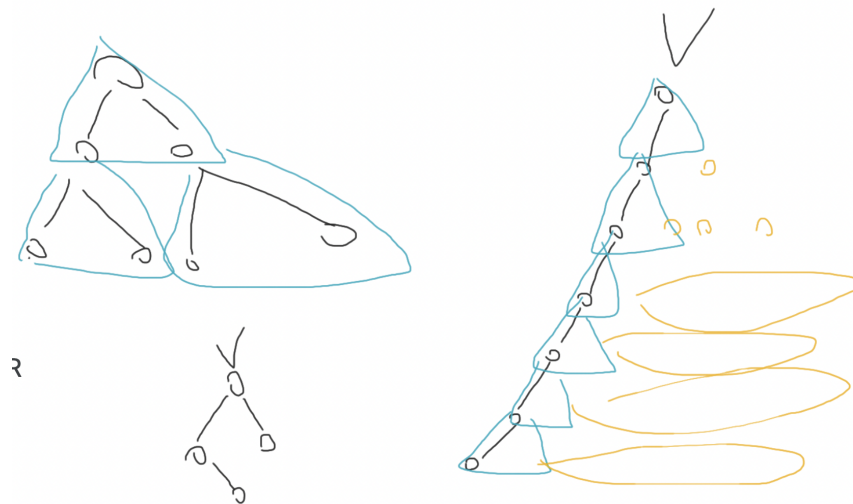


Phill-DS-0320

https://youtu.be/a854lhHq_a0

AVL tree - Adelson V L

高度平衡的二元搜尋樹 → efficiency (不能有空隙, 計算量會增加)



$$T \in AVL$$

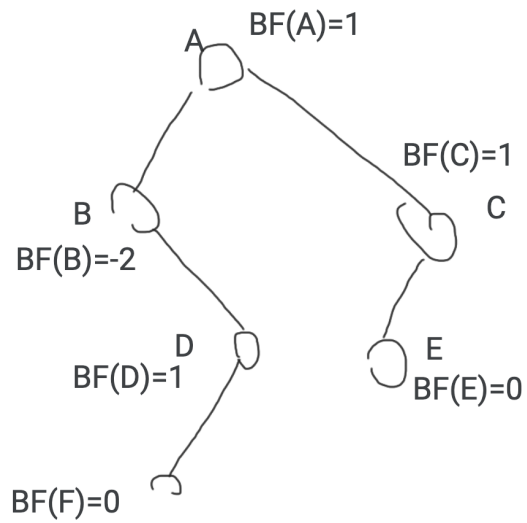
$$T_L, T_R \in AVL$$

$$|h_L - h_R| \leq 1 \rightarrow \text{balanced}$$

T_L T_R



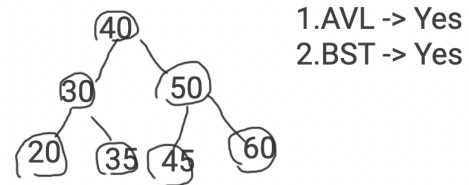
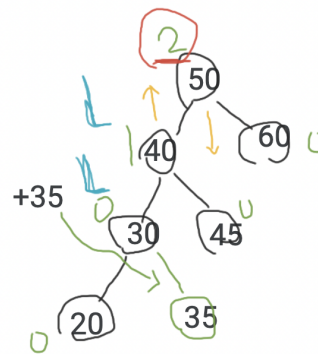
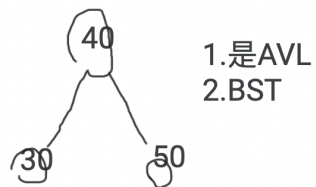
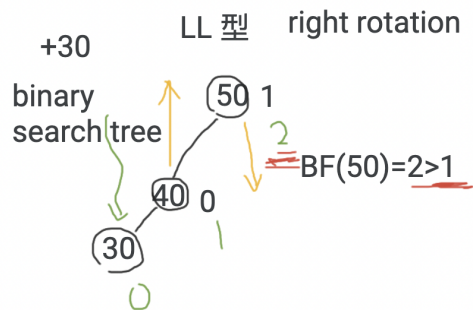
balance factor 平衡因子 BF \rightarrow 針對某一個節點的高度計算結果 $\rightarrow BF(n)$, $n \rightarrow$ node
 $|BF(n)| \leq 1 \rightarrow -1, 0, 1$



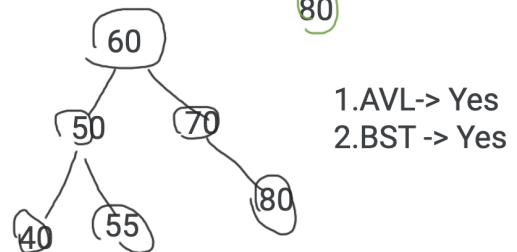
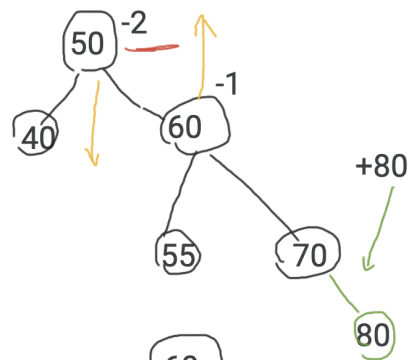
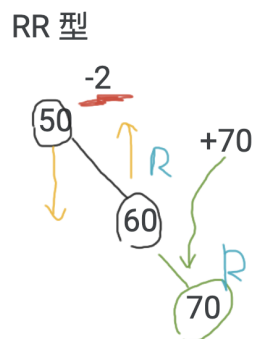
AVL tree 加入 node

- 針對四種不同的 types \rightarrow 作 re-balanced

LL type

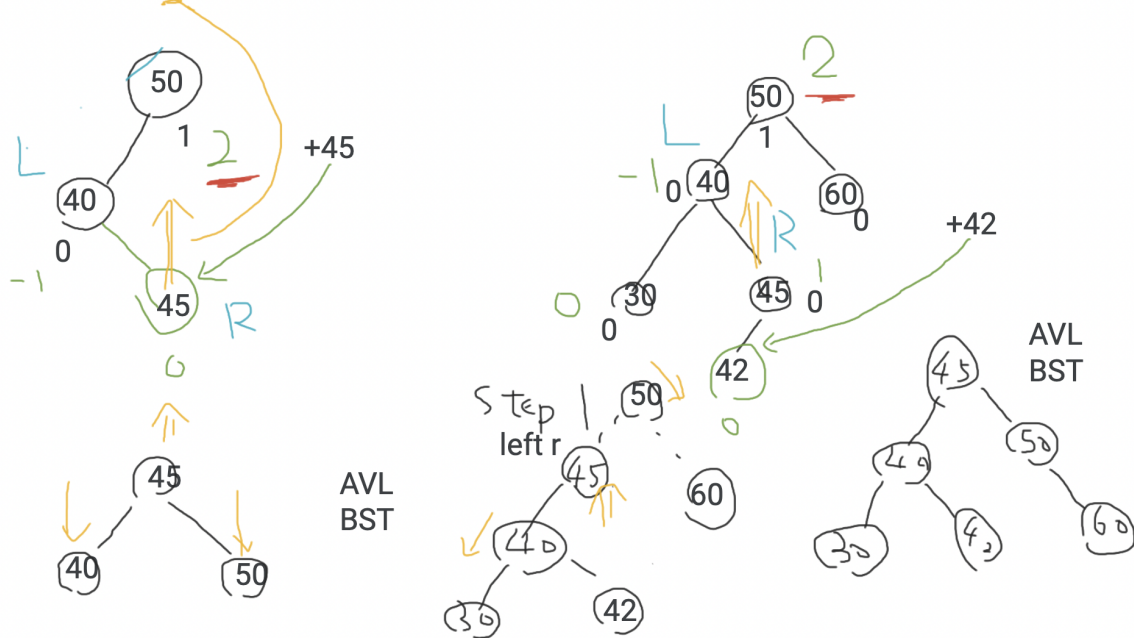


RR type → left rotation



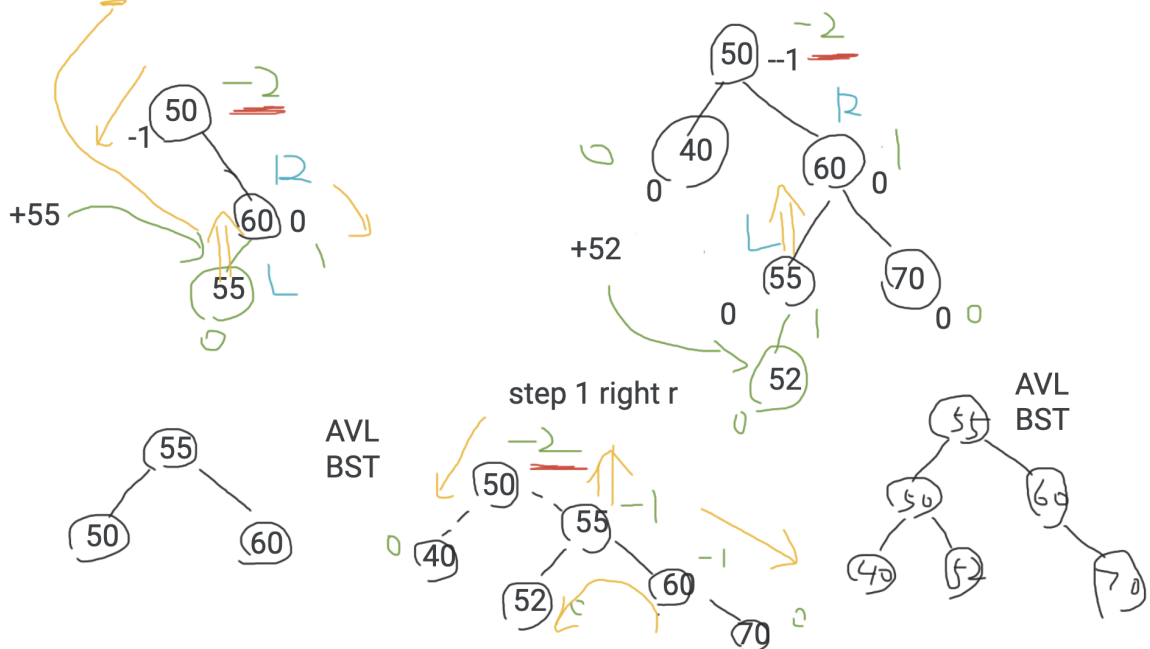
LR type

LR type -> (R45, left rotation) -> 整個right rotation



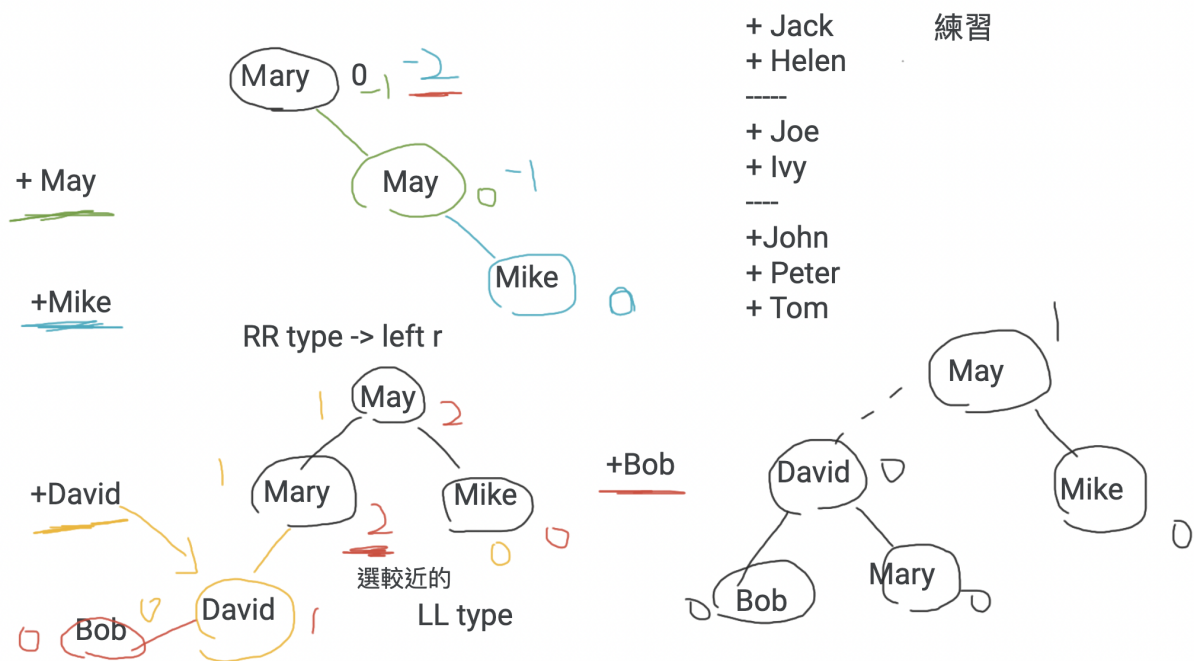
RL type

RL type -> (L55 Right rotation), 整個left rotation



例子

字串 AVL -> BST 原則大小 alphabetic order 大小



tldraw

A free and instant collaborative diagramming tool.

; <https://www.tldraw.com/r/V5WtU61rVHub3ZHeUXEg8?v=11,4492,1920,1004&p=page>



實作

```
#include <iostream>
using namespace std;
```

```
class Node{
public:
    int key;
    Node* left;
    Node* right;
    int height;
```

```

    Node(int k):key(k), left(nullptr), right(nullptr), height(1)
};

class AVLTree{
public:
    Node* root;

    AVLTree():root(nullptr){}

    int height(Node* n){
        if(n==nullptr) return 0;
        return n->height;
    }

    int getBalance(Node* n){
        if(n==nullptr) return 0;
        return height(n->left) - height(n->right);
    }

    void updateHeight(Node* n){
        if(n!=nullptr){
            n->height = max(height(n->left), height(n->right))+1;
        }
    }

    Node* rightRotation(Node* y){
        Node* x=y->left;
        Node* T2 = x->right;

        x->right = y;
        y->left = T2;

        updateHeight(y);
        updateHeight(x);

        return x;
    }
};

```

```
    }  
};  
  
int main()  
{  
    cout << "Hello, World!";  
    return 0;  
}
```