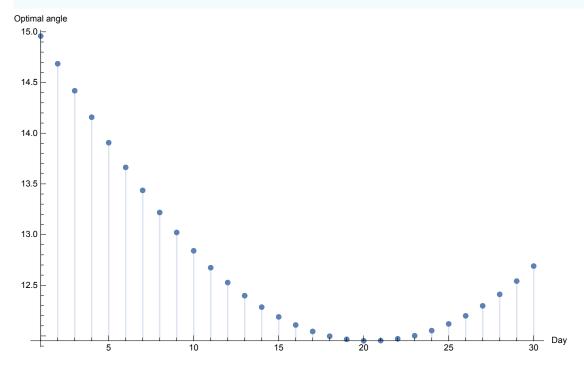
dayAngle[day of month, month, year] returns optimal angle for this day



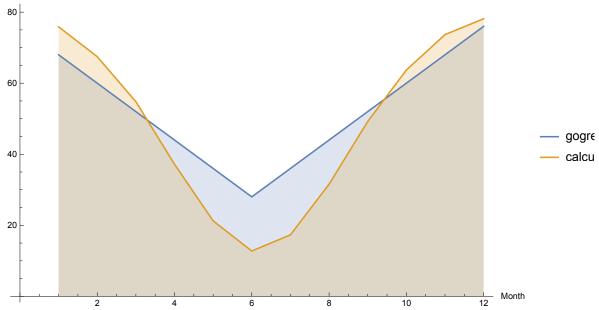
```
(* Comparison with perpendicular to sun at noon, per month,
http://www.gogreensolar.com/pages/solar-panel-tilt-calculator *)
<< SolArduino`
? monthAngle
greenList = {68, 60, 52, 44, 36, 28, 36, 44, 52, 60, 68, 76};
list = Table[monthAngle[x, 2016], {x, 1, 12}]
ListLinePlot[{greenList, list}, Filling → Axis,
 PlotLegends → {"gogreensolar", "calculations"}, ImageSize → Large,
 AxesLabel → {"Month", "Average of optimal angle"}]
```

monthAngle[month, year] returns optimal angle for a specific month by taking the average of the optimal angle each day

- ... FindMaximum: The line search decreased the step size to within the tolerance specified by AccuracyGoal and PrecisionGoal but was unable to find a sufficient increase in the function. You may need more than MachinePrecision digits of working precision to meet these tolerances.
- ... FindMaximum: The line search decreased the step size to within the tolerance specified by AccuracyGoal and PrecisionGoal but was unable to find a sufficient increase in the function. You may need more than MachinePrecision digits of working precision to meet these tolerances.
- ... FindMaximum: The line search decreased the step size to within the tolerance specified by AccuracyGoal and PrecisionGoal but was unable to find a sufficient increase in the function. You may need more than MachinePrecision digits of working precision to meet these tolerances.
- General: Further output of FindMaximum::Istol will be suppressed during this calculation.

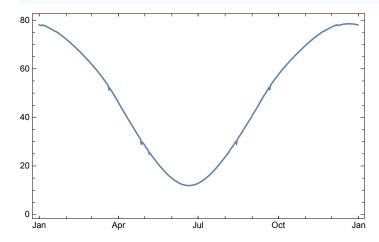
```
{75.8754, 67.4699, 54.7956, 37.1887, 21.2384,
12.7559, 17.3159, 31.5787, 49.223, 63.7122, 73.67, 78.1485}
```

Average of optimal angle



```
(* season values *)
<< SolArduino`
year = 2016;
monthSum[m_{j}, j_{j}] := ( (* month, begin day, end day *)
   Quiet[dayAngle[x, m, year]],
   \{x, i, j\}
(* takes winter of [year] only. dates according to solarpaneltilt.com,
summer april 18, autumn august 24, winter oct 7, spring march 5 *)
summerSum = Quiet[monthSum[4, 18, 30] + monthSum[5, 1, 31] +
    monthSum[6, 1, 30] + monthSum[7, 1, 31] + monthSum[8, 1, 23]];
summerDays = QuantityMagnitude[Quantity[DateDifference[{year, 4, 18}, {year, 8, 23}]]] + 1;
summerSum / summerDays (* 21 degrees *)
autumnSum = monthSum[8, 24, 31] + monthSum[9, 1, 30] + monthSum[10, 1, 6];
autumnDays = DayCount[{year, 8, 24}, {year, 10, 6}] + 1;
autumnSum / autumnDays (* 49 degrees *)
winterSum = Quiet[monthSum[10, 7, 31] + monthSum[11, 1, 30] +
    monthSum[12, 1, 31] + monthSum[1, 1, 31] + monthSum[2, 1, 29] + monthSum[3, 1, 4]];
winterDays = DayCount[{year, 10, 7}, {year + 1, 3, 4}] + 1;
winterSum / winterDays (* 73 degrees *)
springSum = Quiet[monthSum[3, 5, 31] + monthSum[4, 1, 17]];
springDays = DayCount[{year, 3, 5}, {year, 4, 17}] + 1;
springSum / springDays (* 49 degrees *)
(* Year average *)
(winterSum + summerSum + springSum + autumnSum) / 366 (* 49 degrees *)
(* standalone *)
(*Sum[
   days =
    With[{first=DateObject[{year,m,1}]},DayCount[first,DatePlus[first,{{1,"Month"}}]]];
    Quiet[dayAngle[d,m]]
    ,{d,1,days}]
   , \{m,1,12\}] / \ Quantity Magnitude [Quantity [Date Difference [ \{year,1,1\}, \{year,12,31\}]]] + 1 
(* 50 degrees *)
*)
20.8601
48.4822
72.5455
48.9036
48.5365
```

dayAngle[day of month, month, year] returns optimal angle for this day



```
(* angle over the day *)
<< SolArduino`
calculatesunPos[DateObject[{2016, 8, 17}]]
res = dayAngles[DateObject[{2016, 8, 17}], 14]
ListLinePlot[Table[res[[i]][[2]], {i, 1, Length[res]}],
 AxesLabel → {"Angle of the day", "degrees"}, ImageSize → Large]
\{\{38.9735, 54.7261\}, \{254.734, 52.1053\}, \{612.696, 50.1369\},
 {873.733, 48.0889}, {1033.03, 45.853}, {1118.3, 43.2855}, {1146.28, 40.1852},
 \{1660.85, 34.9526\}, \{993.106, 27.2792\}, \{837.73, 17.3171\},
 \{647.221, 0.819512\}, \{435.721, 0.\}, \{200.062, 0.\}, \{80.8025, 0.\}\}
degrees
50
40
30
20
10
                                                                          Angle of the day
                                                      10
                                                                12
```

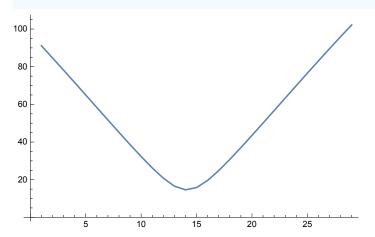
```
(* Plot of power increase when adjusting more times a day *)
<< SolArduino`
calculatesunPos[DateObject[{2016, 8, 17}]]
(* percentages *)
t = Table[
  dayPower[dayAngles[DateObject[{2016, 8, 17}], x]],
(* relative to first *)
s = Table[
  (t[[i]] - t[[1]]) / t[[1]],
  {i, 2, Length[t]}
(* relative to previous *)
Table[
 (t[[i]] - t[[i-1]]) / t[[i-1]],
 {i, 2, Length[t]}
ListLinePlot[t, PlotRange → All]
ListLinePlot[s, PlotRange → All]
{9144.18, 9561.69, 9873.62, 9882.66, 9885.25, 9894.52, 9924.12, 9921.82, 9914.93, 9924.79}
{0.0456588, 0.0797716, 0.0807601, 0.0810428,
 0.0820569, 0.0852942, 0.0850424, 0.0842891, 0.0853679}
{0.0456588, 0.0326232, 0.000915529, 0.000261591,
 0.000938063, 0.0029918, -0.000232073, -0.000694221, 0.000994926
9800
9600
9400
9200
```

```
0.08
0.07
0.06
0.05
(* list of angles for a day *)
<< SolArduino`
calculatesunPos[DateObject[{2016, 8, 17}]]
? dayAngles
dayAngles[DateObject[{2016, 8, 17}], 14][[All, 2]]
```

dayAngles[date, number of adjustment times per day ≥ 1] returns List with optimal angles and power received with that angle over each interval (spread evenly over the day) after an angle adjustment

```
{54.7261, 52.1053, 50.1369, 48.0889, 45.853, 43.2855,
 40.1852, 34.9526, 27.2792, 17.3171, 0.819512, 0., 0., 0.}
(* misalignment over day *)
<< SolArduino`
calculatesunPos[DateObject[{2016, 8, 17}]]
? angle
ListLinePlot[Table[
  angle[i, 25, DateObject[{2016, 8, 17}]] * 180 / Pi
  , {i, 1, getSunPositionsLength[]}
 ]]
```

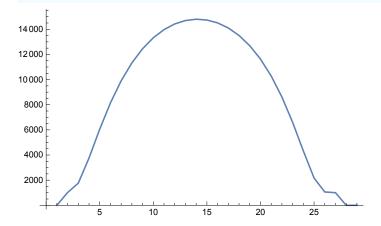
angle[index of sunPositions table, solar panel angle in degrees, date (date object)] returns misalignment with the sun in radians



```
(* sun insolation over day, 26.4 m2 panels *)
<< SolArduino`
calculatesunPos[DateObject[{2016, 8, 17}]]
?directPower
ListLinePlot[Table[
  directPower[i, 25, DateObject[{2016, 8, 17}]] * 26.4
  , {i, 1, getSunPositionsLength[]}
 ]]
```

directPower[index of sunPositions table, solar panel angle in degrees,

date (date object)] returns power that the solar panels receive from the sun in W/m^2



```
(* efficiency over the day for adjusting once a day *)
<< SolArduino`
(*date = DateObject[{2016,8,17}];
ListLinePlot[
 calculatesunPos[date];
 Table
  dataAugust[[i]]*100/(directPower[i,dayAngle[17,8,2016],date]*26.4)
  ,{i,1,getSunPositionsLength[]}
(*
(* efficiency adjusting every hour *)
(*data = Import[ NotebookDirectory[]<>"data24_30.csv"];
data = Delete[data,1];
?csvToList
   date = DateObject[{2016,8,30}];
data3008 = csvToList[date,data]*)
data3008 = {0, 95.8333`, 280.6667`, 514.5`, 785, 1117.5`, 1465, 1740, 1997.5`, 2230.8333`,
   2440, 1979.75`, 2830.3333`, 3014.3333`, 3151.5`, 3280.5`, 3400, 3479.6667`, 3580.5`,
   3657.1667`, 3679.5`, 3735, 3777.1667`, 3794.3333`, 3789, 3769.8333`, 3730.1667`, 3678.5`,
   3628.5, 3543.5, 3468.333, 3375.5, 3246, 3148, 3000.333, 2843.5, 2700.5, 2578.5,
   2368.3333, 2089.6667, 1901.6666, 1768.8334, 1615.8334, 1363, 1082.5, 879.8333,
   752.5`, 597.3333`, 349, 187.6667`, 127.1667`, 97.3333`, 75.8333`, 41.6667`, 6.3333`};
? initialiseSunPositionByPrecision
initialiseSunPositionByPrecision[date, 25];
(*Length[data3008]
 getSunPositionsLength[]*)
ListLinePlot
 calculatesunPos[date];
  data3008[[i]] * 100 / (directPower[i, dayAngle[30, 8, 2016], date] * 26.4)
  , {i, 1, getSunPositionsLength[]}
```

initialiseSunPositionByPrecision[date,precision (hours*100)] initializes sunPositions table with positions of the sun for this day

```
Power: Infinite expression — encountered.
Power: Infinite expression - encountered.
Power: Infinite expression -
General: Further output of Power::infy will be suppressed during this calculation.
```

```
100
80
60
40
20
                                                   25
(* now for adjusting panels three times a day! *)
(* for 17/8, optimal angles and times are: 50,34,0 at 6.5,
11.3, 16.2, but directPower takes indices of sunPosition *)
<< SolArduino`
factor = 6.7;
date = DateObject[{2016, 8, 23}];
initialiseSunPositionByPrecision[date, 25];
(* initialise sunPositions with precision of real data *)
(* three plots *)
ListLinePlot[{
  Table[
   directPower[i, 25, date] * factor
   , {i, 1, getSunPositionsLength[]}
  ],
  dataAugust,
  Join[
   Table
    directPower[i, 49, date] * factor
    , {i, 1, Round[getSunPositionsLength[] / 3]}
   ],
   Table[
    directPower[i, 34, date] * factor
    , {i, Round [getSunPositionsLength[] / 3] + 1, Round [getSunPositionsLength[] * 2 / 3]}
   ],
   Table [
    directPower[i, 0, date] * factor
    , {i, Round[getSunPositionsLength[] *2/3] + 1, getSunPositionsLength[]}
  ],
  Join[
   Table
```

```
directPower[i, 41, date] * factor
    , {i, 1, Round[getSunPositionsLength[] 9/14]} (*16:00 is around 9/14 *)
   Table[
    directPower[i, 0, date] * factor
    , {i, Round[getSunPositionsLength[] 9/14] + 1, getSunPositionsLength[]}
 \}, PlotLegends \rightarrow {"calculations 23/8", "real data 17/8",
   "calculations adjusting three times", "adjusting two times"}, ImageSize \rightarrow Large
4000
3000
                                                                                             calcu
                                                                                             real c
2000
                                                                                             - calcu
                                                                                             adjus
1000
```

```
(* two adjustment times, optimised *)
<< SolArduino`
? twoAnglesOptimal
twoAnglesOptimal[DateObject[{2016, 6, 20}]]
twoAnglesOptimal[DateObject[{2016, 12, 20}]]
```

twoAnglesOptimal[date] returns in a list the date/time at which to change the angle of solar panels (besides before to get optimal power, then the two angles of the day, then the percent increase sunrise) one setting for the whole day, then the percent increase compared of power compared to to one setting if you would adjust fourteen times a day, spread evenly over the day

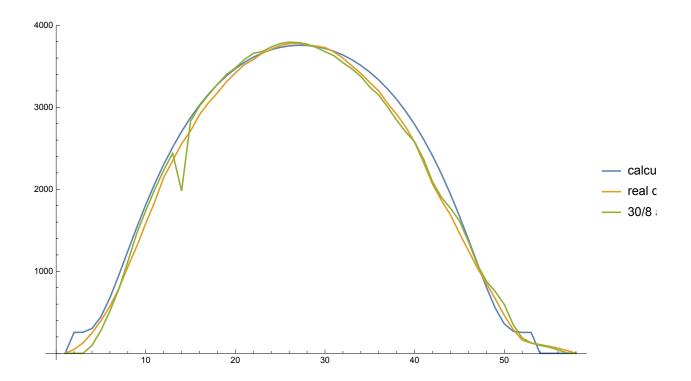
- ... FindMaximum: The line search decreased the step size to within the tolerance specified by AccuracyGoal and PrecisionGoal but was unable to find a sufficient increase in the function. You may need more than MachinePrecision digits of working precision to meet these tolerances.
- FindMaximum: The line search decreased the step size to within the tolerance specified by AccuracyGoal and PrecisionGoal but was unable to find a sufficient increase in the function. You may need more than MachinePrecision digits of working precision to meet these tolerances.

```
Mon 20 Jun 2016 15:43 GMT+2. , {27.9359, 0.}, 7.72683, 8.63226}
```

- ... FindMaximum: Encountered a gradient that is effectively zero. The result returned may not be a maximum; it may be a minimum or a saddle point.
- ... FindMaximum: Encountered a gradient that is effectively zero. The result returned may not be a maximum; it may be a minimum or a saddle point.

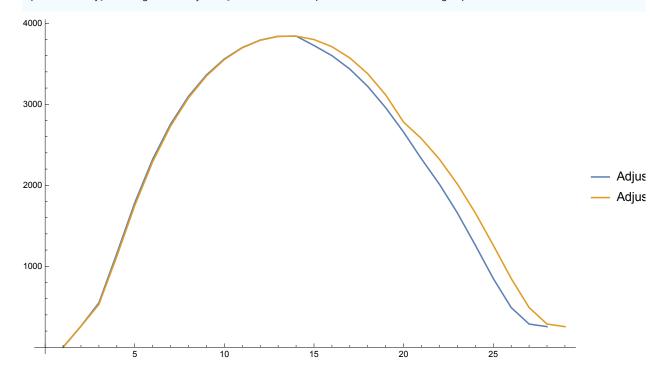
```
Tue 20 Dec 2016 13:42 GMT+2. , {81.2945, 75.5525}, 0.106733, -8.17048}
```

```
(* plot for one day, times 6.7 to compare form of graph *)
<< SolArduino`
(* data adapted to from sunrise, 6:33, to sunset,
21:00. Length of sunPositions and data are both 58 *)
(* day = DateObject[{2016,8,17}]; *)
dataAugust = {0, 47.5, 128.167, 247.833, 398.167, 574.333, 789, 1053.83, 1304.83,
   1584.33, 1846.17, 2144, 2348.33, 2555.83, 2712, 2908.67, 3055.33, 3176.33, 3310.33,
   3419.17, 3519.17, 3580.67, 3659.33, 3707.17, 3753.17, 3775.17, 3781, 3759.5,
   3746.17, 3728.5, 3675, 3599.67, 3504.67, 3411.83, 3302.83, 3197.33, 3046.5,
   2912.83, 2761.17, 2574.83, 2324.33, 2062.5, 1862.17, 1688.83, 1465, 1254, 1041.5,
   853.167, 666, 463, 291.833, 160.667, 124.333, 106.833, 86, 62.8333, 33.3333, 2};
(* day = DateObject[{2016,5,13}]; *)
dataMay = {0, 19.5, 57, 118.667, 200.833, 278, 301.333, 497.667, 691.5, 995.667, 1323.5,
   1663, 1857.33, 2262.67, 2571, 2789.83, 3003, 3177.5, 3324.5, 3483.17, 3597, 3719.33,
   3813.67, 3888, 3929.83, 3997.83, 4012.33, 4036, 4080.5, 4067.67, 4034, 3957.67,
   3954.33, 3889.17, 3837, 3746.83, 3641.67, 3453.33, 3423.67, 3215.5, 3121.83,
   2954.5, 2762.67, 2541, 2298.83, 2055.33, 1692, 1540.17, 1253, 1027.17, 782, 579,
   419.5, 295, 226.833, 185.833, 158.667, 115, 84.5, 70.1667, 58.1667, 20.1667, 0};
(* 30/8, adjusting every hour *)
data3008 = {0, 0, 0, 95.8333, 280.6667, 514.5, 785, 1117.5, 1465, 1740,
   1997.5, 2230.8333, 2440, 1979.75, 2830.3333, 3014.3333, 3151.5, 3280.5,
   3400, 3479.6667`, 3580.5`, 3657.1667`, 3679.5`, 3735, 3777.1667`, 3794.3333`,
   3789, 3769.8333`, 3730.1667`, 3678.5`, 3628.5`, 3543.5`, 3468.3333`, 3375.5`,
   3246, 3148, 3000.3333`, 2843.5`, 2700.5`, 2578.5`, 2368.3333`, 2089.6667`,
   1901.6666, 1768.8334, 1615.8334, 1363, 1082.5, 879.8333, 752.5, 597.3333,
   349, 187.6667, 127.1667, 97.3333, 75.8333, 41.6667, 6.3333, 0};
(*Length[dataAugust]
 Length [data3008] *)
ListLinePlot[{
  initialiseSunPositionByPrecision[DateObject[{2016, 8, 17}], 25];
   directPower[i, 25, DateObject[{2016, 8, 17}]] * 6.7
   , {i, 1, getSunPositionsLength[]}
  , dataAugust, data3008}, PlotLegends →
  {"calculations 17/8", "real data 17/8", "30/8 adjusting every hour"}, ImageSize → Large]
```



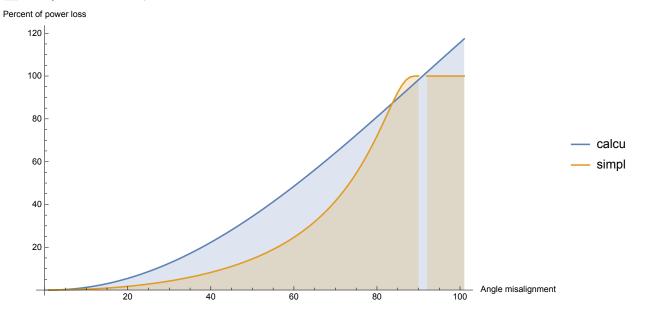
```
(* plot to compare 14 times with 2 times optimised *)
<< SolArduino`
? powerOverDay
date = DateObject[{2016, 8, 17}];
calculatesunPos[date];
factor = 6.7;
angles = dayAngles[date, 14][[All, 2]];
(* prepare legend for graph *)
legend = StringForm["Adjusting `` times", Length[angles]];
{\tt ListLinePlot[\{powerOverDay[angles, date] * factor,}\\
  Join[
   Table[
    directPower[i, 41, date] * factor
    , {i, 1, Round [getSunPositionsLength[] 9/14]} (* 16:00 is around 9/14 *)
   ],
   Table[
    directPower[i, 0, date] * factor
    , {i, Round[getSunPositionsLength[]9/14]+1, getSunPositionsLength[]}
 }, ImageSize → Large, PlotLegends → {legend, "Adjusting 2 times"}]
```

powerOverDay[list of angles of a day, date] returns a list with power received for each angle-period



```
<< SolArduino`
(*directPowerPercent := Function[ (* convert power to a percent loss *)
  (1-directPower[#1,30,DateObject[{2016,6,20}]]/580)*100
 ]*)
solarPanelTilt[z_] := (
  If [z > 90]
   100,
   i = 1.35 * (1/1.35) ^ (Sec[z * Pi/180]);
   (1-i) * 100
(* DiscretePlot[directPower[x,30,DateObject[{2016,6,20}]],{x,1,20},ImageSize→Large] *)
ListLinePlot[{
  Table [100 * (1 - \cos[x * Pi / 180]), \{x, 0, 100\}],
  Table[solarPanelTilt[x], \{x, 0, 100\}], Filling \rightarrow Axis,
 PlotLegends → {"calculations", "simple cos", "solarpaneltilt.com"},
 ImageSize → Large, AxesLabel → {"Angle misalignment", "Percent of power loss"}
```

Infinity: Indeterminate expression 0.740741^{ComplexInfinity} encountered.

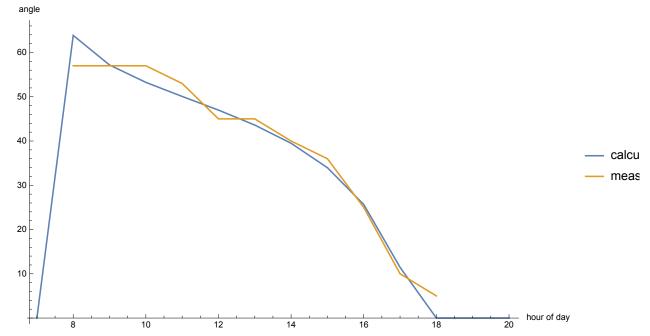


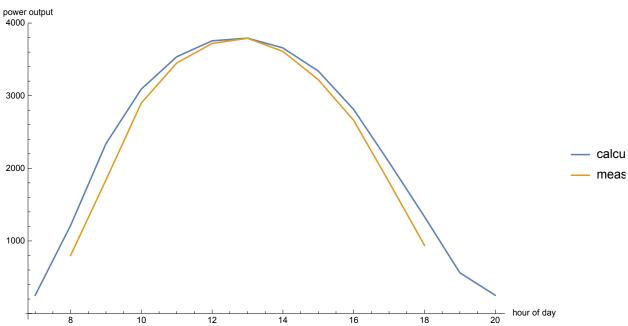
```
(* exporting *)
<< SolArduino`
? anglesPeriod
t = anglesPeriod[DateObject[{2016, 8, 21}], DateObject[{2016, 8, 23}]]
(* Convert all the DateObjects to YYYY-MM-DD *)
Do [
  t[[i, 1]] =
   DateString[t[[i, 1]], {"Year", "-", "Month", "-", "Day"}],
  {i, Length[t]}
 ];
(* Export the table to csv, format YYYY-MM-DD, angle *)
Export[NotebookDirectory[] <> "export.csv", t];
 anglesPeriod[begin date, end date] creates list of optimal angles per day over given interval
   Sun 21 Aug 2016 , 34.2879 ,
    iii Mon 22 Aug 2016 , 34.8863 , { iii Tue 23 Aug 2016 , 35.4718 } }
(* Plot measured data (angle, power output) each hour the sun is up to expected data *)
? dayAnglesHour
t = dayAnglesHour[DateObject[{2016, 8, 30}]]
(* 26/8 *)
measuredData2608 = {{Indeterminate, Indeterminate}, {700, 55}, {1390, 55},
   {2400, 55}, {3100, 55}, {3000, 55}, {3540, 48}, {Indeterminate, Indeterminate},
   {1900, 0}, {Indeterminate, 0}, {Indeterminate, Indeterminate},
   {Indeterminate, 0}, {Indeterminate, 0}, {Indeterminate, 0}};
measuredData3008 = {{Indeterminate, Indeterminate}, {800, 57}, {1840, 57}, {2900, 57},
  {3450, 53}, {3720, 45}, {3790, 45}, {3610, 40}, {3220, 36}, {2660, 25}, {1810, 10},
  {940, 5}, {Indeterminate, Indeterminate}, {Indeterminate, Indeterminate}}
hours = Table[
   х,
   \{x, 7, 20\}
  ];
ListLinePlot[{
  Transpose[{hours, t[[All, 2]]}],
  Transpose[{hours, measuredData3008[[All, 2]]}]
 },
 PlotLegends → {"calculated angle", "measured angle 26/8"},
 AxesLabel → {"hour of day", "angle"}
 , ImageSize → Large]
ListLinePlot[{
  Transpose [\{\text{hours}, t[[All, 1]] * 6.6\}],
  Transpose[{hours, measuredData3008[[All, 1]]}]
 PlotLegends → {"calculated power output (scaled down)", "measured power output 26/8"},
 AxesLabel → {"hour of day", "power output"}, ImageSize → Large
]
```

dayAnglesHour[date] returns a list of {power output, optimal angle} at each whole hour of the time the sun is up

```
... FindMaximum: Encountered a gradient that is effectively zero. The result returned may not be a maximum; it may be a
     minimum or a saddle point.
```

```
\{\{38.1281, 0.\}, \{183.787, 63.8613\}, \{354.526, 57.1733\},
 {468.432, 53.2523}, {535.804, 50.073}, {569.026, 46.9878}, {574.589, 43.6033},
 {554.207, 39.4922}, {505.901, 33.9698}, {425.702, 25.6649},
 \{315.711, 11.4608\}, \{202.144, 0.\}, \{85.0896, 0.\}, \{38.1843, 0.\}\}
{{Indeterminate, Indeterminate}, {800, 57}, {1840, 57}, {2900, 57}, {3450, 53},
 \{3720, 45\}, \{3790, 45\}, \{3610, 40\}, \{3220, 36\}, \{2660, 25\}, \{1810, 10\},
 {940, 5}, {Indeterminate, Indeterminate}, {Indeterminate, Indeterminate}}
```

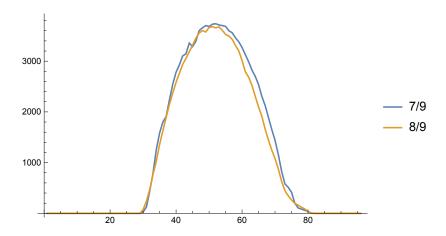




```
<< SolArduino`
(* change name of imported csv,
change dates in ListLinePlot to dates exisiting in data *)
data = Import[NotebookDirectory[] <> "data2 8.csv"];
data = Delete[data, 1];
?csvToList
ListLinePlot[
 {csvToList[DateObject[{2016, 9, 7, 0, 0}], data],
  csvToList[DateObject[\{2016, 9, 8, 0, 0\}], data]\}, PlotLegends \rightarrow \{"7/9", "8/9"\}
]
(*
ListLinePlot[
  f[DateObject[{2016,8,16,0,0}]],
  f[DateObject[{2016,8,17,0,0}]],
  f[DateObject[{2016,8,18,0,0}]],
  f[DateObject[{2016,8,19,0,0}]]
 },PlotLegends → {"24","24","40","5"}
]*)
(*ListLinePlot[
  f[DateObject[{2016,8,17,0,0}]],
  f[DateObject[{2016,8,22,0,0}]],
  f[DateObject[{2016,8,23,0,0}]],
 PlotLegends → {"17/8","22/8","23/8"}
(*Select[data,DateDifference[DateObject[ #[[1]]],{2016,8,18,0,0} ]≤ 0 &,1 ]*)
```

csvToList[date,data] returns list of values for that date that exist in data

- DateString: Warning: the interpretation of the string 09/02/2016 00:00 as a date is ambiguous.
- DateObject: Warning: the interpretation of the string 09-02-2016 00:00 as a date is ambiguous.
- DateString: Warning: the interpretation of the string 09/02/2016 00:15 as a date is ambiguous.
- DateObject: Warning: the interpretation of the string 09–02–2016 00:15 as a date is ambiguous.
- DateString: Warning: the interpretation of the string 09/02/2016 00:30 as a date is ambiguous.
- General: Further output of DateString::ambig will be suppressed during this calculation.
- DateObject: Warning: the interpretation of the string 09-02-2016 00:30 as a date is ambiguous.
- General: Further output of DateObject::ambig will be suppressed during this calculation.



(* to export angles and times *) << SolArduino` exportPeriod[DateObject[{2016, 10, 29}], DateObject[{2016, 11, 1}], 10] 40