Variant 2



1. Nonlinear optimization problem is given in the following form

$$\min\{f(x) = 10x_1^2x_2^2 + 2x_1^2x_3^2 + x_2^4 - 10x_2^2x_3^2 - 3x_3^4\},\$$

subject to

$$h_1(x) = 13x_1^2 + 8x_1x_2 - 2x_1x_3 + 1063x_1 + 3x_2^2 + 2x_2x_3 + 951x_2 + 10x_3^2 - 232x_3 - 120 = 0,$$

$$g_1(x) = 538 x_1 + 479.5 x_2 - 118 x_3 - 58.5 \le 0,$$

$$g_2(x) = 930.75 x_1 + 755.25 x_2 - 22.5 x_3 - 657 \le 0.$$

Check whether $\bar{x} = (1, -1, 0)^{\top}$, $\tilde{x} = (116.514008, -424.475095, 52.491911)^{\top}$, $\hat{x} = (4, -4, 2)^{\top}$ are stationary points. (1.0)

$$\left(h_{1}(x)\right)_{x_{1}}^{1} = 2GY_{1} + 8X_{2} - 2Y_{3} + 1063$$

$$\left(h_{1}(x)\right)_{x_{2}}^{1} = 8Y_{1} + 6X_{2} + 2X_{3} + 951$$

$$\left(h_{1}(x)\right)_{x_{3}}^{1} = -2X_{1} + 2Y_{2} + 20X_{3} - 232$$

$$\left(f(x)\right)_{x_{1}}^{1} = 20Y_{1}X_{2}^{2} + 4X_{1}X_{3}^{2}$$

$$\left(f(x)\right)_{x_{2}}^{1} = 20X_{1}^{2}X_{2} + 4X_{2}^{3} - 20X_{2}X_{3}^{2}$$

$$\left(f(x)\right)_{x_{3}}^{1} = 4Y_{1}^{2}X_{3} - 20Y_{2}^{2}X_{3} - 12X_{3}^{3}$$

$$\left(f(x)\right)_{x_{3}}^{1} = 4Y_{1}^{2}X_{3} - 20Y_{2}^{2}X_{3} - 12X_{3}^{3} + 12X_{3}^{3} +$$

Chocking stationarity conditions: Values of the points in constraints: * hi, gi, gz respectively s fationa vity True 0 0.0 -481.5 False 9.67132109508384e-06 -147103.8172465 -213977.47055025003 True 0 -60.5 0.0 (20 + 1.1081 + 538.M. 1930,75.M2 = 0) (-24 + 1.953 + 479,5M. + 755.25.M2 = 0) $(0+\lambda\cdot(-236)-118\mu_{11}-22,5\mu_{2}=0$ 10811 + 538 M1+20=0 $2953\lambda + 479,5\mu,-24=0$

591.5796259999998 -558.7546840000002 -264.139985999999 421151967.72610205 -397783545.7692034 -188044128.50252962

 $\widehat{X}_{1} \quad \widehat{X}_{2} \quad \widehat{X}_{3} \quad \widehat{X}_{4} \quad \widehat{X}_{5} \quad \widehat{X}_{6}$ $\widehat{X}_{4} + \lambda \widehat{X}_{1} = 0$ $\widehat{X}_{5} + \lambda \widehat{X}_{2} = 0 \quad \text{as } M = M_{2} = 0 \text{ for } \widehat{X}$ $\widehat{X}_{6} + \lambda \widehat{X}_{3} = 0 \quad \text{solution doesn't exist}$

Stationarity conditions:

$$\int 1344 + 1131 + 1930,75 \cdot M_2 = 0$$

$$-1216 + 963 + 755,25 \cdot N_2 = 0$$

$$|-1216 + 9631 + 75525.102 = 0$$

$$-608 - 208\lambda - 22,5\mu_z = 6$$

$$0 \le \mu, = 0$$

$$for x$$

No solution exists



3. Find a stationary point of function

$$f(x) = \sum_{i=1}^{n-1} (x_i^2 - 2)^2 + \left(\sum_{i=1}^n x_i^2 - 0.5\right)^2$$

for n = 10 using Broyden-Fletcher-Goldfarb-Shanno (BFGS) quasi-Newton method with the Wolfe inexact line search. Starting point $x_0 = (1, 1, ..., 1)^{\top}$, convergence tolerance $\varepsilon = 0.001$. Give as the answer the obtained point, the corresponding value of the objective function f, and the number of iterations. (2.0)

Code in Git Hub

Dut put.

Final Result (obtained point): [-5.00001514e-01 -5.00001514e-01 -5.00001514e-01 -5.00001514e-01 -5.00001514e-01 -5.00001514e-01 -5.00001514e-01 -5.00001514e-01

-5.00001514e-01 -1.43849011e-06]

Iteration Count: 7

Corresponding value of the objective function f: 30.625000000213618

Code in Git Hub, Output: