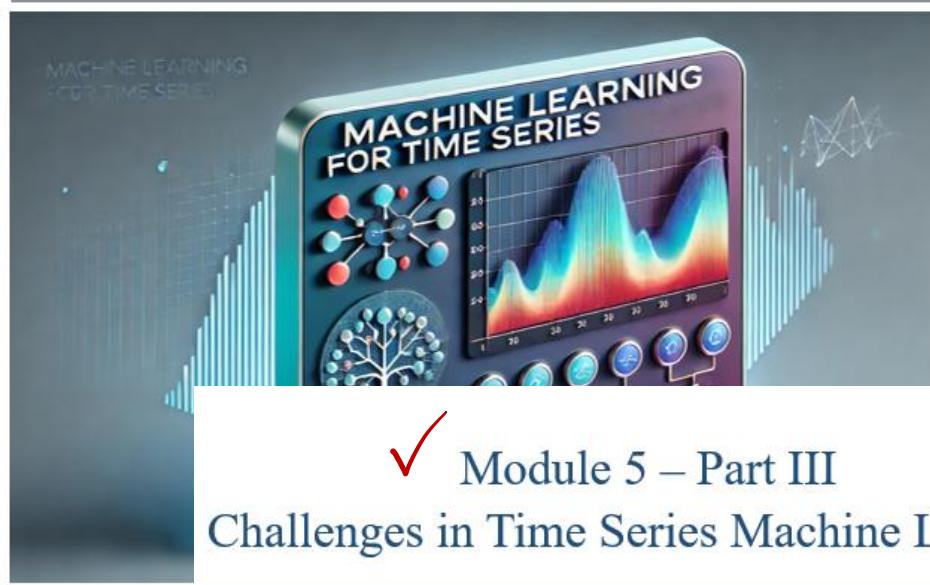


Road map!

- Module 1- Introduction to Deep Forecasting
- Module 2- Setting up Deep Forecasting Environment
- Module 3- Exponential Smoothing
- Module 4- ARIMA models
- **Module 5- Machine Learning for Time series Forecasting**
- Module 6- Deep Neural Networks
- Module 7- Deep Sequence Modeling (RNN, LSTM)
- Module 8- Prophet and Neural Prophet



✓ Module 5 – Part I Machine Learning For timeseries Forecasting

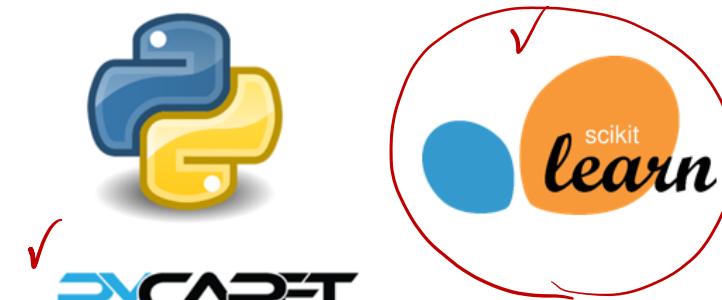


✓ Module 5 – Part II Machine Learning for timeseries Decision Tree based Models



Aspect	Decision Tree (DT)	Random Forest (RF)	XGBoost	CatBoost	LightGBM
1. Sampling Process	Naïve	Naïve	Histogram-based	Feature Binning (Quantization)	GOSS
Method	Greedy	Leaf-wise			
with Trees					Boosting

✓ Module 5 – Part IV ML for timeseries in Python

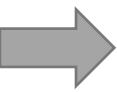


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Module 5 – Part I

Machine Learning For timeseries Forecasting





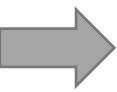
Model Comparison



Two red arrows point from the top of the slide down to the 'Econometric Models' and 'Machine Learning (ML)' columns.

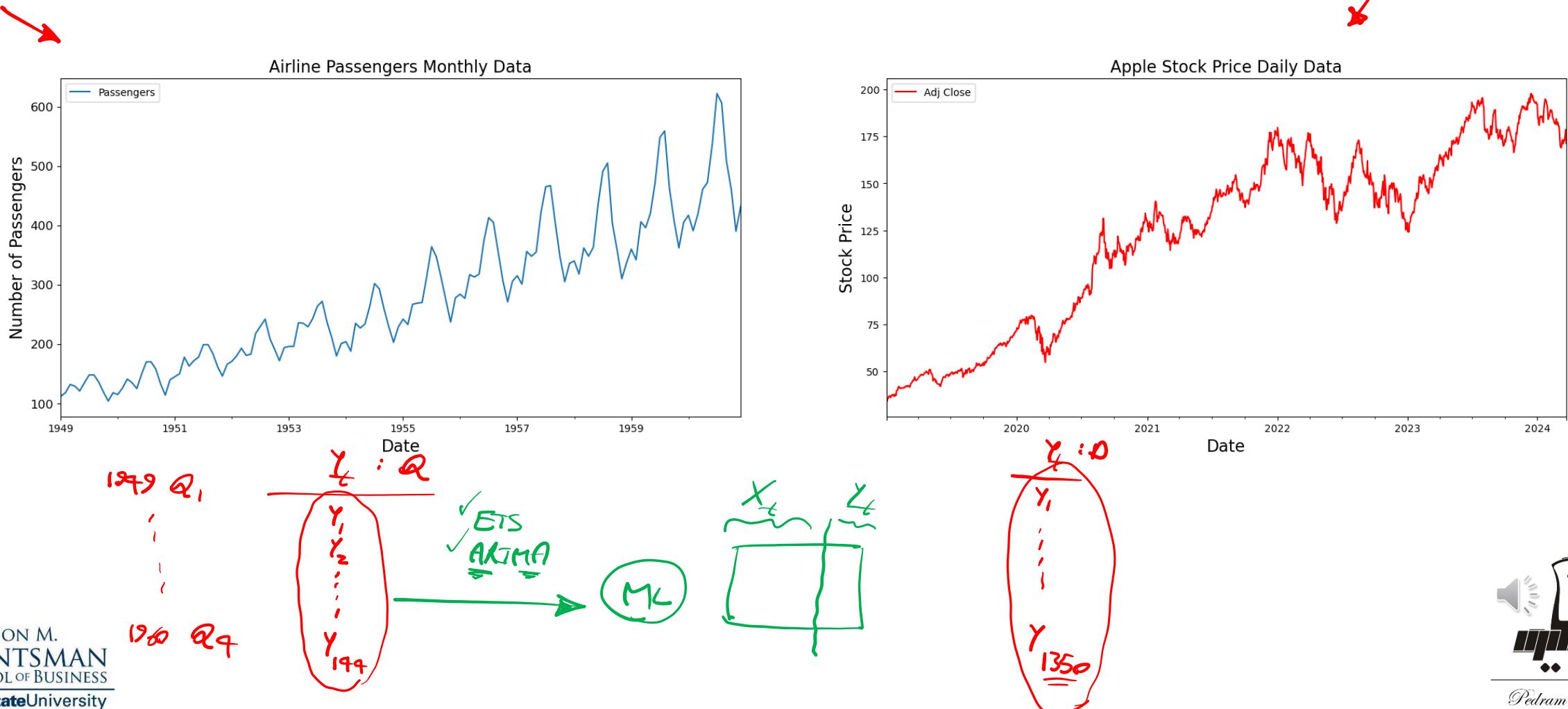
Aspect	Econometric Models	Machine Learning (ML)	Deep Learning (DL)
✓ Feature Engineering	Requires explicit modeling of seasonality and trend <i>ARIMA</i>	Captures complex patterns with less need for manual engineering	Often automates feature engineering
✓ Model Complexity	Lower; focuses on data generation process	Moderate; can handle non-linear interactions	High; suited for complex and high-dimensional data
✓ Interpretability	High; interpretable parameters, statistical tests	Moderate; provides feature importance	Low; considered a 'black box' approach
✓ Computational Intensity	Generally lower	Varies; dependent on model complexity and data size	High; requires significant computational resources
✓ Data Suitability	Works well when the underlying process is well understood	Effective for structured datasets with complex relationships	Ideal for large datasets, including unstructured data
Core Models	ARIMA, Exponential Smoothing (ETS)	Random Forest, Gradient Boosting	RNNs, LSTMs, CNNs

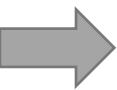




Pre-processing the data for machine learning

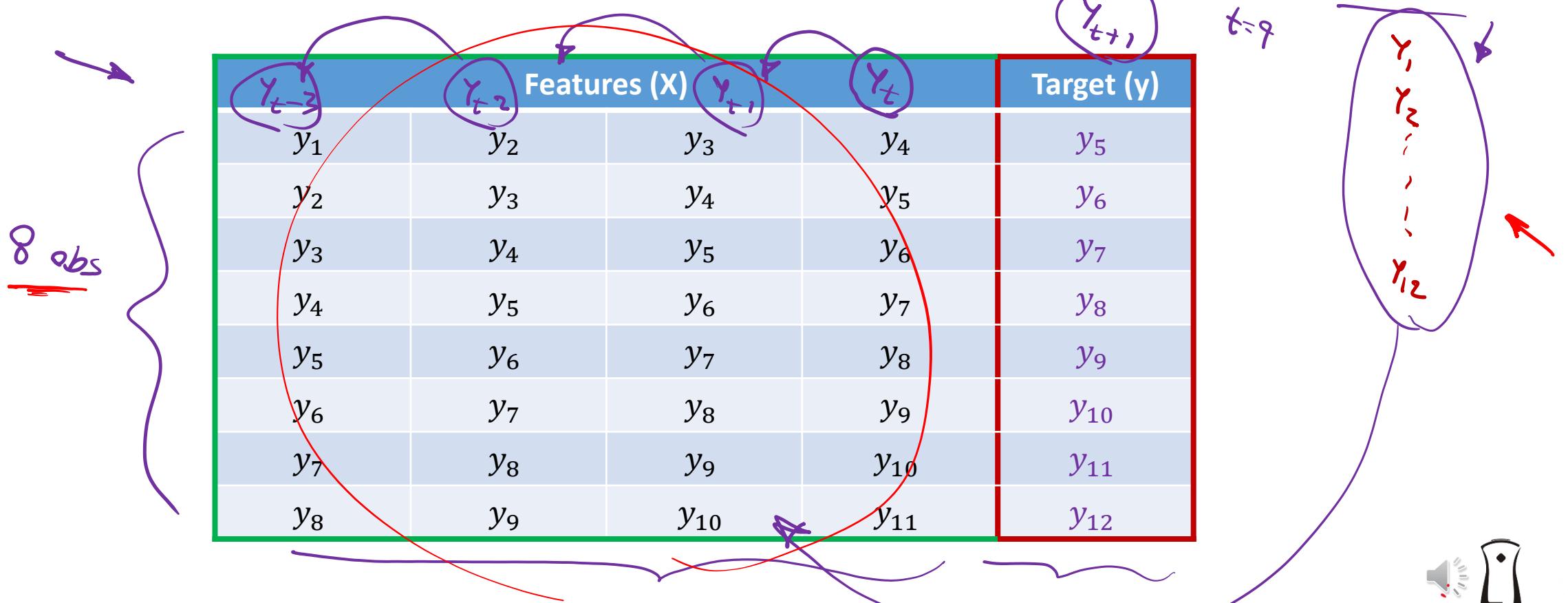
- How to convert time series problems into machine learning problems?

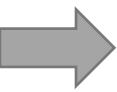




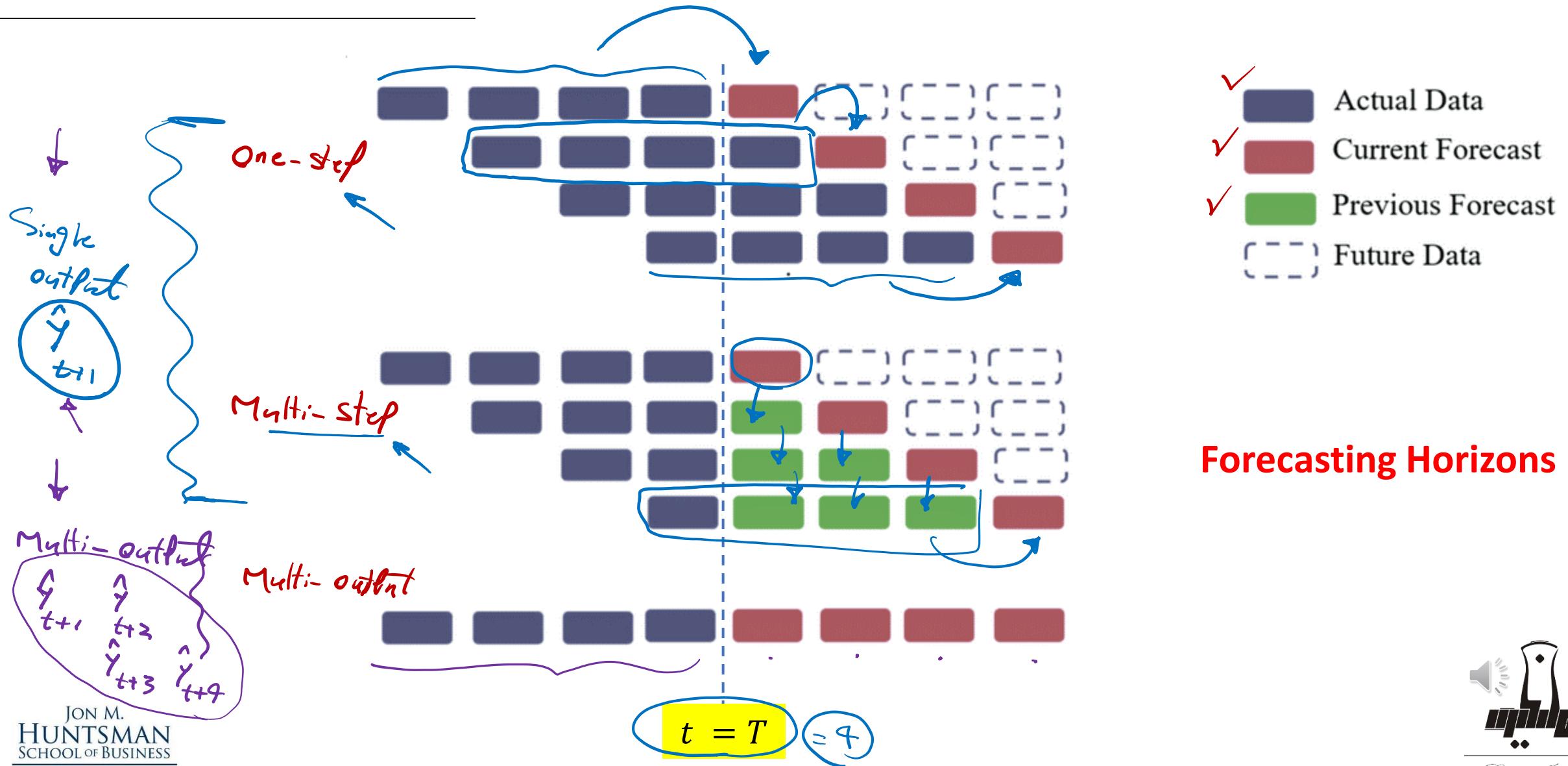
Preparing data for machine learning

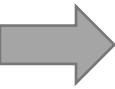
- How to convert time series problems into machine learning problems?





One-step, Multi-step, Multi-output Forecasts





Single-Output (one-step ahead)

y_{t-3}	Input Features (X)			y_t	Single-Output (y)
Lag 3	Lag 2	Lag 1	Lag 0		Lead 1 y_{t+1}
y_1	y_2	y_3	y_4		y_5
y_2	y_3	y_4	y_5		y_6
y_3	y_4	y_5	y_6		y_7
y_4	y_5	y_6	y_7		y_8
y_5	y_6	y_7	y_8		y_9
y_6	y_7	y_8	y_9		y_{10}
y_7	y_8	y_9	y_{10}		y_{11}
y_8	y_9	y_{10}	y_{11}		y_{12}
y_9	y_{10}	y_{11}	y_{12}		y_{13}
y_{10}	y_{11}	y_{12}	y_{13}		y_{14}

- ✓ y_t : Actuals
- ✓ \hat{y}_t : Predictions



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Single-Output (multiple-step ahead)



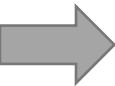
y_t : Actuals
 \hat{y}_t : Predictions

Input Features (X)				Single-Output (y)
Lag 3	Lag 2	Lag 1	Lag 0	Lead 1
y_1	y_2	y_3	y_4	y_5
y_2	y_3	y_4	y_5	y_6
y_3	y_4	y_5	y_6	y_7
y_4	y_5	y_6	y_7	y_8
y_5	y_6	y_7	y_8	y_9
y_6	y_7	y_8	y_9	y_{10}
y_7	y_8	y_9	y_{10}	y_{11}
y_8	y_9	y_{10}	y_{11}	y_{12}
y_9	y_{10}	y_{11}	y_{12}	y_{13}
y_{10}	y_{11}	y_{12}	y_{13}	y_{14}

y_t : Actuals
 \hat{y}_t : Predictions



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Multi-Output

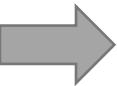
ETS, ARIMA

Input Features (X)				Multi-Output (Y)		
Lag 3	Lag 2	Lag 1	Lag 0	Lead 1	Lead 2	Lead 3
y_1	y_2	y_3	y_4	y_5	y_6	y_7
y_2	y_3	y_4	y_5	y_6	y_7	y_8
y_3	y_4	y_5	y_6	y_7	y_8	y_9
y_4	y_5	y_6	y_7	y_8	y_9	y_{10}
y_5	y_6	y_7	y_8	y_9	y_{10}	y_{11}
y_6	y_7	y_8	y_9	y_{10}	y_{11}	y_{12}
y_7	y_8	y_9	y_{10}	y_{11}	y_{12}	y_{13}
y_8	y_9	y_{10}	y_{11}	y_{12}	y_{13}	y_{14}
y_9	y_{10}	y_{11}	y_{12}	y_{13}	y_{14}	y_{15}
y_{10}	y_{11}	y_{12}	y_{13}	y_{14}	y_{15}	y_{16}

y_t : Actuals

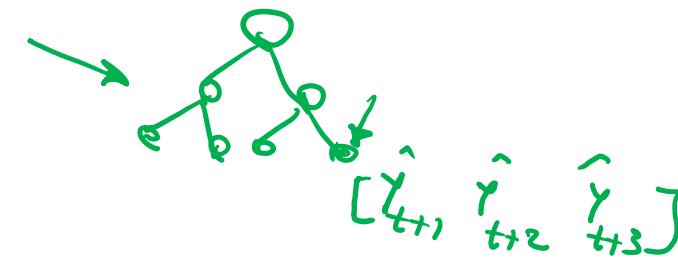
$\underline{y_t}$: Predictions





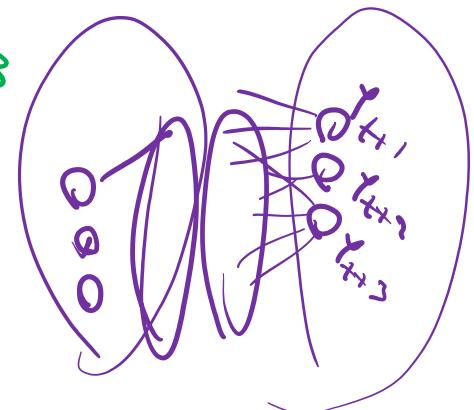
Multi-Output

LR X



Input Features (X)				Multi-Output (Y)		
Lag 3	Lag 2	Lag 1	Lag 0	Lead 1	Lead 2	Lead 3
y_1	y_2	y_3	y_4	y_5 \hat{y}_{t+1}	y_6 \hat{y}_{t+2}	y_7 \hat{y}_{t+3}
y_2	y_3	y_4	y_5	y_6	y_7	y_8
y_3	y_4	y_5	y_6	y_7	y_8	y_9
y_4	y_5	y_6	y_7	y_8	y_9	y_{10}
y_5	y_6	y_7	y_8	y_9	y_{10}	y_{11}
y_6	y_7	y_8	y_9	y_{10}	y_{11}	y_{12}
y_7	y_8	y_9	y_{10}	y_{11}	y_{12}	y_{13}
y_8	y_9	y_{10}	y_{11}	y_{12}	y_{13}	y_{14}
y_9	y_{10}	y_{11}	y_{12}	y_{13}	y_{14}	y_{15}
y_{10}	y_{11}	y_{12}	y_{13}	y_{14}	y_{15}	y_{16}

y_t : Actuals
 \hat{y}_t : Predictions



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Machine Learning Fundamentals (review)

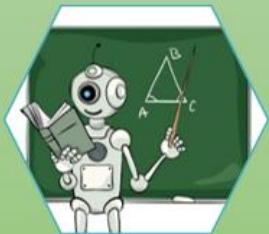
Artificial intelligence: Any technique which enables machines to mimic human behavior

Machine Learning: Subset of AI that enables computers to learn from data. the model is trained with a set of algorithms

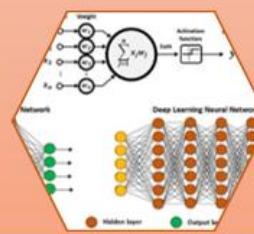
Deep Learning: Subset of ML that extract patterns from data using neural networks.



1950's

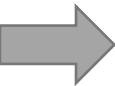


1980's



2010's

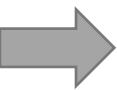




Machine Learning Fundamentals

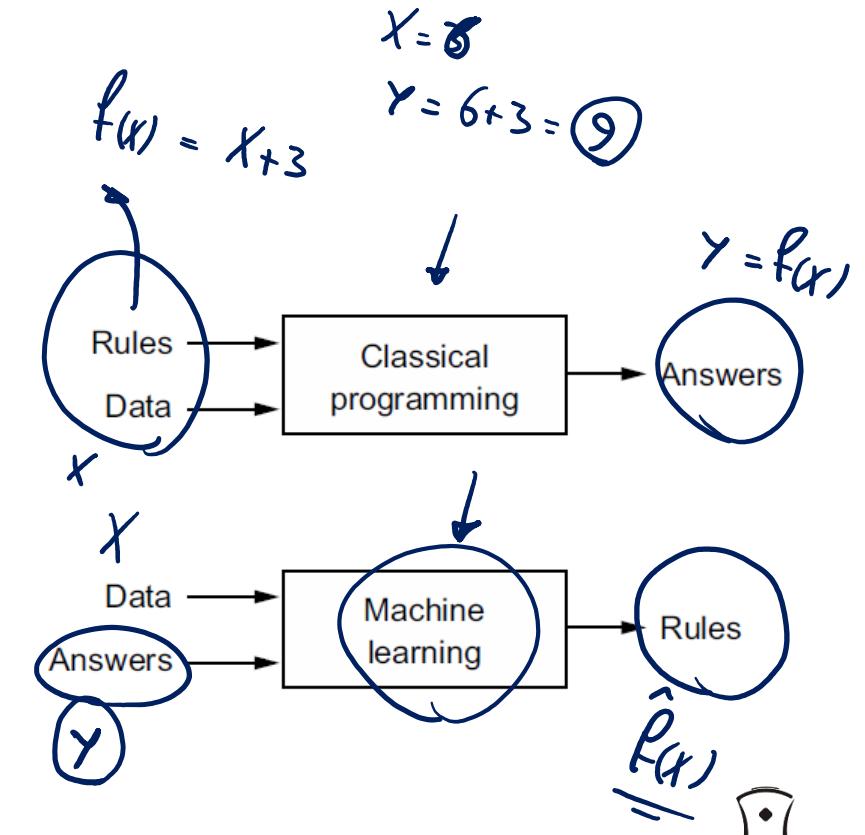
- ✓ • ML vs traditional programming
- ✓ • Types of ML
- ✓ • The Model
- ✓ • Evaluation metrics *RMSE*
- ✓ • Bias-Variance tradeoff, overfitting
- ✓ • Train, Test, Validation
- ✓ • Resampling methods
- ✓ • Cost Function
- ✓ • Solvers/learners (GD, SGD)
- ✓ • How do machines actually learn?

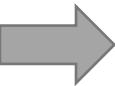




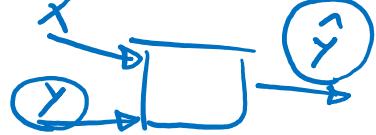
What is Machine Learning?

- Machine Learning is a subset of AI that enables computers to learn from data.
- A machine learning system is trained (with algorithms) rather than explicitly programmed.
- ML involves automated detection of meaningful **patterns** in data and apply the pattern to make **predictions** on **unseen data!**
- The goal is to **maximize** the performance on the unseen data. The purpose is to generalize.



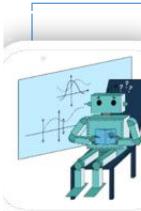


Types of Machine Learning



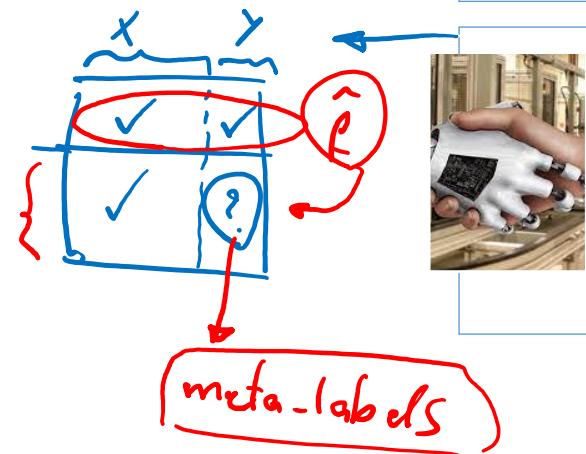
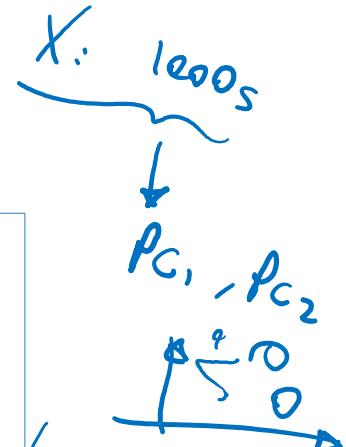
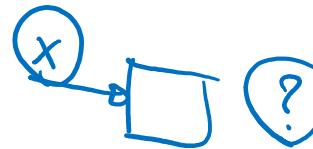
Supervised

- Regression ✓
- Classification ✓



Unsupervised

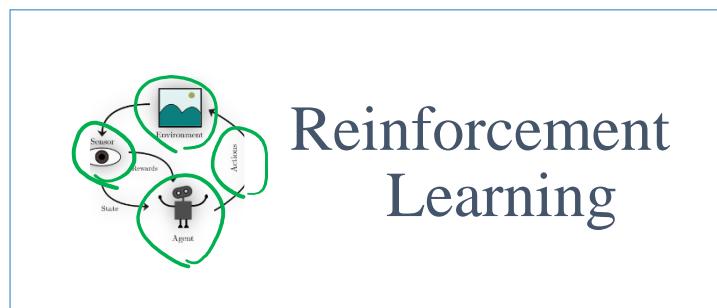
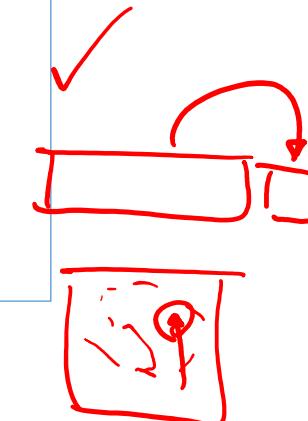
- Clustering ✓
- Anomaly detection ✓
- Dimensionality reduction ✓



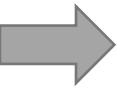
Semi-supervised



Self-supervised



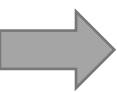
Reinforcement Learning



The Model

$$\checkmark \quad y = \underline{f}(\underline{X}, \underline{\theta}) + \epsilon = f(X_1, X_2, \dots, X_m, \theta_1, \theta_2, \dots, \theta_k) + \epsilon$$

- ✓ y : response, dependent variables, output, Target
- ✓ X : predictors, independent variables, input, Features
- ✓ θ : estimates, specifications, Parameters
- ✓ It is all about estimating f by \hat{f} for two purposes:
 - ✓ 1) Inference (interpretable ML)
 - ✓ 2) Prediction

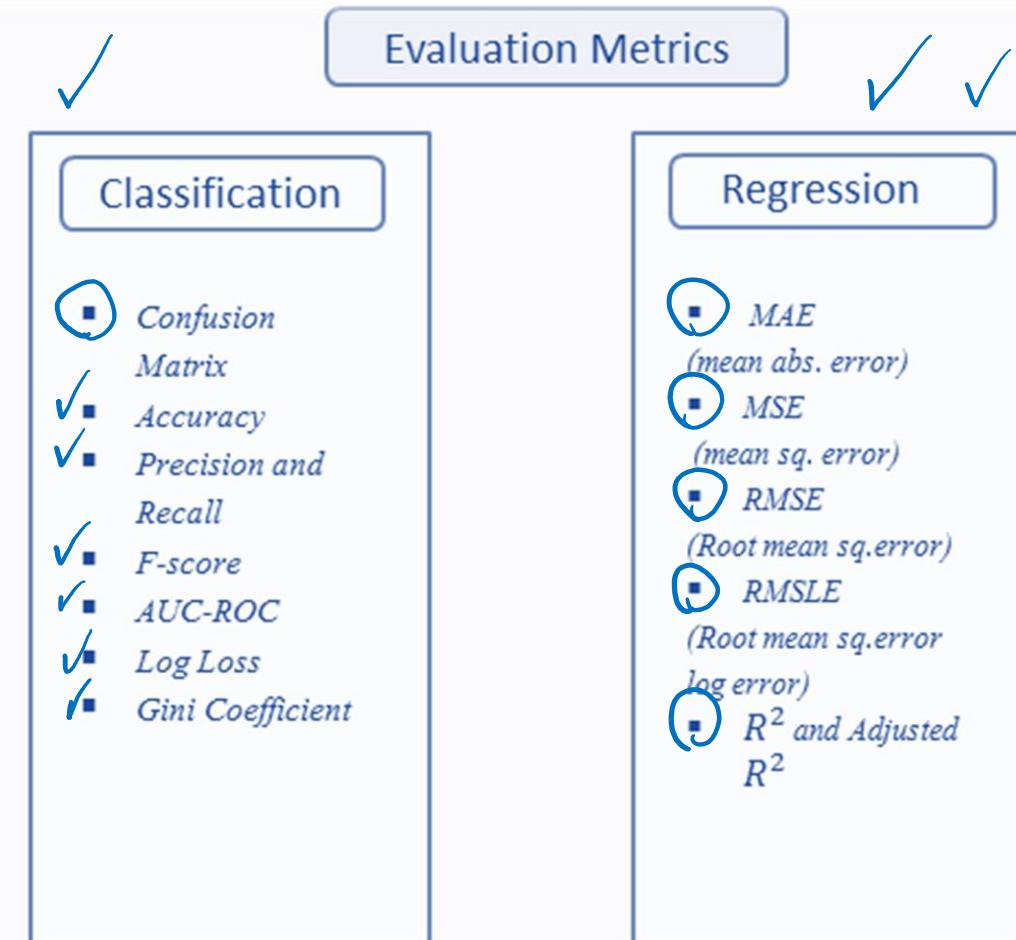


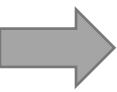
Evaluation metrics

In general, we want to compare how close are the predictions to the actual numbers in the **test set**.

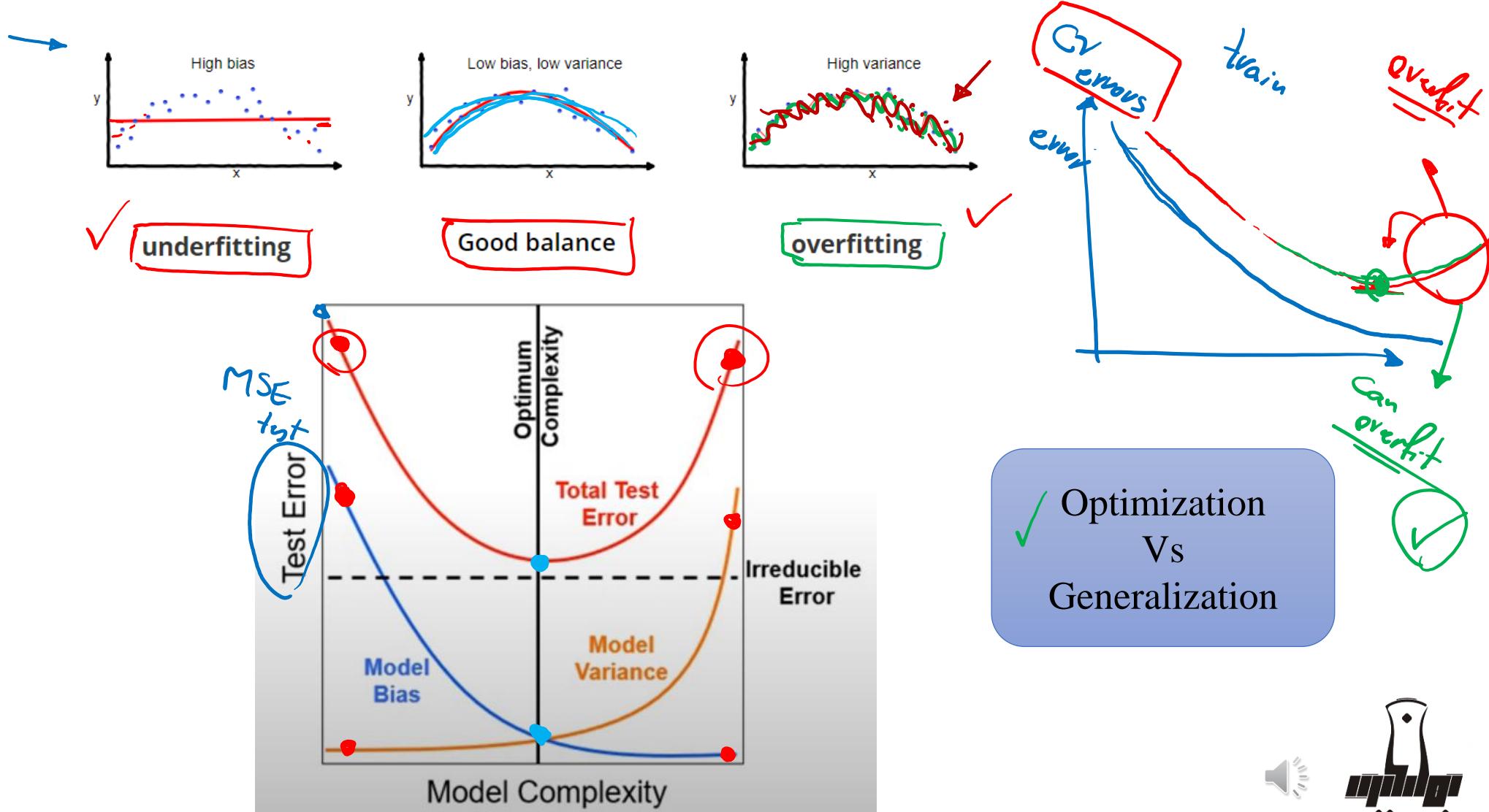
This is typically assessed using

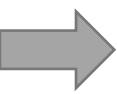
- MSE for **quantitative** response
- Misclassification rate for **qualitative** response



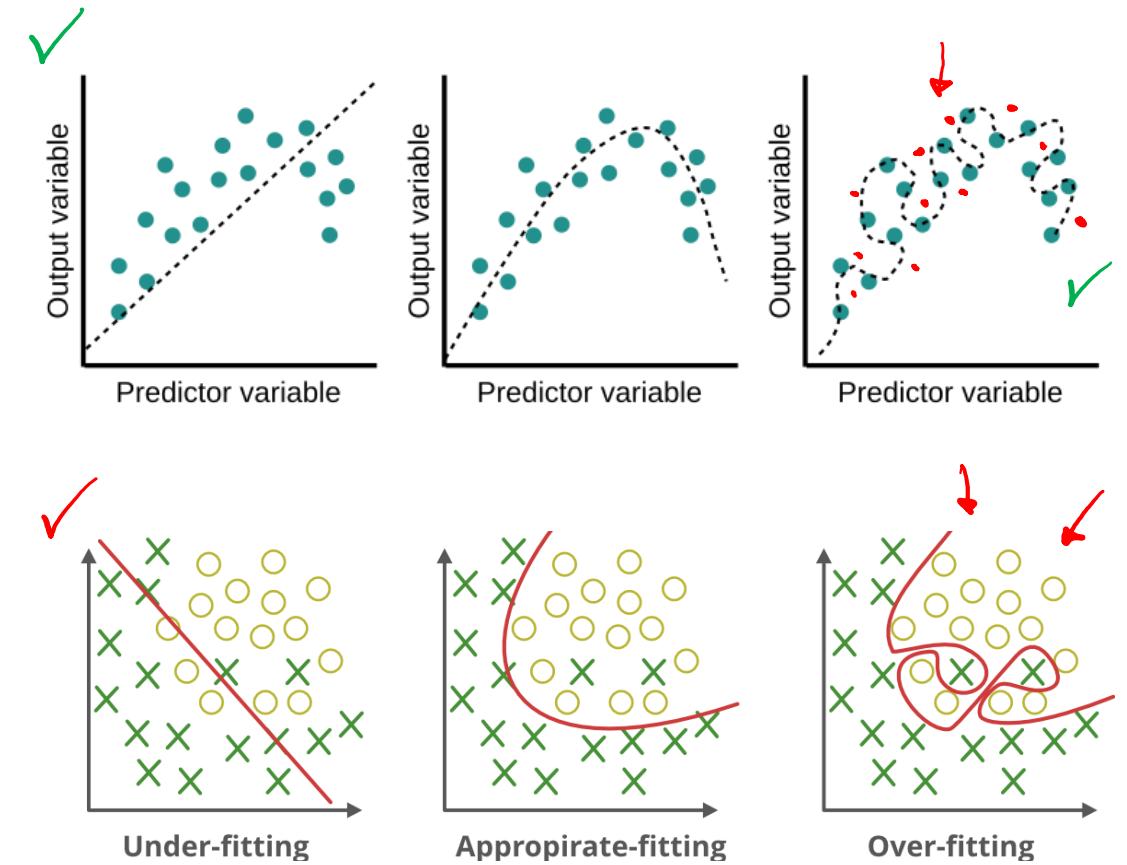
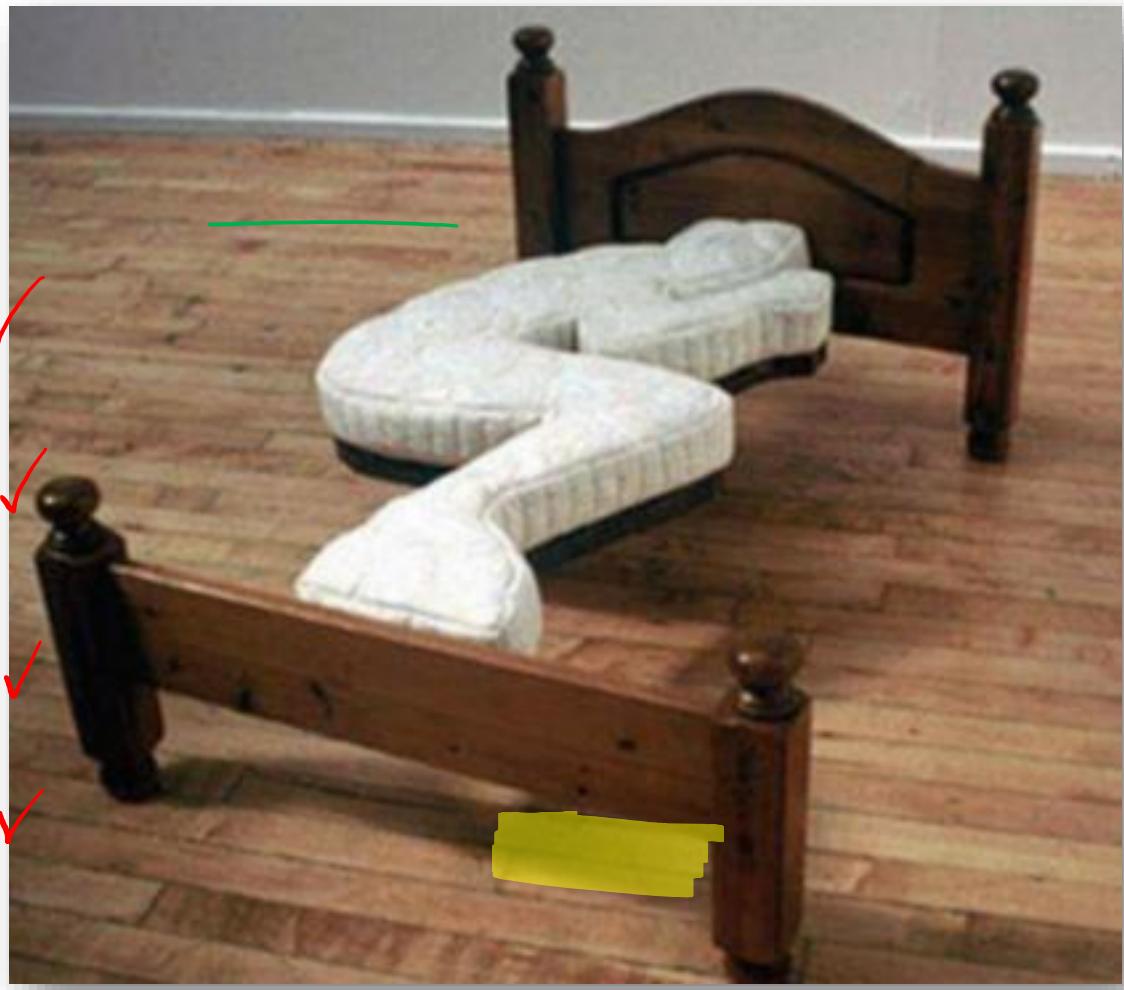


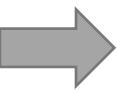
Representations of the bias-variance tradeoff





Overfitting

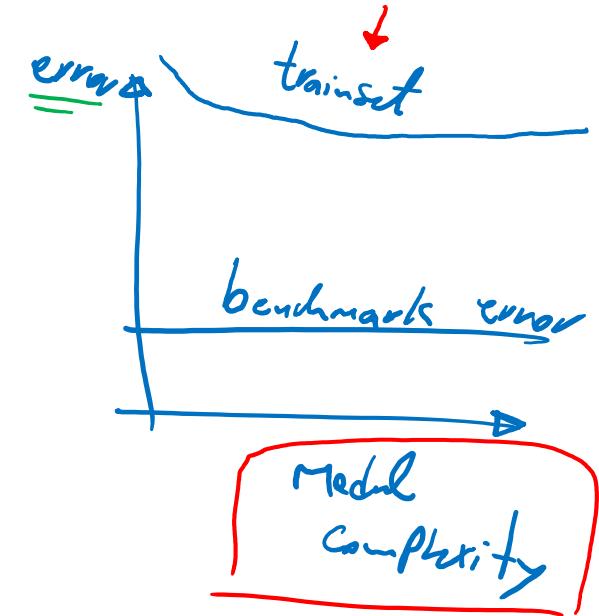
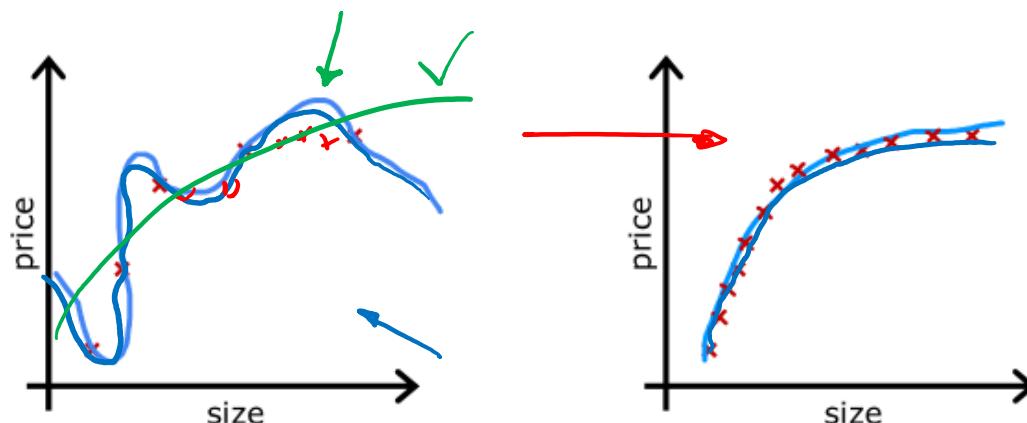




Mitigate overfitting

The main techniques used to mitigate overfitting risk in a model construction are:

- ✓ 1) Collect **more data** (Can reduce bias AND variance)
- ✓ 2) **Complexity** reduction (regularization, feature selection)
- ✓ 3) **Cross validation** (estimate the performance in test set)

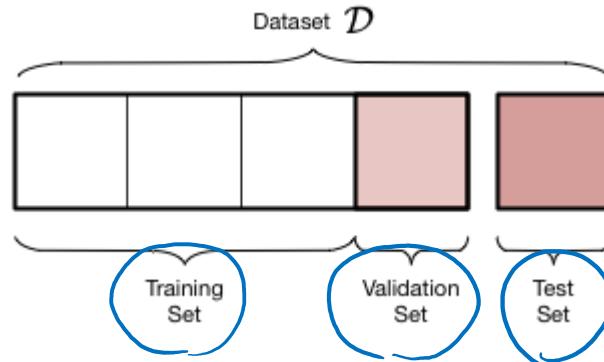


With more training example

Partitioning of the dataset

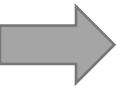
The data set is typically divided into three non-overlapping samples:

- ✓ 1) Training set: to train the model
- ✓ 2) Validation set: to validate and tune the model
- ✓ 3) Test set: to test the model's ability to predict well on new data (**generalize**)



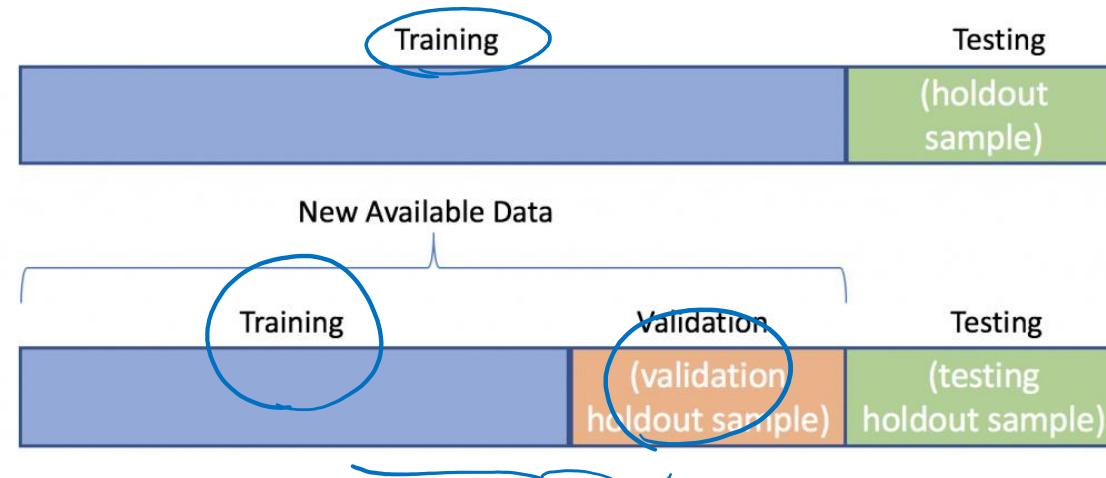
- ✓ To be valid and useful, any supervised machine learning model **must** generalize well beyond the training data.

Large dataset is needed! But what if we don't have it?



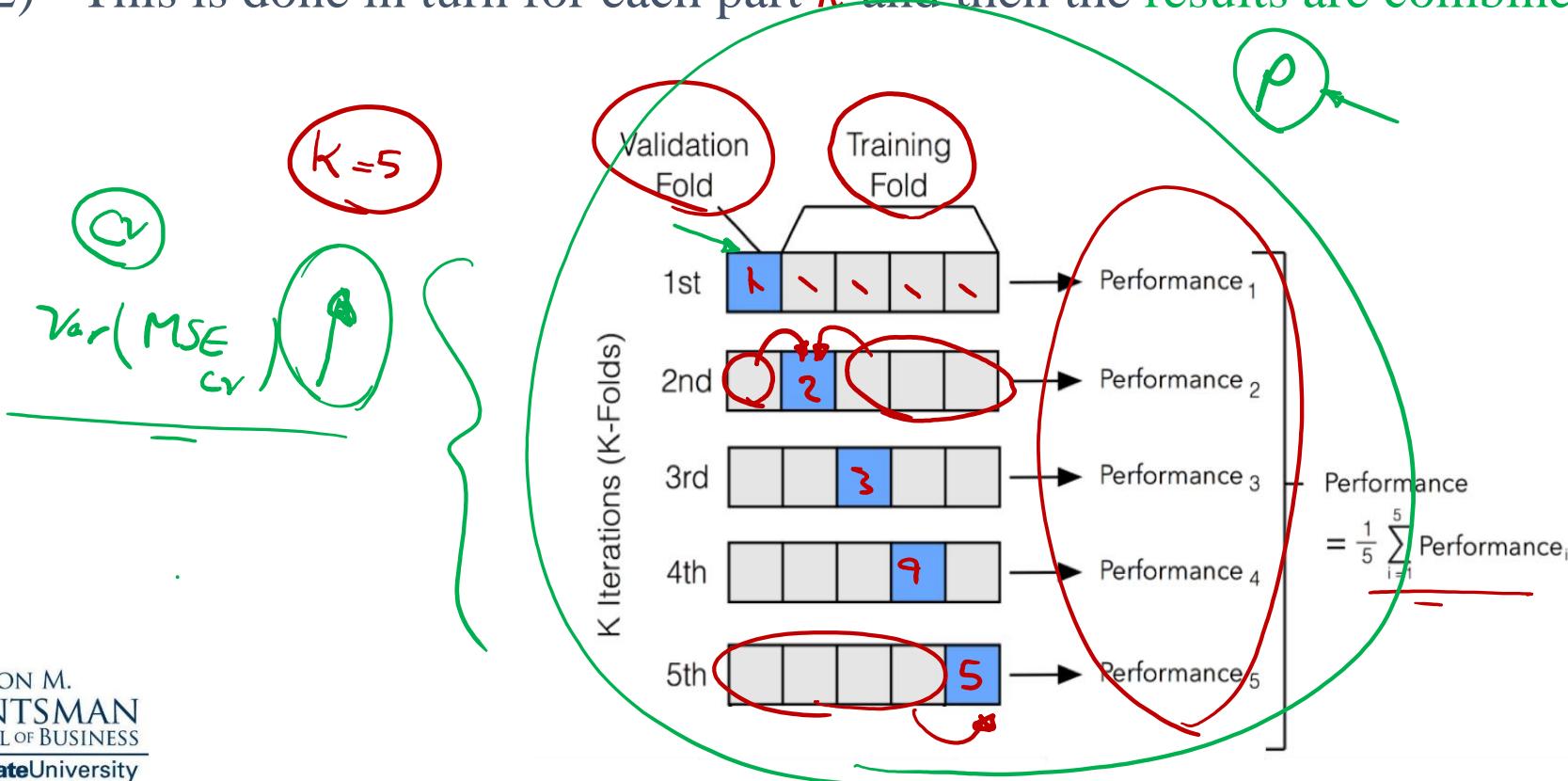
Resampling methods

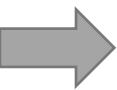
- Sometimes we cannot afford to split the data in three because the algorithm may **not learn** anything from a **small training dataset!**
- **Small validation set** is also problematic because we cannot tune the hyperparameters properly! **Unstable** model performance in validation set!
- **Solution:** combining the training and validation sets and use cross validation!



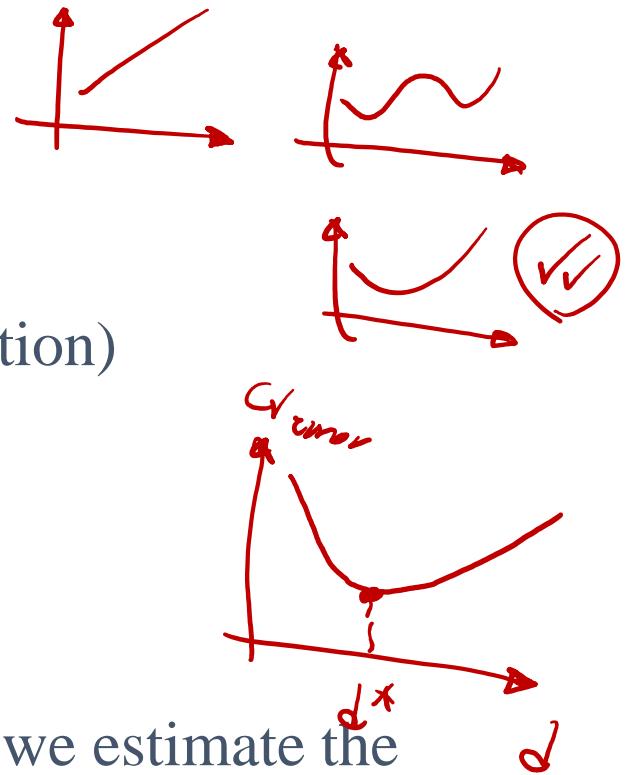
→ K-fold Cross Validation

- 1) Divide the training data into K roughly equal-sized non-overlapping groups. Leave out k^{th} fold and fit the model to the other $k - 1$ folds. Finally, obtain predictions for the left-out k^{th} fold.
- 2) This is done in turn for each part k and then the results are combined.



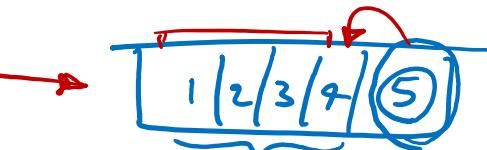


Why do we use Cross Validation?

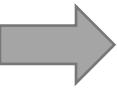


Cross validation is mainly used for two purposes:

- ✓ 1. Model architecture selection (optimization vs generalization)
- ✓ 2. Estimation of model performance in the test set

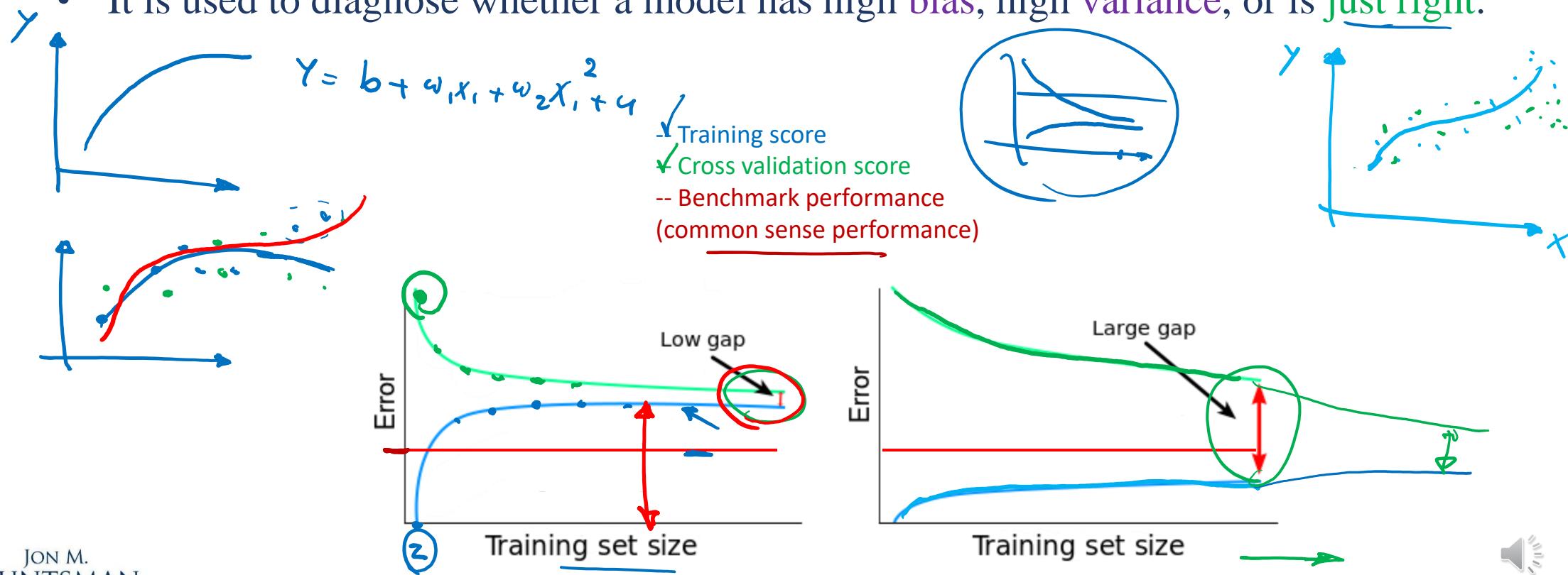


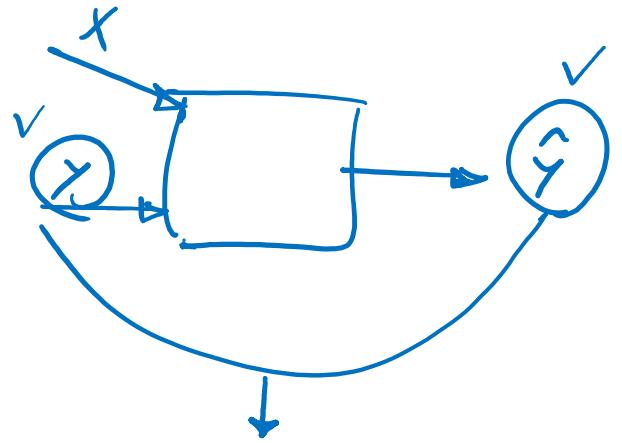
- After selecting the best model architecture, we estimate the generalization error using the test set.
- Different model comparison is based on test set performance!



The Learning Curve: Do we need to collect more data?

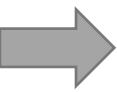
- ✓ A learning curve is a plot that shows the relationship between the amount of **training data** and the **performance** of a machine learning model.
- It is used to diagnose whether a model has high **bias**, high **variance**, or is just right.





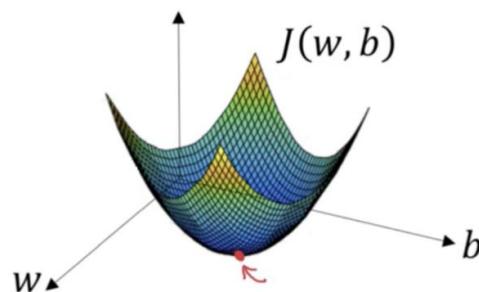
How do Machines Learn?

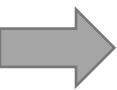




Terminology

- Learning: Finding the model **weights** (parameters' values)
- **Cost Function**: Tells us “**how good**” our model is at making predictions for a given set of parameters.
- The cost function has its own curve and its own gradients. The slope of this curve tells us how to update our parameters to make the model more accurate.
- The two most frequently used optimization algorithms when the cost function is **continuous** and **differentiable** are Gradient Descent (GD) and Stochastic GD.





Solvers (learners)!

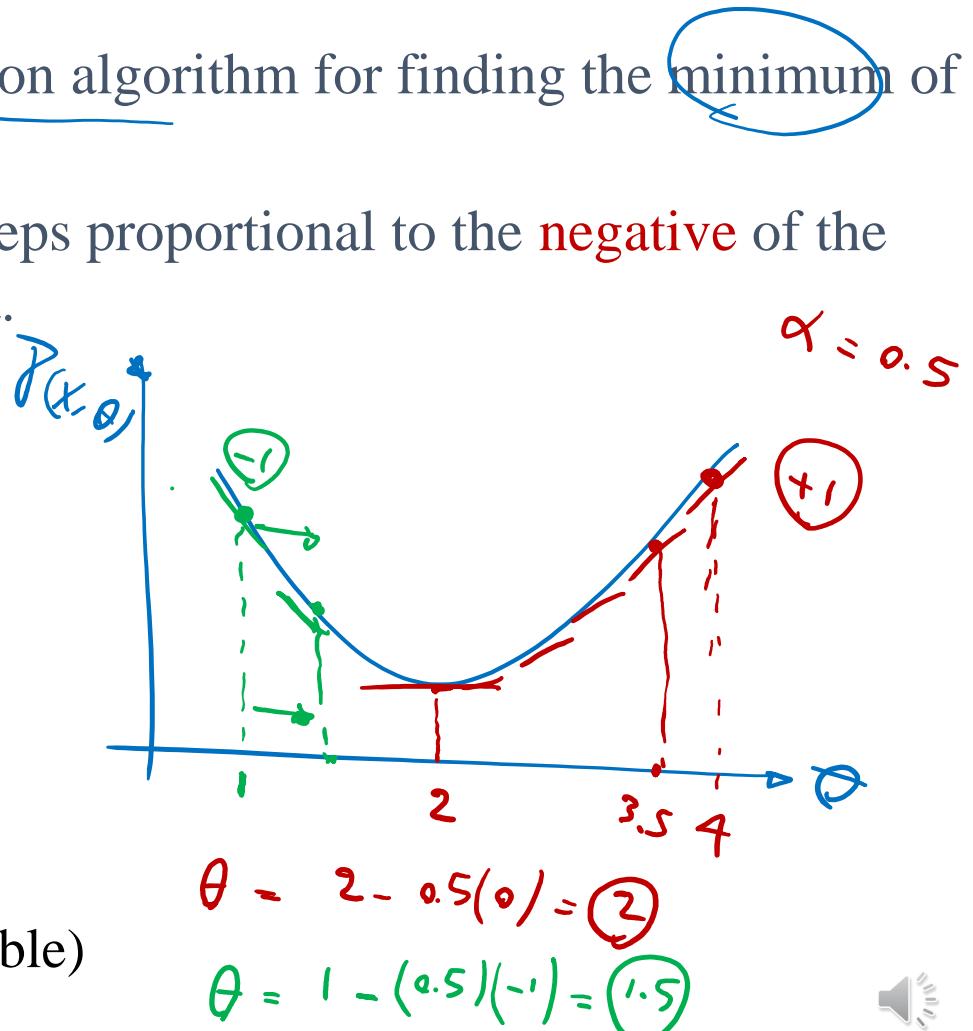
- Gradient Descent: is an **iterative** optimization algorithm for finding the **minimum** of a function.
- We start at some random point and take steps proportional to the **negative** of the gradient of the function at the current point.

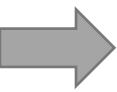
$$\theta_j := \underline{\theta_j} - \alpha \frac{\partial}{\partial \theta_j} J(\theta)$$

4 -0.5 = 3.5

Handwritten annotations: $\alpha = 0.5$, $+1$, -1 .

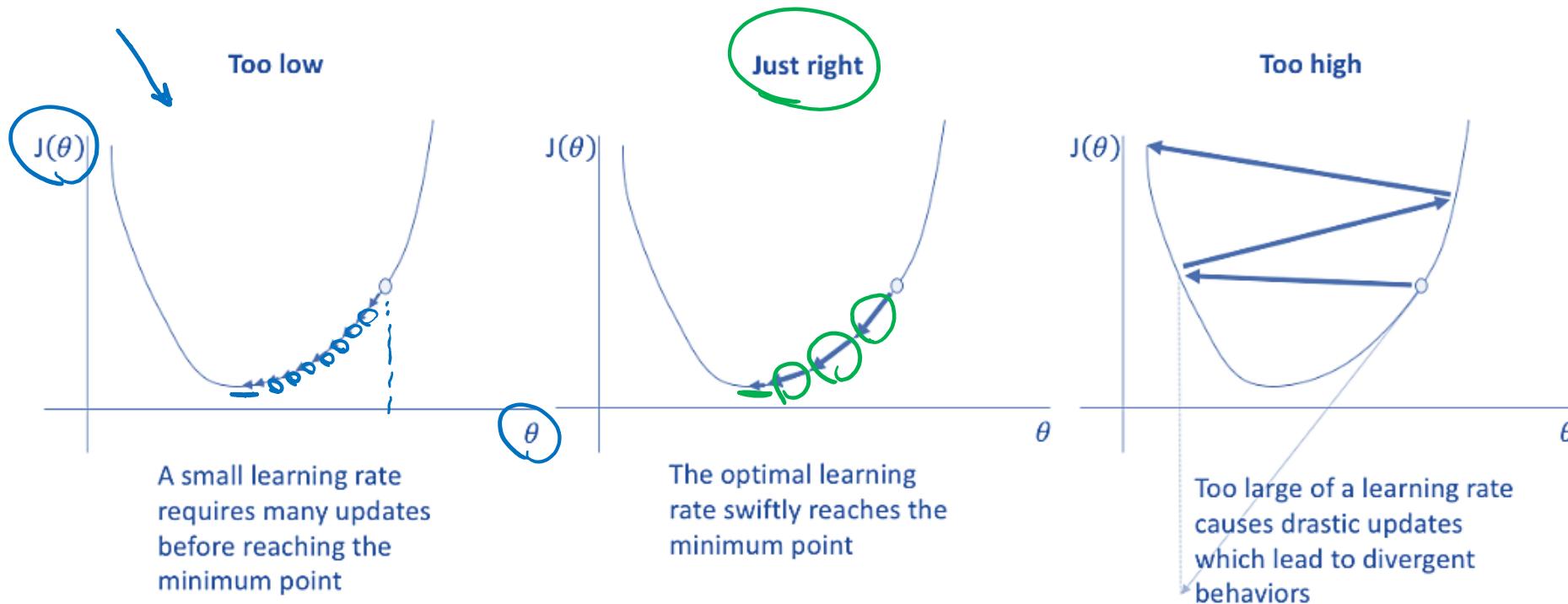
- θ_j is the model's j^{th} parameter
- α is the learning rate
- $J(\theta)$ is the cost function (which is differentiable)

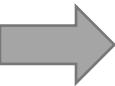




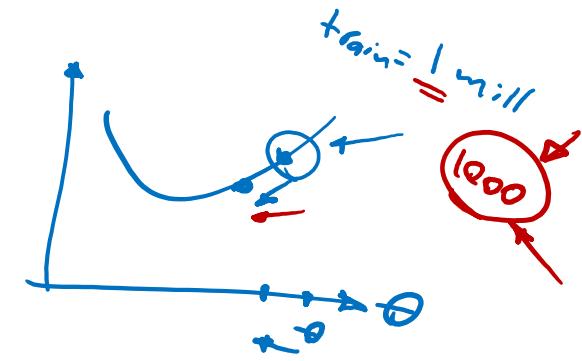
Choice of learning rate

- If α is too small, gradient descent can be **slow**
- If α is too large, the gradient descent can even **diverge**.





Beyond Gradient Descent?

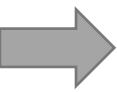


Disadvantages of gradient descent:

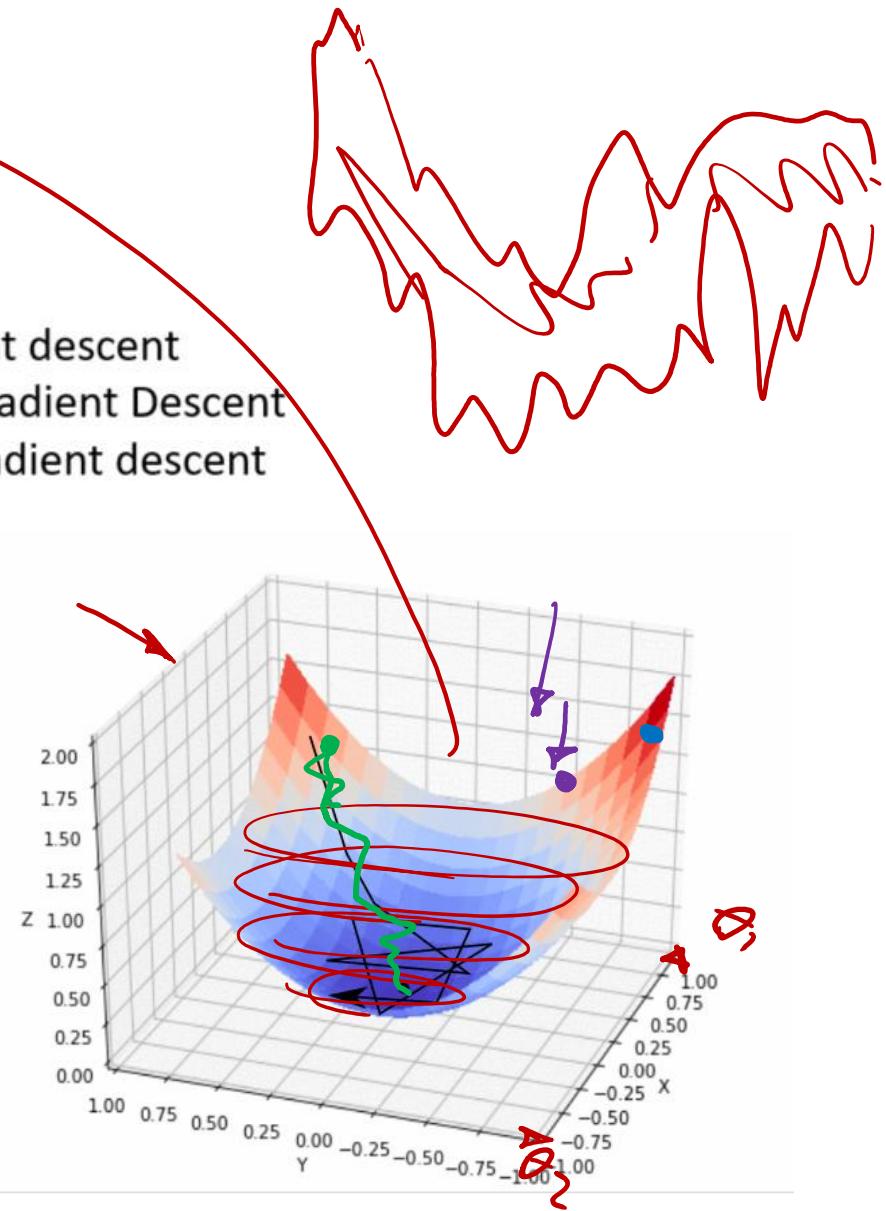
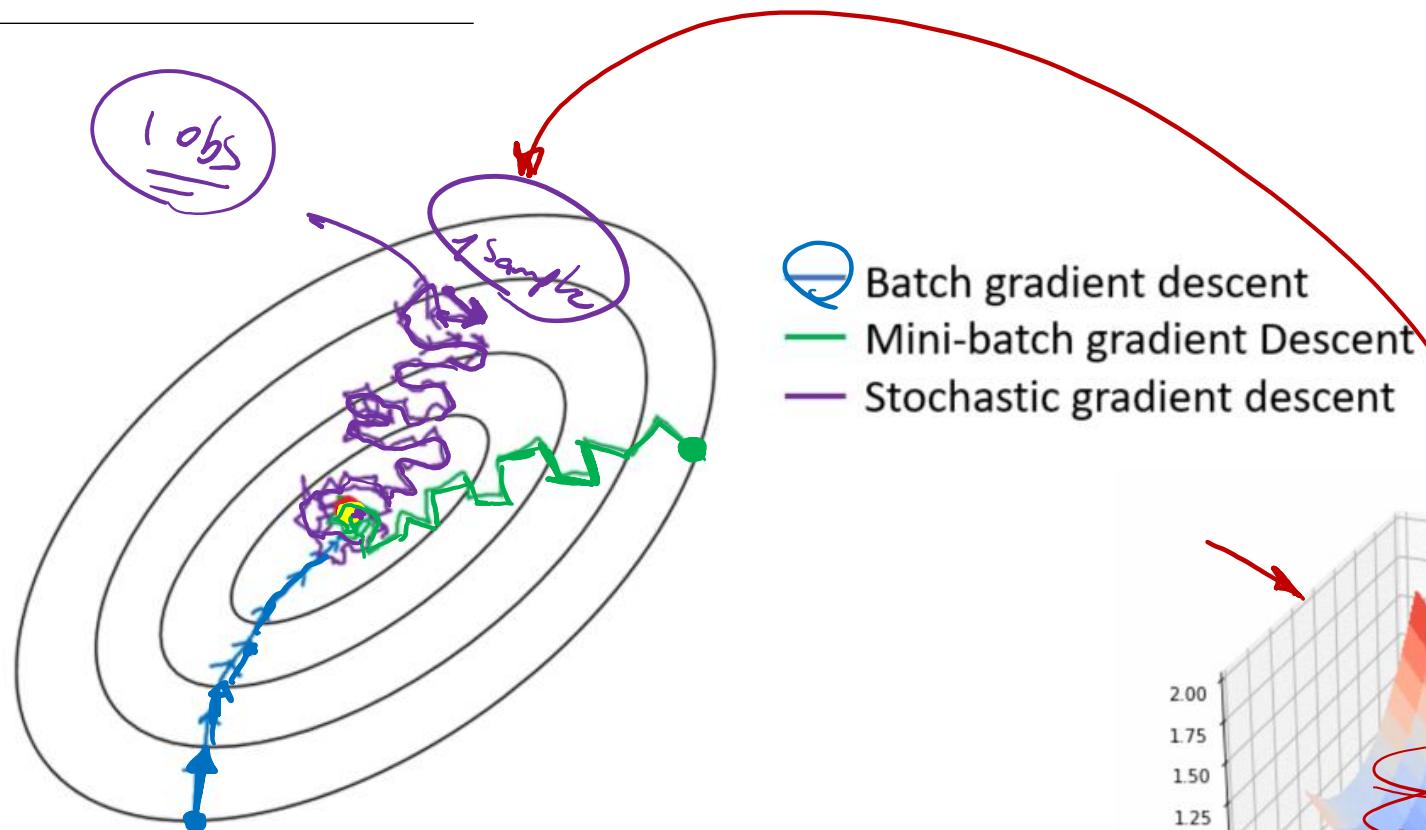
- ✓ • Single batch: use the entire training set to update parameters!
- ✓ • Sensitive to the choice of the learning rate
- Slow for large datasets

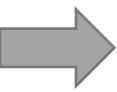
(Minibatch) Stochastic Gradient Descent: is a version of the algorithm that speeds up the computation by approximating the gradient using smaller batches (subsets) of the training data. SGD itself has various “upgrades”.

$$b = 1$$



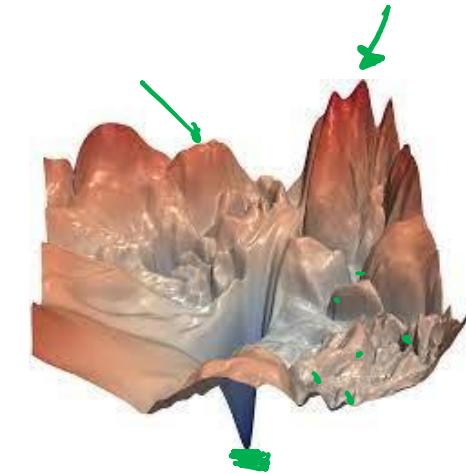
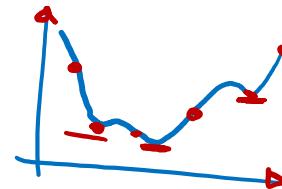
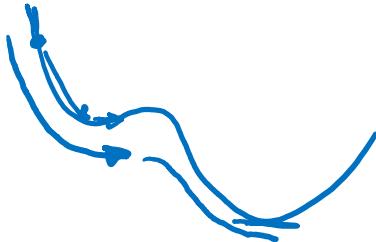
SGD vs GD



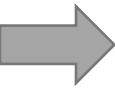


Beyond SGD?

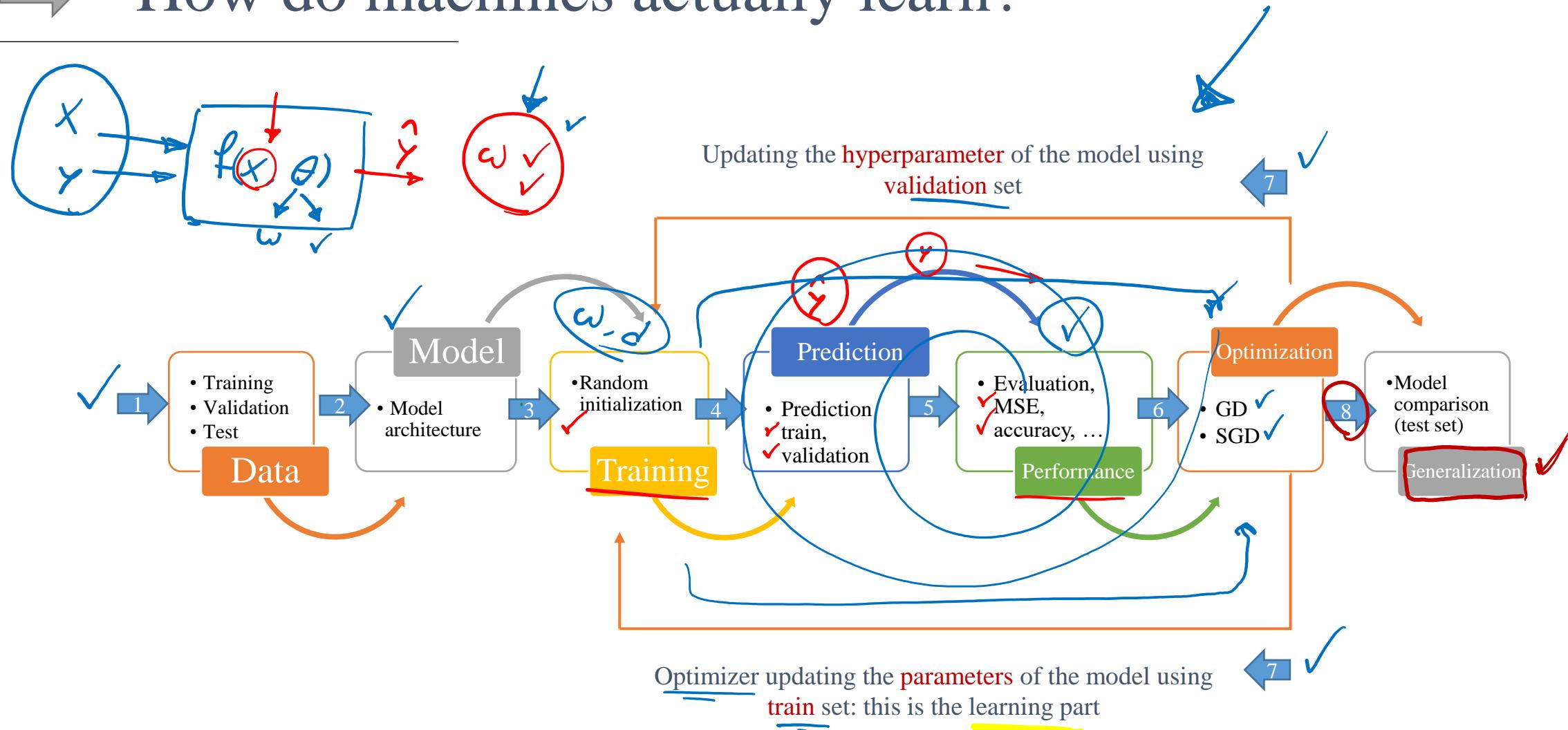
- Loss functions can be difficult to optimize!
- *Visualizing the loss landscape of neural nets*, Li et all, 2018



- Solution: Designing an adaptive learning rate that can adapt to the loss landscape.
- Rather than just looking at the current gradient, consider the previous weight updates.
- This is called, momentum!
- Examples: Adam, Adadelta, Adagrad, RMSProp!

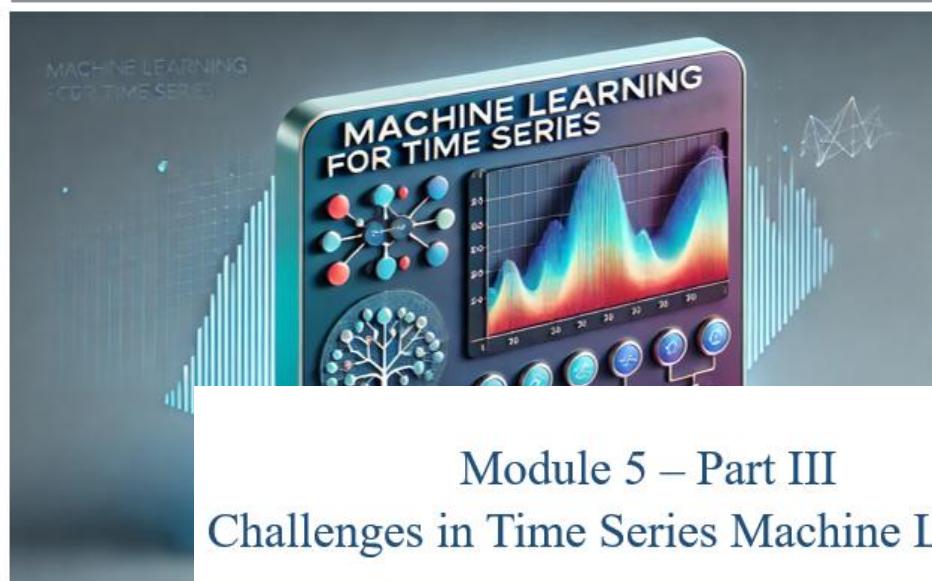


How do machines actually learn?



Module 5 – Part I

Machine Learning For timeseries Forecasting



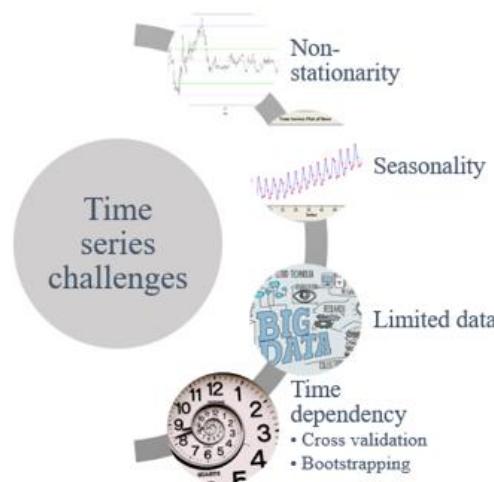
Module 5 – Part II

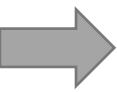
Machine Learning for timeseries Decision Tree based Models

Aspect	Decision Tree (DT)	Random Forest (RF)	XGBoost	CatBoost	LightGBM
1. Sampling Process	Naïve	Naïve	Histogram-based	Feature Binning (Quantization)	GOSS
Method	Greedy	Leaf-wise			
with Trees					Boosting

Module 5 – Part IV

ML for timeseries in Python

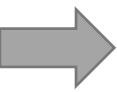




Road map!

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Road map!

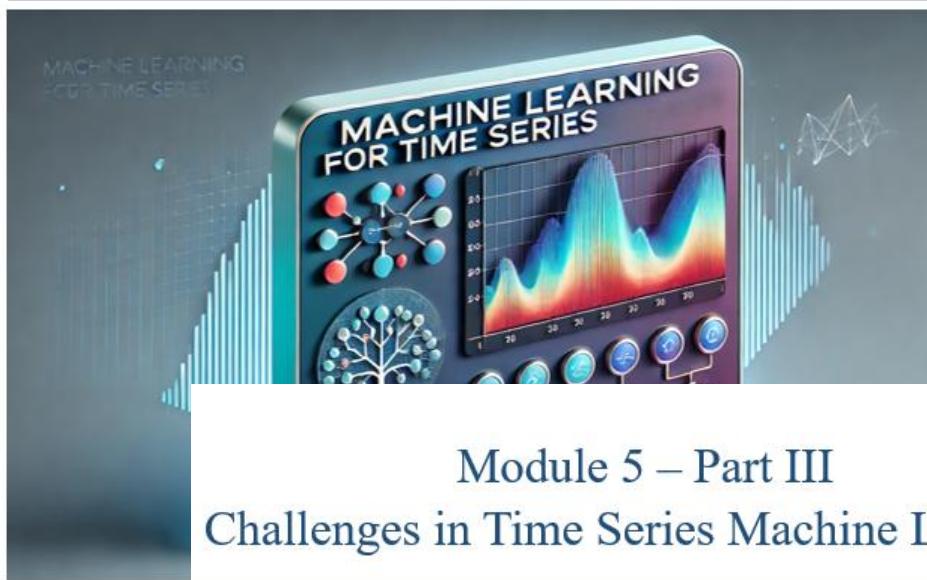
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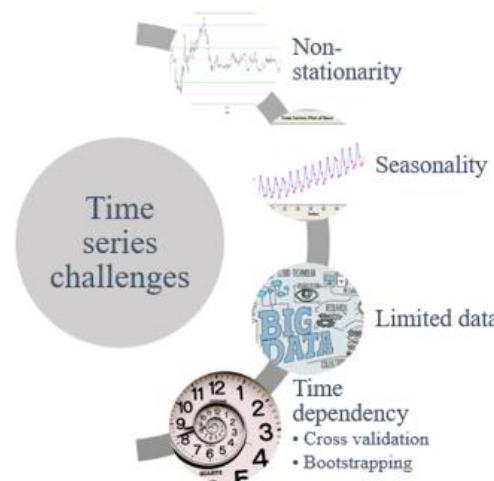
Module 5 – Part I

Machine Learning For timeseries Forecasting



Module 5 – Part III

Challenges in Time Series Machine Learning



✓ Module 5 – Part II

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Module 5 – Part IV

ML for timeseries in Python



Module 5 – Part II

Machine Learning for timeseries

Decision Tree based Models

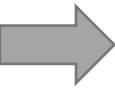
dmlc
XGBoost



LightGBM

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1. Sampling Process	Naïve	Naïve	Histogram-based	Feature Binning (Quantization)	GOSS
2. Splitting Method	Greedy	Greedy	Greedy	Greedy	Greedy
3. Tree Growth Strategy	Depth-wise	Depth-wise	Depth-wise (Leaf-wise)	Symmetric	Leaf-wise
4. Combining Trees	Not applicable	Bagging	Boosting	Boosting	Boosting

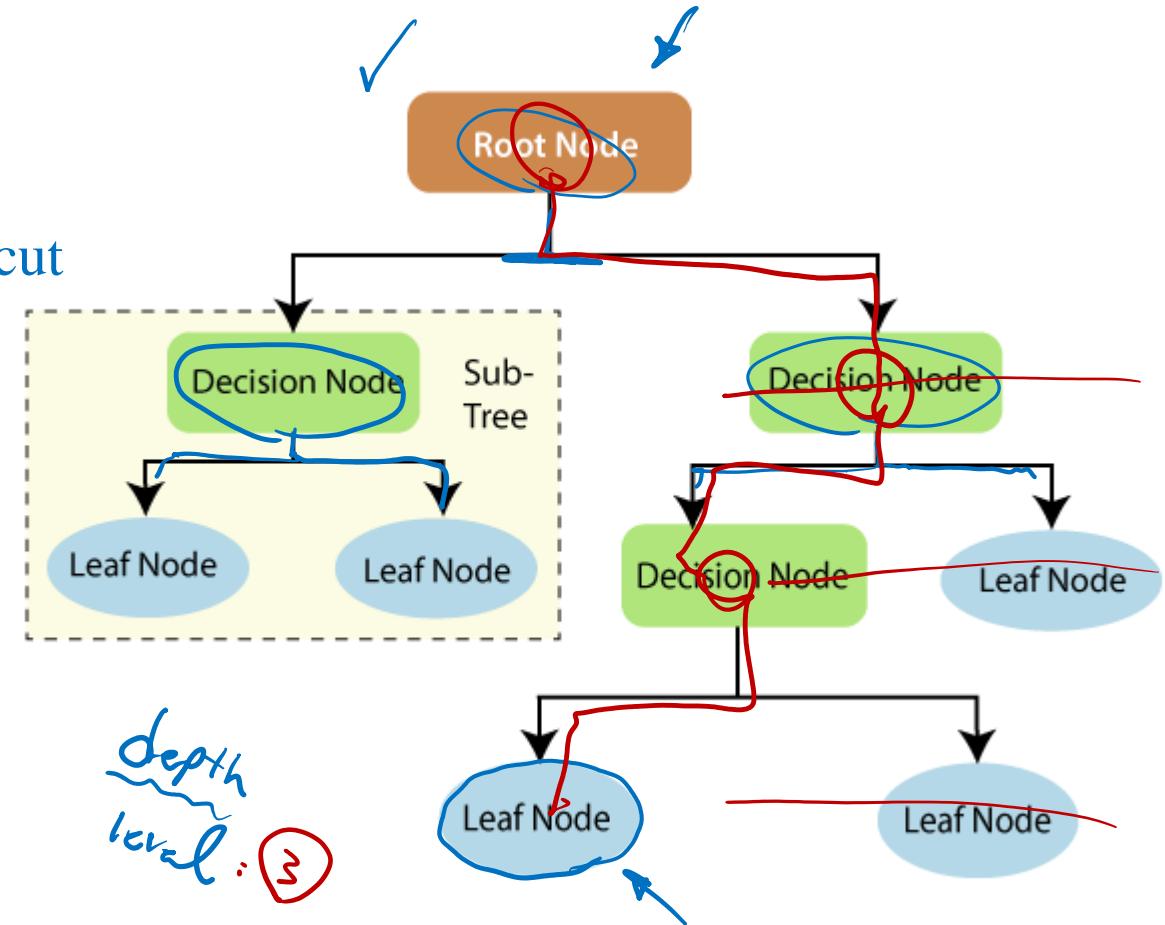


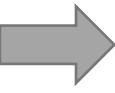


Decision Trees Fundamental questions

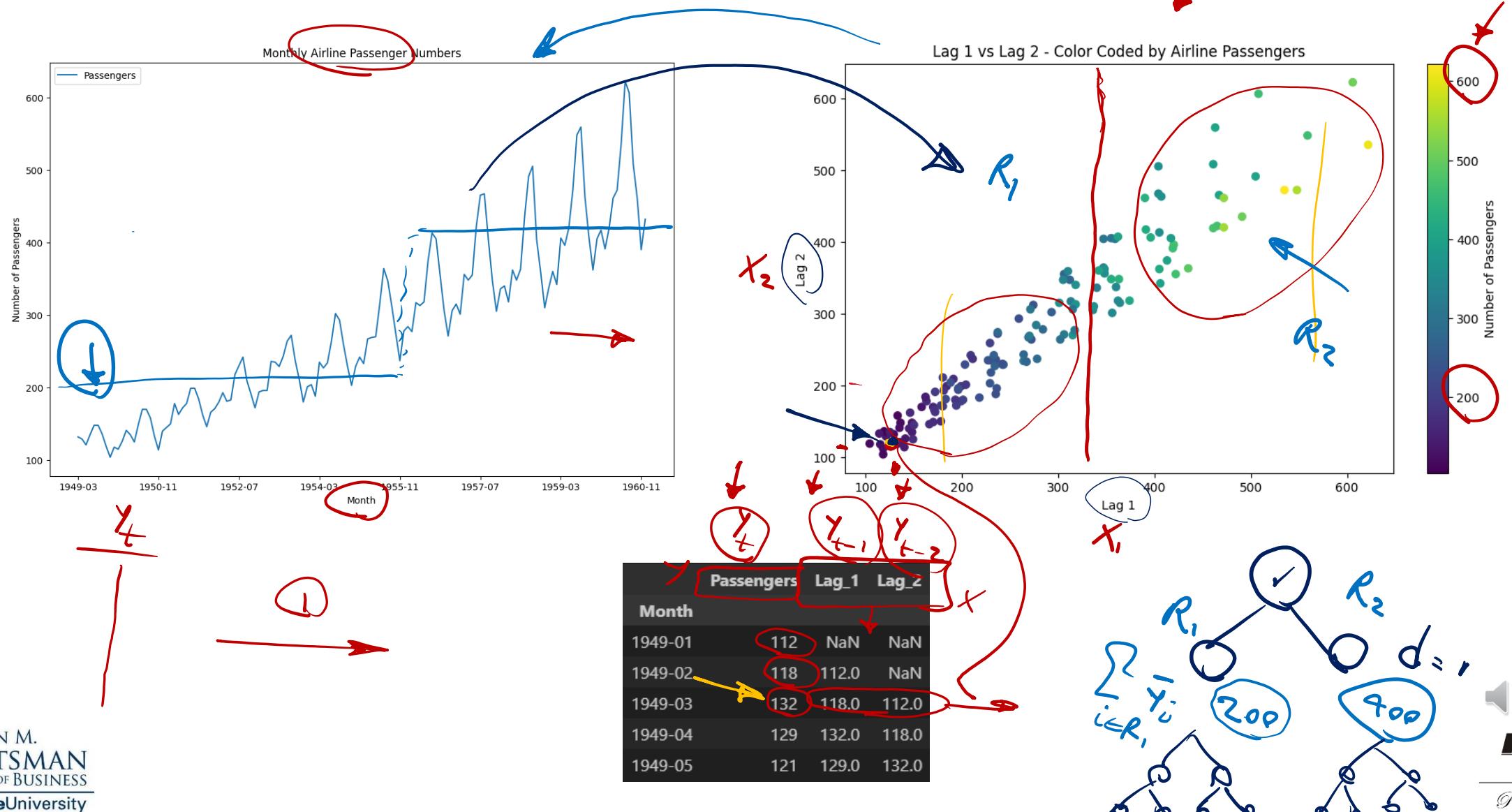
- ✓ • Four fundamental questions to be answered:
 - 1) How to sample the data for splitting?
 - 2) How to split the samples, What feature and cut off to start with?
 - 3) How to grow a tree?
 - 4) How to combine trees?

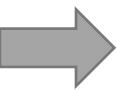
DT, RF, TBoost





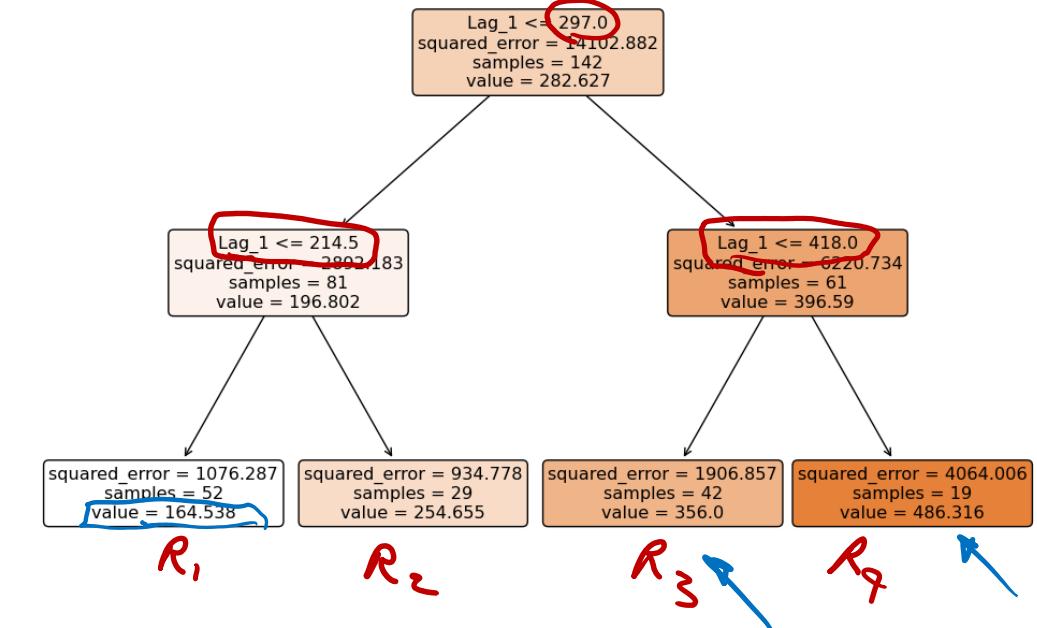
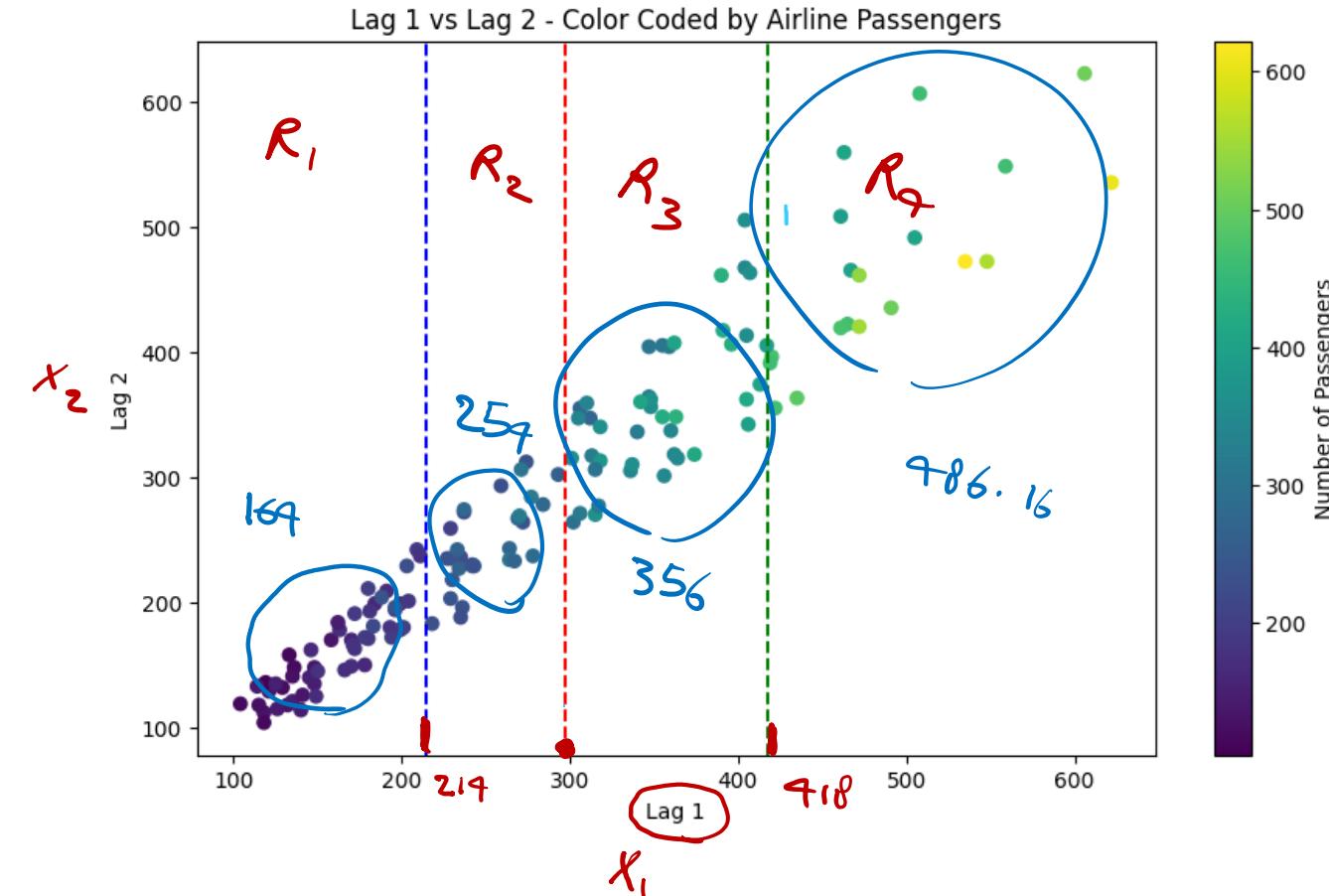
Decision Tree TS regression (Intuition)



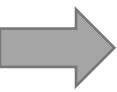


Decision Tree TS regression (Intuition)

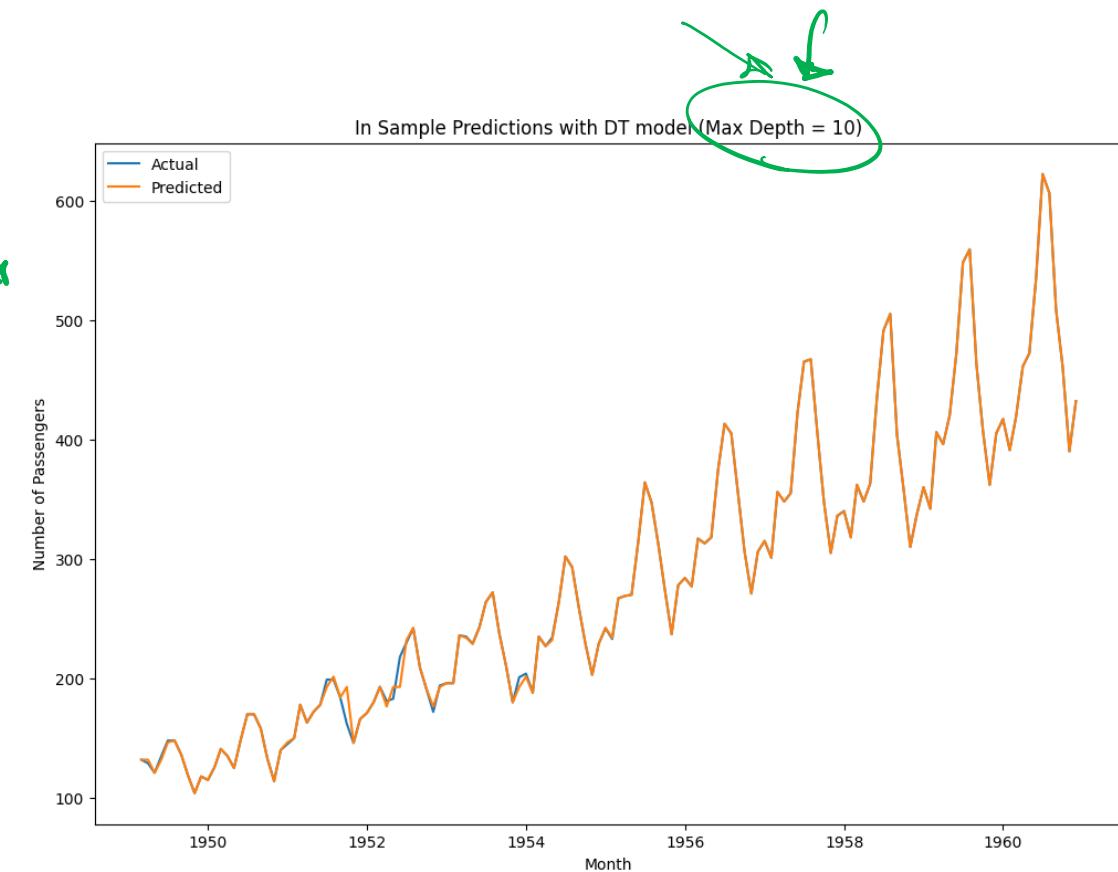
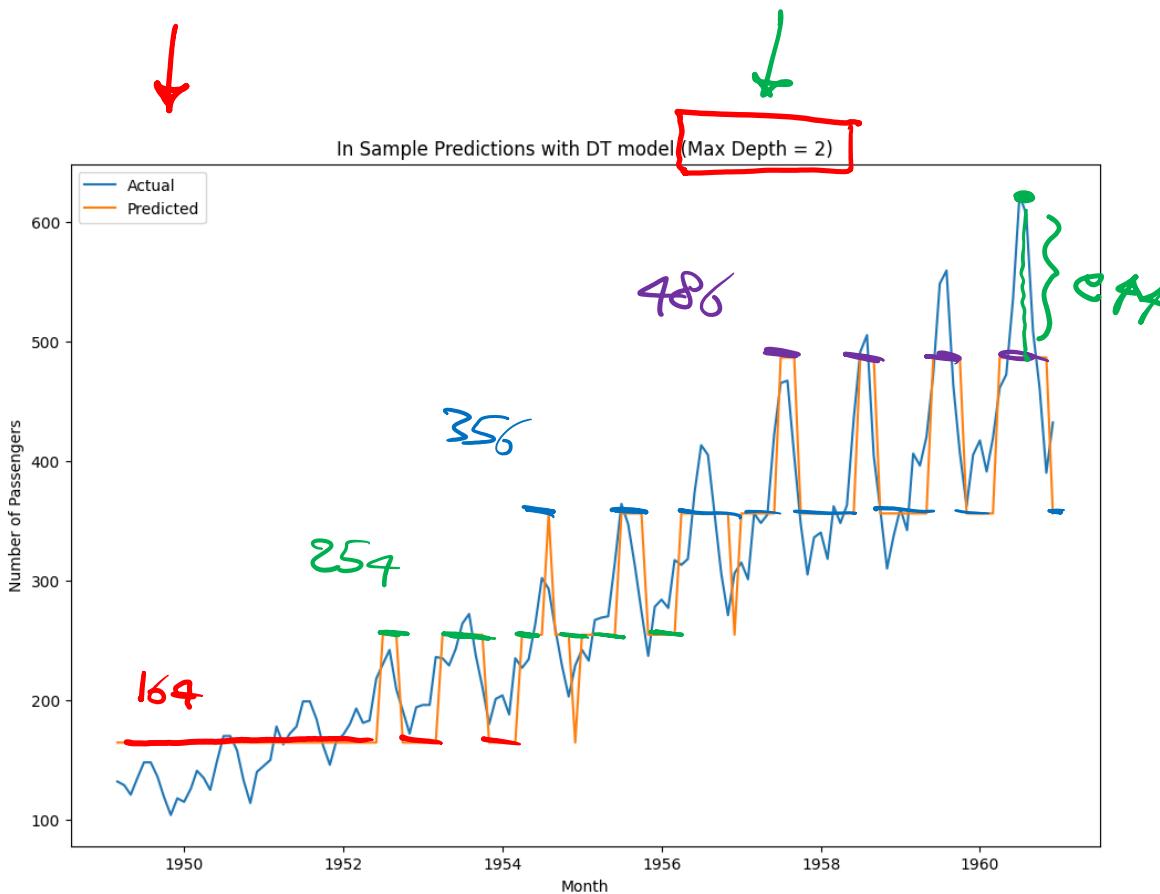
$$\sigma = \sqrt{s}$$



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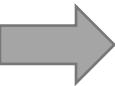
Decision Tree TS regression (Intuition)



RMSE \downarrow

train set RMSE $\rightarrow 0$





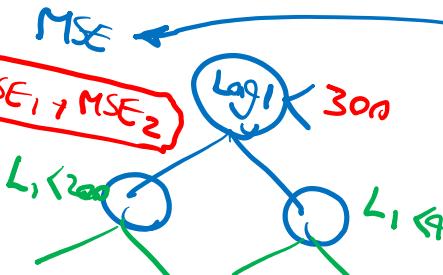
What feature and cut off to start with?

- Which feature and cut off adds the most information gain (minimum impurity)?

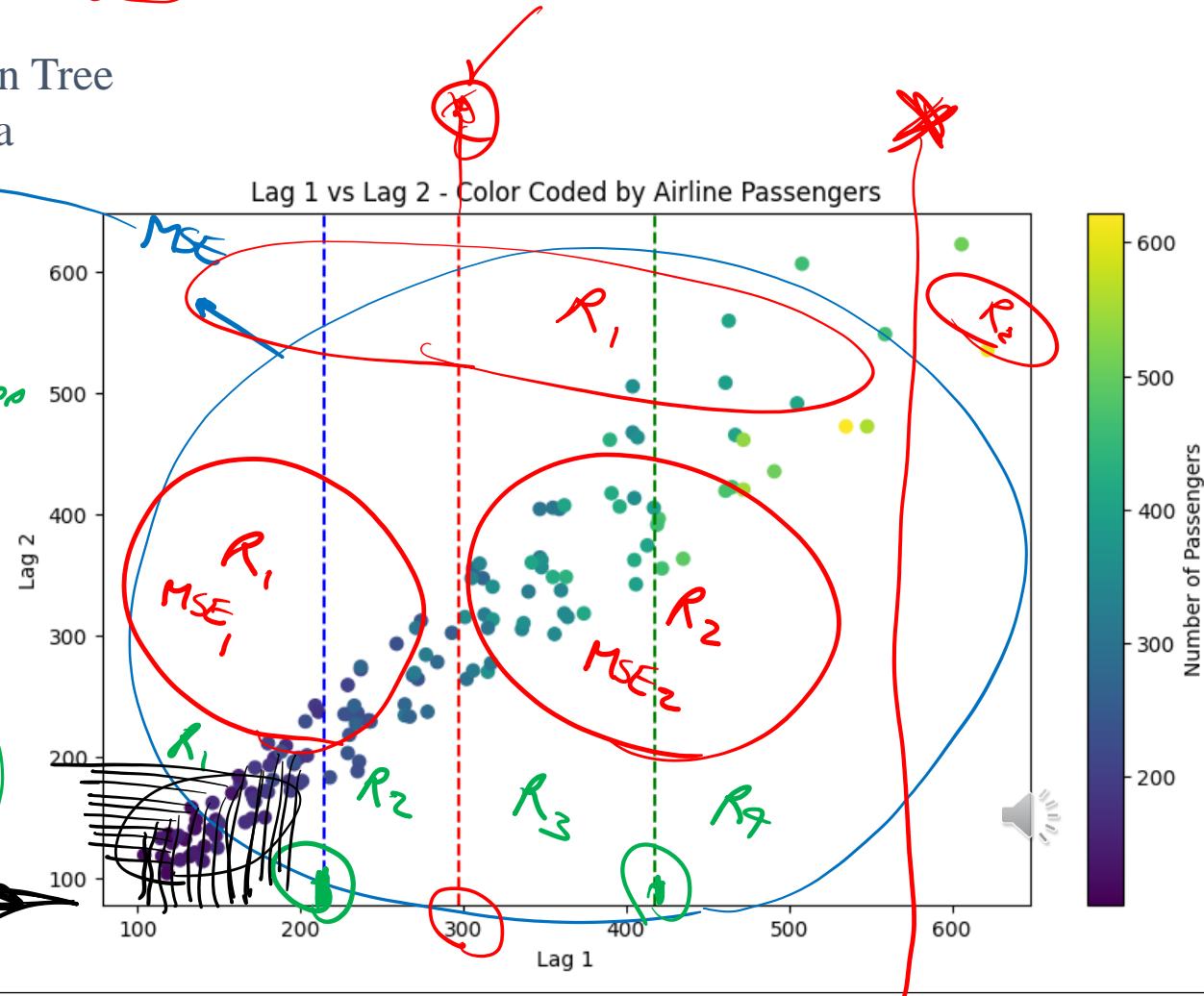
- ✓ • Regression trees: MSE
- ✓ • Classification trees:
 - ✓ 1. Error rate
 - ✓ 2. Entropy
 - ✓ 3. Gini Index

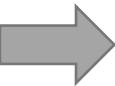
$$\sum_{j=1}^J \sum_{i \in R_j} (y_i - \hat{y}_{R_j})^2$$

Control how a Decision Tree decides to **split** the data



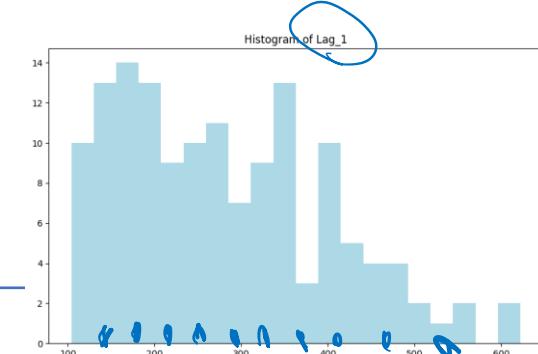
$$\sum_{j=1}^J \text{MSE}_j$$





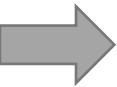
How to sample the data for splitting?

$$x_1 \text{ Lag}_1 (112, -500)$$
$$x_2 \text{ Lag}_2 (112, -500)$$

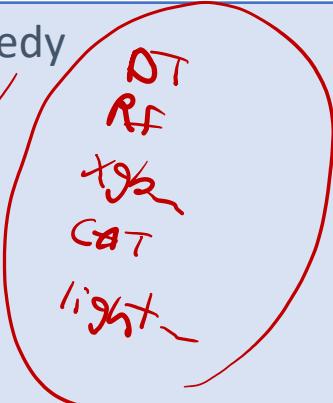


Method	Description
✓ Pre-sorted <u>Naive</u> DT RF	Sorts all data for each feature to evaluate every possible split point. Data is pre-sorted to expedite split evaluation. + Simple and accurate - Computationally intensive
✓ Histogram-Based XGBoost	Bins continuous feature values into discrete intervals (histograms) to reduce the number of potential split points evaluated. + Reduces computational load - May miss optimal splits within bins
✓ GOSS (Gradient-based <u>One-Side Sampling</u>) for Gradient Boosting models only lightGBM	Focuses on samples with large gradients (errors) by retaining them and <u>under-sampling</u> those with <u>small gradients</u> . Adjusts sample weights <u>accordingly</u> . + Reduces computational cost - Adds complexity to the implementation.

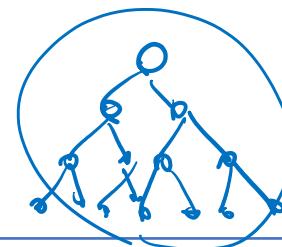
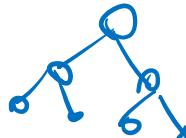




How to Split the Samples? (What Features and Cutoffs to Start With)

Method	Description
<p>Greedy</p> 	<p>At each node, selects the feature and cutoff that provide <u>the greatest immediate reduction in the loss function</u> (e.g., <u>MSE</u>). Decisions are made based solely on local optimization without considering future splits.</p> <ul style="list-style-type: none">+ Simple and computationally efficient- May not lead to the <u>globally optimal tree</u>
<p>Non-Greedy</p> 	<p>Considers the global impact of splits by evaluating <u>future nodes</u> or using <u>global optimization techniques</u>. Methods include optimal decision trees, lookahead splits, evolutionary algorithms, Bayesian trees, and etc.</p> <ul style="list-style-type: none">+ More accurate and generalizable models by avoiding local optima- Computationally intensive and complex

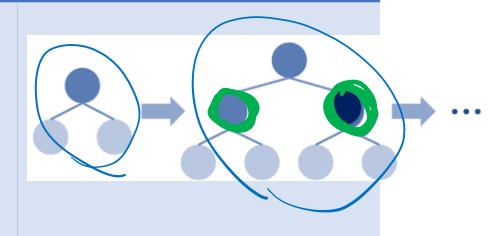
How to grow a tree?



Algorithm

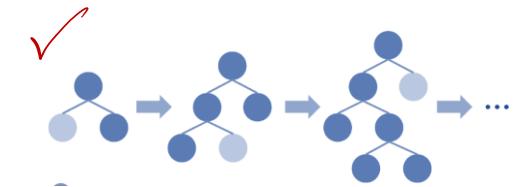
✓ Depth-Wise Level-Wise

This strategy grows the tree **level by level** (one level at a time), all nodes are expanded simultaneously before moving to the next level. This results in a **balanced** tree structure.



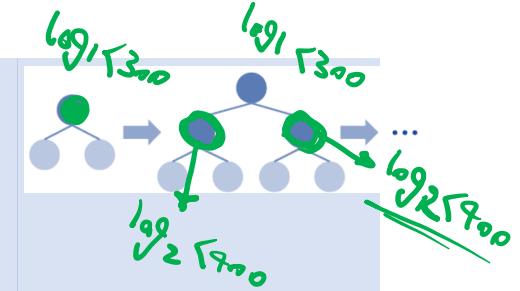
✓ Leaf-wise

This strategy, rather than growing by levels, focuses on expanding the tree **by adding nodes to the leaves**, specifically those that result in the highest decrease in impurity or error. This can lead to a more unbalanced tree but potentially more efficient learning.



✓ Symmetric

This strategy attempts to maintain balance **not just in the depth of the tree but also in how the features are split**, aiming for a tree that grows evenly across all paths. This results in faster compute.



✓ All the methods, repeatedly split the data along the feature with the highest information gain and process continues until a stopping criterion is met (max depth, min samples at nodes, etc)

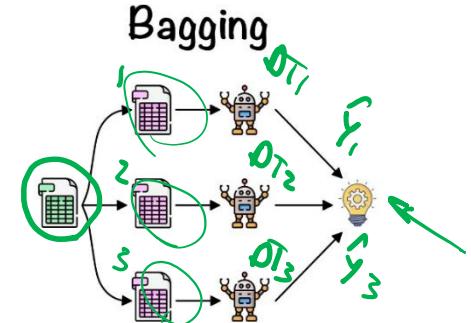


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How to combine trees?

- **Bagging** consists of creating many “copies” of the training data at the same time (each copy is slightly different from another) and then apply the weak learner to each copy to obtain multiple weak models and then combine them.

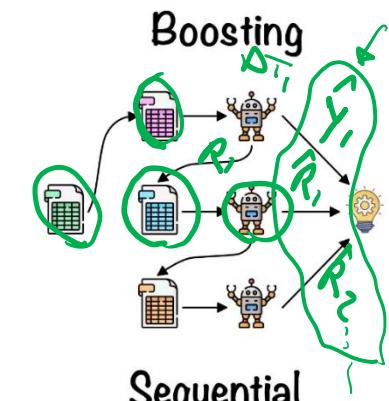
RF



- In bagging, the bootstrapped trees are independent from each other.

- **Boosting** consists of using the “original” training data and iteratively (sequentially) creating multiple models by using a weak learner. Each new model tries to “fix” the errors which previous models make.
- In boosting, each tree is grown using information from previous tree.

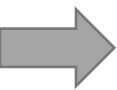
Parallel



Sequential



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Decision-Tree based models

dmlc
XGBoost



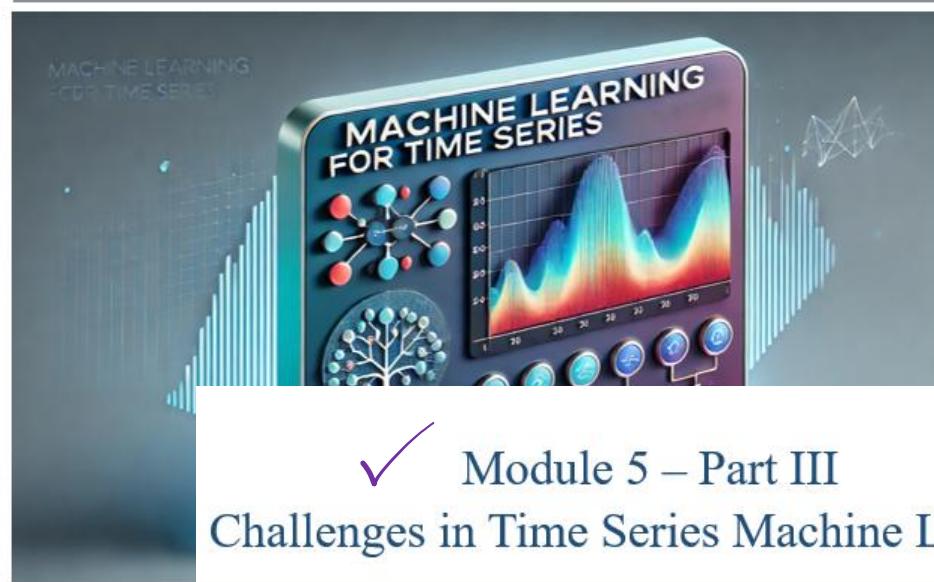
 LightGBM

Aspect	Decision Tree (DT)	Random Forest (RF)	XGBoost	CatBoost	LightGBM
1. Sampling Process	Naïve	Naïve	Histogram-based	Feature Binning (Quantization)	GOSS
2. Splitting Method	Greedy ✓	Greedy ✎	Greedy ✓	Greedy ✓	Greedy ✓
3. Tree Growth Strategy	Depth-wise	Depth-wise	Depth-wise (Leaf-wise) ✓	Symmetric ✓	Leaf-wise ✓
4. Combining Trees	Not applicable	Bagging ✓	Boosting ✓	Boosting ✓	Boosting ✓



Module 5 – Part I ✓

Machine Learning For timeseries Forecasting



Module 5 – Part II

Machine Learning for timeseries Decision Tree based Models

dmlc
XGBoost

CatBoost

LightGBM

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Module 5 – Part IV

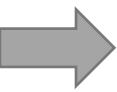
ML for timeseries in Python



PYCARET



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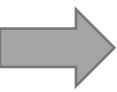


Road map!

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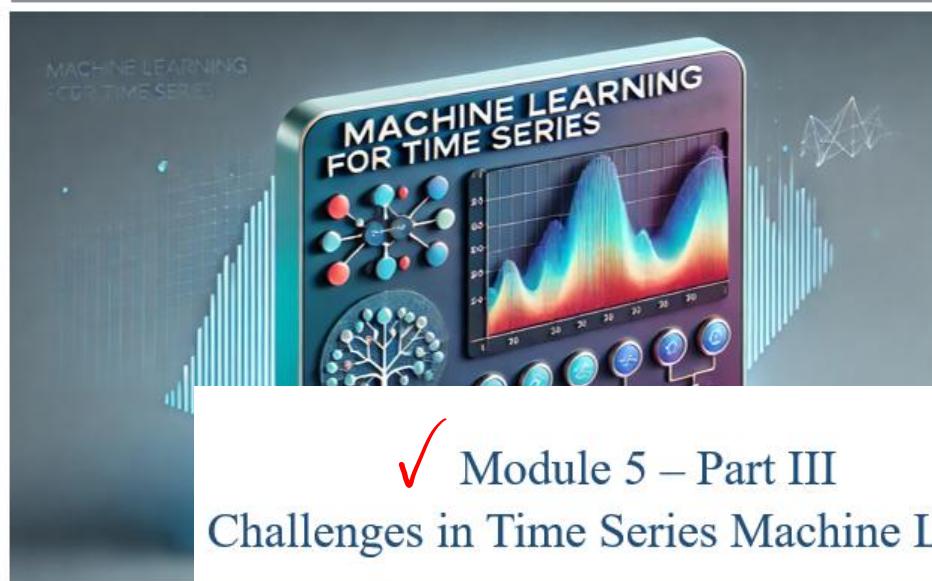
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✓ Module 5 – Part I

Machine Learning For timeseries Forecasting



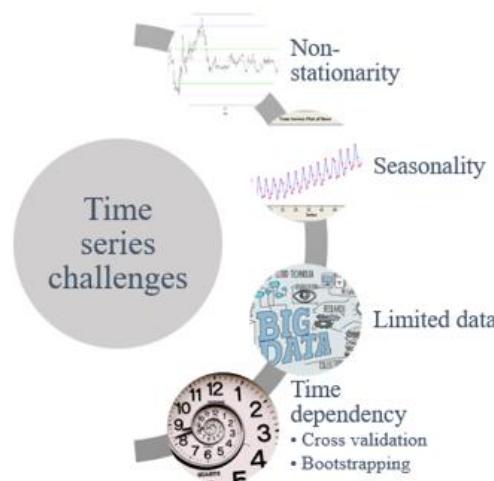
✓ Module 5 – Part II

Machine Learning for timeseries Decision Tree based Models

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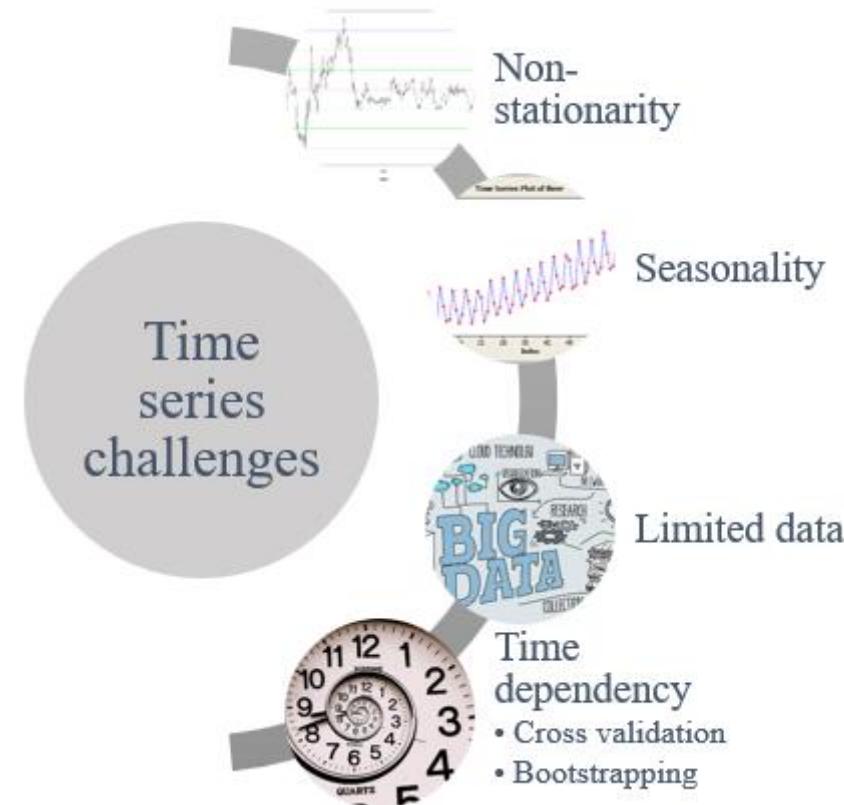
Module 5 – Part IV

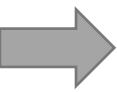
ML for timeseries in Python



Module 5 – Part III

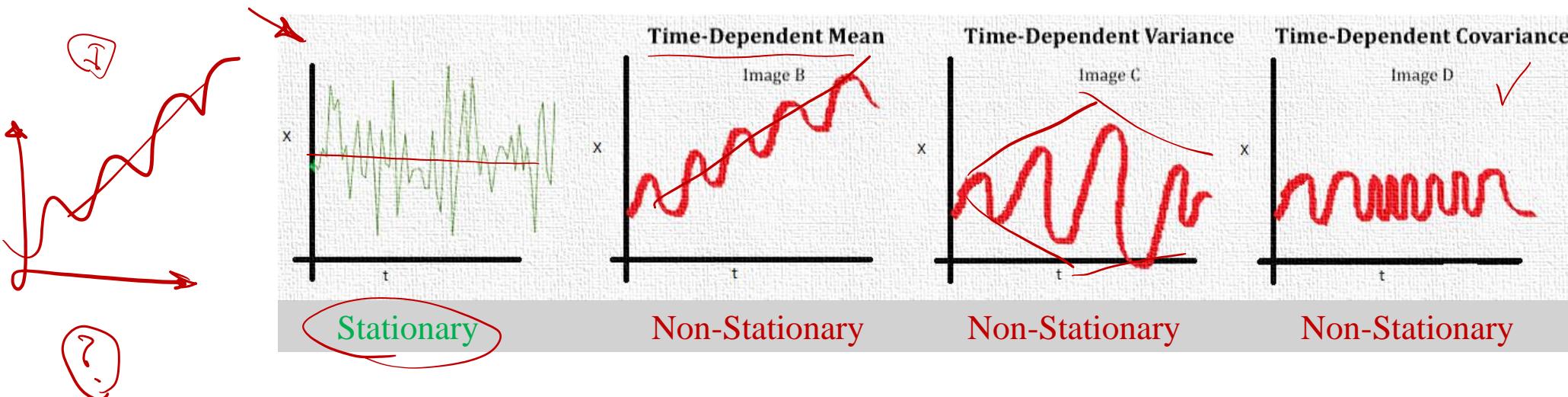
Challenges in Time Series Machine Learning



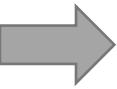


Stationarity

- Stationary vs Non-Stationary Data. What makes a data set **Stationary**?
- ✓ • In a stationary timeseries, the statistical properties **do not depend** on the time



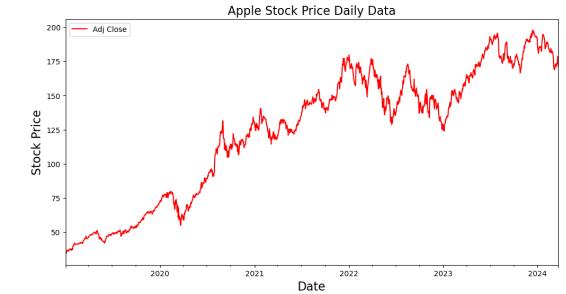
- ✓ • Data with **trend** and **seasonality** are **NOT** stationary!



Time Series Stationarity & ML: Well-Behaved Non-Stationary Data

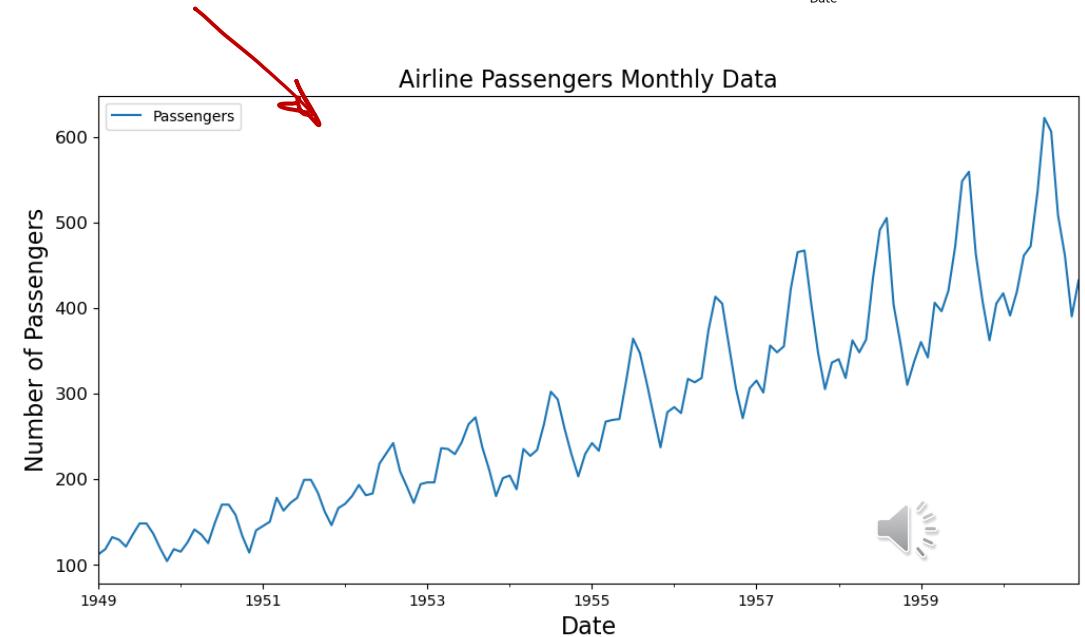
Example: Airline Passenger Data

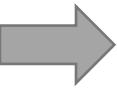
- Shows a **clear** upward trend and seasonal pattern
- Non-stationary but predictable structure



Methods That Can Handle It:

- ✓ ETS: Handles trend and seasonality directly
- ✓ ARIMA: Differencing (the “I”) to remove trend
- ✓ Machine Learning: Lag features and **time-based feature** engineering





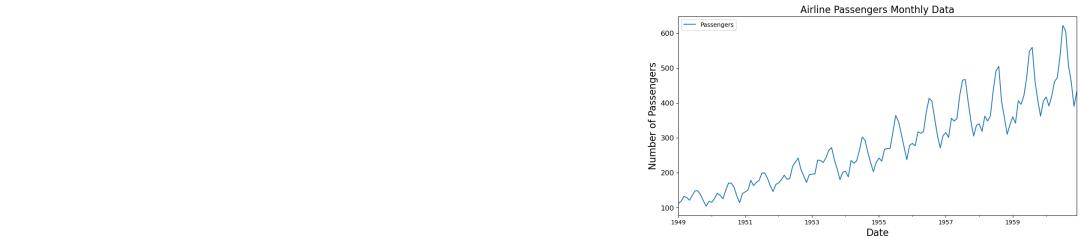
Time Series Stationarity & ML: Complex Non-Stationary Data

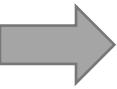
Example: Apple Stock Price

- ✓ • Driven by **external/random** factors (markets, news, events)
- ✓ • May have sudden jumps, volatility, and **regime shifts**

Challenges:

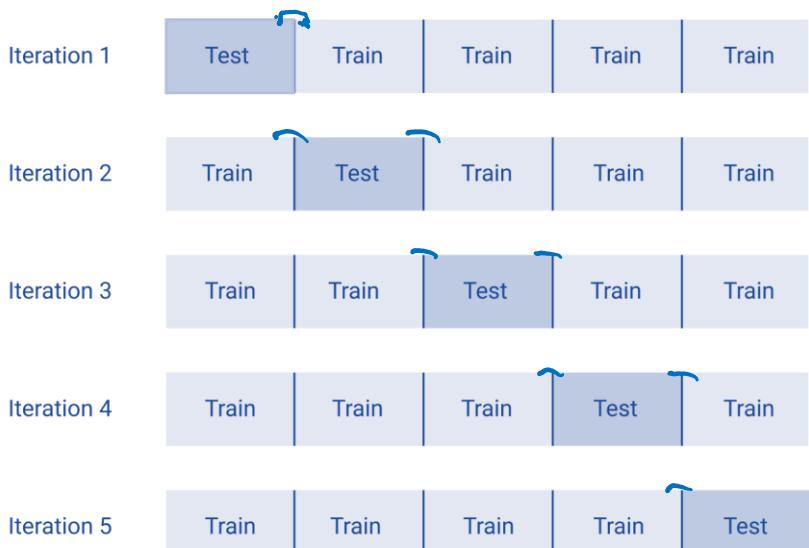
- Simple differencing or trend/seasonality modeling may **not** suffice. Need more advanced techniques:
- ✓ **Additional feature engineering** (e.g., volatility measures, external economic indicators)
- ✓ Regime-switching models (to capture structural breaks)
- ✓ **Deep learning / advanced ML** with more sophisticated patterns



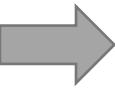


Time Series Cross Validation

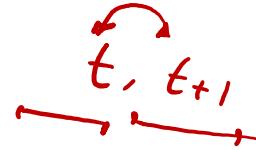
- ✓ With time series data, we **cannot shuffle** the data! TS data is not IID.
- ✓ We also need to avoid **data leakage**!



- The main time series CV methods are:
 - 1) Purged K-Fold CV
 - 2) Walk forward **rolling / expanding** window
 - 3) **Combinatorial purged CV**



Purged K-Fold CV



- **Leakage** takes place when the training set contains information that also appears in the testing set.
- Leakage will enhance the model performance
- Solution: **Purging** and **Embargoing**
- **Purged K-Fold CV:** Adding purging and embargoing whenever we produce a train/test split in K-Fold CV.

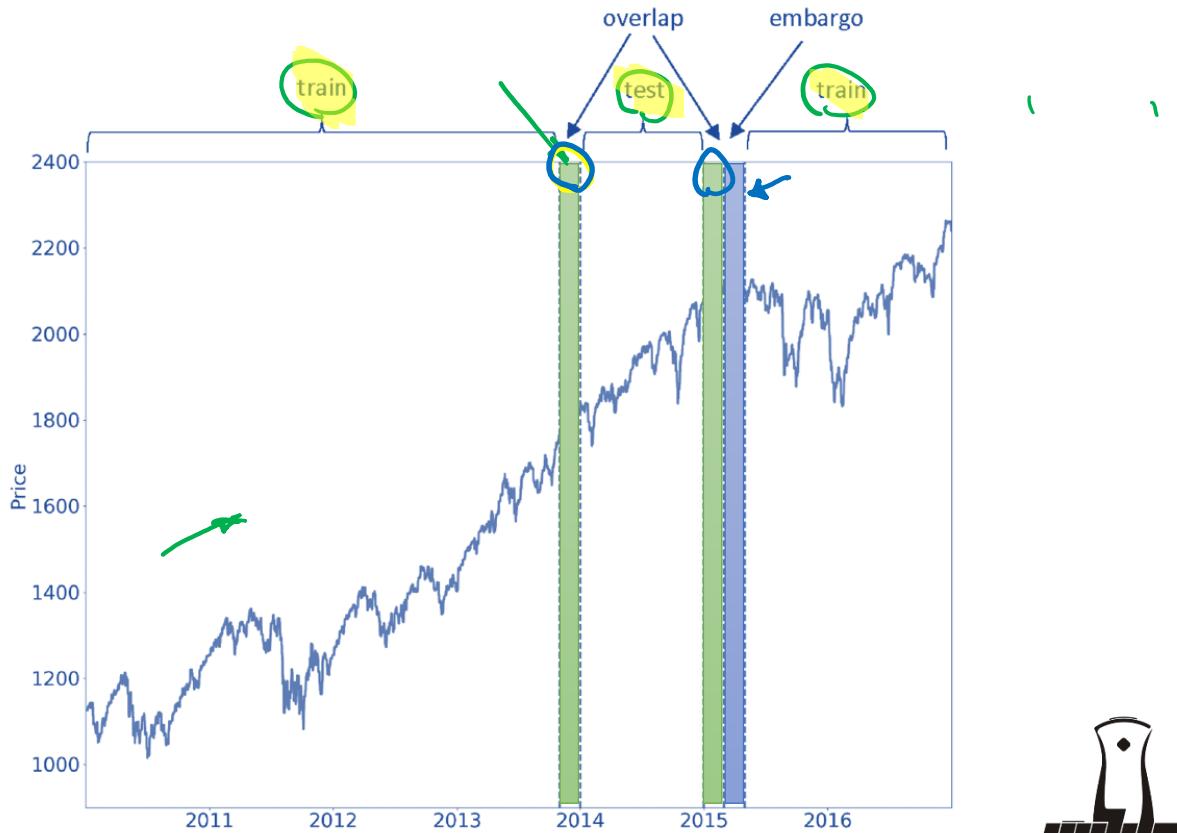
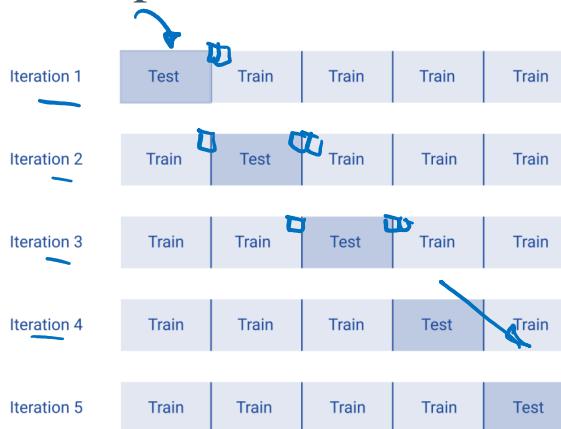
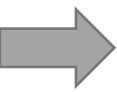


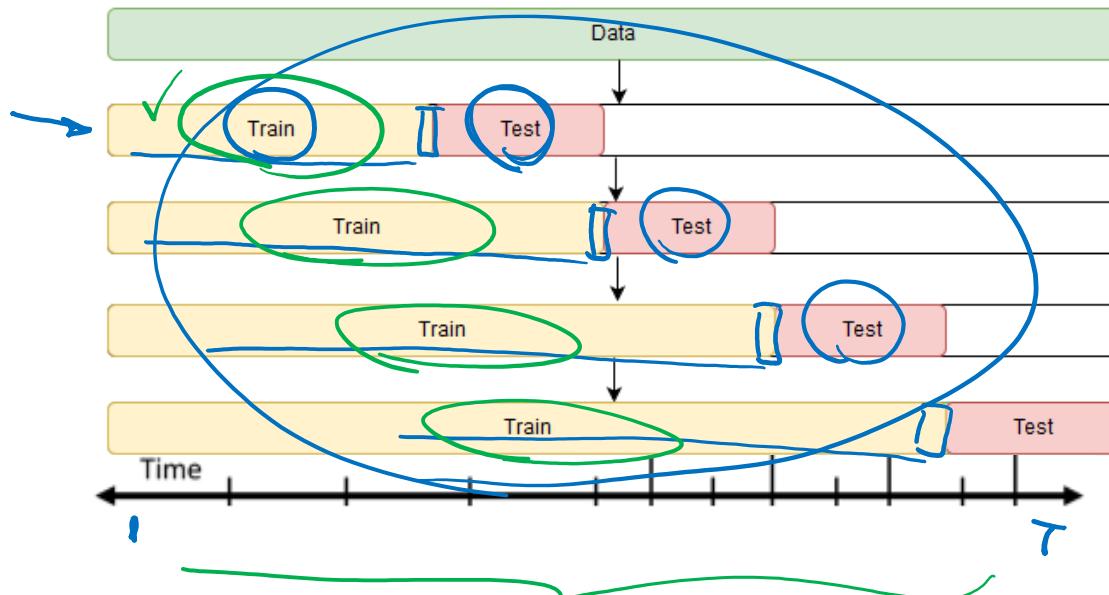
FIGURE 7.3 Embargo of post-test train observations





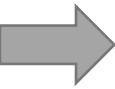
Walk Forward Cross Validation

✓ Walk forward cross validation
Expanding windows



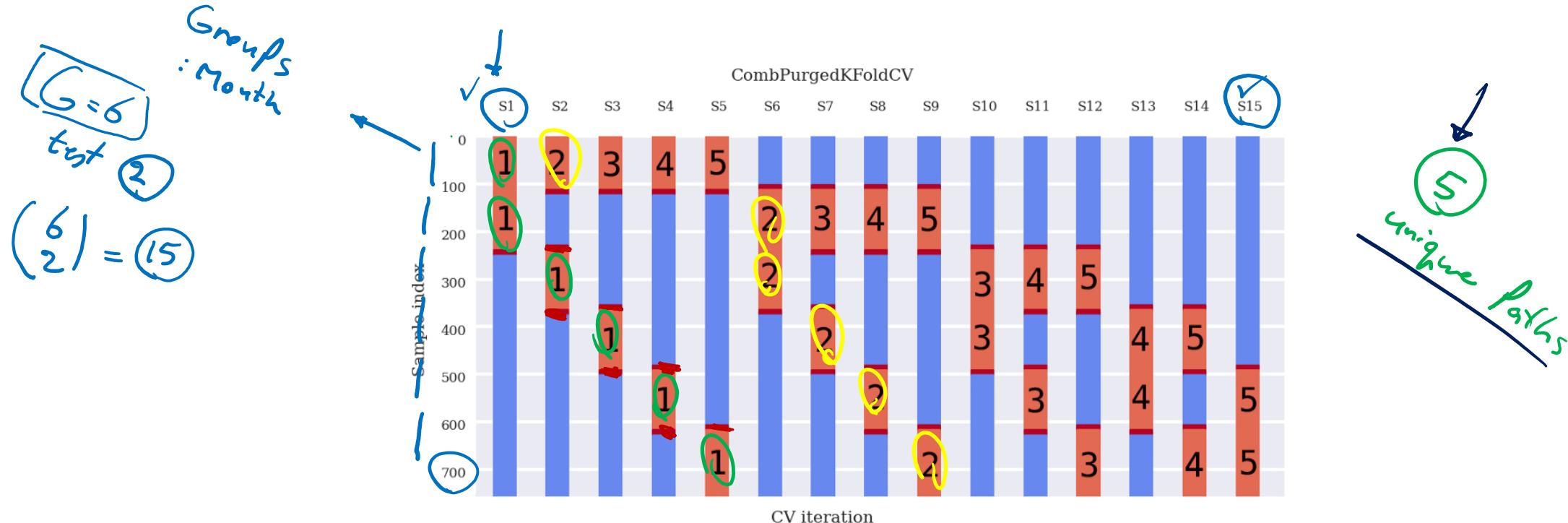
✓ Walk forward cross validation
Rolling windows





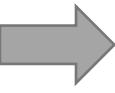
Combinatorial Purged Cross Validation (CPCV)

- ✓ The goal is to generate multiple unique back-test path that span the entire data set.
- ✓ In each path, we can look at the model's **OOS performance** for the entire time period.



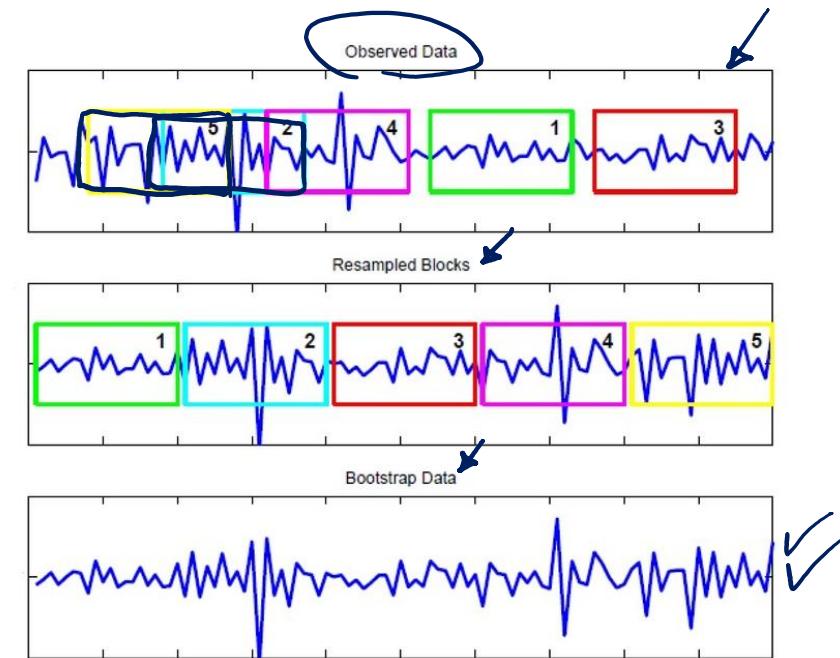
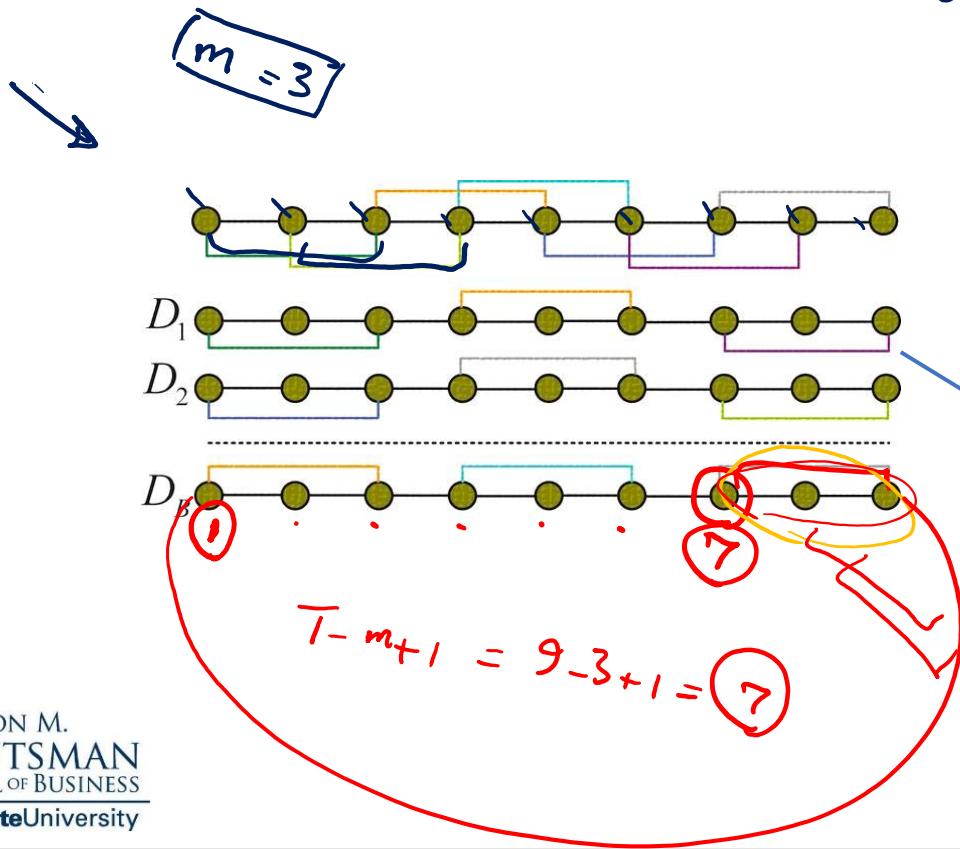
Time Series Bootstrapping

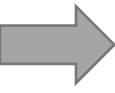
- IID bootstrapping (random sample with replacement) does not work for time series data with temporal dependency.
- Time series Bootstrapping methods:
 - ✓ • Parametric (based on models with **iid residuals** and resampling from residuals.
Example: ARIMA bootstrap)
 - ✓ • Non-parametric **block** bootstrap (data is directly resampled. Assumption: blocks can be samples so that they are **approximately iid**)
 - Moving Block Bootstrap (MBB)
 - Circular Block Bootstrap (CBB)
 - Stationary Bootstrap (SB)



Moving Block Bootstrap (MBB)

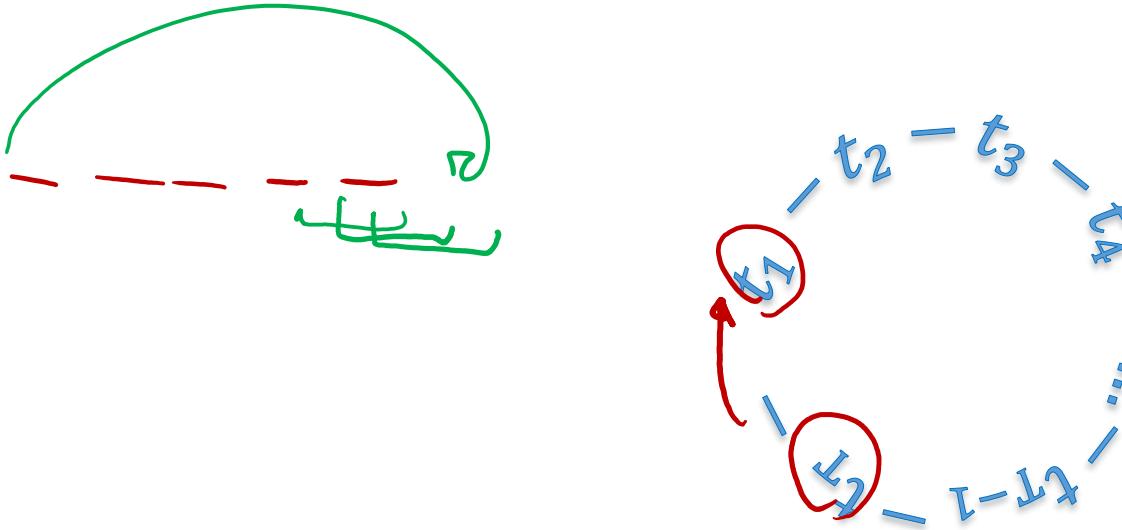
- Moving Block Bootstrap, samples overlapping fixed size blocks of m consecutive observations.
- Blocks starts at indices $1, \dots, \underbrace{T-m+1}$

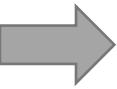




Circular Block Bootstrap (CBB)

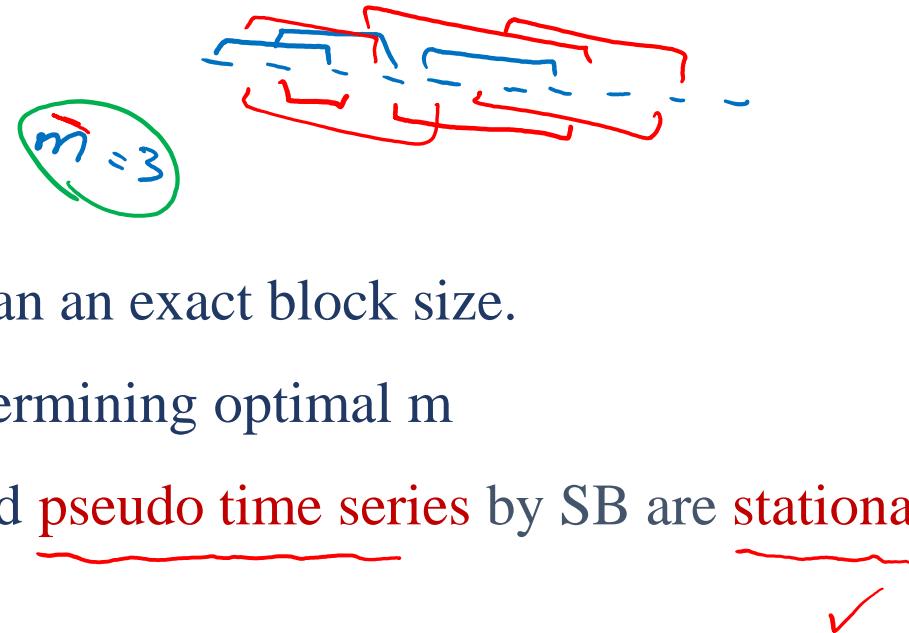
- ✓ • CBB is a simple extension of MBB which assumes the data live on a circle so that $y_{T+1} = y_1$, $y_{T+2} = y_2$, etc.
- ✓ • CBB has better finite sample properties since all data points get sampled with equal probability.





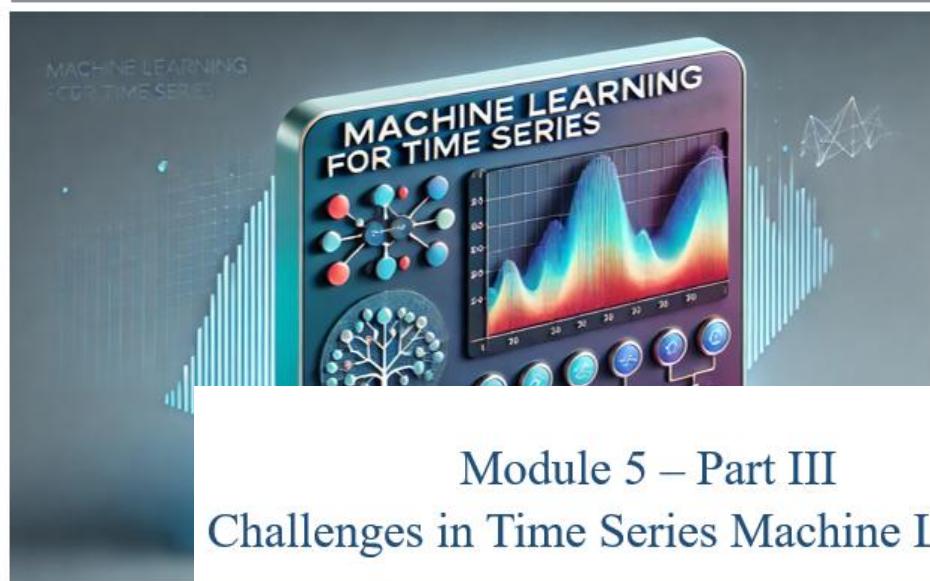
Stationary Bootstrap (SB)

- ✓ • In SB, the **block size** is no longer fixed.
- ✓ • Chooses an **average block size** of m rather than an exact block size.
- ✓ • Popularity of SB stems from difficulty in determining optimal m
- ✓ • Once applied to stationary data, the resampled pseudo time series by SB are stationary.
This is not the case for MBB and CBB.



Module 5 – Part I

Machine Learning For timeseries Forecasting



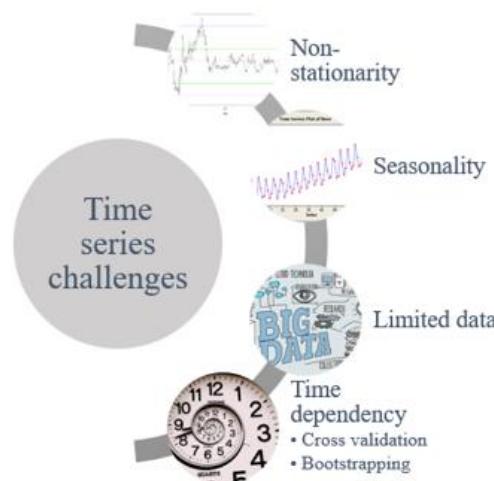
Module 5 – Part II

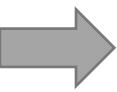
Machine Learning for timeseries Decision Tree based Models

Aspect	Decision Tree (DT)	Random Forest (RF)	XGBoost	CatBoost	LightGBM
1. Sampling Process	Naïve	Naïve	Histogram-based	Feature Binning (Quantization)	GOSS
Method	Greedy	Leaf-wise			
with Trees					Boosting

Module 5 – Part IV

ML for timeseries in Python



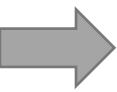


Road map!

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- ✓ Module 2- Setting up Deep Forecasting Environment
- ✓ Module 3- Exponential Smoothing
- ✓ Module 4- ARIMA models
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 - Module 6- Deep Neural Networks
 - Module 7- Deep Sequence Modeling (RNN, LSTM)
 - Module 8- Prophet and Neural Prophet



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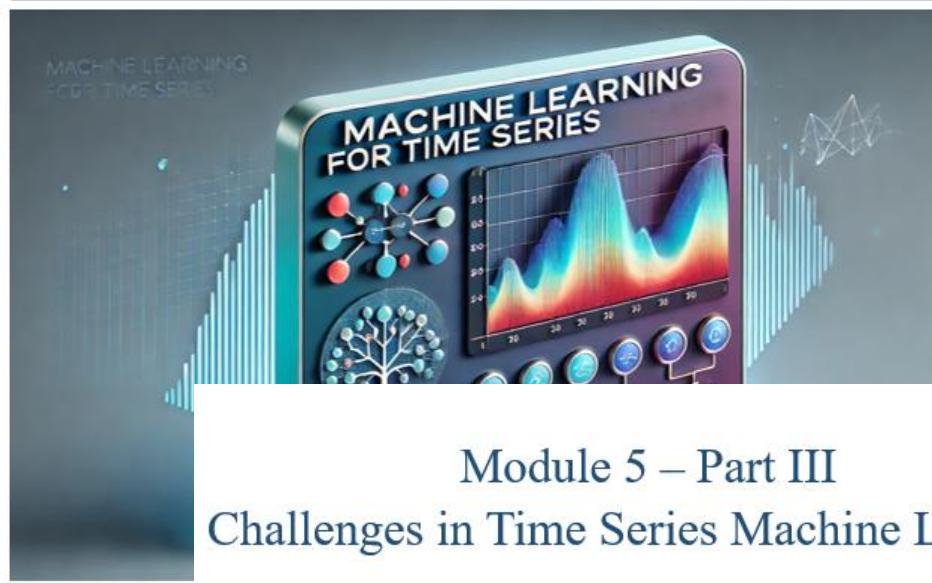
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- Miscellaneous topics



Module 5 – Part I

Machine Learning For timeseries Forecasting



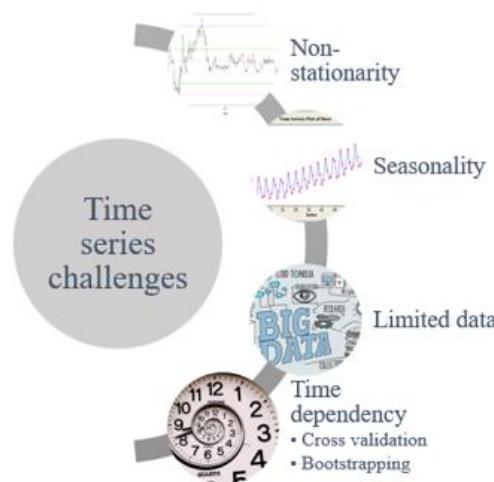
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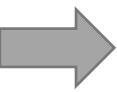


Module 5 – Part IV

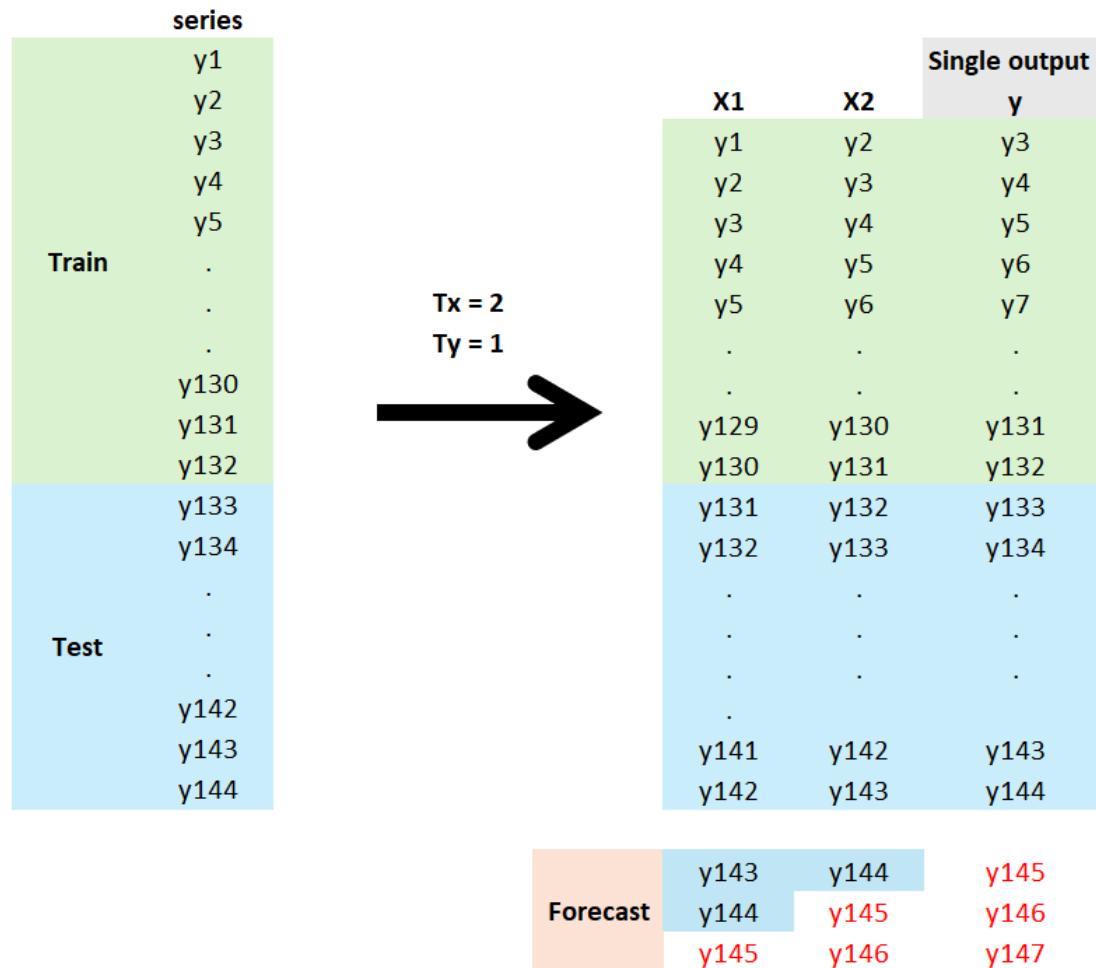


ML for timeseries in Python



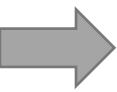


Single-Output

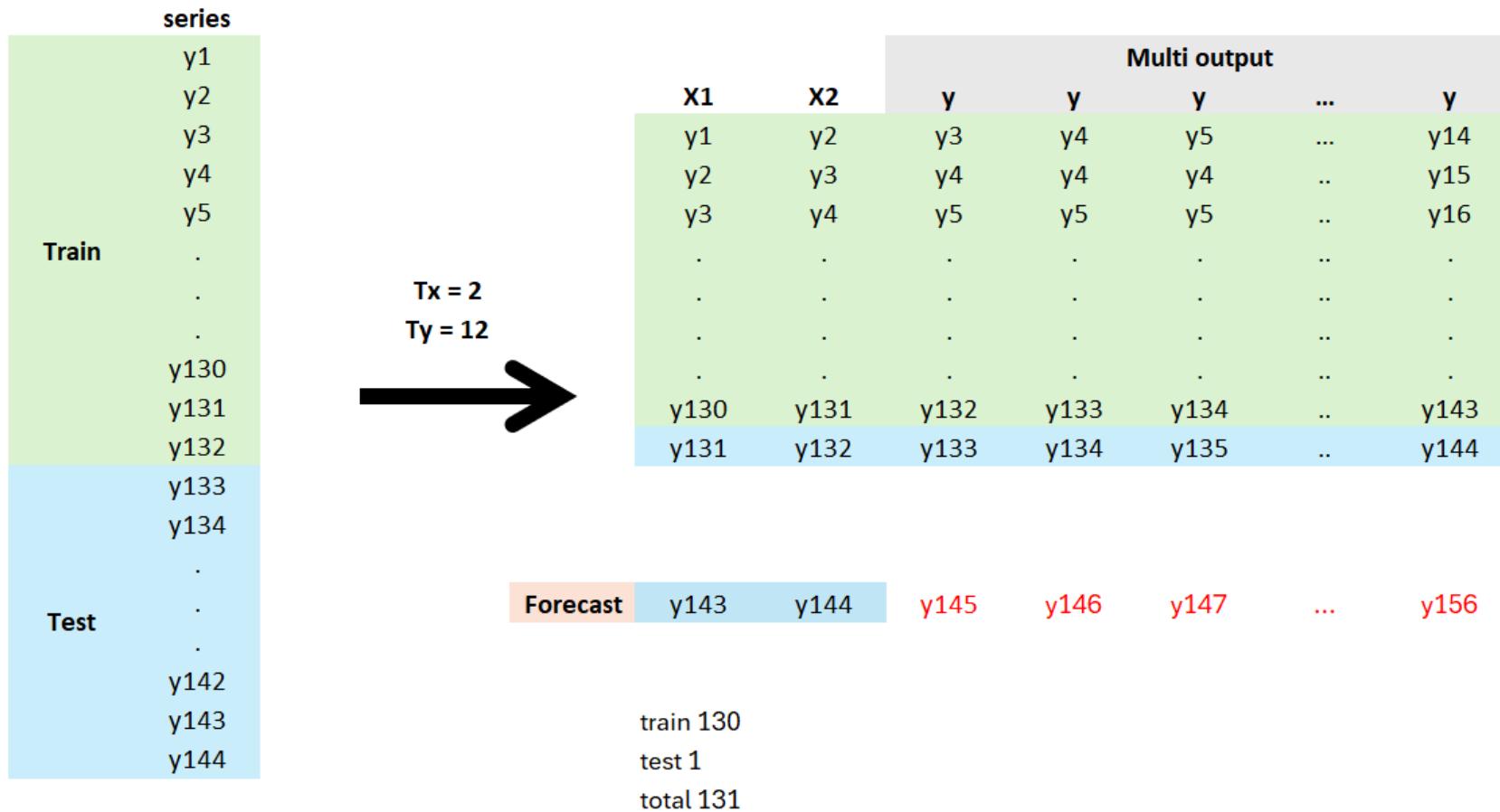


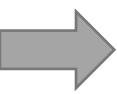
train 132
test 12
total 144

train 130
test 12
total 142



Multi-Output





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