

# Scope



# Recall: substitution model

- Way of giving semantics to the  $\lambda$ -calculus
  - E.g.,  $(\lambda x.f\ x\ x)\ (\lambda y.z) \rightarrow_{\beta} f\ (\lambda y.z)\ (\lambda y.z)$
- Translate this knowledge to JavaScript functions
  - $(x \Rightarrow f(x)(x))\ (y \Rightarrow z) \rightarrow_{\beta} f(y \Rightarrow z)(y \Rightarrow z)$

# Let's think about this more..

- Why would you not actually want to do function application in this way for a language like JavaScript?

# Let's think about this more..

- Why would you not actually want to do function application in this way for a language like JavaScript?
  - It's super slow! Why?

# Let's think about this more..

- Why would you not actually want to do function application in this way for a language like JavaScript?
  - It's super slow! Why?
  - It's actually nonsensical sometimes! When?

# Substitution gone wrong

- Consider variable mutation in JavaScript:

```
let y = 1;  
let z = 0;  
...  
z++;  
console.log(z);
```

$\rightarrow \beta.$     0++;  
...

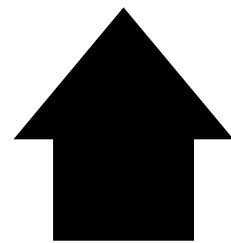
- There is nothing wrong with substitution per say
  - It's symbolic evaluation/computation
  - Problem is JavaScript has mutation and not amendable to symbolic evaluation

# What can we do?

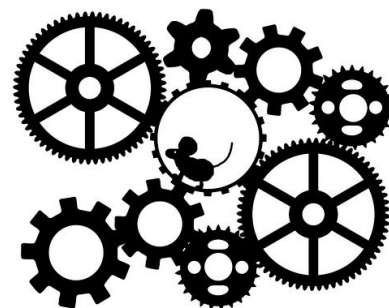
$\lambda$ -calculus



environment model



machine model



# The environment model (by example)

- Anatomy of a scope
- First-order functions
- Free variables
- High-order functions (bonus)



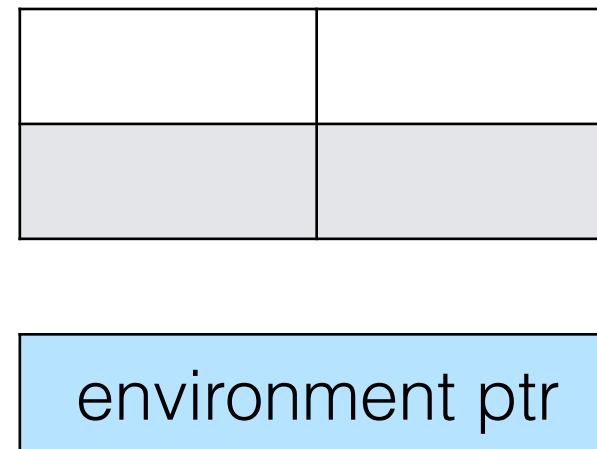
# Anatomy of a scope

- What's the point of a scope (e.g., block scope)?

# Anatomy of a scope

- Recall our previous example:

```
let y = 1;  
let z = 0;  
z++;  
console.log(z);
```

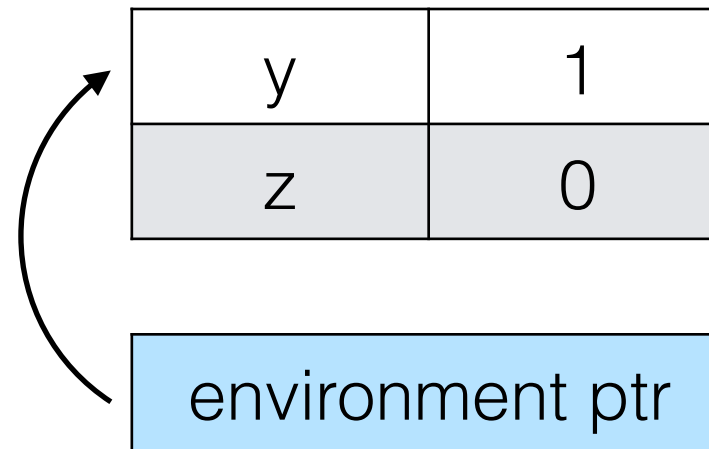


- In this model, we associate an environment (activation record) with the code we're executing
  - Environment contains entries of all variables in scope
  - Environment/stack ptr: points to cur activation record

# Anatomy of a scope

- Recall our previous example:

```
let y = 1;  
let z = 0;  
z++;  
console.log(z);
```



- In this model, we associate an environment (activation record) with the code we're executing
  - Environment contains entries of all variables in scope
  - Environment/stack ptr: points to cur activation record

# Anatomy of a scope

- In the environment model, we can distinguish between values and locations
  - r-values: plain old values; we can reason about them using substitution semantics
  - l-values: refer to locations where r-values are stored; they persist beyond single expressions.
- Why is this important?
  - It tells us the kind of values operators like ++ must take. Which does ++ take? A: r-values. B: l-values

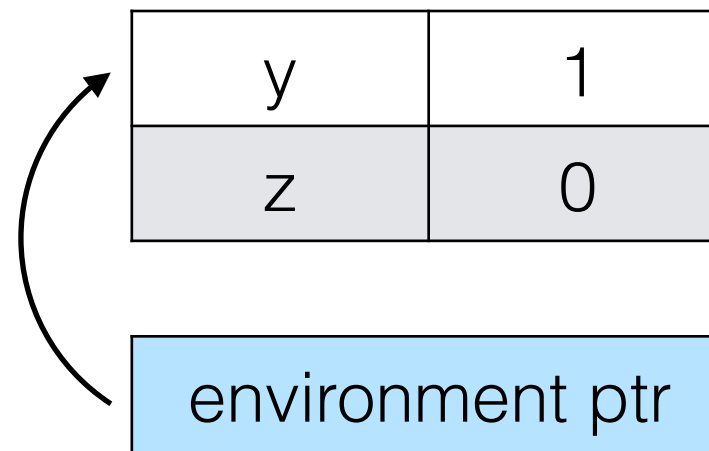
# Anatomy of a scope

- In the environment model, we can distinguish between values and locations
  - r-values: plain old values; we can reason about them using substitution semantics
  - l-values: refer to locations where r-values are stored; they persist beyond single expressions.
- Why is this important?
  - It tells us the kind of values operators like ++ must take. Which does ++ take? A: r-values. B: l-values

# Anatomy of a scope

- What's the process for executing `z++`:

```
let y = 1;  
let z = 0;  
z++;  
console.log(z);
```

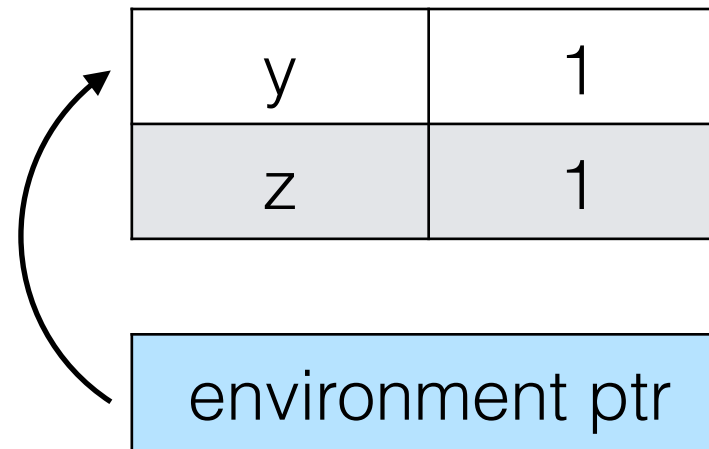


- Algorithm:
  - Find the current environment
  - Check to see if variable being reference is in env: if so, mutate!

# Anatomy of a scope

- What's the process for executing `console.log(z)`

```
let y = 1;  
let z = 0;  
z++;  
console.log(z);
```



- Algorithm:
  - Find the current environment
  - Check to see if variable being reference is in env: if so, read it!

# Anatomy of a scope

- This sounds slow!
  - It is!
  - But remember: this is not the machine model, this is still an abstract model!
- Not too far off from machine model
  - In x86, you dereference `%esp` to figure out where stack is and use offset to that location
  - In JavaScript, you often do table lookup to find location of variables



# The environment model (by example)

- Anatomy of a scope ✓
- First-order functions
- Free variables
- High-order functions (bonus)

# When do we create an environment?

- A: every time we enter a new block scope
- B: every time we enter a new function scope
- C: A and B
- D: we don't create new environments

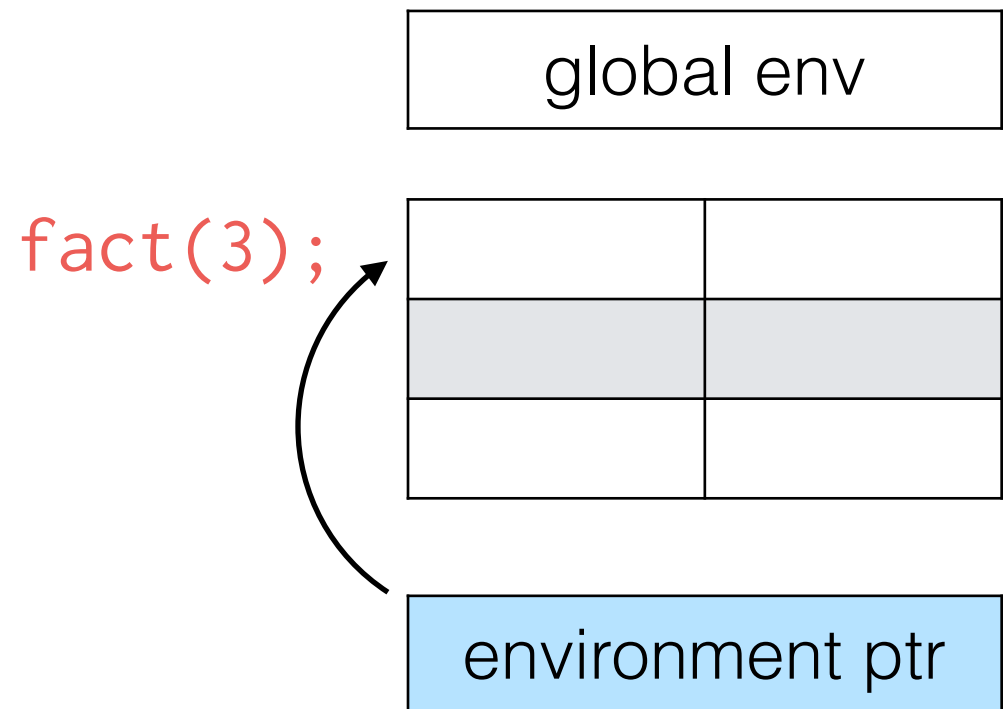
# When do we create an environment?

- A: every time we enter a new block scope
- B: every time we enter a new function scope
- C: A and B
- D: we don't create new environments

# First-order functions

- Consider activation record when calling function:

```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```

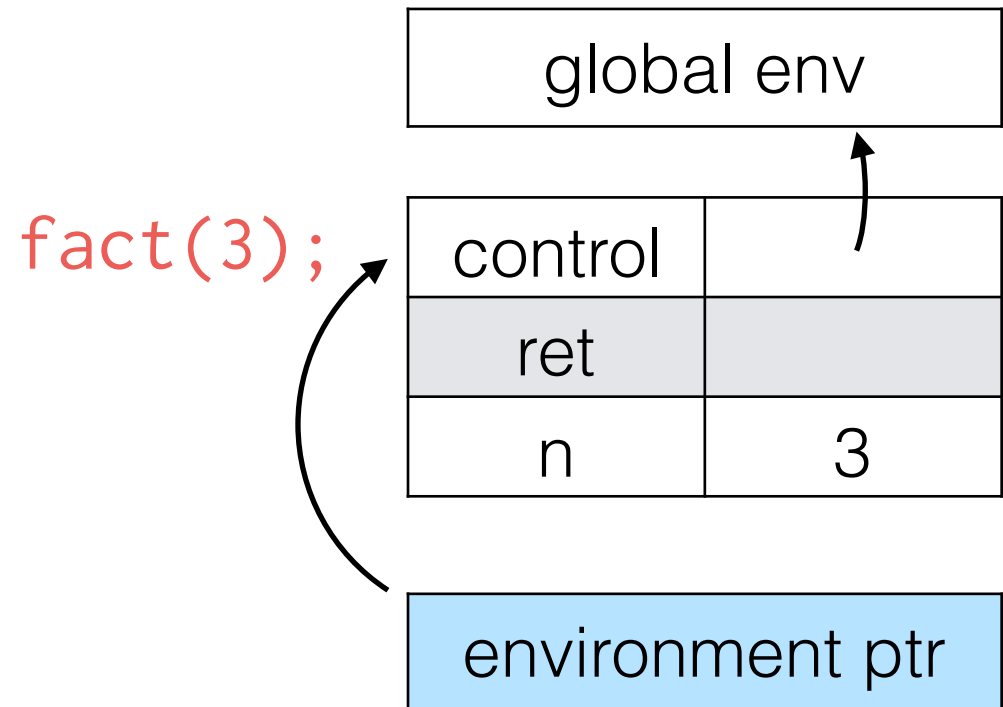


- What else do we need to keep track of?

# First-order functions

- Consider activation record when calling function:

```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



- What else do we need to keep track of?

# More bookkeeping

- The parts of an activation record when calling function
  - control link: records where to switch the environment pointer to when we finish evaluating in this scope.
  - Do we need this for block scopes too? A: yes, B:no
  - return value: l-value where the return value of function should be stored
  - parameters: l-value for each formal parameter
  - local variables: l-values for each let+const declaration

# More bookkeeping

- The parts of an activation record when calling function
  - control link: records where to switch the environment pointer to when we finish evaluating in this scope.
  - Do we need this for block scopes too? A: yes B:no
  - return value: l-value where the return value of function should be stored
  - parameters: l-value for each formal parameter
  - local variables: l-values for each let+const declaration

# More bookkeeping

- Do we need anything else besides the control link?



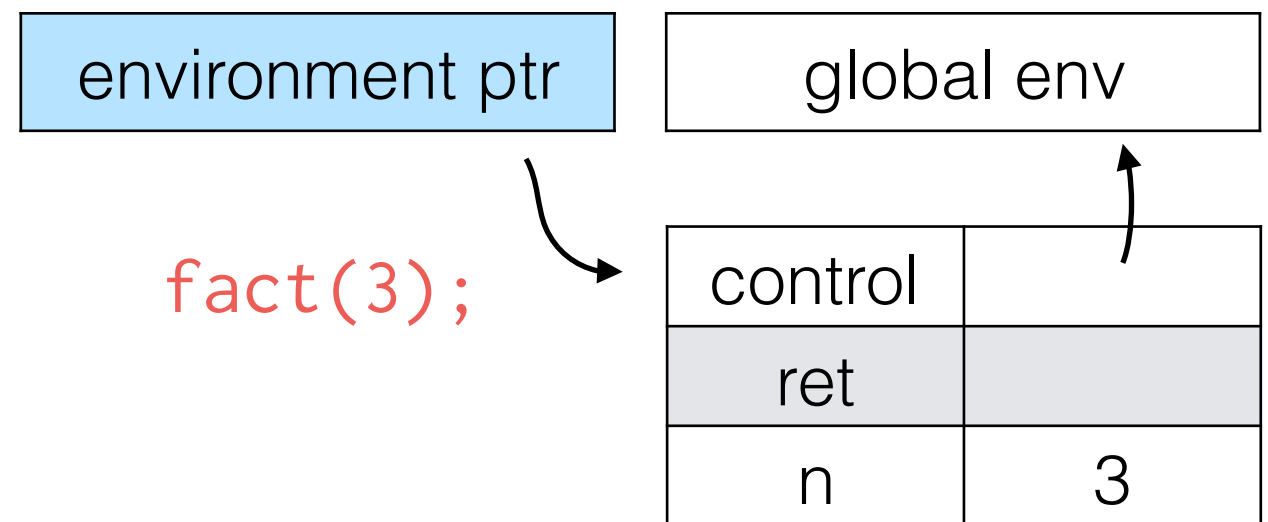
# More bookkeeping

- Do we need anything else besides the control link?
  - Yes! Typically activation records will store the return address where to resume code execution — we'll talk about this in the control flow lecture

# Let's look at how evaluation works

- Consider activation records when calling function:

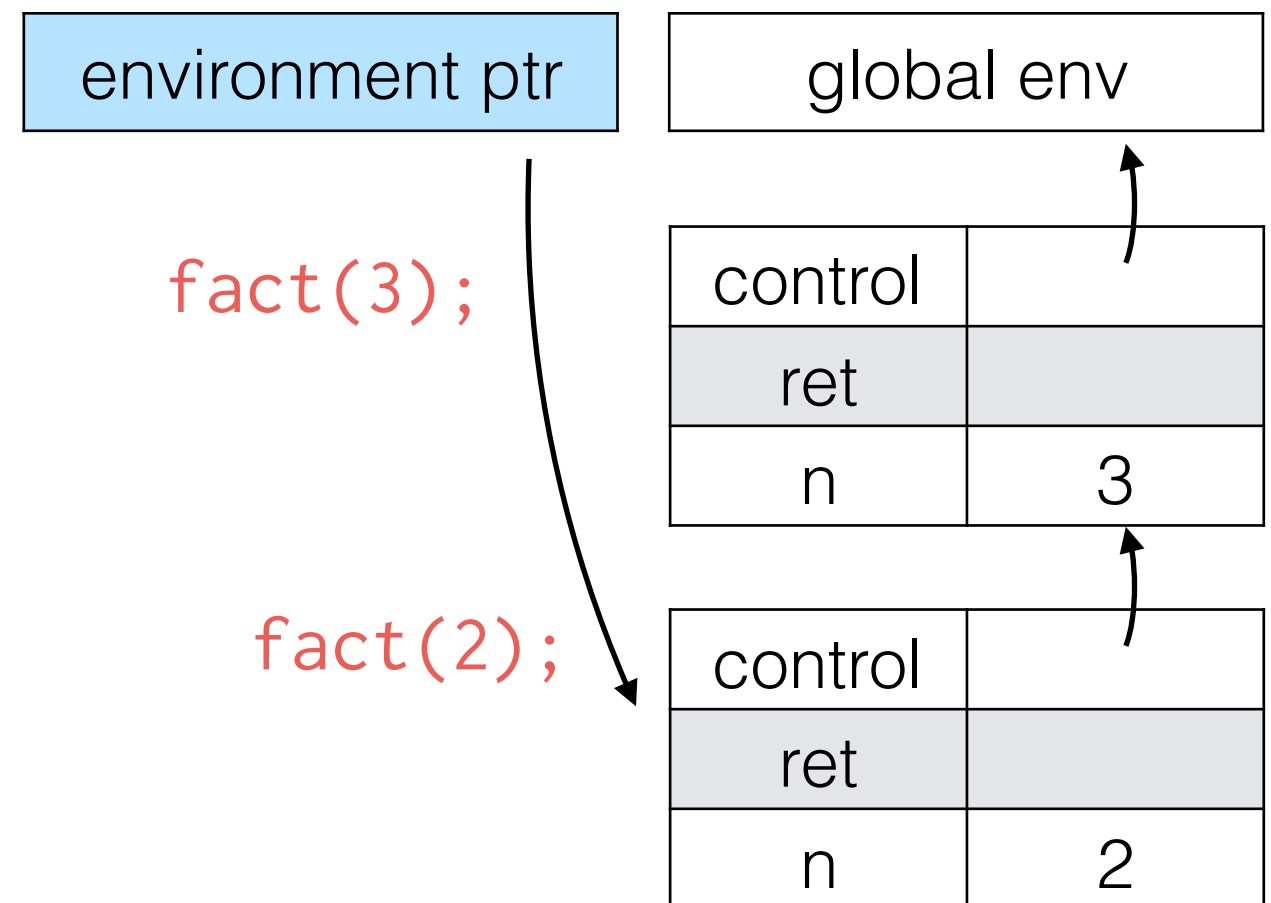
```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



# Let's look at how evaluation works

- Consider activation records when calling function:

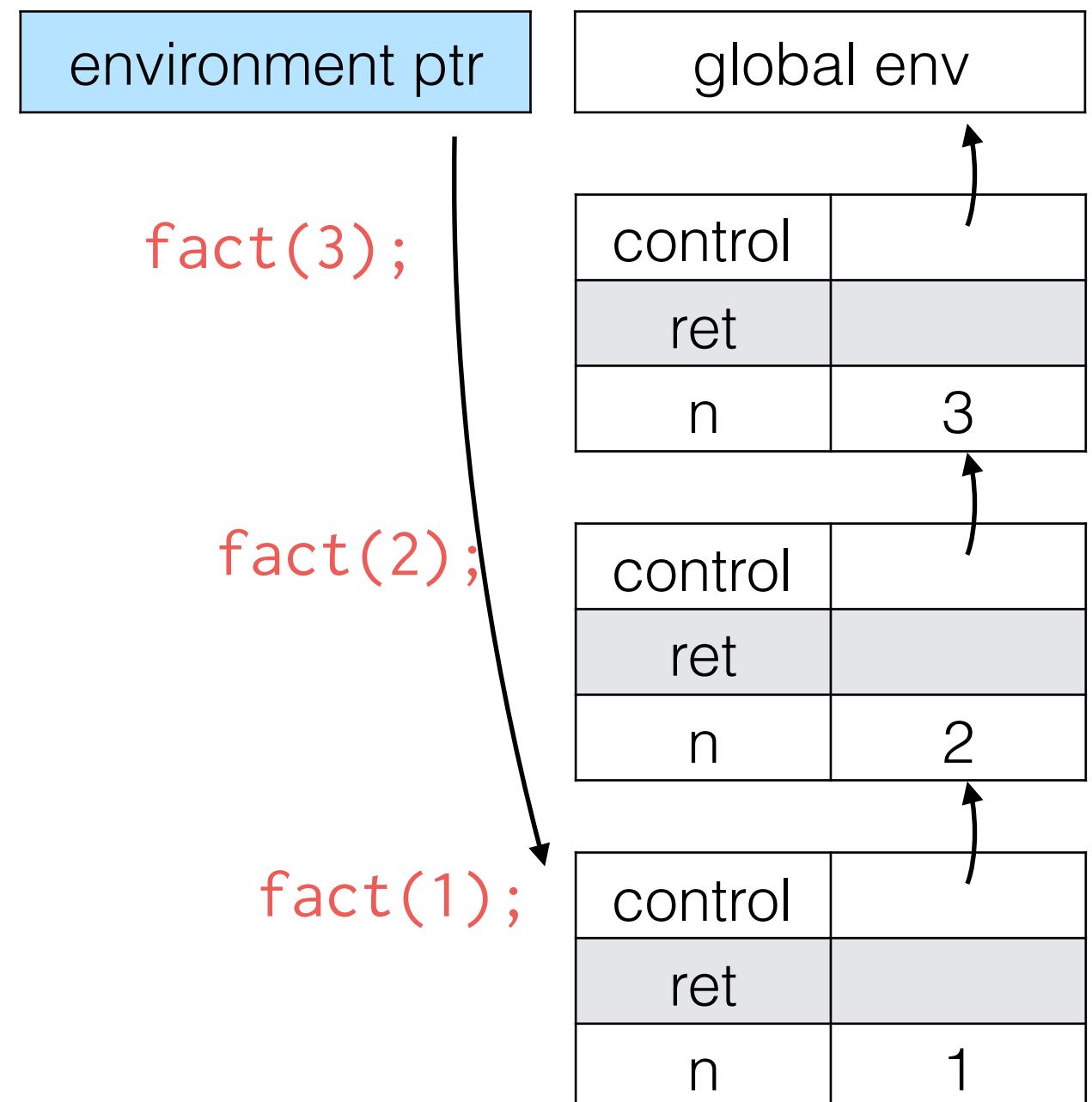
```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



# Let's look at how evaluation works

- Consider activation records when calling function:

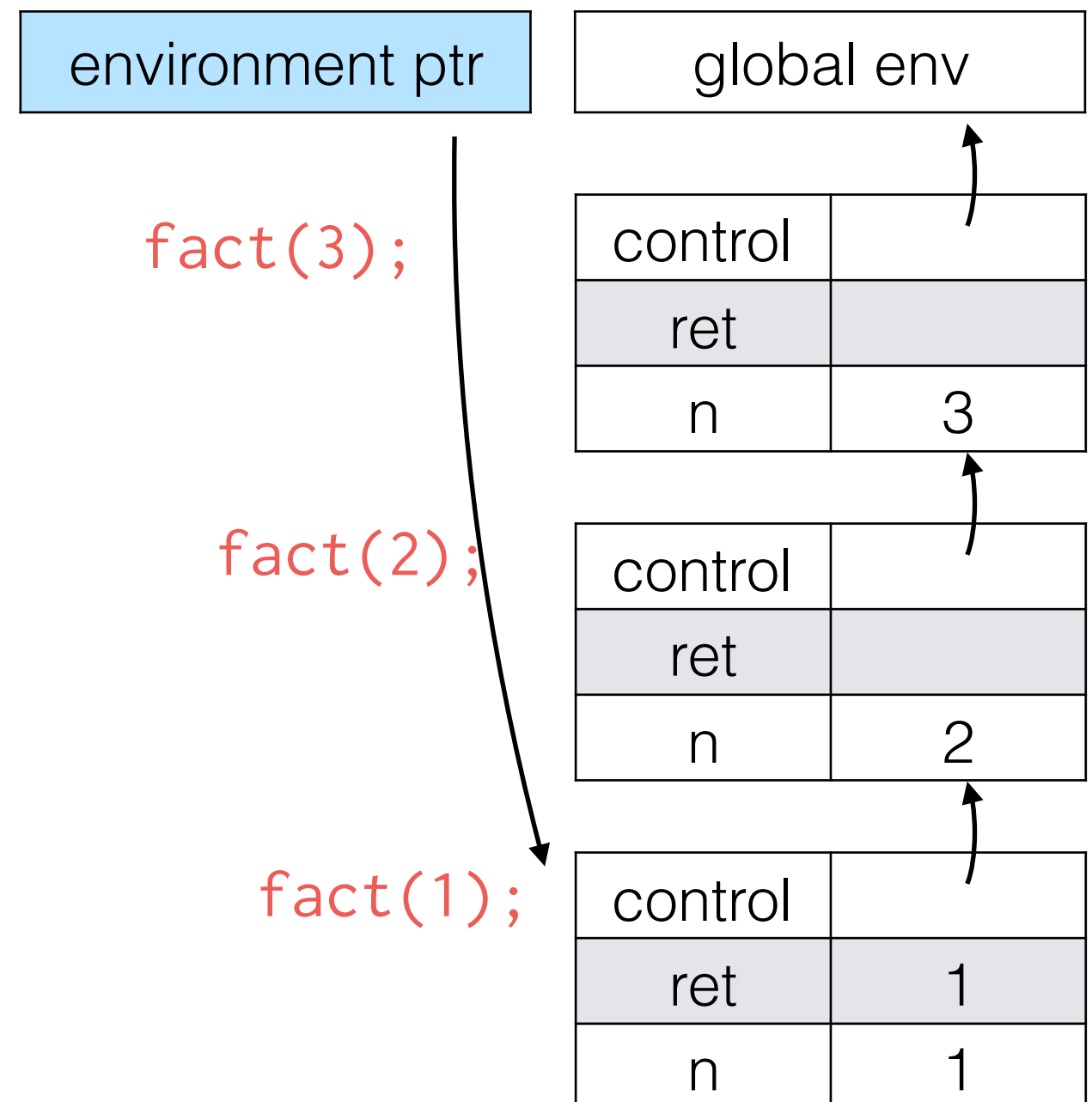
```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



# Let's look at how evaluation works

- Consider activation records when calling function:

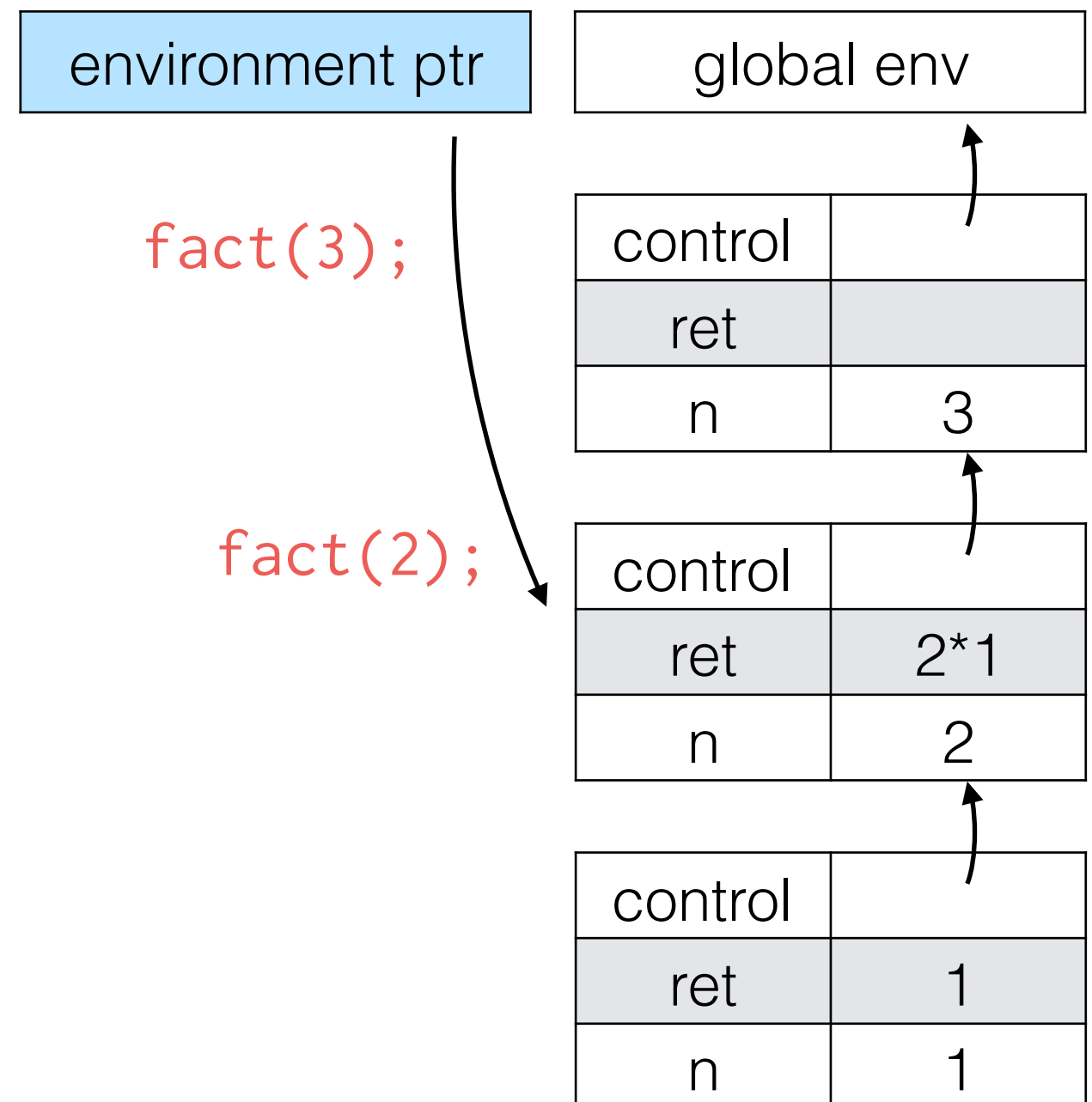
```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



# Let's look at how evaluation works

- Consider activation records when calling function:

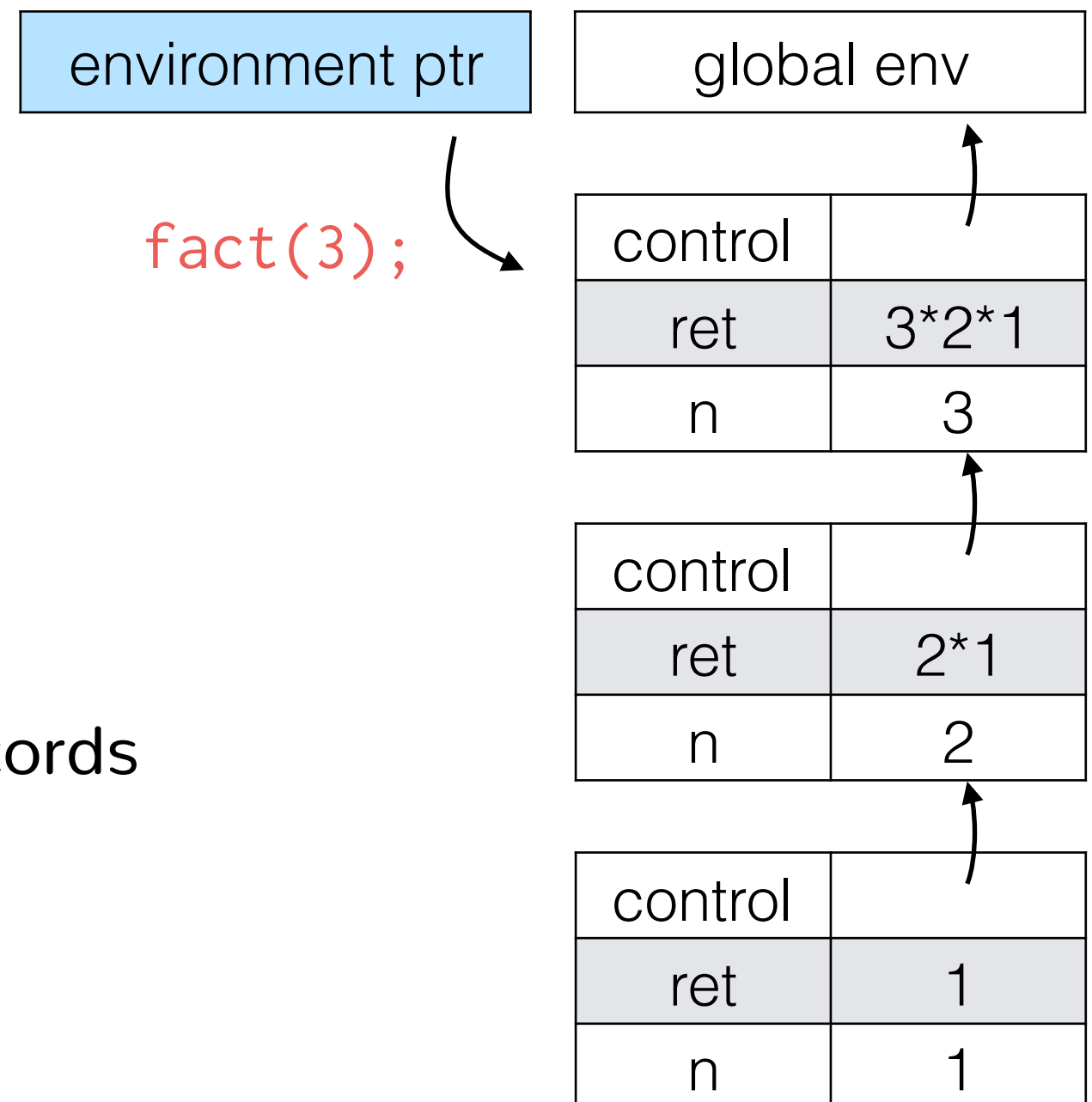
```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



# Let's look at how evaluation works

- Consider activation records when calling function:

```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```

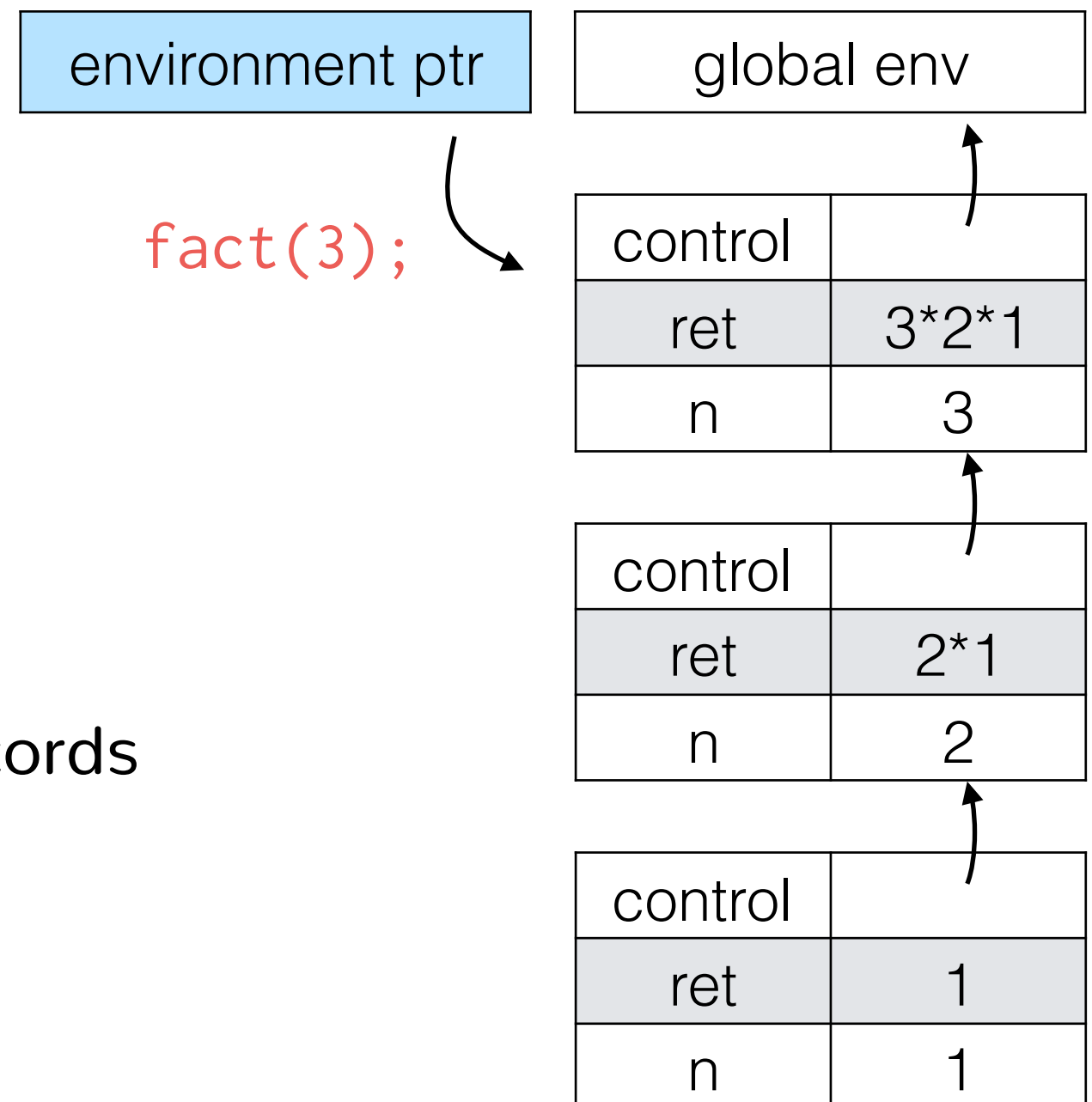


- Do we keep the activation records on the stack after evaluation?  
A: yes, B: no

# Let's look at how evaluation works

- Consider activation records when calling function:

```
function fact(n) {  
  if (n <= 1) {  
    return 1;  
  } else {  
    return n * fact(n-1);  
  }  
}  
fact(3);
```



- Do we keep the activation records on the stack after evaluation?

A: yes, B: no



# The environment model (by example)

- Anatomy of a scope ✓
- First-order functions ✓
- Free variables
- High-order functions (bonus)

- Should we lookup  $x$  via the control link?
  - A: yes
  - B: no

- Should we lookup x via the control link?

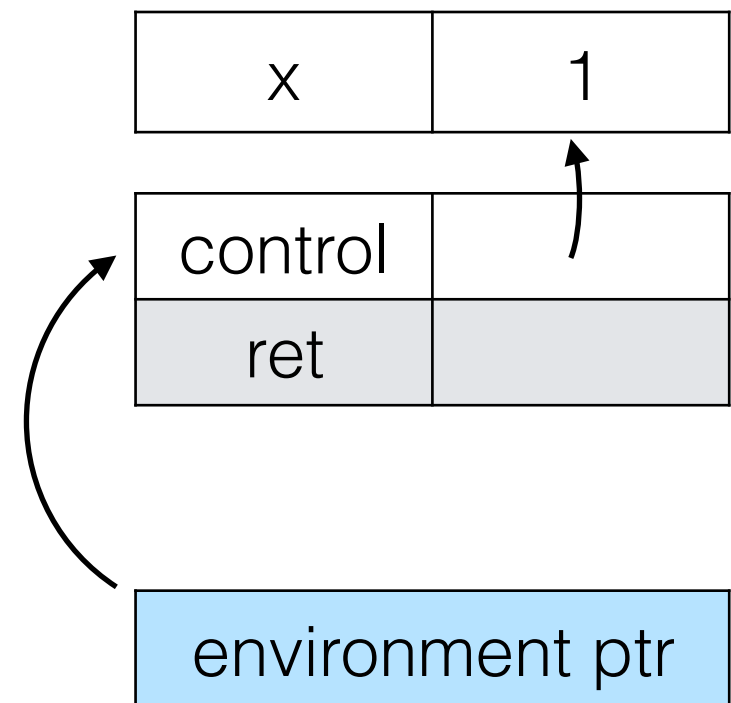
- A: yes

- B: no

# Free variables

- Consider activation records when calling f:

```
let x = 1;  
function f() {  
  console.log(x)  
}  
f();
```



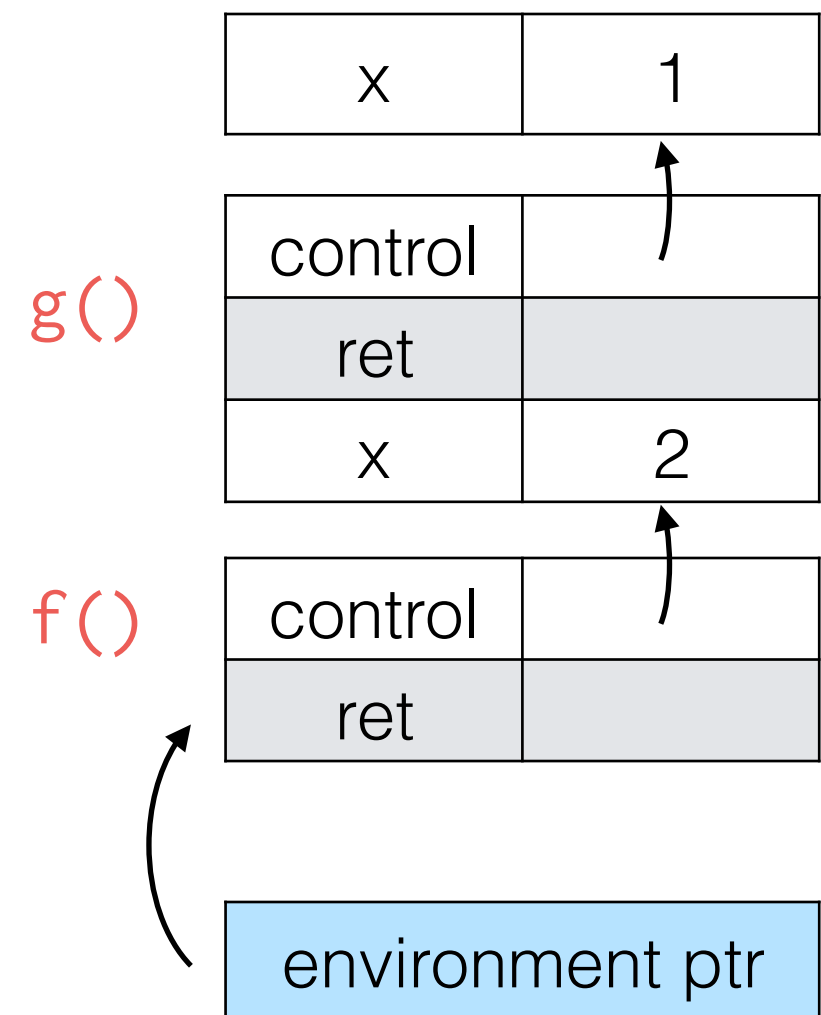
# Free variables

- Consider activation records when calling g:

```
let x = 1;  
function f() {  
  console.log(x)  
}
```

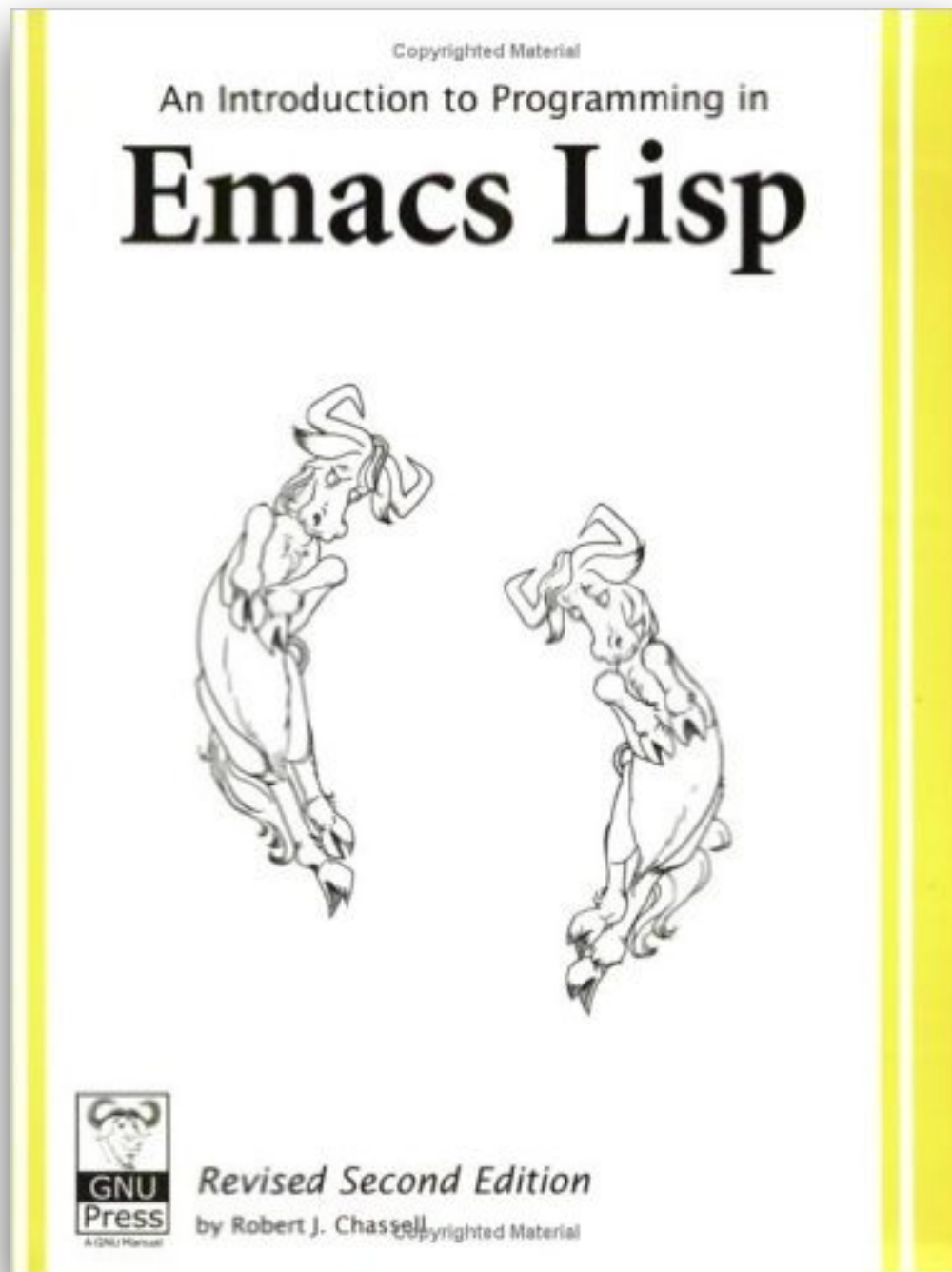
```
function g() {  
  let x = 2;  
  f();  
}
```

```
g();
```



- What happens when we follow the control link?

# Congrats, you did it!



You invented dynamic scoping!

# How do we “fix” this?

- We need more bookkeeping!
  - access link: reference to activation record of closest enclosing lexical scope
- Modify our lookup algorithm:
  - Find the current environment
  - Check to see if variable being reference is in env
  - If not, follow the access link and repeat

# Retry with access links

- Consider activation records when calling g:

```
let x = 1;  
function f() {  
  console.log(x)  
}
```

```
function g() {  
  let x = 2;  
  f();  
}
```

```
g();
```

x	1
---	---

environment ptr





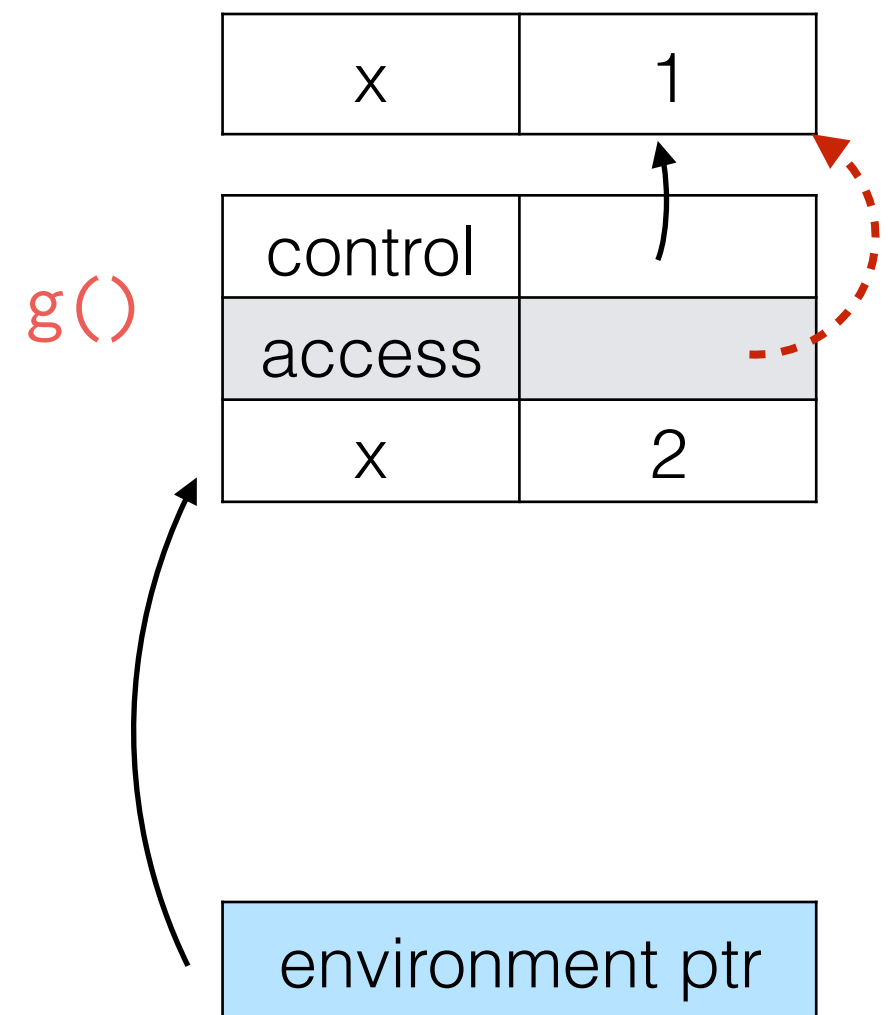
# Retry with access links

- Consider activation records when calling g:

```
let x = 1;  
function f() {  
  console.log(x)  
}
```

```
function g() {  
  let x = 2;  
  f();  
}
```

```
g();
```



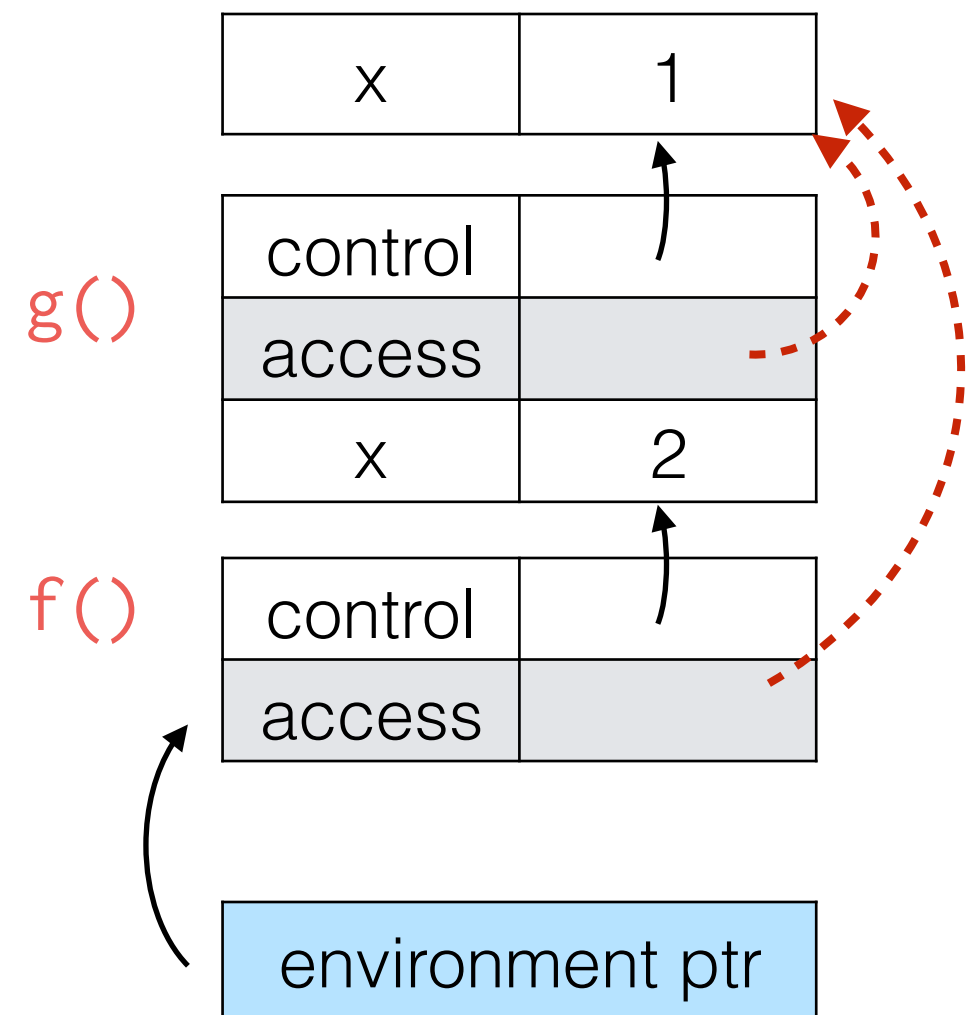
# Retry with access links

- Consider activation records when calling g:

```
let x = 1;  
function f() {  
  console.log(x)  
}
```

```
function g() {  
  let x = 2;  
  f();  
}
```

```
g();
```



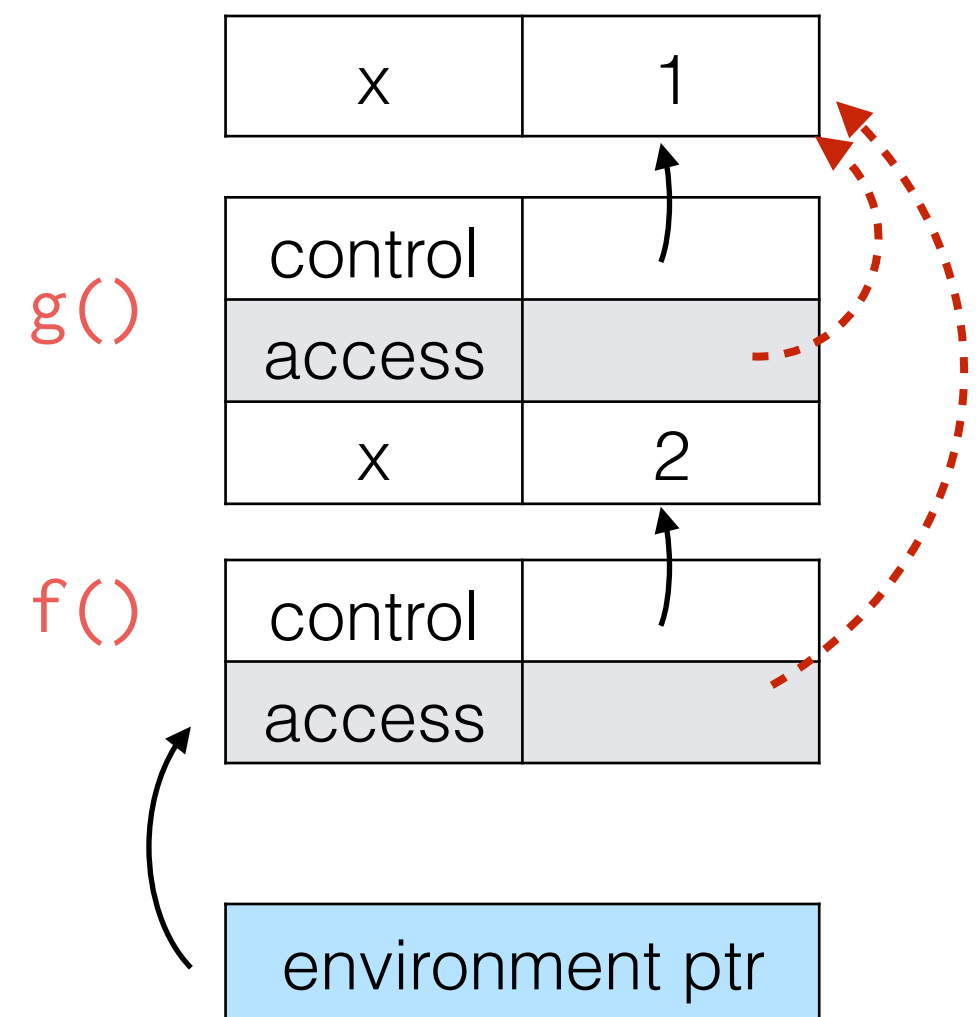
# Wait, there is some magic here

- How do we know how to wire up the access links?

```
let x = 1;  
function f() {  
  console.log(x)  
}
```

```
function g() {  
  let x = 2;  
  f();  
}
```

```
g();
```



# Functions are data!

The act of defining a function should include the act of recording the access link associated with the function

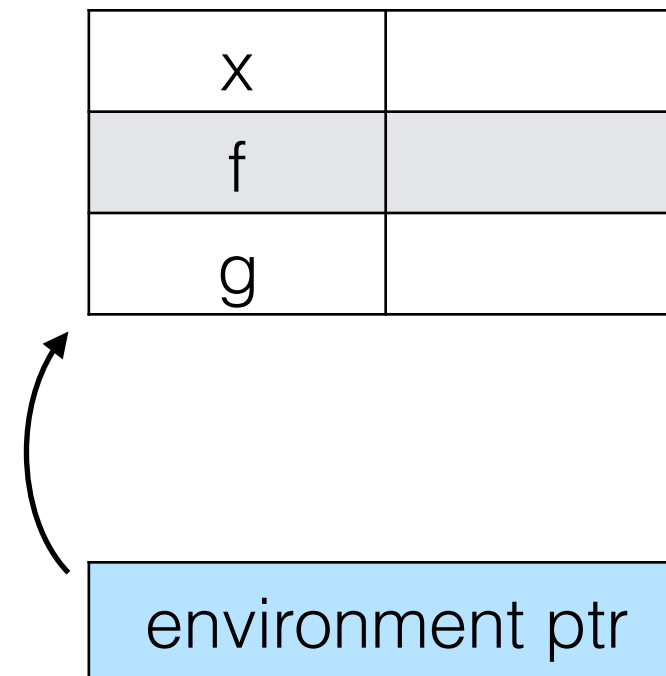
# Treating functions as data

- Let's look at the example again, with minor rewrite

```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```



- Function as data = closures = (current env ptr, code pointer)

# Treating functions as data

- Let's look at the example again, with minor rewrite

```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```

x	1
f	
g	



environment ptr

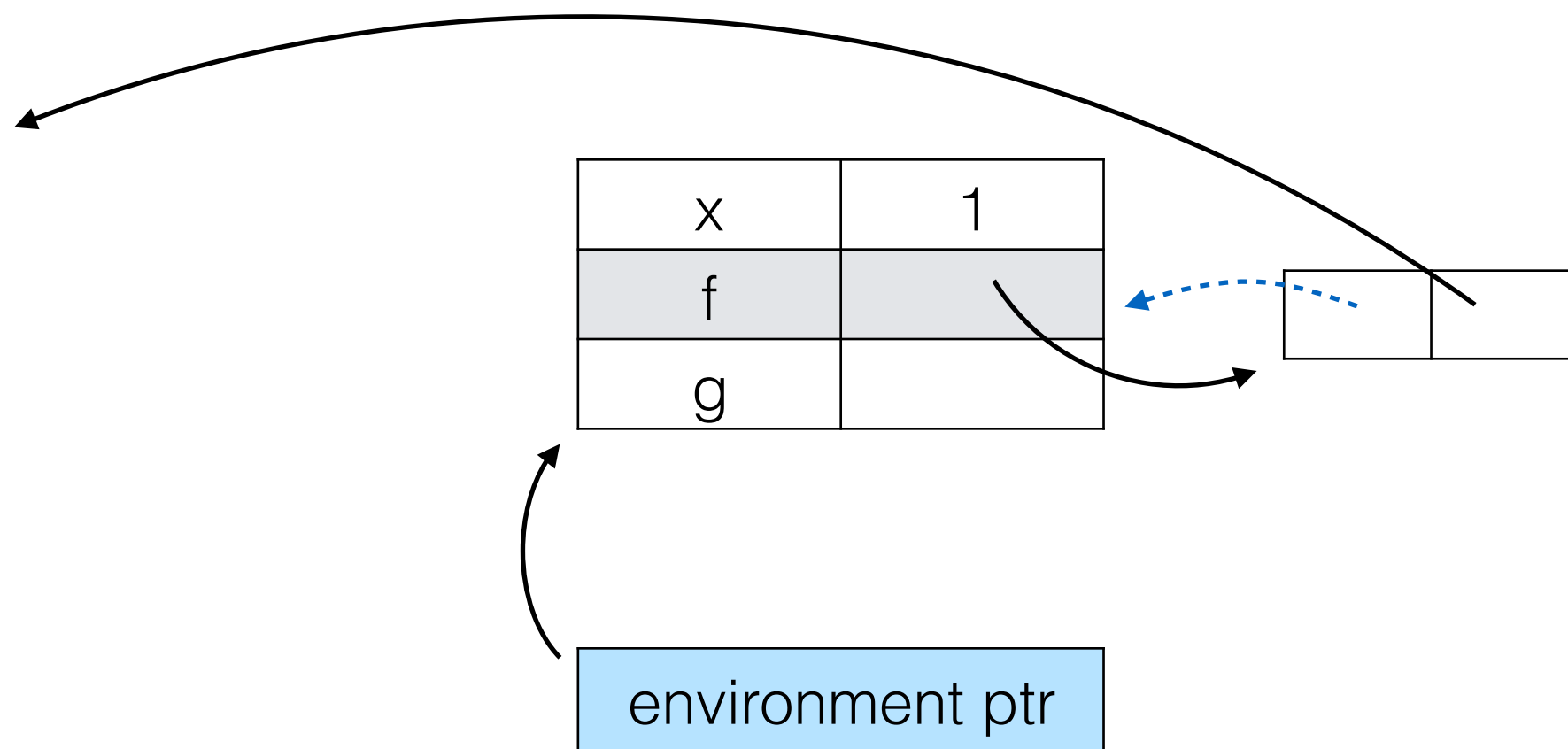
- Function as data = closures = (current env ptr, code pointer)

# Treating functions as data

- Let's look at the example again, with minor rewrite

```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

```
let g = () => {  
  let x = 2;  
  f();  
}  
  
g();
```



- Function as data = closures = (current env ptr, code pointer)

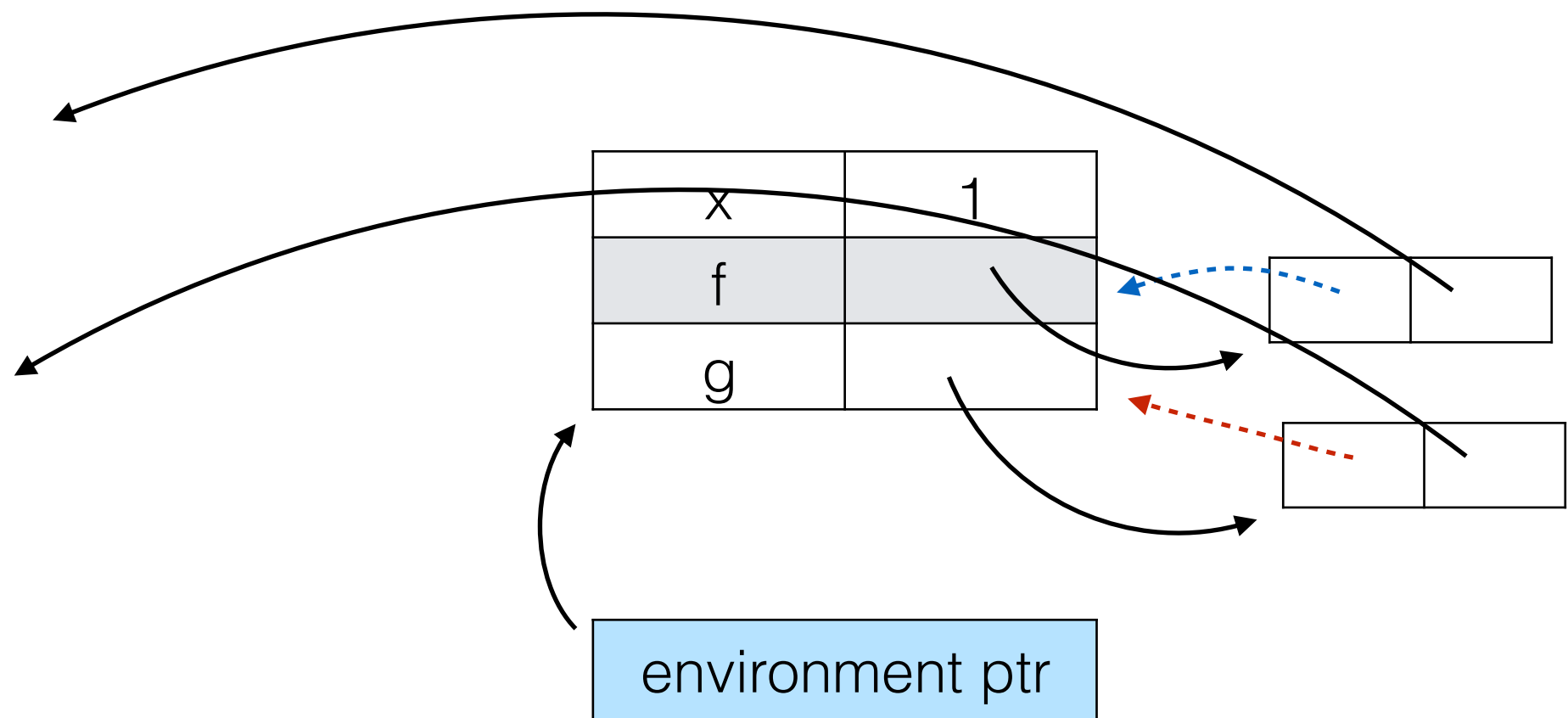
# Treating functions as data

- Let's look at the example again, with minor rewrite

```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```



- Function as data = closures = (current env ptr, code pointer)



# Treating functions as data

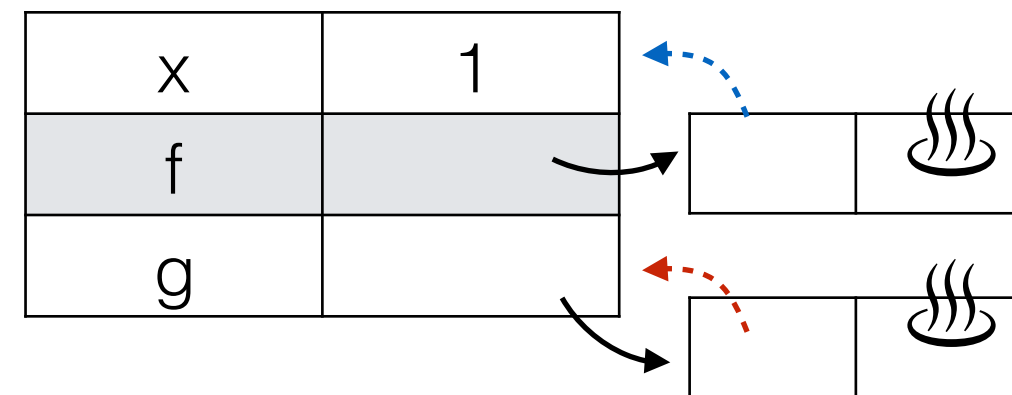
- When we evaluate function, the access link is set to the pointer in the closure

```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```

environment ptr



# Treating functions as data

- When we evaluate function, the access link is set to the pointer in the closure

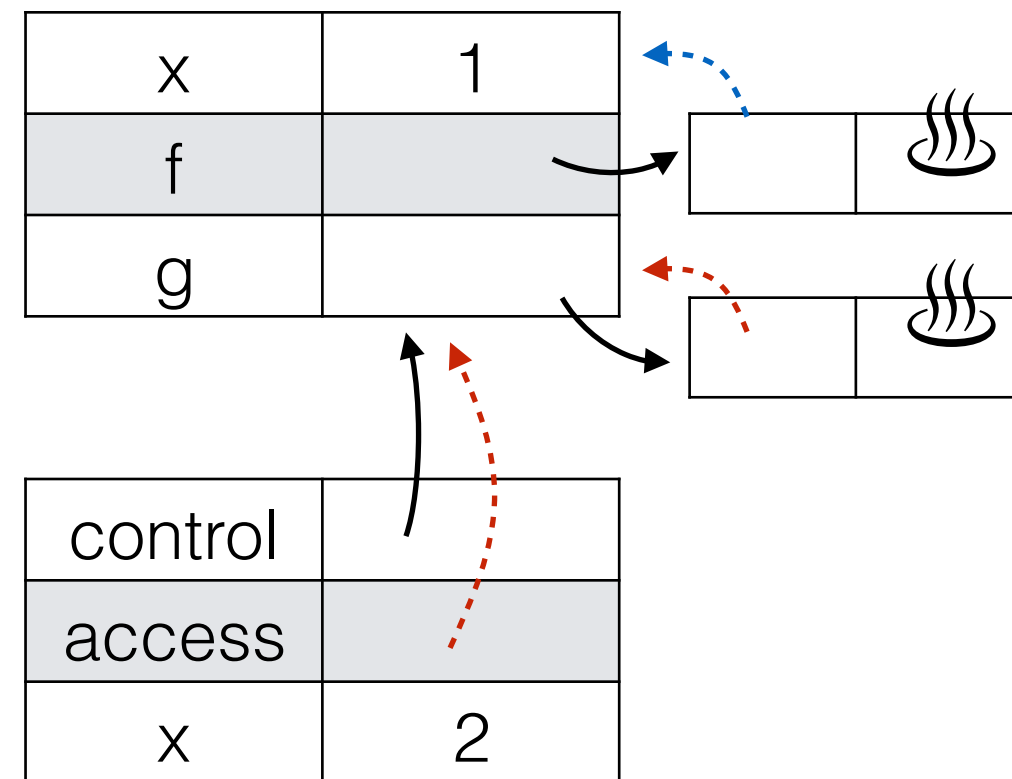
```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```

environment ptr

g()



# Treating functions as data

- When we evaluate function, the access link is set to the pointer in the closure

```
let x = 1;  
let f = () => {  
  console.log(x)  
}
```

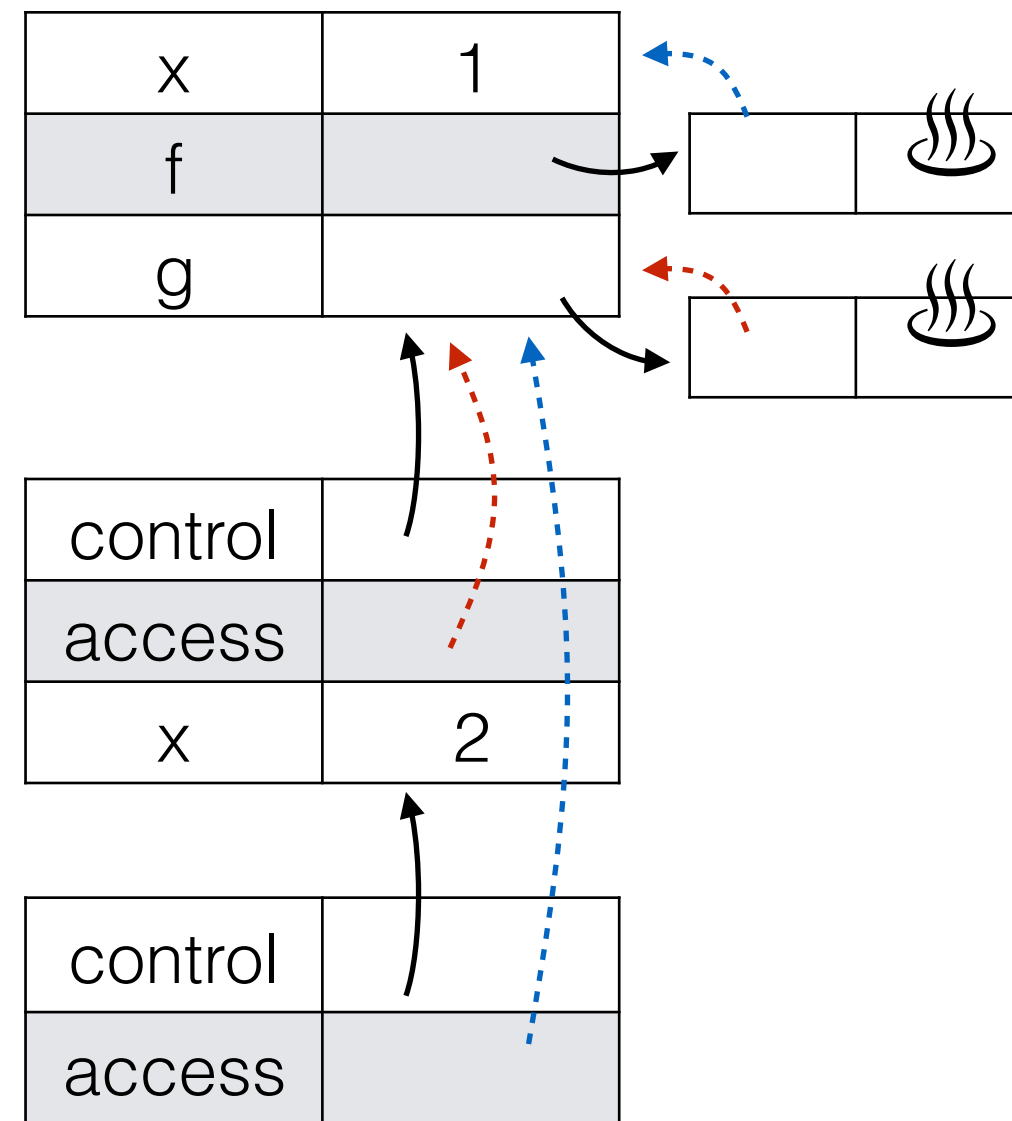
```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```

environment ptr

g()

f()



# Treating functions as data

- When we evaluate function, the access link is set to the pointer in the closure

```
let x = 1;  
let f = () => {  
  console.log(x) // 1  
}
```

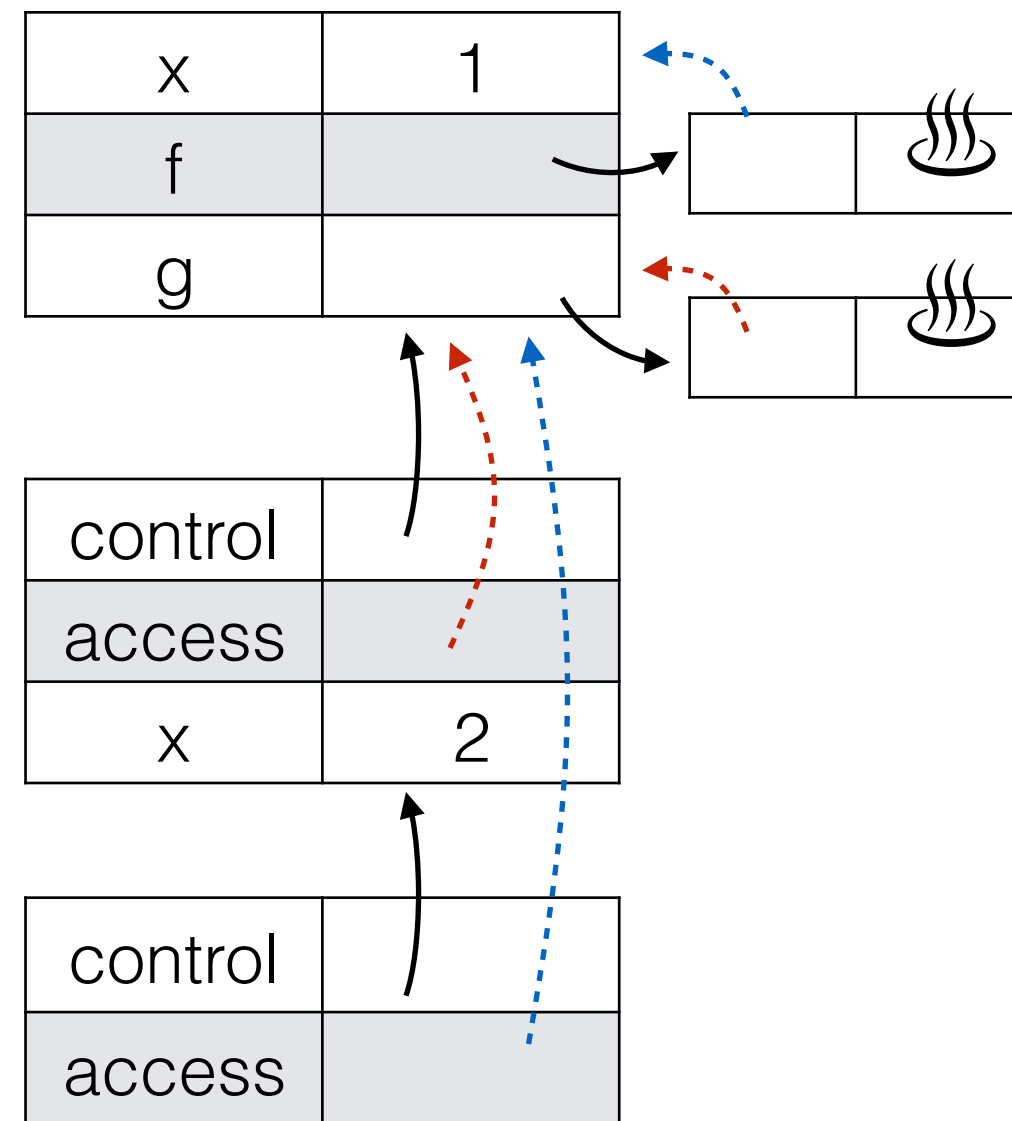
```
let g = () => {  
  let x = 2;  
  f();  
}
```

```
g();
```

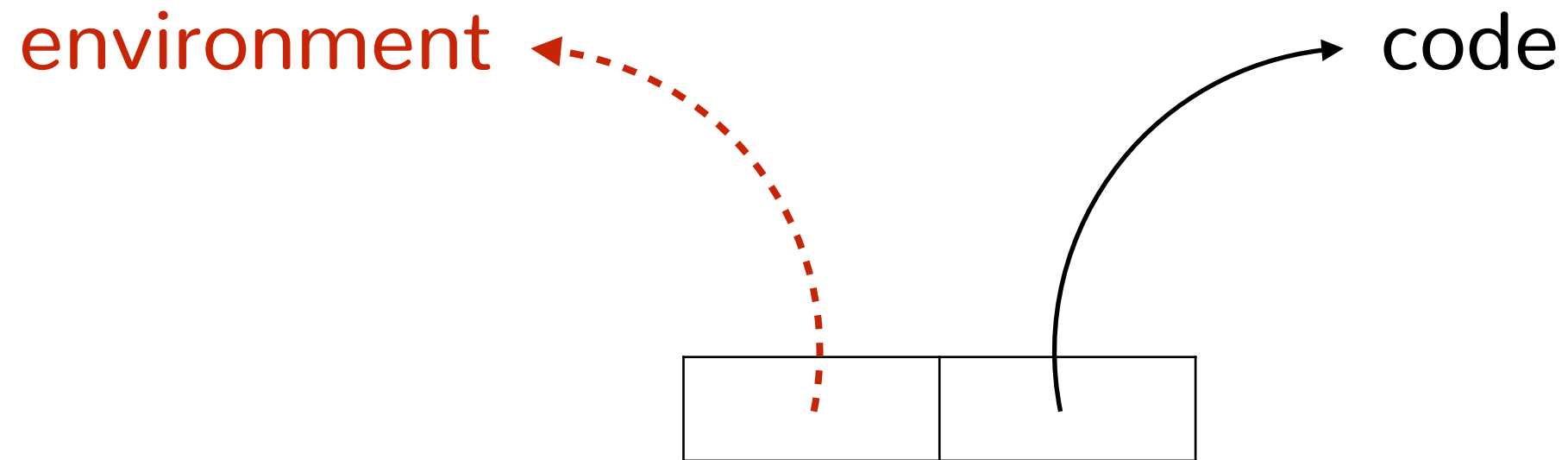
environment ptr

g()

f()



# Closures



# The environment model (by example)

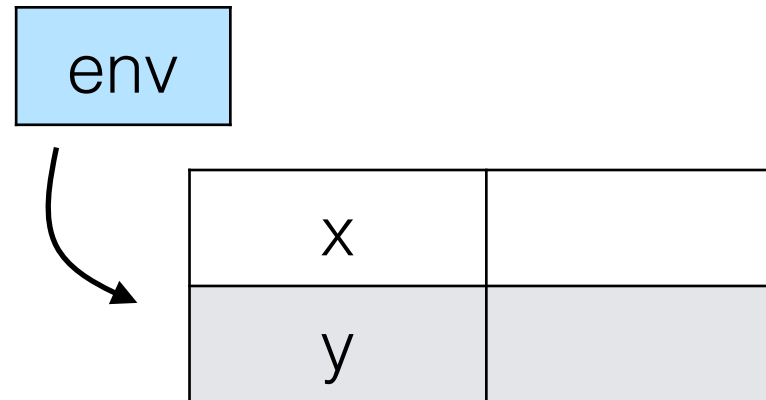
- Anatomy of a scope ✓
- First-order functions ✓
- Free variables ✓
- High-order functions (bonus)

# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```

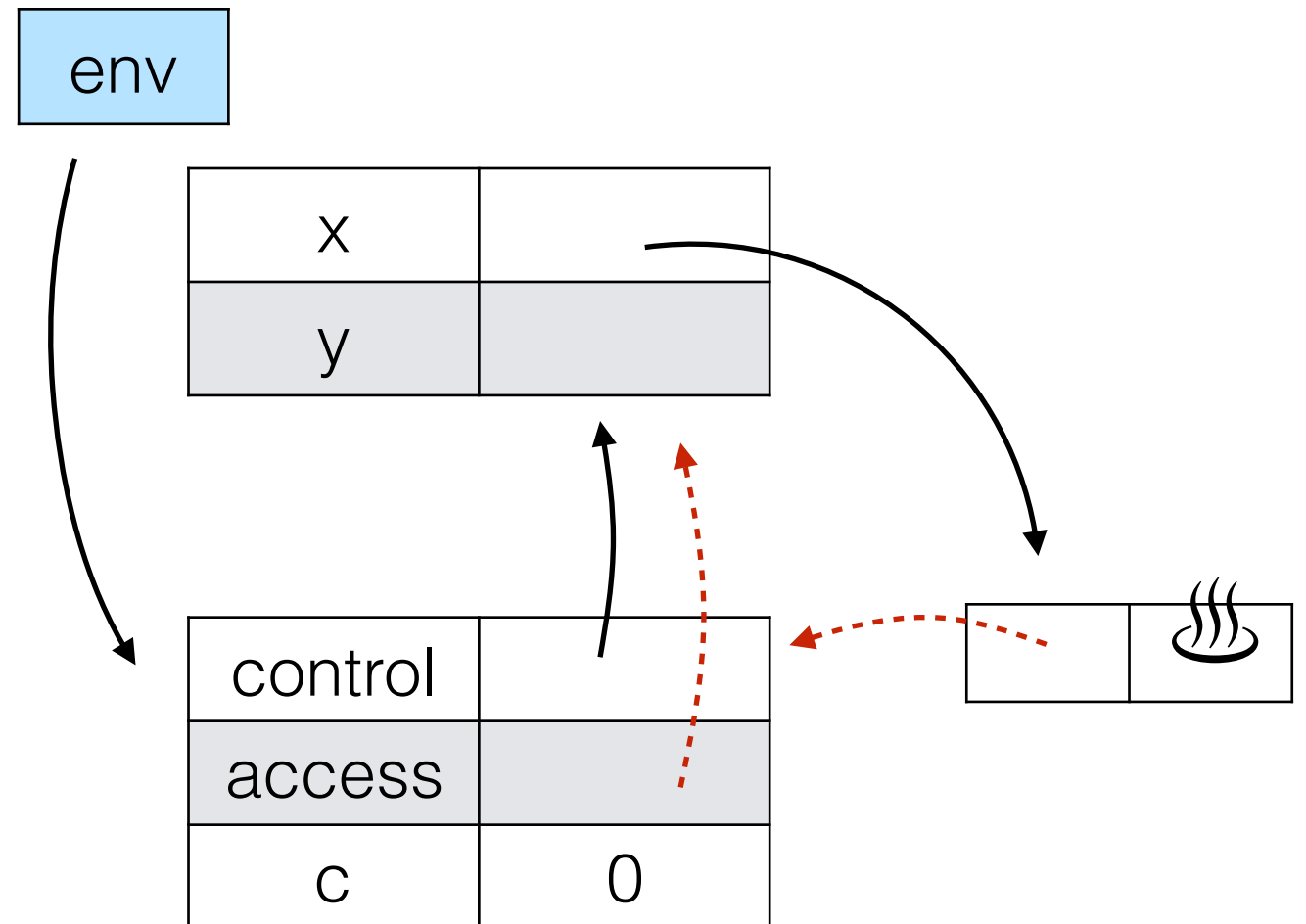


# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```



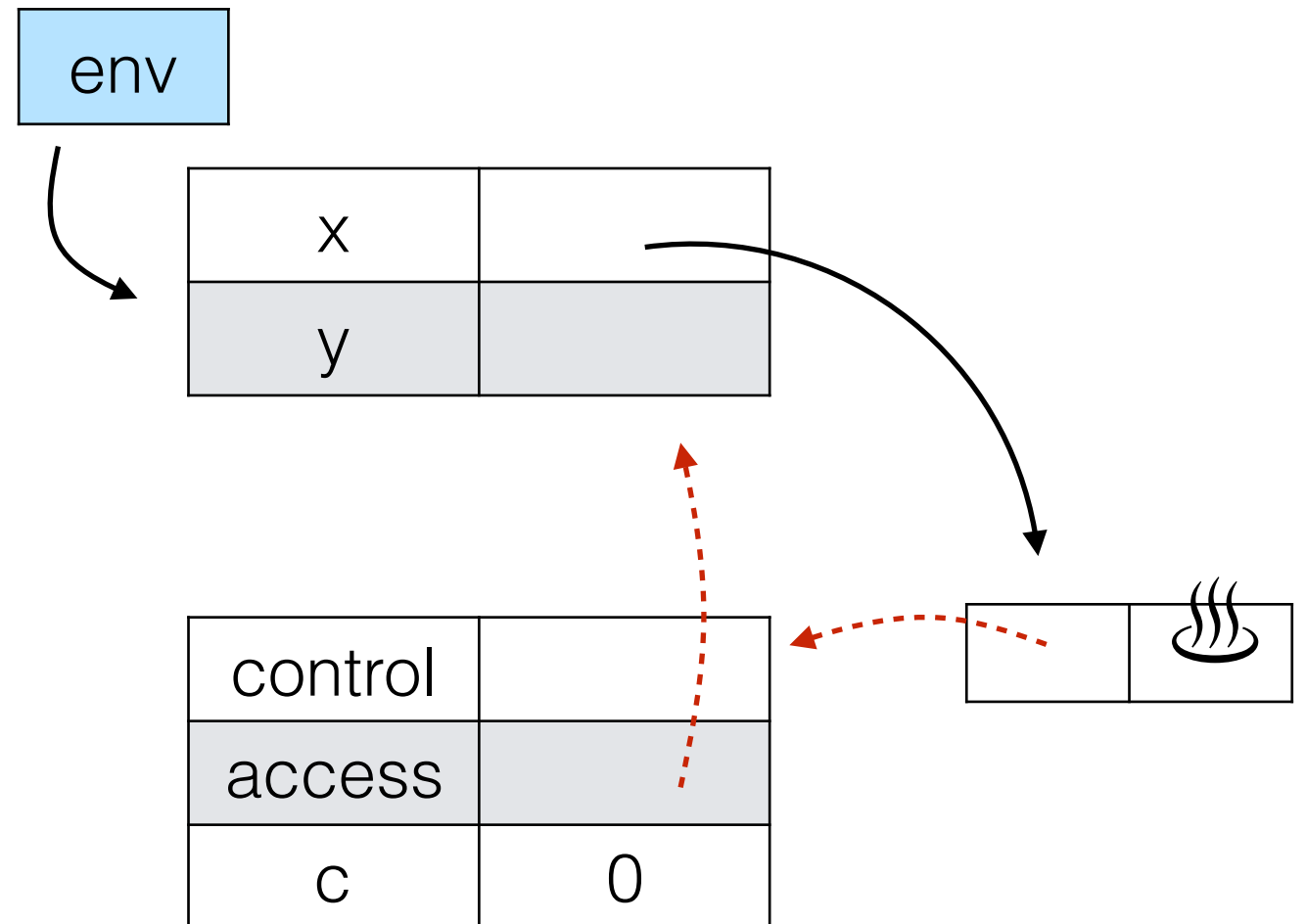


# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```

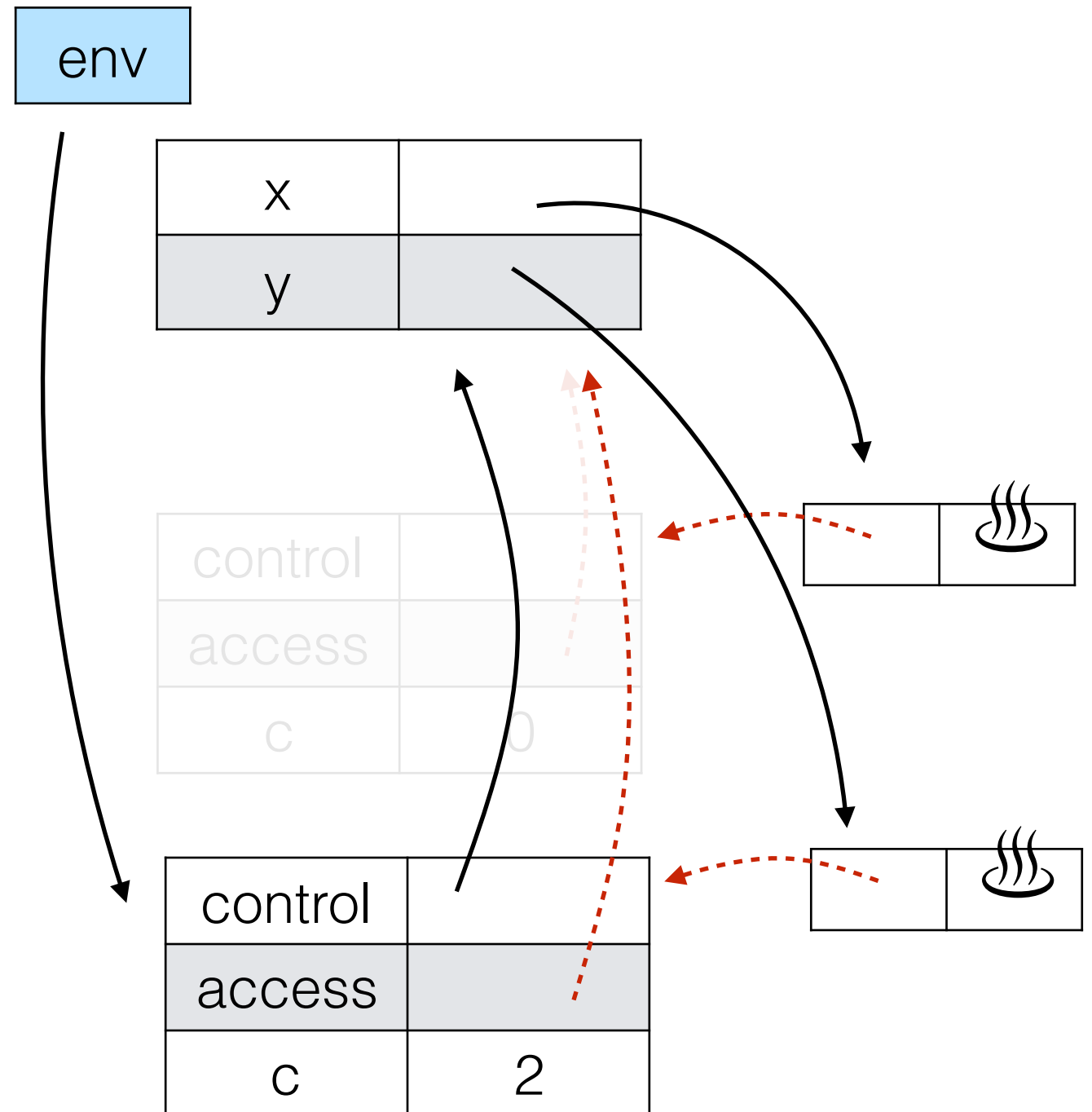


# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```

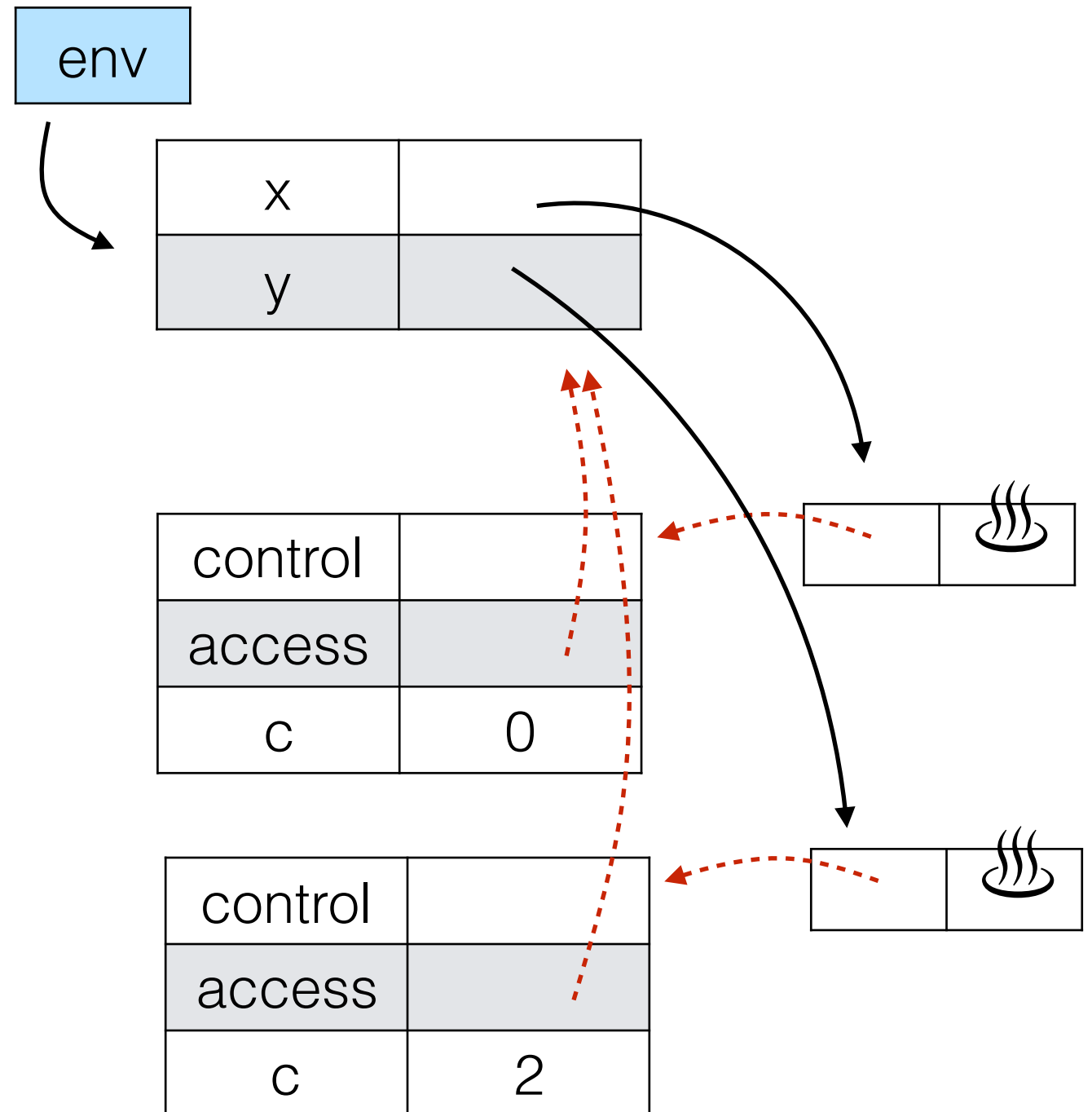


# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```

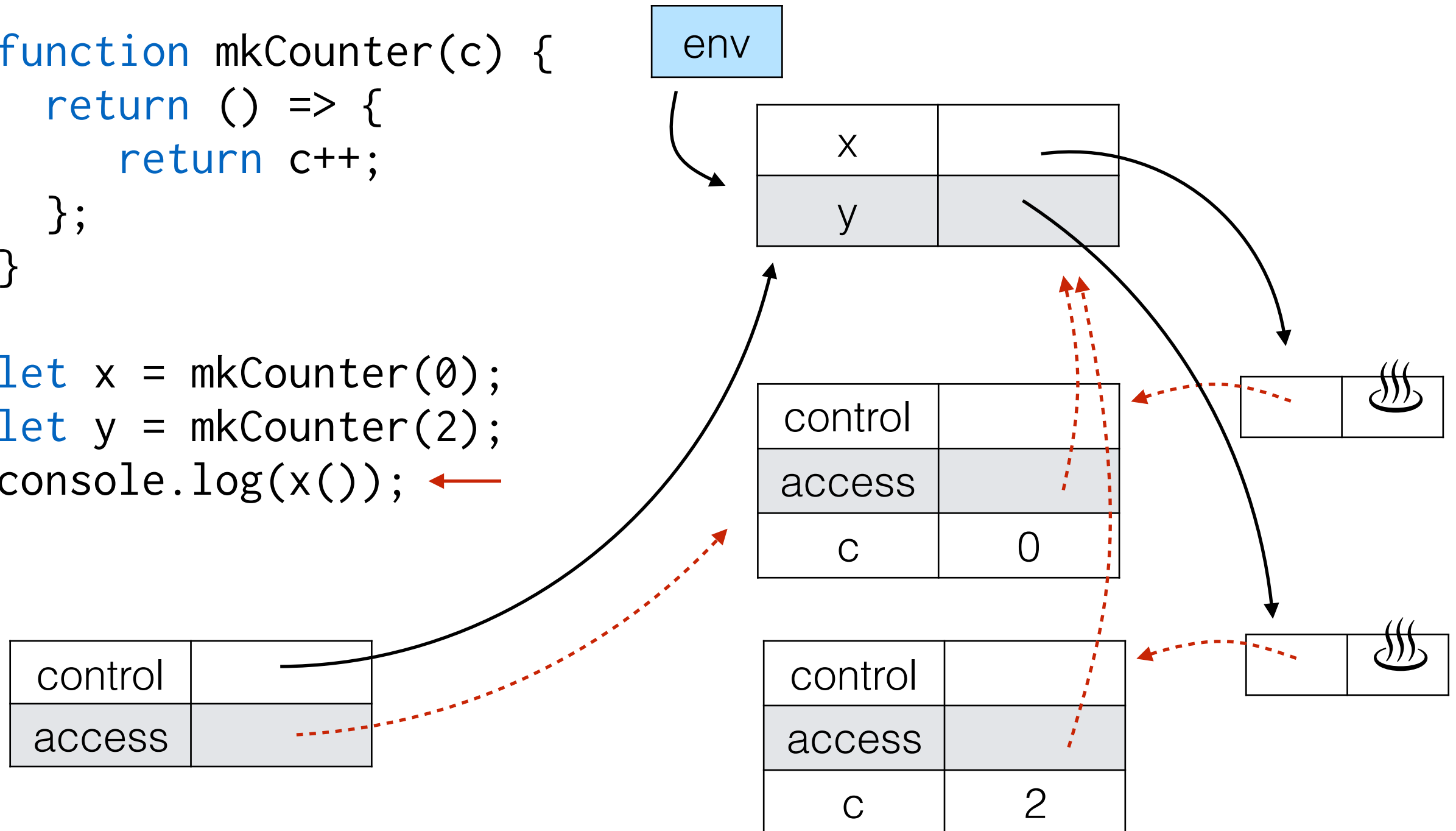


# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```

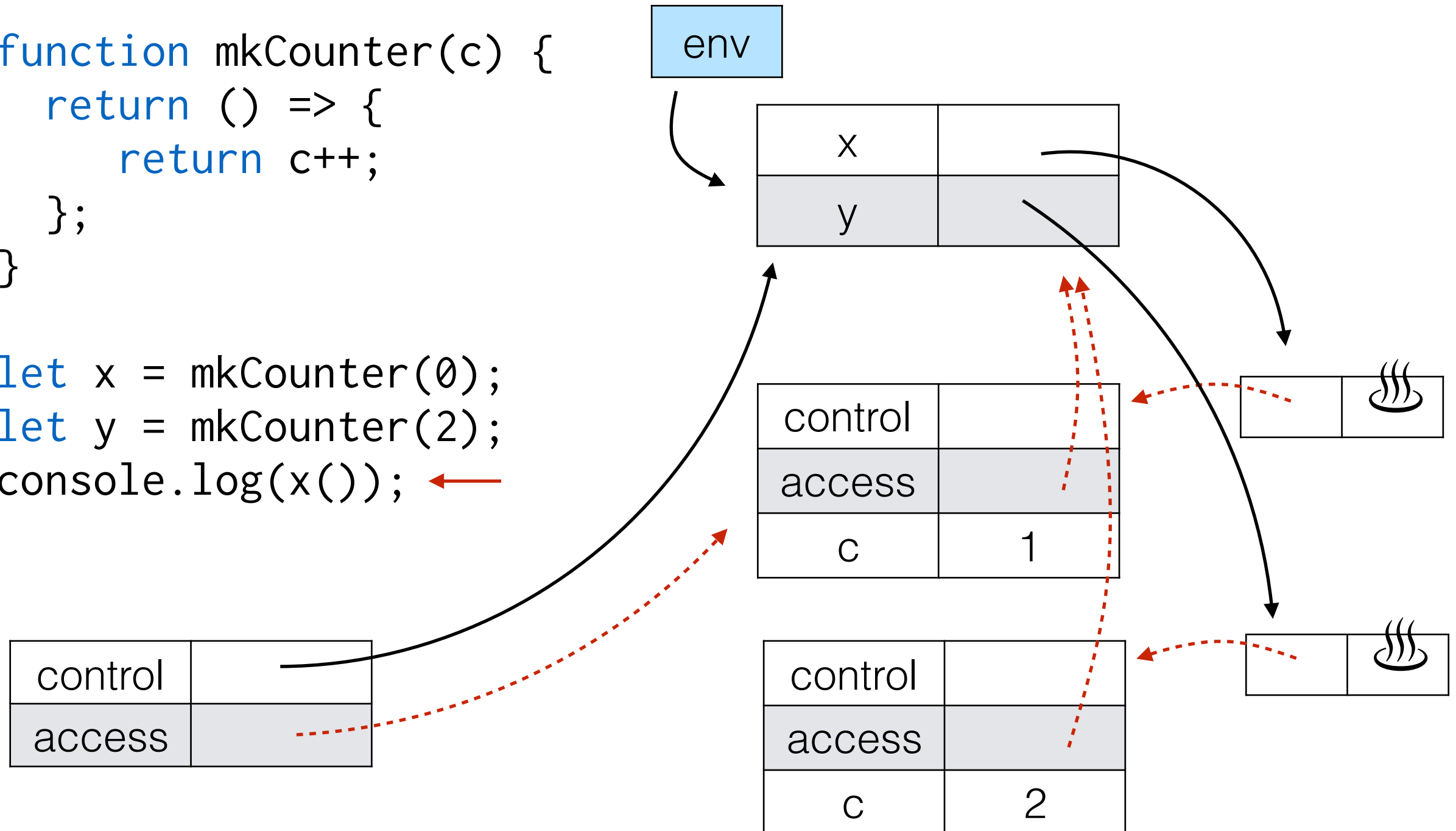


# Higher-order functions

- Consider the use of high-order mkCounter function

```
function mkCounter(c) {  
  return () => {  
    return c++;  
  };  
}
```

```
let x = mkCounter(0);  
let y = mkCounter(2);  
console.log(x());
```



# The environment model (by example)

- Anatomy of a scope ✓
- First-order functions ✓
- Free variables ✓
- High-order functions (bonus) ✓