Package 'mcmc'

July 17, 2015

Version 0.9-4

2 initseq

morph	 	•		•									 		•				Č
morph.metrop	 												 						10
olbm	 												 						12
temper	 												 						13

Index 18

foo

Simulated logistic regression data.

Description

Like it says

Usage

data(foo)

Format

A data frame with variables

- **x1** quantitative predictor.
- x2 quantitative predictor.
- x3 quantitative predictor.
- y Bernoulli response.

Examples

```
library(mcmc)
data(foo)
out <- glm(y ~ x1 + x2 + x3, family = binomial, data = foo)
summary(out)</pre>
```

initseq

Initial Sequence Estimators

Description

Variance of sample mean of functional of reversible Markov chain using methods of Geyer (1992).

```
initseq(x)
```

initseq 3

Arguments

x a numeric vector that is a scalar-valued functional of a reversible Markov chain.

Details

Let

$$\gamma_k = \text{cov}(X_i, X_{i+k})$$

considered as a function of the lag k be the autocovariance function of the input time series. Define

$$\Gamma_k = \gamma_{2k} + \gamma_{2k+1}$$

the sum of consecutive pairs of autocovariances. Then Theorem 3.1 in Geyer (1992) says that Γ_k considered as a function of k is strictly positive, strictly decreasing, and strictly convex, assuming the input time series is a scalar-valued functional of a reversible Markov chain. All of the MCMC done by this package is reversible. This R function estimates the "big gamma" function, Γ_k considered as a function of k, subject to three different constraints, (1) nonnegative, (2) nonnegative and nonincreasing, and (3) nonnegative, nonincreasing, and convex. It also estimates the variance in the Markov chain central limit theorem (CLT)

$$\gamma_0 + 2\sum_{k=1}^{\infty} \gamma_k = -\gamma_0 + 2\sum_{k=0}^{\infty} \Gamma_k$$

Note: The batch means provided by metrop are also scalar functionals of a reversible Markov chain. Thus these initial sequence estimators applied to the batch means give valid standard errors for the mean of the match means even when the batch length is too short to provide a valid estimate of asymptotic variance. One does, of course, have to multiply the asymptotic variance of the batch means by the batch length to get the asymptotic variance for the unbatched chain.

Value

a list containing the following components:

origin indexing so Gamma.pos[1] is Γ_0 . Gamma.dec the vector Γ , estimated so as to be nonnegative and nonincreasing, where, as always, R uses one-origin indexing so Gamma.dec[1] is Γ_0 . Gamma.con the vector Γ , estimated so as to be nonnegative and nonincreasing and convex, where, as always, R uses one-origin indexing so Gamma.con[1] is Γ_0 . var.pos the scalar - gamma0 + 2 * sum(Gamma.pos), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.dec the scalar - gamma0 + 2 * sum(Gamma.dec), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.con the scalar - gamma0 + 2 * sum(Gamma.con), which is the asymptotic variance	gamma0	the scalar γ_0 , the marginal variance of x.
always, R uses one-origin indexing so Gamma.dec[1] is Γ_0 . the vector Γ , estimated so as to be nonnegative and nonincreasing and convex, where, as always, R uses one-origin indexing so Gamma.con[1] is Γ_0 . var.pos the scalar - gamma0 + 2 * sum(Gamma.pos), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.dec the scalar - gamma0 + 2 * sum(Gamma.dec), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.con the scalar - gamma0 + 2 * sum(Gamma.con), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance in the Markov chain CLT. Divide by length(x) to get the approximate variance	Gamma.pos	the vector Γ , estimated so as to be nonnegative, where, as always, R uses one-origin indexing so Gamma.pos[1] is Γ_0 .
where, as always, R uses one-origin indexing so Gamma.con[1] is Γ_0 . var.pos the scalar - gamma0 + 2 * sum(Gamma.pos), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.dec the scalar - gamma0 + 2 * sum(Gamma.dec), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.con the scalar - gamma0 + 2 * sum(Gamma.con), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance	Gamma.dec	the vector Γ , estimated so as to be nonnegative and nonincreasing, where, as always, R uses one-origin indexing so Gamma . dec[1] is Γ_0 .
in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.dec the scalar - gamma0 + 2 * sum(Gamma.dec), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.con the scalar - gamma0 + 2 * sum(Gamma.con), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance	Gamma.con	the vector Γ , estimated so as to be nonnegative and nonincreasing and convex, where, as always, R uses one-origin indexing so Gamma.con[1] is Γ_0 .
in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x. var.con the scalar - gamma0 + 2 * sum(Gamma.con), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance	var.pos	the scalar - gamma0 + 2 * sum(Gamma.pos), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x .
in the Markov chain CLT. Divide by length(x) to get the approximate variance	var.dec	the scalar - gamma0 + 2 * sum(Gamma.dec), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x .
	var.con	the scalar - gamma0 + 2 * sum(Gamma.con), which is the asymptotic variance in the Markov chain CLT. Divide by length(x) to get the approximate variance of the sample mean of x .

4 logit

Bugs

Not precisely a bug, but var.pos, var.dec, and var.con can be negative. This happens only when the chain is way too short to estimate the variance, and even then rarely. But it does happen.

References

Geyer, C. J. (1992) Practical Markov Chain Monte Carlo. Statistical Science 7 473-483.

See Also

metrop

Examples

```
n <- 2e4
rho <- 0.99
x \leftarrow arima.sim(model = list(ar = rho), n = n)
out <- initseq(x)
## Not run:
plot(seq(along = out$Gamma.pos) - 1, out$Gamma.pos,
   xlab = "k", ylab = expression(Gamma[k]), type = "1")
lines(seq(along = out$Gamma.dec) - 1, out$Gamma.dec, col = "red")
lines(seq(along = out$Gamma.con) - 1, out$Gamma.con, col = "blue")
## End(Not run)
\# asymptotic 95% confidence interval for mean of x
mean(x) + c(-1, 1) * qnorm(0.975) * sqrt(out$var.con / length(x))
# estimated asymptotic variance
out$var.con
# theoretical asymptotic variance
(1 + \text{rho}) / (1 - \text{rho}) * 1 / (1 - \text{rho}^2)
# illustrating use with batch means
bm \leftarrow apply(matrix(x, nrow = 5), 2, mean)
initseq(bm)$var.con * 5
```

logit

Simulated logistic regression data.

Description

Like it says

```
data(logit)
```

metrop 5

Format

A data frame with variables

- x1 quantitative predictor.
- **x2** quantitative predictor.
- **x3** quantitative predictor.
- x4 quantitative predictor.
- y Bernoulli response.

Examples

```
library(mcmc)
data(logit)
out <- glm(y ~ x1 + x2 + x3 + x4, family = binomial, data = logit)
summary(out)</pre>
```

metrop

Metropolis Algorithm

Description

Markov chain Monte Carlo for continuous random vector using a Metropolis algorithm.

Usage

```
metrop(obj, initial, nbatch, blen = 1, nspac = 1, scale = 1, outfun,
    debug = FALSE, ...)
```

Arguments

obj

an R function that evaluates the log unnormalized probability density of the desired equilibrium distribution of the Markov chain. First argument is the state vector of the Markov chain. Other arguments arbitrary and taken from the . . . arguments of this function. Should return – Inf for points of the state space having probability zero under the desired equilibrium distribution. Alternatively, an object of class "metropolis" from a previous run can be supplied, in which case any missing arguments (including the log unnormalized density function) are taken from this object (up until version 0.7-2 this was incorrect with respect to the debug argument, now it applies to it too).

initial a real vector, the initial state of the Markov chain.

nbatch the number of batches. blen the length of batches.

nspac the spacing of iterations that contribute to batches.

6 metrop

scale controls the proposal step size. If scalar or vector, the proposal is x + scale * z

where x is the current state and z is a standard normal random vector. If matrix,

the proposal is x + scale % x z.

outfun controls the output. If a function, then the batch means of outfun(state, ...)

are returned. If a numeric or logical vector, then the batch means of state[outfun]

(if this makes sense). If missing, the the batch means of state are returned.

debug if TRUE extra output useful for testing.
... additional arguments for obj or outfun.

Details

Runs a "random-walk" Metropolis algorithm, terminology introduced by Tierney (1994), with multivariate normal proposal producing a Markov chain with equilibrium distribution having a specified unnormalized density. Distribution must be continuous. Support of the distribution is the support of the density specified by argument obj. The initial state must satisfy obj(state, ...) > - Inf. Description of a complete MCMC analysis (Bayesian logistic regression) using this function can be found in the vignette demo (../doc/demo.pdf).

Suppose the function coded by the log unnormalized function (either obj or obj\$lud) is actually a log unnormalized density, that is, if w denotes that function, then e^w integrates to some value strictly between zero and infinity. Then the metrop function always simulates a reversible, Harris ergodic Markov chain having the equilibrium distribution with this log unnormalized density. The chain is not guaranteed to be geometrically ergodic. In fact it cannot be geometrically ergodic if the tails of the log unnormalized density are sufficiently heavy. The morph.metrop function deals with this situation.

Value

an object of class "mcmc", subclass "metropolis", which is a list containing at least the following components:

accept fraction of Metropolis proposals accepted.

batch nbatch by p matrix, the batch means, where p is the dimension of the result of

outfun if outfun is a function, otherwise the dimension of state[outfun] if

that makes sense, and the dimension of state when outfun is missing.

initial value of argument initial. final final state of Markov chain.

initial.seed value of .Random.seed before the run. final.seed value of .Random.seed after the run.

time running time of Markov chain from system.time().

the function used to calculate log unnormalized density, either obj or obj\$lud

from a previous run.

nbatch the argument nbatch or obj\$nbatch.

blen the argument blen or obj\$blen.

nspac the argument nspac or obj\$nspac.

outfun the argument outfun or obj\$outfun.

metrop 7

Description of additional output when debug = TRUE can be found in the vignette debug (../doc/debug.pdf).

Warning

If outfun is missing or not a function, then the log unnormalized density can be defined without a ... argument and that works fine. One can define it starting ludfun <- function(state) and that works or ludfun <- function(state, foo, bar), where foo and bar are supplied as additional arguments to metrop.

If outfun is a function, then both it and the log unnormalized density function can be defined without ... arguments *if they have exactly the same arguments list* and that works fine. Otherwise it doesn't work. Start the definitions ludfun <- function(state, foo) and outfun <- function(state, bar) and you get an error about unused arguments. Instead start the definitions ludfun <- function(state, foo, ...) and outfun <- function(state, bar, ...), supply foo and bar as additional arguments to metrop, and that works fine.

In short, the log unnormalized density function and outfun need to have ... in their arguments list to be safe. Sometimes it works when ... is left out and sometimes it doesn't.

Of course, one can avoid this whole issue by always defining the log unnormalized density function and outfun to have only one argument state and use global variables (objects in the R global environment) to specify any other information these functions need to use. That too follows the R way. But some people consider that bad programming practice.

References

Tierney, L. (1994) Markov chains for exploring posterior distributions (with discussion). *Annals of Statistics* **22** 1701–1762.

See Also

```
morph.metrop
```

Examples

```
h <- function(x) if (all(x >= 0) && sum(x) <= 1) return(1) else return(-Inf)
out <- metrop(h, rep(0, 5), 1000)
out$accept
# acceptance rate too low
out <- metrop(out, scale = 0.1)
out$accept
# acceptance rate o. k. (about 25 percent)
plot(out$batch[ , 1])
# but run length too short (few excursions from end to end of range)
out <- metrop(out, nbatch = 1e4)
out$accept
plot(out$batch[ , 1])
hist(out$batch[ , 1])</pre>
```

8 morph

morph	Variable Transformation
mor pri	rantate in antigormation

Description

Utility functions for variable transformation.

Usage

```
morph(b, r, p, center)
morph.identity()
```

Arguments

b	Positive real number. May be missing.
r	Non-negative real number. May be missing. If p is specified, r defaults to 0.
p	Real number strictly greater than 2. May be missing. If r is specified, p defaults to 3.
center	Real scalar or vector. May be missing. If center is a vector it should be the same length of the state of the Markov chain, center defaults to 0

Details

The morph function facilitates using variable transformations by providing functions to (using X for the original random variable with the pdf f_X , and Y for the transformed random variable with the pdf f_Y):

- Calculate the log unnormalized probability density for Y induced by the transformation.
- Transform an arbitrary function of X to a function of Y.
- Transform values of X to values of Y.
- Transform values of Y to values of X (the inverse transformation).

for a select few transformations.

morph.identity implements the identity transformation, Y = X.

The parameters r, p, b and center specify the transformation function. In all cases, center gives the center of the transformation, which is the value c in the equation

$$Y = f(X - c).$$

If no parameters are specified, the identity transformation, Y = X, is used.

The parameters r, p and b specify a function g, which is a monotonically increasing bijection from the non-negative reals to the non-negative reals. Then

$$f(X) = g(|X|)\frac{X}{|X|}$$

morph 9

where |X| represents the Euclidean norm of the vector X. The inverse function is given by

$$f^{-1}(Y) = g^{-1}(|Y|) \frac{Y}{|Y|}.$$

The parameters r and p are used to define the function

$$g_1(x) = x + (x - r)^p I(x > r)$$

where $I(\cdot)$ is the indicator function. We require that r is non-negative and p is strictly greater than 2. The parameter b is used to define the function

$$g_2(x) = (e^{bx} - e/3)I(x > \frac{1}{b}) + (x^3b^3e/6 + xbe/2)I(x \le \frac{1}{b})$$

We require that b is positive.

The parameters r, p and b specify f^{-1} in the following manner:

• If one or both of r and p is specified, and b is not specified, then

$$f^{-1}(X) = g_1(|X|) \frac{X}{|X|}.$$

If only r is specified, p = 3 is used. If only p is specified, r = 0 is used.

• If only b is specified, then

$$f^{-1}(X) = g_2(|X|) \frac{X}{|X|}.$$

• If one or both of r and p is specified, and b is also specified, then

$$f^{-1}(X) = g_2(g_1(|X|)) \frac{X}{|X|}.$$

Value

a list containing the functions

- outfun(f), a function that operates on functions. outfun(f) returns the function function(state, ...) f(inverse(state), ...).
- inverse, the inverse transformation function.
- transform, the transformation function.
- lud, a function that operates on functions. As input, lud takes a function that calculates a log unnormalized probability density, and returns a function that calculates the log unnormalized density by transforming a random variable using the transform function. lud(f) = function(state, ...) f(inverse(state), ...) + log.jacobian(state), where log.jacobian represents the function that calculate the log Jacobian of the transformation. log.jacobian is not returned.

Warning

The equations for the returned transform function (see below) do not have a general analytical solution when p is not equal to 3. This implementation uses numerical approximation to calculate transform when p is not equal to 3. If computation speed is a factor, it is advisable to use p=3. This is not a factor when using morph.metrop, as transform is only called once during setup, and not at all while running the Markov chain.

10 morph.metrop

See Also

```
morph.metrop
```

Examples

```
# use an exponential transformation, centered at 100.
b1 <- morph(b=1, center=100)
# original log unnormalized density is from a t distribution with 3
# degrees of freedom, centered at 100.
lud.transformed <- b1$lud(function(x) dt(x - 100, df=3, log=TRUE))
d.transformed <- Vectorize(function(x) exp(lud.transformed(x)))
## Not run:
curve(d.transformed, from=-3, to=3, ylab="Induced Density")
## End(Not run)</pre>
```

morph.metrop

Morphometric Metropolis Algorithm

Description

Markov chain Monte Carlo for continuous random vector using a Metropolis algorithm for an induced density.

Usage

```
morph.metrop(obj, initial, nbatch, blen = 1, nspac = 1, scale = 1,
  outfun, debug = FALSE, morph, ...)
```

Arguments

```
obj
                  see metrop.
initial
                  see metrop.
nbatch
                  see metrop.
blen
                  see metrop.
                  see metrop.
nspac
scale
                  see metrop.
outfun
                  unlike for metrop must be a function or missing; if missing the identity function,
                  function(x) x, is used.
debug
                  see metrop.
                  morph object used for transformations. See morph.
morph
                  see metrop.
. . .
```

morph.metrop 11

Details

morph.metrop implements morphometric methods for Markov chains. The caller specifies a log unnormalized probability density and a transformation. The transformation specified by the morph parameter is used to induce a new log unnormalized probability density, a Metropolis algorithm is run for the induced density. The Markov chain is transformed back to the original scale. Running the Metropolis algorithm for the induced density, instead of the original density, can result in a Markov chain with better convergence properties. For more details see Johnson and Geyer (submitted). Except for morph, all parameters are passed to metrop, transformed when necessary. The scale parameter is *not* transformed.

If X is a real vector valued continuous random variable, and Y = f(X) where f is a diffeomorphism, then the pdf of Y is given by

$$f_Y(y) = f_X(f^{-1}(y))|\nabla f^{-1}(y)|$$

where f_X is the pdf of X and ∇f^{-1} is the Jacobian of f^{-1} . Because f is a diffeomorphism, a Markov chain for f_X may be transformed into a Markov chain for f_X . Furthermore, these Markov chains are isomorphic (Johnson and Geyer, submitted) and have the same convergence rate. The morph variable provides a diffeomorphism, morph metrop uses this diffeomorphism to induce the log unnormalized density, $\log f_Y$ based on the user supplied log unnormalized density, $\log f_X$. morph metrop runs a Metropolis algorithm for $\log f_Y$ and transforms the resulting Markov chain into a Markov chain for f_X . The user accessible output components are the same as those that come from metrop, see the documentation for metrop for details.

Subsequent calls of morph.metrop may change to the transformation by specifying a new value for morph.

Any of the other parameters to morph. metrop may also be modified in subsequent calls. See metrop for more details.

The general idea is that a random-walk Metropolis sampler (what metrop does) will not be geometrically ergodic unless the tails of the unnormalized density decrease superexponentially fast (so the tails of the log unnormalized density decrease faster than linearly). It may not be geometrically ergodic even then (see Johnson and Geyer, submitted, for the complete theory). The transformations used by this function (provided by morph) can produce geometrically ergodic chains when the tails of the log unnormalized density are too light for metrop to do so.

When the tails of the unnormalized density are exponentially light but not superexponentially light (so the tails of the log unnormalized density are asymptotically linear, as in the case of exponential family models when conjugate priors are used, for example logistic regression, Poisson regression with log link, or log-linear models for categorical data), one should use morph with b = 0 (the default), which produces a transformation of the form g_1 in the notation used in the details section of the help for morph. This will produce a geometrically ergodic sampler if other features of the log unnormalized density are well behaved. For example it will do so for the exponential family examples mentioned above. (See Johnson and Geyer, submitted, for the complete theory.)

The transformation g_1 behaves like a shift transformation on a ball of radius r centered at center, so these arguments to morph should be chosen so that a sizable proportion of the probability under the original (untransformed) unnormalized density is contained in this ball. This function will work when r = 0 and center = 0 (the defaults) are used, but may not work as well as when r and center are well chosen.

When the tails of the unnormalized density are not exponentially light (so the tails of the log unnormalized density decrease sublinearly, as in the case of univariate and multivariate t distributions),

12 olbm

one should use morph with r > 0 and p = 3, which produces a transformation of the form g_2 composed with g_1 in the notation used in the details section of the help for morph. This will produce a geometrically ergodic sampler if other features of the log unnormalized density are well behaved. For example it will do so for the t examples mentioned above. (See Johnson and Geyer, submitted, for the complete theory.)

Value

an object of class mcmc, subclass morph.metropolis. This object is a list containing all of the elements from an object returned by metrop, plus at least the following components:

morph the morph object used for the transformations.

morph.final the final state of the Markov chain on the transformed scale.

References

Johnson, L. T. and Geyer, C. J. (submitted) Variable Transformation to Obtain Geometric Ergodicity in the Random-walk Metropolis Algorithm.

See Also

metrop, morph.

Examples

```
out <- morph.metrop(function(x) dt(x, df=3, log=TRUE), 0, blen=100,
    nbatch=100, morph=morph(b=1))
# change the transformation.
out <- morph.metrop(out, morph=morph(b=2))
out$accept
# accept rate is high, increase the scale.
out <- morph.metrop(out, scale=4)
# close to 0.20 is about right.
out$accept</pre>
```

olbm

Overlapping Batch Means

Description

Variance of sample mean of time series calculated using overlapping batch means.

```
olbm(x, batch.length, demean = TRUE)
```

Arguments

a matrix or time series object. Each column of x is treated as a scalar time series.

batch.length length of batches.

demean when demean = TRUE (the default) the sample mean is subtracted from each

batch mean when estimating the variance. Using demean = FALSE would essentially assume the true mean is known to be zero, which might be useful in a

toy problem where the answer is known.

Value

The estimated variance of the sample mean.

See Also

ts

Examples

```
h <- function(x) if (all(x >= 0) && sum(x) <= 1) return(1) else return(-Inf) out <- metrop(h, rep(0, 5), 1000) out <- metrop(out, scale = 0.1) out <- metrop(out, nbatch = 1e4) olbm(out$batch, 150) # monte carlo estimates (true means are same by symmetry) apply(out$batch, 1, mean) # monte carlo standard errors (true s. d. are same by symmetry) sqrt(diag(olbm(out$batch, 150))) # check that batch length is reasonable acf(out$batch, lag.max = 200)
```

temper

Simulated Tempering and Umbrella Sampling

Description

Markov chain Monte Carlo for continuous random vectors using parallel or serial simulated tempering, also called umbrella sampling. For serial tempering the state of the Markov chain is a pair (i,x), where i is an integer between 1 and k and x is a vector of length p. This pair is represented as a single real vector c(i, x). For parallel tempering the state of the Markov chain is vector of vectors (x_1, \ldots, x_k) , where each x is of length p. This vector of vectors is represented as a $k \times p$ matrix.

```
temper(obj, initial, neighbors, nbatch, blen = 1, nspac = 1, scale = 1,
  outfun, debug = FALSE, parallel = FALSE, ...)
```

Arguments

obj

either an R function or an object of class "tempering" from a previous run. If a function, should evaluate the log unnormalized density $\log h(i,x)$ of the desired equilibrium distribution of the Markov chain for serial tempering (the same function is used for both serial and parallel tempering, see details below for further explanation). If an object, the log unnormalized density function is obj\$lud, and missing arguments of temper are obtained from the corresponding elements of obj. The first argument of the log unnormalized density function is the state for simulated tempering (i,x) is supplied as an R vector c(i,x); other arguments are arbitrary and taken from the ... arguments of temper. The log unnormalized density function should return -Inf for points of the state space having probability zero.

initial

for serial tempering, a real vector c(i, x) as described above. For parallel tempering, a real $k \times p$ matrix as described above. In either case, the initial state of the Markov chain.

neighbors

a logical symmetric matrix of dimension k by k. Elements that are TRUE indicate jumps or swaps attempted by the Markov chain.

nbatch the number of batches. blen the length of batches.

nspac the spacing of iterations that contribute to batches.

scale

controls the proposal step size for real elements of the state vector. For serial tempering, proposing a new value for the x part of the state (i,x). For parallel tempering, proposing a new value for the x_i part of the state (x_1,\ldots,x_k) . In either case, the proposal is a real vector of length p. If scalar or vector, the proposal is x + scale * z where x is the part x or x_i of the state the proposal may replace. If matrix, the proposal is x + scale * x z. If list, the length must be x_i and each element must be scalar, vector, or matrix, and operate as described above. The x_i -th component of the list is used to update x_i when the

state is (i, x) or x_i otherwise.

outfun

controls the output. If a function, then the batch means of outfun(state, ...) are returned. The argument state is like the argument initial of this function. If missing, the batch means of the real part of the state vector or matrix are returned, and for serial tempering the batch means of a multivariate Bernoulli indicating the autrent appropriate are returned.

indicating the current component are returned.

debug if TRUE extra output useful for testing.

parallel if TRUE does parallel tempering, if FALSE does serial tempering.

... additional arguments for obj or outfun.

Details

Serial tempering simulates a mixture of distributions of a continuous random vector. The number of components of the mixture is k, and the dimension of the random vector is p. Denote the state (i,x), where i is a positive integer between 1 and k, and let h(i,x) denote the unnormalized joint density of their equilibrium distribution. The logarithm of this function is what obj or obj\$lud

calculates. The mixture distribution is the marginal for x derived from the equilibrium distribution h(i,x), that is,

$$h(x) = \sum_{i=1}^{k} h(i, x)$$

Parallel tempering simulates a product of distributions of a continuous random vector. Denote the state (x_1, \ldots, x_k) , then the unnormalized joint density of the equilibrium distribution is

$$h(x_1,\ldots,x_k) = \prod_{i=1}^k h(i,x_i)$$

The update mechanism of the Markov chain combines two kinds of elementary updates: jump/swap updates (jump for serial tempering, swap for parallel tempering) and within-component updates. Each iteration of the Markov chain one of these elementary updates is done. With probability 1/2 a jump/swap update is done, and with probability 1/2 a with-component update is done.

Within-component updates are the same for both serial and parallel tempering. They are "random-walk" Metropolis updates with multivariate normal proposal, the proposal distribution being determined by the argument scale. In serial tempering, the x part of the current state (i,x) is updated preserving h(i,x). In parallel tempering, an index i is chosen at random and the part of the state x_i representing that component is updated, again preserving h(i,x).

Jump updates choose uniformly at random a neighbor of the current component: if i indexes the current component, then it chooses uniformly at random a j such that neighbors[i, j] == TRUE. It then does does a Metropolis-Hastings update for changing the current state from (i, x) to (j, x).

Swap updates choose a component uniformly at random and a neighbor of that component uniformly at random: first an index i is chosen uniformly at random between 1 and k, then an index j is chosen uniformly at random such that neighbors[i, j] == TRUE. It then does does a Metropolis-Hastings update for swapping the states of the two components: interchanging x_i and x_j while preserving $h(x_1, \ldots, x_k)$.

The initial state must satisfy lud(initial, ...) > - Inf for serial tempering or must satisfy lud(initial[i,], ...) > - Inf for each i for parallel tempering, where lud is either obj or obj\$lud. That is, the initial state must have positive probability.

Value

an object of class "mcmc", subclass "tempering", which is a list containing at least the following components:

batch	the batch means of the continuous part of the state. If outfun is missing, an nbatch by k by p array. Otherwise, an nbatch by m matrix, where m is the length of the result of outfun.
ibatch	(returned for serial tempering only) an nbatch by k matrix giving batch means for the multivariate Bernoulli random vector that is all zeros except for a 1 in the i-th place when the current state is (i,x) .
acceptx	fraction of Metropolis within-component proposals accepted. A vector of length

k giving the acceptance rate for each component.

accepti fraction of Metropolis jump/swap proposals accepted. A k by k matrix giving

the acceptance rate for each allowed jump or swap component. NA for elements

such that the corresponding elements of neighbors is FALSE.

initial value of argument initial. final final state of Markov chain.

initial.seed value of .Random.seed before the run. final.seed value of .Random.seed after the run.

time running time of Markov chain from system.time().

lud the function used to calculate log unnormalized density, either obj or obj\$lud

from a previous run.

nbatch the argument nbatch or obj\$nbatch.
blen the argument blen or obj\$blen.
nspac the argument nspac or obj\$nspac.
outfun the argument outfun or obj\$outfun.

Description of additional output when debug = TRUE can be found in the vignette debug (../doc/debug.pdf).

Warning

If outfun is missing, then the log unnormalized density function can be defined without a ... argument and that works fine. One can define it starting ludfun <- function(state) and that works or ludfun <- function(state, foo, bar), where foo and bar are supplied as additional arguments to temper and that works too.

If outfun is a function, then both it and the log unnormalized density function can be defined without ... arguments *if they have exactly the same arguments list* and that works fine. Otherwise it doesn't work. Start the definitions ludfun <- function(state, foo) and outfun <- function(state, bar) and you get an error about unused arguments. Instead start the definitions ludfun <- function(state, foo, ...) and outfun <- function(state, bar, ...), supply foo and bar as additional arguments to temper, and that works fine.

In short, the log unnormalized density function and outfun need to have ...in their arguments list to be safe. Sometimes it works when ... is left out and sometimes it doesn't.

Of course, one can avoid this whole issue by always defining the log unnormalized density function and outfun to have only one argument state and use global variables (objects in the R global environment) to specify any other information these functions need to use. That too follows the R way. But some people consider that bad programming practice.

Examples

```
d <- 9
witch.which <- c(0.1, 0.3, 0.5, 0.7, 1.0)
ncomp <- length(witch.which)

neighbors <- matrix(FALSE, ncomp, ncomp)
neighbors[row(neighbors) == col(neighbors) + 1] <- TRUE
neighbors[row(neighbors) == col(neighbors) - 1] <- TRUE</pre>
```

```
ludfun <- function(state, log.pseudo.prior = rep(0, ncomp)) {</pre>
    stopifnot(is.numeric(state))
    stopifnot(length(state) == d + 1)
    icomp <- state[1]</pre>
    stopifnot(icomp == as.integer(icomp))
    stopifnot(1 <= icomp && icomp <= ncomp)</pre>
    stopifnot(is.numeric(log.pseudo.prior))
    stopifnot(length(log.pseudo.prior) == ncomp)
    theta <- state[-1]</pre>
    if (any(theta > 1.0)) return(-Inf)
   bnd <- witch.which[icomp]</pre>
    lpp <- log.pseudo.prior[icomp]</pre>
    if (any(theta > bnd)) return(lpp)
    return(-d * log(bnd) + lpp)
}
# parallel tempering
thetas <- matrix(0.5, ncomp, d)</pre>
out <- temper(ludfun, initial = thetas, neighbors = neighbors, nbatch = 20,
    blen = 10, nspac = 5, scale = 0.56789, parallel = TRUE, debug = TRUE)
# serial tempering
theta.initial <- c(1, rep(0.5, d))
# log pseudo prior found by trial and error
qux <- c(0, 9.179, 13.73, 16.71, 20.56)
out <- temper(ludfun, initial = theta.initial, neighbors = neighbors,</pre>
    nbatch = 50, blen = 30, nspac = 2, scale = 0.56789,
    parallel = FALSE, debug = FALSE, log.pseudo.prior = qux)
```

Index

```
*Topic datasets
    foo, 2
    logit, 4
*Topic misc
    metrop, 5
    morph, 8
    morph.metrop, 10
    temper, 13
*Topic ts
    initseq, 2
    olbm, 12
foo, 2
initseq, 2
logit, 4
metrop, 3, 4, 5, 10–12
morph, 8, 10-12
morph.metrop, 6, 7, 9, 10, 10
olbm, 12
temper, 13
ts, 13
```