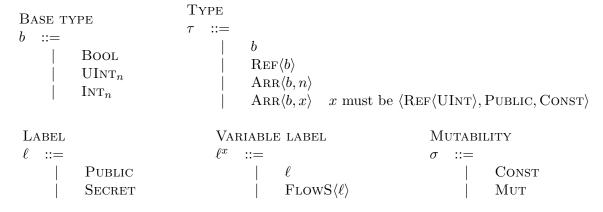
Grammar



EXPRESSION

STATEMENT

$$\begin{array}{lll} s & ::= & & & & & & & \\ & | & \diamond & & & & & \\ & | & s_1; s_2 & & & & & \\ & | & \langle \operatorname{Ref}\langle b\rangle, \sigma \rangle x = e & & & & \\ & | & \langle \operatorname{Arr}\langle b, n \rangle, \ell, \sigma \rangle x = e & & & & \\ & | & x := e & & & & & \\ & | & x[e_1] := e_2 & & & & & \\ & | & x[e_1] := e_2 & & & & \\ & | & x[e_1] := e_2 & & & & \\ & | & x[e_1] := e_2 & & & & \\ & | & x[e_1] := e_2 & & & & \\ & | & x[e_1] := e_2 & & & & \\ & | & x[e_1] := e_2 & & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 & & \\ & | & x[e_1] := e_2 &$$

FUNCTION DEFINITION

$$fdec ::= \begin{cases} \langle b, \ell \rangle f(\langle \tau_1, \ell_1, \sigma_1 \rangle x_1, \dots, \langle \tau_n, \ell_n, \sigma_n \rangle x_n) \ \{s\} \end{cases}$$

Metavariables

$$\begin{array}{lll} \text{Type context} & \text{Variable type store} \\ \Gamma & ::= & \mu & ::= \\ & \mid \quad \emptyset & \quad \mid \quad \mid \quad \emptyset \\ & \mid \quad \Gamma[e \mapsto \langle \tau, \ell, \sigma \rangle] & \quad \mid \quad \mu[x \mapsto \langle \tau, \ell^x, \sigma \rangle] \\ \\ \text{Function type store} \\ \mathbb{F} & ::= & \quad \mid \quad \emptyset \\ & \mid \quad \mathbb{F}[f \mapsto f dec(\langle \tau_1, \ell_1, \sigma_1 \rangle, \ldots, \langle \tau_n, \ell_n, \sigma_n \rangle) : \langle b, \ell \rangle] \end{array}$$

Type Lattice

$$\frac{n_1 < n_2}{\text{UINT}_{n_1} \sqsubset \text{UINT}_{n_2}} \qquad \frac{n_1 < n_2}{\text{INT}_{n_1} \sqsubset \text{INT}_{n_2}} \qquad \overline{\text{UINT}_n \sqsubset \text{INT}_{2n}} \qquad \overline{\text{PUBLIC} \sqsubset \text{SECRET}}$$

$$\frac{\Gamma \mid \mu \vdash e : \langle b, \ell, \text{Const} \rangle \quad b \sqsubseteq b' \quad \ell \sqsubseteq \ell'}{\Gamma \mid \mu \vdash e : \langle b, \ell, \text{Const} \rangle}$$

$$\frac{\Gamma \mid \mu \vdash e : \langle \text{Arr} \langle b, n \rangle, \ell, \sigma \rangle \quad \ell \sqsubseteq \ell'}{\Gamma \mid \mu \vdash e : \langle \text{Arr} \langle b, n \rangle, \ell', \text{Const} \rangle} \qquad \frac{\Gamma \mid \mu \vdash e : \langle \text{Arr} \langle b, x \rangle, \ell, \sigma \rangle \quad \ell \sqsubseteq \ell'}{\Gamma \mid \mu \vdash e : \langle \text{Arr} \langle b, x \rangle, \ell', \text{Const} \rangle}$$

Expressions

$$\Gamma \, | \, \mu \, \vdash \, e : \langle \tau, \ell, \sigma \rangle$$

$$\frac{V_{\text{AR}}}{\mu(x) = \langle \text{Ref}\langle b \rangle, \ell^x, \sigma \rangle} \qquad \ell^x = \ell' \text{ or } \ell^x = \text{FlowS}\langle \ell' \rangle}{\Gamma \mid \mu \vdash x : \langle b, \ell', \text{Const} \rangle}$$

ARRVAR
$$\mu(x) = \langle \text{ARR}\langle b, n \rangle, \ell, \sigma \rangle$$

$$\Gamma \mid \mu \vdash x : \langle \text{ARR}\langle b, n \rangle, \ell, \text{Const} \rangle$$

$$\frac{\Gamma \mid \mu \vdash e : \langle \tau_1, \ell_1, \sigma_1 \rangle \qquad \ominus : \langle \tau_1, \ell_1, \sigma_1 \rangle \rightarrow \langle \tau_2, \ell_2, \sigma_2 \rangle}{\Gamma \mid \mu \vdash \ominus e : \langle \tau_2, \ell_2, \sigma_2 \rangle}$$

BINOP

$$\frac{\Gamma \mid \mu \vdash e_1 : \langle \tau_1, \ell_1, \sigma_1 \rangle \qquad \Gamma \mid \mu \vdash e_2 : \langle \tau_2, \ell_2, \sigma_2 \rangle \qquad \oplus : \langle \tau_1, \ell_1, \sigma_1 \rangle \rightarrow \langle \tau_2, \ell_2, \sigma_2 \rangle \rightarrow \langle \tau_3, \ell_3, \sigma_3 \rangle}{\Gamma \mid \mu \vdash e_1 \oplus e_2 : \langle \tau_3, \ell_3, \sigma_3 \rangle}$$

TERNOP

$$\frac{\Gamma \mid \mu \vdash e_1 : \langle \tau_1, \ell_1, \sigma_1 \rangle \qquad \Gamma \mid \mu \vdash e_2 : \langle \tau_2, \ell_2, \sigma_2 \rangle}{\Gamma \mid \mu \vdash e_3 : \langle \tau_3, \ell_3, \sigma_3 \rangle \qquad (?:) : \langle \tau_1, \ell_1, \sigma_1 \rangle \rightarrow \langle \tau_2, \ell_2, \sigma_2 \rangle \rightarrow \langle \tau_3, \ell_3, \sigma_3 \rangle \rightarrow \langle \tau_4, \ell_4, \sigma_4 \rangle}{\Gamma \mid \mu \vdash e_1 ? e_2 : e_3 : \langle \tau_4, \ell_4, \sigma_4 \rangle}$$

ARRGET

$$\frac{\mu(x) = \langle \text{Arr}\langle b, n \rangle, \ell, \sigma \rangle}{\Gamma \mid \mu \vdash e : \langle \text{UInt}, \text{Public}, \text{Const} \rangle} \qquad \frac{SMT(e < n)}{\Gamma \mid \mu \vdash x[e] : \langle b, \ell, \text{Const} \rangle}$$

ARRGETDYN

$$\frac{\mu(x) = \langle \text{Arr}\langle b, x_n \rangle, \ell, \sigma \rangle \qquad \Gamma \mid \mu \vdash e : \langle \text{UInt, Public, Const} \rangle \qquad SMT(e < x_n)}{\Gamma \mid \mu \vdash x[e] : \langle b, \ell, \text{Const} \rangle}$$

ArrComp

$$\frac{\Gamma \mid \mu[x \mapsto \langle b_x, \text{Public}, \text{Const} \rangle] \vdash e : \langle b, \ell, \text{Const} \rangle \quad \text{UInt}_{\lceil \log_2 n \rceil} \sqsubseteq b_x}{\Gamma \mid \mu \vdash \langle b, n, b_x \rangle x \Rightarrow e : \langle \text{Arr}\langle b, n \rangle, \ell, \text{Mut} \rangle}$$

ArrView

$$\frac{\mu(x) = \langle \operatorname{Arr}\langle b, n \rangle, \ell, \sigma \rangle \qquad \Gamma \mid \mu \vdash e : \langle \operatorname{UInt}, \operatorname{Public}, \operatorname{Const} \rangle \qquad SMT(e + n' < n)}{\Gamma \mid \mu \vdash \operatorname{View}(x, e, n') : \langle \operatorname{Arr}\langle b, n' \rangle, \ell, \sigma \rangle}$$

ArrViewDyn

$$\frac{\mu(x) = \langle \operatorname{Arr}\langle b, x_n \rangle, \ell, \sigma \rangle \qquad \Gamma \mid \mu \vdash e : \langle \operatorname{UInt}, \operatorname{Public}, \operatorname{Const} \rangle \qquad SMT(e + n' < x_n)}{\Gamma \mid \mu \vdash \operatorname{VIEW}(x, e, n') : \langle \operatorname{Arr}\langle b, n' \rangle, \ell, \sigma \rangle}$$

$$\frac{\mu(x) = \langle \tau, \ell^x, \text{Mut} \rangle \qquad \ell^x = \ell' \text{ or } \ell^x = \text{FlowS}\langle \ell' \rangle}{\Gamma \mid \mu \vdash \text{REF } x : \langle \tau, \ell', \text{Mut} \rangle}$$

FNCALL

$$\mathbb{F}(f) = f dec(\langle \tau_1, \ell_1, \sigma_1 \rangle, \dots, \langle \tau_n, \ell_n, \sigma_n \rangle) : \langle b, \ell \rangle$$

$$\frac{\Gamma \mid \mu \vdash e_1 : \langle \tau_1, \ell_1, \sigma_1 \rangle \qquad \dots \qquad \Gamma \mid \mu \vdash e_n : \langle \tau_n, \ell_n, \sigma_n \rangle}{\Gamma \mid \mu \vdash f(e_1, \dots, e_n) : \langle b, \ell, \text{Const} \rangle}$$

$$\overline{\Gamma \mid \mu \vdash \text{TRUE} : \langle \text{Bool}, \text{Public}, \text{Const} \rangle}$$

False

POSNUMBER
$$c >= 0 \qquad n = \lceil \log_2 c \rceil$$

$$\frac{\Gamma \mid \mu \vdash c : \langle \text{UINT}_n, \text{PUBLIC, CONST} \rangle}{}$$

 $\Gamma \mid \mu \vdash \text{False} : \langle \text{Bool}, \text{Public}, \text{Const} \rangle$

$$\frac{N_{\text{EGNUMBER}}}{c < 0} \quad \frac{3}{n = \lceil \log_2 |c| \rceil + 1}$$
$$\frac{\Gamma \mid \mu \vdash c : \langle \text{Int}_n, \text{Public}, \text{Const} \rangle}{r \mid \mu \vdash c : \langle \text{Int}_n, \text{Public}, \text{Const} \rangle}$$

Statements $\Gamma \mid \mu \mid_{pc} s$

$$\begin{array}{c} \text{VarDecBaseMut} \\ x \notin Dom(\mu) \quad \Gamma \mid \mu \vdash e : \langle b, \ell, \text{Const} \rangle \\ \hline \Gamma \mid \mu \mid_{\overline{p}c} \diamond \\ \hline \Gamma \mid \mu \mid_{\overline{p}c} \diamond \\ \hline \end{array} \begin{array}{c} \Gamma \mid \mu \mid_{\overline{p}c} \langle \text{Ref} \langle b \rangle, \text{Mut} \rangle \mid_{\overline{p}c} s \\ \hline \Gamma \mid \mu \mid_{\overline{p}c} \langle \text{Ref} \langle b \rangle, \text{Mut} \rangle x = e; s \end{array}$$

VARDEC
$$x \notin Dom(\mu) \qquad \Gamma \mid \mu \vdash e : \langle b, \ell, \sigma \rangle$$

$$\frac{\Gamma \mid \mu[x \mapsto \langle \text{Ref}\langle b \rangle, \text{FlowS}\langle \ell \rangle, \sigma \rangle] \mid_{\overline{p}c} s}{\Gamma \mid \mu \mid_{\overline{p}c} \langle \text{Ref}\langle b \rangle, \sigma \rangle x = e; s}$$

ARRDEC
$$x \notin Dom(\mu) \qquad \Gamma \mid \mu \vdash e : \langle ARR\langle b, n \rangle, \ell, \sigma \rangle$$

$$\frac{\Gamma \mid \mu[x \mapsto \langle ARR\langle b, n \rangle, \ell, \sigma \rangle] \vdash_{pc} s}{\Gamma \mid \mu \vdash_{pc} \langle ARR\langle b, n \rangle, \ell, \sigma \rangle x = e; s}$$

VarAssign

$$\frac{\mu(x) = \langle \operatorname{Ref}\langle b \rangle, \ell, \operatorname{Mut} \rangle \qquad \Gamma \mid \mu \vdash e : \langle b, \ell', \operatorname{Const} \rangle \qquad \ell' \sqcup pc \sqsubseteq \ell \qquad \Gamma \mid \mu \mid_{\overline{p}c} s}{\Gamma \mid \mu \mid_{\overline{p}c} x := e; s}$$

VARASSIGNFLOWS

$$\frac{\mu(x) = \langle \text{Ref}\langle b \rangle, \text{FlowS}\langle \ell \rangle, \text{Mut}\rangle}{\Gamma \mid \mu \vdash e : \langle b, \ell', \text{Const}\rangle \qquad \Gamma \mid \mu[x \mapsto \langle \text{Ref}\langle b \rangle, \text{FlowS}\langle \ell' \rangle \text{Mut}\rangle] \mid_{\overline{p}c} s}{\Gamma \mid \mu \mid_{\overline{p}c} x := e; s}$$

Arrassign

$$\frac{\mu(x) = \langle \operatorname{Arr}\langle b, n \rangle, \ell, \operatorname{Mut} \rangle \quad \Gamma \mid \mu \vdash e_1 : \langle \operatorname{UInt}, \operatorname{Public}, \operatorname{Const} \rangle}{SMT(e_1 < n) \quad \Gamma \mid \mu \vdash e_2 : \langle b, \ell', \operatorname{Const} \rangle \quad \ell' \sqcup pc \sqsubseteq \ell \quad \Gamma \mid \mu \models_{pc} s}{\Gamma \mid \mu \models_{pc} x[e_1] := e_2; s}$$

ArrassignDyn

$$\frac{\mu(x) = \langle \operatorname{Arr}\langle b, x_n \rangle, \ell, \operatorname{Mut} \rangle \quad \Gamma \mid \mu \vdash e_1 : \langle \operatorname{UInt}, \operatorname{Public}, \operatorname{Const} \rangle}{SMT(e_1 < x_n) \quad \Gamma \mid \mu \vdash e_2 : \langle b, \ell', \operatorname{Const} \rangle \quad \ell' \sqcup pc \sqsubseteq \ell \quad \Gamma \mid \mu \models_{pc} s}{\Gamma \mid \mu \models_{pc} x[e_1] := e_2; s}$$

ΙF

$$\frac{\Gamma \mid \mu \vdash e : \langle \text{Bool}, \ell, \sigma \rangle \qquad pc' = \ell \sqcup pc \qquad \Gamma \mid \mu \vdash_{pc'} s_1}{\mu^* = extract \mu[\ell](s_1, s_2) \qquad pc^* = extract pc[pc'](s_1, s_2) \qquad \Gamma \mid \mu^* \vdash_{pc^*} s}$$

$$\frac{\Gamma \mid \mu \vdash_{pc'} s_2 \qquad \mu^* = extract \mu[\ell](s_1, s_2) \qquad \Gamma \mid \mu^* \vdash_{pc^*} s}{\Gamma \mid \mu \vdash_{pc} \text{ if } e \mid \{s_1\} \text{ ELSE } \{s_2\}; s}$$

For

$$\frac{\Gamma \mid \mu \vdash e_1 : \langle b, \text{Public}, \text{Const} \rangle}{\Gamma \mid \mu \vdash e_2 : \langle b, \text{Public}, \text{Const} \rangle} \frac{\Gamma \mid \mu \vdash e_2 : \langle b, \text{Public}, \text{Const} \rangle}{b = \text{UInt or } b = \text{Int}} \frac{\text{typecheck } s_1 \text{ somehow???}}{\text{typecheck } s_1 \text{ somehow???}} \frac{\Gamma \mid \mu \vdash_{p_c} \text{ for } \langle b \rangle_x \text{ from } e_1 \text{ to } e_2 \{s_1\}; s}{\text{typecheck } s_1 \text{ somehow???}}$$

$$\frac{\mathbb{R}^{\text{ET}}}{\mathbb{F}(f) = f dec : \langle b, \ell \rangle} \qquad \frac{\Gamma \mid \mu \vdash e : \langle b, \ell' \rangle}{\Gamma \mid \mu \vdash_{pc} \text{ return } e} \qquad \ell' \sqcup pc \sqsubseteq \ell$$

Interesting Semantics

$$\begin{array}{ccc} \Sigma, \mu, s & \longrightarrow & \Sigma', \mu', s' \\ \Sigma, \mu, e & \longleftarrow & \Sigma', \mu', e' \end{array}$$

$$\frac{\Sigma, \mu, s_1 \longrightarrow \Sigma', \mu', s_1'}{\Sigma, \mu, s_1; s_2 \longrightarrow \Sigma', \mu', s_1'; s_2} \qquad \frac{\text{Skip}}{\Sigma, \mu, \text{Skip}; s_2 \longrightarrow \Sigma, \mu, s_2}$$

Ret $\Sigma, \mu, \text{RETURN } v; s_2 \longrightarrow \Sigma, \mu, \text{RETURN } v$

$$\frac{\text{VarDec}}{\Sigma' = \Sigma[x \mapsto r] \qquad \mu' = \mu[r \mapsto v] \qquad \text{fresh } r}{\Sigma, \mu, \langle \tau, \cdot, \sigma \rangle x = v \quad \longrightarrow \quad \Sigma', \mu', \text{SKIP}}$$

$$\frac{\text{VarAssign}}{\mu' = \mu[r \mapsto v]}$$
$$\frac{\sum_{i} \mu_{i} + \sum_{j} \mu_{i}}{\sum_{j} \mu_{j} + \sum_{j} \mu_{j}} \sum_{j} \mu_{j} + \sum_{j} \mu_{j$$

$$\frac{v = \text{false}}{\Sigma, \mu, \text{if } v \ \{s_1\} \ \text{else} \ \{s_2\} \ \longrightarrow \ \Sigma, \mu, s_2}$$

FORITER

$$\frac{v_1 < v_2 \qquad v_1' = v_1 + 1}{\Sigma, \mu, \text{for } \langle b \rangle x \text{ from } v_1 \text{ to } v_2 \text{ } \{s\} \ \longrightarrow \ \Sigma, \mu, s[x \mapsto v_1]; \text{for } \langle b \rangle x \text{ from } v_1' \text{ to } v_2 \text{ } \{s\}}$$

FOREND
$$\frac{v_1 \geq v_2}{\sum, \mu, \text{for } \langle b \rangle x \text{ from } v_1 \text{ to } v_2 \ \{s\} \ \longrightarrow \ \Sigma, \mu, \text{skip} } \qquad \frac{\nabla \text{Ar}}{\sum(x) = r} \qquad \mu(r) = v \\ \overline{\Sigma, \mu, x} \hookrightarrow \Sigma, \mu, v$$

$$\frac{\Sigma(x) = r}{\Sigma, \mu, \text{REF } x \iff \Sigma, \mu, r}$$

FNCALL

FREALE
$$\mathbb{F}(f) = f \operatorname{dec} f(x_1, \dots, x_n) \{s\} \qquad \Sigma_0 = \{x_1 \mapsto r_1, \dots, x_n \mapsto r_n\}$$

$$\frac{\text{fresh } r_i \text{ when necessary} \qquad \Sigma_0, \mu, s \longrightarrow^* \qquad \Sigma'_0, \mu', \text{RETURN } v \qquad \mu'' = \operatorname{copyback}(\mu, \mu')}{\Sigma, \mu, f(v_1, \dots, v_n) \iff \Sigma, \mu'', v}$$