

x	term variable	
f	function declaration?	
cnt	program counter	
n	index variable	
k	index variable	
v	$::=$	values
	c	numeric value
	a	bytearray
e	$::=$	expressions
	x	variable
	c	numeric value
	a	bytearray
	$x[e]$	array access
	$\sim e$	unary operation
	$e_1 \oplus e_2$	binary operation
	$f(e_1, \dots, e_n)$	function application
s	$::=$	statements
	skip	skip
	$s_1; s_2$	sequence
	def $x := e$	variable declaration
	$x := e$	variable assignment
	$x[e_1] := e_2$	array assignment
	for x from v_1 to v_2 : s	for loop
	return e	return statement
$fdef$	$::=$	function definitions
	$fdef\ f(x_1, \dots, x_n) : s$	
$program$	$::=$	program
	$fdef_1; \dots; fdef_n; \mathbf{expose}\ fdef$	list of fdefs
fm	$::=$	function store
	\emptyset_{fm}	empty function store
	$fm, f(v_1, \dots, v_k) = s; \mathbf{return}\ e$	define function
m	$::=$	memory
	\emptyset_m	empty memory
	$m[x := v]$	add/update variable
	m/x	remove variable

$$\boxed{\{fm, m, cnt\}e \longrightarrow \{fm', m', cnt'\}e'} \quad e \text{ reduces to } e'$$

$$\begin{array}{c}
m = m'[x := v] \\
cnt' = cnt + 1 \\
\hline
\{fm, m, cnt\}x \longrightarrow \{fm, m, cnt'\}v \quad \text{EXR_VAR} \\
\\
\frac{\{fm, m, cnt\}e \longrightarrow \{fm, m, cnt'\}e'}{\{fm, m, cnt\}x[e] \longrightarrow \{fm, m, cnt'\}x[e']} \quad \text{EXR_ARR_GET_EXPR}
\end{array}$$

$$\begin{array}{c}
\frac{m = m'[x := \mathbf{a}] \quad v' = a[v] \quad cnt' = cnt + 1}{\{fm, m, cnt\}x[v] \longrightarrow \{fm, m, cnt'\}v'} \text{EXR_ARR_GET_VAL} \\
\frac{\{fm, m, cnt\}e \longrightarrow \{fm, m, cnt'\}e'}{\{fm, m, cnt\} \sim e \longrightarrow \{fm, m, cnt'\} \sim e'} \text{EXR_UNOP_EXPR} \\
\frac{v' \equiv \llbracket \sim v \rrbracket \quad cnt' = cnt + 1}{\{fm, m, cnt\} \sim v \longrightarrow \{fm, m, cnt'\}v'} \text{EXR_UNOP_VAL} \\
\frac{\{fm, m, cnt\}e_1 \longrightarrow \{fm, m, cnt'\}e'_1}{\{fm, m, cnt\}e_1 \oplus e_2 \longrightarrow \{fm, m, cnt'\}e'_1 \oplus e_2} \text{EXR_BINOP_L} \\
\frac{\{fm, m, cnt\}e_2 \longrightarrow \{fm, m, cnt'\}e'_2}{\{fm, m, cnt\}v \oplus e_2 \longrightarrow \{fm, m, cnt'\}v \oplus e'_2} \text{EXR_BINOP_R} \\
\frac{v_3 \equiv \llbracket v_1 \oplus v_2 \rrbracket \quad cnt' = cnt + 1}{\{fm, m, cnt\}v_1 \oplus v_2 \longrightarrow \{fm, m, cnt'\}v_3} \text{EXR_BINOP_VAL} \\
\frac{\{fm, m, cnt\}e_1 \longrightarrow \{fm, m, cnt'\}e'_1}{\{fm, m, cnt\}f(v_1, \dots, v_k, e_1, e_2, \dots, e_n) \longrightarrow \{fm, m, cnt'\}f(v_1, \dots, v_k, e'_1, e_2, \dots, e_n)} \text{EXR_FN_EXPR} \\
\frac{fm = fm', f(v_1, \dots, v_k) = s; \mathbf{return} \ e}{\{fm, m, cnt\}f(v_1, \dots, v_k) \longrightarrow \{fm, m, cnt'\}e} \text{EXR_FN_CALL} \\
\boxed{\{fm, m, cnt\}s \longrightarrow \{fm', m', cnt'\}s'} \quad s \text{ reduces to } s'
\end{array}$$

$$\begin{array}{c}
\frac{}{\{fm, m, cnt\}\mathbf{skip}; s \longrightarrow \{fm, m, cnt\}s} \text{STR_SKIP} \\
\frac{\{fm, m, cnt\}s_1 \longrightarrow \{fm, m', cnt'\}s'_1}{\{fm, m, cnt\}s_1; s_2 \longrightarrow \{fm, m', cnt'\}s'_1; s_2} \text{STR_SEQ} \\
\frac{\{fm, m, cnt\}e \longrightarrow \{fm, m, cnt'\}e'}{\{fm, m, cnt\}\mathbf{def} \ x := e \longrightarrow \{fm, m, cnt'\}\mathbf{def} \ x := e'} \text{STR_DEF_EXPR} \\
\frac{cnt' = cnt + 1 \quad m' = m[x := v]}{\{fm, m, cnt\}\mathbf{def} \ x := v \longrightarrow \{fm, m', cnt'\}\mathbf{skip}} \text{STR_DEF_VAL} \\
\frac{\{fm, m, cnt\}e \longrightarrow \{fm, m, cnt'\}e'}{\{fm, m, cnt\}x := e \longrightarrow \{fm, m, cnt'\}x := e'} \text{STR_ASSIGN_EXPR} \\
\frac{cnt' = cnt + 1 \quad m' = m[x := v]}{\{fm, m, cnt\}x := v \longrightarrow \{fm, m', cnt'\}\mathbf{skip}} \text{STR_ASSIGN_VAL} \\
\frac{\{fm, m, cnt\}e_1 \longrightarrow \{fm, m, cnt'\}e'_1}{\{fm, m, cnt\}x[e_1] := e_2 \longrightarrow \{fm, m, cnt'\}x[e'_1] := e_2} \text{STR_ARR_ASSIGN_EXPR_L} \\
\frac{\{fm, m, cnt\}e_2 \longrightarrow \{fm, m, cnt'\}e'_2}{\{fm, m, cnt\}x[v_1] := e_2 \longrightarrow \{fm, m, cnt'\}x[v_1] := e'_2} \text{STR_ARR_ASSIGN_EXPR_R} \\
\frac{cnt' = cnt + 1 \quad m' = m[x := \mathbf{a}]}{\{fm, m, cnt\}x[v_1] := v_2 \longrightarrow \{fm, m', cnt'\}\mathbf{skip}} \text{STR_ARR_ASSIGN_VAL}
\end{array}$$

$$\begin{array}{c}
v_1 < v_2 \\
v'_1 = v_1 + 1 \\
\neg(m = m'[x := v']) \\
m'' = m[x := v_1] \\
\hline
\{fm, m, cnt\} \textbf{for } x \textbf{ from } v_1 \textbf{ to } v_2 : s \longrightarrow \{fm, m'', cnt\} s; \textbf{for } x \textbf{ from } v'_1 \textbf{ to } v_2 : s
\end{array}
\quad \text{STR_FOR}$$

$$\begin{array}{c}
v_1 = v_2 \\
m' = m/x \\
\hline
\{fm, m, cnt\} \textbf{for } x \textbf{ from } v_2 \textbf{ to } v_2 : s \longrightarrow \{fm, m', cnt\} \textbf{skip}
\end{array}
\quad \text{STR_FOR_BASE}$$

Definition rules: 21 good 0 bad
Definition rule clauses: 53 good 0 bad