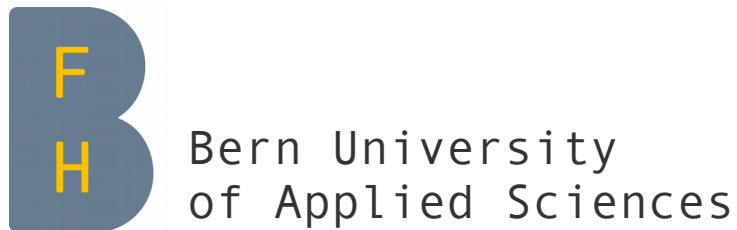


# Mastering Machine Learning for spatial prediction I

**GEOSTAT 2017**  
**Thursday 11-12:30**



**Madlene Nussbaum**

# Objectives ...

- Get an **overview**, understand ML techniques
- Get to know quite different approaches in detail
- Move away from **ML = black box**
- Get to know how to compute and evaluate **uncertainty**
- **Be critical!**

**Be able to judge if computing  
model averaging on 78 methods  
found in Package caret is a sensible  
thing to do ...**

# Overview

## Spatial modelling

- define requirements
- get overview

## Get to know ..

- Lasso
- Gradient boosting
- Model averaging

## Exercises

# Literature

## Books:

Very good and detailed book on ML, although quite complex:

**Hastie**, T., Tibshirani, R., and Friedman, J.: The Elements of Statistical Learning; Data Mining, Inference and Prediction, Springer, New York, 2 edn., 2009. with examples and data in R package ElemStatLearn, <https://cran.r-project.org/web/packages/ElemStatLearn/index.html>

Extended book on bootstrapping:

**Davison**, A. C. and Hinkley, D. V.: Bootstrap Methods and Their Applications, Cambridge University Press, Cambridge, doi:10.1017/cbo9780511802843, 1997.

Very good book on categorical responses, mostly parametric methods, some ML described, comes with R package:

**Tutz**, G.: Regression for Categorical Data, Cambridge University Press, doi:10.1017/cbo9780511842061, 2012.

Useful book for validation measures including for uncertainty, see chapter 8 and R package “verification”:

**Wilks**, D. S.: Statistical Methods in the Atmospheric Sciences, Academic Press, 3 edn., 2011.

## Some articles the slides are referring to:

Behrens, T., Schmidt, K., Ramirez-Lopez, L., Gallant, J., Zhu, A.-X., and Scholten, T.: Hyper-scale digital soil mapping and soil formation analysis, Geoderma, 213, 578–588, doi:10.1016/j.geoderma.2013.07.031, 2014.

Brungard, C. W., Boettinger, J. L., Duniway, M. C., Wills, S. A., and Edwards Jr., T. C.:

Machine learning for predicting soil classes in three semi-arid landscapes, Geoderma, 239–240, 68–83, doi:10.1016/j.geoderma.2014.09.019, 2015.

Hothorn, T., Müller, J., Schröder, B., Kneib, T., and Brandl, R.: Decomposing environmental, spatial, and spatiotemporal components of species distributions, Ecological Monographs, 81, 329–347, 2011.

Nussbaum, M., Spiess, K., Baltensweiler, A., Grob, U., Keller, A., Greiner, L., Schaepman, M., and Papritz: Evaluation of digital soil mapping approaches with large sets of environmental covariates, SOIL Discussions, 2017, 1–32, doi:10.5194/soil-2017-14, URL <http://www.soil-discuss.net/soil-2017-14/>, in review, 2017a.

Nussbaum, M., Walthert, L., Fraefel, M., Greiner, L., and Papritz, A.: Mapping of soil properties at high resolution in Switzerland using boosted geosadditive models, SOIL Discussions, 2017, 1–32, doi:10.5194/soil-2017-13, URL <http://www.soil-discuss.net/soil-2017-13/>, in review, 2017b.

# Spatial predictions ...

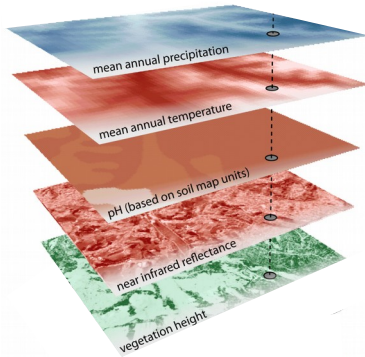
For example:  
**Digital soil mapping**



texture  
density  
gravel  
soil depth  
drainage  
pH, ECEC  
SOC

**300-1400**  
locations with  
soil properties in

**2-4** soil depth  
**3** study areas



**300-500**  
environmental  
covariates



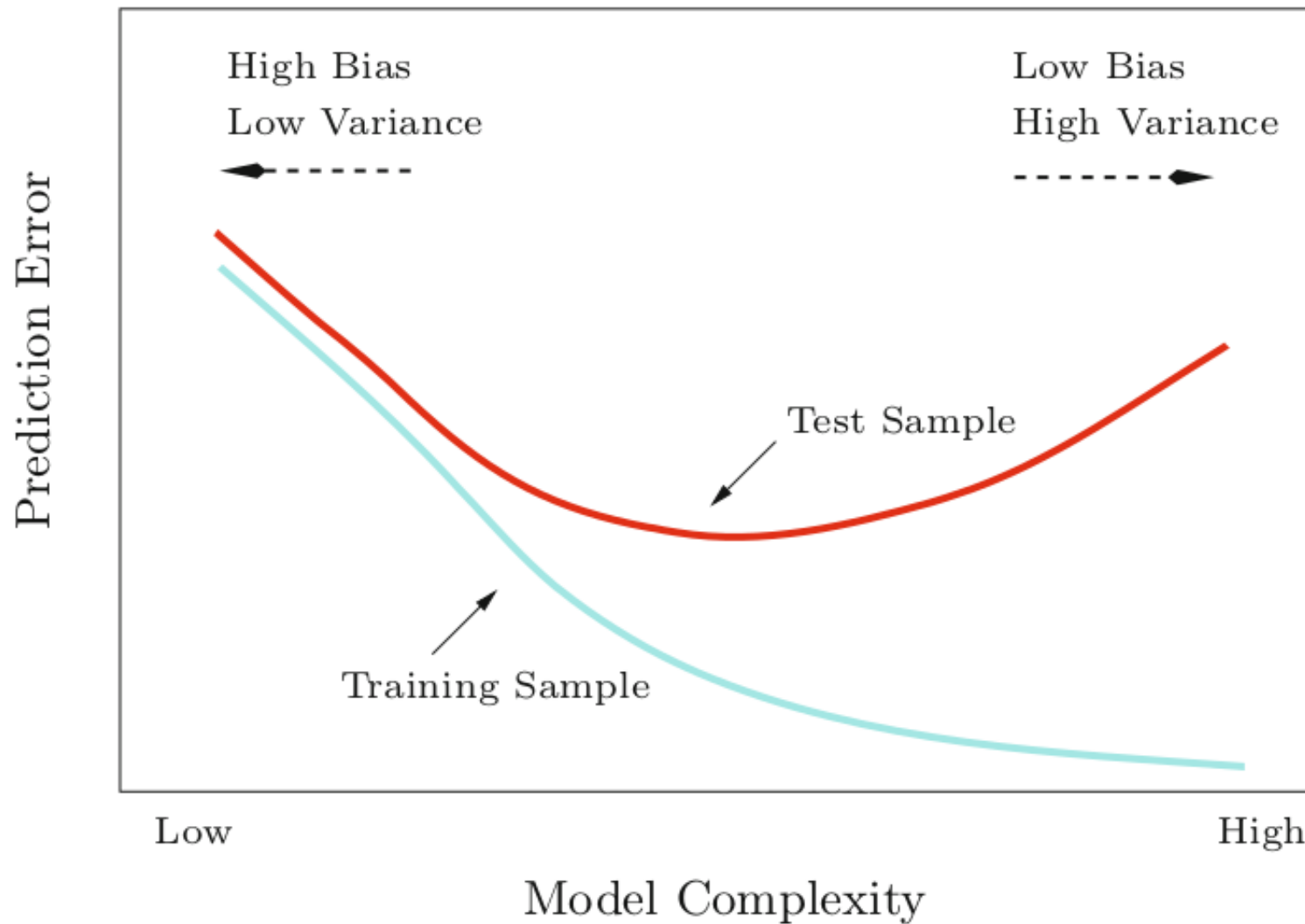
**48**  
statistical models

## Requirements

A spatial prediction method should ...

- model **nonlinear** relations
- consider **spatial** autocorrelation
- model continuous and categorical responses
- handle **numerous** correlated **covariates** without overfitting calibration data
- **automatically** build models with **good predictive power**
- preferably result in **sparse model**
- accurately quantify **accuracy** of **predictions**
- give prediction **uncertainty**

# Bias-Variance tradeoff

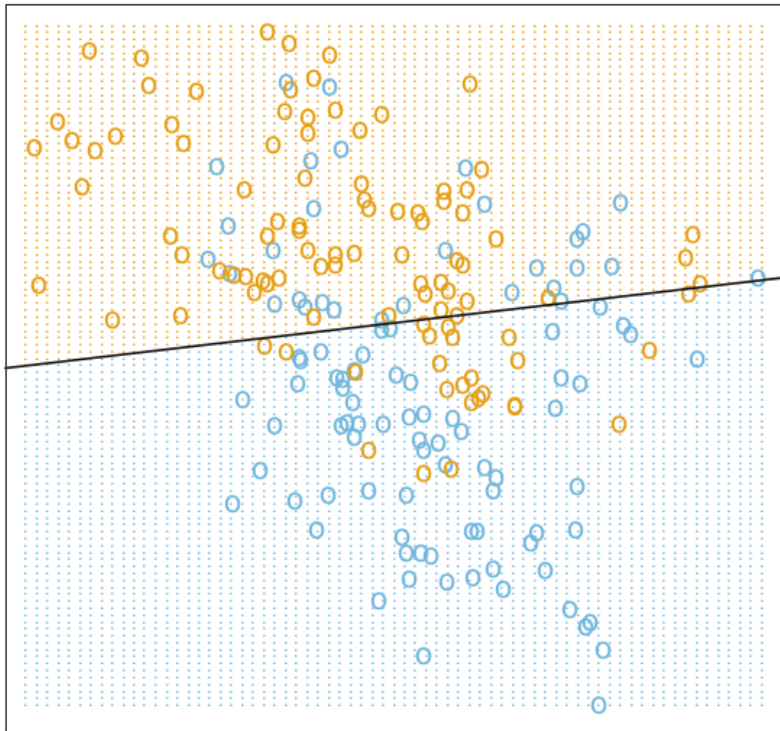


**FIGURE 2.11.** *Test and training error as a function of model complexity.*

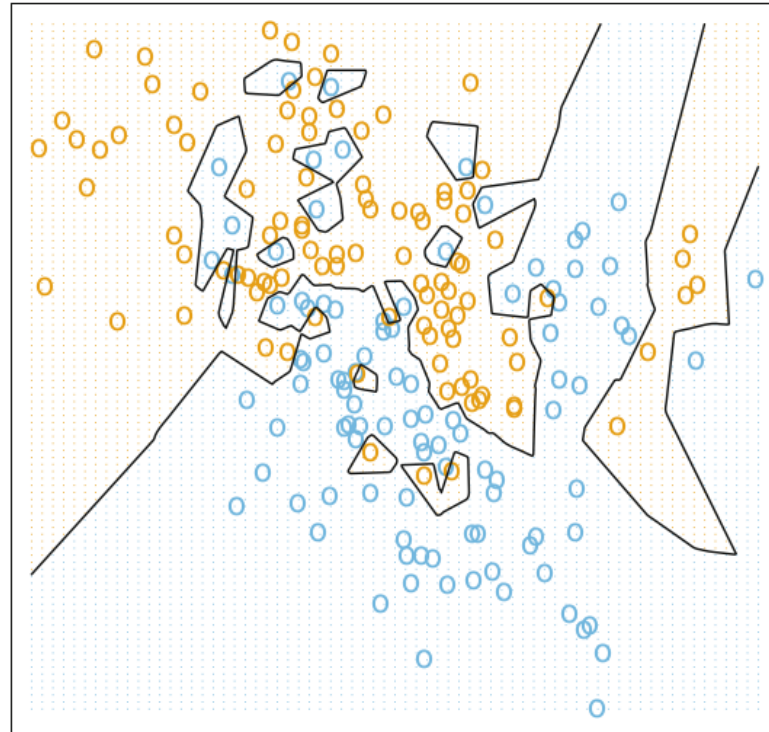
Hastie et al. 2009, p. 38.

# Bias-Variance tradeoff

Linear Regression of 0/1 Response



1-Nearest Neighbor Classifier



Hastie et al. 2009, Chap. 2.3.

## Linear model

high bias, but stable

## 1-nearest neighbours

low bias, high variance

$$\mathbb{E}[(y - \hat{f}(x))^2] = \text{Bias}[\hat{f}(x)]^2 + \text{Var}[\hat{f}(x)] + \sigma^2$$

**Bias:** erroneous assumptions in the model, miss relevant relationship (underfitting).

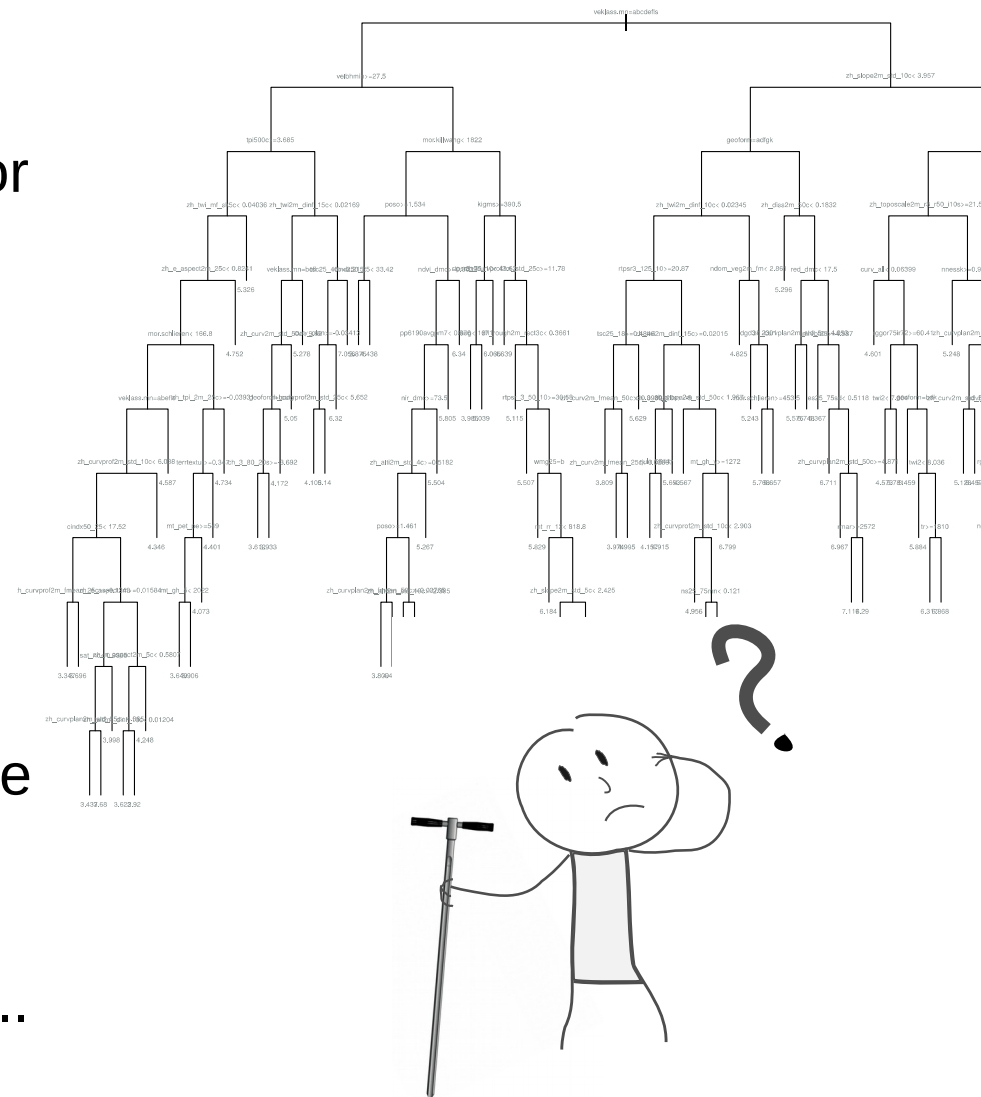
**Variance:** sensitivity to small fluctuations in the calibration data, algorithm models random noise in calibration data, instead of just relevant relationship (overfitting).

# Is there a reason for model selection? Or is it enough to do model building?

**Model selection** = reduce the initial covariate set

**Model building** = find relationships between covariates and response

- ✓ Model interpretation
- ✓ Better just use relevant covariates for prediction
- ✓ Computational effort for predictions (just prepare 12 instead of 300 rasters)
- ✓ Maybe reduce effort for future data collection and modelling on same topic
- ✗ However, theoretical statisticians do not recommend selection, because it is often biased, difficult to find the true model..
- ✗ We might lose prediction accuracy...





# I tried to tidy up ...

- linear regression
- geostatistical methods  
external-drift kriging, regression kriging
- additive models (GAM)
- machine learning  
classification and regression trees (CART),  
support vector machines, neural nets
- ensemble machine learners  
random forest, boosted regression trees
- model averaging

**parametric** (rely on distribution assumptions), solve some likelihood function.

Drawback: transformations, extrapolation, lack of stability with collinear covariates, with many covariates → **how to select trend?** No fit for  $n > p$ .

**based on algorithms**, stepwise procedure to build up model.

For (spatial) prediction:  
**supervised learning**

response ← model trained on covariates

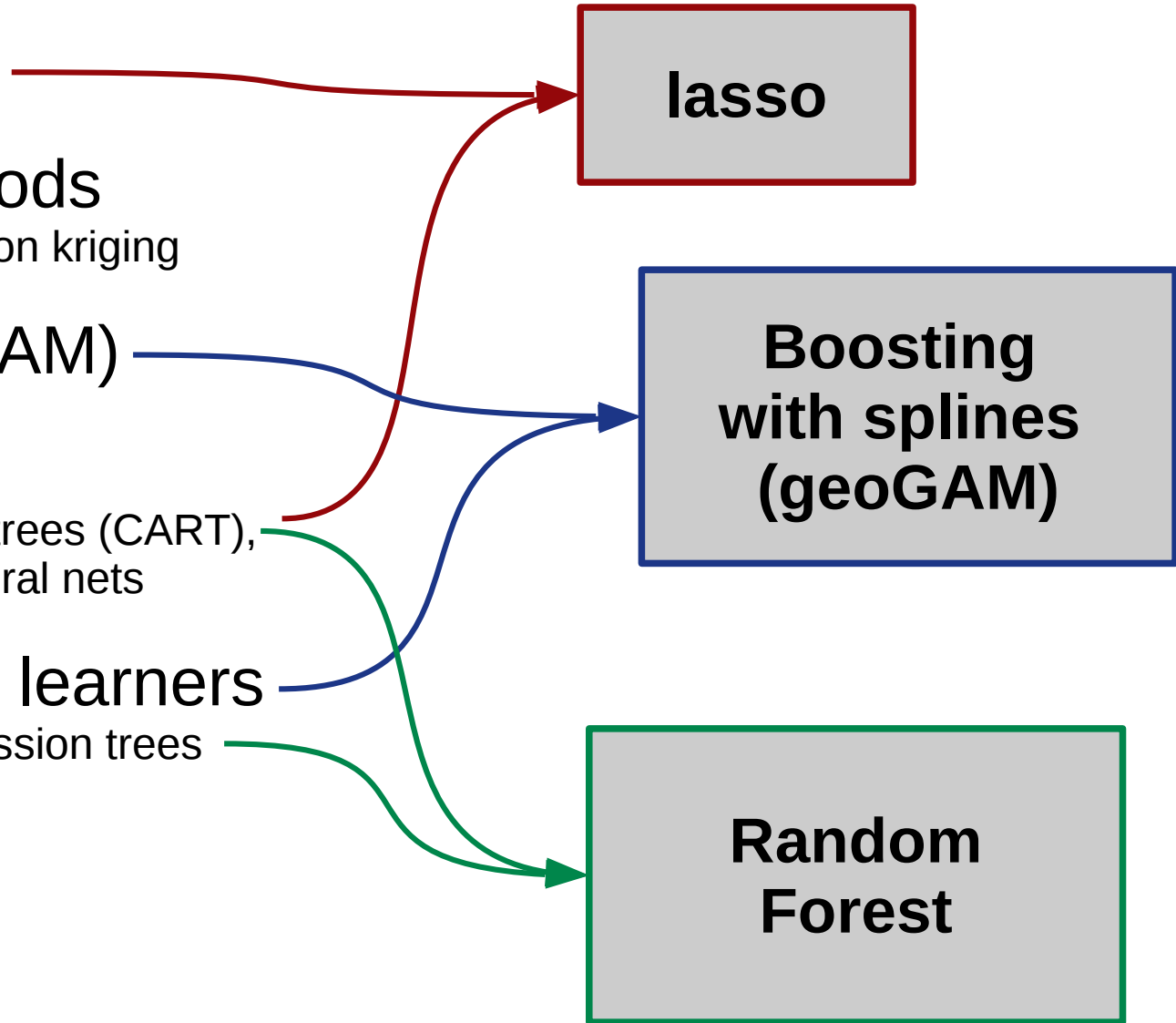
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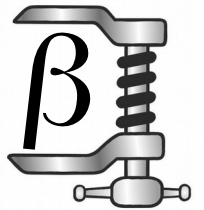
**lasso**

**Boosting  
with splines  
(geoGAM)**

**Random  
Forest**



# Lasso: ML for linear models

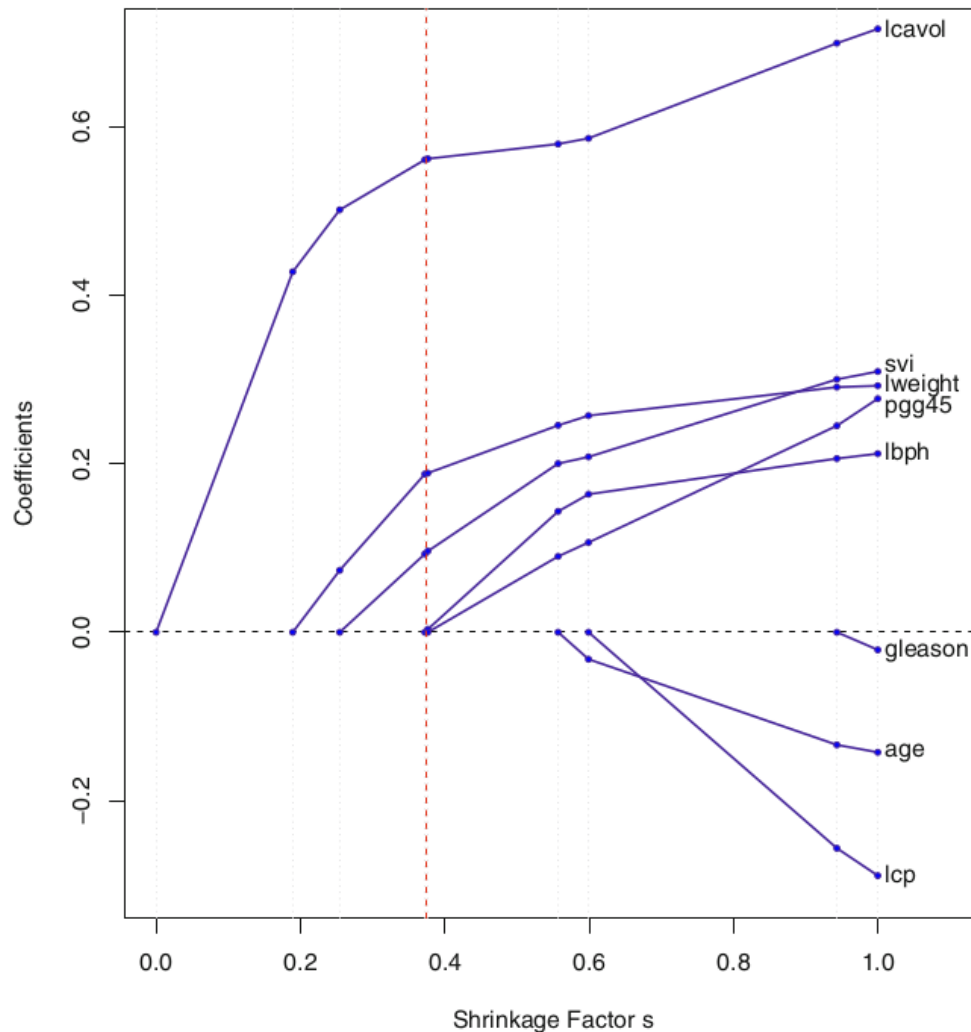
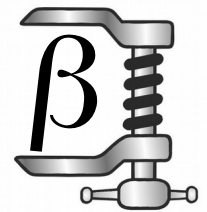


- Select linear regression with stepwise forward/backward, best subset: Most often does not find true model, does overfit, selection is binary – either in or out
- **Shrinkage:** include a covariate, but with smaller / downweighted coefficients
- Different approaches (ridge regression etc.), most promising: Lasso: least absolute shrinkage and selection operator

$$\hat{\beta}^{\text{lasso}} = \underset{\beta}{\operatorname{argmin}} \left\{ \underbrace{\frac{1}{2} \sum_{i=1}^N \left( y_i - \beta_0 - \sum_{j=1}^p x_{ij} \beta_j \right)^2}_{\text{OLS}} + \underbrace{\lambda \sum_{j=1}^p |\beta_j|}_{\text{Lasso penalty}} \right\}.$$

- Thus the lasso does a kind of continuous subset selection.
- Tuning Parameter  $\lambda$ , find by cross validation

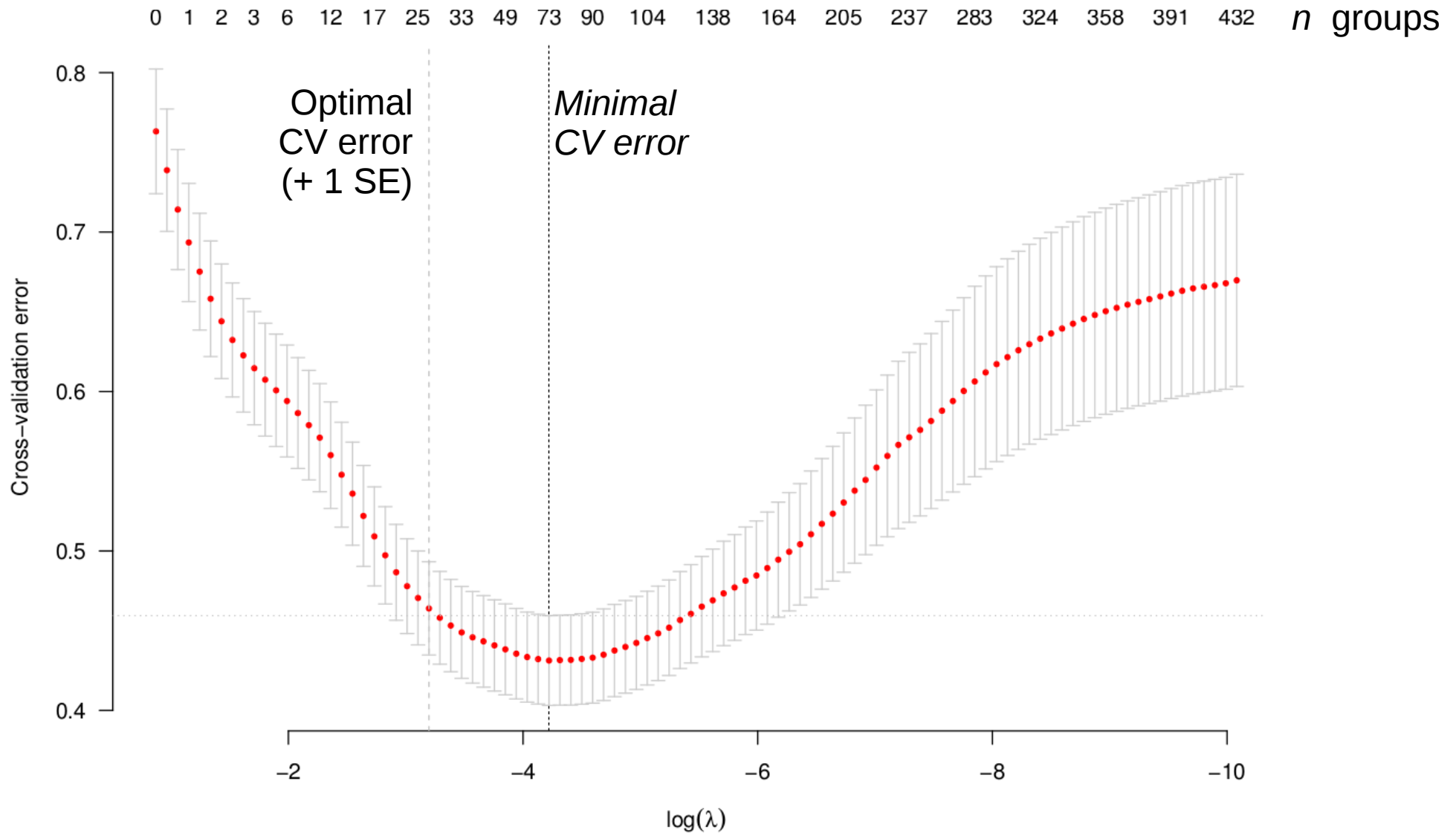
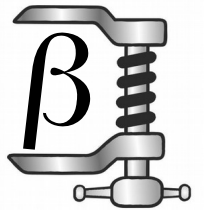
# Lasso: ML for linear models



Path of coefficients for increasing tuning parameter

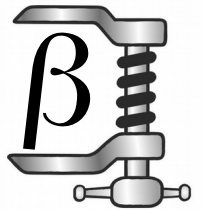
**FIGURE 3.10.** Profiles of lasso coefficients, as the tuning parameter  $t$  is varied. Coefficients are plotted versus  $s = t / \sum_1^p |\hat{\beta}_j|$ . A vertical line is drawn at  $s = 0.36$ , the value chosen by cross-validation. Compare Figure 3.8 on page 65; the lasso profiles hit zero, while those for ridge do not. The profiles are piece-wise linear, and so are computed only at the points displayed; see Section 3.4.4 for details.

# Lasso: ML for linear models



Berne data set, subspoil pH, >400 partly highly correlated and noisy covariates

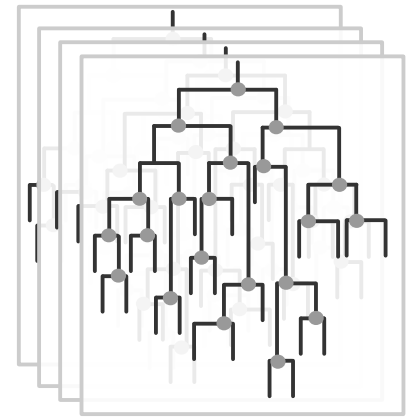
# Lasso: ML for linear models



- ✓ Very fast
- ✓ Selects covariates
- ✓ No problems with collinearity
- ✓ Easy interpretation (linear relationships)
- ✓ Linear regression with a lot of covariates, even  $n \gg p$
- ✗ Linear only, no interactions if not added explicitly  
(if  $n \gg p$  becomes nonlinear again)
- ✗ Take care, not always stable
- ✗ Rather underfitting  
(possible solution: relaxed Lasso with a second fit on non-zero covariates only)
- ✗ Standard errors not defined, prediction uncertainty only with bootstrap
- ✗ No direct spatial modelling, only via workaround

# Ensemble Machine Learners

- Combine predictions of several learners (any method)
- Meaningful for low-bias, high-variance procedures



## Strategies:

- Bagging = *bootstrap aggregation*.

Uniform *resampling* the data with replacement (no change of response distribution), fit the data to each resampled set, prediction = average of all single predictions

## **Random forest = bagged trees?**

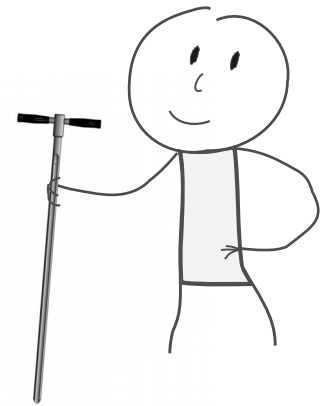
- Gradient boosting

Adaptive updating strategy, shrunken stepwise forward selection, fits on residuals → change of distribution

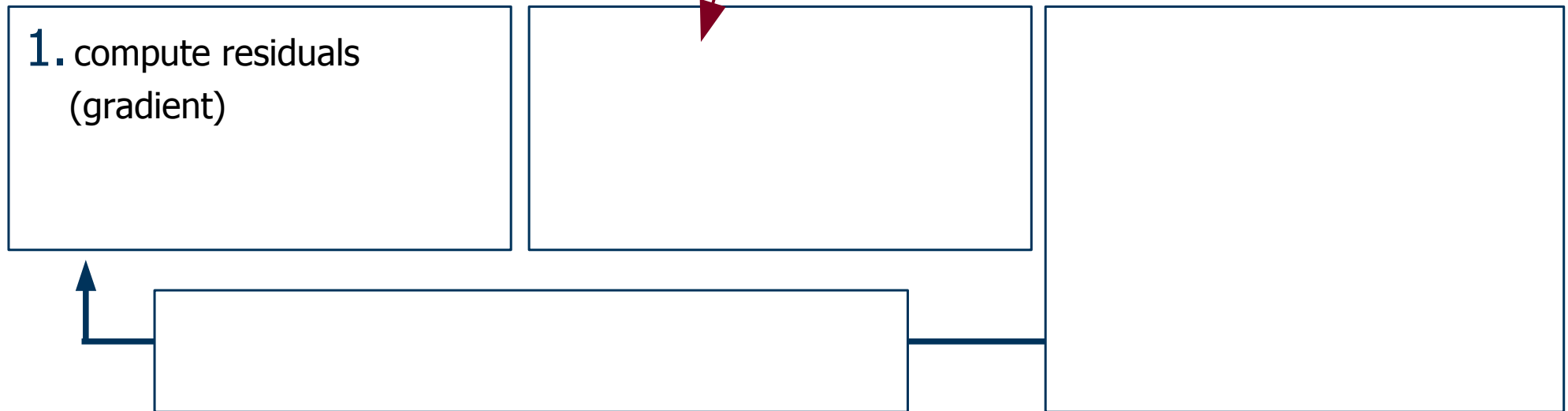
- Model averaging

Fits on the same response by different methods

# Gradient boosting: Algorithm



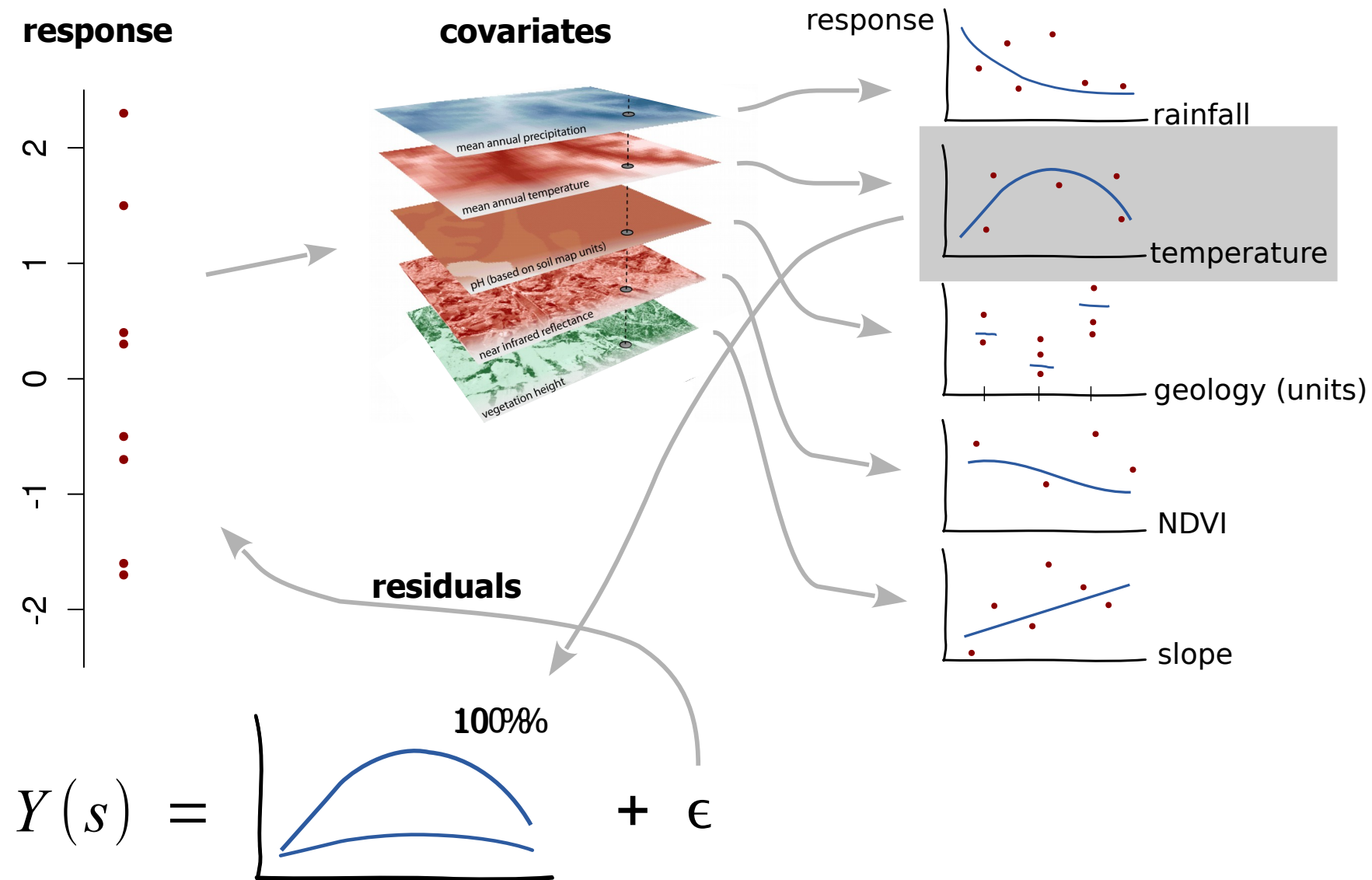
model selection for  
high-dimensional regression



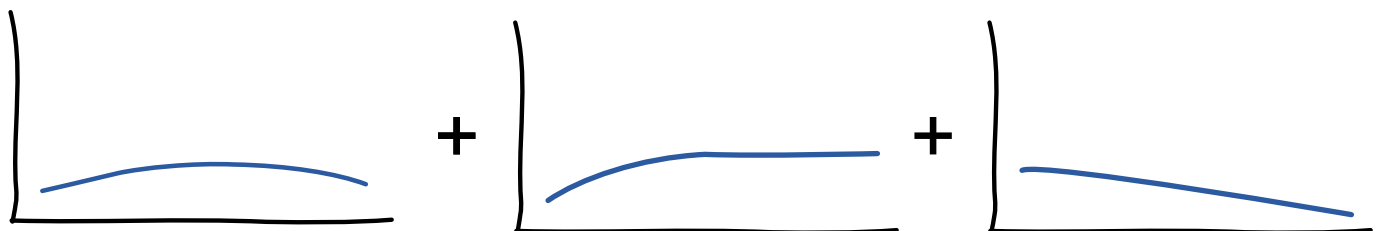
small step size  $v$   
= "weak" learner  
(again shrinkage!)



# Gradient boosting: mini example

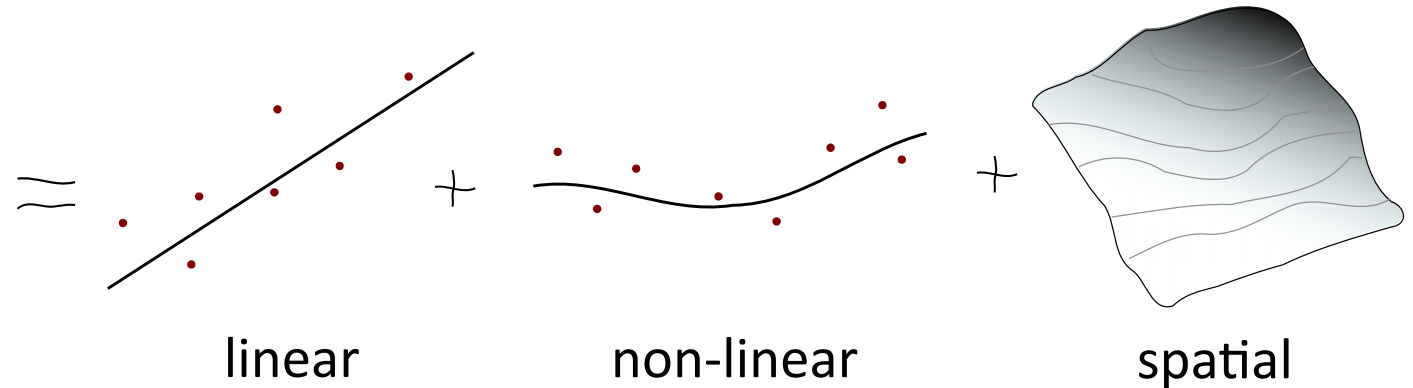


# Gradient boosting: mini example

$$Y(s) = \text{[Graph 1]} + \text{[Graph 2]} + \text{[Graph 3]} + \dots$$


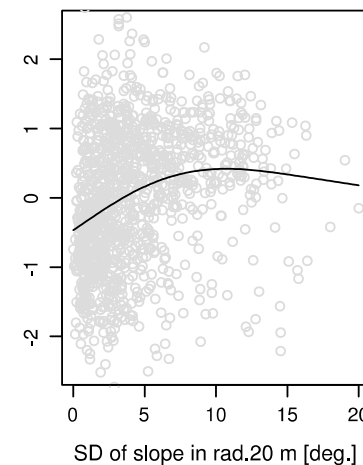
The image illustrates the concept of gradient boosting by showing the function  $Y(s)$  as a sum of multiple weak models. Each weak model is represented by a hand-drawn graph on a coordinate system. The first graph shows a blue curve that starts low, rises to a peak, and then falls. The second graph shows a blue curve that starts low, rises to a plateau, and then remains flat. The third graph shows a blue curve that starts at a medium height and gradually decreases to a low height. The graphs are separated by plus signs, indicating that they are added together to form the final function  $Y(s)$ .

# Gradient boosting: linear, splines and spatial baselearners



$$Y(s) = f_{env}(X) + f_s(s) + f_{ns}(X, s) \dots + \epsilon$$

see e.g. Hothorn et al. 2011



partial residuals

# Gradient boosting: Spatial modelling with splines

Spatial autocorrelation can be modelled by including a „smooth spatial surface“ as baselearner, non-stationary effects by creating interactions with the spatial surface

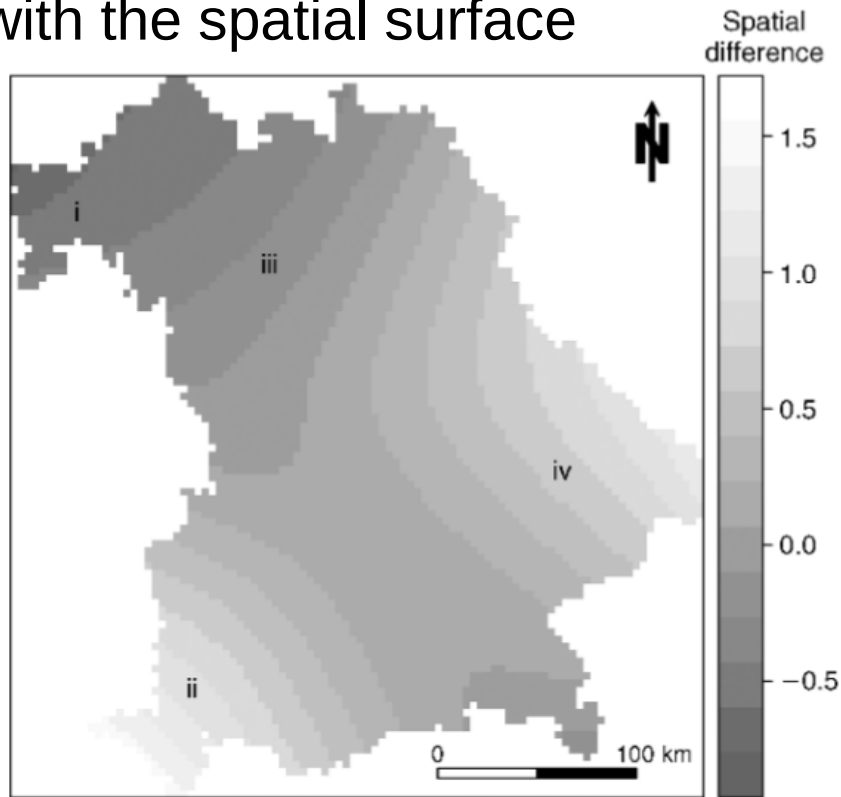


FIG. 6. Spatial difference in Red Kite breeding between 1979–1983 and 1996–1999 for model (add/vary). The breeding probabilities in the northwestern part decreased, while the southwestern part goes with increased breeding probabilities. For the four selected areas [(i) Unterfranken, (ii) Schwaben, (iii) Mittelfranken, and (iv) Niederbayern], the variability of the estimated spatial difference is shown in Fig. 7. Spatial differences can be interpreted as difference in log-odds ratios.

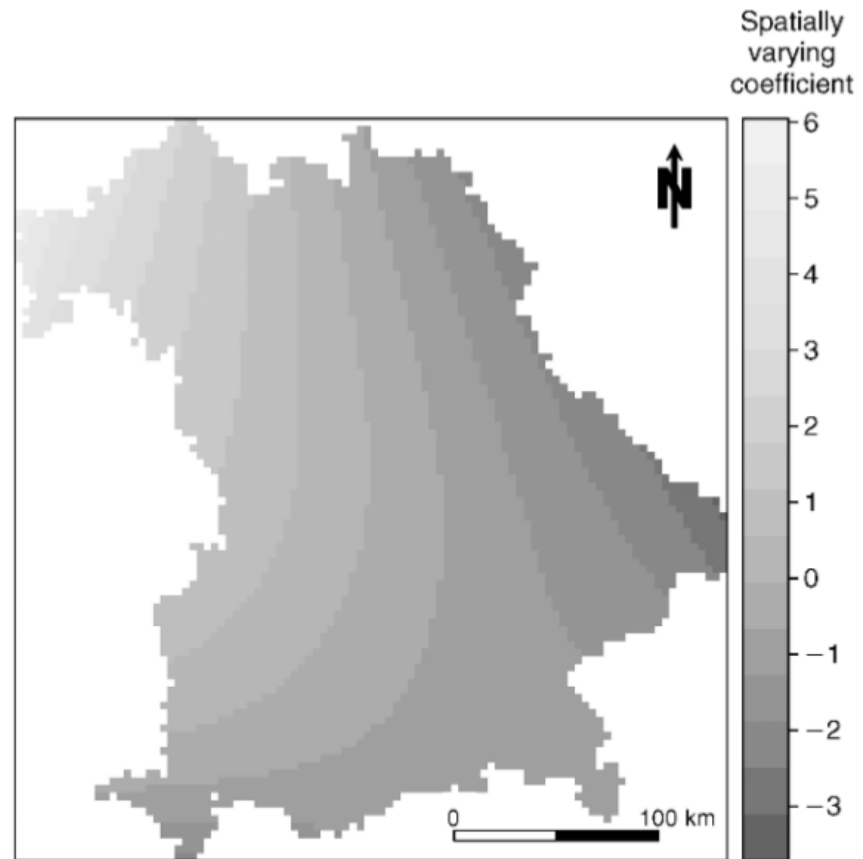


FIG. 8. Spatially varying coefficients for altitude in Red Kite breeding model (add/vary); here altitude was standardized to the unit interval. Altitude has a positive effect in the western and northwestern part, while its effect is zero or even negative in the rest of Bavaria.

# Gradient boosting: with splines baselearner

- ✓ Finally a ML method that explicitly models spatial surfaces and non-stationarity!
- ✓ Selects covariates (but not very rigorous)
- ✓ Simple Interpretation of non-linear relationships
- ✗ Not so fast, needs a lot of setup for fitting ★
- ✗ Unfair/biased selection of categorical covariates ★
- ✗ Interpretation of covariate importance difficult, if no strong selection ★
- ✗ Parametric method: transformations, extrapolation errors
- ✗ Prediction uncertainty only with bootstrap

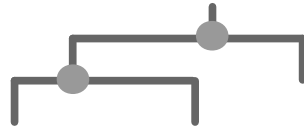


## geoGAM

- ✓ Strong covariate selection (after boosting), improves interpretation
- ✓ Simple application for prediction problems (binary, ordinal, continuous) with roughly fair covariate selection
- ✗ Reduced model performance
- ✗ Spatial surface too coarse to capture small scale variability
- ✗ Selection stability?

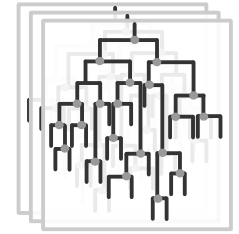
# Should I use boosted trees or random forests?

## Boosted trees



- ✓ Selects covariates weakly
- ✓ Covariate importance for interpretation and maybe selection
- ✗ Predictive accuracy slightly lower than random forest
- ✗ Prediction uncertainty only by bootstrapping
- ✓ Reduces bias by fitting on residuals

## Random forest



- ✗ Does not select covariates
- ✓ Covariate importance for interpretation and maybe selection
- ✓ From my datasets on average best performance (up to 50 different responses tested)
- ✓ Prediction uncertainty with quantile regression forest
- ✗ Always fits on data with same distribution

Speed?

Do some benchmarking if interested ;-)

# Model averaging

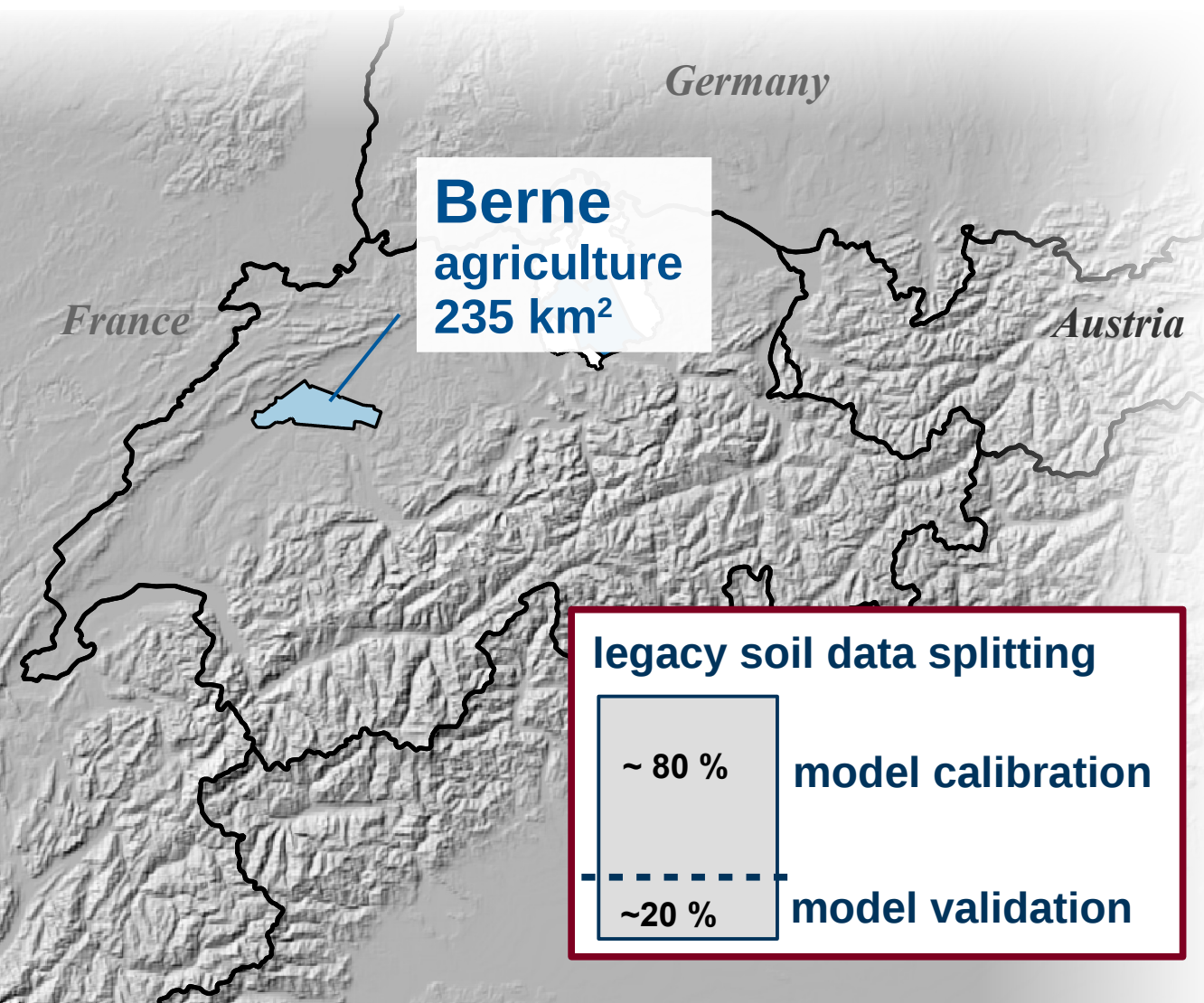
- Create predictions from different (ML) methods and **combine them**.
- Idea: each (ML) method as a mean of **reducing dimensions** in the dataset capturing different properties of the dataset → used methods should not be similar.
- Mathematical proofs show that combinations of different linear models result always in better performance. For other methods that's not a priori given, but very likely.
- Strategies
  - just take mean for every prediction
  - weighted mean, weights from model performance e.g.  $\frac{1}{MSE}$
  - local weights with uncertainties of each method and prediction
  - linear fit with predictions as covariates and original data as response → but take care, never fit on validation set!!
  - or stacked generalisation, Bayesian approach



# Exercise:

## Berne soil mapping study

~ 1000 sites with legacy soil data from 1970-1980  
Nussbaum et al. 2017b



## Numerous covariates

### Climate

different data sets  
(monthly resolution)

### Soil

soil overview map  
historic wetlands  
anthropogenic soil interventions  
drainage networks

### Parent material

(hydro)geological maps  
and derivatives

### Vegetation

Landsat, SPOT5, DMC mosaic  
forest vegetation map and  
species composition

### Terrain

90 derived attributes  
(multiple scales)