Type Lattice

$$\frac{n_1 < n_2}{uint\langle n_1 \rangle <: uint\langle n_2 \rangle} \qquad \frac{n_1 < n_2}{int\langle n_1 \rangle <: int\langle n_2 \rangle} \qquad \frac{\tau_1 <: \tau_2 \qquad \Gamma \vdash e : \tau_1}{\Gamma \vdash e : \tau_2}$$

Expressions

$$\begin{array}{ll} \text{VAR} & \text{UNOP} \\ \underline{\Gamma(x) = \tau} \\ \hline \Gamma \vdash x : \tau \end{array} & \begin{array}{l} \underline{\Gamma \vdash e : \tau} & \ominus : \tau \to \tau \\ \hline \Gamma \vdash e : \tau & \ominus : \tau \to \tau \end{array} & \begin{array}{l} \underline{\Gamma \vdash e_1 : \tau_1} & \Gamma \vdash e_2 : \tau_2 & \ominus : \tau_1 \to \tau_2 \to \tau_3 \\ \hline \Gamma \vdash e_1 \oplus e_2 : \tau_3 \end{array} \\ \\ \underline{\frac{\text{ARRGet}}{\Gamma \vdash e : uint \langle max \rangle}} & \begin{array}{l} \underline{\Gamma \vdash a : array \langle \tau, n \rangle} \\ \hline \Gamma \vdash a [e] : \tau \end{array} \\ \end{array}$$

$$\frac{\text{FnCall}}{\mathbb{F}(f) = f decf(x_1 : \tau_1, \dots, x_n : \tau_n) : \tau_r \qquad \Gamma \vdash e_1 : \tau_1 \qquad \cdots \qquad \Gamma \vdash e_n : \tau_n}{\Gamma \vdash f(e_1, \dots, e_n) : \tau_r} \qquad \frac{\text{True}}{\Gamma \vdash true : bool}$$

False
$$\begin{array}{c} \text{ArrLiteral} \\ \forall i: \Gamma \vdash e_i: \tau \\ \hline \Gamma \vdash false: bool \end{array} \qquad \begin{array}{c} \text{PosNumber} \\ \ell >= 0 \quad n = \lceil \log_2 \ell \rceil \\ \hline \Gamma \vdash [e_1, \ldots, e_n]: array \langle \tau, n \rangle \end{array} \qquad \begin{array}{c} \text{PosNumber} \\ \ell >= 0 \quad n = \lceil \log_2 \ell \rceil \\ \hline \Gamma \vdash \ell: uint \langle n \rangle \end{array}$$

 $\Gamma \vdash \ell : int\langle n \rangle$