

# CS350-HW5- Fall 2020

easyabi

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## 1 Question 1

### 1.1 a:

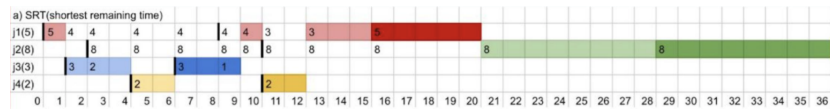


Figure 1: SRT

### 1.2 b:

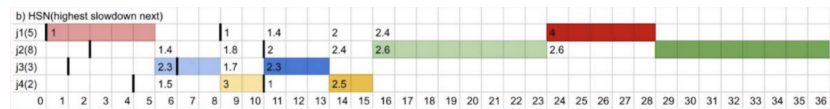


Figure 2: HSN

### 1.3 c:

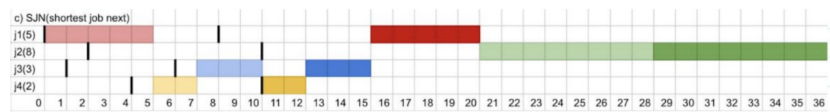


Figure 3: SJN

### 1.4 d:



### 2.3 c:

$$S = \frac{(15 - 8.9)^2 + \dots + (-8.9)^2}{30 - 1} = 3.03$$

$$E = Z_{\frac{\alpha}{2}} \times \frac{S}{\sqrt{N}}$$

$$1.5 = Z_{\frac{\alpha}{2}} = 2.709$$

using the table:

$$Z_{\frac{\alpha}{2}} = 0.99664 = 1 - \frac{\alpha}{2} \longrightarrow \alpha = 0.993$$

### 2.4 d:

We know  $q$  in M/M/1 system depends on the arrival rate and service rate. Here arrival rate is known. Therefore, Error in  $q$  is determined by error in service time

$$\alpha = 1 - 0.99 = 0.01 \longrightarrow 1 - \alpha/2 = 0.995$$

using Z table, we have :

$$Z_{\frac{\alpha}{2}} = 2.58$$

$$E = Z_{\frac{\alpha}{2}} \times \frac{\alpha}{\sqrt{N}} = 2.58 * \frac{\sqrt{9.196}}{\sqrt{30}} = 1.428$$

Thus, the Ts interval is:

$$[7.47, 10.32]$$

We know that:

$$q = \frac{\lambda Ts}{1 - \lambda Ts}$$

$$q' = \frac{0.0907 \times 10.32}{1 - 0.09 \times 10.32} = 14.8$$

Therefore, the confidence interval is :

$$[2.1, 14.8711]$$

### 2.5 e:

Lets first find  $n$ , the number of samples we need to reach the desired confidence interval:

$$n = \left( \frac{Z_{\frac{\alpha}{2}}}{E} \right)^2$$

$$\alpha = 1 - 0.9996 \longrightarrow 1 - \alpha/2 = 0.9998$$

Using Z table:

$$Z \frac{\alpha}{2} = 3.54$$

$$n = \left( \frac{3.54 \times 3.032}{1} \right)^2 = 116$$

And finally the amount needed to observe the system to get 116 samples is as follows :

$$n/\lambda = 116/90.72 = 1.279 \text{seconds}$$

## 2.6 f

We quantify correlation for different values of d

d=4 yields to the highest possible correlation. The correlation for d=4 is -0.548. Therefore, there is pattern and its periodicity equal to 4

## 3 Question 3

### 3.1 a

Job parameters:

$j_i$	$a_i$	$C_i$
$j_{1.1}$	0	3
$j_{2.1}$	1	5
$j_{3.1}$	3	2
$j_{4.1}$	5	6
$j_{5.1}$	7	2
$j_{1.2}$	10	1
$j_{3.2}$	11	4

Figure 5:

### 3.2 b

SRT

### 3.3 c

At this time a new job of j3 arrives with remaining execution time of 4. Therefore, the scheduler has to make a decision choosing the next job to execute. Since j2's job has a lower remaining time, the scheduler chooses to schedule j2's job.

### 3.4 d



Figure 6: HSN

### 3.5 e

Yes, consider two jobs  $j_1$  and  $j_2$ .  $j_1$  has execution time of 1000000 and arrives at time 0 and  $j_2$  has a execution time of 2 and arrives at time 1. The scheduler at time 0 has no choice but choosing job  $j_1$ . Hence, the slowdown down of  $j_2$  which is a short job is notably high and therefore not fair.