# Types



#### Week 4

- General discussion of types
- Type inference
- Type polymorphism

### What is a type?

- Examples of types:
  - Integer
  - [Char]
  - Either (Either Char Int) Bool
- Working, informal definition: set of values
  - Where does this definition break down?

### A type is: a way to prevent errors

```
• E.g.,
  const y = 1;
  y + "w00t";
• E.g.,
  function apply(f, x) {
     return f(x);
```

### A type is: a way to prevent errors

```
• E.g.,
  -- | Function must be applied to 2 Ints
  plus :: Int -> Int -> Int
  plus a b = ...
• E.g.,
  -- | Must be applied to a function and
  -- argument that that function can be applied to
  apply :: (a -> b) -> a -> b
  apply f x = f x
```

### A type is: a way to prevent errors

- The world's most lightweight\* and widely-used formal method!
  - Prevent meaningless computations from being expressed or executed

#### A type is: a method of organization & documentation

• E.g., consider abstract data type for sets

```
data Set k = ...
empty :: Set k
insert :: k -> Set k -> Set k
delete :: k -> Set k -> Set k
member :: k -> Set k -> Bool
```

• E.g., consider type for reading a file

```
readFile :: FilePath -> IO String
```

### A type is: a hint to the compiler

E.g., what should obj.prop1 be compiled down to?

### Who enforces types?

- Consider, for example: arr[200]
  - What happens in JavaScript if arr is null?
  - What happens in C/C++ if arr is of size 10?
  - What happens in Haskell if arr is not an array?

### Who enforces types?

- This is language dependent...
  - The compiler at compile time
  - The runtime system at run-time
  - The hardware at run-time

#### What are the tradeoffs of each?

	Compile-time	Run-time checks	Hardware
Pro	No runtime overhead	Permissive	Super fast
Con	Over approximates	Runtime overhead	Catch bugs late

Compile-time is the best! (Is it?)

### The cost of compile-time checking

Sometimes you give up expressivity

```
function f(x) {
   return x < 10 ? x : x();
}</pre>
```

- More advanced type systems can "type" this function (dependent types); at what cost?
- Why is this fundamental? A: static analysis
   approximates it has to work for every run of the program

- <u>Def:</u> A language is type safe if no program is allowed to violate its type distinctions
  - Is Haskell type safe? A: yes, B: no
  - Is JavaScript type safe? A: yes, B: no
  - ➤ Is C/C++ type safe? A: yes, B: no
- What language features make it hard to guarantee type safety? A: raw pointer/memory access, casts, etc.

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### Type inference

 What's the difference between type checking and type inference?

```
E.g.,

int f(int x) {
  return x + 1;
}
```

- Type checking: checks that x is actually used as an int
- Type inference: based usage infers that x is an int

### Why study type inference?

- Reduces syntactic overhead of expressive types
- Guaranteed to produce the most general type
- One of the most important language innovations
  - Even C++ has type inference now!
- Good example of a flow-insensitive static analysis alg

# What we're going to look at

Hindley-Milner type inference for uHaskell!

### Hindley-Milner type inference

- [1958] Curry and Feys invented type inference algorithm for the simply typed  $\lambda$  calculus
- [1969] Hindley extended algorithm to richer language and proved it always produced most general type
- [1978] Milner developed Algorithm W
- [1982] Damas prove the algorithm was compete

### Hindley-Milner type inference

- 1. Parse the program
- 2. Assign type variables to all nodes
- 3. Generate constraints between type variables
- 4. Solve constraints (via unification)
- 5. Read out types of top-level declarations

#### uHaskell

```
Declarations: d ::= name p = e
```

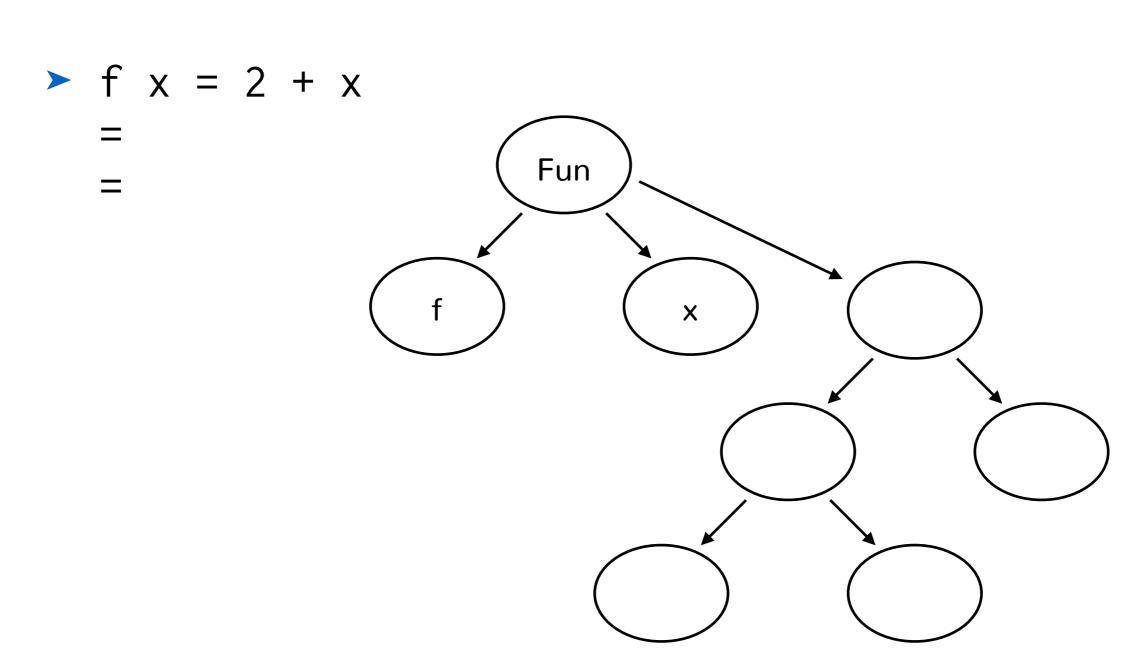
- Patterns:
   p ::= id | (p, p) | p:p | []
- Types: τ ::= τ -> τ | [τ] | (τ,τ)
   | Bool | Int

### Type inference by example

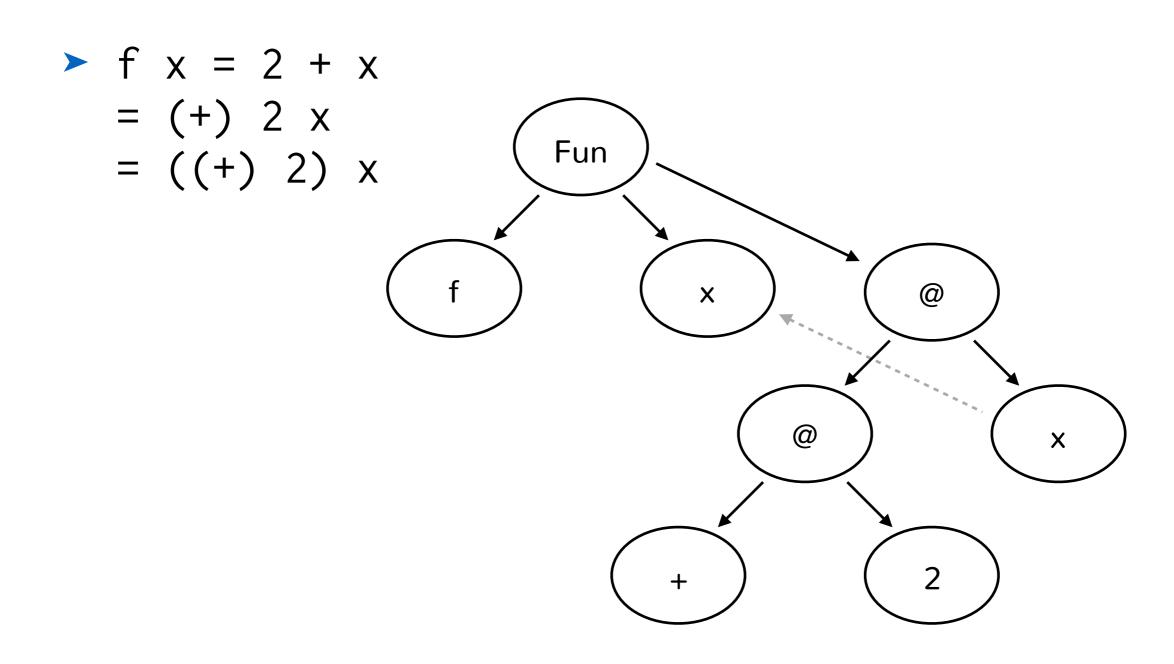
- 1.Basic idea
- 2.Polymorphism
- 3. Data types
- 4. Type error: cannot unify
- 5. Type error: occurs check

- Example: f x = 2 + x
- Goal: What is the type of f? Let's do it informally:
  - > 2 :: Int
  - (+) :: Int -> Int -> Int
  - We are applying (+) to x, we need x :: Int
  - ➤ Thus: f x = 2 + x :: Int -> Int -> Int

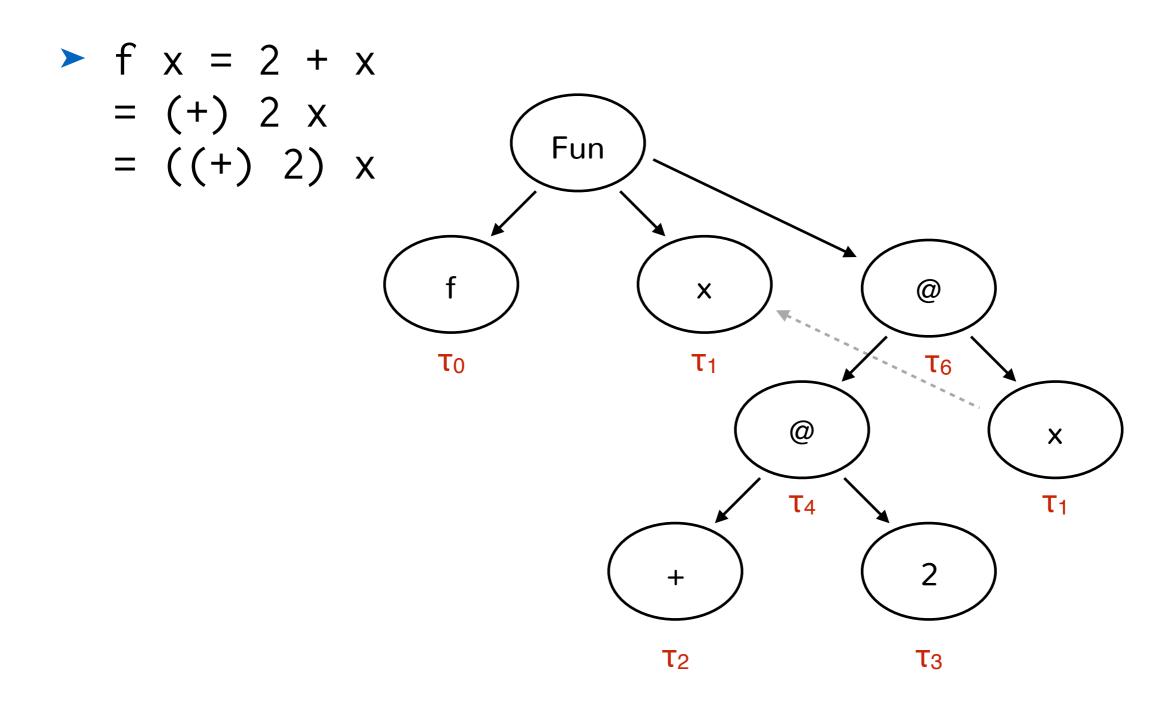
• Step 1: parse program to construct parse tree



• Step 2: assign type variables to nodes

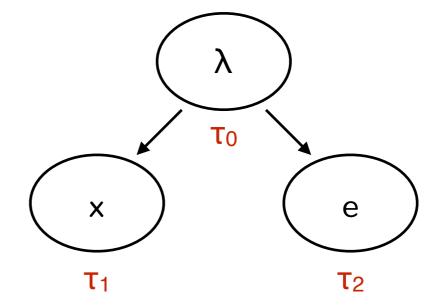


Step 3: add constraints



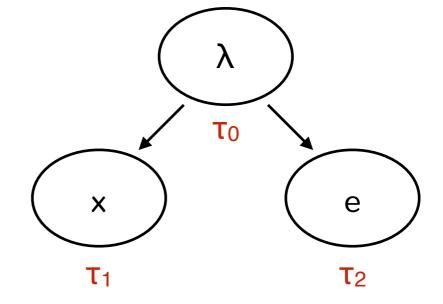
Lambda abstraction (λx.e)





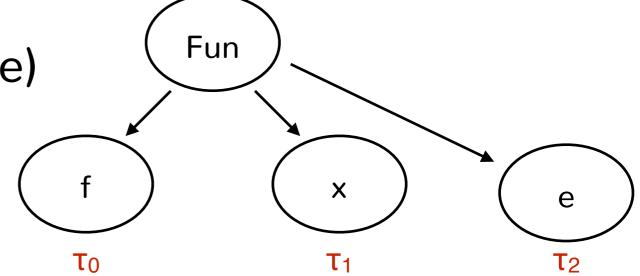
Lambda abstraction (λx.e)

$$T_0 = \tau_1 -> \tau_2$$



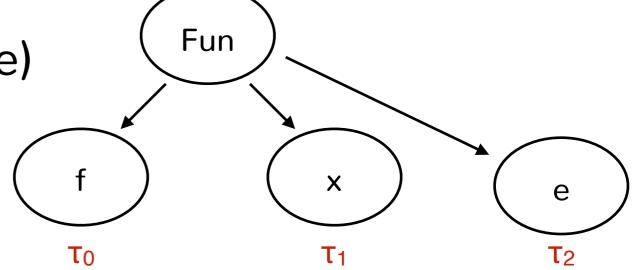
• Function declaration (f x = e)

 $\rightarrow$   $\tau_0 =$ 



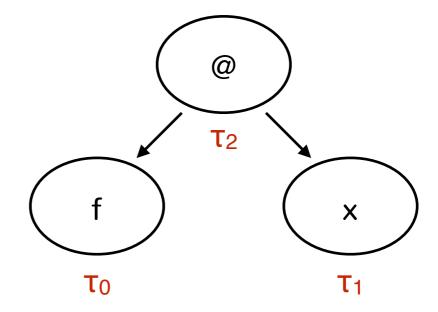
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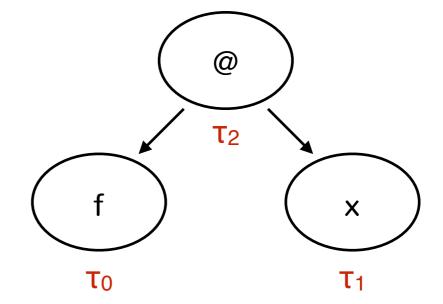


Function application (f x)

 $\rightarrow$   $\tau_0 =$ 



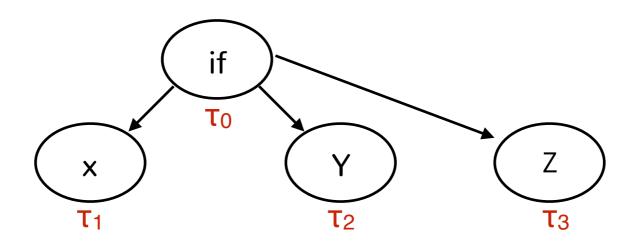
- Function application (f x)
  - $T_0 = \tau_1 -> \tau_2$



Conditionals if x then y else y

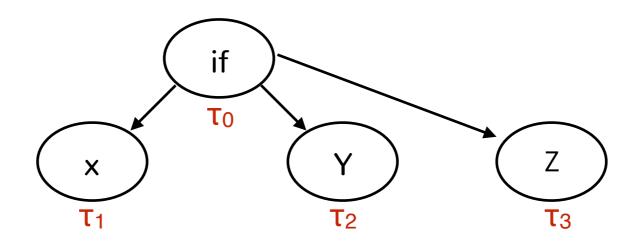
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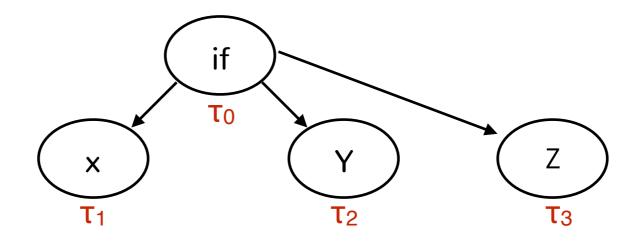
- Conditionals if x then y else y
  - $\succ$   $\tau_1 = Bool$

**>** 

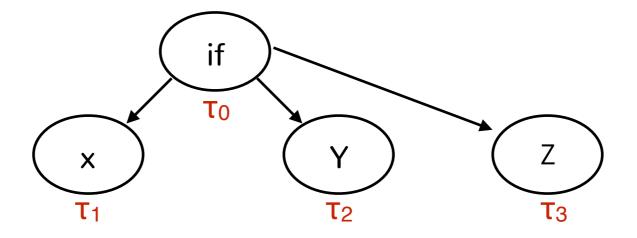


- Conditionals if x then y else y
  - $\succ$   $\tau_1 = Bool$
  - $T_0 = T_2$

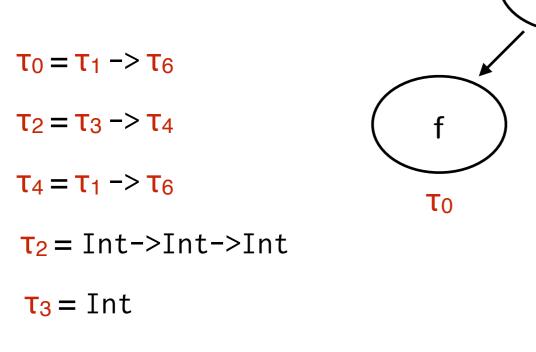
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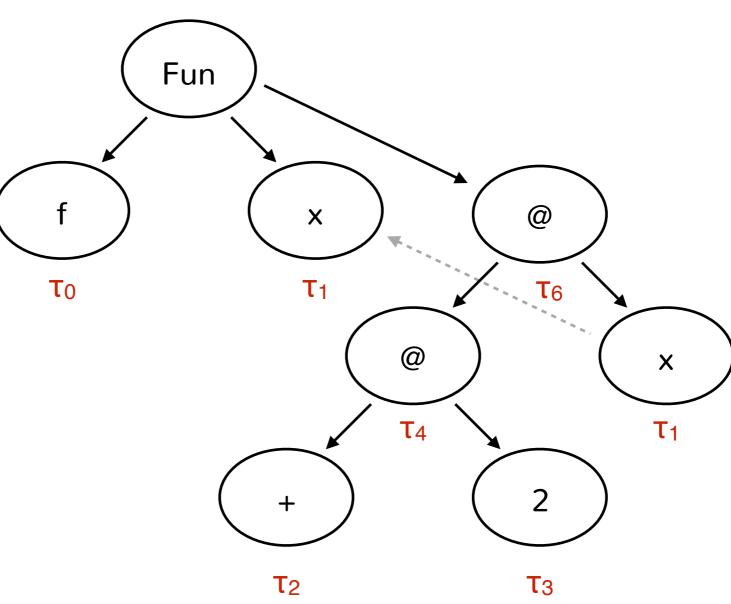


- Conditionals if x then y else y
  - $\succ$   $\tau_1 = Bool$
  - $T_0 = T_2$
  - $T_2 = T_3$



Step 4: solve constraints via unification





Step 5: read out type

```
T<sub>0</sub> = Int->Int

T<sub>1</sub> = Int

T<sub>2</sub> = Int->Int

T<sub>3</sub> = Int

T<sub>4</sub> = Int->Int

T<sub>6</sub> = Int
```

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