

Graphs Are Everywhere

Christopher Hoult
@choult

Who is this guy?

Practicing PHP commercially since 2004

Senior Software Engineer at Datto

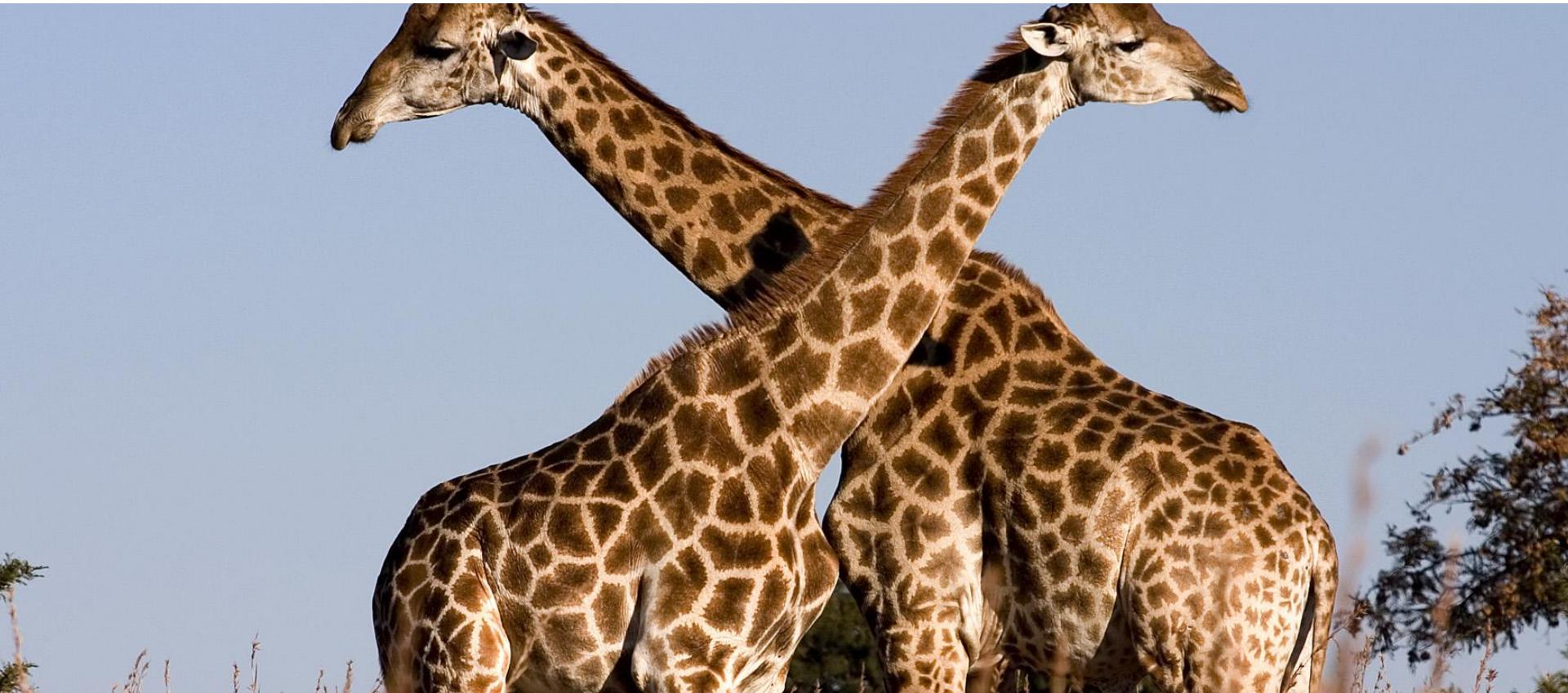
Formerly at DataSift and Time Out Digital

Founder/co-organizer of the PHP Berkshire User Group

I also act



Graphs are everywhere



The Seven Bridges of Königsberg

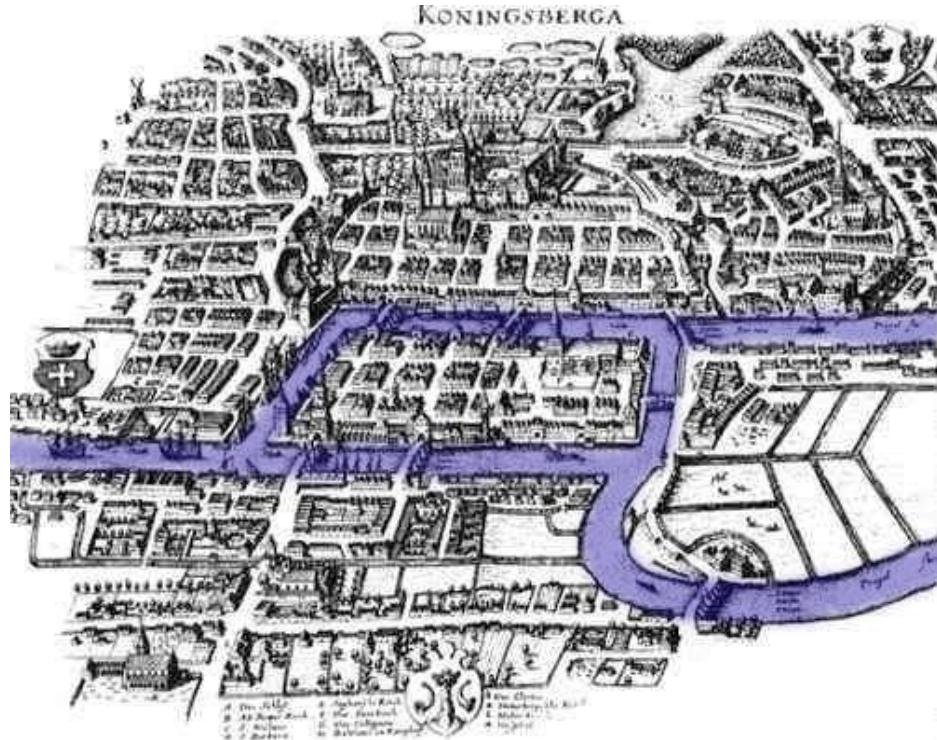
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Now Kaliningrad, Russia;
built around the Pregel River

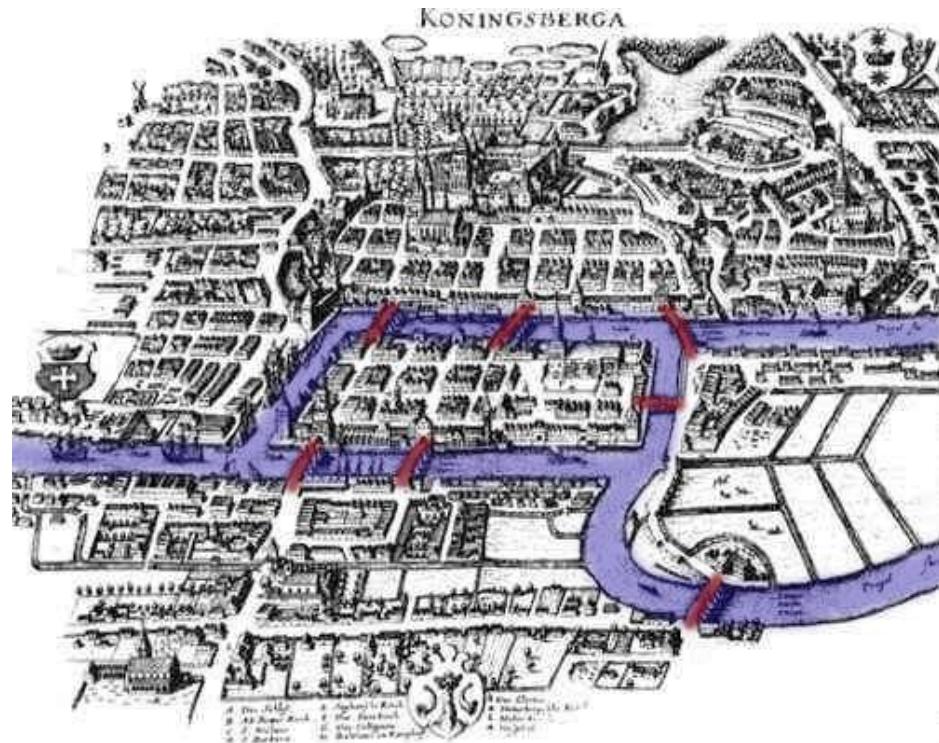


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“Can you walk through the
city, crossing each bridge
only once?”



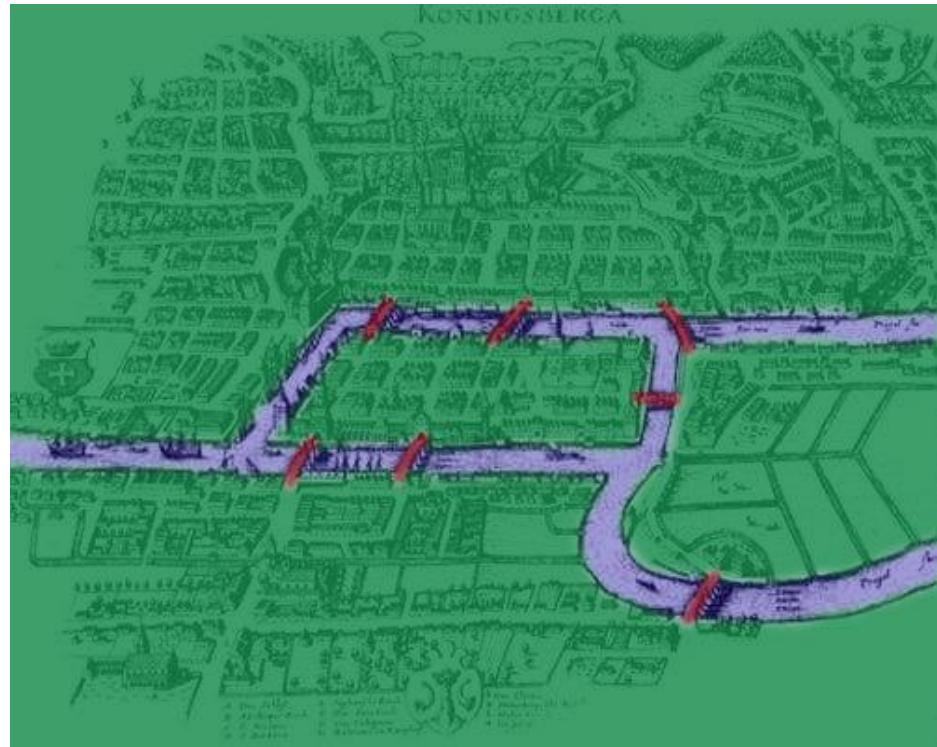
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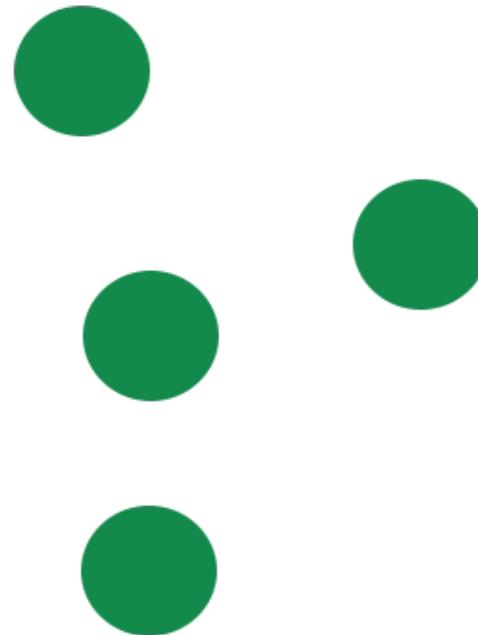
“Can you walk through the
city, crossing each bridge
only once?”

Reduce to four land-masses,
and seven connections



The Seven Bridges of Königsberg

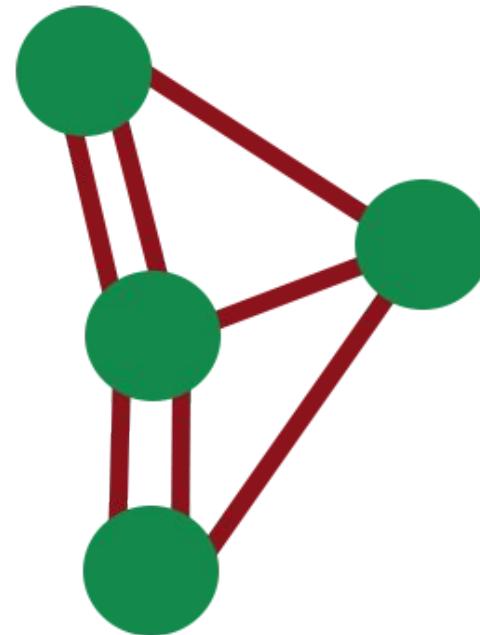
Nodes (or vertices)



The Seven Bridges of Königsberg

Nodes (or vertices)

Edges

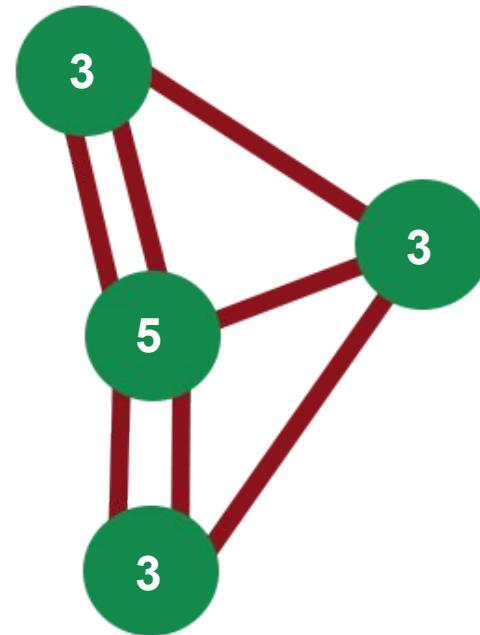


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Nodes (or vertices)

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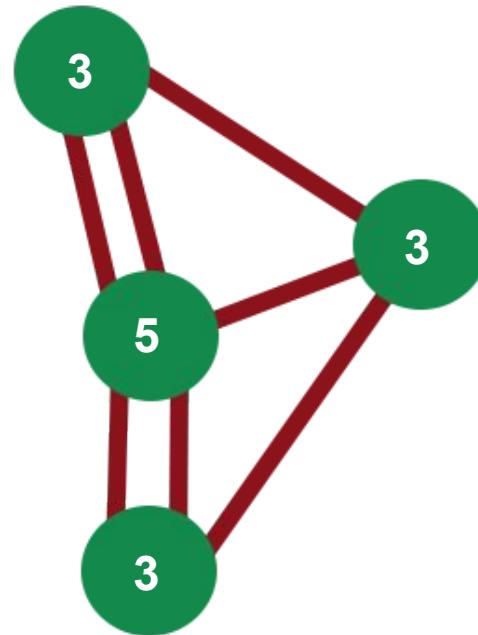
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Example of an undirected graph - you can go either way over each bridge.



The Seven Bridges of Königsberg

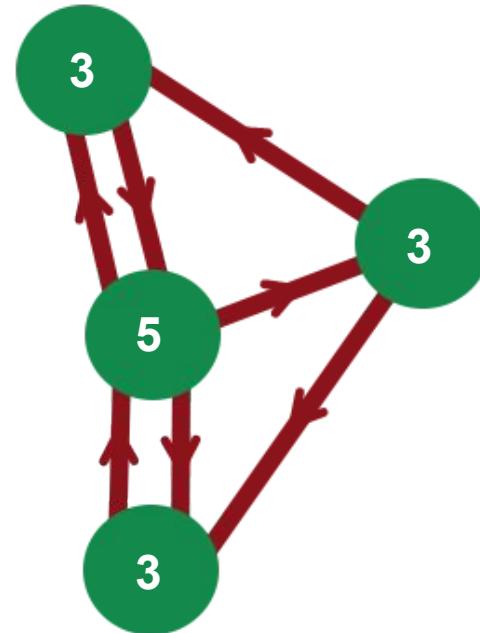
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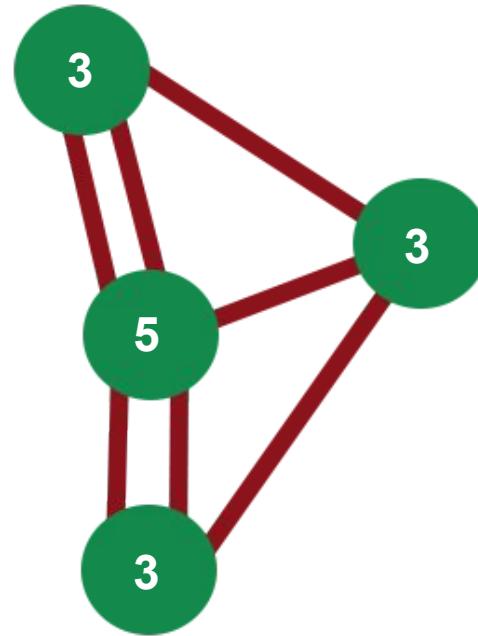
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A one-way system would be a directed graph.



The Seven Bridges of Königsberg

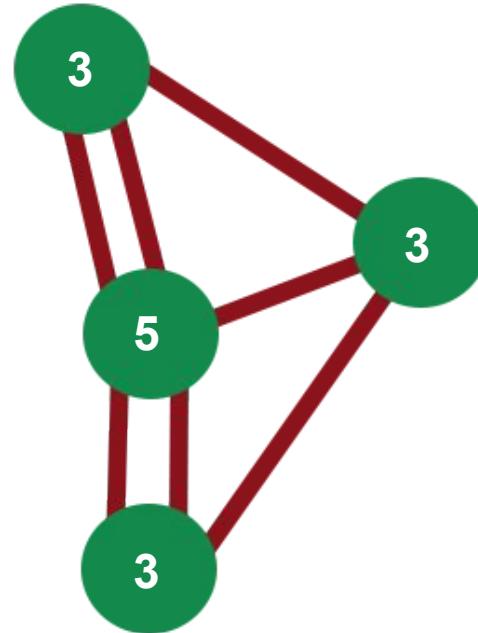
To get into and out of a node, there must be an even number of edges; its *degree* must be even.



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Only the start and end can have odd degrees.

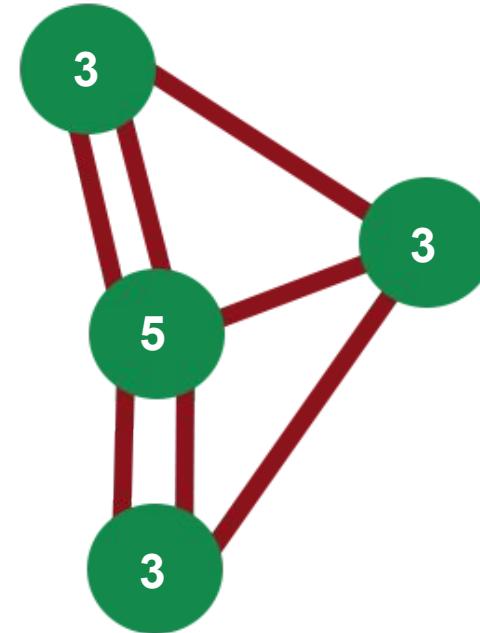


The Seven Bridges of Königsberg

To get into and out of a node, there must be an even number of edges; its *degree* must be even.

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Therefore, only possible if zero or two nodes of odd degree - these will be start and end.

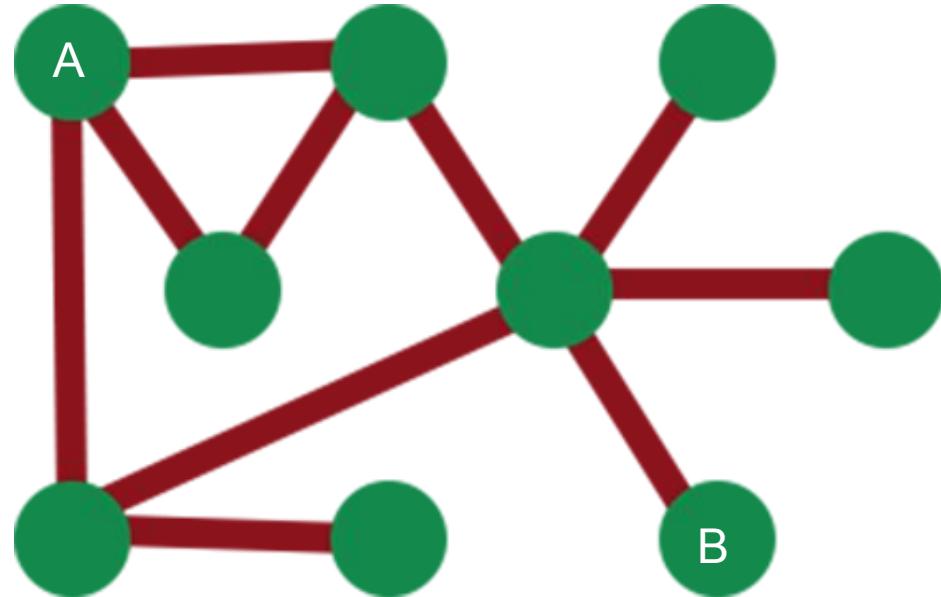


Pathfinding



Pathfinding

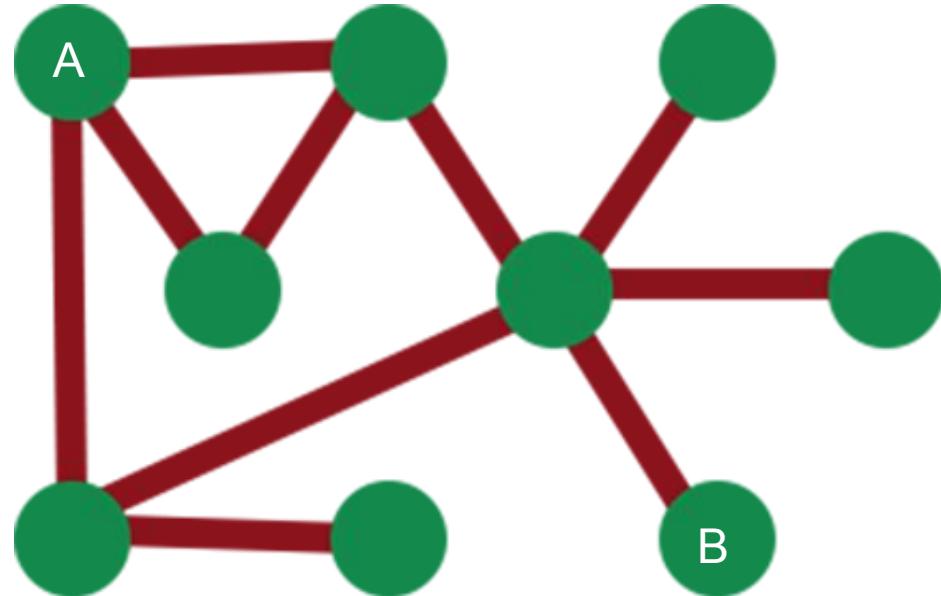
Problem: Find your way from arbitrary node A to arbitrary node B.



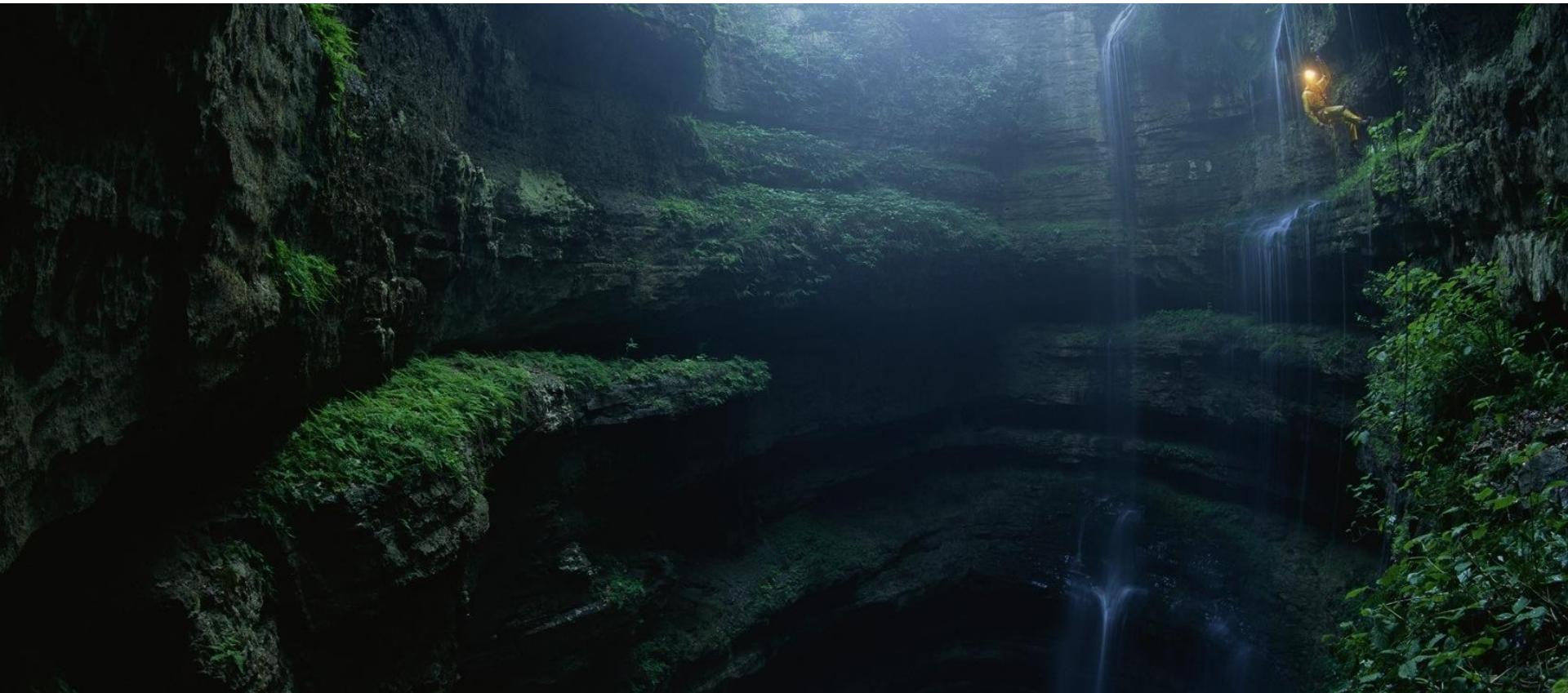
Pathfinding

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Two approaches: depth-first and breadth-first.



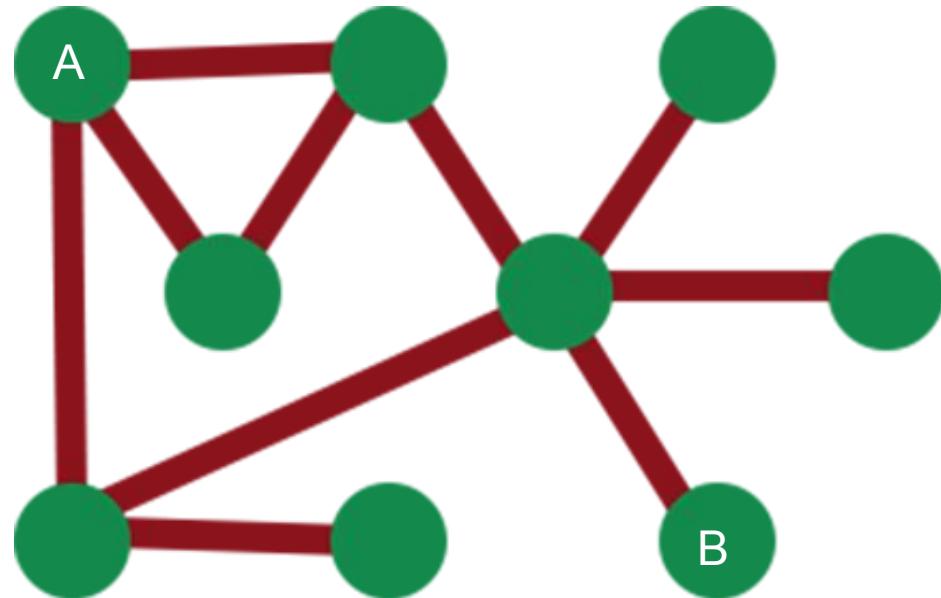
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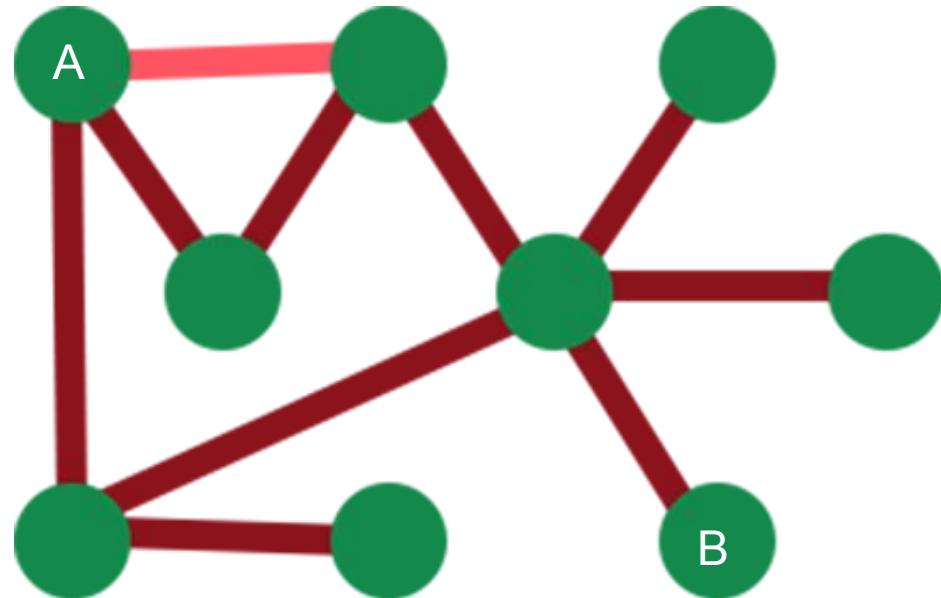
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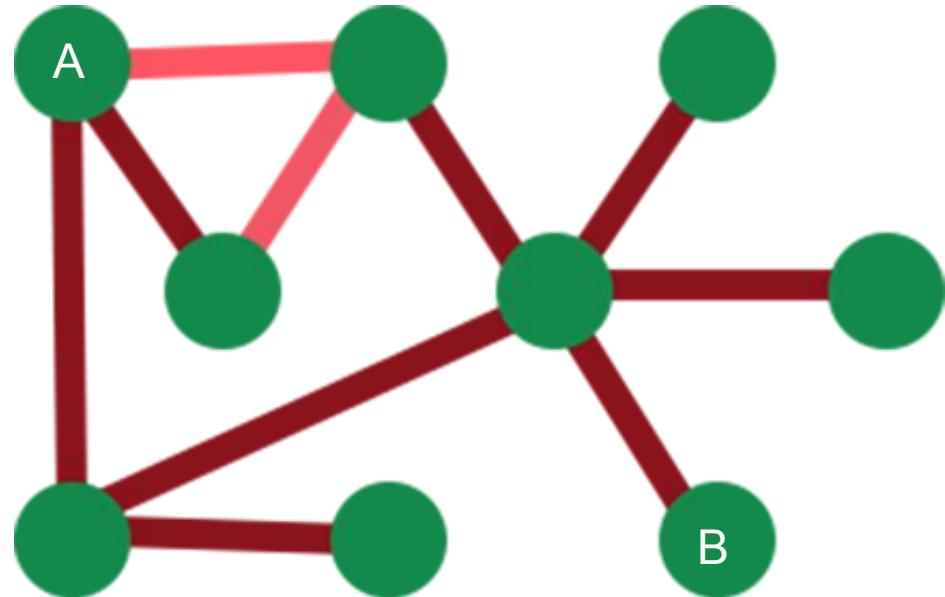
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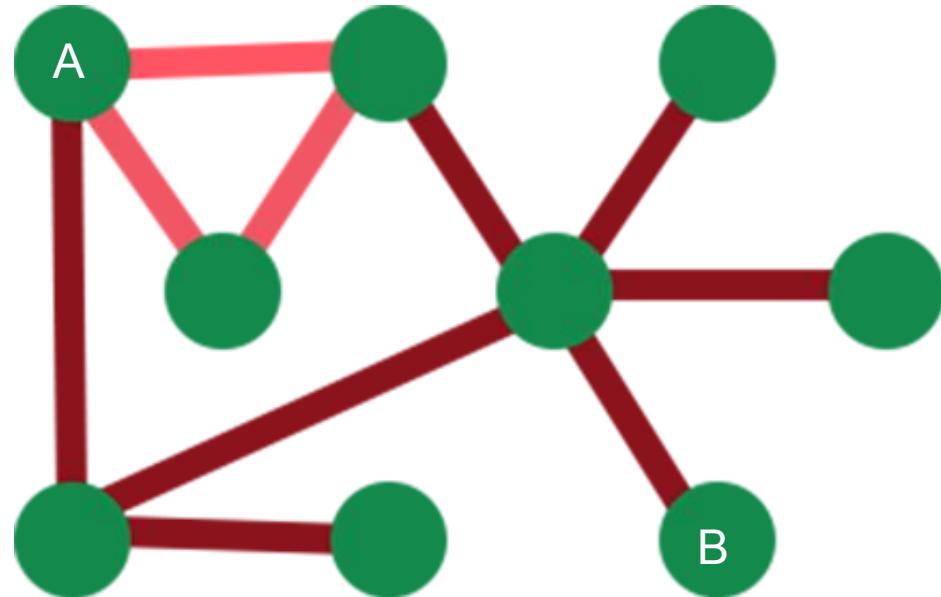
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A cycle is where a collection of nodes are interconnected such that a path will loop back on itself.

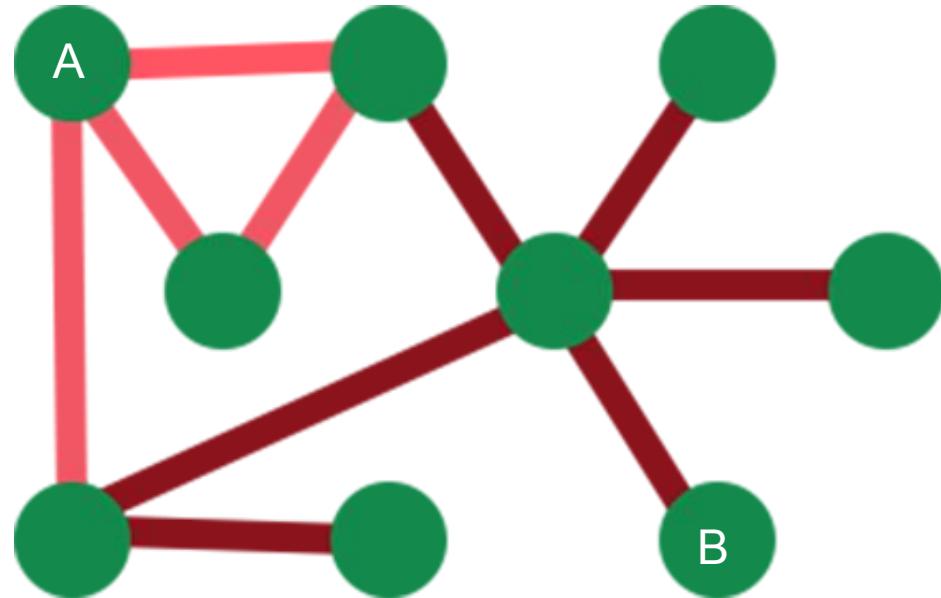


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Cope by tracking which nodes have already been traversed.

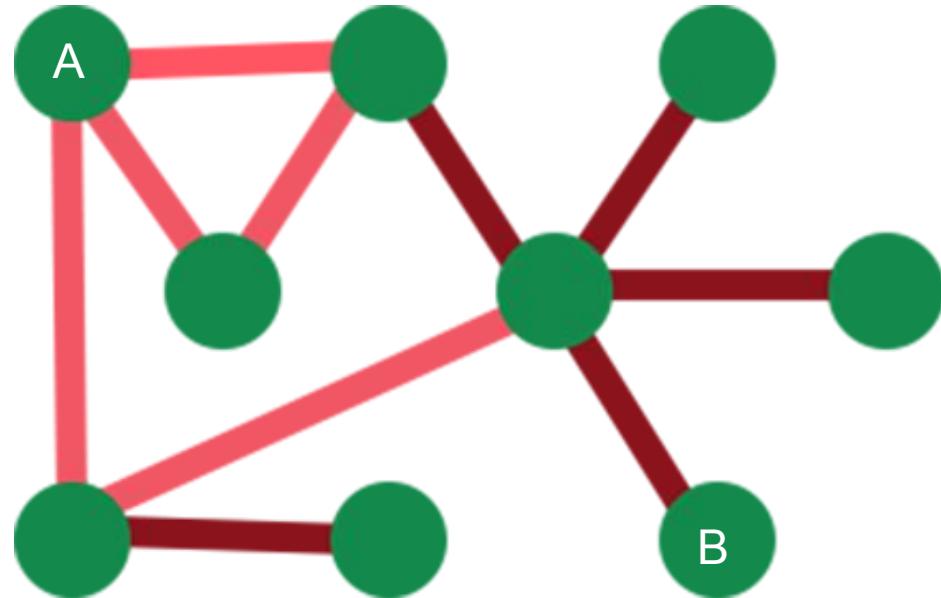


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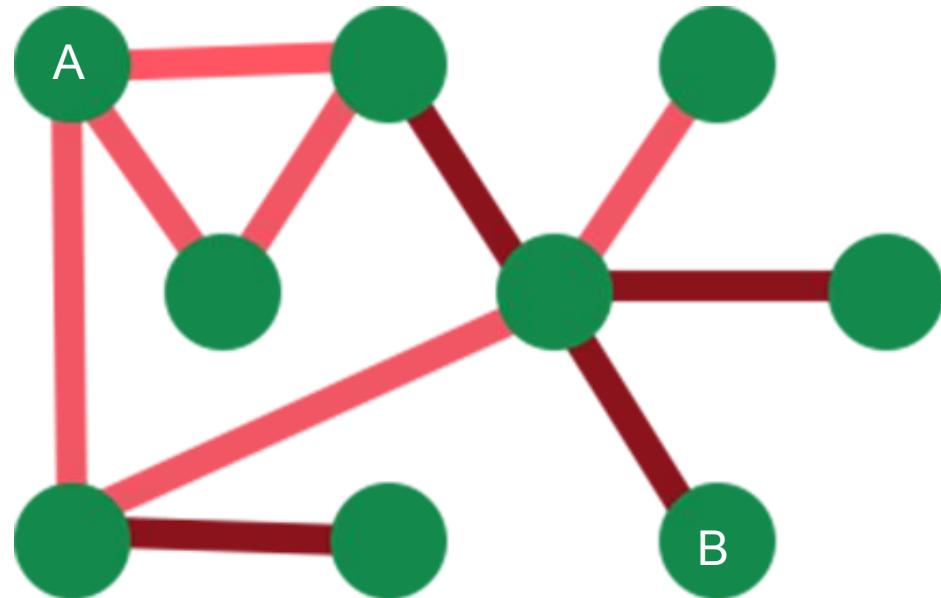
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We've now hit a dead-end, and can go no further - so backtrack and try again.

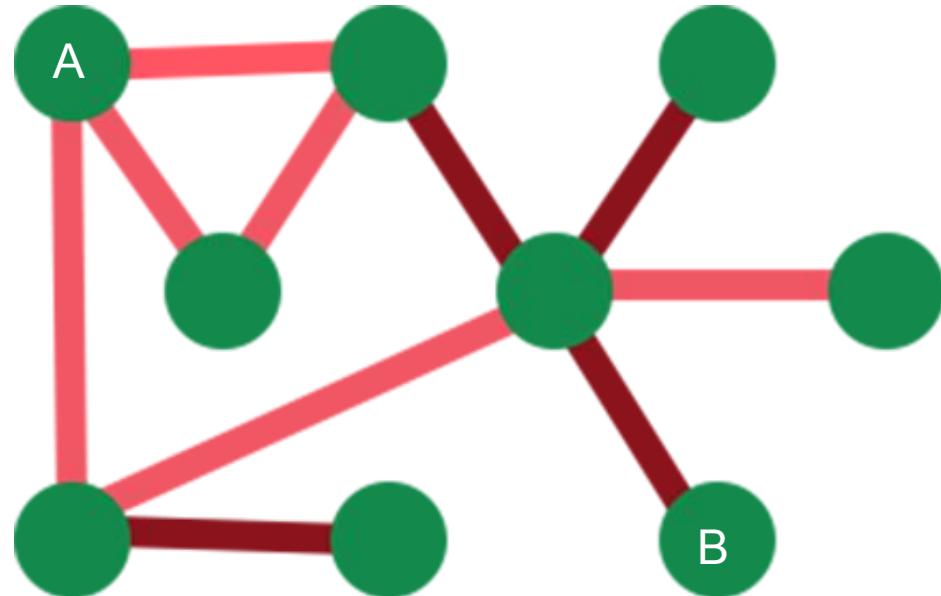


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Best-case: we get to node B as quickly as possible.

Worst-case: we get to node B last, having explored the whole graph!

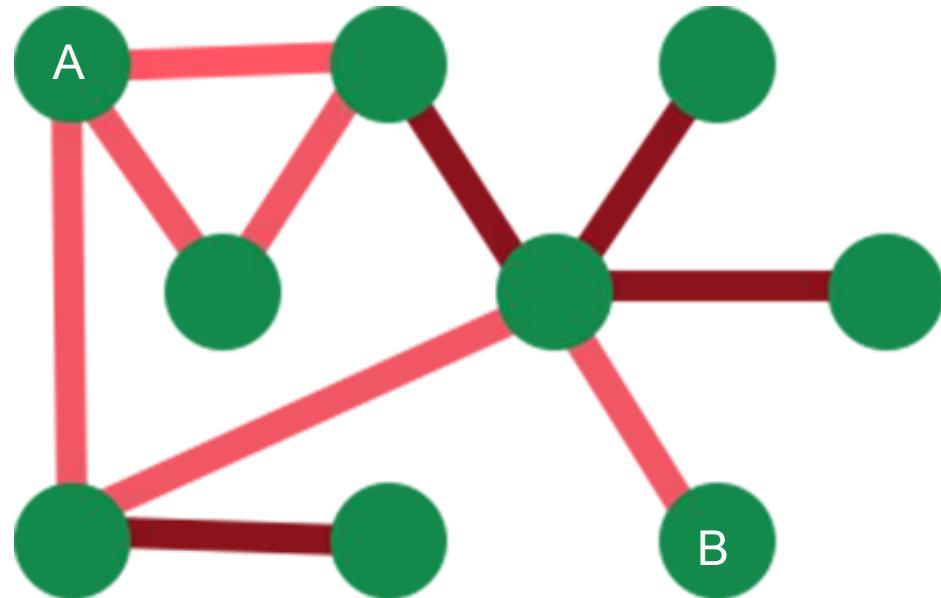


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Depth-first: Mazes

... happy to have another one. His former captain and perpetual apologist, sent on the committee, apparently, he could trust

sensitivity and a selfish obsession with how he was being portrayed by the media that he will be remembered. Funny people, folk.

Effectively, it is a genuine reflection of his character.

In the chapter dealing with the exhilarating Grand Prix, for example, and his spat with his dangerous team-mate, his driving is so

The various pieces of fresh fruit are placed
over the actual raw food.
The British Virgin Islands. Over the
years, the country has paid less attention
to its natural beauty, and more to its
first-choice tourists.
Government focused on the 100,000
British prisoners released every year.
The idea behind "a prison system that

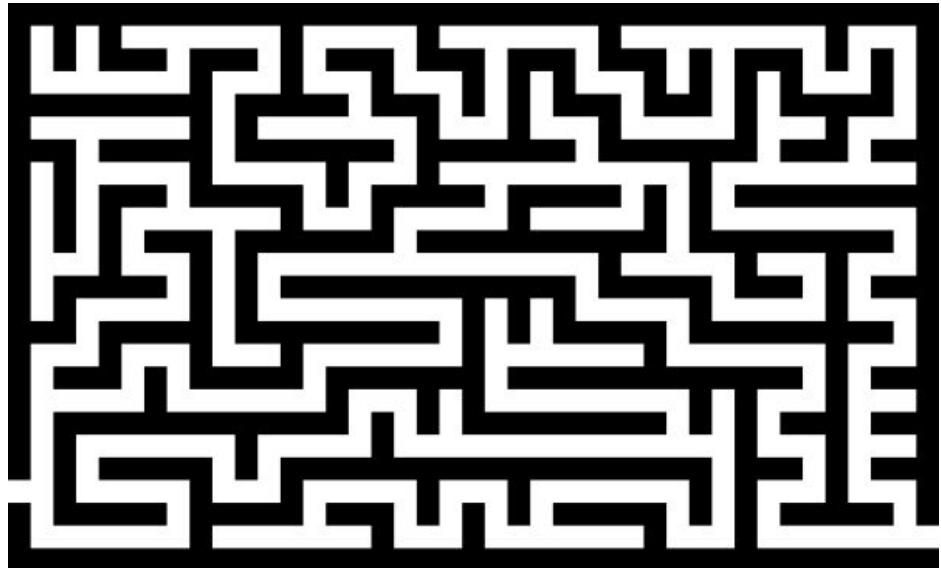
Depth-first: Mazes

Solving mazes with
depth-first:

At a junction, take first path
on left, keep going.

If you hit a dead end,
backtrack until you can take
another turn.

Repeat...



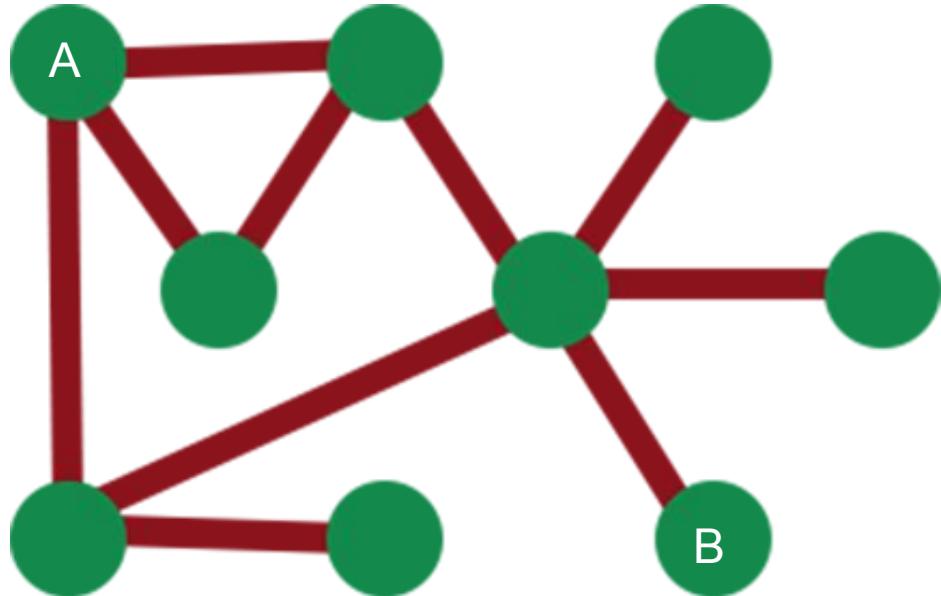
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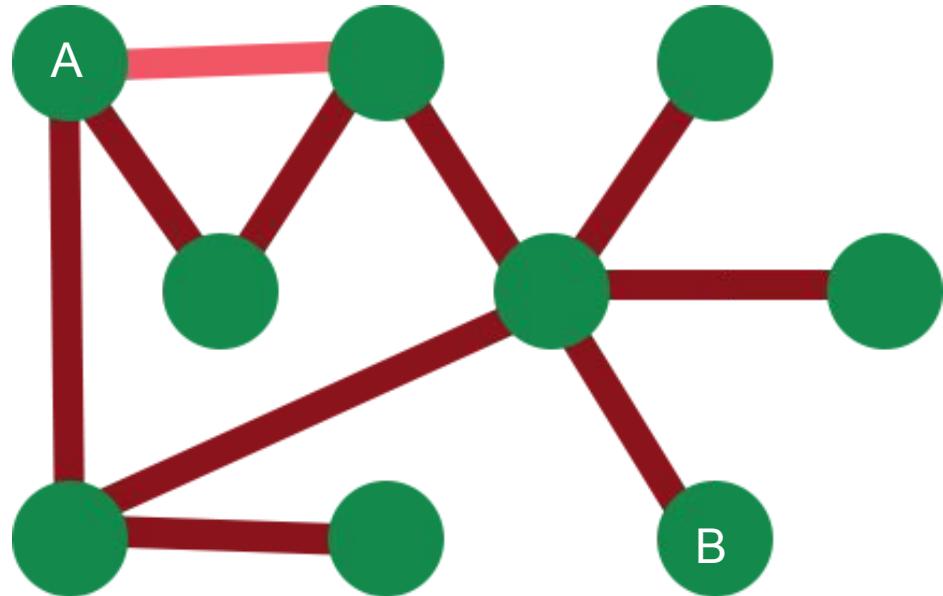
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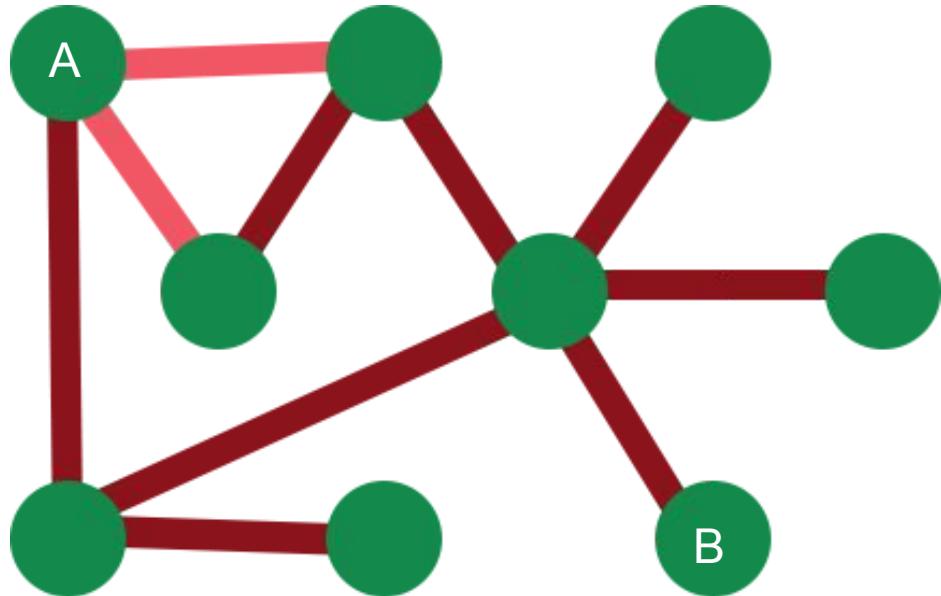
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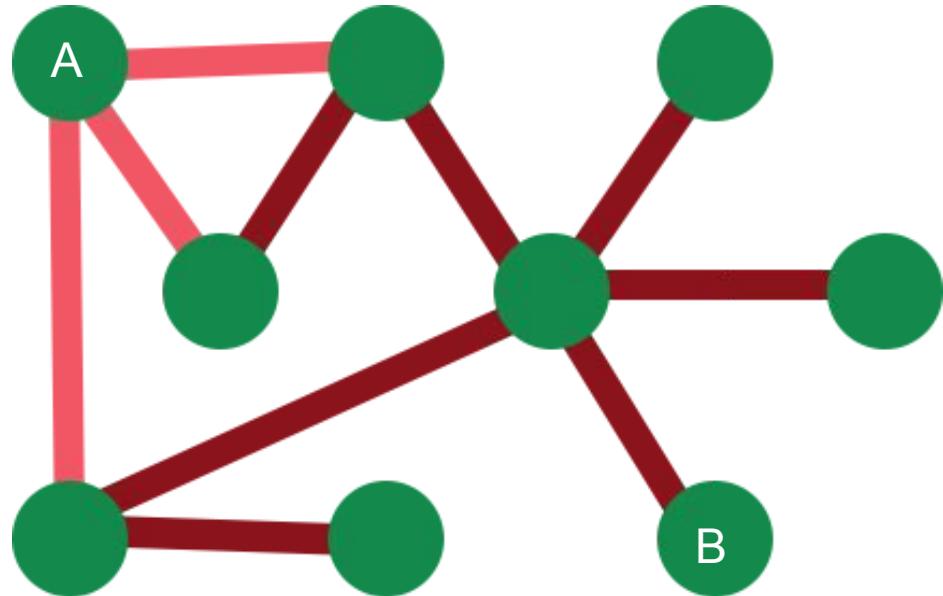
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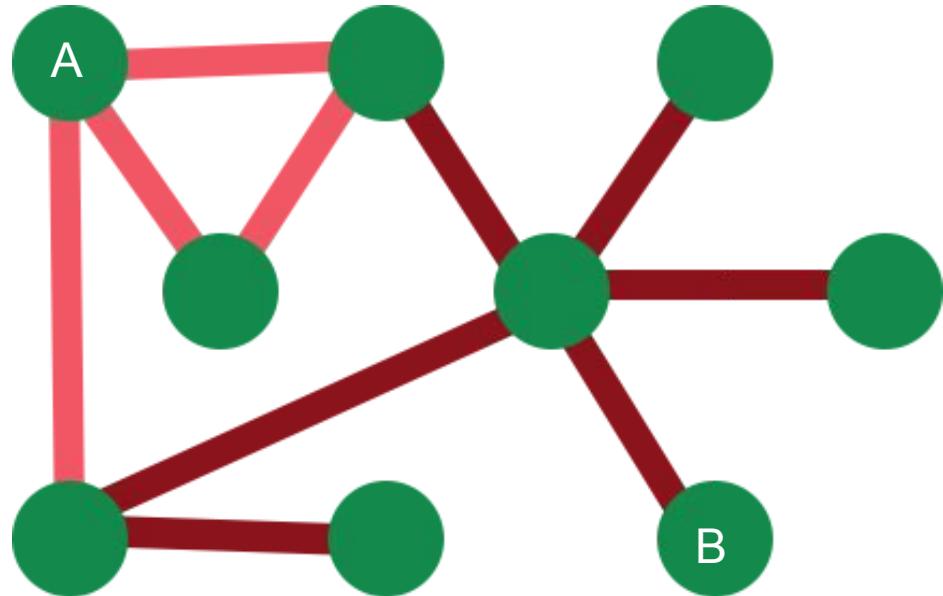
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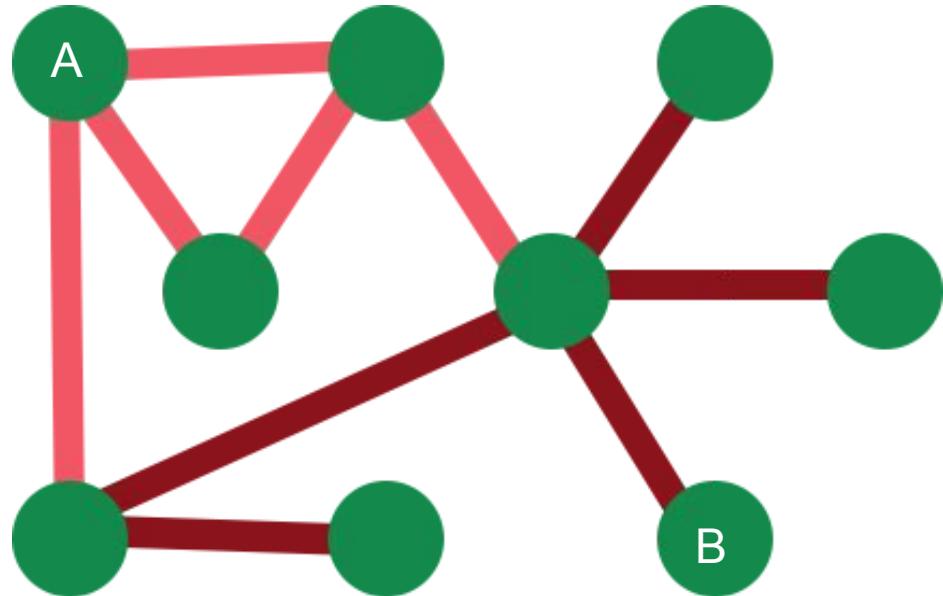
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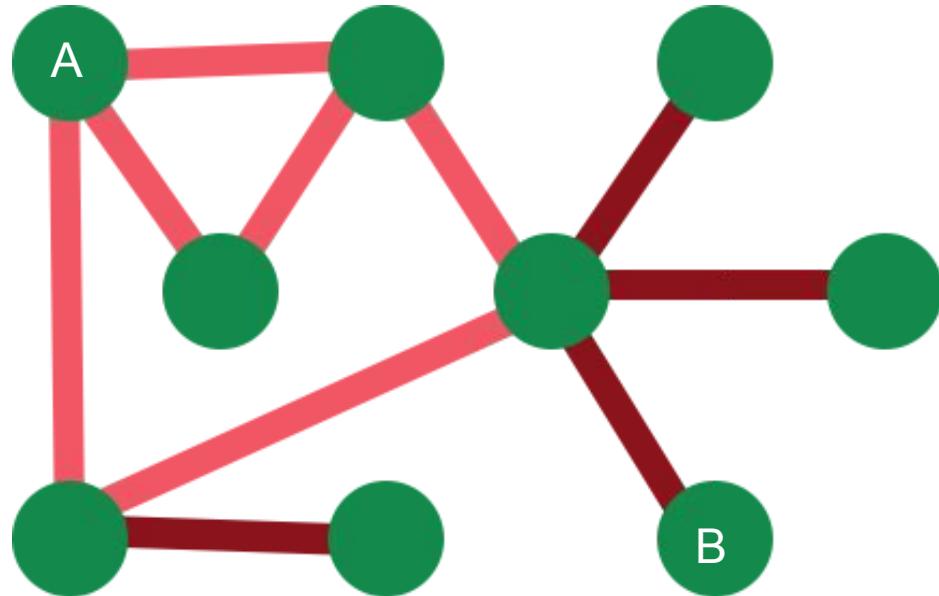
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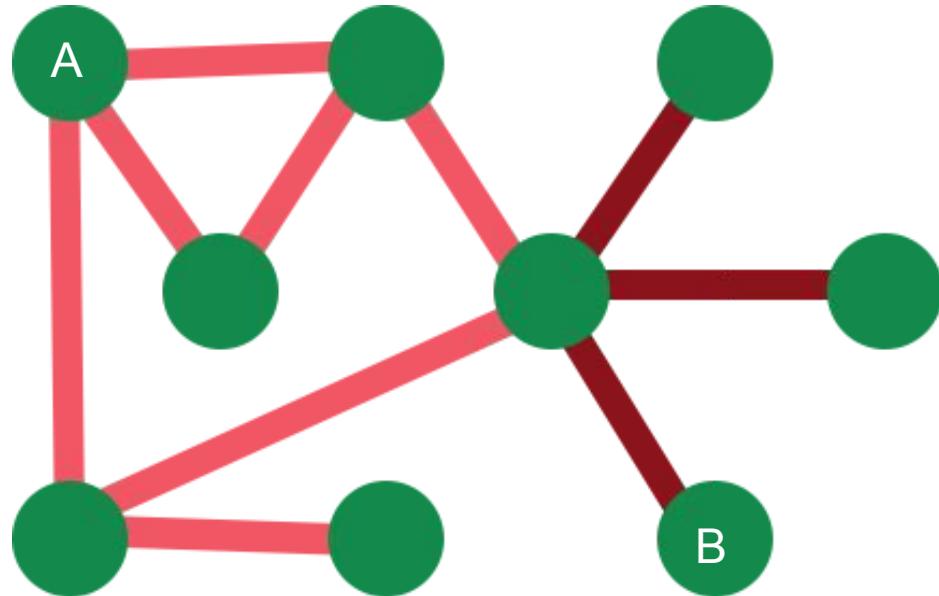


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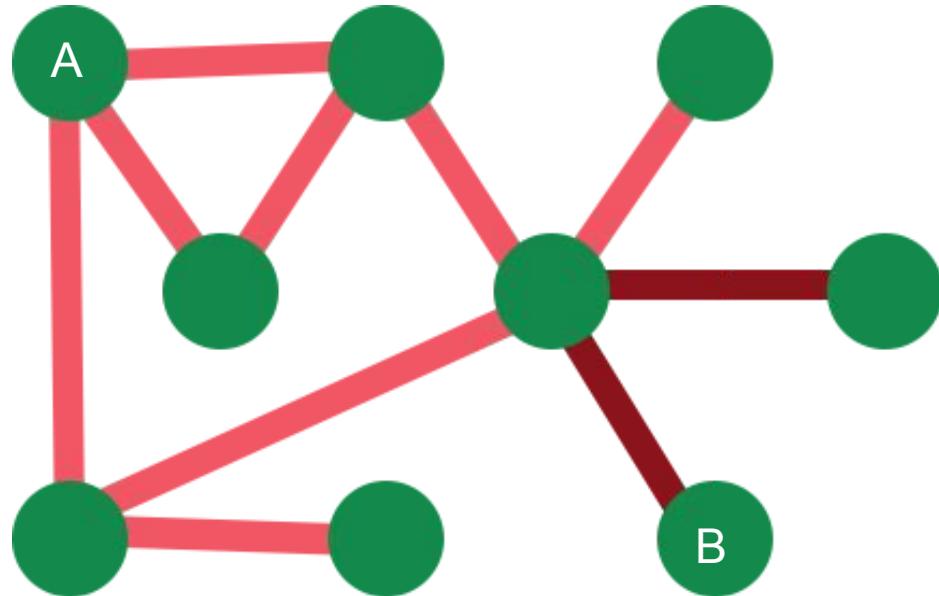


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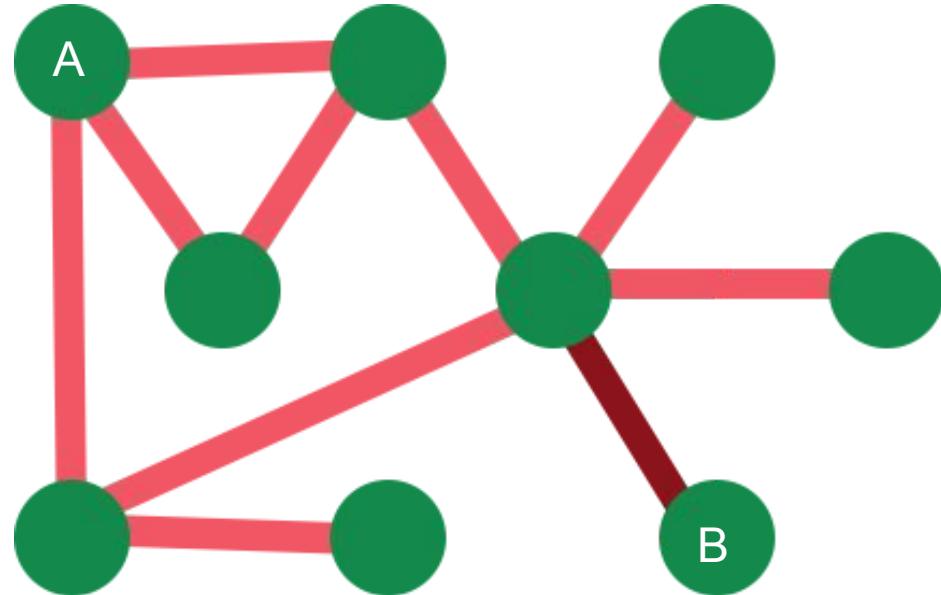


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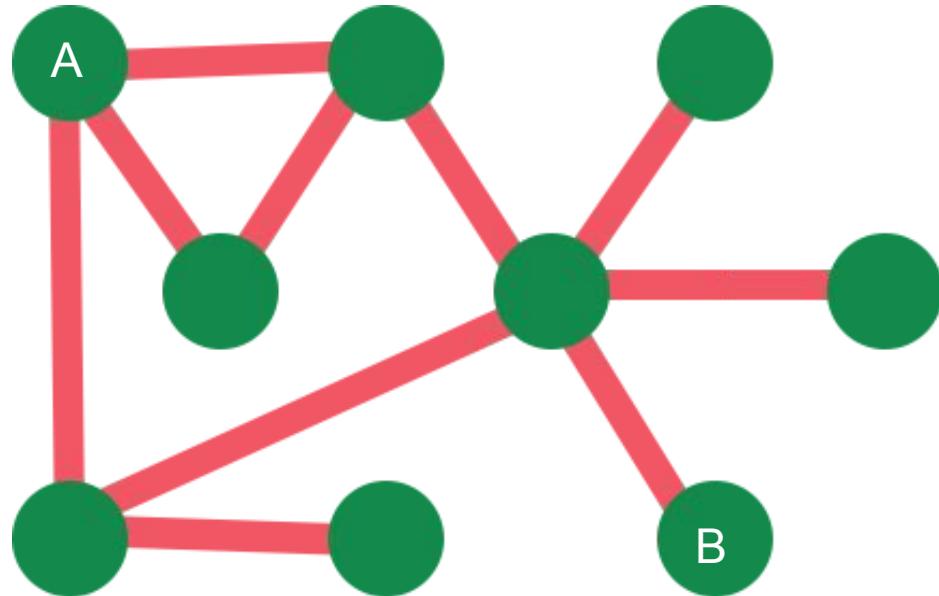


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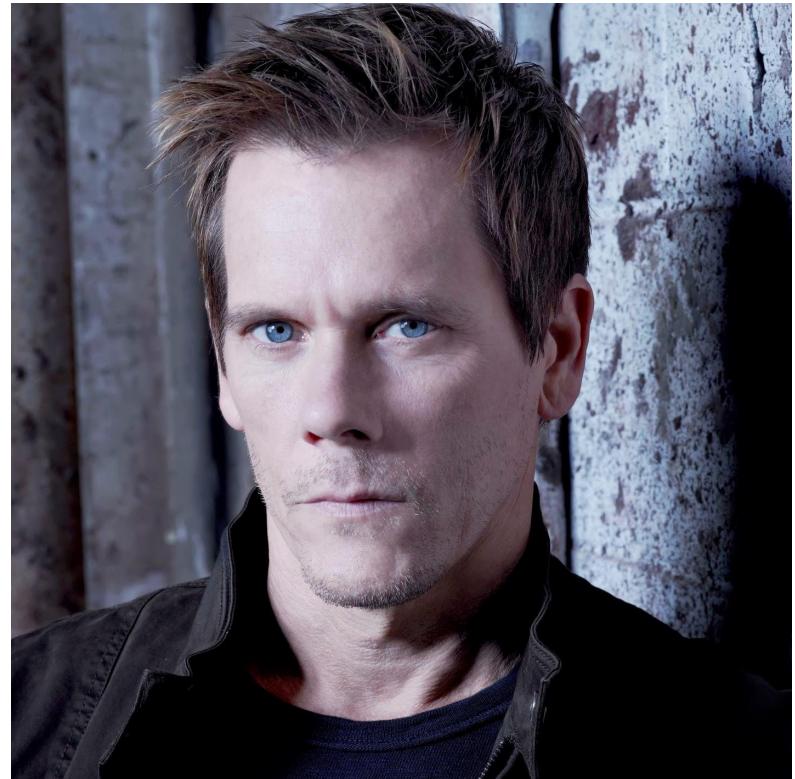


Breadth-first: The six degrees of Kevin Bacon



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An actor's Bacon Number is the number of steps between them and Kevin Bacon via working with other actors on movies.



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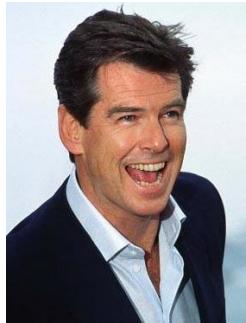
An actor's Bacon Number is the number of movies between them and Kevin Bacon via working with other actors.

Eg. Actor A worked with Actor B on movie 1; Actor B worked with Actor C on movie 2; Actor C worked with Kevin Bacon on movie 3 therefore Actor A's *Bacon Number* is 3



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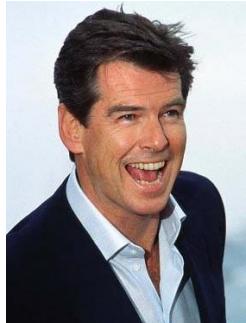
Pierce Brosnan has a Bacon Number of 2



Pierce Brosnan

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Was in

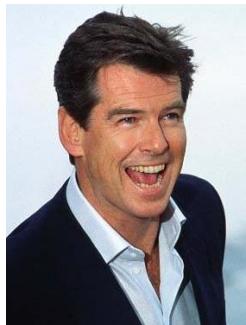


Pierce Brosnan

After the
Sunset

Breadth-first: The six degrees of Kevin Bacon

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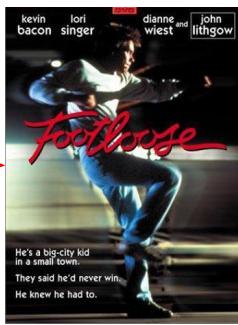
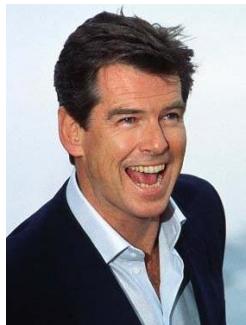
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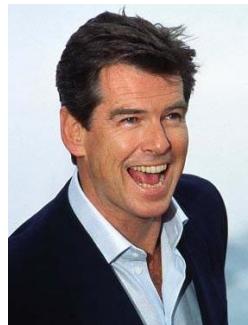
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Was in



With



Was in



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A graph to represent the search-space of IMDB (say) would be huge: 3m+ actors; 2m+ movies and TV shows.



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Depth-first search would be more susceptible to its worst-case scenario - it would just get lost without supreme luck!



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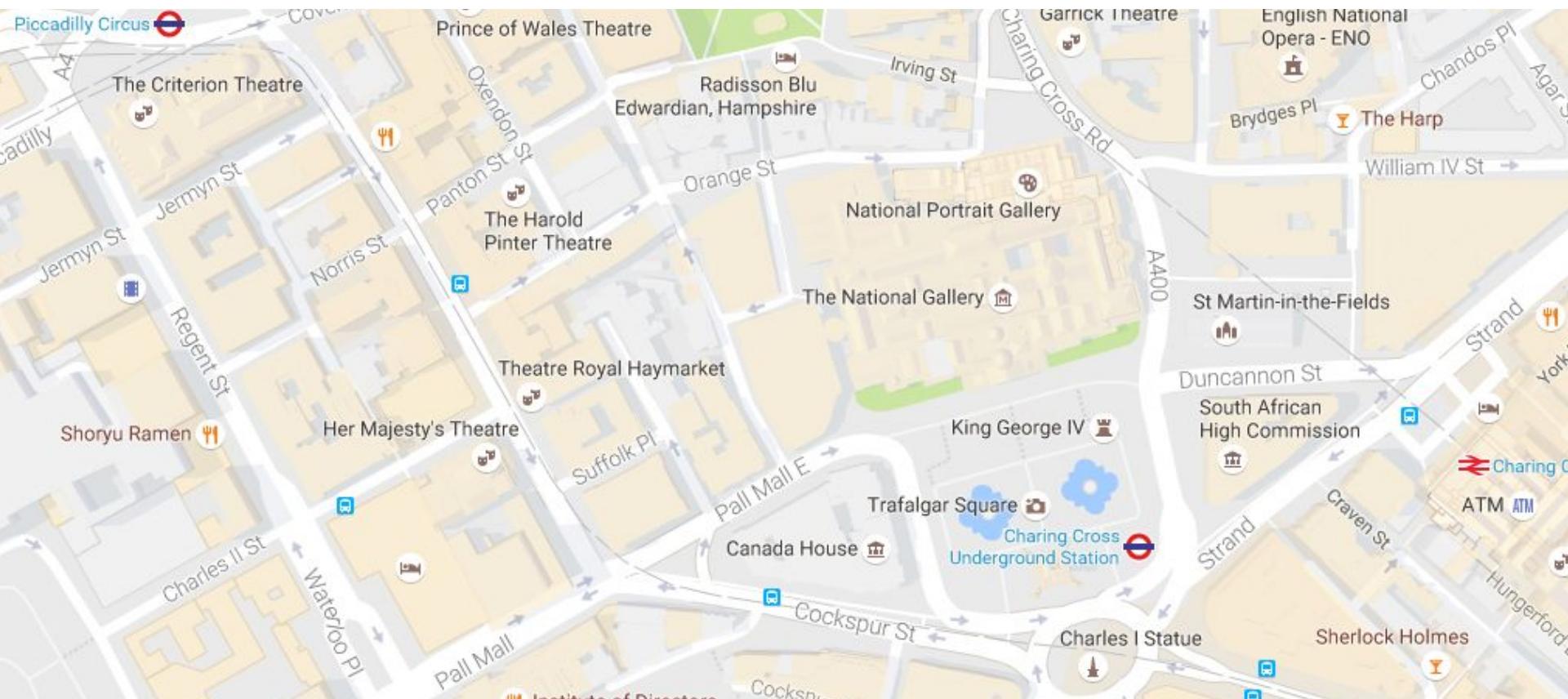
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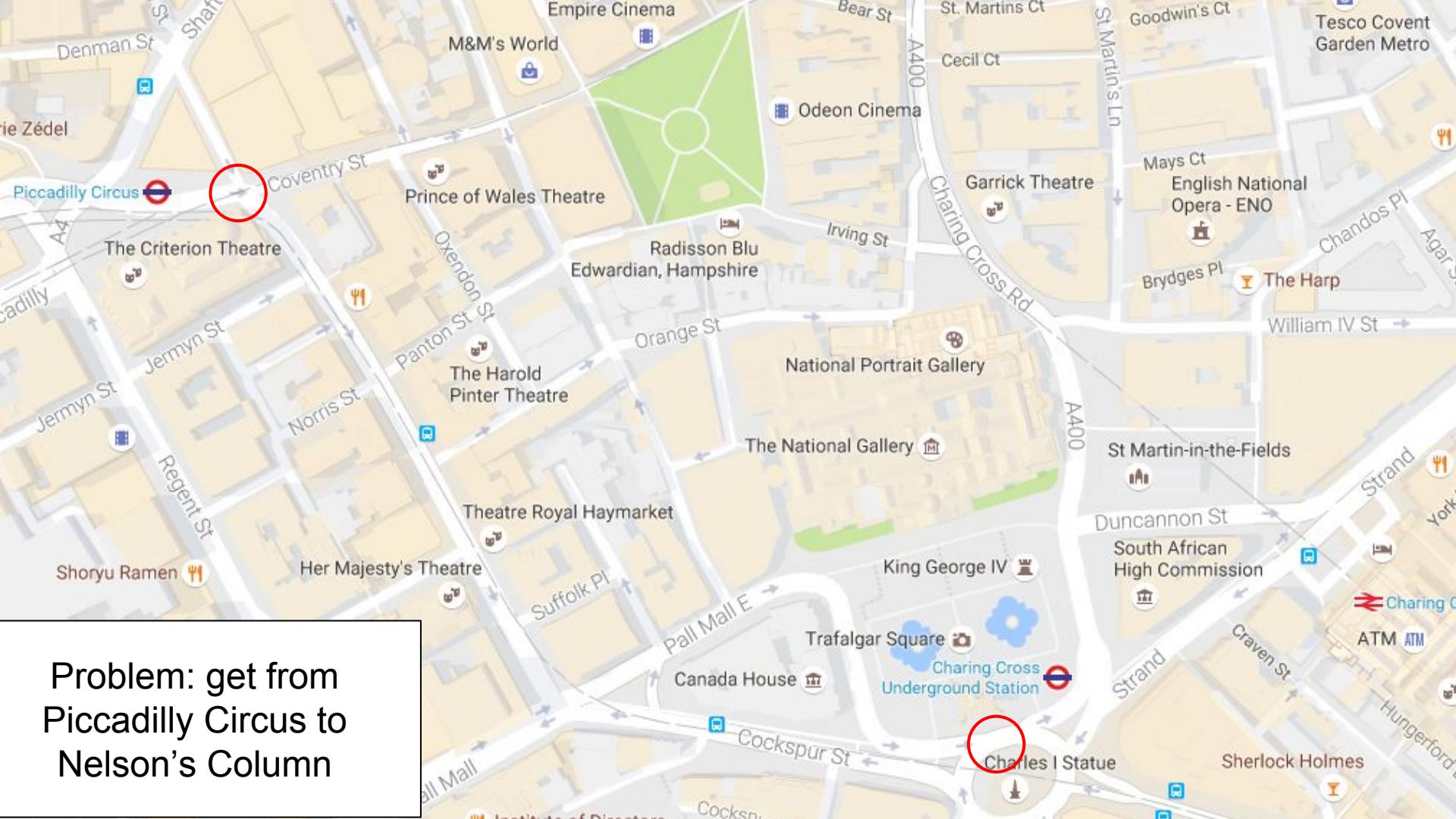
Breadth-first approaches such as Dijkstra's algorithm or A* search would fare much better.



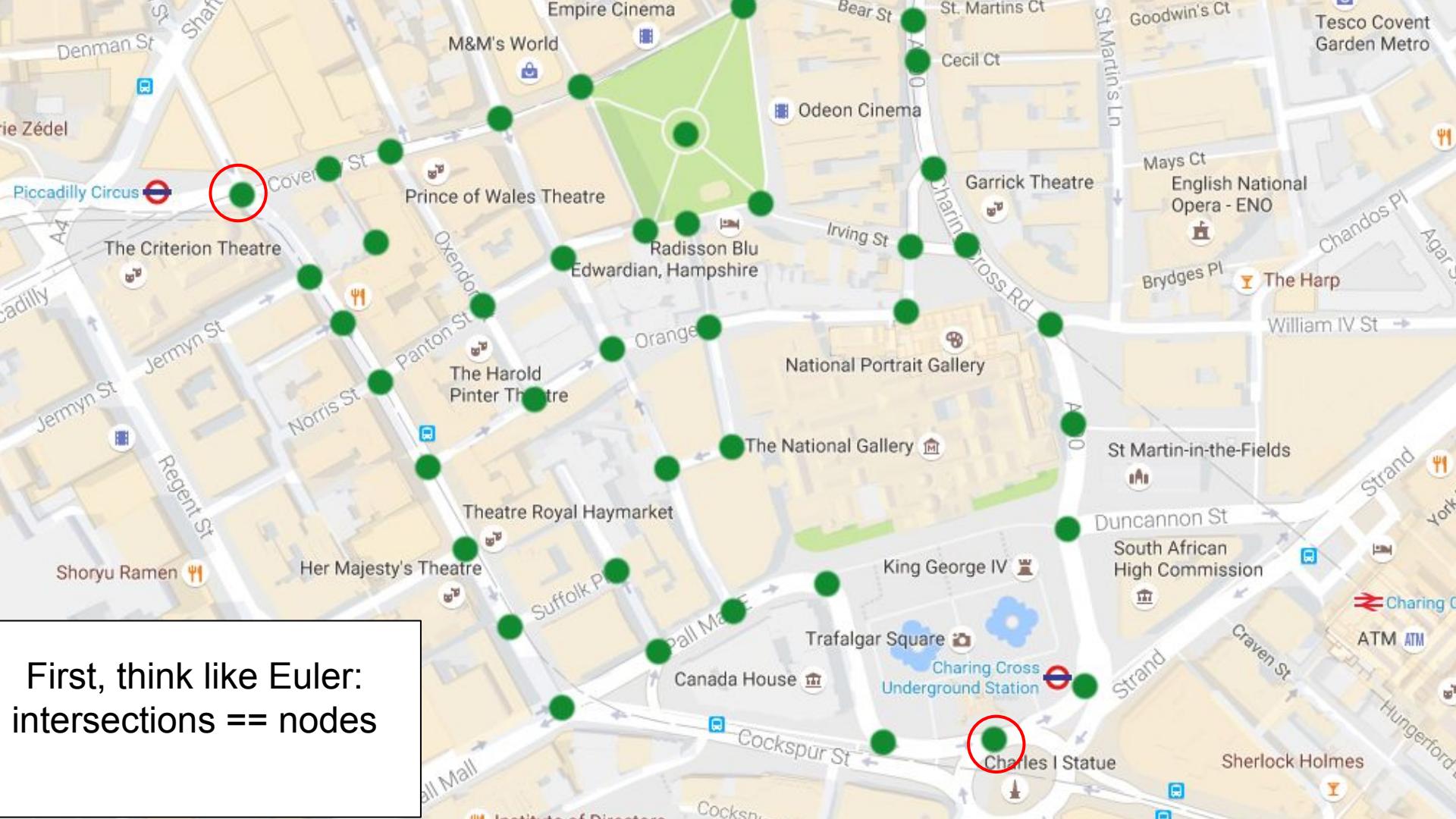


Breadth-first: Dijkstra's algorithm

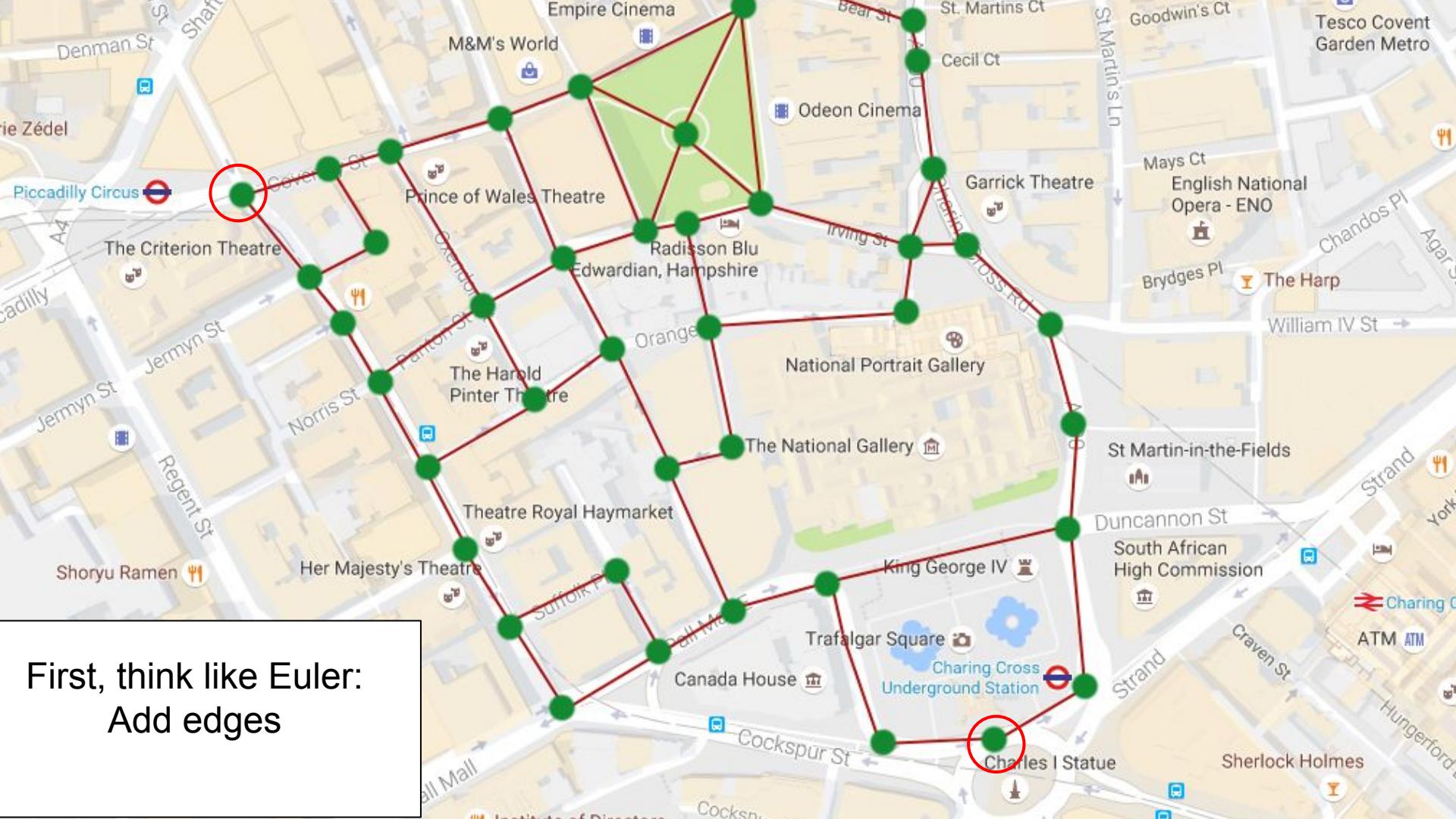




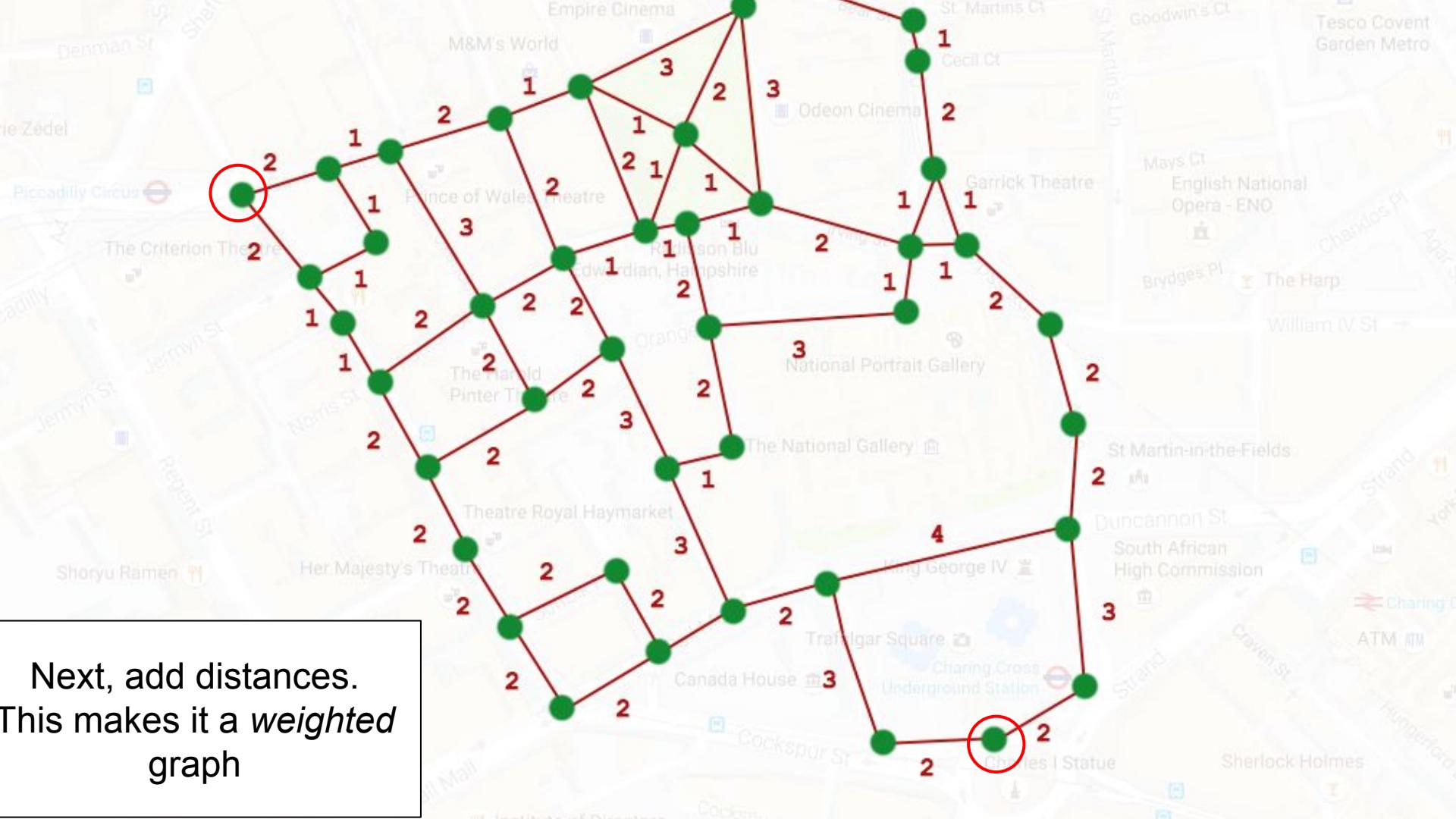
Problem: get from
Piccadilly Circus to
Nelson's Column



First, think like Euler:
intersections == nodes



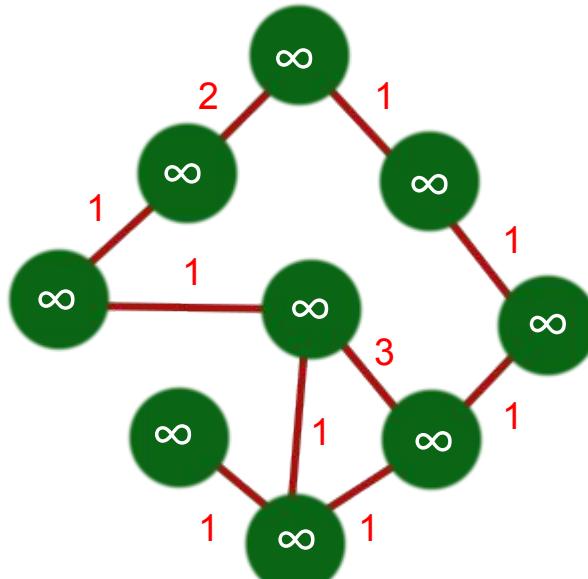
First, think like Euler:
Add edges



Next, add distances.
This makes it a *weighted* graph

Dijkstra's algorithm

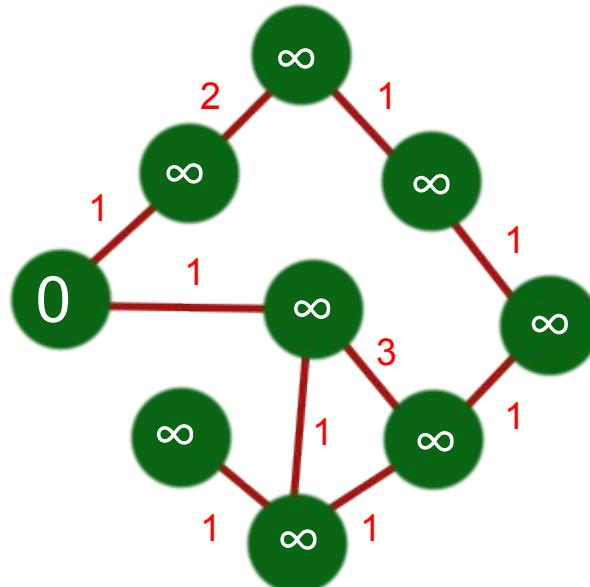
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The start node has score 0

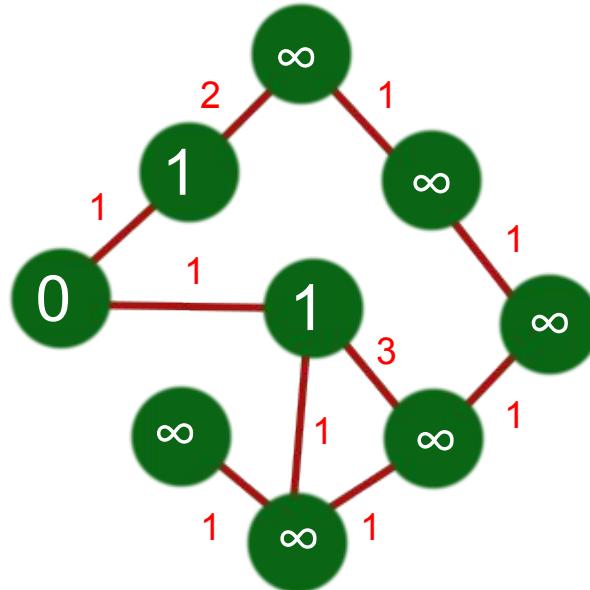


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Visit all connected nodes and set their score to node score plus weight if this number is less than current score



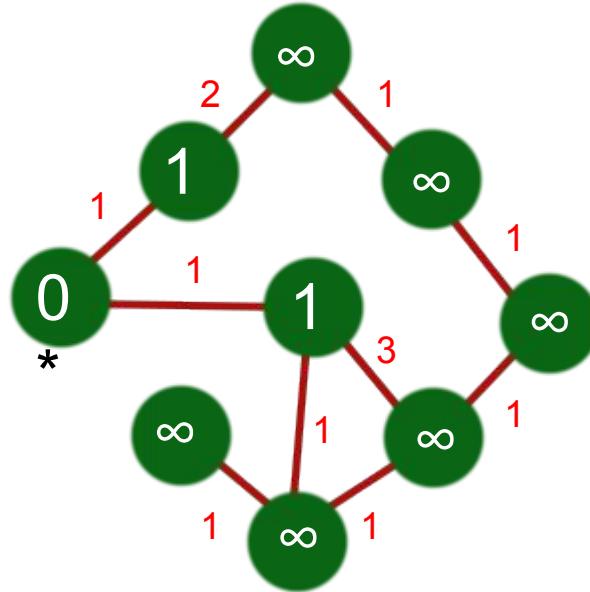
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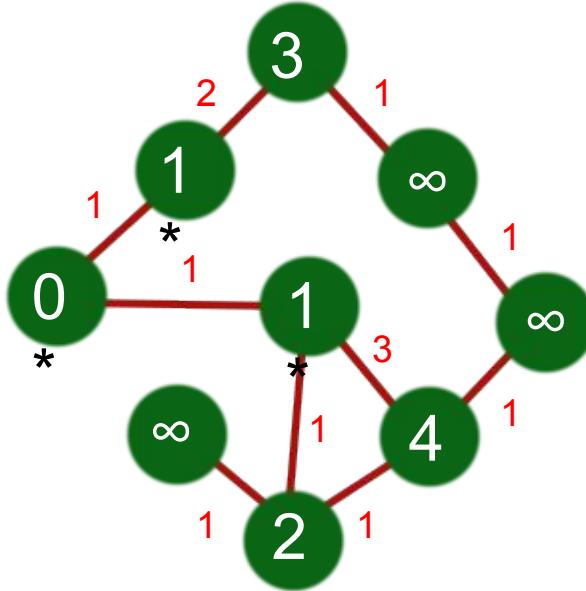
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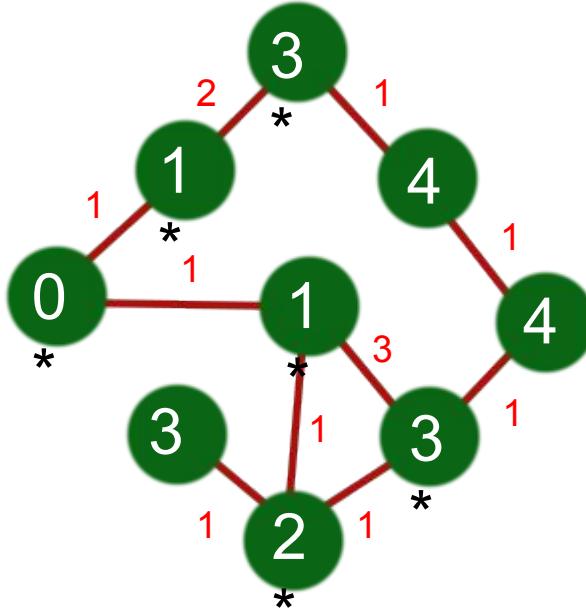
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Once all nodes at current depth *with a score* are marked as visited,
proceed to next depth.



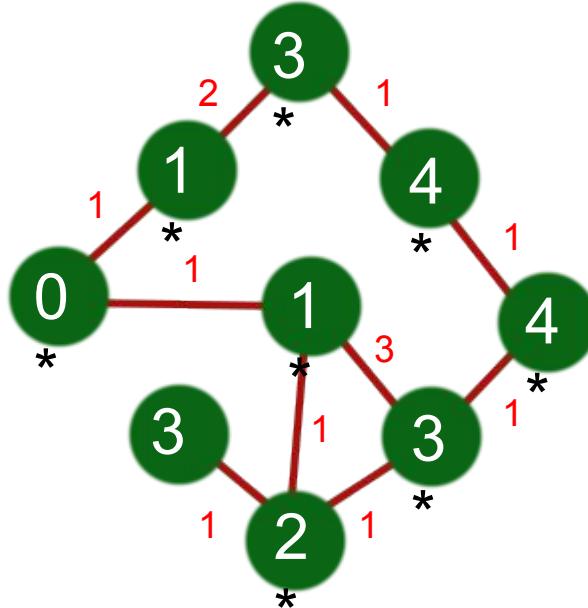
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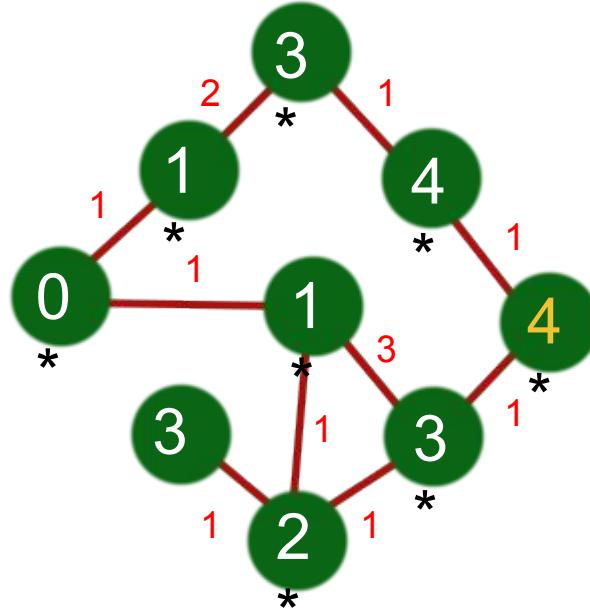
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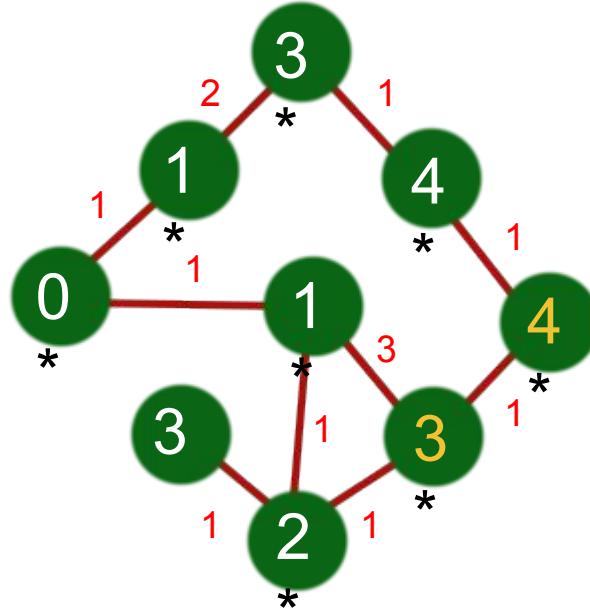
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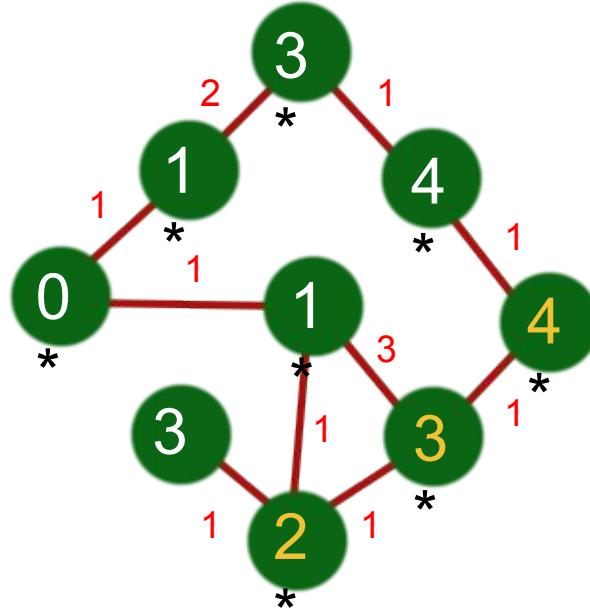
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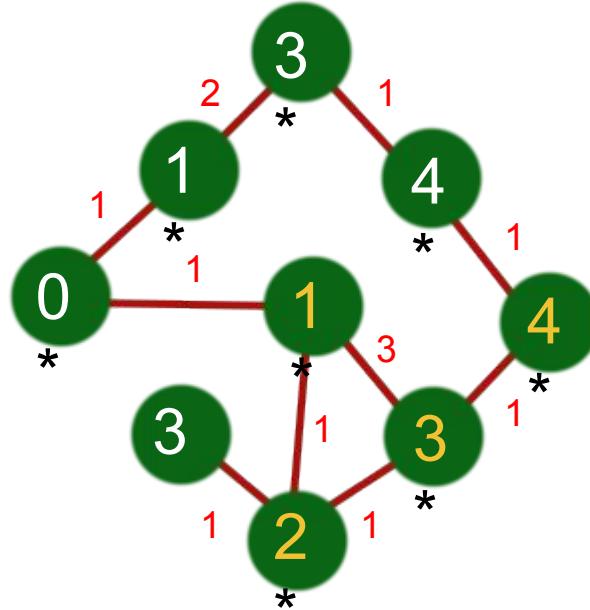
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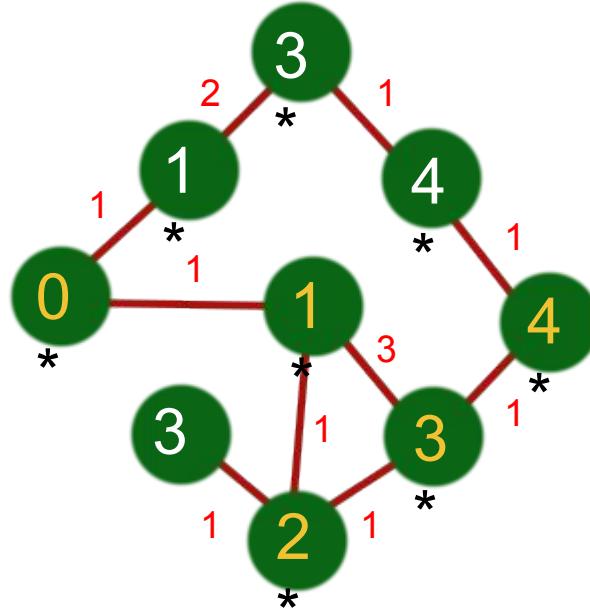
The shortest path can then be found
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Dijkstra's algorithm

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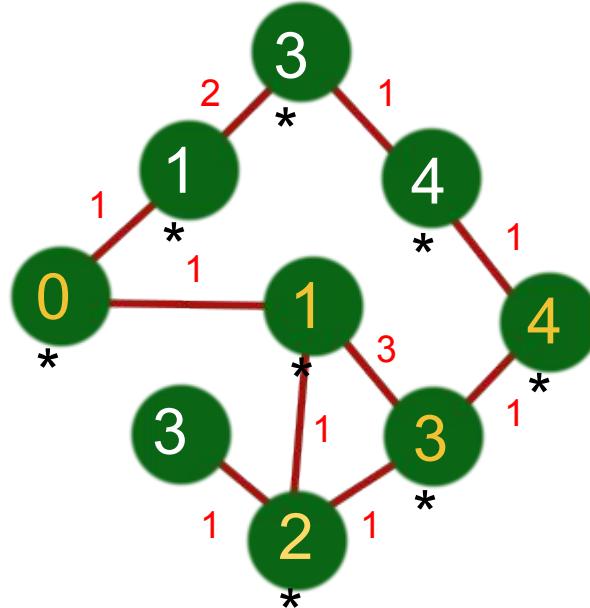


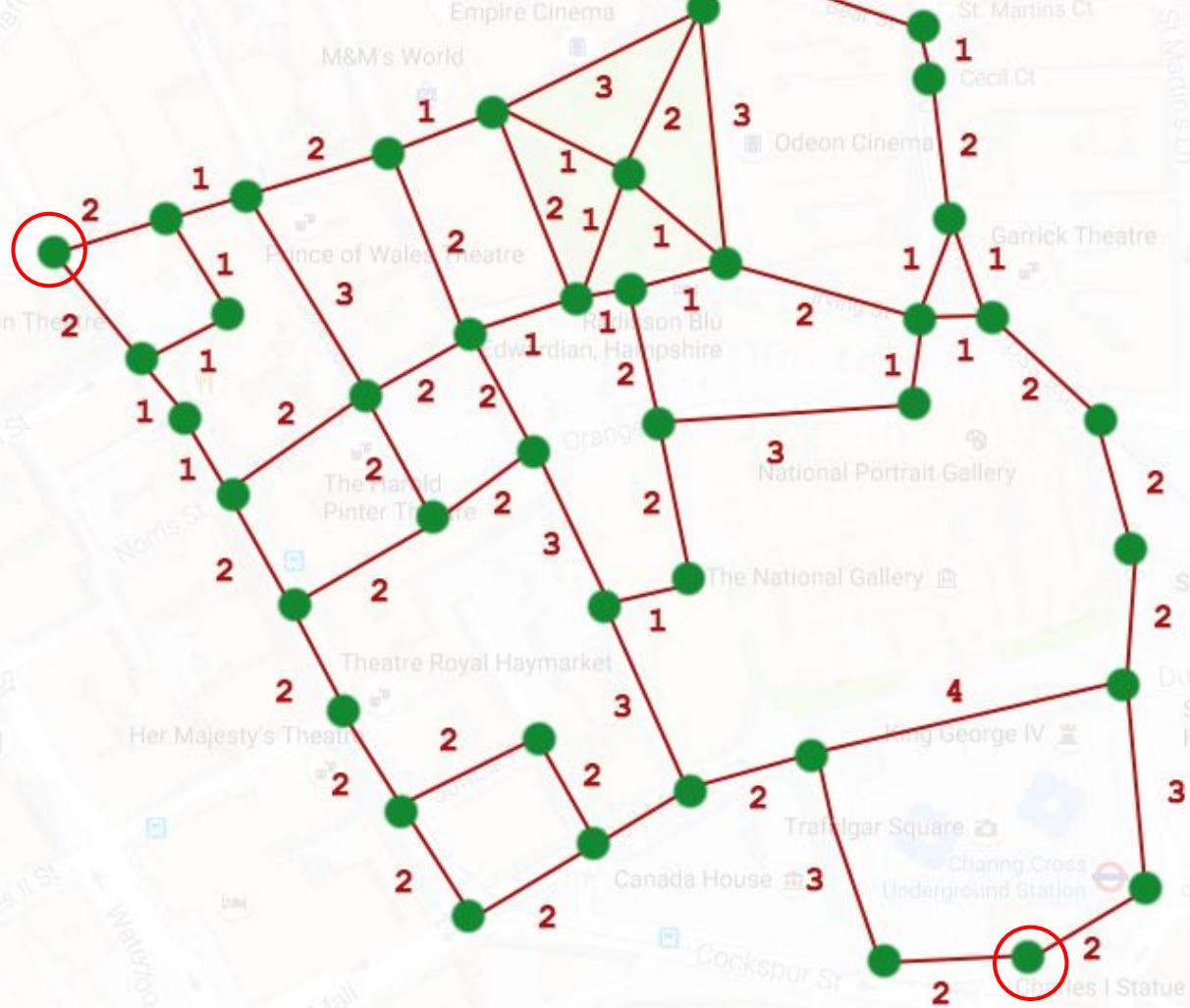
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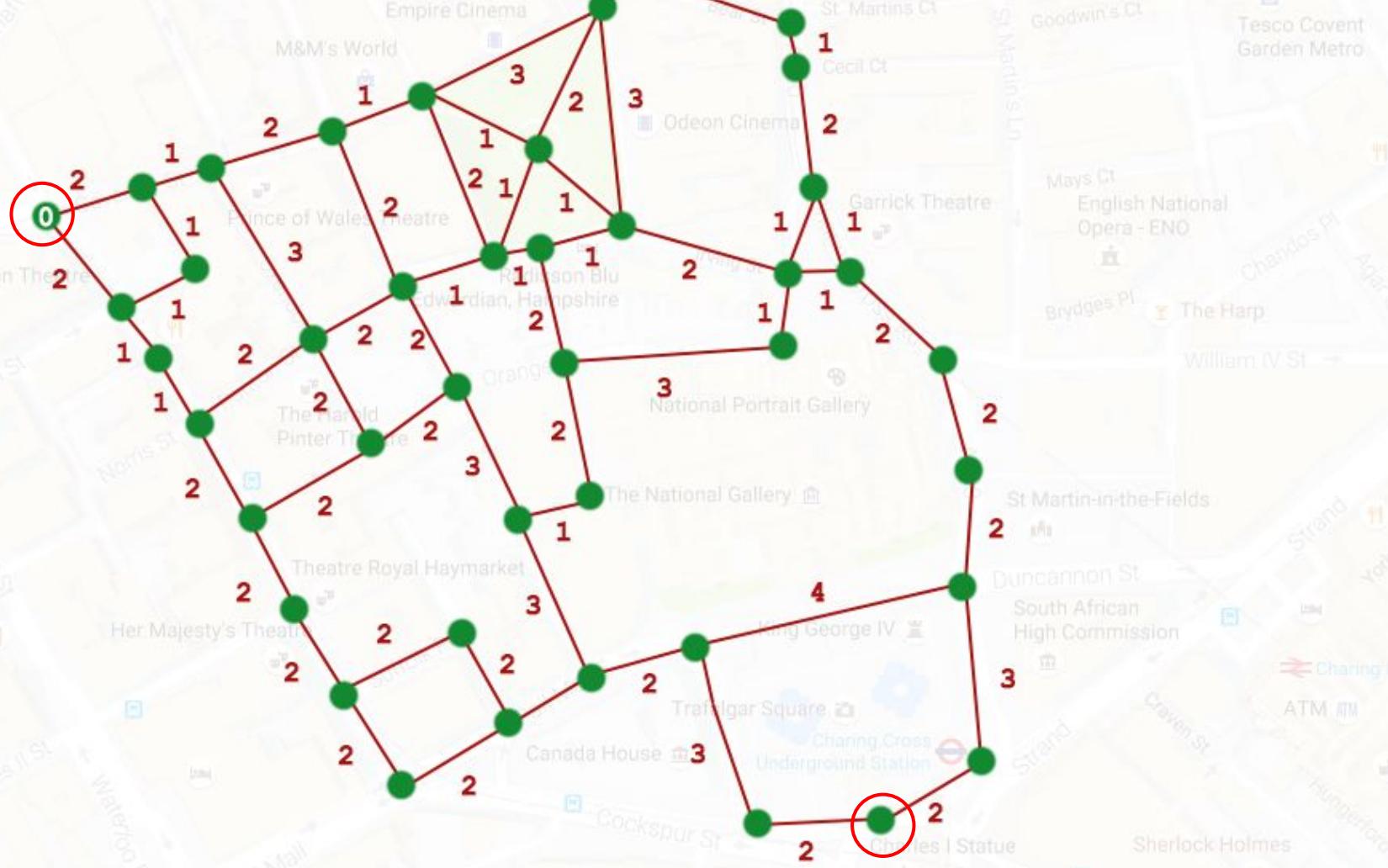
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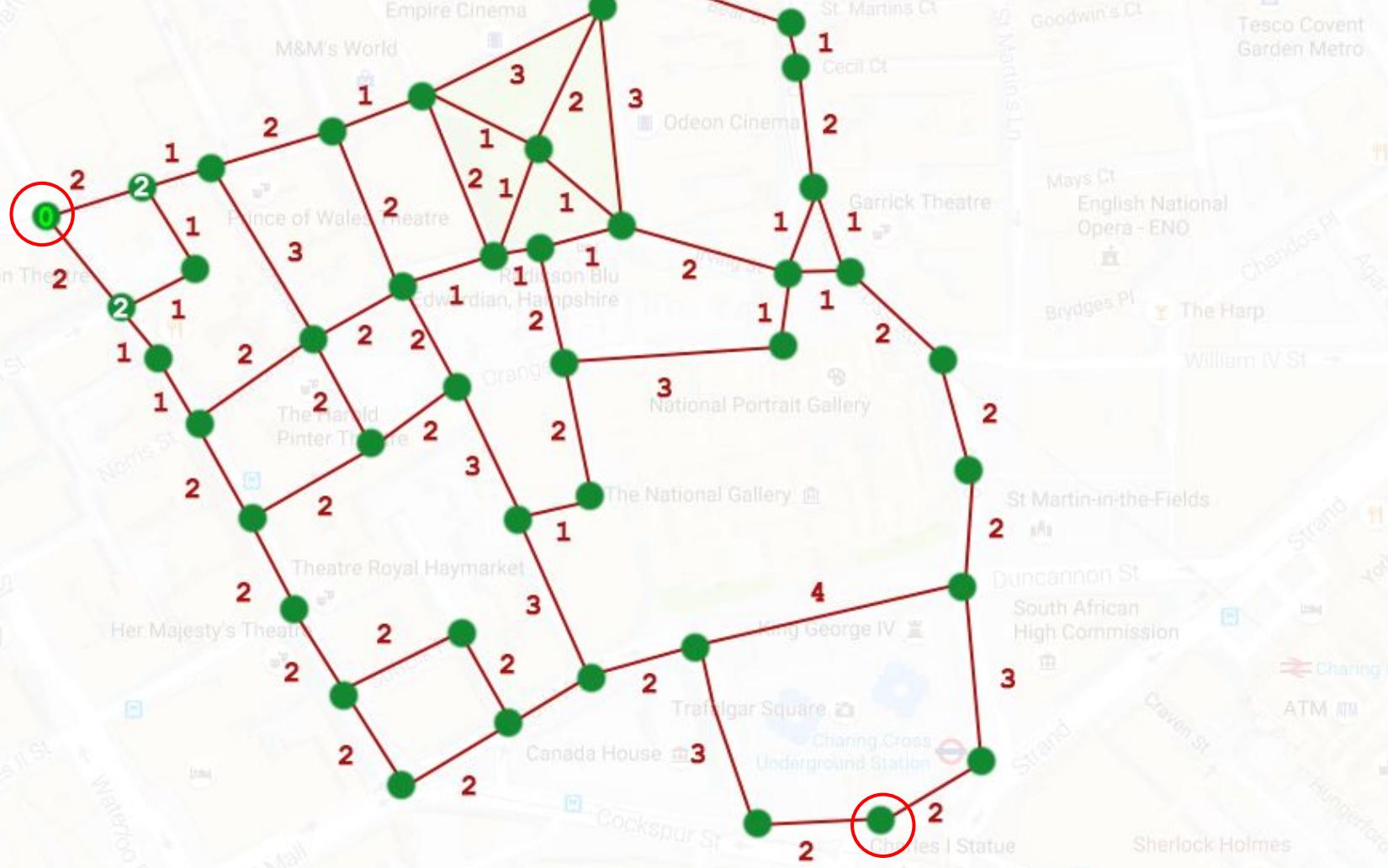
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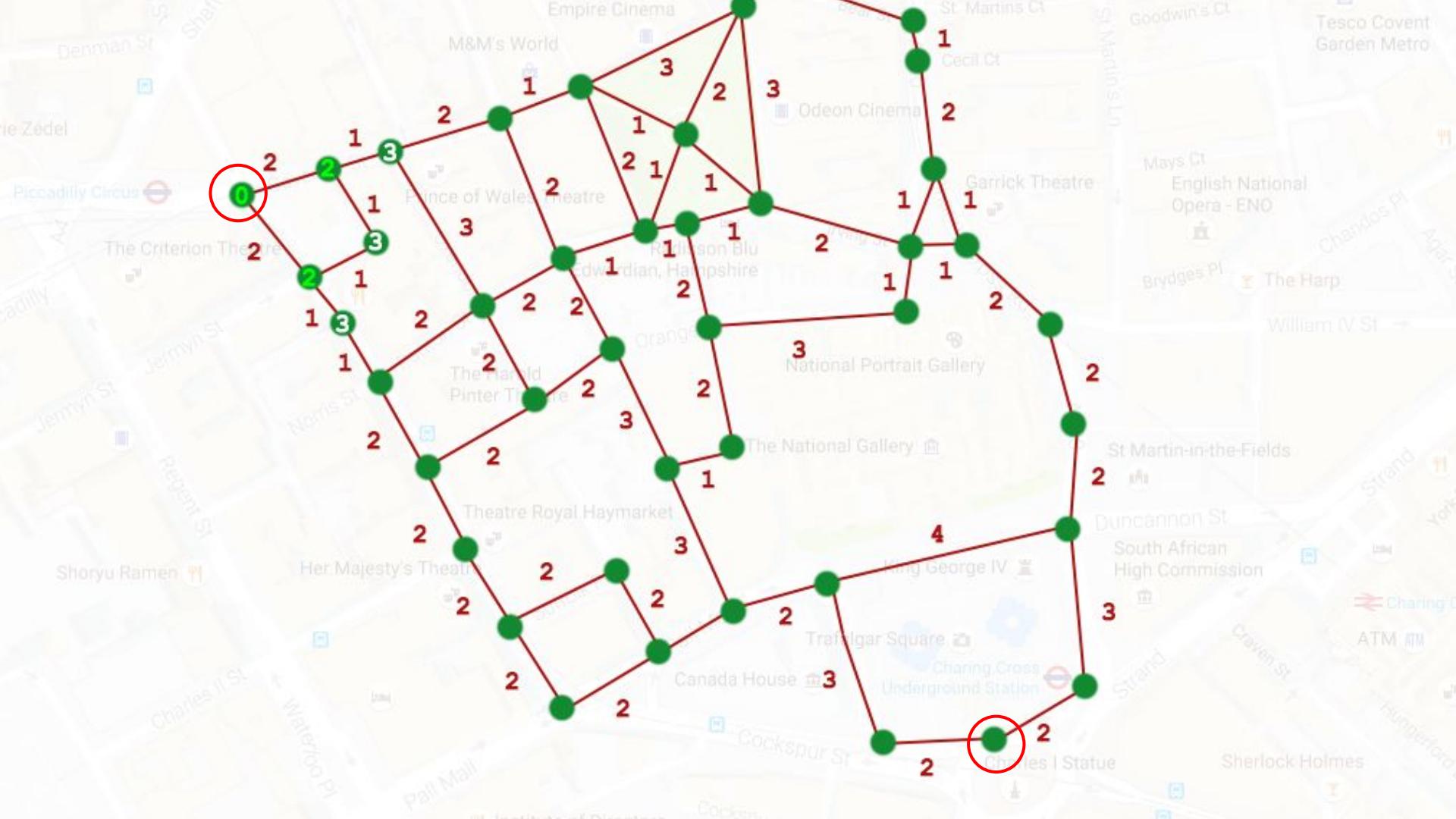
If no nodes with a score are left, and
the end has not been found, then
there is no path.

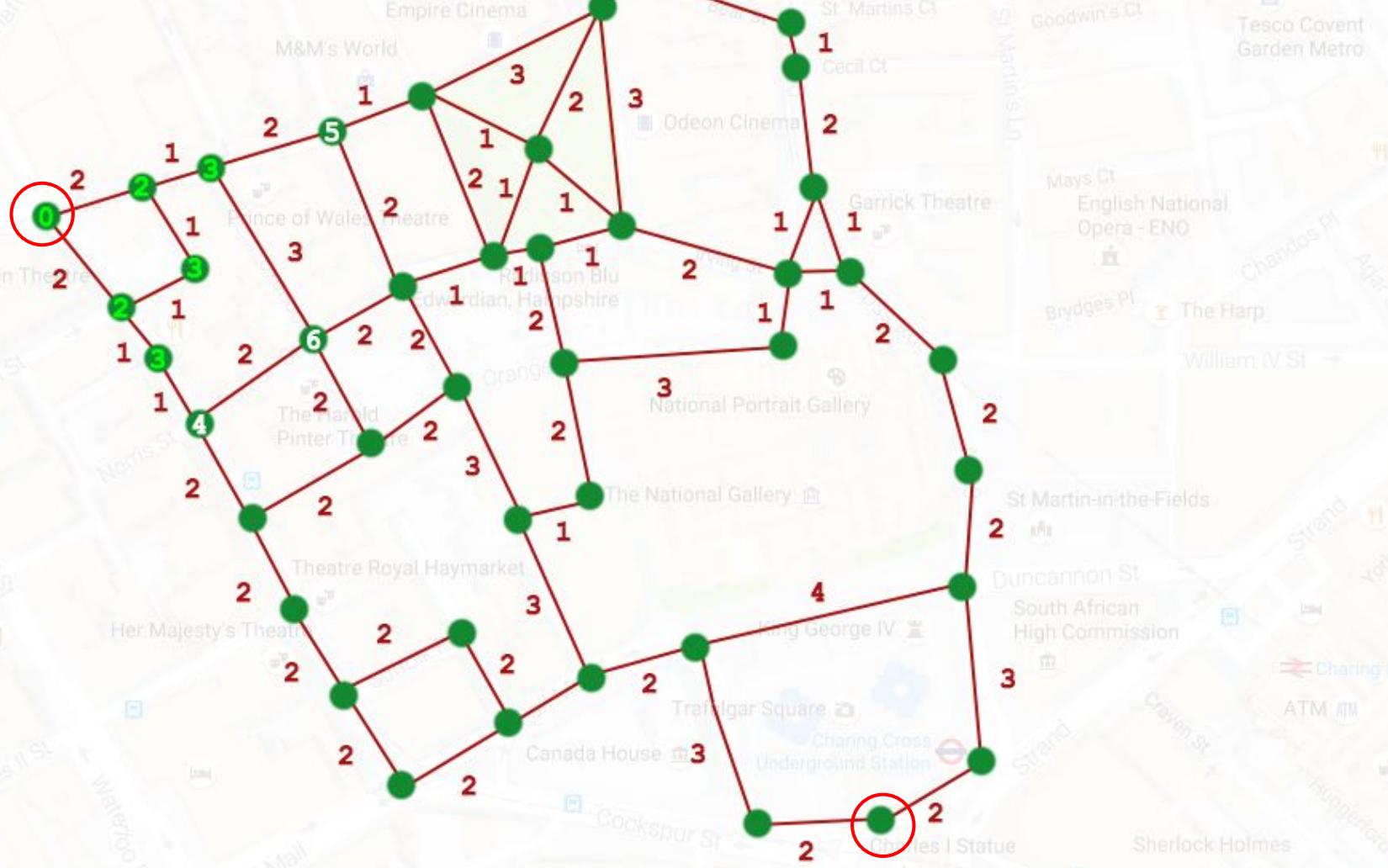


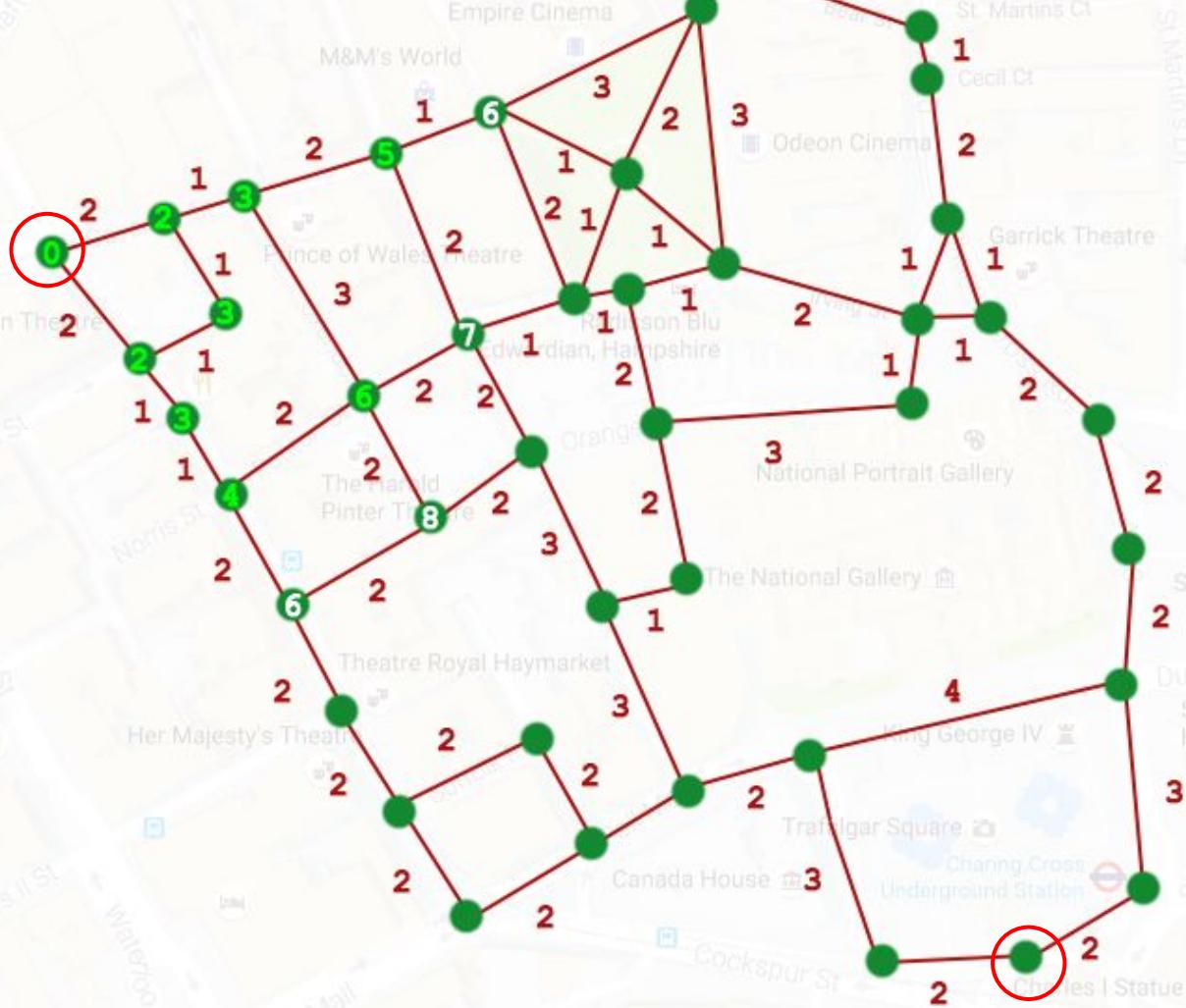


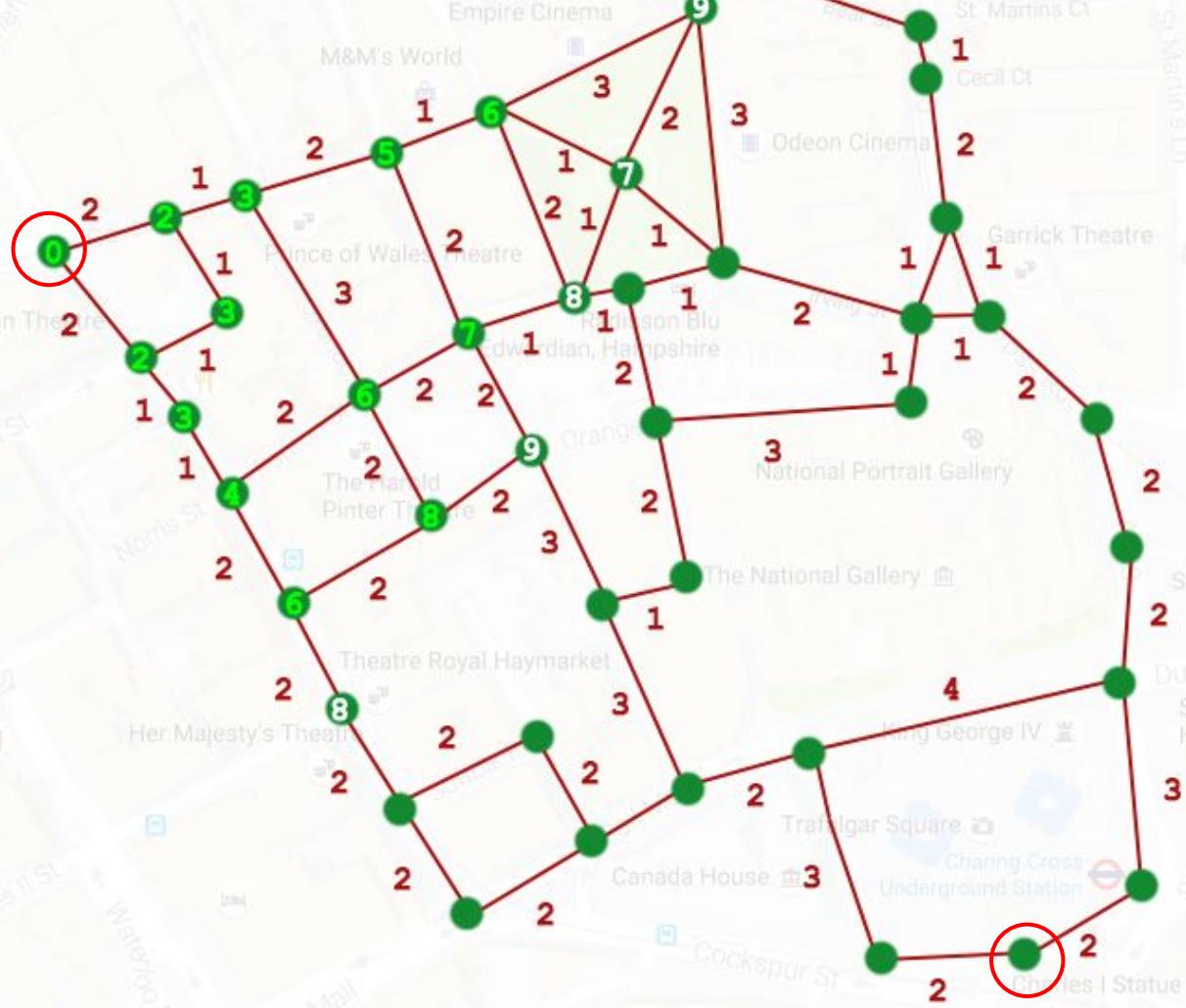


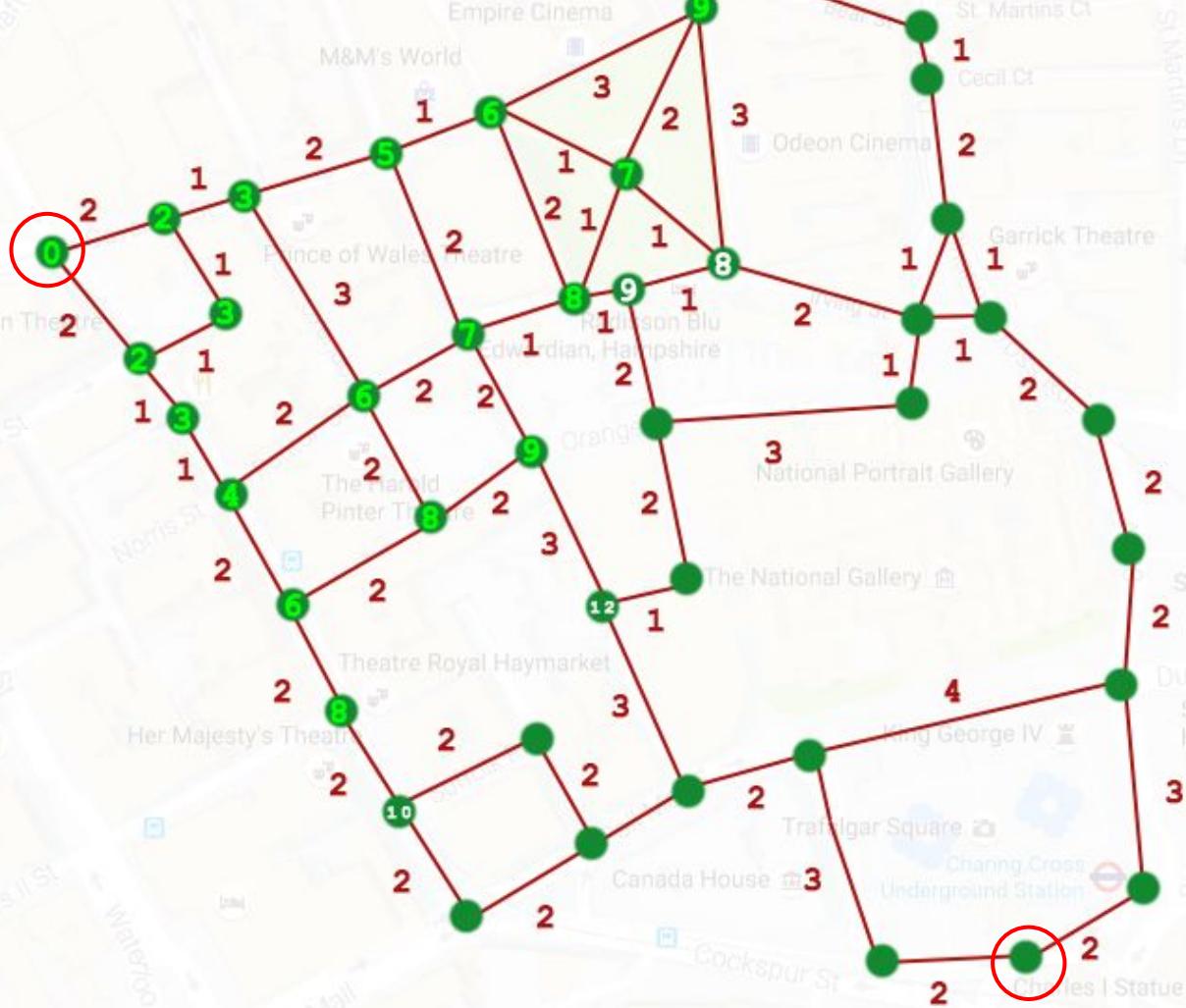


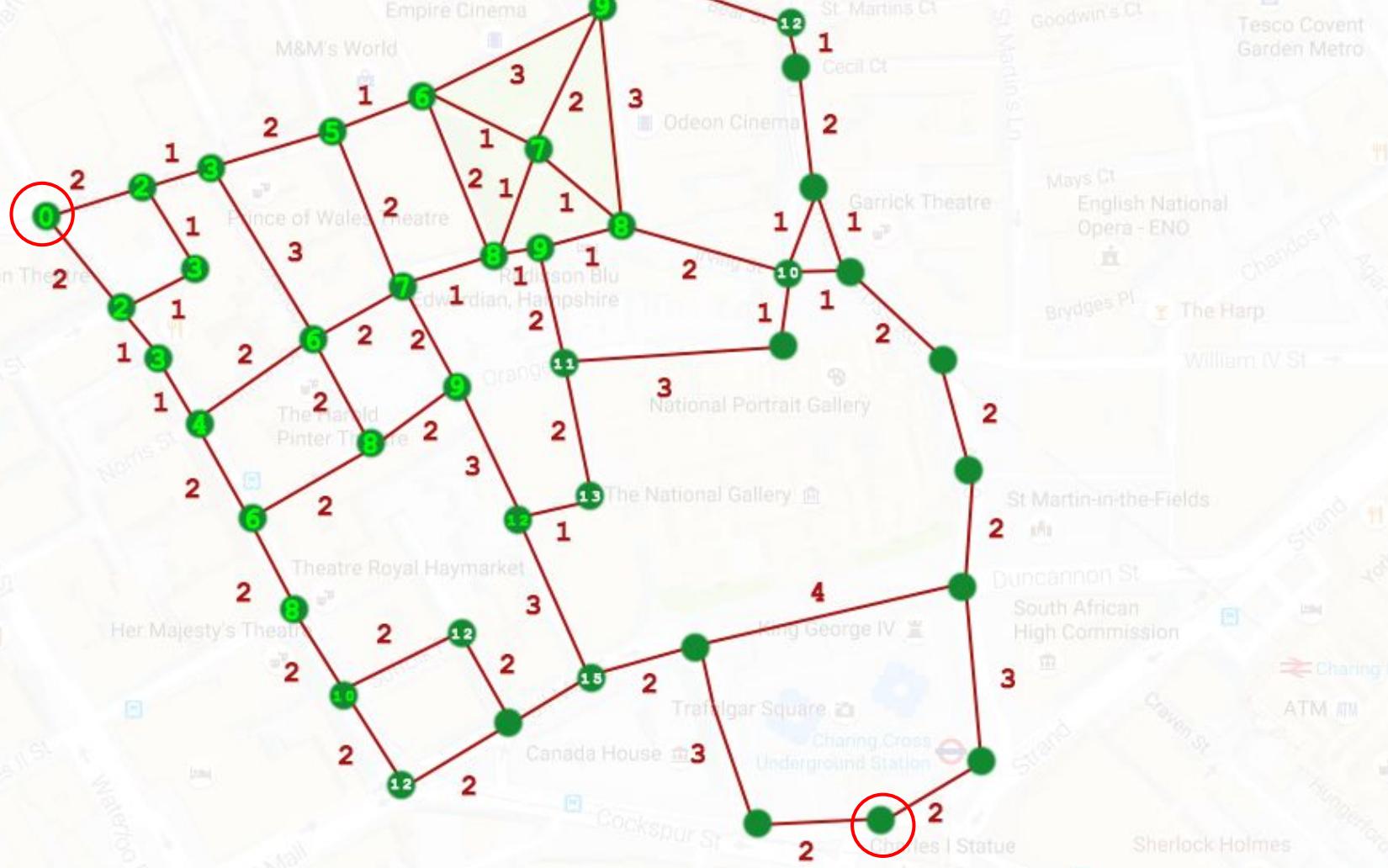


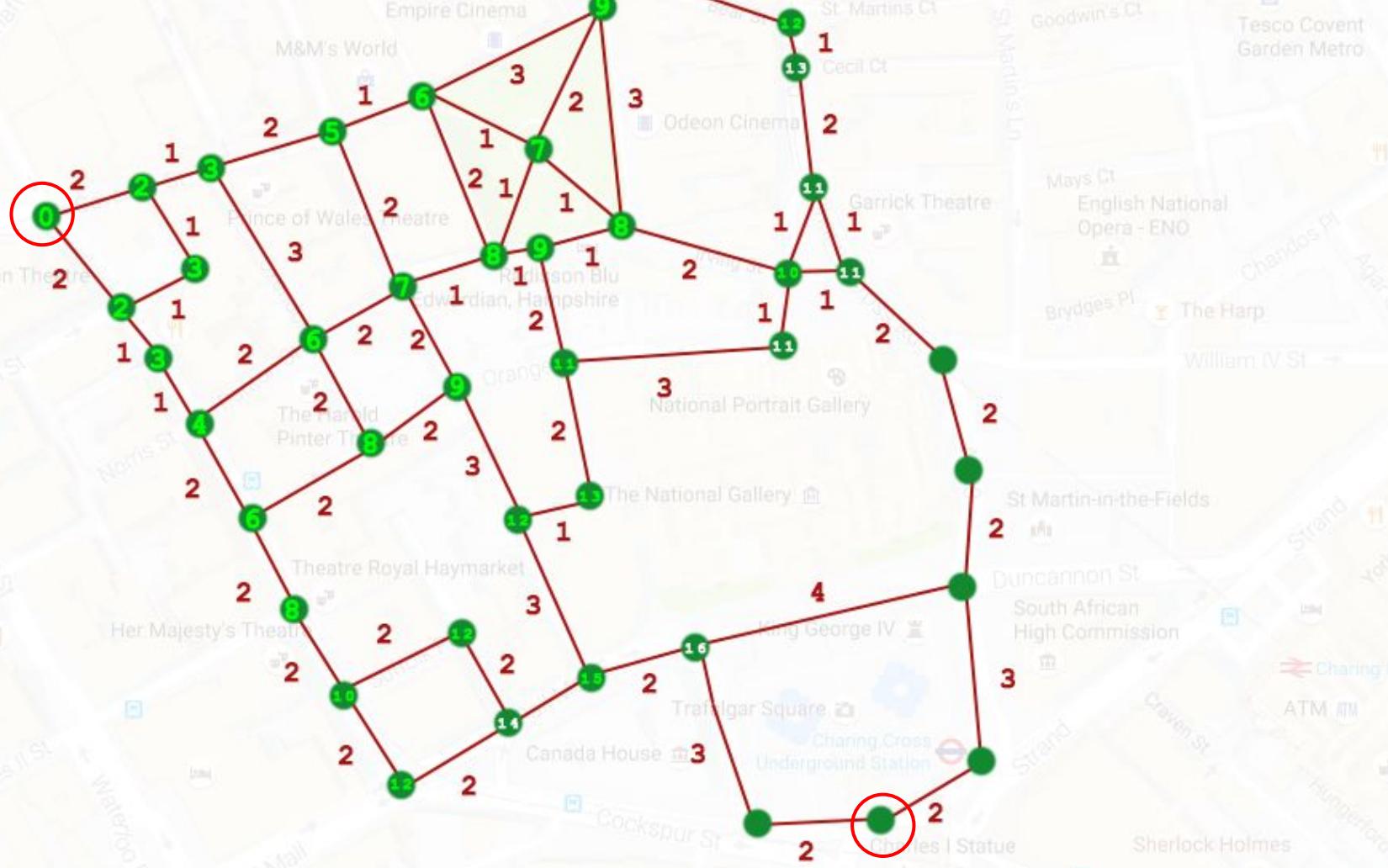


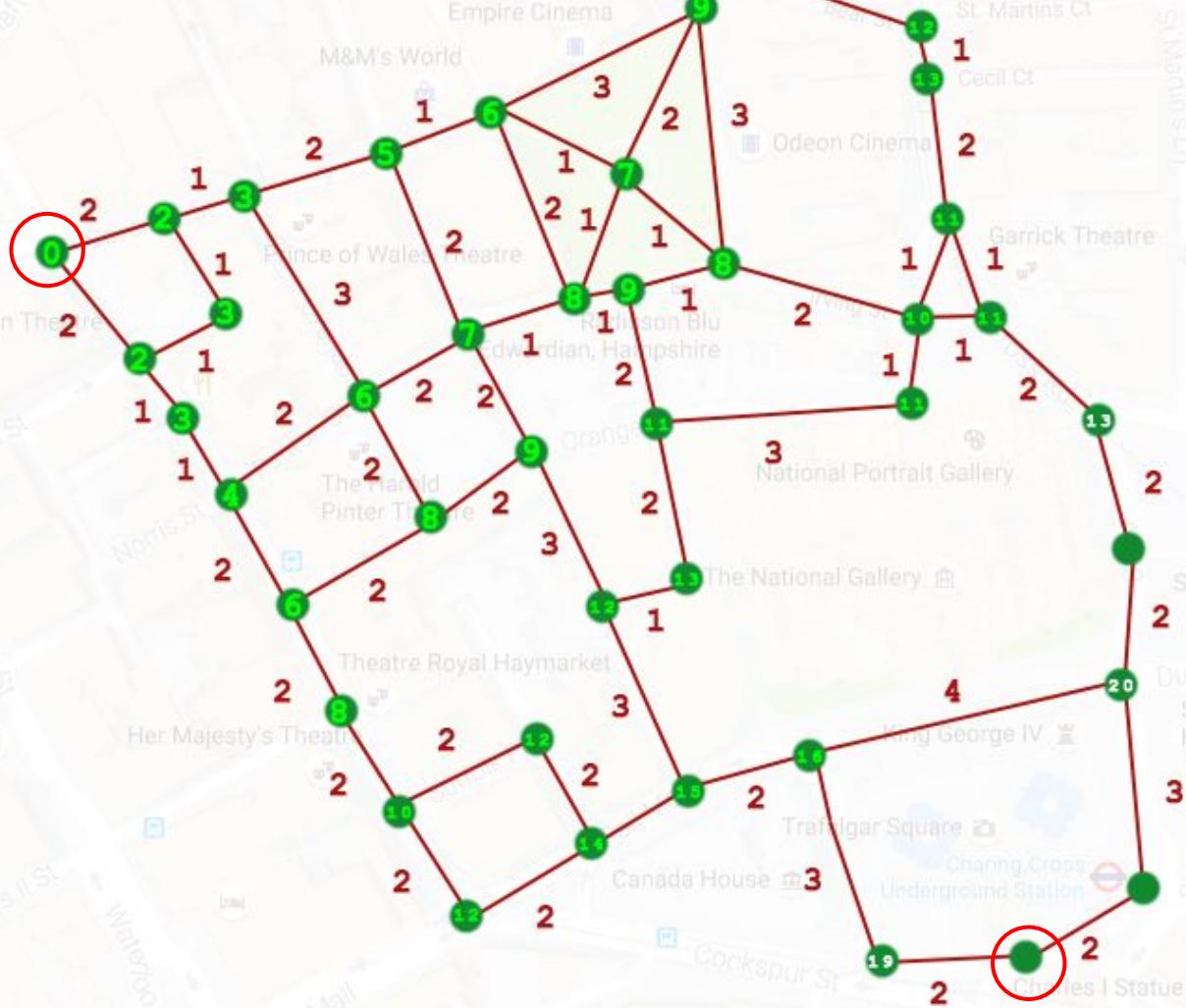


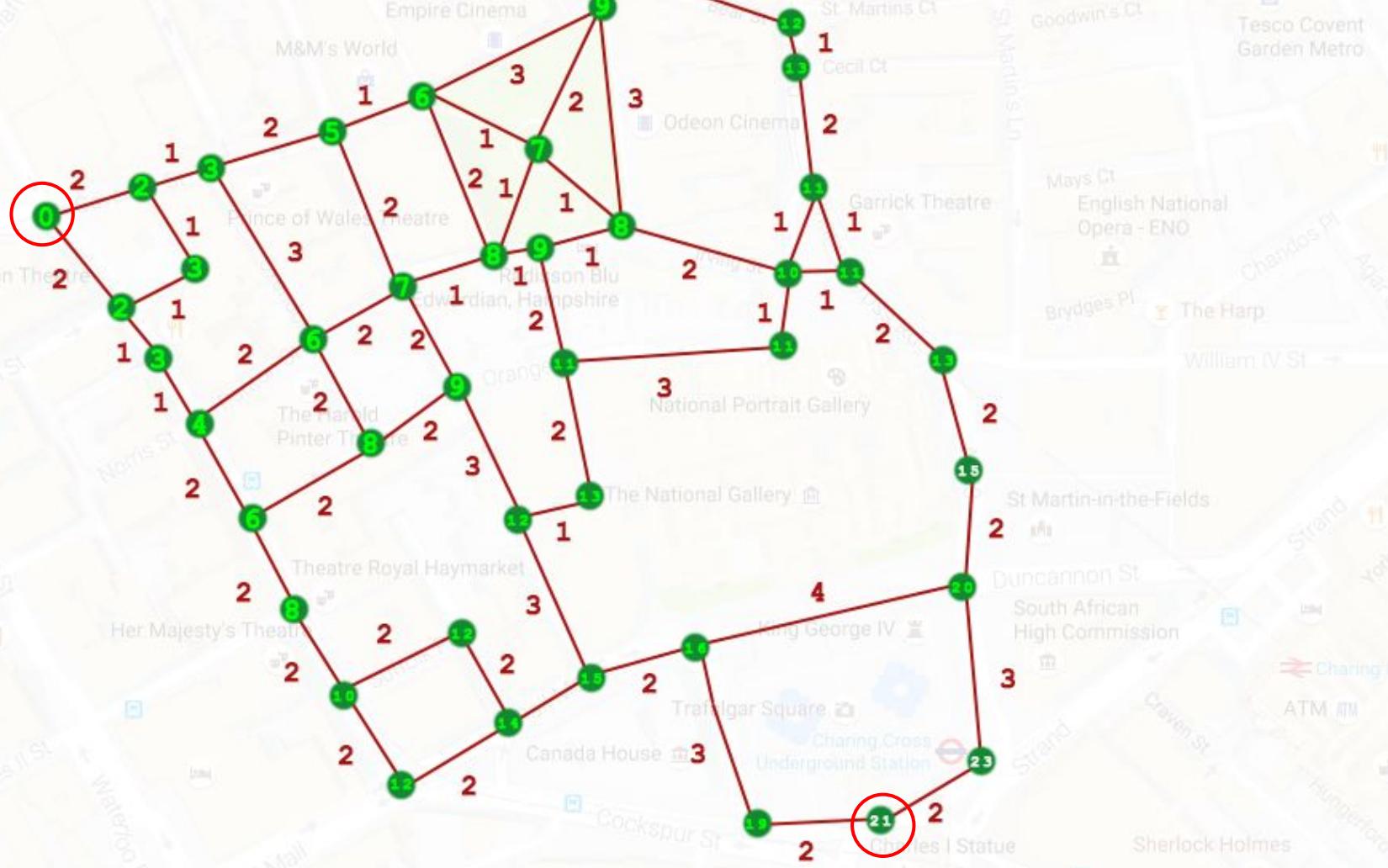


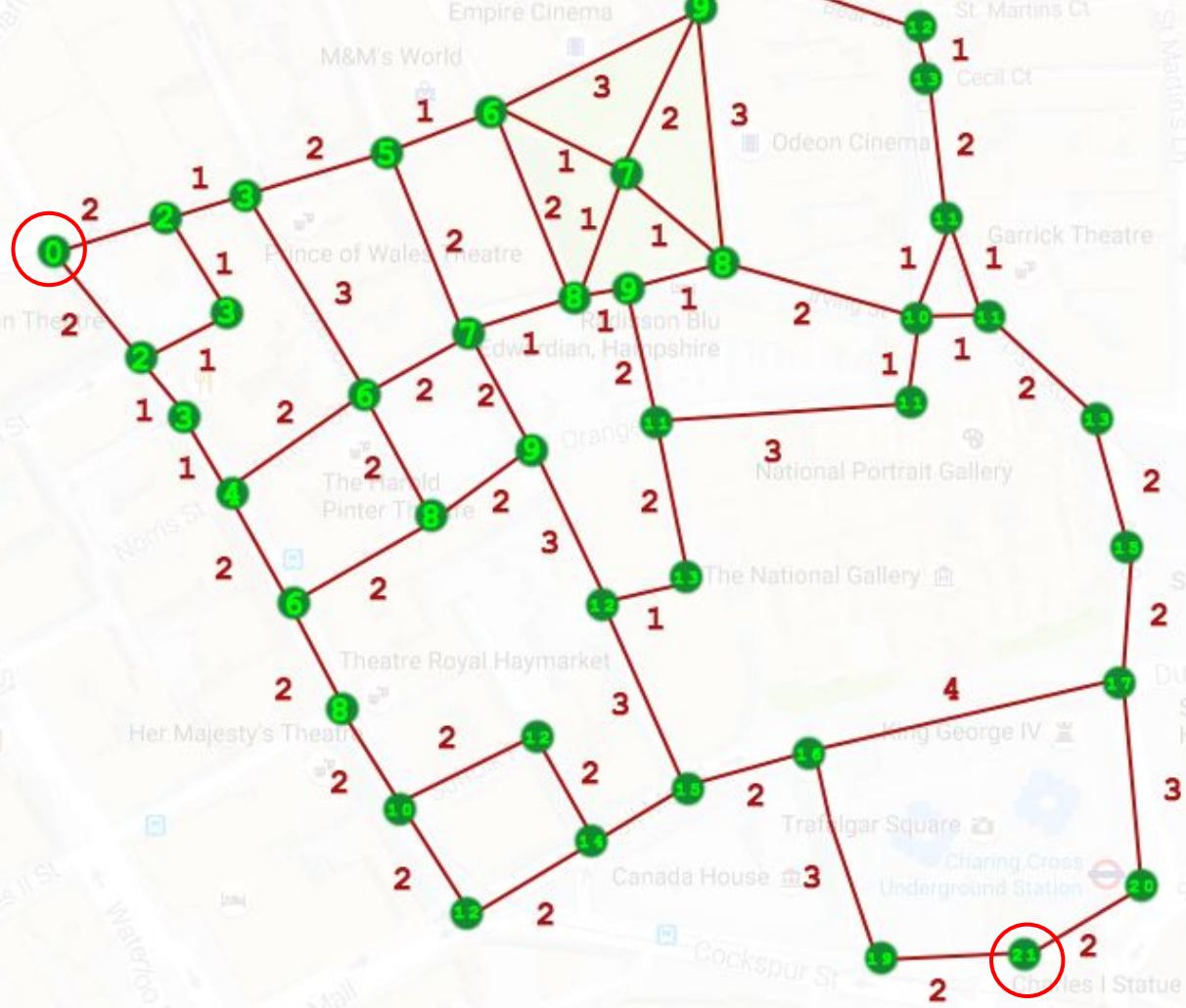


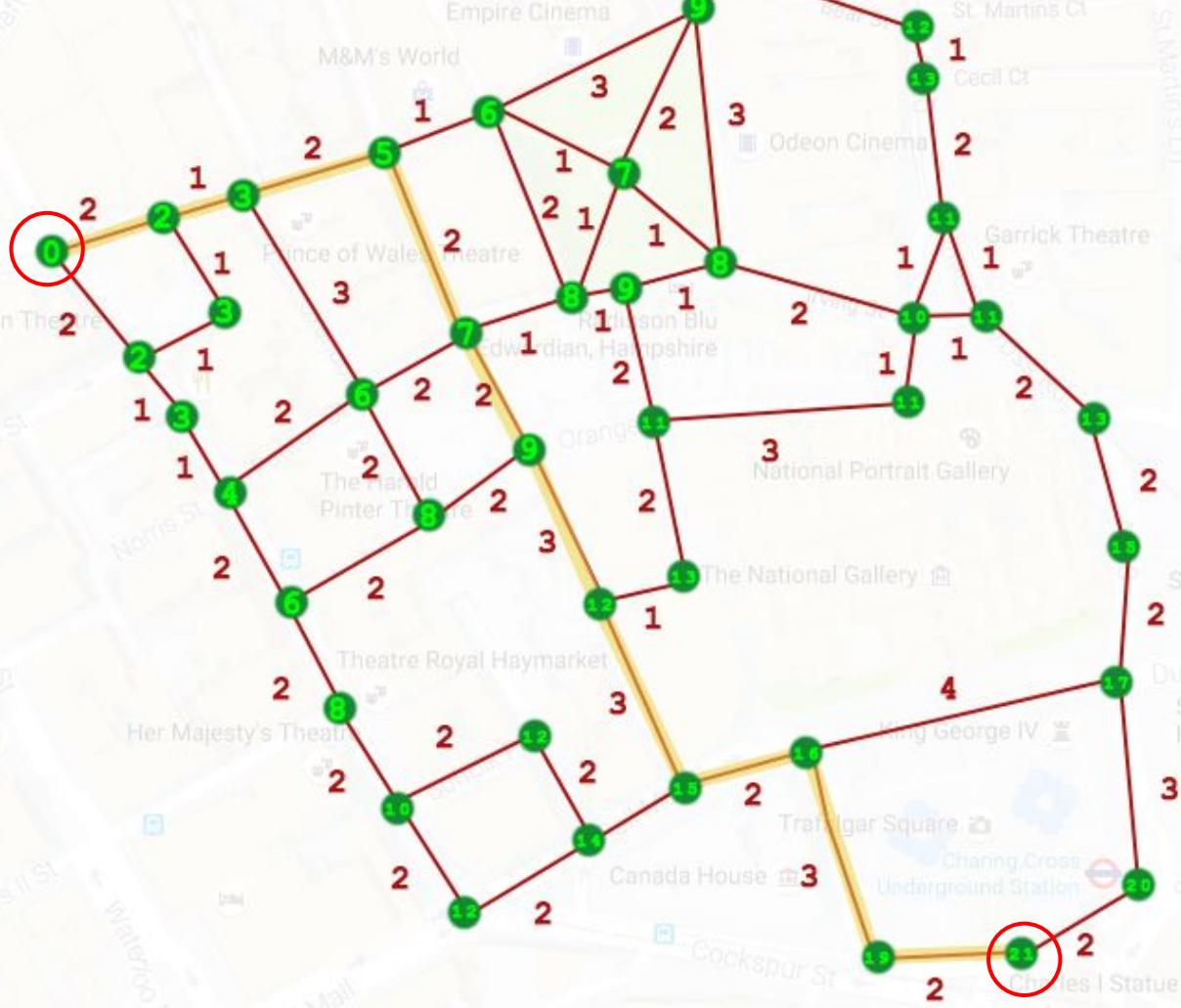












Weighted graphs

Useful for modelling physical systems
and biased networks.



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We could have used a beauty score to
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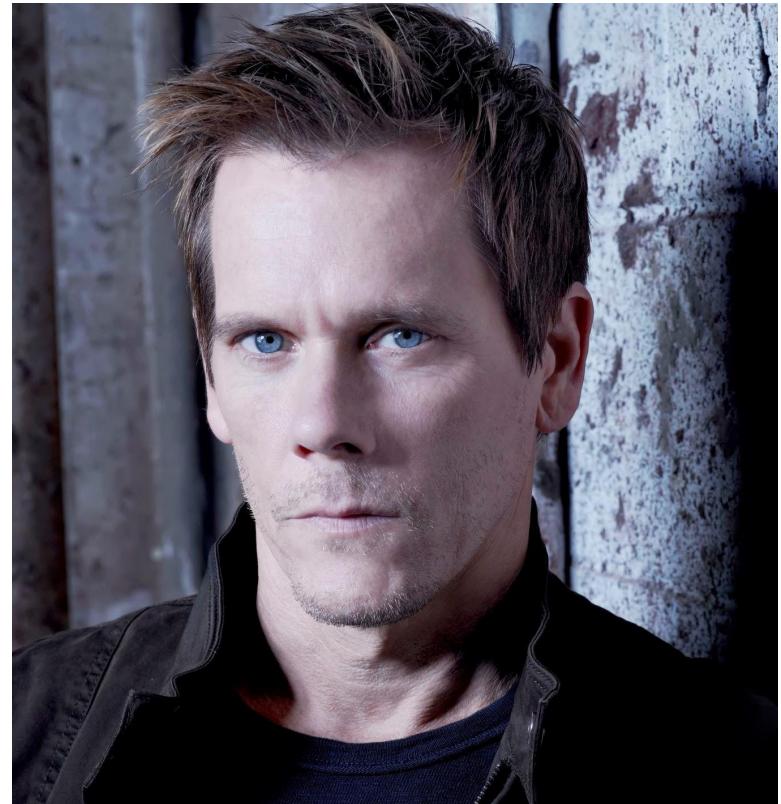
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We could even use IMDB ratings to
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going via the worst movies.



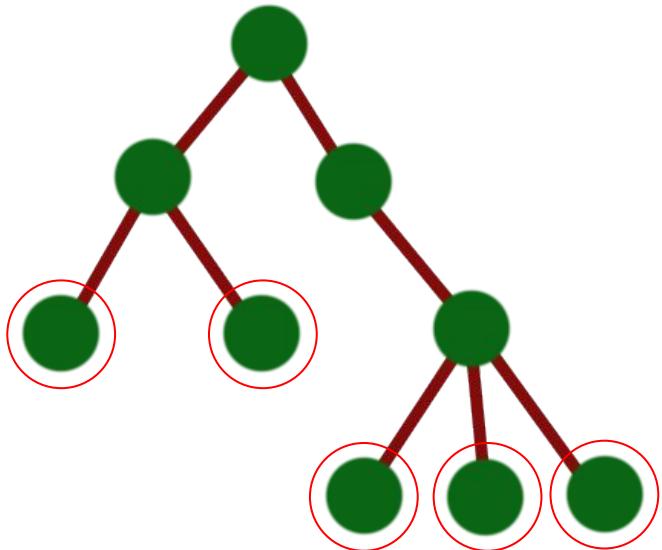
Trees



Trees

A tree is a special kind of graph; it still has nodes and edges.

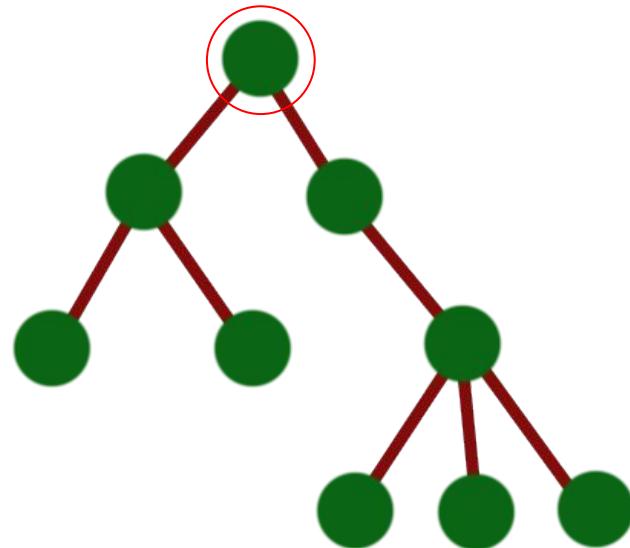
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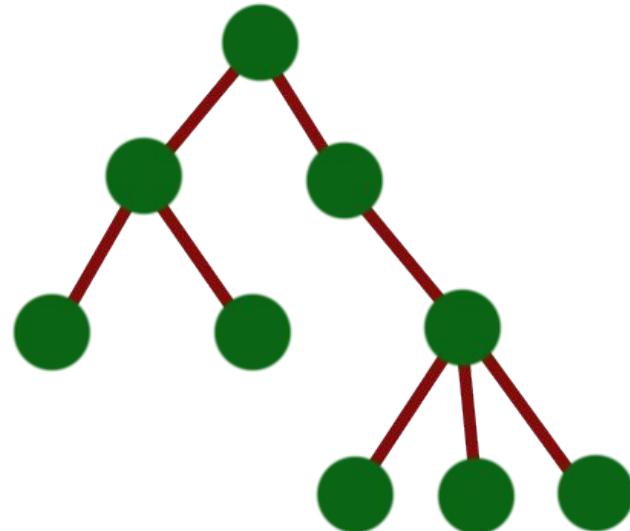


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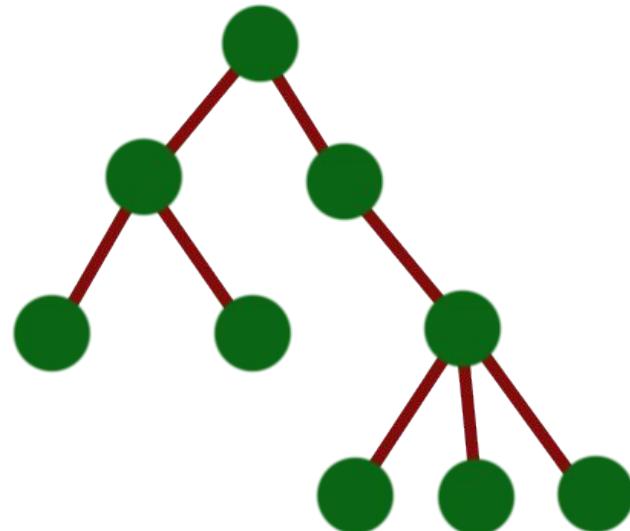
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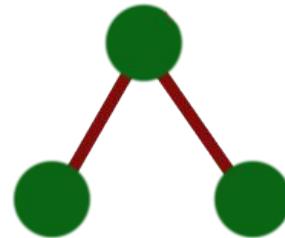
Trees are constructed in such a way that there is only one path between any two nodes.

It is an example of an Acyclic Graph - it has no cycles.



Trees

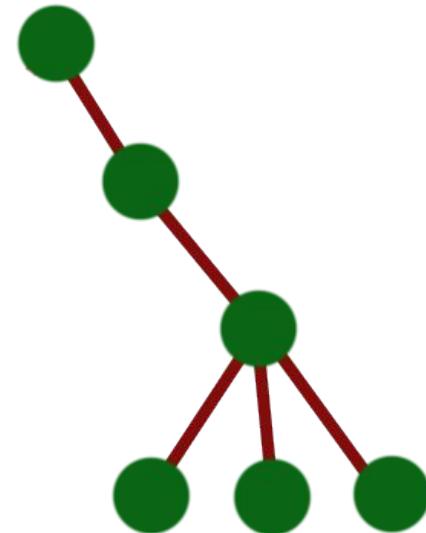
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When you look at smaller pieces, they
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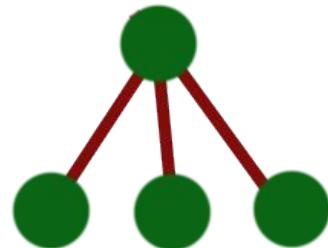


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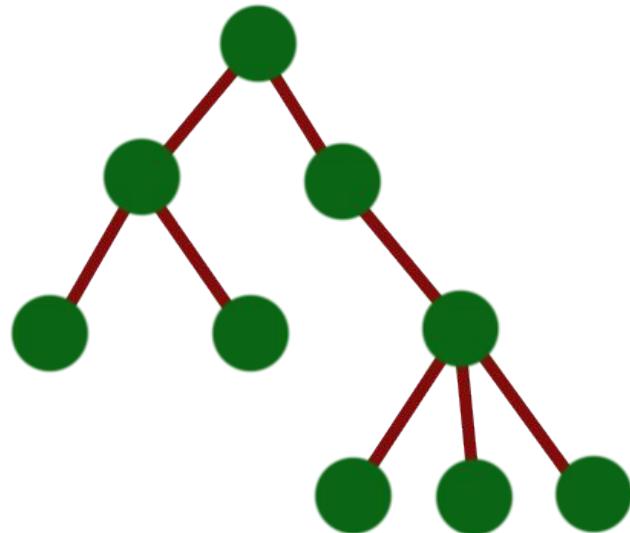
Trees

Much like real trees, they are *self-similar*

When you look at smaller pieces, they look a lot like the bigger piece.

A tree with depth greater than one is a *forest* of other trees.

Therefore any operation you perform on a small tree can be performed on any tree.



Walking trees: Arithmetic





Continuous Memory



HEWLETT-PACKARD

Reverse Polish Notation

The first pocket calculators used RPN to input arithmetic.



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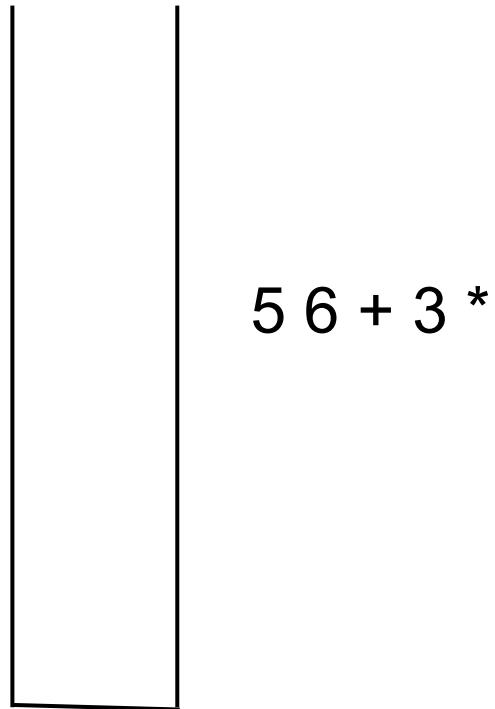
This is somewhat... counter-intuitive.

The reason for this is rooted in how computers process arithmetic.



Reverse Polish Notation

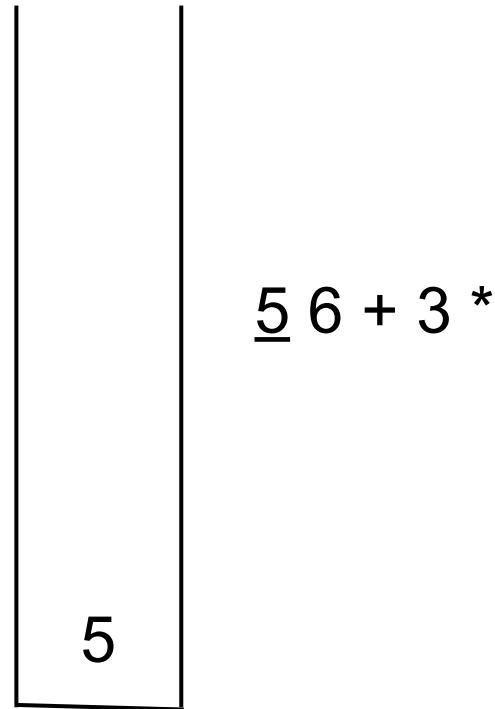
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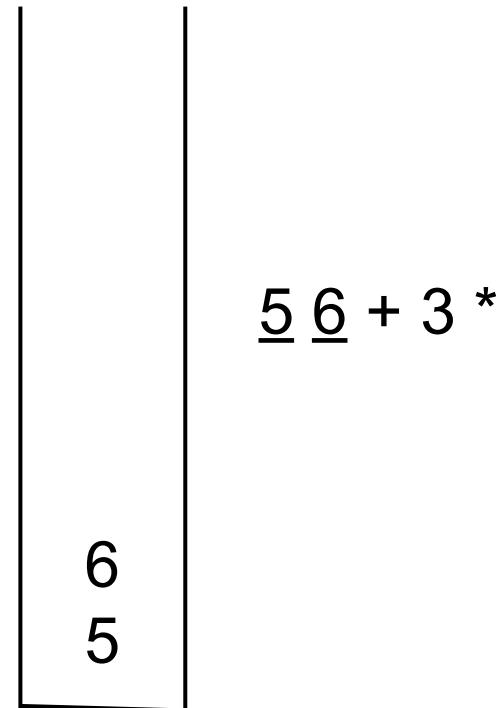
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When you reach an operator, pop the last two items from the stack, perform the operation and return the result to the stack.



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Essentially, stack arithmetic uses a queue and a stack.

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When you reach an operator, pop the last two items from the stack, perform the operation and return the result to the stack.

When your queue is finished, you have your answer!

$$\underline{5} \ \underline{6} \ \underline{+} \ \underline{3} \ \underline{*} = 33$$

Reverse Polish Notation

Another property of RPN is there is no need for operator precedence.

3 5 7 + * 23 / 7 +

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But: RPN is pretty illegible!

3 5 7 + * 23 / 7 + = ?!

Reverse Polish Notation

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But: RPN is pretty illegible!

How can we transpose it to “natural”?

(Not that it's much better in this example!)

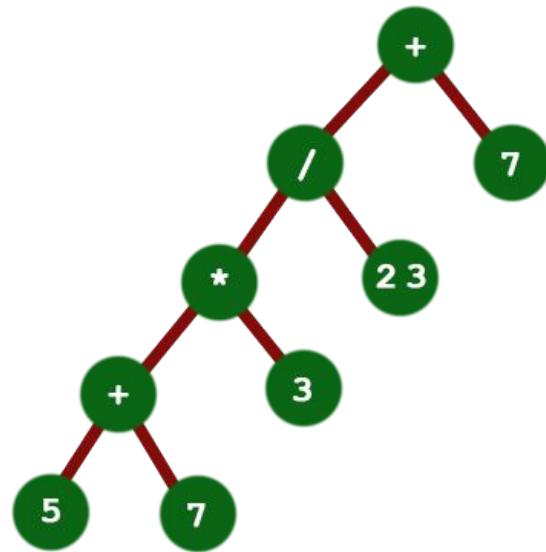
$$3 \ 5 \ 7 \ + \ * \ 23 \ / \ 7 \ + \ = \ ?!$$

$$(((5 + 7) * 3) / 23) + 7 = ?$$

Reverse Polish Notation

Answer: TREES!

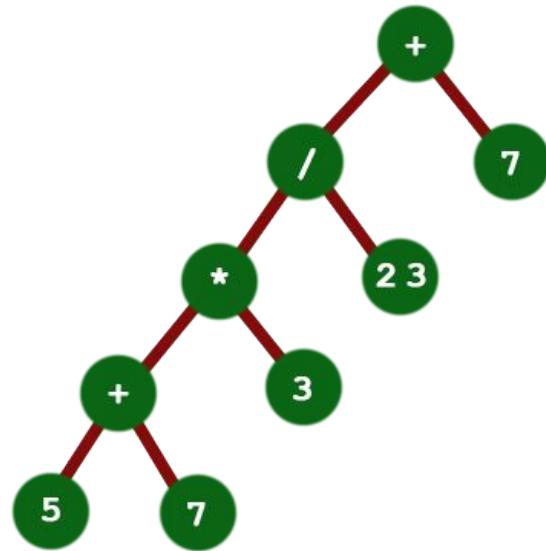
(Bet you didn't see that coming!)



Reverse Polish Notation

Answer: TREES!

Operators become nodes; operands become leaves.

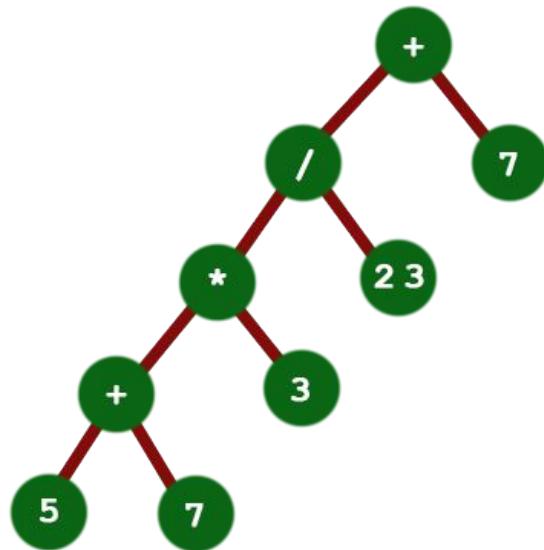


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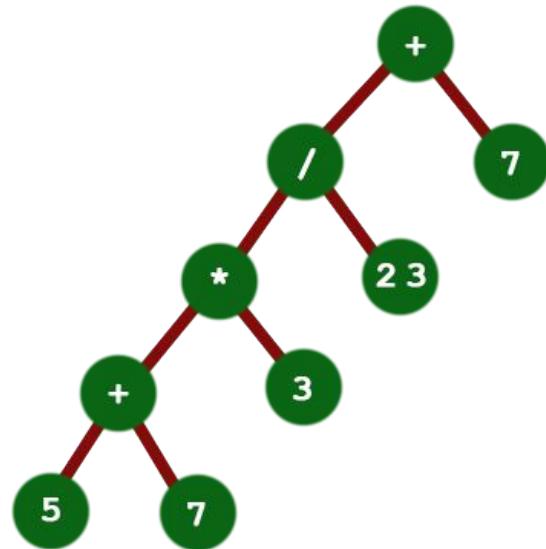
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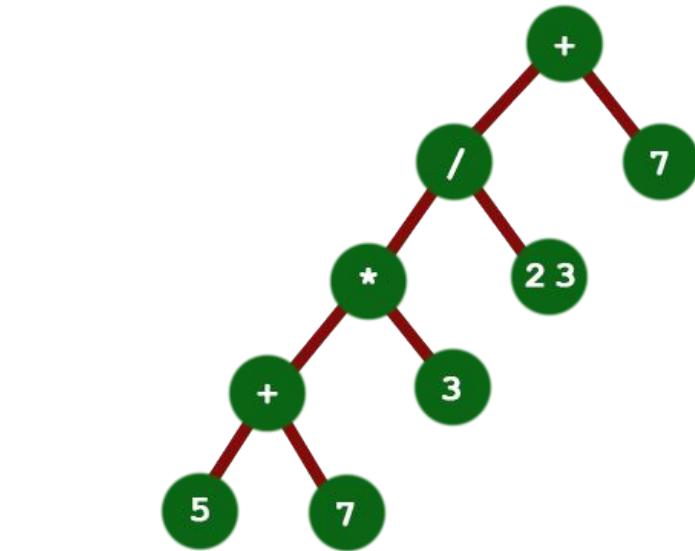
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+

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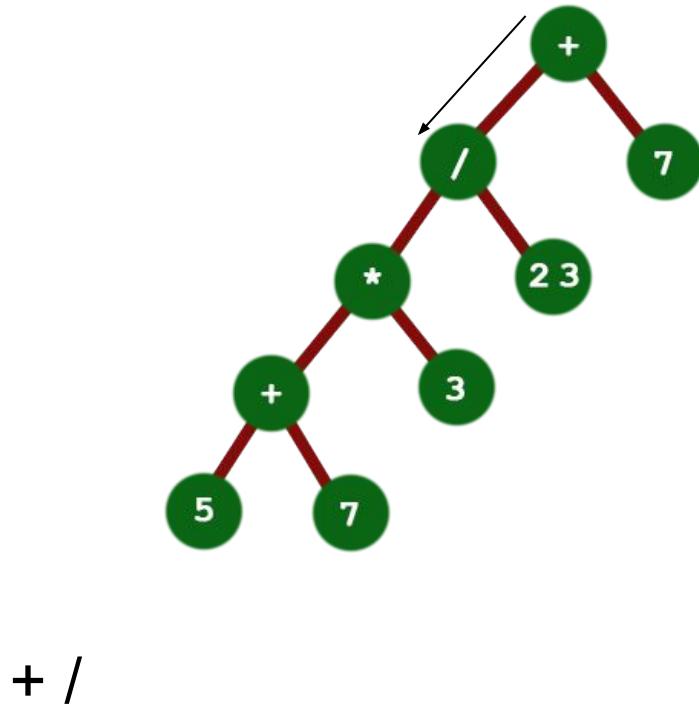
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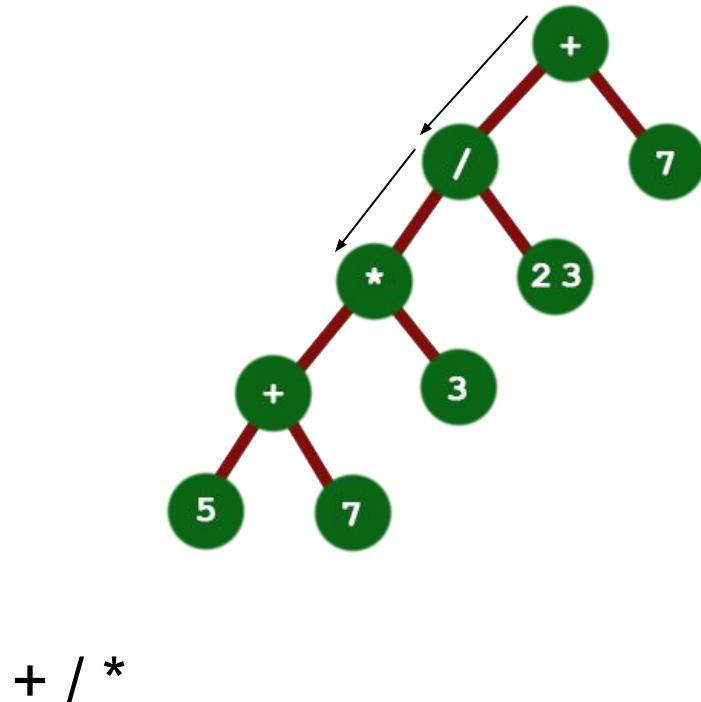
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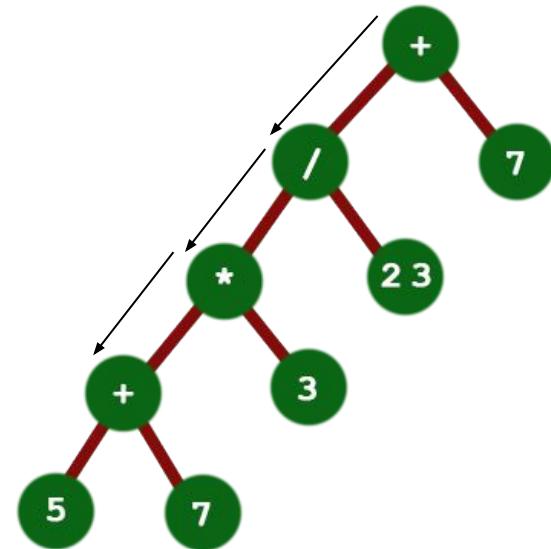
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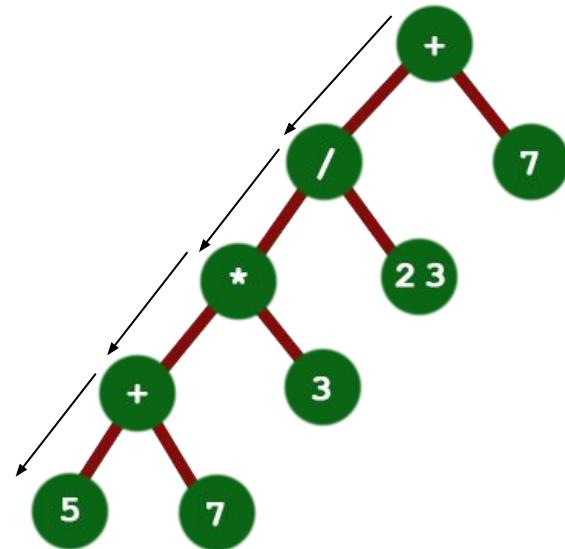
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+ / * + 5

Reverse Polish Notation

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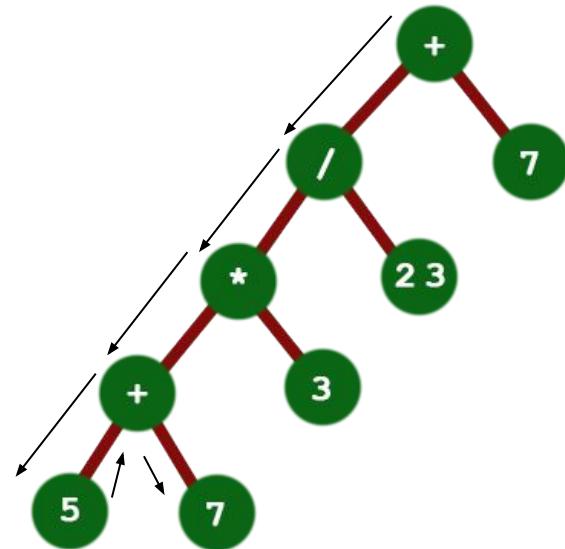
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+ / * + 5 7

Reverse Polish Notation

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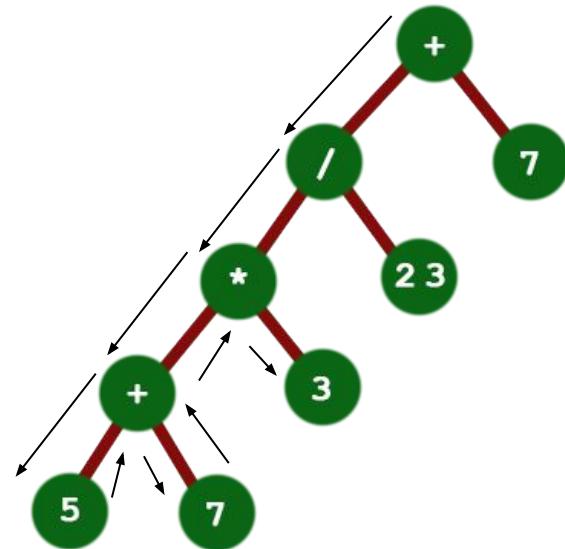
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+ / * + 5 7 3

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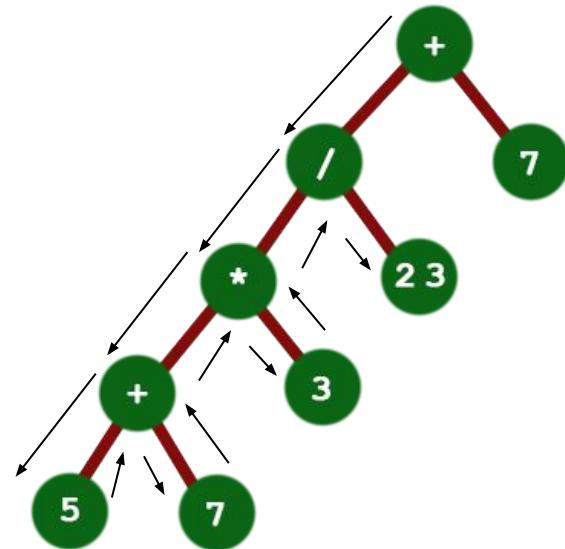
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+ / * + 5 7 3 23

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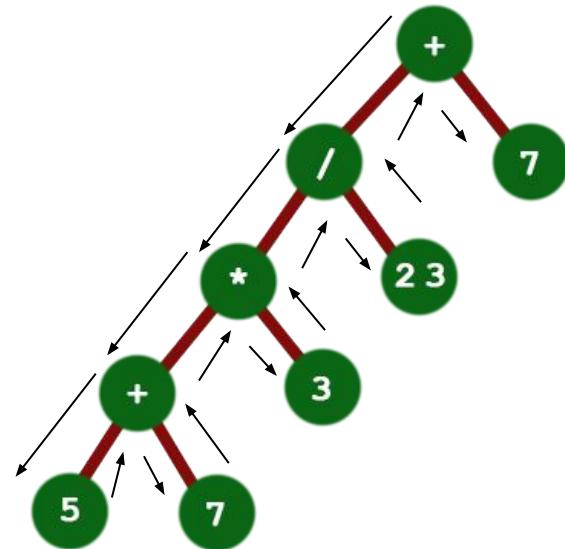
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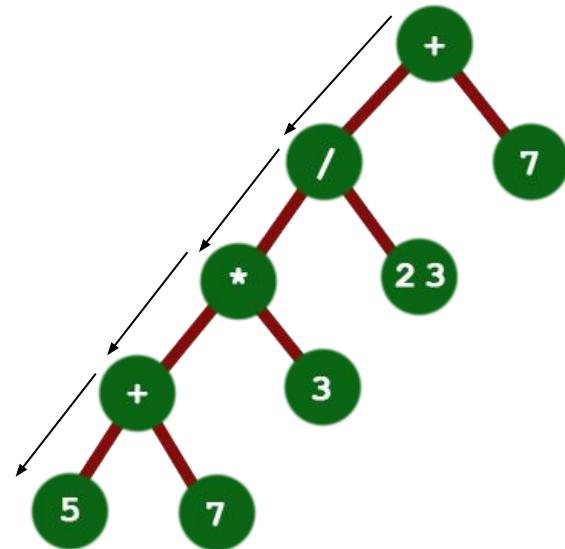
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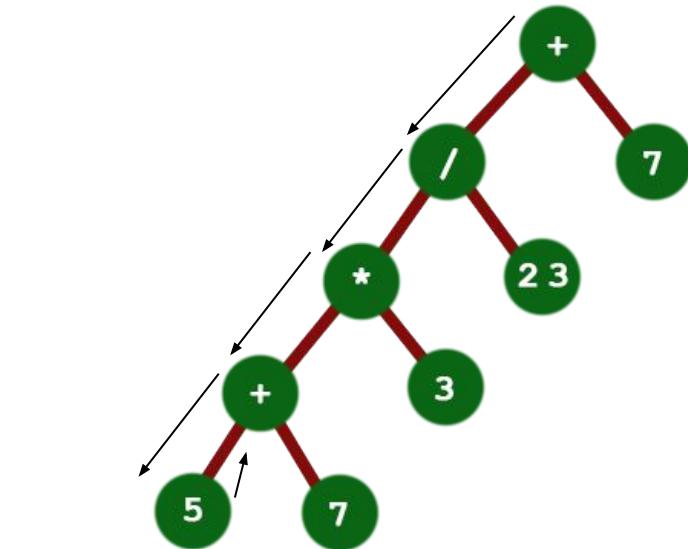
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5 +

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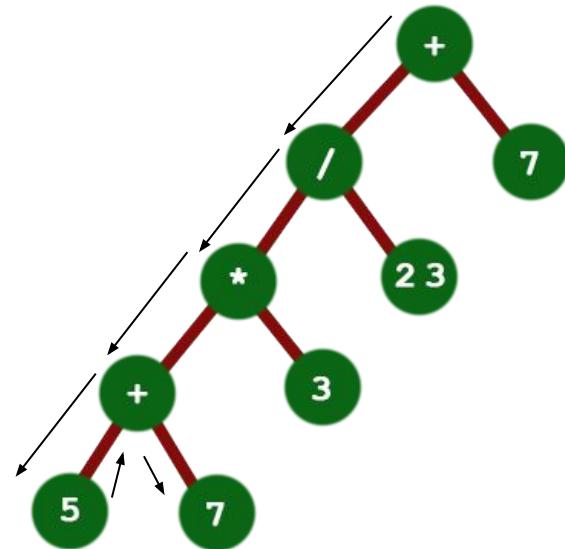
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$$5 + 7$$

Reverse Polish Notation

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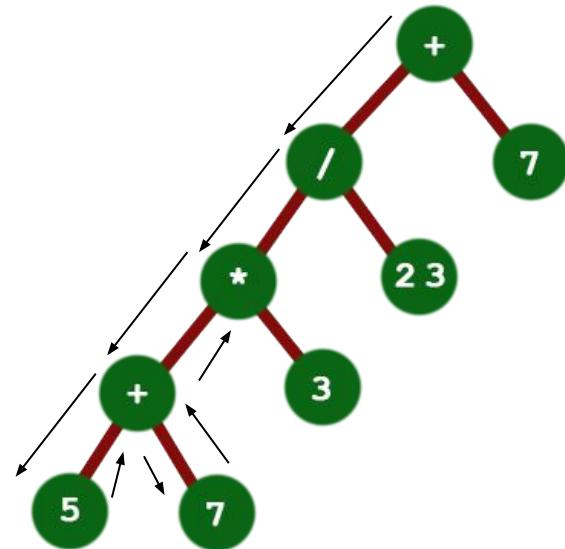
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$5 + 7 *$

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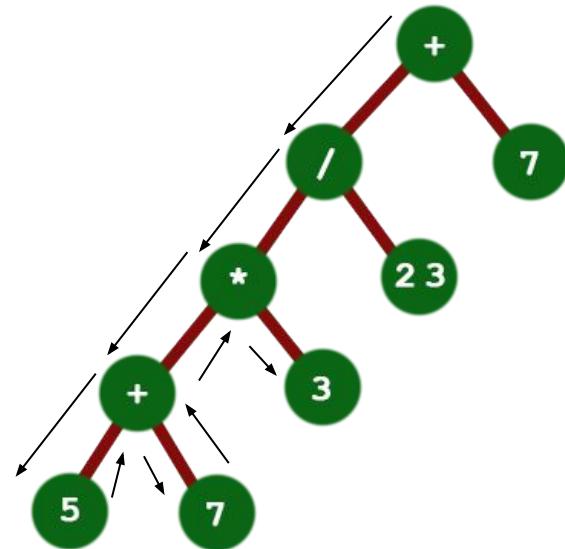
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$$5 + 7 * 3$$

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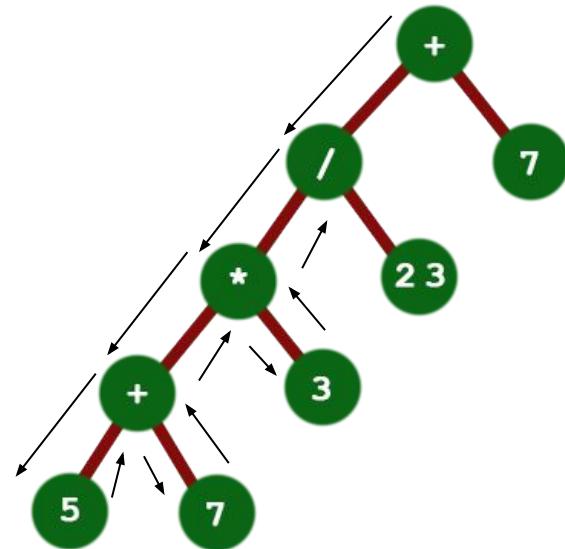
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$$5 + 7 * 3 /$$

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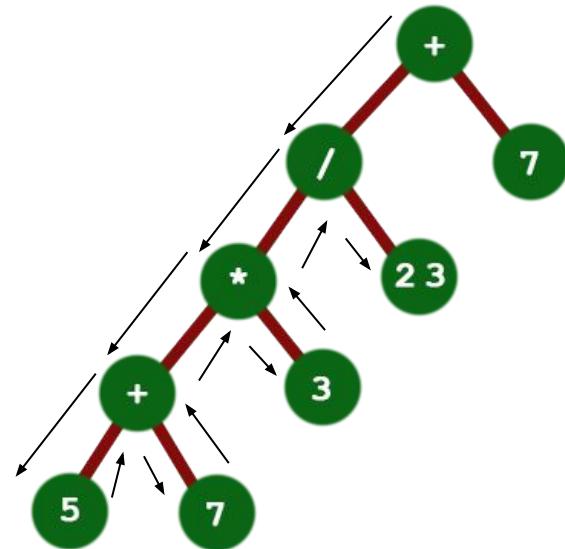
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$$5 + 7 * 3 / 23$$

Reverse Polish Notation

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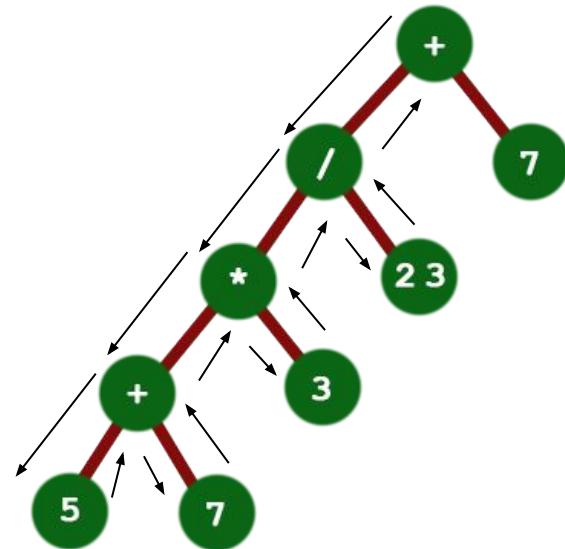
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$5 + 7 * 3 / 23 +$

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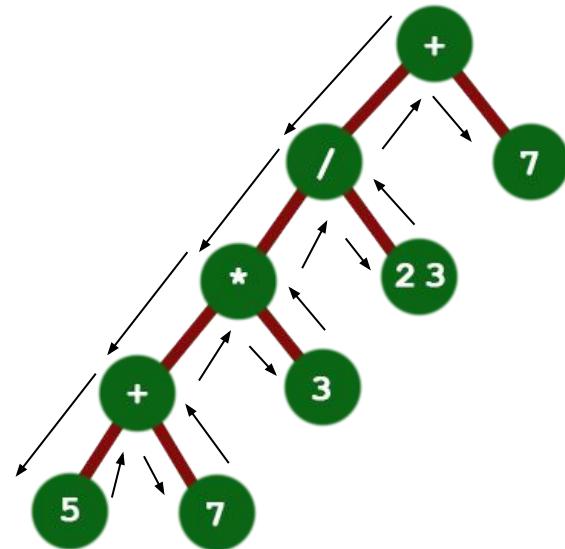
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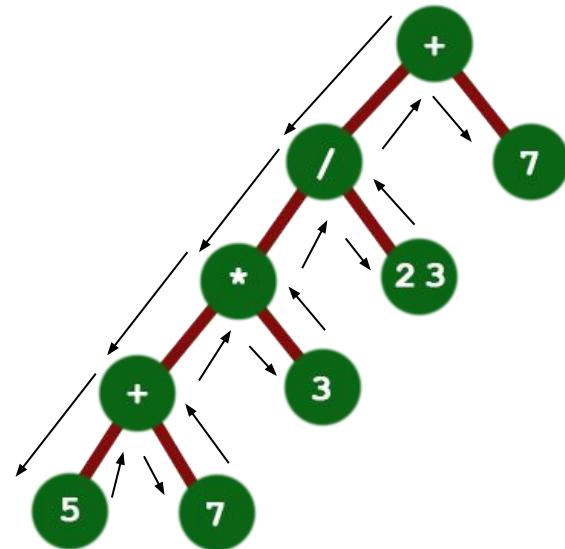
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$$(((5 + 7) * 3) / 23) + 7$$

(Operator precedence matters!)

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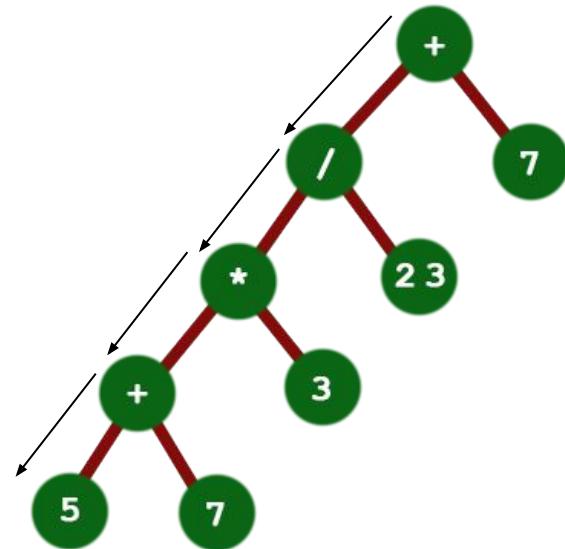
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Reverse Polish Notation

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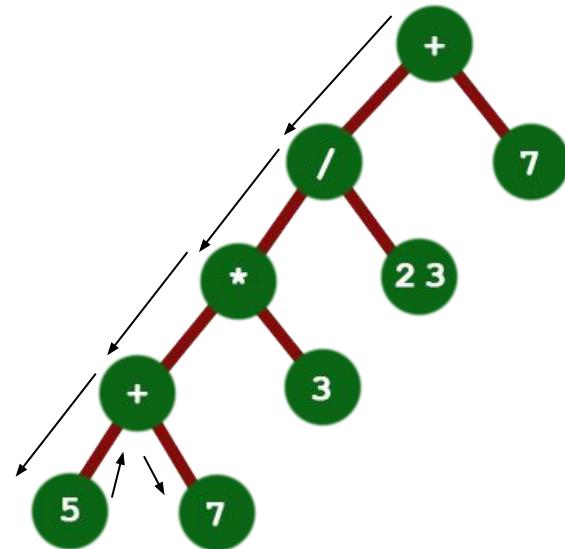
Operators become nodes; operands become leaves.

We can then walk the tree to produce our output. There are three methods.

Pre-order: Node, Left child, Right child

In-order: Left child, Node, Right child

Post-order: Left child, Right child, Node



5 7

Reverse Polish Notation

Answer: TREES!

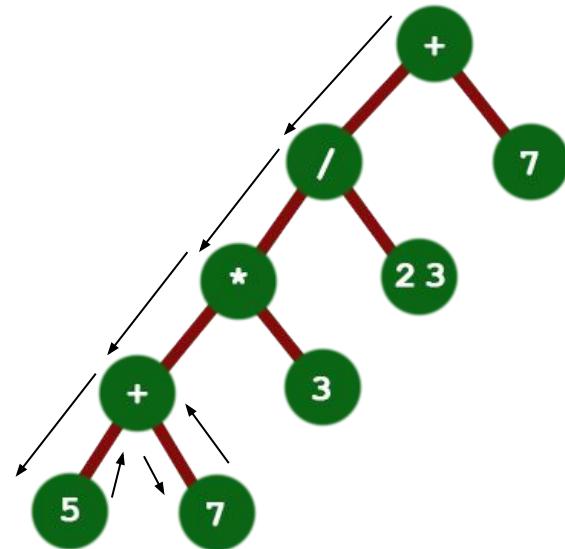
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5 7 +

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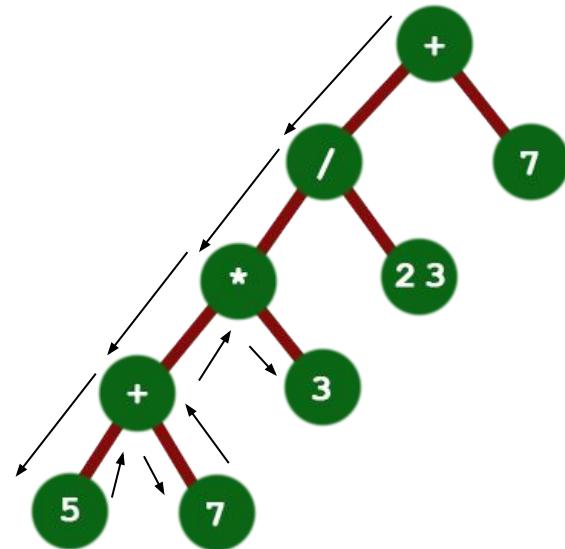
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Post-order: Left child, Right child, Node



5 7 + 3

Reverse Polish Notation

Answer: TREES!

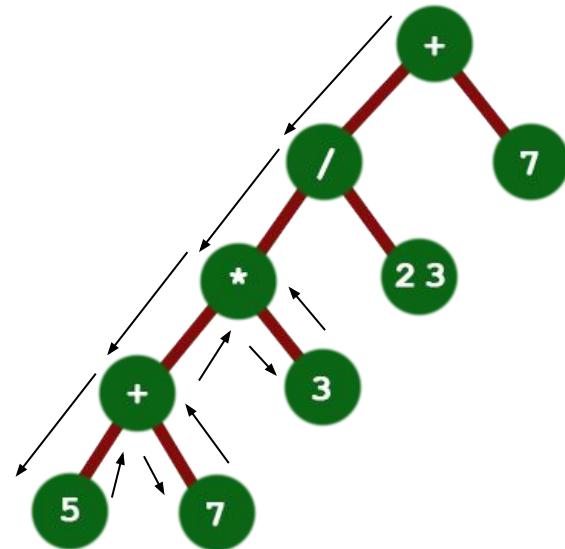
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5 7 + 3 *

Reverse Polish Notation

Answer: TREES!

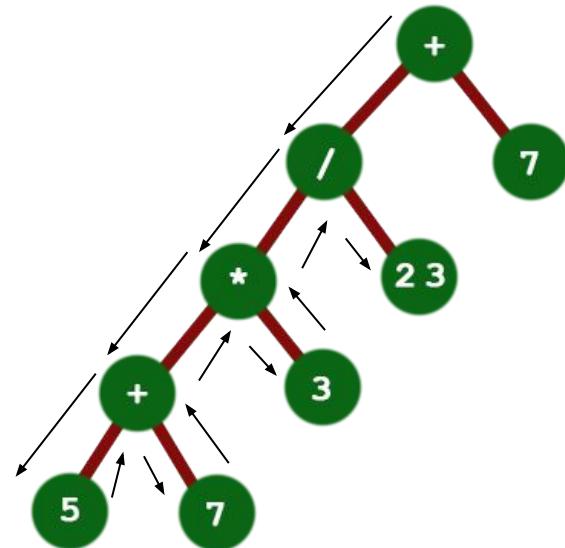
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$$5 \ 7 \ + \ 3 \ * \ 23$$

Reverse Polish Notation

Answer: TREES!

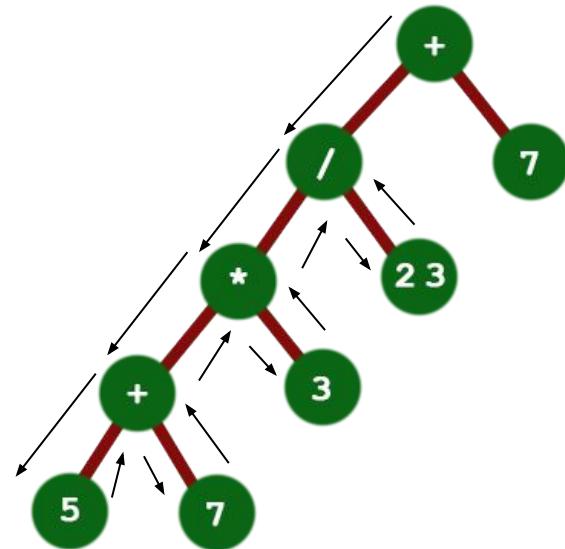
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5 7 + 3 * 23 /

Reverse Polish Notation

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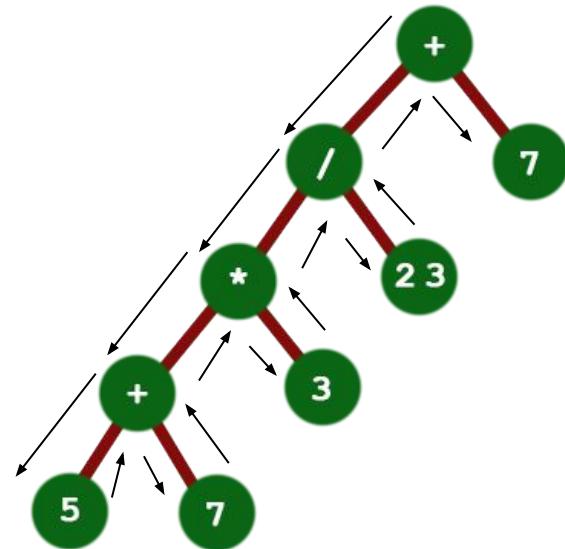
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$5 \ 7 \ + \ 3 \ * \ 2 \ 3 \ / \ 7$

Reverse Polish Notation

Answer: TREES!

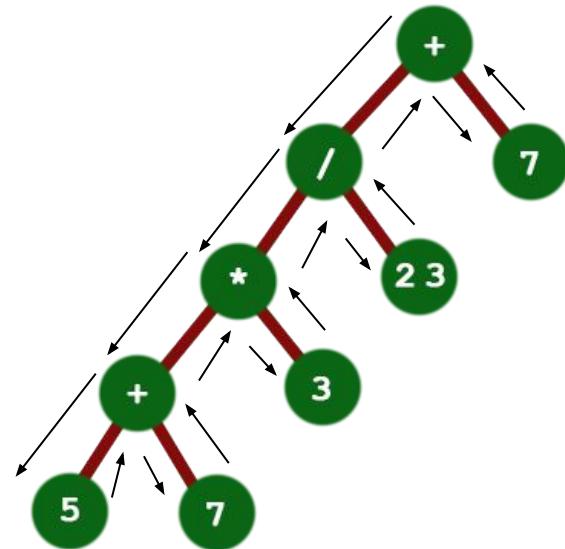
Operators become nodes; operands become leaves.

We can then walk the tree to produce our output. There are three methods.

Pre-order: Node, Left child, Right child

In-order: Left child, Node, Right child

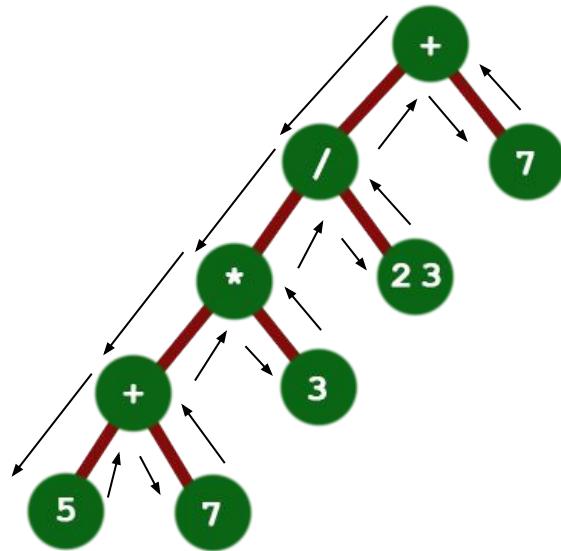
Post-order: Left child, Right child, Node



5 7 + 3 * 23 / 7 +

Reverse Polish Notation

How do we get it into the tree in the first place?

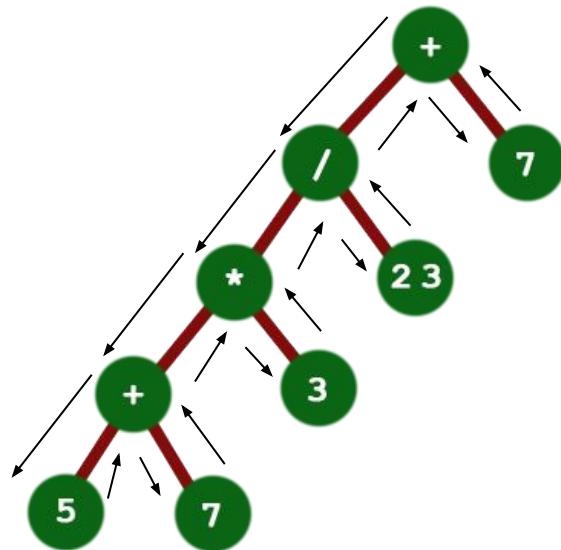


5 7 + 3 * 23 / 7 +

Reverse Polish Notation

How do we get it into the tree in the first place?

Parsers will do it - creating an *Abstract Syntax Tree* - but operator precedence is messy.



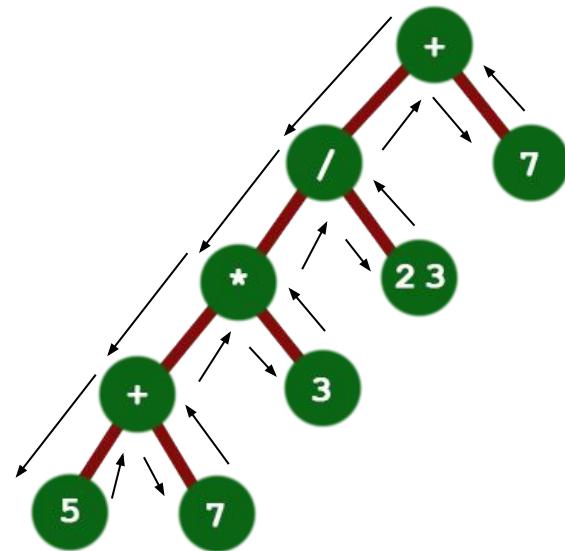
5 7 + 3 * 23 / 7 +

Reverse Polish Notation

How do we get it into the tree in the first place?

Parsers will do it - creating an *Abstract Syntax Tree* - but operator precedence is messy.

Enter Edsger Dijkstra again - his “shunting yard” algorithm is outside the scope of this talk.



5 7 + 3 * 23 / 7 +

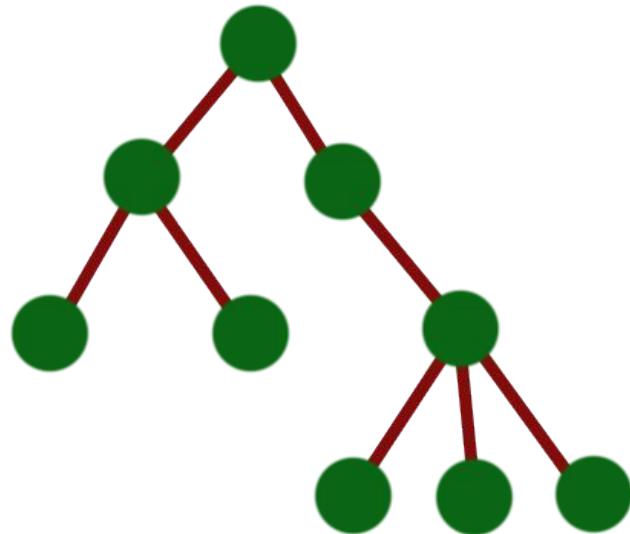


Nested sets



Nested sets

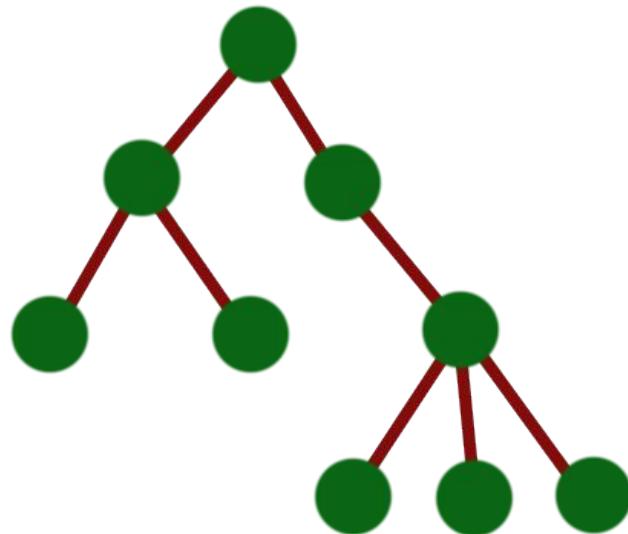
Problem: how do you store a tree in a database?



Nested sets

Problem: how do you store a tree in a database?

Answer: use a GraphDB like neo4j



HIPSTER OVERLOAD!

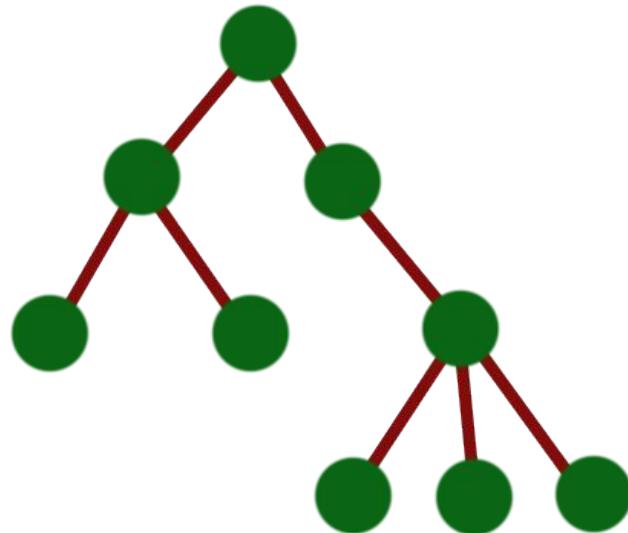


(Fine, we're just afraid of change)



Nested sets

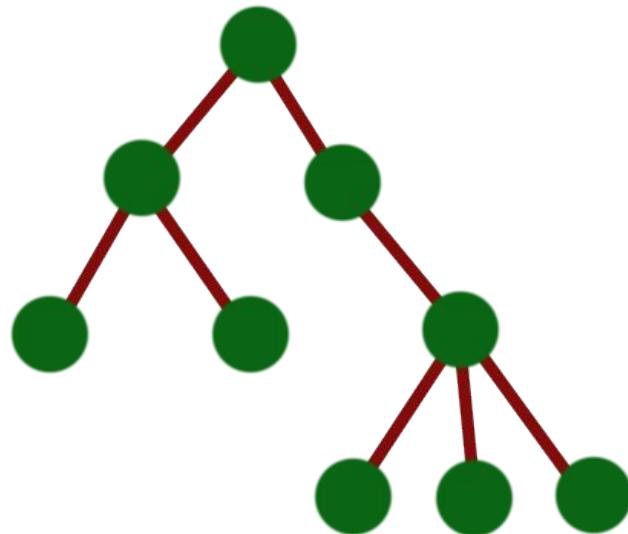
Problem: how do you store a tree in a RDBMS?



Nested sets

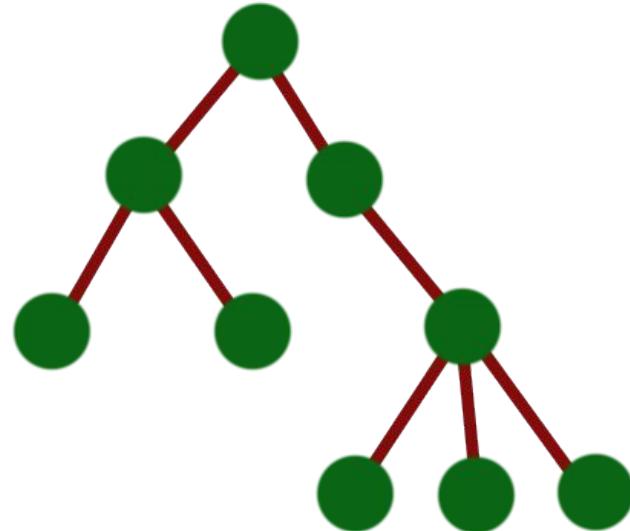
Problem: how do you store a tree in a RDBMS?

Easy! Each record has an id and a parent id; the root is the record with no parent id.



Nested sets

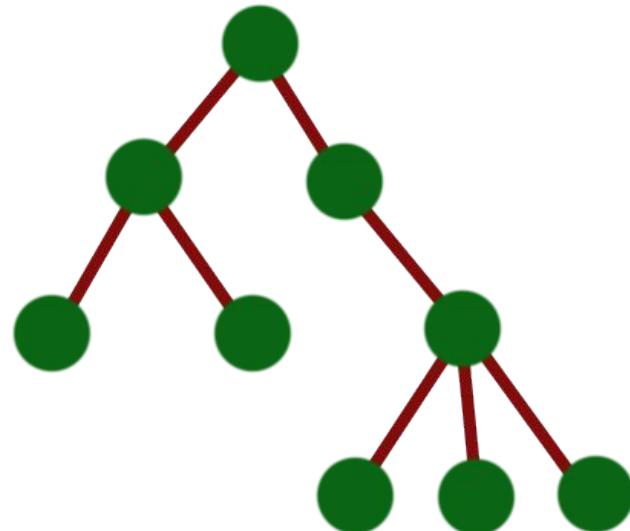
Problem: how do you retrieve all of a node's antecedents in a RDBMS?



Nested sets

Problem: how do you retrieve all of a node's antecedents in a RDBMS?

Easy! Get that node's id, find all records with that as a parent id. Then for each of those records find all records with the parent id matching that record's id. Then for each of *those* records...

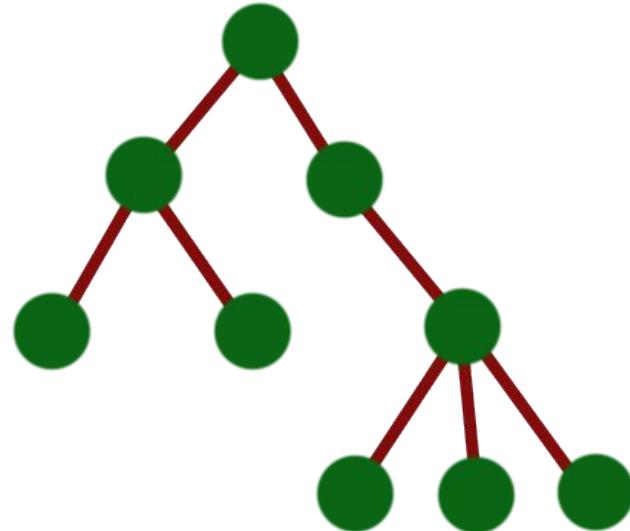


Nested sets

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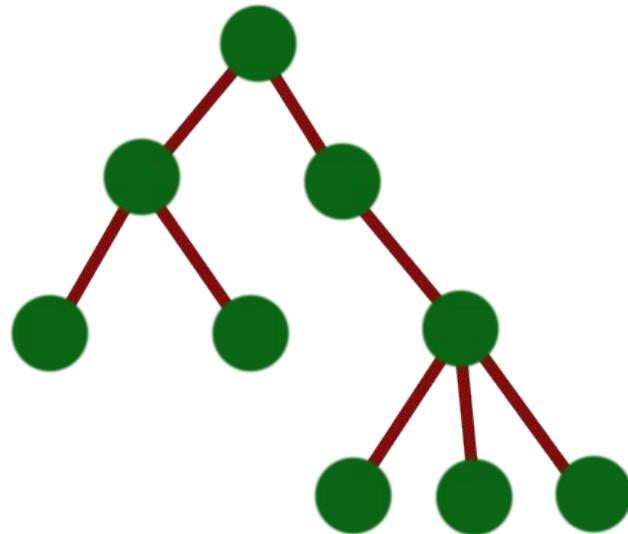
Easy! Get that node's id, find all records with that as a parent id. Then for each of those records find all records with the parent id matching that record's id. Then for each of *those* records...

The above solution can easily spiral out of control and generate huge numbers of queries.



Nested sets

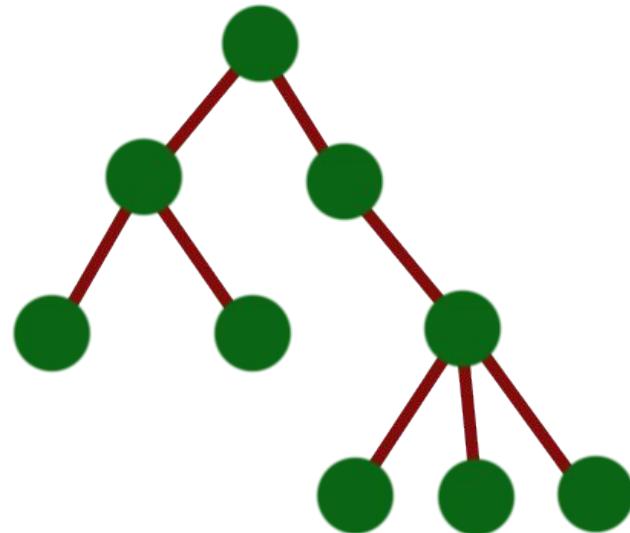
This is where *nested sets* come in.



Nested sets

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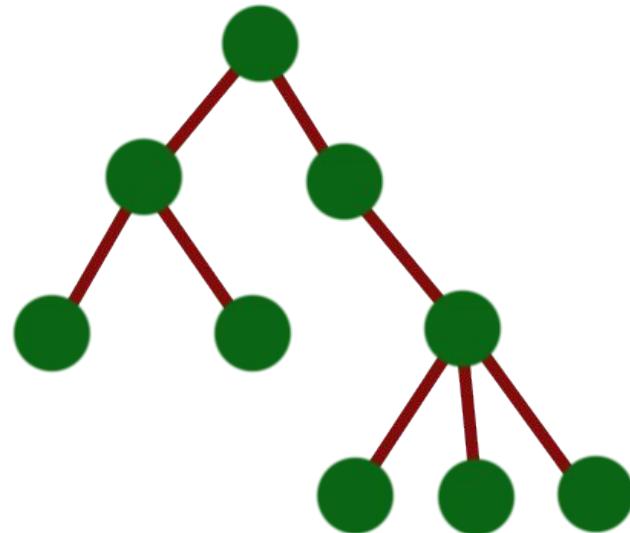
Add two more columns to your records,
left and *right*.



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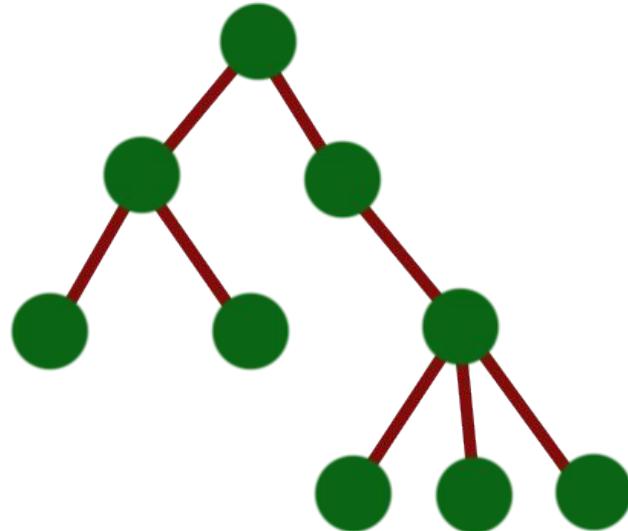


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Add two more columns to your records,
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Then to store the tree, walk it while
counting the times you enter a node. If
it's your first time there, set its left value
to the counter; if you've been there
before, set its right value to the counter.

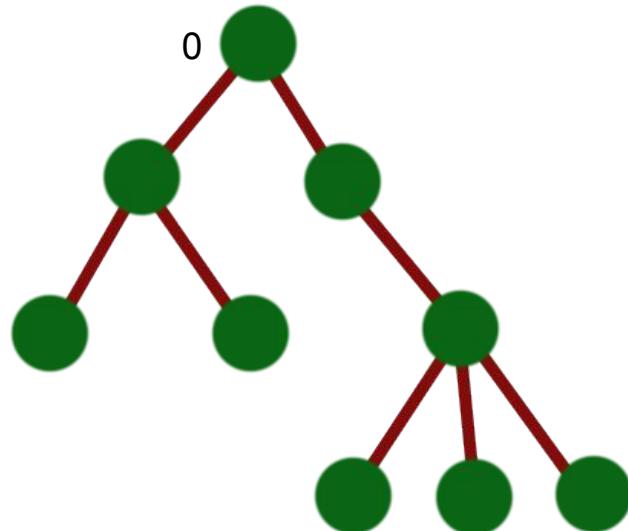


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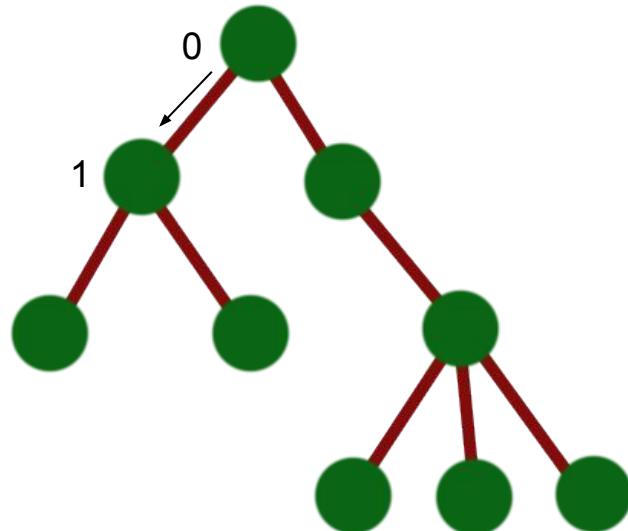


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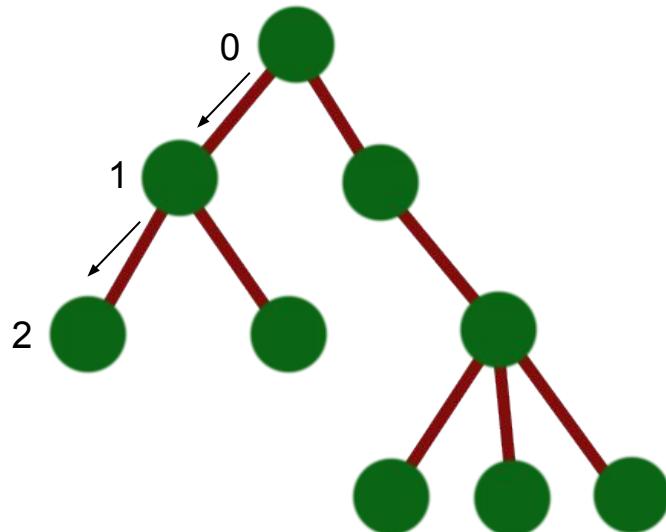


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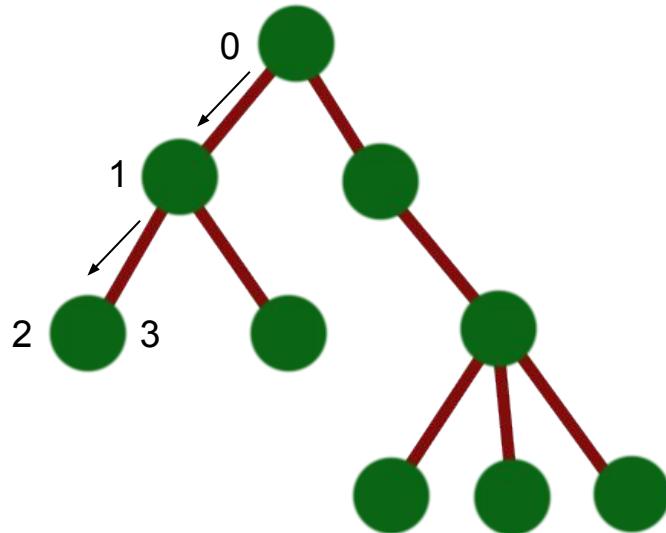
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If there are no more children to walk, set
the node's right value to the counter.



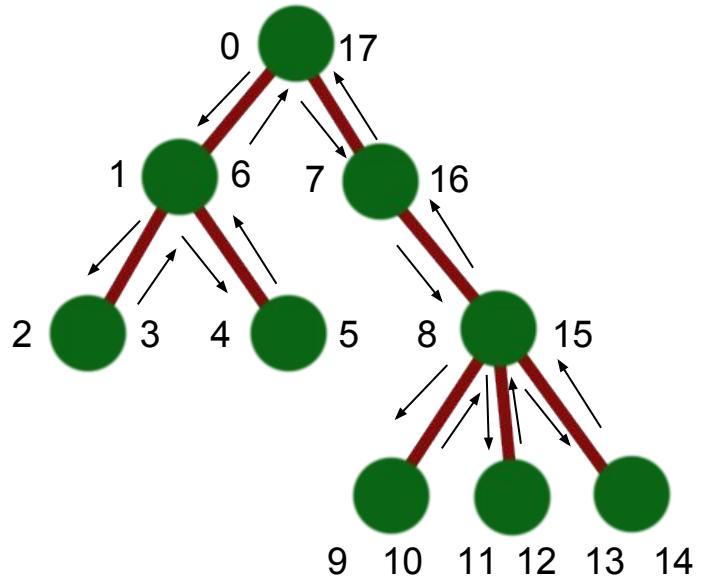
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Add two more columns to your records, *left* and *right*.

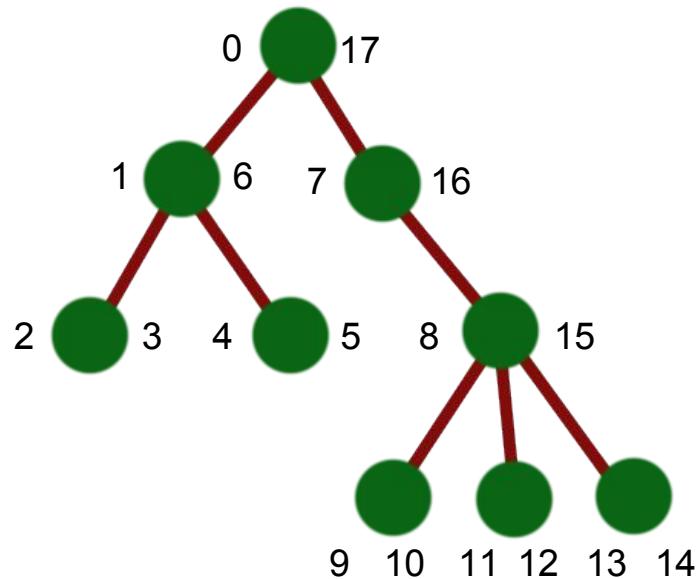
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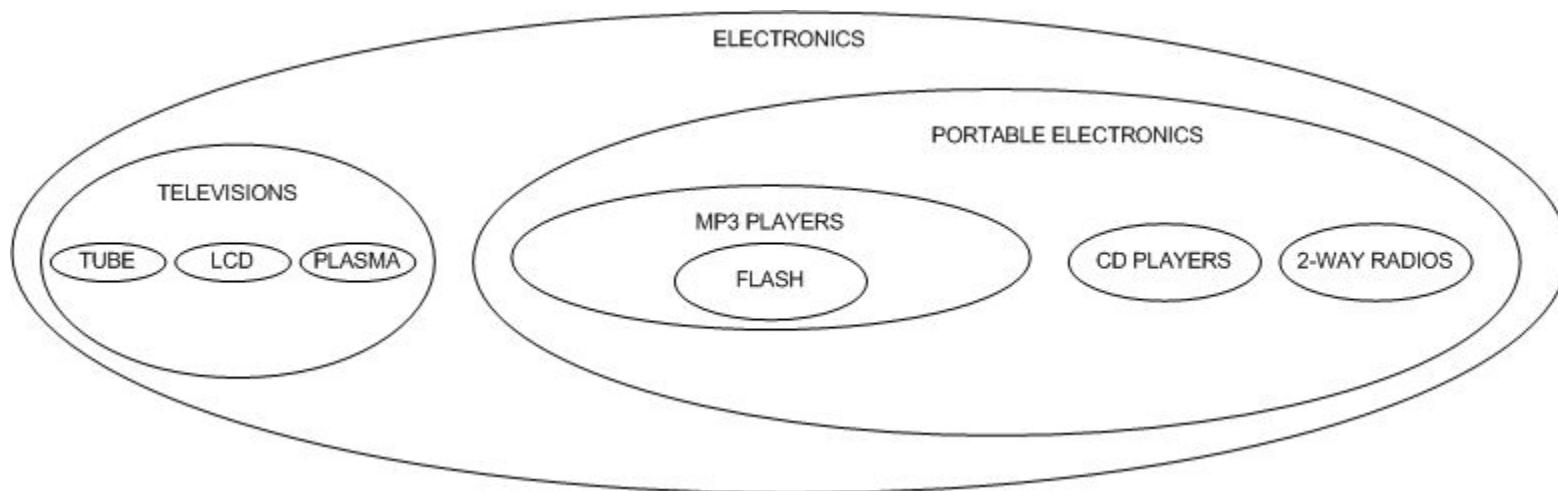


Nested sets

Every node now has the property that its children have left and right values between its own.



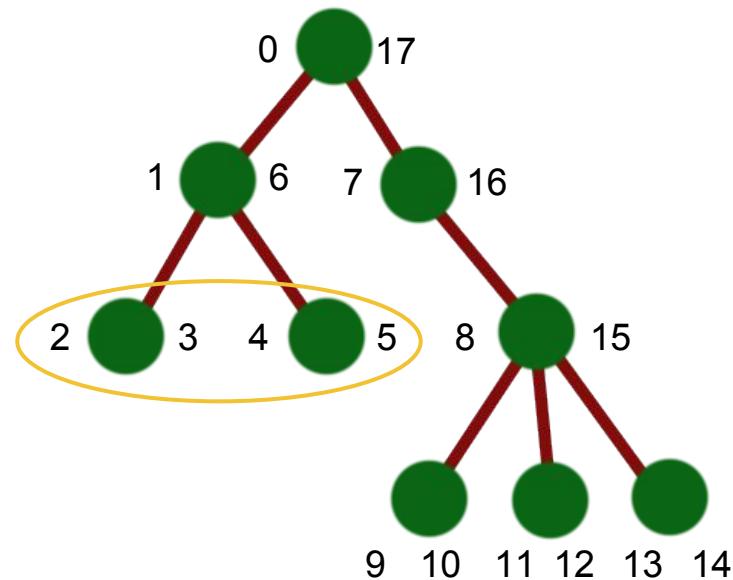
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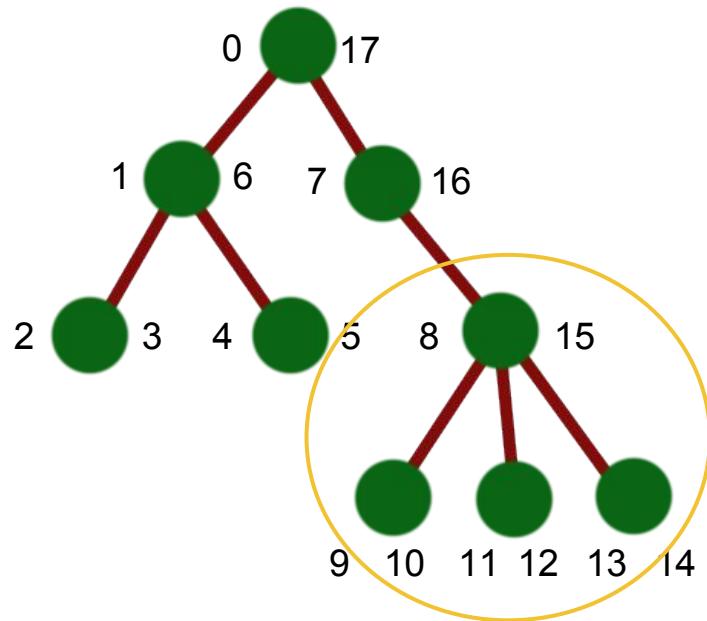
```
SELECT * FROM nodes  
WHERE left > 1 AND right < 6
```



Nested sets

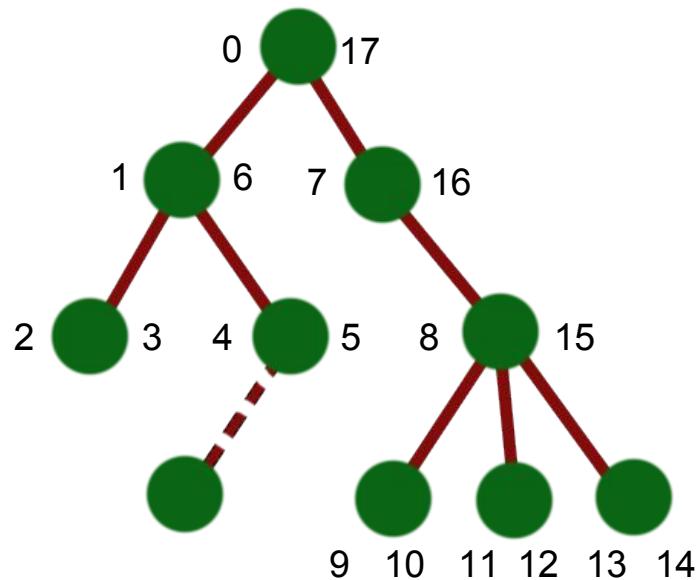
Every node now has the property that its children have left and right values between its own.

```
SELECT * FROM nodes  
WHERE left > 7 AND right < 16
```



Nested sets

Insertion in SQL is then easy - with the left value for the parent node:



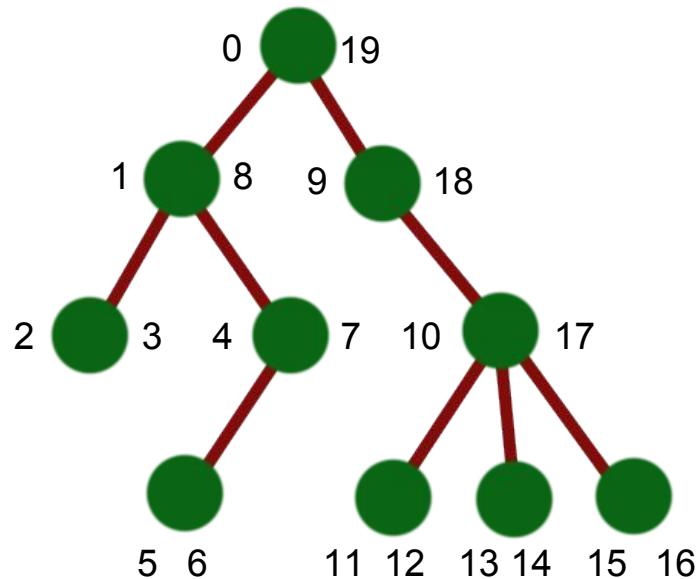
Nested sets

Insertion in SQL is then easy - with the left value for the parent node as *pleft*:

```
UPDATE node SET left = left + 2  
WHERE left > pleft;
```

```
UPDATE node SET right = right + 2  
WHERE right > pleft;
```

```
INSERT INTO node (left, right)  
VALUES (pleft + 1, pleft + 2);
```



Nested sets

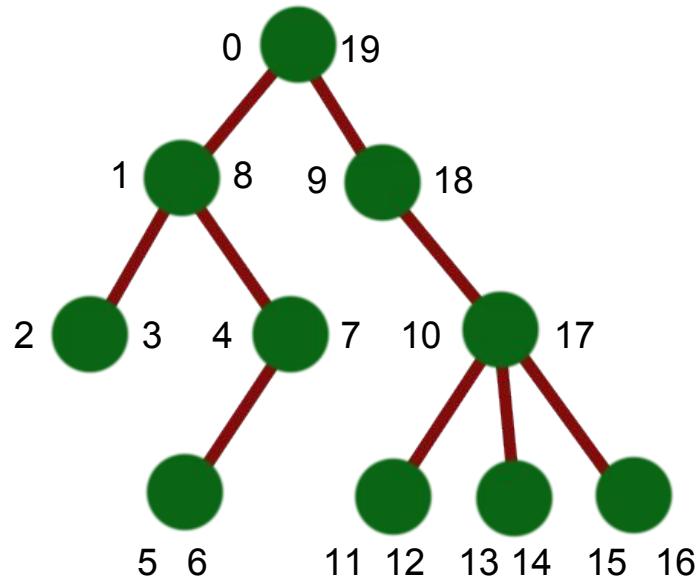
Deletion in SQL is easy too - with the left value for the node to be deleted as *p/left*:

```
UPDATE node SET left = left - 2
```

```
WHERE left > pleft;
```

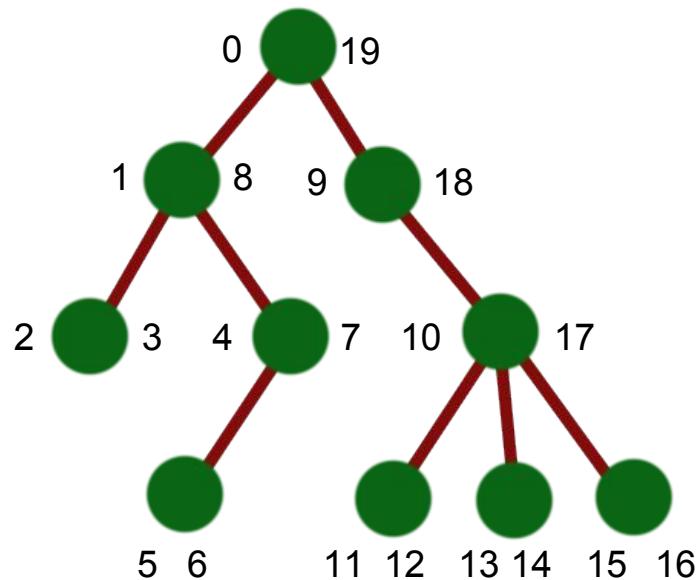
```
UPDATE node SET right = right - 2
```

```
WHERE right > pleft;
```



Nested sets

There are extensions to do this for you in both versions of Doctrine, Eloquent and Propel.



Depth-first: Modelling language



Depth-first: Modelling language

Sentences can be modelled as directed graphs:

The

cat

sat

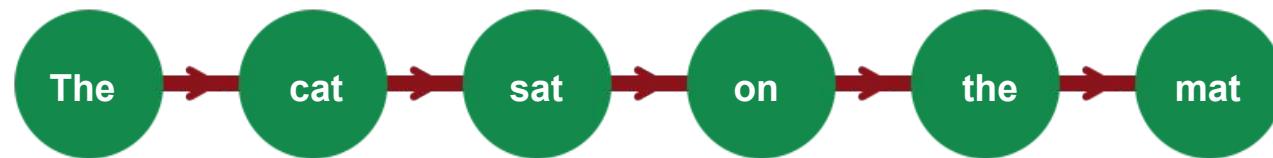
on

the

mat

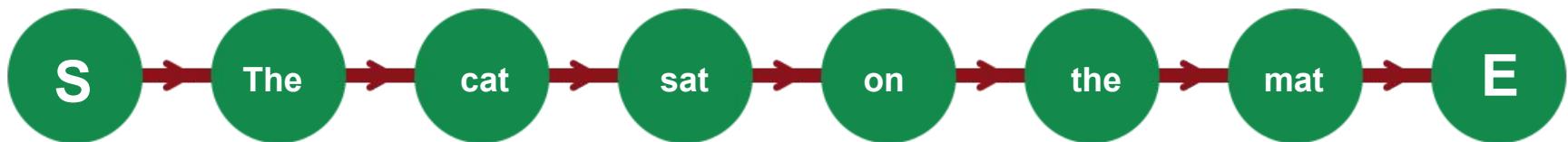
Depth-first: Modelling language

Sentences can be modelled as directed graphs:



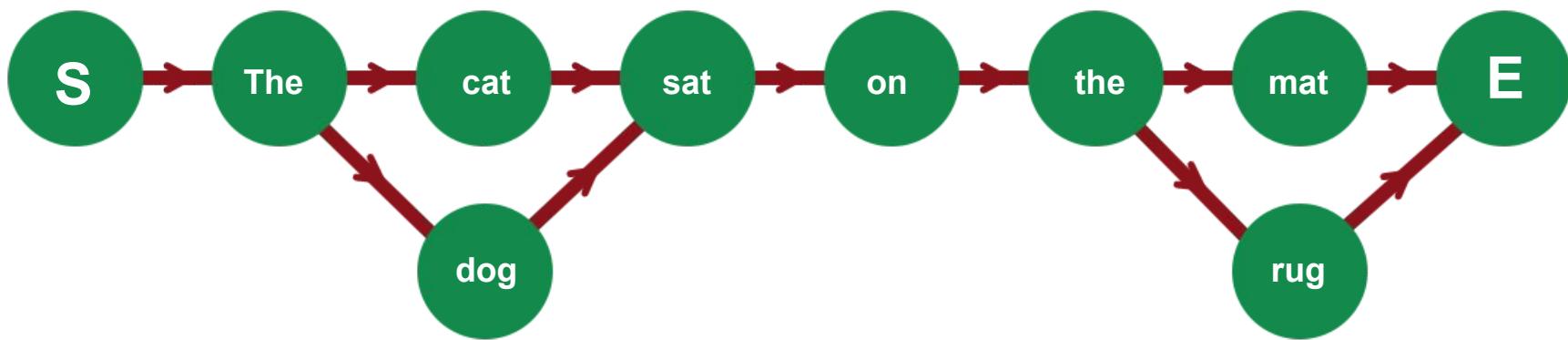
Depth-first: Modelling languages

We can then add special start and end nodes:



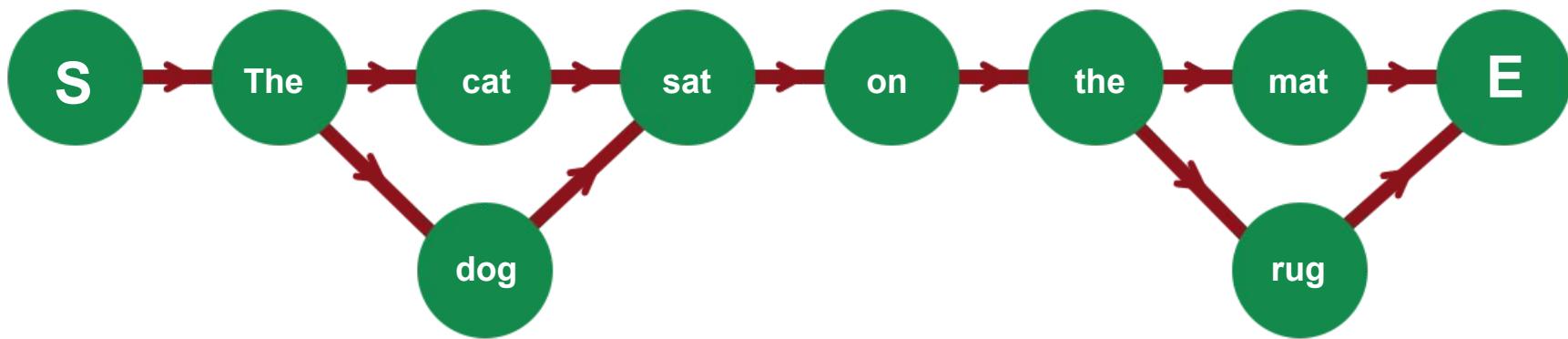
Depth-first: Modelling languages

Now add another sentence:



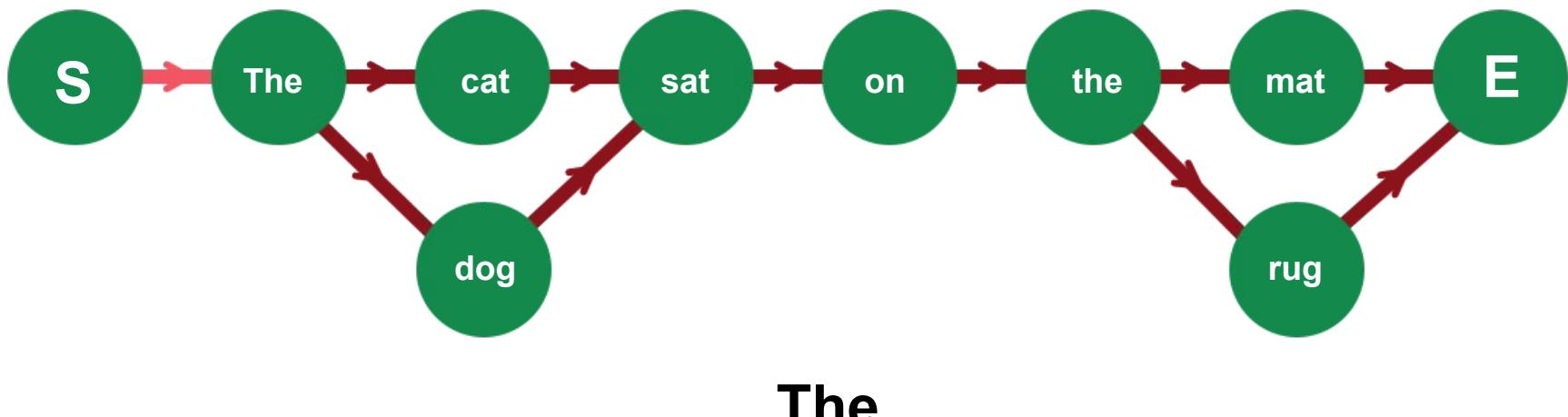
Depth-first: Modelling languages

We can now generate a novel sentence by randomly traversing it:



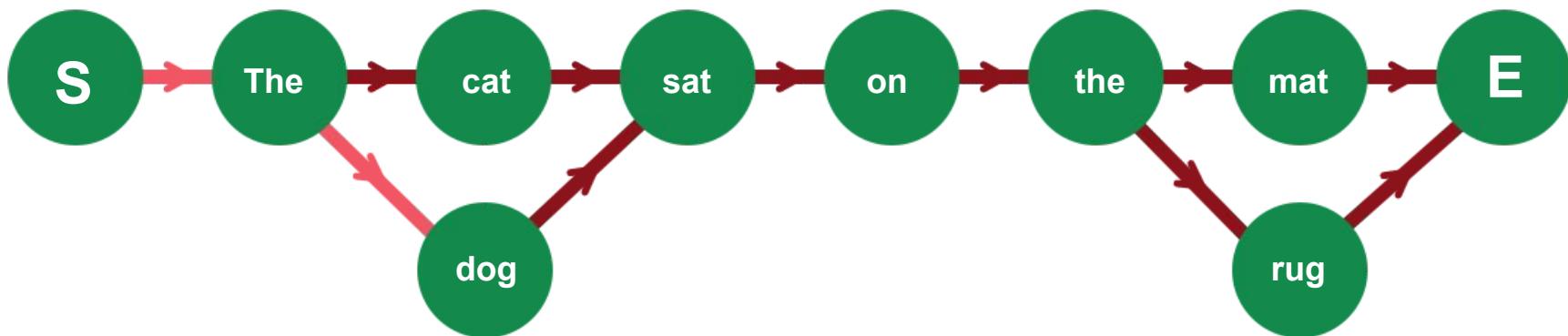
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Depth-first: Modelling languages

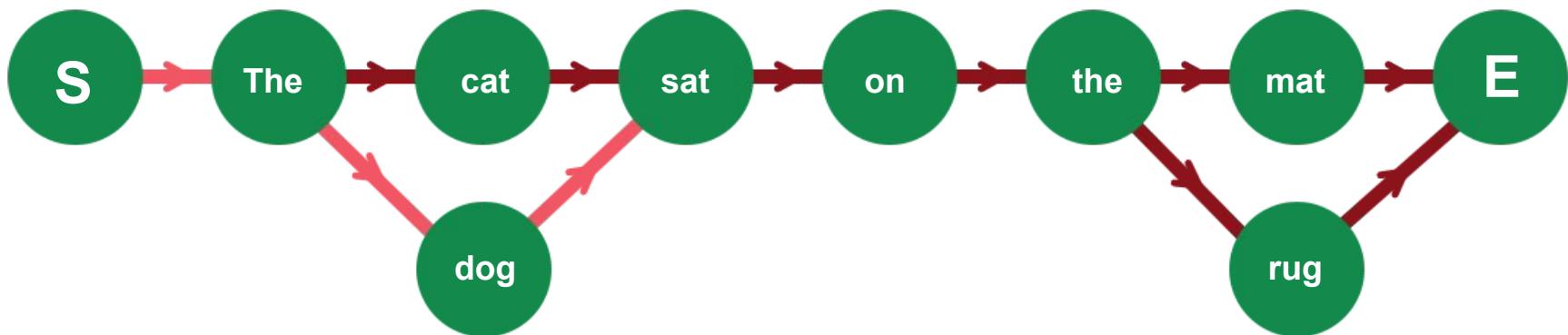
We can now generate a novel sentence by randomly traversing it:



The dog

Depth-first: Modelling languages

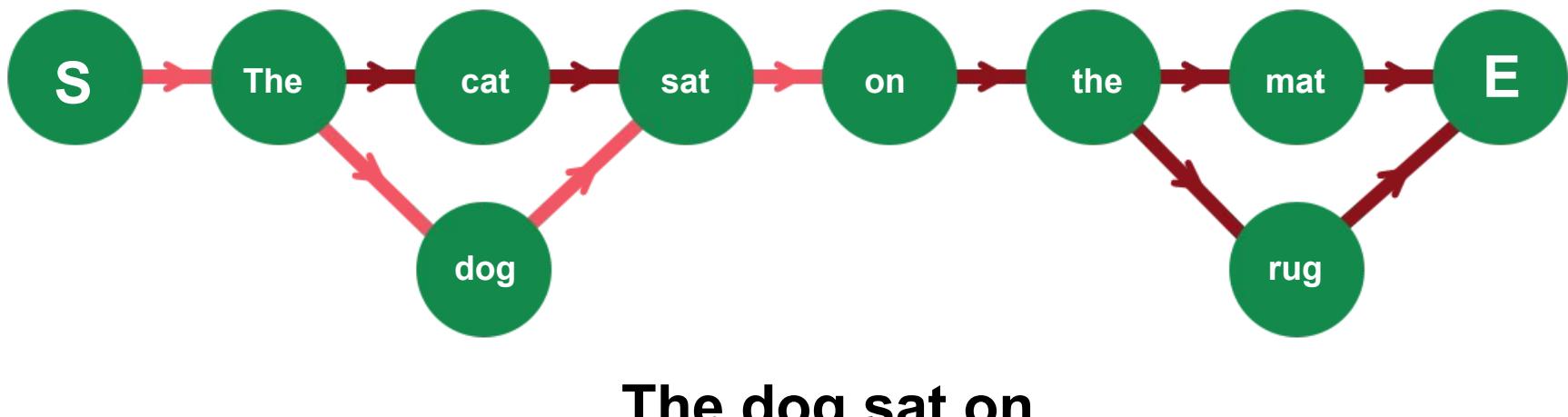
We can now generate a novel sentence by randomly traversing it:



The dog sat

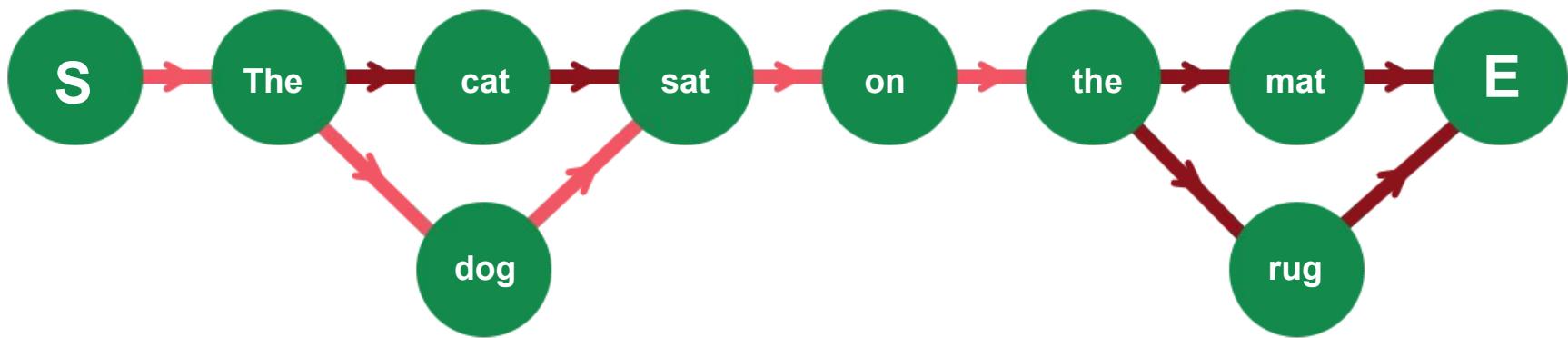
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Depth-first: Modelling languages

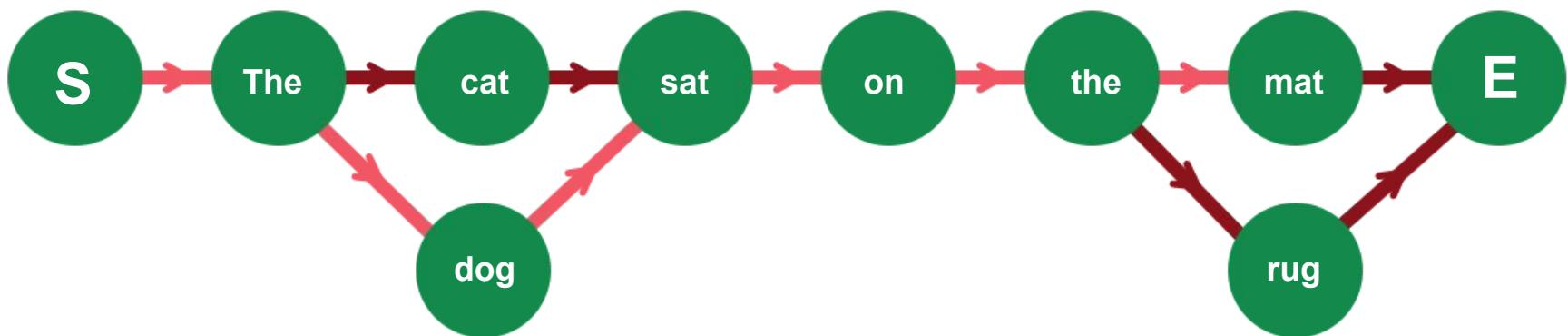
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The dog sat on the

Depth-first: Modelling languages

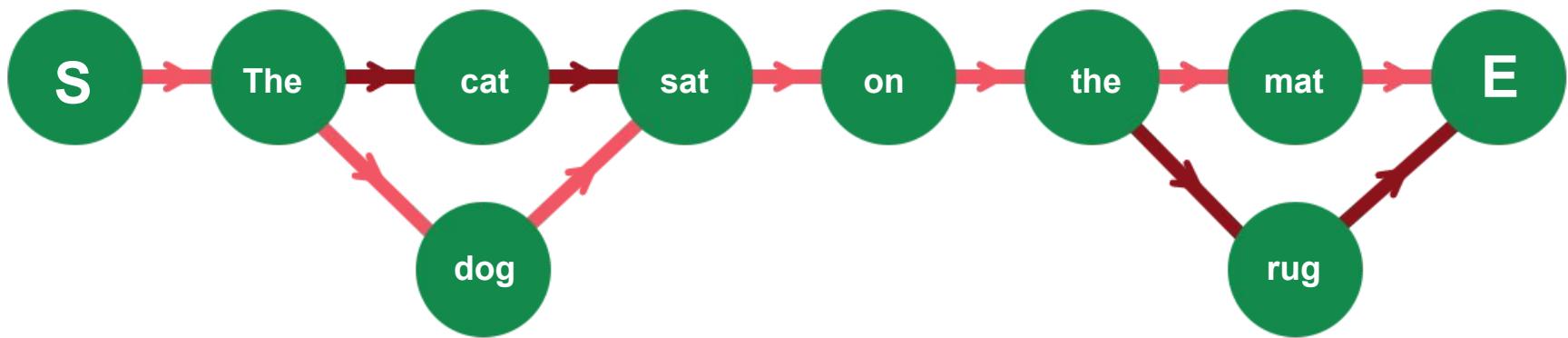
We can now generate a novel sentence by randomly traversing it:



The dog sat on the mat

Depth-first: Modelling languages

When we find the end node, we have a (structurally sound) sentence.



The dog sat on the mat.

Depth-first: Modelling sentences

Daily Mail Headline Generator

<http://choult.com/dm>

Source: <http://bit.ly/2aNrWF4>

Depth-first: Modelling sentences

**NORTH KOREA FIRES A 60FT WELL IN THE
FIRST JOB - SAYS HE WAS SHOT DEAD HIS
EMOTIONAL VISIT TO LONG-FORGOTTEN
1846 WILD WEST SETTLERS WHO WON BY
ISIS ATTACK**

Depth-first: Modelling sentences

**MICHAEL PHELPS GETS HIS
FRIEND'S JAPANESE AKITA DOG**

Depth-first: Modelling sentences

**AWE-INSPIRING MOMENT
AMERICA'S GOT TALENT ACT GOES
GLUTEN-FREE WITH HER BROTHER**

In Summary

Graphs are cool!



Questions?



Have you been affected by any of the issues in this talk?

Email: chris@choult.com

Twitter: @choult

LinkedIn: Christopher Hoult