handwritten values for x and with the value 1 for all observations for y.

10.7.2.3 Modifications on One or More Rows

To replace a row with a constant value (of little interest in the current example):

```
df.iloc[1,:] = 1
print("df: \n", df)
## df:
##
            city
                 year
## 0
     Marseille
                  2020
                        2
                           1
## 1
                  1
                           1
                        1
## 2 Marseille
                       4 1
                  2018
## 3
            Aix
                  2018
                          1
## 4
          Paris
                  2019
                        1 1
          Paris
## 5
                  2019
                        0 1
```

It may be more interesting to replace an observation as follows:

```
df.iloc[1,:] = ["Aix", 2018, 1, 2]
print("df: \n", df)
## df:
##
             city year
                        X
                            У
## 0 Marseille
                  2020
                            1
## 1
                            2
             Aix
                  2018
                         1
## 2 Marseille
                        4 1
                  2018
## 3
             Aix
                  2018
                            1
                       1 1
## 4
          Paris
                  2019
## 5
          Paris
                  2019
                            1
```

To replace several rows, the method is identical:

```
df.iloc[[1,3],:] = [
        ["Aix", 2018, 1, 2],
        ["Aix", 2018, -1, -1]
]
print("df: \n", df)

## df:
## city year x y
## 0 Marseille 2020 2 1
## 1 Aix 2018 1 2
## 2 Marseille 2018 4 1
## 3 Aix 2018 -1 -1
## 4 Paris 2019 1 1
## 5 Paris 2019 0 1
```

10.8 Adding Values

Now let's look at how to add values, first in a series, then in a dataframe.

10.8.1 For a Series

Let's consider the following series:

10.8.1.1 Adding a Single Value in a Series

To add a value, we use the append() method. Here, with s_num, as the index is manual, we are compelled to provide a series with a value for the index as well:

```
s_num_2 = pd.Series([1], index = [2])
print("s_num_2: \n", s_num_2)
## s_num_2:
##
   2 1
## dtype: int64
s num = s num.append(s num 2)
print("s_num: \n", s_num)
## s_num:
## 5 1.0
        4.0
       -1.0
## 4
## 1
       NaN
## 2
       1.0
## dtype: float64
```

Note that the append() method returns a view. To effectively add values, we must make a new assignment.

By having a series with an automatically generated numerical index, we can specify the value True for the <code>ignore_index</code> argument of the <code>append()</code> method to indicate that we do not take into account the value of the index of the object we add:

```
s = pd.Series([10, 2, 4])
s = s.append(pd.Series([2]), ignore_index=True)
print("s: \n", s)

## s:
## 0    10
## 1    2
## 2    4
## 3    2
```

```
## dtype: int64
```

10.8.1.2 Adding Several Values in a Series

To add several values, we use the append() method. Here, with s_num, as the index is manual, we are required to provide a series with a value for the index as well:

```
s_num_2 = pd.Series([1], index = [2])
s_num.append(s_num_2)

## 5    1.0
## 0    4.0
## 4    -1.0
## 1    NaN
## 2    1.0
## 2    1.0
## dtype: float64
```

```
print("s_num: ", s_num)

## s_num: 5  1.0

## 0  4.0

## 4  -1.0

## 1  NaN

## 2  1.0

## dtype: float64
```

By having a series with an automatically generated numerical index:

```
## dtype: int64
```

10.8.2 For a dataframe

Let's go back to our dataframe:

10.8.2.1 Adding a Row in a Dataframe

As for a series, to add a row, we use the append() method. First, let's create a new dataframe with the line to add:

```
## 0 Marseille 2021 2 4
```

We made sure to have the same column name here, by indicating in the columns parameter of the pd.DataFrame method the name of the df columns, *i.e.*, df.columns.

Let's add the new row to df:

```
df = df.append(new_row, ignore_index=True)
```

Again, the append() method applied to a dataframe, returns a view and does not affect the object.

It can be noted that when adding a row, if the column names are not indicated in the same order as in the dataframe in which the addition is made, an indication must be added to the out parameter of the append() method:

- if sort=True, the order of the columns of the added row will be applied to the destination dataframe
- if sort=False, the column order of the destination dataframe will not be modified.

```
print("avec sort=True : \n",
    df.append(new_row, ignore_index=True, sort = True))
```

```
## avec sort=True :
                                 year
##
            city
                      coty
                            \mathbb{X}
                              У
## 0 Marseille
                      NaN
                           1
                              3
                                  2019
## 1
           Aix
                      NaN
                           2 3
                                 2019
## 2 Marseille
                      NaN
                          2 2
                                 2018
                      NaN 2 1
## 3
           Aix
                                 2018
         Paris
                          0 4
                                 2019
## 4
                      NaN
         Paris
## 5
                      NaN
                          0 4
                                 2019
```

```
## 6 Marseille NaN 2 4 2021
## 7 NaN Marseille 2 4 2021
```

10.8.2.2 Adding Multiple Rows in a Dataframe

To add several rows, it's exactly the same principle as with a single one, just add a dataframe of several rows, with the same names again.

The rows to be inserted:

Then the insertion:

```
df = df.append(new_rows, ignore_index=True)
```

10.8.2.3 Adding a Column to a Dataframe

To add a column in a dataframe:

```
from numpy import random
df["z"] = random.rand(len(df.index))
print("df: \n", df)

## df:
## city year x y z
## 0 Marseille 2019 1 3 0.117443
## 1 Aix 2019 2 3 0.393782
```

```
##
  2
      Marseille
                 2018
                       2
                           2
                              0.452730
##
  3
            Aix
                 2018
                       2
                              0.538148
                          1
## 4
          Paris
                 2019
                       0
                          4
                              0.790622
          Paris 2019
                              0.465836
## 5
                       0 4
## 6
     Marseille
                 2021
                       2
                              0.435332
      Marseille
                 2022
                       2 4
                              0.569479
## 7
## 8
            Aix
                 2022
                              0.969259
```

10.8.2.4 Adding Multiple Columns to a Dataframe

To add several columns:

```
df["a"] = random.rand(len(df.index))
df["b"] = random.rand(len(df.index))
print("df: \n", df)
## df:
##
            city
                  year
                        X
                           У
                                                  0.689236
##
  0
      Marseille
                 2019
                       1
                             0.117443
                                       0.040556
            Aix
                 2019
                       2
                             0.393782
                                        0.548120
                                                  0.929546
     Marseille
                             0.452730
                                       0.462577
                                                  0.918117
## 2
                 2018
                       2
                          2
## 3
            Aix
                 2018
                       2 1
                             0.538148
                                       0.376472
                                                 0.975302
## 4
          Paris
                      0 4
                            0.790622
                                                 0.397002
                2019
                                       0.327912
## 5
          Paris 2019
                      0 4 0.465836
                                       0.813529
                                                 0.262626
## 6
     Marseille 2021
                       2 4 0.435332
                                       0.646552
                                                  0.430151
                       2 4 0.569479
## 7
      Marseille
                 2022
                                       0.047426
                                                  0.764531
## 8
          Aix 2022
                      3 3 0.969259
                                        0.994958
                                                  0.599731
```

10.9 Removing Duplicate Values

To remove duplicate values from a dataframe, NumPy offers the drop_duplicates() method, which takes several optional arguments:

• subset: by indicating one or more column names, the search for duplicates is only done on these columns;

- keep: allows to indicate which observation to keep in case of identified duplicates:
 - if keep='first', all duplicates are removed except the first occurrence,
 - if keep='last', all duplicates are removed except the last occurrence,
 - if keep='False', all duplicates are removed;
- inplace: boolean (default: False) to indicate if duplicates should be removed from the dataframe or if a copy should be returned (default).

Let's give some examples using this dataframe which makes up two duplicates when we consider its totality. If we focus only on years or cities, or both, other duplicates can be identified.

```
##
           city
                 year
                           У
                        X
     Marseille
                 2019
                           3
## 0
                       1
## 1
            Aix
                 2019
                       2
                           3
## 2 Marseille
                 2018
                       2
                           2
                          1
## 3
            Aix
                 2018
## 4
          Paris
                 2019
                       0
                          4
## 5
          Paris
                 2019
                       0
                           4
```

To remove the duplicates:

print(df.drop duplicates())

```
##
             city
                    year
                              У
                          \mathbb{X}
## 0
     Marseille
                    2019
                              3
                          1
## 1
              Aix
                    2019
                          2
                              3
                              2
## 2 Marseille
                    2018
             Aix
                              1
## 3
                   2018
## 4
           Paris
                   2019
```

Remove duplicates by keeping the last value of the identified duplicates:

```
df.drop duplicates(keep='last')
##
          city year
                       У
## 0 Marseille 2019
                       3
                    1
                    2 3
## 1
          Aix 2019
                     2 2
## 2 Marseille 2018
## 3
          Aix 2018
                    2 1
## 5
         Paris 2019 0 4
```

To remove identified duplicates when focusing on city names, and keeping only the first value :

Same as above but with a focus on couples (city, year)

```
print(df.drop duplicates(subset = ["city", "year"], keep = 'first'))
##
          city
                year
                        У
                     X
                        3
## 0 Marseille
                2019
                     1
           Aix 2019
                     2 3
## 1
                     2 2
## 2 Marseille 2018
           Aix 2018
                     2 1
## 3
## 4
        Paris 2019
```

Note that the original dataframe was not impacted, since we did not touch the inplace argument. If we now ask that the changes be made on the dataframe instead of getting a copy:

```
df.drop_duplicates(subset = ["city", "year"], keep = 'first', inplace = True)
print(df)
```

```
##
                              У
            city
                    year
                          \mathbb{X}
     Marseille
## 0
                    2019
                          1
                              3
## 1
             Aix
                    2019
                              3
                              2
## 2 Marseille
                    2018
                    2018
## 3
              Aix
                              1
           Paris
## 4
                    2019
```

To find out if a value is duplicated in a dataframe, NumPy offers the duplicated() method, which returns a mask indicating for each observation, whether it is duplicated or not. Its operation is similar to df.drop_duplicates(), except for the inplace parameter which is not present.

```
print(df.duplicated(subset = ["city"], keep = 'first'))

## 0    False
## 1    False
## 2    True
## 3    True
## 4    False
## dtype: bool
```

We can use the any() method to find out if there are duplicates:

```
print(df.duplicated(subset = ["city"], keep = 'first').any())
## True
```

10.10 Operations

It is often necessary to perform operations on the columns of a dataframe, especially when it comes to creating a new variable.

By using the principles of column modification (see Section @ref(#pandas-ajout-valeurs)), it is quite easy to imagine that it is possible to apply the functions and methods of NumPy (see Section 9.1) on the values of the columns.

For example, let's consider the following dataframe:

```
##
       height
                weight
            58
## 0
                   115
## 1
            59
                    117
## 2
            60
                    120
## 3
            61
                    123
## 4
            62
                    126
## 5
            63
                   129
                    132
## 6
            64
## 7
            65
                   135
            66
                    139
## 8
## 9
            67
                   142
            68
## 10
                    146
## 11
            69
                    150
## 12
            70
                   154
## 13
            71
                    159
## 14
            72
                    164
```

Let's add the column height_2, increasing the values of the column height to square:

```
df["height_2"] = df.height**2
print(df.head(3))
```

```
## height weight height_2
## 0 58 115 3364
## 1 59 117 3481
```

```
## 2 60 120 3600
```

Now, let's add the column bmi, providing the body mass indicator values for individuals in the dataframe (bmi = $\frac{\text{weight}}{\text{height}^2}$):

```
df["bmi"] = df.weight / df.height_2
print(df.head(3))
```

```
##
      height
               weight
                        height_2
                                        bmi
          58
                  115
                            3364
                                   0.034185
## 0
## 1
          59
                  117
                            3481
                                   0.033611
## 2
           60
                  120
                            3600
                                  0.033333
```

10.10.1 Statistics

pandas offers some methods for performing descriptive statistics for each column or row. To do this, the syntax is as follows (all arguments have a default value, the list is simplified here):

```
dataframe.stat_method(axis, skipna)
```

- axis: 0 for rows, 1 for columns
- skipna: if True, excludes missing values from the calculations

Among the available methods: -mean(): mean -mode(): mode -median(): median -std(): standard error -min(): minimum -max(): maximum -mad(): mean absolute deviation -sum(): sum -prod(): product -count(): counting the elements

For example, to calculate the average of the values for each column:

```
dico = {"height" : [58, 59, 60, 61, 62],
        "weight": [115, 117, 120, 123, 126],
        "age": [28, 33, 31, 31, 29],
        "height_cm": [162, 156, 172, 160, 158],
        "married": [True, True, False, False, True],
        "city": ["A", "B", "B", "A"]
    }
```

```
df = pd.DataFrame(dico)
print(df.mean())

## height 60.0
## weight 120.2
```

height_cm 161.6 ## married 0.6

30.4

dtype: float64

age

If desired, we can average the column values (without any meaning here):

```
print(df.mean(axis=1))
```

```
## 0 72.8

## 1 73.2

## 2 76.6

## 3 75.0

## 4 75.2

## dtype: float64
```

These functions can be applied to a single column. For example, to display the minimum value:

```
print("min: ", df.height.min())
## min: 58
```

It is also useful to be able to obtain the position of the min and max values; this can be obtained with the methods idxmin() and idxmax(), respectively.

```
print("pos min: ", df.height.idxmin())
## pos min: 0
```

```
print("pos min: ", df.height.idxmax())
## pos min: 4
```

A very useful method is describe(), it allows to return descriptive statistics on all numerical columns:

print(df.describe())

##		height	weight	age	height_cm
##	count	5.00000	5.000000	5.000000	5.000000
##	mean	60.000000	120.200000	30.400000	161.600000
##	std	1.581139	4.438468	1.949359	6.228965
##	min	58.000000	115.000000	28.000000	156.000000
##	25%	59.00000	117.000000	29.000000	158.000000
##	50%	60.000000	120.000000	31.000000	160.000000
##	75%	61.000000	123.000000	31.000000	162.000000
##	max	62.00000	126.000000	33.000000	172.000000

10.11 Sorting

It is easy to sort a dataframe in ascending or descending order by one or more of its columns. To do this, we use the method sort values(). The syntax is as follows:

- by: name or list of names of the column(s) used to sort
- axis: 0 for the index (default), 1 for the columns
- ascending: boolean or boolean list, when True the sorting is done by increasing values (default), when False it is done by decreasing values
- inplace: if True, the sorting affects the dataframe, otherwise it returns a view
- kind: choice of sorting algorithm (quicksort (default), mergesort, heapsort)
- na_position: if first, the missing values are placed at the beginning; if last (default), at the end.

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Let us give some examples:

If we sort the values in descending order of the values in the height column:

```
df.sort_values(by="height", ascending=False)
```

```
##
      height
                weight
                         age
                               height_cm married city
## 4
           62
                 126.0
                          29
                                      158
                                              True
                                                       Α
## 3
           61
                 123.0
                                      160
                                             False
                                                       В
                          31
## 2
                                                       В
           60
                 120.0
                          31
                                      172
                                               NaN
## 1
           59
                   NaN
                          33
                                      156
                                              True
                                                       В
## 0
           58
                 115.0
                          28
                                      162
                                              True
                                                       Α
```

To sort in ascending order of the married values (recall that True is interpreted as 1 and False as 0), then decreasing by weight, placing the values NaN first:

```
height
##
               weight
                         age
                               height_cm married city
                                                       В
## 2
           60
                 120.0
                          31
                                      172
                                               NaN
## 3
           61
                 123.0
                          31
                                      160
                                            False
                                                       В
## 1
           59
                   NaN
                          33
                                      156
                                              True
                                                       В
## 4
           62
                                                       Α
                 126.0
                          29
                                      158
                                              True
## 0
           58
                 115.0
                          28
                                      162
                                              True
                                                       Α
```

Note that the NaN values have increased for the subgroups composed according to the married values.

10.12 Concatenation

4 -0.363095 -0.067318

It is frequent to obtain data from multiple sources when conducting an analysis. It is then important to be able to combine the different sources into one. In this section, we will limit ourselves to concatenating different dataframes between them, in simple cases in which we know *a priori* that all we have to do is put two dataframes side by side or one below the other. The case of slightly more elaborate joints with matching according to one or more columns is discussed in Section 10.13.

First, let's create two dataframes with the same number of lines:

```
x 1 = pd.DataFrame(np.random.randn(5, 4),
                  columns=["a", "b", "c", "d"])
x_2 = pd.DataFrame(np.random.randn(5, 2),
                  columns = ["e", "f"])
print("x 1: \n", x 1)
## x_1:
##
      0.231711 -0.474710 -0.309147 -2.032396
  1 -0.174468 -0.642475 -0.625023
## 2
      0.531255
                1.275284 -0.682826 -0.948186
               0.325113 -1.203486
## 3
     0.777362
                                     1.209543
## 4
     0.157622 -0.293555 0.111560
                                      0.597679
```

```
print("\nx_2: \n", x_2)

##

## x_2:

## e f

## 0 -1.270093 0.120949

## 1 -0.193898 1.804172

## 2 -0.234694 0.939908

## 3 -0.171520 -0.153055
```

To "paste" the dataframe x_2 to the right of x_1 , we can use the concat() method of pandas. To indicate that concatenation is performed on the columns, the value 1 for the parameter axix is specified as follows:

-0.067318

$print(pd.concat([x_1, x_2], axis = 1))$ ## b d f ## 0 0.231711 -0.474710 -0.309147 -2.032396 -1.270093 0.120949 ## 1 -0.174468 -0.642475 -0.625023 1.325887 -0.193898 1.804172 ## 2 0.531255 1.275284 -0.682826 -0.948186 -0.234694 0.939908 ## 3 0.777362 0.325113 -1.203486 1.209543 -0.171520 -0.153055

To paste the dataframes below each other, the append() method can be used, as described in Section 10.8.2.1, or the concat() method can also be used.

4 0.157622 -0.293555 0.111560 0.597679 -0.363095

Let's add the observations of x_3 below those of x_2 :

```
## 0 -1.270093 0.120949
## 1 -0.193898 1.804172
## 2 -0.234694 0.939908
## 3 -0.171520 -0.153055
```

```
## 4 -0.363095 -0.067318

## 0 1.444721 0.325771

## 1 -0.855732 -0.697595

## 2 -0.276134 -1.258759

## 3 0.478094 -0.859764

## 4 0.571988 -0.173965
```

As can be seen, the line index of x_2 has not been modified. If we want it to be, we can specify it via the <code>ignore_index</code> argument:

If the column names are not identical, values NaN will be inserted:

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```
pd.concat([x_2, x_4], axis = 0, sort=False, ignore_index=True)
##
                                  g
## 0 -1.270093
               0.120949
                                NaN
## 1 -0.193898 1.804172
                               NaN
## 2 -0.234694 0.939908
                               NaN
## 3 -0.171520 -0.153055
                               NaN
## 4 -0.363095 -0.067318
                               NaN
## 5 1.534900
                    NaN 0.872856
## 6 1.856835
                    NaN 0.025914
```

NaN -0.191163

NaN 1.655677 NaN -0.686884

10.13 Joins

7 0.171984

8 -0.292936 ## 9 -0.207182

It is more likely to use slightly more elaborate joins to bring together the different data sources into one. pandas offers a powerful way to gather data, the merge() function.

To illustrate the different joins in this section, let's create some dataframes:

```
"year" : np.arange(2014, 2017),
     "exports": [2208.678084, 2217.733347, 2210.442218]
    })
imports_us = pd.DataFrame(
    {"country" : "USA",
    "year" : np.arange(2015, 2018),
    "imports": [2827.336251, 2863.264745, np.nan]
    })
imports morocco = pd.DataFrame(
    {"pays" : "Morocco",
    "annee" : np.arange(2015, 2018),
    "imports": [46.39884177, 53.52375588, 56.68165748]
exports morocco = pd.DataFrame(
    {"country" : "Morocco",
    "year" : np.arange(2014, 2017),
    "exports": [35.50207915, 37.45996653, 39.38228396]
    })
exports = pd.concat([exports_fr, exports_us], ignore_index=True)
imports = pd.concat([imports fr, imports us], ignore index=True)
print("exports: \n", exports)
## exports:
## country year exports
## 0 France 2014 816.819217
## 1 France 2015 851.663257
## 2 France 2016 867.401425
## 3 USA 2014 2208.678084
## 4 USA 2015 2217.733347
## 5 USA 2016 2210.442218
```

print("\nimports: \n", imports)

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```
##
  imports:
##
      country
                year
                            imports
## 0
      France
               2015
                       898.524296
               2016
                       936.369117
## 1
      France
## 2
      France
               2017
                       973.876215
## 3
                      2827.336251
         USA
               2015
                      2863.264745
## 4
         USA
               2016
## 5
         USA
               2017
                               NaN
```

The merge() function of pandas requires to specify the left table (which we will call here x) via the left argument on which the joining of the right table (which we will call here y) will be performed via the right argument.

By default, the merge() function performs an inner type join, *i.e.*, all x rows that match y, and all x and y columns will be in the result of the join:

```
print(pd.merge(left = imports, right = exports))
##
     country
               year
                           imports
                                         exports
##
  0
      France
               2015
                       898.524296
                                      851.663257
## 1
      France
               2016
                       936.369117
                                     867.401425
## 2
                      2827.336251
                                    2217.733347
          USA
               2015
## 3
          USA
               2016
                      2863.264745
                                     2210.442218
```

If we want to change the type of join, we can modify the value of the how parameter of the merge() function, to give it one of the following values:

- left: all x rows, and all x and y columns. Rows in x for which there is no match in y will have values NaN in the new columns. If there are several matches in the names between x and y, all combinations are returned
- inner: all x rows for which there are corresponding values in y, and all x and y columns. If there are several matches in the names between x and y, all possible combinations are returned
- right: all y rows, and all y and x columns. Rows in y for which there is no match in x will have values NaN in the new columns. If there are several matches in the names between y and x, all combinations are returned
- outer: all rows of x and y, and all columns of x and y. Lines of x for which there is no match in y and those of y for which there is no match in x will have values NaN.

```
print("left: \n", pd.merge(left = imports, right = exports, how="left"))
## left:
##
     country year
                      imports exports
## 0 France 2015 898.524296 851.663257
## 1 France 2016 936.369117 867.401425
## 2 France 2017 973.876215
                                    NaN
## 3 USA 2015 2827.336251 2217.733347
      USA 2016 2863.264745 2210.442218
## 4
## 5 USA 2017
                        NaN
                                    NaN
print("\nright: \n", pd.merge(left = imports, right = exports, how="right"))
##
## right:
## country year imports exports
## 0 France 2015 898.524296 851.663257
## 1 France 2016 936.369117 867.401425
## 2
      USA 2015 2827.336251 2217.733347
## 3 USA 2016 2863.264745 2210.442218
## 4 France 2014
                       NaN 816.819217
## 5 USA 2014
                       NaN 2208.678084
print("\nouter: \n", pd.merge(left = imports, right = exports, how="outer"))
##
## outer:
     country year imports exports
## 0 France 2015 898.524296 851.663257
## 1 France 2016 936.369117 867.401425
## 2 France 2017 973.876215
                                   NaN
## 3 USA 2015 2827.336251 2217.733347
## 4
       USA 2016 2863.264745 2210.442218
## 5 USA 2017
                       NaN
                                    NaN
## 6 France 2014
                        NaN 816.819217
## 7 USA 2014
                        NaN 2208.678084
```

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The on argument, which expects a column name or list of names, is used to designate the columns used to make the join. The column names must be identical in both dataframes.

<pre>print(pd.merge(left = imports, right = exports, on = "country"))</pre>						
##		country	year_x	imports	year_y	exports
##	0	France	2015	_	2014	-
##	1	France	2015	898.524296	2015	851.663257
##	2	France	2015	898.524296	2016	867.401425
##	3	France	2016	936.369117	2014	816.819217
##	4	France	2016	936.369117	2015	851.663257
##	5	France	2016	936.369117	2016	867.401425
##	6	France	2017	973.876215	2014	816.819217
##	7	France	2017	973.876215	2015	851.663257
##	8	France	2017	973.876215	2016	867.401425
##	9	USA	2015	2827.336251	2014	2208.678084
##	10	USA	2015	2827.336251	2015	2217.733347
##	11	USA	2015	2827.336251	2016	2210.442218
##	12	USA	2016	2863.264745	2014	2208.678084
##	13	USA	2016	2863.264745	2015	2217.733347
##	14	USA	2016	2863.264745	2016	2210.442218
##	15	USA	2017	NaN	2014	2208.678084
##	16	USA	2017	NaN	2015	2217.733347
##	17	USA	2017	NaN	2016	2210.442218

If the names of the columns used to make the join are different between the left and right dataframe, the argument left_on indicates the column name(s) of the left dataframe to be used for the join; and the argument right_on indicates the corresponding name(s) in the right dataframe:

```
pd.merge(left = imports_morocco, right = exports_morocco,
         left on= ["pays", "annee"], right on = ["country", "year"] )
##
                          imports
                                     country
                                                        exports
          pays
                 annee
                                               year
## 0
      Morocco
                  2015
                        46.398842
                                     Morocco
                                               2015
                                                      37.459967
## 1
      Morocco
                 2016
                        53.523756
                                     Morocco
                                               2016
                                                      39.382284
```

With the argument suffixes, suffixes can be defined to be added to column names

when there are columns in x and y with the same name but not used for joining. By default, the suffixes $(_x$ and $_y)$ are added.

```
print(pd.merge(left = imports, right = exports,
              on = "country",
              suffixes=("_left", "_right")).head(3))
##
     country
              year_left
                              imports
                                       year_right
                                                        exports
## 0
                    2015
                           898.524296
                                                     816.819217
      France
                                               2014
                                                     851.663257
      France
                           898.524296
## 1
                    2015
                                               2015
## 2
      France
                    2015
                           898.524296
                                               2016
                                                     867.401425
```

10.14 Aggregation

Sometimes we want to aggregate the values of a variable, for example, from a quarterly to an annual dimension. With spatial observations, this can also be the case, for example, when data are available at the county level and the aggregate values at the state level.

To illustrate the different aggregation operations, let's create a dataframe with unemployment data for different French regions, departments and years:

```
##
         region
                      departement
                                    year
                                          workers
                                                    engineers
       Bretagne
                    Cotes-d'Armor
                                    2011
                                                          1420
## 0
                                              8738
## 1
       Bretagne
                        Finistere
                                    2011
                                             12701
                                                          2530
```

##	2	Bretagne	Ille-et-Vilaine	2011	11390	3986
##	3	Bretagne	Morbihan	2011	10228	2025
##	4	Corse	Corse-du-Sud	2011	975	259
##	5	Corse	Haute-Corse	2011	1297	254
##	6	Bretagne	Cotes-d'Armor	2010	8113	1334
##	7	Bretagne	Finistere	2010	12258	2401
##	8	Bretagne	Ille-et-Vilaine	2010	10897	3776
##	9	Bretagne	Morbihan	2010	9617	1979
##	10	Corse	Corse-du-Sud	2010	936	253
##	11	Corse	Haute-Corse	2010	1220	241

As previously discussed (see Section 10.10.1), methods can be used to calculate simple statistics on the data set. For example, to display the average of each of the numerical columns:

print(unemployment.mean())

```
## year 2010.500000
## workers 7364.166667
## engineers 1704.833333
## dtype: float64
```

What we are interested in in this section is to perform calculations on subgroups of data. The principle is simple: first, the data are separated according to identified groups (*split*), then an operation is applied to each group (*apply*), and finally the results are collected (*combine*). To perform grouping, depending on factors before performing aggregation calculations, pandas offers the method groupby(). The argument provided is the column name(s) used to perform the groups.

10.14.1 Aggregation According to the Values of a Single Column

For example, let us assume that we want to obtain the total number of unemployed workers per year. First, we use the <code>groupby()</code> method on our dataframe, indicating that the groups must be created according to the values in the <code>year</code> column

Then, we extract the variable workers:

```
print(unemployment.groupby("year")["workers"])
## <pandas.core.groupby.groupby.SeriesGroupBy object at 0
x129add358>
```

And finally, we can perform the calculation on each subgroup and display the result: print(unemployment.groupby("year")["workers"].sum())

```
## year
## 2010     43041
## 2011     45329
## Name: workers, dtype: int64
```

If we want to perform this calculation for several columns, for example workers and engineers, we just have to select $a\ priori$ the grouping variance and the variables for which we want to perform the calculation:

```
unemployment.loc[:,["year", "workers", "engineers"]].groupby("year").sum()
## workers engineers
## year
## 2010 43041 9984
```

2011 45329 10474

10.14.2 Aggregation According to the Values of Several Columns

Now, let's assume that we want to aggregate by year and region. The only thing we need to do is to give a list containing the names of the columns used to create the different groups:

```
unemployment.loc[:,["year", "region",
              "workers", "engineers"]].groupby(["year",
                                                 "region"]).sum()
##
                             engineers
                   workers
## year region
## 2010 Bretagne
                     40885
                                  9490
                      2156
                                   494
        Corse
## 2011 Bretagne
                     43057
                                  9961
##
        Corse
                      2272
                                   513
```

10.15 Data Export and Import

pandas offers many functions for importing and exporting data in different formats.

10.15.1 Data Export

10.15.1.1 Exporting Tabular Data

10.15.1.1.1 To a CSV File {pandas-export_csv}

To export tabular data, such as those contained in a dataframe, NumPy offers the to_csv() method, which accepts many specifications. Let's look at some of them that seem to me to be the most common:

zip, xz)

end of line character

character used to put fields between quotes

date format for datetime objects

(integer) number of lines to be written at a time

line_terminator

##

quotechar

chunksize

date_format

Description Argument path to the file path_or_buf field separation character sep decimal character to be used for the decimal separator representation to be used for missing values na rep indicates whether the column names should be exported header (True by default) indicates whether the line names should be exported (True index by default) python writing mode (see Table 5.1, by default w) mode character encoding (utf-8 by default) encoding compression compression to be used for the destination file (gzip, bz2.

Table 10.1: Main arguments of the to csv function

Let's assume that we want to export the contents of the 'unemployment' dataframe to a CSV file whose fields are separated by semicolons, and by not exporting the index:

```
unemployment = pd.DataFrame(
    {"region" : (["Bretagne"]*4 + ["Corse"]*2)*2,
     "departement" : ["Cotes-d'Armor", "Finistere",
                      "Ille-et-Vilaine", "Morbihan",
                      "Corse-du-Sud", "Haute-Corse"] *2,
     "year" : np.repeat([2011, 2010], 6),
     "workers": [8738, 12701, 11390, 10228, 975, 1297,
                   8113, 12258, 10897, 9617, 936, 1220],
     "engineers": [1420, 2530, 3986, 2025, 259, 254,
                     1334, 2401, 3776, 1979, 253, 241]
    })
print(unemployment)
          region
                       departement year workers
                                                      engineers
```

##	0	Bretagne	Cotes-d'Armor	2011	8738	1420
##	1	Bretagne	Finistere	2011	12701	2530
##	2	Bretagne	Ille-et-Vilaine	2011	11390	3986
##	3	Bretagne	Morbihan	2011	10228	2025
##	4	Corse	Corse-du-Sud	2011	975	259
##	5	Corse	Haute-Corse	2011	1297	254
##	6	Bretagne	Cotes-d'Armor	2010	8113	1334
##	7	Bretagne	Finistere	2010	12258	2401
##	8	Bretagne	Ille-et-Vilaine	2010	10897	3776
##	9	Bretagne	Morbihan	2010	9617	1979
##	10	Corse	Corse-du-Sud	2010	936	253
##	11	Corse	Haute-Corse	2010	1220	241

For export:

```
path = "./fichiers_exemples/unemployment.csv"
unemployment.to_csv(path, decimal=";", index=False)
```

If you want the CSV file to be compressed into a gzip file, you name it with the extension .csv.gz and add the value gzip to the compression parameter:

```
path = "./fichiers_exemples/chomage.csv.gz"
unemployment.to_csv(path, decimal=";", index=False, compression="gzip")
```

10.15.1.1.2 To an HDF5 File

To save the data of a dataframe in an HDF5 file using HDFStore, pandas offers the method to_hdf() which works in the same way as the function to_csv() (see Section @ref(pandas-export_csv)).

The argument path_or_buf must be specified to indicate the path and the argument key to identify the object to be saved in the file.

The syntax is as follows:

```
path = "./fichiers_exemples/chomage.h5"
unemployment.to_hdf(path, "base_chomage", decimal=";", index=False)
```

10.16 Data Import

pandas offers many functions for importing data. In this version of the course notes, we will discuss 3: read_csv(), to read CSV files; read_excel(), to read Excel files; and read_hdf() to read HDF5 files.

10.16.1 CSV Files

To import data from a CSV file, pandas offers the function read_csv():

```
path = "./fichiers_exemples/unemployment.csv"
unemployment = pd.read_csv(path, decimal=";")
```

It is possible to provide a URL pointing to a CSV file as a path, the read_csv() function.

Among the parameters that are frequently used:

- sep, delimiter: field separator
- decimal: decimal separator
- header: line number(s) to be used as data header
- skiprows: line number(s) to be skipped at the beginning
- skipfooter: line number(s) to be skipped at the end
- nrows: number of lines to read
- na_values: additional character strings to be considered as missing values (in addition to #N/A, #N/A N/A, #NA, -1.#IND, -1.#QNAN, -NaN, -nan, 1.#IND, 1.#QNAN, N/A, NA, NULL, NaN, n/a, nan, null)
- quotechar: quote character
- encoding: character encoding (utf-8 by default).

10.16.2 Excel Files

To import Excel files, pandas offers the function read excel().

```
path = "./fichiers_exemples/chomage.xlsx"
unemployment = pd.read_excel(path, skiprows=2, header=1, sheet = 1)
print(unemployment)
```

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##		Bretagne	Cotes-d'Armor	2011	8738	1420
##	0	Bretagne	Finistere	2011	12701	2530
##	1	Bretagne	Ille-et-Vilaine	2011	11390	3986
##	2	Bretagne	Morbihan	2011	10228	2025
##	3	Corse	Corse-du-Sud	2011	975	259
##	4	Corse	Haute-Corse	2011	1297	254
##	5	Bretagne	Cotes-d'Armor	2010	8113	1334
##	6	Bretagne	Finistere	2010	12258	2401
##	7	Bretagne	Ille-et-Vilaine	2010	10897	3776
##	8	Bretagne	Morbihan	2010	9617	1979
##	9	Corse	Corse-du-Sud	2010	936	253
##	10	Corse	Haute-Corse	2010	1220	241

Among the frequently used arguments:

- header: row number to be used as header
- sheet: name or sheet number
- skiprows: number of lines to be skipped at the beginning
- thousands: thousands separator.

10.16.3 HDF5 Files

```
path = "./fichiers_exemples/chomage.h5"
print(pd.read_hdf(path, "base_chomage"))
```

10.17 Exercise

Exercise 1: Import and export

- 1. Download the csv file by hand at the following address: http://egallic.fr/ Enseignement/Python/Exercices/donnees/notes.csv and place it in the current directory. Import its content into Python.
- 2. Import the data back into Python, but this time by providing the url directly to the import function.

- 3. Now, import the contents of the file available at http://egallic.fr/Enseignement/Python/Exercices/donnees/notes_decim.csv. The field separator is a semicolon and the decimal separator is a comma.
- 4. Import the contents of the file http://egallic.fr/Enseignement/Python/ Exercices/donnees/notes_h.csv. The column names are not present.
- 5. Importer le contenu du fichier http://egallic.fr/Enseignement/Python/ Exercices/donnees/notes_h_s.csv. The first line is not to be imported.
- 6. Import the contents of the first sheet of the Excel file http://egallic.fr/Enseignement/Python/Exercices/donnees/notes.xlsx.
- 7. Import the content of the second sheet (notes_h_s) from the Excel file available here: http://egallic.fr/Enseignement/Python/Exercices/donnees/notes.xlsx. The first line is a comment not to be considered during the import.
- 8. Export the content of the object containing the notes of the previous question in csv format (comma as field separator, dot as decimal separator, do not keep the line numbers).

Exercise 2: Handling Dataframes

- 1. Using the read_excel() function of the pandas library, import the contents of the sheet entitled notes_2012 from the Excel file available at the following address: http://egallic.fr/Enseignement/Python/Exercices/donnees/notes_etudiants.xlsx and store it in a variable called notes_2012.
- 2. Display the first 6 lines of the dataset, then the dimensions of the table.
- 3. Keep only the column note_stat of the data table notes_2012 in an object called tmp.
- 4. Keep only the columns number_student, note_stat and note_macro in an object named tmp.
- 5. Replace the content of tmp with observations of notes_2012 for which the individual obtained a stat score greater (strictly) than 10.
- 6. Replace the content of tmp with observations of notes_2012 for which the individual obtained a stats score within the interval (10, 15).
- 7. Look for duplicates in the notees_2012 data table; if so, remove them from the table.
- 8. Display the type of data in the column num_etudiant, then display the type of all note columns_2012.
- 9. Add the following columns to the notes 2012 table:
- (a) note stat maj: the stat score (note stat) increased by one point,
- (b) note macro maj: the macro note (note macro) plus three points (do it in two

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- steps: first two more points, then one point).
- 10. Rename the column year to year.
- 11. From the file notes_etudiants.xlsx (see question 1), import the contents of the sheets notes_2013, notes_2014 and prenoms and store them in the objects grades_2013, grades_2014 and first_names, respectively.
- 12. Stack the contents of the data tables grades_2012, grades_2013 and grades_2014 in an object that will be called grades.
- 13. Merge the grades and first_names tables using a left join, so as to add the information contained in the first name table to the grade observations. The join must be done by the student number and the year, the final object will replace the content of the grades
- 14. Sort the grades table by increasing years and decreasing macro grades
- 15. Create a column after_2012 which takes the value True if the observation concerns a score assigned after 2012.
- 16. By grouping on the grades dataframe compute:
- (a) the annual mean and standard deviation of the scores for each of the two classes,
- (b) the annual and gender average and standard deviation of the grades for each of the two classes.

Chapter 11

Data Visualization

In this chapter, we will explore the basics of data visualization with the Matplotlib library.

For the moment, these notes will not talk about the dynamic graphics that can be created in connection with JavaScript libraries, such as D3.js. In a future version, we might see how to make graphs with seaborn. (https://seaborn.pydata.org/).

To have quick access to a type of graphic that you want to create, you can refer to this excellent gallery: https://python-graph-gallery.com/.

Fans of the R software and programming language will be happy to find a graphical grammar like the one proposed by the [R package ggplot2] (https://ggplot2.tidyverse.org/) introduced by Hadley Wickham. Indeed, there is a Python library called ggplot: http://ggplot.yhathq.com/.

To graphically explore one's data, it may be interesting to invest some time in the Altair library (https://altair-viz.github.io/). For a short video introduction, see: https://www.youtube.com/watch?v=aRxahWy-ul8.

11.1 Graphics with Matplotlib

To use the features offered by matplotlib (https://matplotlib.org/), some modules need to be loaded. The most common is the submodule pyplot, to which the alias plt is frequently assigned:

```
import matplotlib.pyplot as plt
```

To make a graph with the pyplot function, we first create a figure by defining its range, then add and/or modify its elements using the functions offered by pyplot.

To illustrate the features of matplotlib, we will need to generate values, using the numpy library, which we load:

```
import numpy as np
```

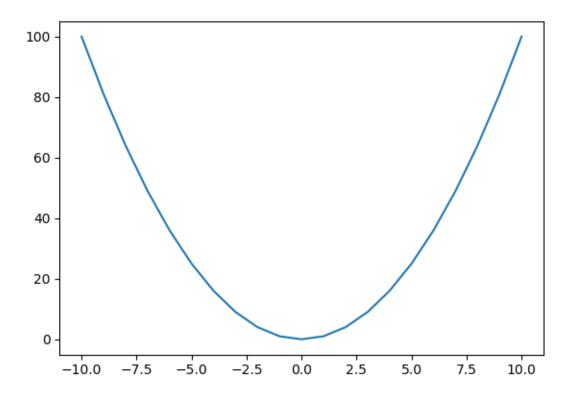
11.1.1 Geometries

11.1.1.1 Lines

To draw lines on a Cartesian coordinate system, we can use the plot() function, to which we provide the coordinates of the x-axis and y-axis as the first two arguments, respectively. The third argument defines the geometry.

By default, the geometry is a curve:

```
x = np.arange(-10, 11)
y = x**2
plt.plot(x, y)
```

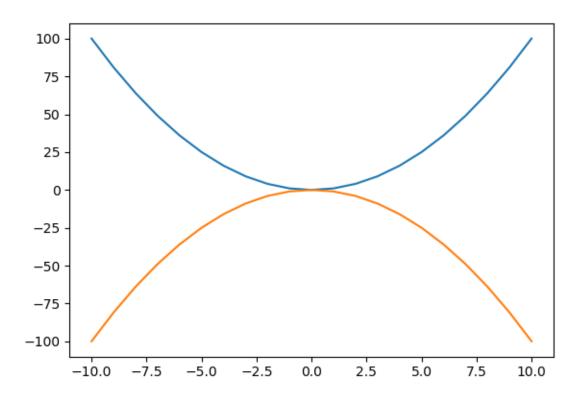


Once the graph is displayed, it can be closed with the close() function:

Similarly, the geometry can be specified as follows:

To add a curve to the graph, the plot() function is used several times:

```
y_2 = -x**2
plt.plot(x, y, "-")
plt.plot(x, y_2, "-")
```

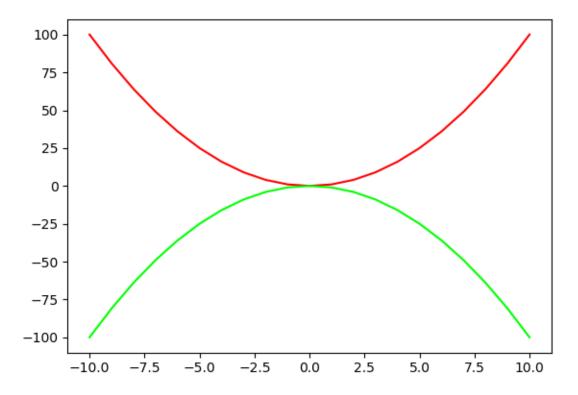


11.1.1.1.1 Aesthetic Arguments

11.1.1.1.1.1 Line Color

To change the color of a line, the argument color is used:

```
plt.plot(x, y, color="red")
plt.plot(x, y_2, color="#00FF00")
```



As can be seen, the reference to color can be done by using its name (the list of colors with a name is available on the matplotlib documentation). A hexadecimal code can also be used to refer to a color.

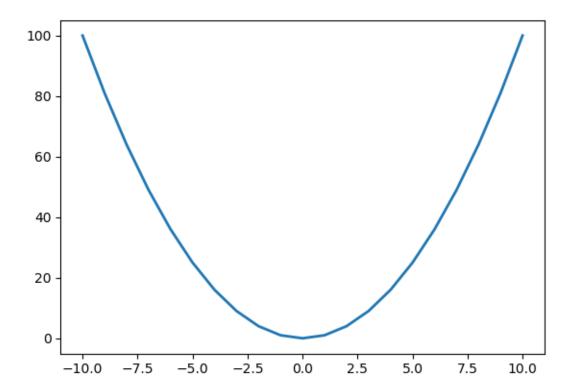
Remark 11.1.1

It may be interesting, when selecting colours, to think about the use afterwards: is it for the screen? For grayscale printing? It is also questionable whether the choice made will not hinder understanding for colourblind people (who represent about 4% of the French population). The Color Brewer website offers colour choices based on desired characteristics such as those mentioned.

11.1.1.1.1.2 Line Thickness

Line thickness can be modified using the linewidth argument, to which a numerical

value is provided:



11.1.1.1.3 Type of lines

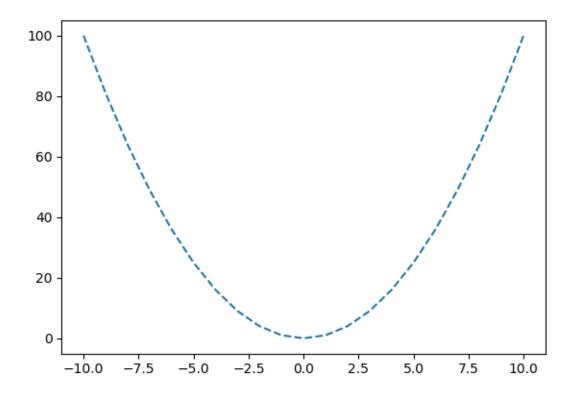
To change the line type, the third argument of the function is modified. As we have seen on the previous example the default is a line. This corresponds to the value – being specified to the third argument. Table 11.1 indicates the different possible formats for the line.

Table 11.1: Line formats

Value	Description		
_	Solid line		

Value	Description
	Dashed line
	Dots and dashs
:	Dots

For example, to have a linear interpolation between our points with a graphical representation made using dashes :

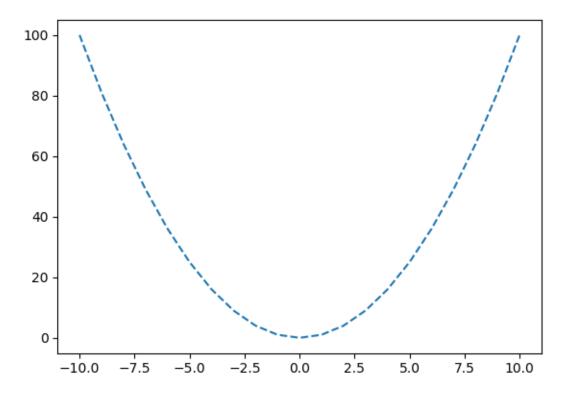


The line type can also be specified using the linestyle parameter, by indicating one of the values given in Table 11.2

Value	Description
- ou solid	Solid line
ou dashed	Dashed
ou dashdot	Dashes and dots
: ou dotted	Dots
None	No line plotted

Table 11.2: Line formats via the linestyle argument

plt.plot(x, y, linestyle="dashed")



11.1.1.1.4 Markers

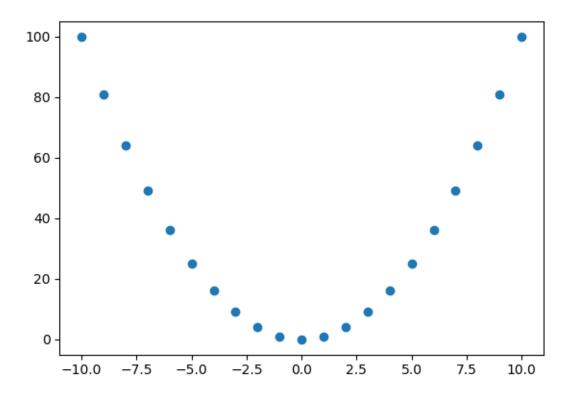
Table 11.3 shows formats that can be specified as markers at each point on the curve.

Table 11.3: Line formats

Value	Description
	Dots
,	Pixels
0	Empty circles
v	Triangles pointing down
^	Triangles pointing up
<	Triangles pointing to the left
>	Triangles pointing to the right
1	'tri_down'
2	'tri_up'
3	'tri_left'
4	'tri_right'
s	Square
р	Pentagon
*	Asterisk
h	Hexagon 1
Н	Hexagon 2
+	Plus symbol
х	Multiply symbol
D	Diamond
d	Thin diamond
1	Vertical line
_	Horizontal line

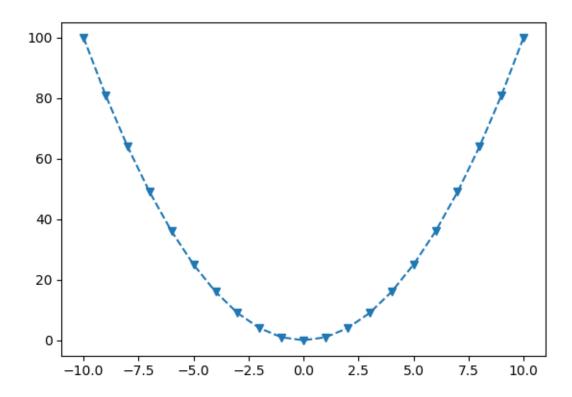
For example, with empty circles:

```
plt.plot(x, y, "o")
```



It can be noted that it is possible to combine the line types in 11.1 with marker types described in Table 11.3:

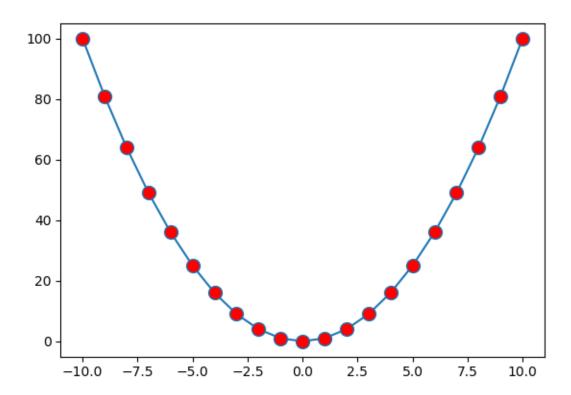
plt.plot(x, y, "--v")



To control the markers more precisely, the following arguments can be used:

- marker: indicates the type of marker (see Table 11.3)
- markerfacecolor: the desired color for the markers
- markersize: size of the markers.

```
plt.plot(x, y, marker="o", markerfacecolor = "red", markersize = 10)
```



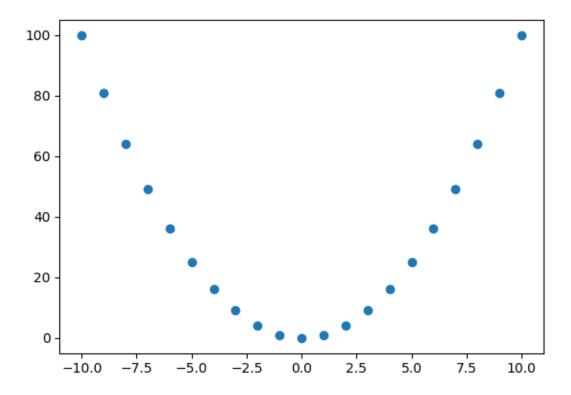
11.1.1.2 Scatter Plots

One of the graphs that we very frequently encounter is the scatterplot. To create one, we can use the scatter() function, which indicates the coordinates (x,y) of the points as well as some optional shape or aesthetic parameters.

Remark 11.1.2

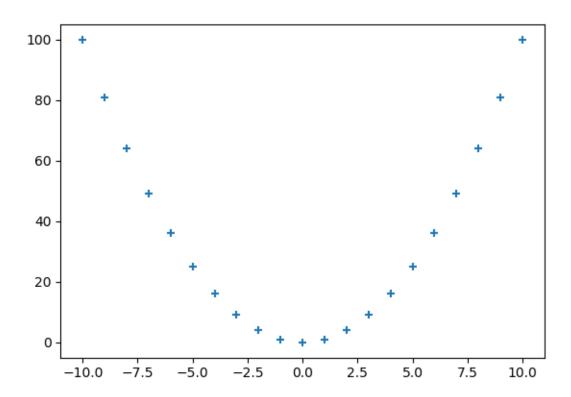
The online documentation of the scatter() function mentions that the plot() function (see Section 11.1.1.1) s faster to perform scatter plots in which the color or size of the points varies.

```
x = np.arange(-10, 11)
y = x**2
plt.scatter(x, y)
```



When we wish to change the shape of the markers, we specify it via the marker argument (see Table 11.3 for the possible values):

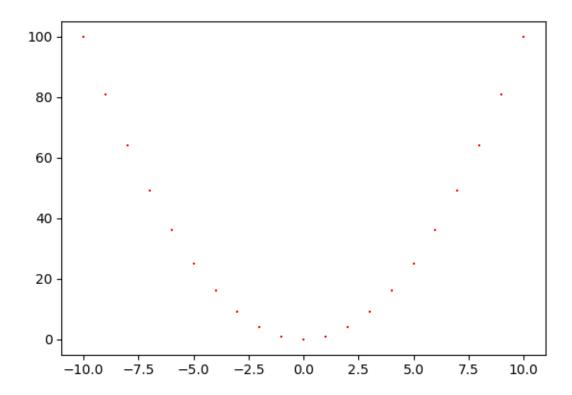
```
x = np.arange(-10, 11)
y = x**2
plt.scatter(x, y, marker="+")
```



11.1.1.3 Size and color

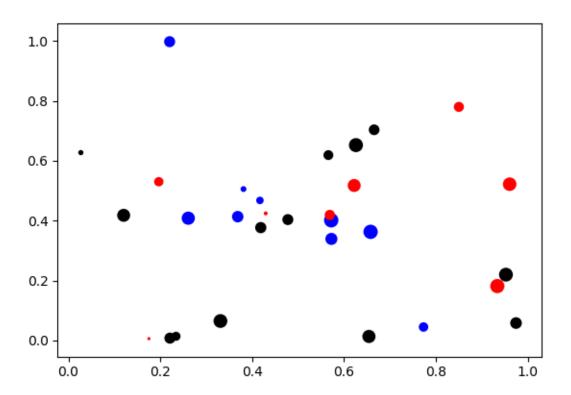
The size of the points is adjustable via the parameter s, while the color changes via the parameter color (or by its alias c):

```
x = np.arange(-10, 11)
y = x**2
plt.scatter(x, y, marker="+", color = "red", s = 2)
```



A specific colour and size can be associated with each point:

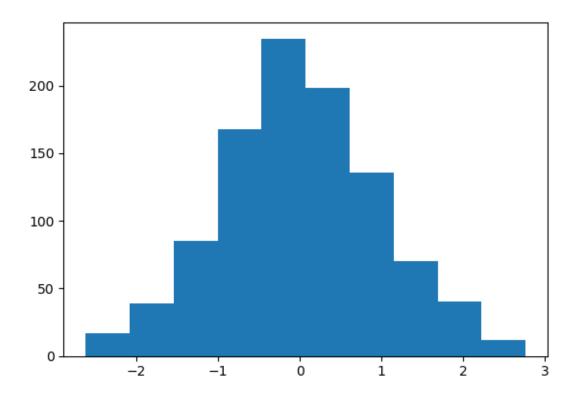
```
x = np.random.rand(30)
y = np.random.rand(30)
z = np.random.rand(30)
colours = np.random.choice(["blue", "black", "red"], 30)
plt.scatter(x, y, marker="o", color = colours, s = z*100)
```



11.1.1.4 Histograms

x = np.random.randn(1000)

To make a histogram with pyplot, the function hist() can be used:

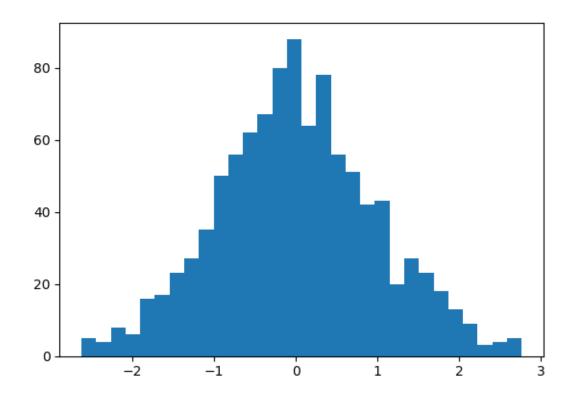


The bins argument is used to specify either the number of classes or their boundaries:

plt.hist(x, bins=30)

```
## (array([ 5., 4., 8., 6., 16., 17., 23., 27., 35., 50.,
   56., 62., 67.,
      80., 88., 64., 78., 56., 51., 42., 43., 20., 27.,
##
  23., 18., 13.,
           9., 3., 4., 5.]), array([-2.62300428,
##
   -2.44344267, -2.26388106, -2.08431945, -1.90475784,
          -1.72519622, -1.54563461, -1.366073 , -1.18651139,
##
   -1.00694978,
          -0.82738816, -0.64782655, -0.46826494, -0.28870333,
##
   -0.10914171,
           0.0704199 , 0.24998151, 0.42954312, 0.60910473,
##
   0.78866635,
```

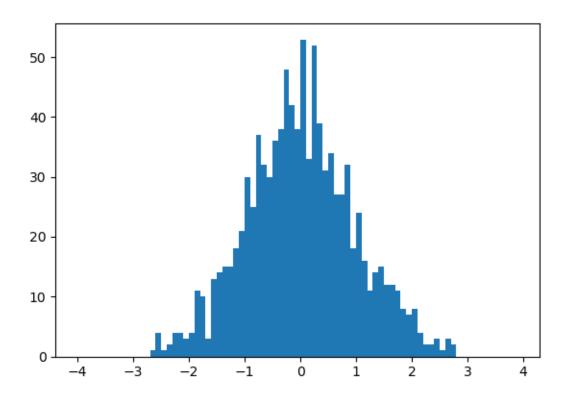
```
## 0.96822796, 1.14778957, 1.32735118, 1.50691279,
    1.68647441,
## 1.86603602, 2.04559763, 2.22515924, 2.40472086,
    2.58428247,
## 2.76384408]), <a list of 30 Patch objects>)
```



And with the boundaries:

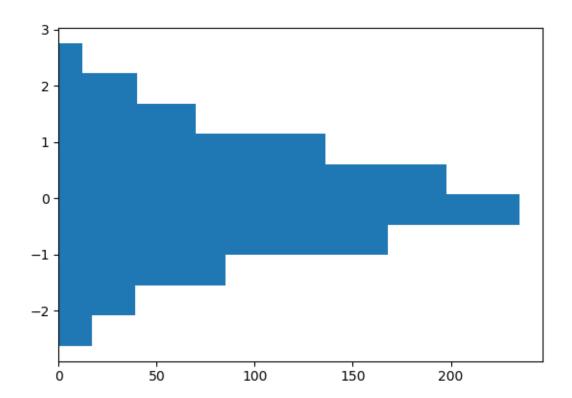
```
3., 13., 14.,
         15., 15., 18., 21., 30., 25., 37., 32., 30., 36.,
  38., 48., 42.,
         38., 53., 33., 52., 39., 31., 34., 27., 27., 32.,
##
  18., 24., 16.,
        11., 14., 15., 12., 12., 11., 8., 7., 8., 4.,
       2., 3.,
  2.,
          1., 3., 2., 0., 0., 0., 0., 0., 0.,
##
  0., 0., 0.,
           0.]), array([-4.00000000e+00, -3.90000000e+00,
##
  -3.80000000e+00, -3.70000000e+00,
          -3.60000000e+00, -3.50000000e+00, -3.40000000e+00,
##
   -3.30000000e+00,
          -3.20000000e+00, -3.10000000e+00, -3.00000000e+00,
   -2.90000000e+00,
##
          -2.80000000e+00, -2.70000000e+00, -2.60000000e+00,
   -2.50000000e+00,
          -2.40000000e+00, -2.30000000e+00, -2.20000000e+00,
##
   -2.10000000e+00,
##
          -2.000000000e+00, -1.90000000e+00, -1.80000000e+00,
   -1.70000000e+00,
          -1.60000000e+00, -1.50000000e+00, -1.40000000e+00,
##
   -1.30000000e+00,
          -1.20000000e+00, -1.10000000e+00, -1.00000000e+00,
##
  -9.00000000e-01,
          -8.00000000e-01, -7.00000000e-01, -6.00000000e-01,
##
  -5.00000000e-01,
          -4.00000000e-01, -3.00000000e-01, -2.00000000e-01,
##
   -1.00000000e-01,
           3.55271368e-15, 1.00000000e-01, 2.00000000e-01,
##
  3.00000000e-01,
           4.00000000e-01, 5.00000000e-01, 6.00000000e-01,
##
  7.00000000e-01,
           8.00000000e-01, 9.00000000e-01, 1.00000000e+00,
##
  1.10000000e+00,
##
          1.20000000e+00, 1.30000000e+00, 1.40000000e+00,
  1.50000000e+00.
          1.60000000e+00, 1.70000000e+00, 1.80000000e+00,
##
  1.90000000e+00,
           2.00000000e+00, 2.10000000e+00, 2.20000000e+00,
##
  2.30000000e+00,
```

```
2.40000000e+00, 2.50000000e+00,
                                              2.60000000e+00,
##
   2.70000000e+00,
           2.80000000e+00, 2.90000000e+00,
##
                                              3.00000000e+00,
   3.10000000e+00,
##
           3.20000000e+00,
                            3.30000000e+00,
                                              3.40000000e+00,
   3.50000000e+00,
           3.60000000e+00,
                            3.70000000e+00,
                                              3.80000000e+00,
##
   3.90000000e+00]), <a list of 79 Patch objects>)
```



The orientation is changed via the orientation argument, indicating either vertical (by default) or horizontal.

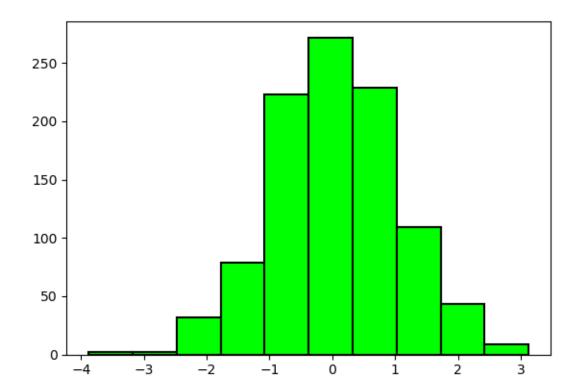
```
plt.hist(x, orientation='horizontal')
```



11.1.1.4.1 Aesthetic Arguments

To change the filling color, we use the color argument; to add a color delimiting the bars, we use the edgecolor argument; to define the contour thickness, we use the linewidth argument:

```
x = np.random.randn(1000)
plt.hist(x, color = "#00FF00", edgecolor='black', linewidth=1.5)
```

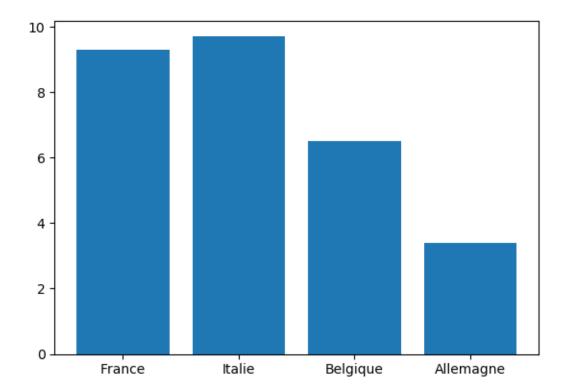


11.1.1.5 Bar Charts

To make bar graphs, pyplot offers the function bar().

```
pays = ["France", "Italie", "Belgique", "Allemagne"]
unemployment = [9.3, 9.7, 6.5, 3.4]
plt.bar(pays, unemployment)
```

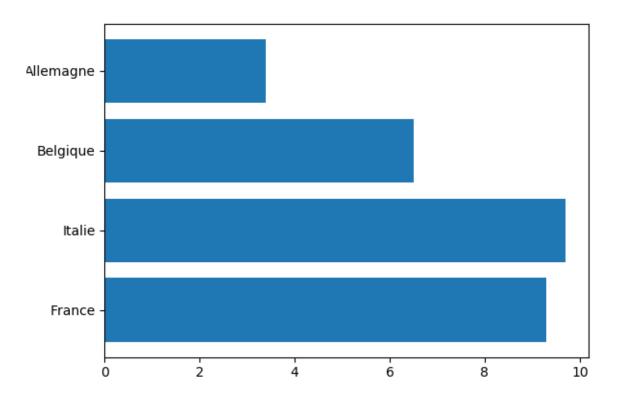
```
## <BarContainer object of 4 artists>
```



For a horizontal diagram, the barh() function is used in the same way:

```
plt.barh(pays, unemployment)
```

<BarContainer object of 4 artists>



11.1.1.5.1 Several Series on a Bar Chart

To compare several side-by-side series, it is necessary to borrow concepts that will only be introduced in Section 11.1.3 (the code is provided here rather as a quick reference to perform this kind of graphs).

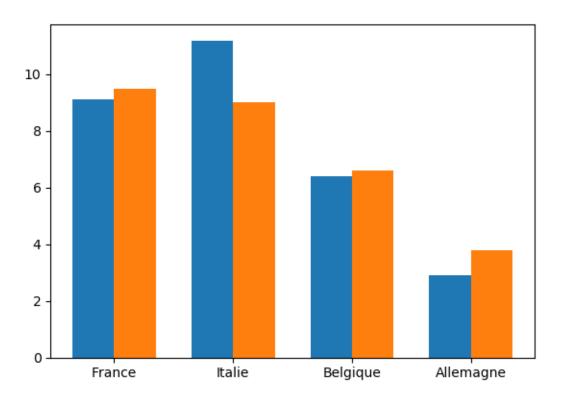
```
countries = ["France", "Italie", "Belgique", "Allemagne"]
unemp_f = [9.1, 11.2, 6.4, 2.9]
unemp_h = [9.5, 9, 6.6, 3.8]
# Position on the x-axis for each label
position = np.arange(len(countries))
```

```
# Bar widths
width = .35

# Creating the figure and a set of subgraphics
fig, ax = plt.subplots()
r1 = ax.bar(position - width/2, unemp_f, width)
r2 = ax.bar(position + width/2, unemp_h, width)

# Modification of the marks on the x-axis and their labels
ax.set_xticks(position)
ax.set_xticklabels(countries)
```

```
## [Text(0,0,'France'), Text(0,0,'Italie'), Text(0,0,'Belgique
'), Text(0,0,'Allemagne')]
```



11.1.1.5.2 Stacked Bar Charts

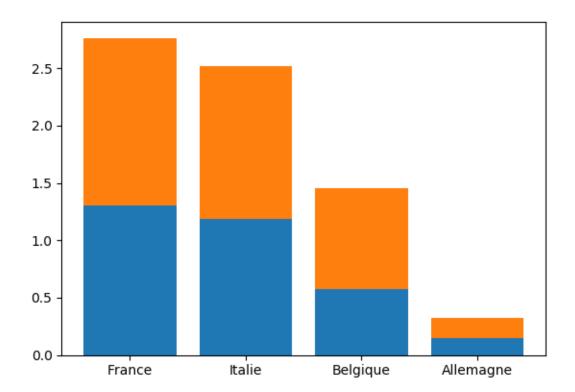
To stack the values of the series, the starting value for the series is specified using the argument bottom:

```
countries = ["France", "Italie", "Belgique", "Allemagne"]
no_unemp_f = [1.307, 1.185, .577, .148]
no_unemp_h = [1.46, 1.338, .878, .179]

plt.bar(countries, no_unemp_f)
plt.bar(countries, no_unemp_h, bottom = no_unemp_f)
```

<BarContainer object of 4 artists>

<BarContainer object of 4 artists>

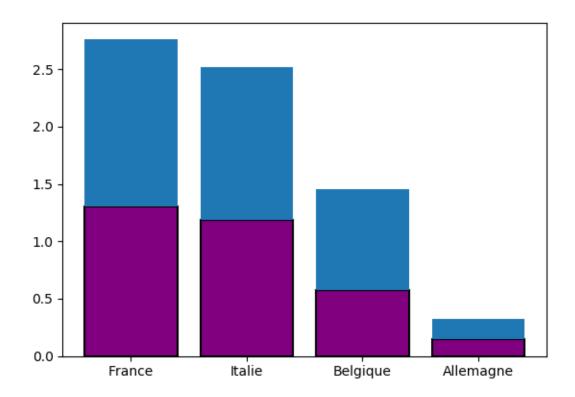


11.1.1.5.3 Aesthetic Arguments

To change the filling color, we use the color argument; for the contour color, we enter the edgecolor argument; for the contour width, we rely on the linewidth argument:

```
countries = ["France", "Italie", "Belgique", "Allemagne"]
no_unemp_f = [1.307, 1.185, .577, .148]
no_unemp_h = [1.46, 1.338, .878, .179]
plt.bar(countries, no_unemp_f, color = "purple",
```

```
edgecolor = "black", linewidth = 1.5)
plt.bar(countries, no_unemp_h, bottom = no_unemp_f)
## <BarContainer object of 4 artists>
## <BarContainer object of 4 artists>
```

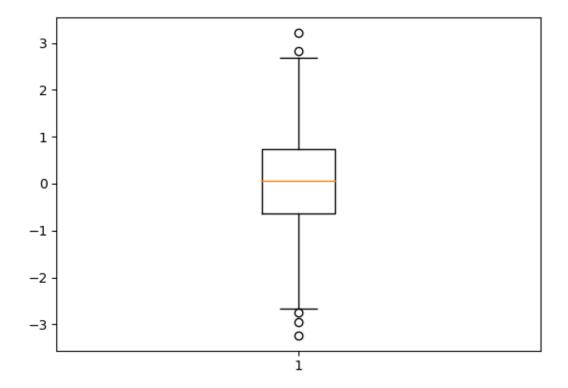


11.1.1.6 Boxplots

To make boxplot, pyplot offers the function boxplot():

```
x = np.random.randn(1000)
plt.boxplot(x)
```

```
## {'whiskers': [<matplotlib.lines.Line2D object at 0
    x1352e8710>, <matplotlib.lines.Line2D object at 0x1352e8c50
>], 'caps': [<matplotlib.lines.Line2D object at 0x1352f30f0
>, <matplotlib.lines.Line2D object at 0x1352f3550>], 'boxes
': [<matplotlib.lines.Line2D object at 0x1352e85c0>], '
    medians': [<matplotlib.lines.Line2D object at 0x1352f39b0
>], 'fliers': [<matplotlib.lines.Line2D object at 0
    x1352f3e10>], 'means': []}
```

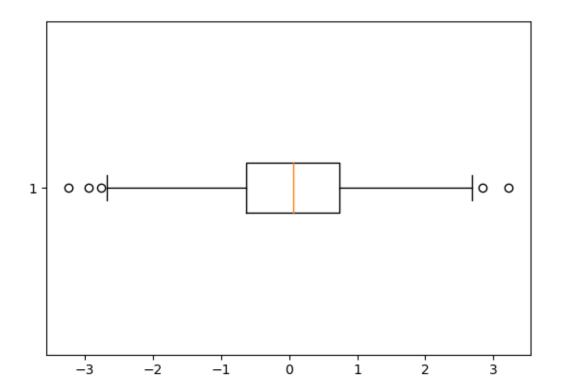


By specifying False as the value of the argument vert, the boxplot is plotted

horizontally:

```
plt.boxplot(x, vert = False)
```

```
## {'whiskers': [<matplotlib.lines.Line2D object at 0
    x135345550>, <matplotlib.lines.Line2D object at 0x135345a90
>], 'caps': [<matplotlib.lines.Line2D object at 0x135345ef0
>, <matplotlib.lines.Line2D object at 0x135352390>], 'boxes
': [<matplotlib.lines.Line2D object at 0x135345400>], '
    medians': [<matplotlib.lines.Line2D object at 0x1353527f0
>], 'fliers': [<matplotlib.lines.Line2D object at 0
    x135352c50>], 'means': []}
```

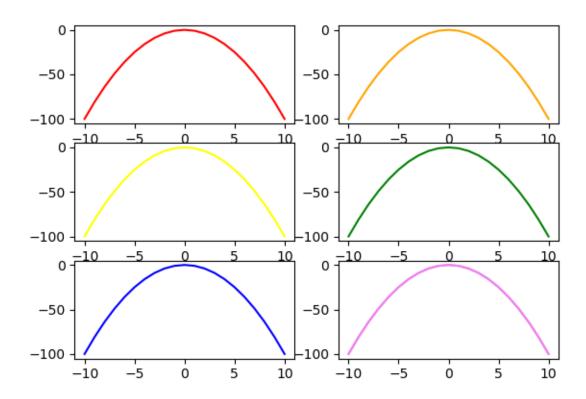


11.1.2 Several Graphs on a Figure

To place graphs next to each other, the function subplot() is used. The graphs will be placed as in a matrix, with a number of rows no_rows and a number of columns no_col. The dimensions of this matrix can be specified as arguments of the subplot() function, using the following syntax:

where current indicates the index of the active graph. Let's look at an example of how it works:

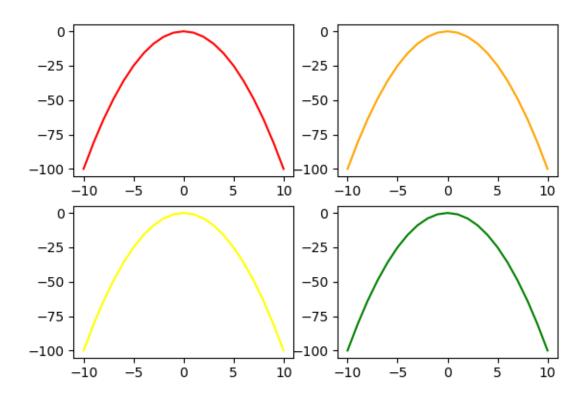
```
x = np.arange(-10, 11)
y = -x**2
# 3x2 dimension matrix of graphs
# Row 1, column 1
plt.subplot(3, 2, 1)
plt.plot(x, y, color = "red")
# Row 1, column 2
plt.subplot(3, 2, 2)
plt.plot(x, y, color = "orange")
# Row 2, column 1
plt.subplot(3, 2, 3)
plt.plot(x, y, color = "yellow")
# Row 2, column 2
plt.subplot(3, 2, 4)
plt.plot(x, y, color = "green")
# Row 3, column 1
plt.subplot(3, 2, 5)
plt.plot(x, y, color = "blue")
# Row 3, column 2
plt.subplot(3, 2, 6)
plt.plot(x, y, color = "violet")
```



Remember that the matrices are filled line by line in Python, which allows a good understanding of the value of the active graph number.

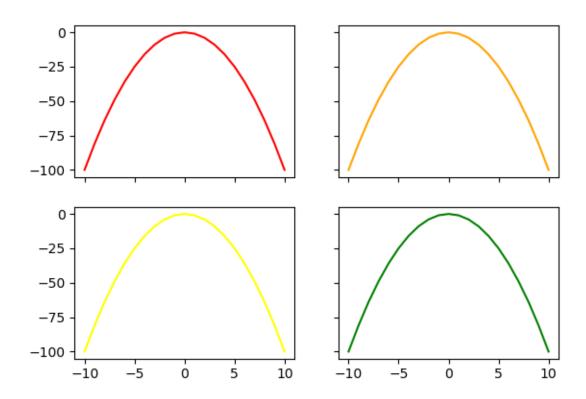
By using the function subplots() (beware of the final "s" of the name of the function that differentiates it from the previous one), it is possible to produce a matrix of graphs as well, by proceeding as follows:

```
f, ax_arr = plt.subplots(2, 2)
ax_arr[0, 0].plot(x, y, color = "red")
ax_arr[0, 1].plot(x, y, color = "orange")
ax_arr[1, 0].plot(x, y, color = "yellow")
ax_arr[1, 1].plot(x, y, color = "green")
```



This approach has the advantage of easily specifying the sharing of axes between the different subgraphs, via the sharex and sharey arguments:

```
f, ax_arr = plt.subplots(2, 2, sharey=True, sharex = True)
ax_arr[0, 0].plot(x, y, color = "red")
ax_arr[0, 1].plot(x, y, color = "orange")
ax_arr[1, 0].plot(x, y, color = "yellow")
ax_arr[1, 1].plot(x, y, color = "green")
```



11.1.3 Graphics Elements

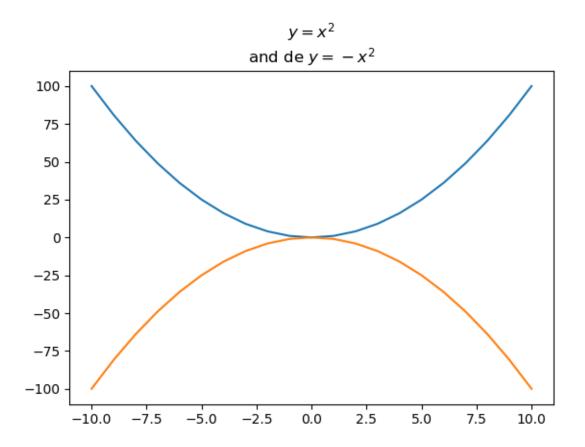
So far, we have looked at how to create different geometries, but we have not touched the axes, their values or labels (except in the unexplained example of side-by-side diagrams), or modified the legends or titles.

11.1.3.1 Title

To add a title to the graph, we can use the title() function:

```
x = np.arange(-10, 11)
y = x**2
y_2 = -y
```

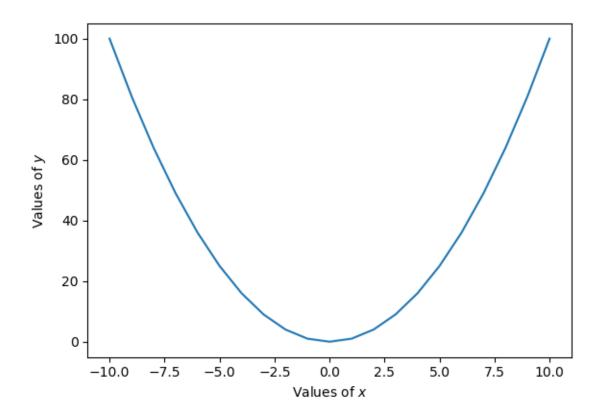
```
plt.plot(x, y)
plt.plot(x, y_2)
plt.title("y = x^2 \ \ y = -x^2")
```



11.1.3.2 Axes

The xlabel() and ylabel() functions allow us to add labels to the axes:

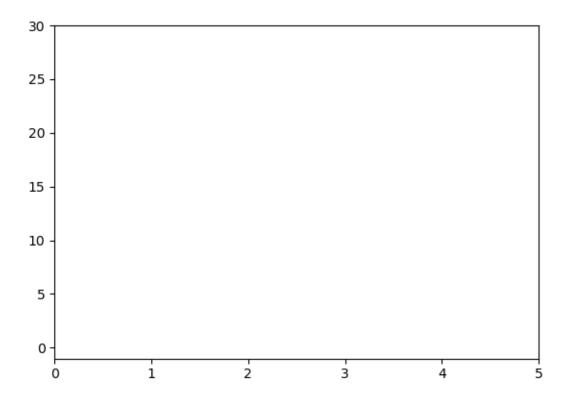
```
x = np.arange(-10, 11)
y = x**2
plt.plot(x, y)
plt.xlabel("Values of $x$")
plt.ylabel("Values of $y$")
```



11.1.3.2.1 Limits

To control the axis limits, the axis() function is used, specifying the arguments xmin, xmax, ymax, ymin and ymax, denoting, respectively, the lower and upper bounds of the x-axis and the lower and upper bounds of the y-axis:

```
plt.axis(xmin = 0, xmax = 5, ymin = -1, ymax = 30)
## (0, 5, -1, 30)
```



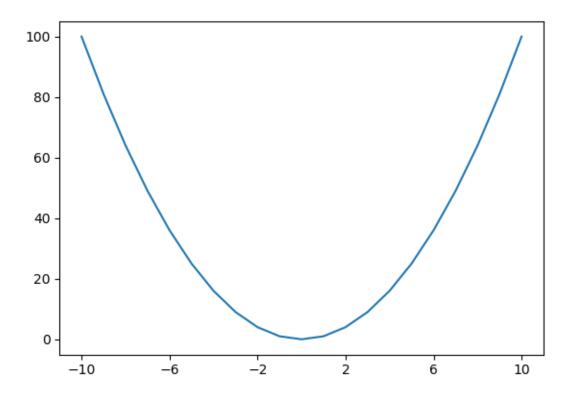
11.1.3.2.2 Marks and labels

The xticks() and yticks() functions are used to obtain or modify the marks of the x-axis and the y-axis, respectively.

```
x = np.arange(-10, 11)
y = x**2
plt.plot(x, y)
plt.xticks(np.arange(-10, 11, step = 4))
```

([<matplotlib.axis.XTick object at 0x135e61ac8>, <
 matplotlib.axis.XTick object at 0x135e61400>, <matplotlib.
 axis.XTick object at 0x135e612e8>, <matplotlib.axis.XTick
 object at 0x135a2c278>, <matplotlib.axis.XTick object at 0x135a2c780>, <matplotlib.axis.XTick object at 0x135a2cc88</pre>

>], <a list of 6 Text xticklabel objects>)

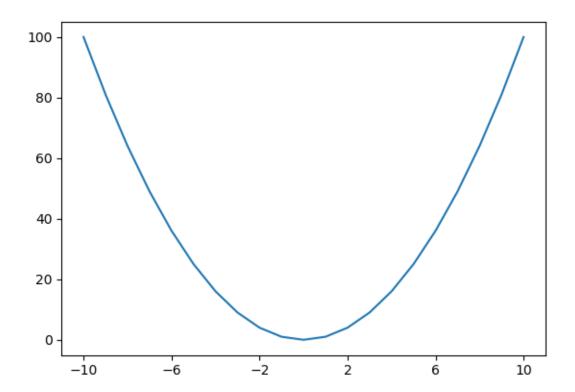


It can be convenient to retrieve the positions and labels of a graph so that we can modify them, for example to define the spacing between each mark:

```
plt.plot(x, y)
locs_x, labels_x = plt.xticks()
locs_y, labels_y = plt.yticks()
loc_x_new = np.arange(locs_x[0], locs_x[-1], step = 5)
loc_y_new = np.arange(locs_y[0], locs_y[-1], step = 10)

plt.xticks(loc_x_new)
plt.yticks(loc_y_new)
```

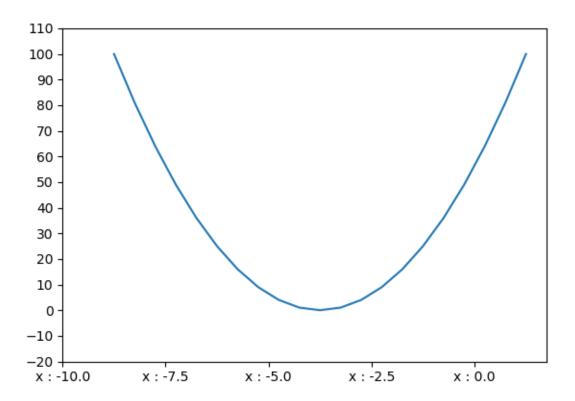
([<matplotlib.axis.XTick object at 0x135eb1f60>, <
 matplotlib.axis.XTick object at 0x135eb1898>, <matplotlib.
 axis.XTick object at 0x135eb15f8>, <matplotlib.axis.XTick
 object at 0x135ed8710>, <matplotlib.axis.XTick object at 0
 x135ed8c18>, <matplotlib.axis.XTick object at 0x135edf198
 >], <a list of 6 Text xticklabel objects>)



The labels on the marks can also be modified:

```
plt.plot(x, y)
locs_x, labels_x = plt.xticks()
locs_y, labels_y = plt.yticks()
loc_x_new = np.arange(locs_x[0], locs_x[-1], step = 5)
loc_y_new = np.arange(locs_y[0], locs_y[-1], step = 10)
```

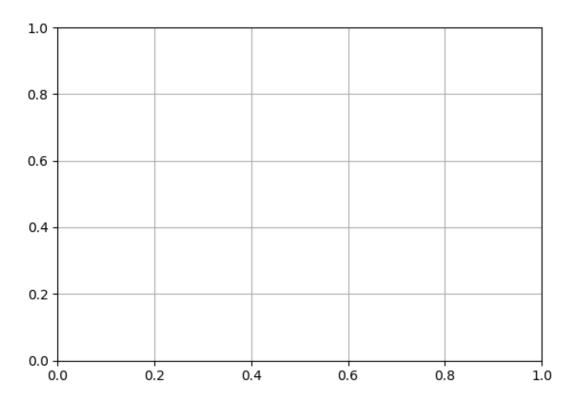
([<matplotlib.axis.XTick object at 0x1360294a8>, <
 matplotlib.axis.XTick object at 0x136022da0>, <matplotlib.
 axis.XTick object at 0x136048898>, <matplotlib.axis.XTick
 object at 0x136048ba8>, <matplotlib.axis.XTick object at 0
 x13628c400>], <a list of 5 Text xticklabel objects>)



11.1.3.2.3 Grid

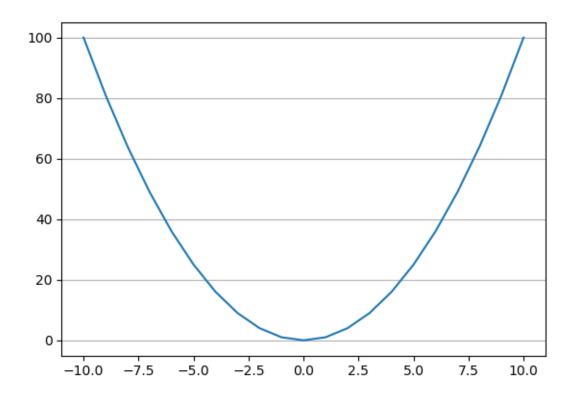
To add a grid, grid() function is used:

```
x = np.arange(-10, 11)
y = x**2
plt.plot(x, y)
plt.grid()
```



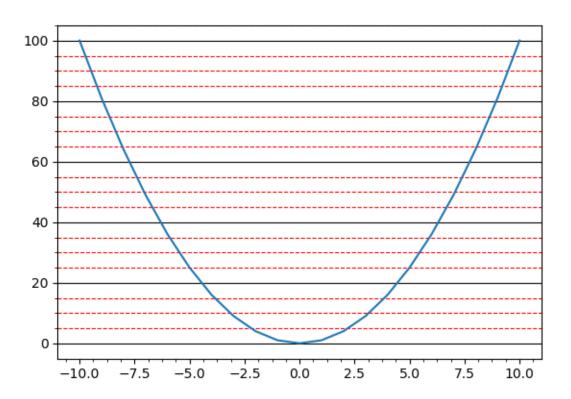
The axis argument allows to define if we want a grid for both axes (both, by default), only for the x-axis (x), or only for the y-axis (y):

```
plt.plot(x, y)
plt.grid(axis = "y")
```



It is possible to set the major or minor lines of the grid:

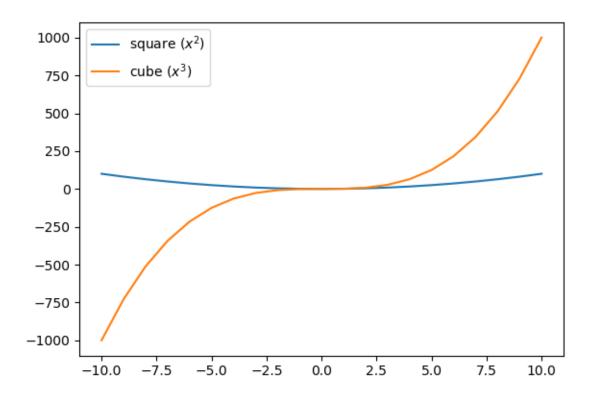
```
plt.plot(x, y)
plt.minorticks_on()
plt.grid(which = "major", axis = "y", color = "black")
plt.grid(which = "minor", axis = "y", color = "red", linestyle = "--")
```



11.1.3.3 Legends

When we wish to add a legend, we specify its label to the label argument in the call of the plot function, then we use the legend() function:

```
x = np.arange(-10, 11)
y = x**2
y_2 = x**3
plt.plot(x, y, label = "square ($x^2$)")
plt.plot(x, y_2, label = "cube ($x^3$)")
plt.legend()
plt.legend()
```



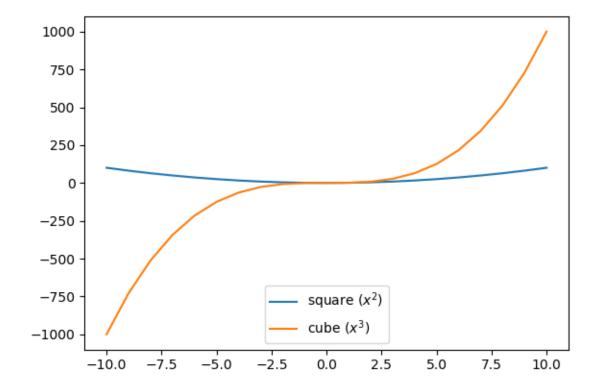
To specify the position of the legend, we can use the loc argument in the legend() function, indicating a value as reported in Table 11.1.3.3.

```
center | 10 | Centered |
```

Table: Position of the legend

For example, to center the legend in the middle, at the bottom of the graph:

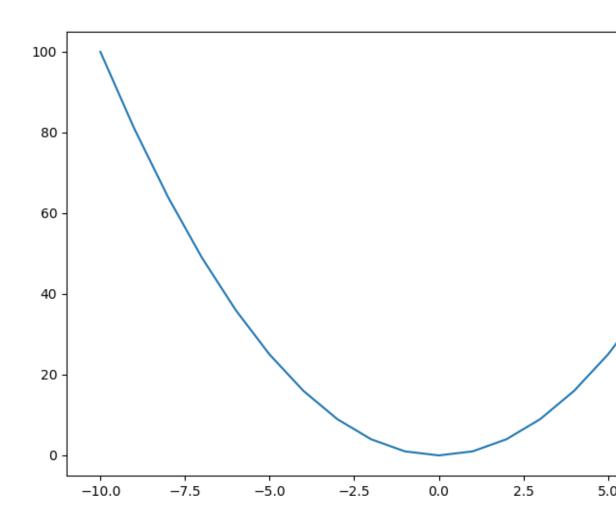
```
x = np.arange(-10, 11)
y = x**2
y_2 = x**3
plt.plot(x, y, label = "square ($x^2$)")
plt.plot(x, y_2, label = "cube ($x^3$)")
plt.legend(loc = "lower center")
```



11.1.4 Dimensions

To define the dimensions of a figure, we specify the figsize argument of the figure() function. It is provided with a tuple of integers whose first element corresponds to the length and the second to the height (the values are in inches):

```
x = np.arange(-10, 11)
y = x**2
plt.figure(figsize=(10,6))
plt.plot(x, y)
```



11.1.5 Exporting Graphs

To save a graph, the function plt.savefig() can be used. We specify the path to the file to be created, indicating the extension of the desired file (e.g., png or pdf):

```
x = np.arange(-10, 11)
y = x**2
y_2 = x**3
plt.figure(figsize=(10,6))
plt.plot(x, y, label = "square ($x^2$)")
plt.plot(x, y_2, label = "cube ($x^3$)")
plt.legend(loc = "lower center")
plt.savefig("test.pdf")
```

The specified extension (in this example, pdf) determines the output file format. The extensions indicated in the keys of the dictionary returned by the following instruction (the values giving a description of the file type) can be used:

```
print(fig.canvas.get_supported_filetypes())
```

```
## {'ps': 'Postscript', 'eps': 'Encapsulated Postscript', 'pdf
': 'Portable Document Format', 'pgf': 'PGF code for LaTeX',
    'png': 'Portable Network Graphics', 'raw': 'Raw RGBA
bitmap', 'rgba': 'Raw RGBA bitmap', 'svg': 'Scalable Vector
    Graphics', 'svgz': 'Scalable Vector Graphics', 'jpg': '
    Joint Photographic Experts Group', 'jpeg': 'Joint
    Photographic Experts Group', 'tif': 'Tagged Image File
    Format', 'tiff': 'Tagged Image File Format'}
```

11.2 Graphics with Seaborn

To be done.

https://seaborn.pydata.org/

Chapter 12

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