

§ SAS : homework 10 :

一. Effect-measure modification :

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(一) Result :

1. RR difference : - 0.0336
2. RR ratio = 0.975

(二) Figure :

Statistics for Table 1 of sex by caco Controlling for apo4car=0				Statistics for Table 2 of sex by caco Controlling for apo4car=1			
Odds Ratio and Relative Risks				Odds Ratio and Relative Risks			
Statistic	Value	95% Confidence Limits		Statistic	Value	95% Confidence Limits	
Odds Ratio	1.3265	0.8888	1.9796	Odds Ratio	1.2929	0.6644	2.5159
Relative Risk (Column 1)	1.2145	0.9206	1.6023	Relative Risk (Column 1)	1.1055	0.8475	1.4420
Relative Risk (Column 2)	0.9156	0.8087	1.0366	Relative Risk (Column 2)	0.8550	0.5724	1.2770

  

rr_nonAPOEe4	rr_APOEe4	rr_diff
1.3265	1.2929	-0.0336

  

rr_nonAPOEe4	rr_APOEe4	rr_ratio
1.3265	1.2929	0.9746702

  

Breslow-Day Test for Homogeneity of Odds Ratios	
Chi-Square	0.0042
DF	1
Pr > ChiSq	0.9485

(三) Descriptions :

Strata1 : non-APOE e4 carrier			Strata 2 : APOE e4 carrier		
	Case	Control		Case	Control
women	n00 = 84	n10 = 161	women	N00 = 64	N10 = 36
Men	n01 = 59	n11 = 150	Men	N01 = 33	N11 = 24
OR(n)	$OR = \frac{(n00 \times n11)}{(n10 \times n01)}$		OR(N)	$OR = \frac{(N00 \times N11)}{(N10 \times N01)}$	
OR difference = OR(n) – OR(N)					

1. 以 APOE e4 status 分層，觀察兩層中 gender 與 AD 的關係。定義 women 為 exposure，men 為 non-exposure；發生 AD 為 disease。
2. 以上述公式計算兩層的 OR。在 non-carrier 層的 OR 為 1.3265（95% CI：0.8888 – 1.9796）；在 carrier 層的 OR 為 1.2929（95% CI：0.6644 – 2.5159）
3. 在抽樣與暴露與否相互獨立的前提下，可以 OR 推論 RR。
4. 計算兩層 RR difference，將 non-carrier 層與 carrier 相減，得 RR difference = - 0.0336。以 RR difference 判斷兩層的 RR 相差不大（接近 1），APOE e4 status

應不造成 effect-measure modification。

5. 計算兩層 RR ratio，將 non-carrier 層與 carrier 相除，得 RR ratio = 0.9746702。兩層的 RR 相差不大，APOE e4 status 應不造成 effect-measure modification。
6. 以 Breslow-Day test 檢定兩層之 OR 是否相等，檢定結果 p-value 為 0.9485，無法拒絕虛無假說，兩層 OR 無顯著不同。表示 APOE e4 status 與 gender 較不可能有交互作用。

Code：

```
/* homework 10 */
dm "odsresult" clear;
dm "log" clear;
/* import data of sasdataset*/
libname data "\\Mac\Home\Desktop";

/* q1 : effect-measure modification , E1 ( women), DZ( AD) , stratified by APOE
status*/
title "q1";
data ad;
set data.ad_dataset_new;
run;
/* Risk difference */
proc sort data = ad;
by apo4car sex descending caco;
run;

proc freq data = ad order = data;
tables apo4car * sex * caco / or nocol nopercent cmh;
run;

proc iml;
rr_nonAPOEe4 = 1.3265;
rr_APOEe4 = 1.2929;
rr_diff = rr_APOEe4 - rr_nonAPOEe4;

print rr_nonAPOEe4 rr_APOEe4 rr_diff;
run;
/* Rate difference */
proc iml;
rr_nonAPOEe4 = 1.3265;
rr_APOEe4 = 1.2929;
rr_ratio = rr_APOEe4 / rr_nonAPOEe4;

print rr_nonAPOEe4 rr_APOEe4 rr_ratio;
quit;
```

## 二. Statistical interaction (adjusted for age , years of education)

### (一) RR of gender and APOE e4 status and both

#### 1. Result :

- (1) RR of APOE e4 status alone : 3.495 ( 95% CI : 1.907 – 6.406 )
- (2) RR of gender alone : 1.326 ( 95% CI : 0.889 – 1.979 )
- (3) RR of both APOE e4 status and gender : 4.518 ( 95% CI : 2.720 – 7.504 )

#### 2. Figure :

Odds Ratio Estimates			
Effect	Point Estimate	95% Wald Confidence Limits	
group A vs U	1.326	0.889	1.979
group AB vs U	4.518	2.720	7.504
group B vs U	3.495	1.907	6.406

#### 3. Descriptions :

	Men ( A' )	Women ( A )
Non APOE e4 carrier ( B' )	RR <sub>U</sub>	RR <sub>A</sub>
APOE e4 carrier ( B )	RR <sub>B</sub>	RR <sub>AB</sub>

- (1)  $RR_A / RR_U = 1.326$  , 單純 gender 這個變項的 RR 為 1.326 。
- (2)  $RR_B / RR_U = 3.495$  , 單純 APOE status 的 RR 為 3.495 。
- (3) 若不存在統計上的交互作用, 則  $RR_{AB}$  應為  $RR_A \times RR_B = 4.634$  。而  $RR_{AB} = 4.518$  。兩者差異不大, 叫不可能有統計上的交互作用

### (二) Create a product interaction term (apo4car \* sex) and run a logistic regression model :

#### 1. Figures :

Analysis of Maximum Likelihood Estimates					
Parameter	DF	Estimate	Standard Error	Wald Chi-Square	Pr > ChiSq
Intercept	1	-0.6506	0.1346	23.3639	<.0001
apo4car	1	1.2259	0.2480	24.4274	<.0001
sex	1	-0.2823	0.2043	1.9093	0.1670
apo4car*sex	1	0.0254	0.3964	0.0041	0.9489

Analysis of Maximum Likelihood Estimates						
Parameter		DF	Estimate	Standard Error	Wald Chi-Square	Pr > ChiSq
Intercept		1	-11.8578	1.5004	62.4590	<.0001
apo4car	1	1	1.6761	0.3926	18.2293	<.0001
sex	0	1	0.0938	0.2698	0.1209	0.7281
apo4car*sex	1 0	1	-0.2464	0.5000	0.2428	0.6222
age		1	0.1725	0.0190	82.8772	<.0001

#### 2. Descriptions :

- (1) 在加入 age, education year 這兩個變項前，apo4car \* sex 這個 interaction term 的 p-value 為 0.9489，未達統計上顯著。
- (2) 加入 age, education year 這兩個變項後，這個 interaction term 的 p-value 為 0.6222，依然未達統計上的顯著。
- (3) 表示 APOE e4 status 與 sex 沒有統計上的交互作用。

(三) Code :

```
/* q2 : statistical interaction, Logistic regression */
title "q2";
data q2;
  set ad;
  if apo4car = 1 and sex = 0 then group = "AB";
  else if apo4car = 1 and sex = 1 then group = "B";
  else if apo4car = 0 and sex = 0 then group = "A" ;
  else if apo4car = 0 and sex = 1 then group = "U";
run;
proc print data = q2;
  var apo4car sex group;
run;

proc logistic data = q2;
  class group (ref = "U") / param = ref;
  model caco (event = "1") = group;
run;

proc iml;
  rr_a = 1.326;
  rr_b = 3.495;
  rr_ab = 4.518;
  diff = rr_ab - (rr_a * rr_b);
  percent_diff = abs(diff) / rr_ab;

  print rr_a rr_b rr_ab diff percent_diff;
quit;

/* unadjusted model */
proc logistic data = q2;
  class group (ref = "U") / param = ref;
  model caco ( event = "1") = apo4car sex apo4car * sex;
run;

/* adjusted model */
proc logistic data = q2;
  class apo4car (ref = "0") sex ( ref = "1") / param = ref;
  model caco (event = "1") = apo4car sex apo4car * sex age eduyr;
run;

proc logistic data = q2;
  class apo4car (ref = "0") sex ( ref = "1") / param = glm;
  model caco (event = "1") = apo4car sex apo4car * sex;
  lsmeans apo4car * sex / diff oddsratio;
run;
```

### 三. Biological interaction

(一)  $((RR_{AB} - 1) - (RR_A - 1) - (RR_B - 1) \neq 0$

1. Result :

$$(1) (RR_{AB} - 1) - (RR_A - 1) - (RR_B - 1) = 0.697$$

$$(2) \frac{(RR_{AB}-1)-(RR_A-1)-(RR_B-1)}{RR_{AB}} = 15.43\%$$

2. Figure :

rr_a	rr_b	rr_ab	diff	percent_diff
1.326	3.495	4.518	0.697	0.1542718

3. Descriptions :

	Men ( A' )	Women ( A )
Non APOE e4 carrier ( B' )	RR <sub>U</sub> = 1	RR <sub>A</sub> = 1.326
APOE e4 carrier ( B )	RR <sub>B</sub> = 3.495	RR <sub>AB</sub> = 4.518

(1) 若 biological interaction 不存在，則  $(RR_{AB} - 1) - (RR_A - 1) - (RR_B - 1) = 0$

(2) 本題上式相減為 0.697，佔 RR<sub>AB</sub> 的 15.43%。代表有 15.43% 的 case 是因為生物交互作用而產生。

(二) Statistical interaction  $\leftrightarrow$  biological interaction :

1. 若沒有 statistical interaction，則 RR<sub>AB</sub> 應為 4.634。
2. 若沒有 biological interaction，則 RR<sub>AB</sub> 應為 3.785。
3. 3.785 ( no biological interaction ) < 4.515 ( observed ) < 4.634 ( no statistical interaction )，代表生物交互作用與統計交互作用的影響方向是反向的。
4. 首先，是否具有生物交互作用，取決於其生理機轉及生物的本質。在本題中，APOE status 與性別之間的交互作用不一定單純地符合相加效應，而可能有更複雜的機轉。是故本題計算生物交互用的方向及大小，不一定可真實反應其兩變項生理機轉的本質。
5. 此外，統計的交互作用是否存在取決於模型的選擇，本題之模型為羅吉斯回歸，兩變項是否具有統計交互作用視其是否偏離相乘效應而定。受限於資料樣態和格式，羅吉斯回歸或為本題最適合的模型，然而此模型不一定可真實反應兩變項與 AD 的關係。

(三) Code :

```
/* q3 : biological interaction */
title "q3" ;
proc iml;
  rr_a = 1.326;
  rr_b = 3.495;
```

```
rr_ab = 4.518;
diff = (rr_ab - 1) - ((rr_a - 1) + (rr_b - 1));
percent_diff = abs(diff) / rr_ab;

print rr_a rr_b rr_ab diff percent_diff;
quit;
```