

# CHAPTER 5

## Multiple Regression Analysis: OLS Asymptotics

Pedram Jahangiry

2

Gauss-Markov Assumptions

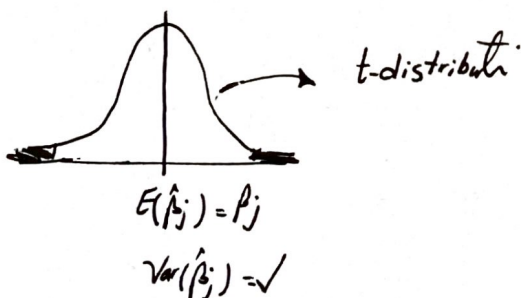
- MLR1. linearity in  $\beta$
- MLR2. Random Sampling
- MLR3.  $\text{Var}(x_j) \neq 0$  and no Perfect Collinearity
- MLR4.  $E(u|x) = 0$
- MLR5.  $\text{Var}(u|x) = \sigma^2$
- MLR6.  $x_j$  are indep +  $u \sim N(0, \sigma^2)$

MLR1-4:  
unbiasedness  
 $E(\hat{\beta}_j) = \beta_j$

MLR1-5:  
$$\text{Var}(\hat{\beta}_j) = \frac{\sigma^2}{\text{SST}_j(1-R_j^2)}$$

Classical linear Model Assumption

we know the exact dist of  $\hat{\beta}_j$



① Relaxing  
MLR4  $\xrightarrow{\text{to}}$  MLR4'  
 $E(u|x) = 0 \xrightarrow{\text{to}} \text{Cov}(u, x) = 0$

and ② Deleting MLR6

③ MLR1-MLR4': Consistency  
$$\lim_{n \rightarrow \infty} \hat{\beta}_j = \beta_j$$