

# Principles of Machine Learning

## Lecture 1: Introduction and Course Overview

Sharif University of Technology  
Dept. of Aerospace Engineering

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2 Session 2: Mathematical Foundations



# Course Overview

- **Course Title:** Principles of Machine Learning
- **Target Audience:** Undergraduate and graduate students from diverse academic backgrounds
- **Focus:** Balancing theoretical foundations with practical implementations
- **Key Tools:** Python, NumPy, Pandas, TensorFlow/Keras
- **Outcome:** Develop skills to understand, implement, and evaluate machine learning solutions



# Course Objectives

By the end of this course, students will be able to:

- ① Understand core machine learning concepts and algorithms
- ② Design and implement ML solutions using Python
- ③ Select appropriate algorithms for different problems
- ④ Preprocess and prepare data for ML tasks
- ⑤ Evaluate and validate ML models
- ⑥ Create end-to-end ML solutions for real-world problems



# Course Structure

- **Week 1:** Introduction to Machine Learning
- **Weeks 1-3:** Mathematical Foundations
- **Weeks 4-5:** Supervised Learning - Regression
- **Weeks 5-6:** Supervised Learning - Classification

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- **Week 7:** Model Evaluation and Validation
- **Week 8:** Practical Considerations
- **Weeks 9-10:** Unsupervised Learning
- **Week 11:** Neural Networks Fundamentals
- **Weeks 12-13:** Deep Learning
- **Week 14:** Reinforcement Learning
- **Week 15:** Advanced Topics



# Week 1: Introduction to Machine Learning

- What is machine learning?
- Types of machine learning problems
- Python programming basics (in Lab)
- Introduction to scientific computing (NumPy, Pandas) (in Lab)
- Case studies: ML applications in aerospace industry



# Mathematical Foundations (Weeks 1-3)

- Linear algebra review
- Probability and statistics
- Calculus concepts
- Optimization basics



# Supervised Learning (Weeks 4-6)

- **Regression:** Linear regression, polynomial regression, regularization techniques, gradient descent
- **Classification:** Logistic regression, SVMs, decision trees, random forests, k-Nearest Neighbors
- Applications: System modeling, fault detection, flight phase classification



# Model Evaluation and Validation (Week 7)

- Cross-validation techniques
- Performance metrics (accuracy, precision, recall, F1-score)
- Bias-variance tradeoff
- Model selection and hyperparameter tuning



# Practical Considerations (Week 8)

- Data cleaning, normalization, and transformation
- Feature selection and extraction techniques
- Industry case studies: Predictive maintenance, flight data analysis, aerospace design optimization
- Model deployment basics



# Unsupervised Learning (Weeks 9-10)

- Clustering algorithms (K-means, Hierarchical, DBSCAN)
- Dimensionality reduction (PCA, t-SNE)
- Anomaly detection
- Applications: Process monitoring, pattern discovery, flight data clustering



# Neural Networks and Deep Learning (Weeks 11-12)

- Neural Networks Fundamentals: Architecture, backpropagation, activation functions
- Deep Learning: CNNs, RNNs, time series data, modern architectures (Transformers), transfer learning
- Applications: Signal processing, computer vision, object detection in satellite imagery



# Reinforcement Learning (Week 13)

- Markov Decision Processes
- Q-learning
- Policy Gradient methods
- Applications: Control systems, resource optimization



# Advanced Topics (Week 15)

- Transfer learning
- Ensemble methods
- Explainable AI
- Few-shot and zero-shot learning



# What is Machine Learning

## Machine Learning

- The science (and art) of programming computers to *learn from data*
- “To give computers the ability to learn without explicit programming”
  - *Arthur Samuel, 1959*
- “To learn from Experience E w.r.t some Task T and performance measure P, if its performance on T, as measured by P, improves with E”
  - *Tom Mitchell, 1997*



# What is Machine Learning

There are three concepts at the core of ML [1]:

## Data

- Training data
- The model input
- Stores valuable information

## Model

- The input-output mapping
- Parametric
- Non-parametric

## Learning

- Determining model's parameters
- Optimization
- Generalization



# What is Machine Learning

## Why ML?

Traditional approach vs. ML approach

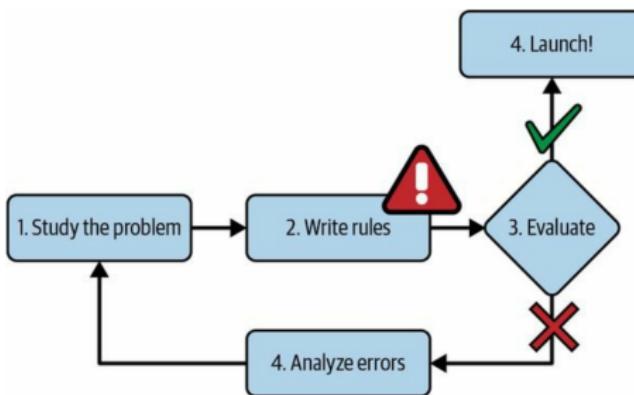


Figure: The traditional approach

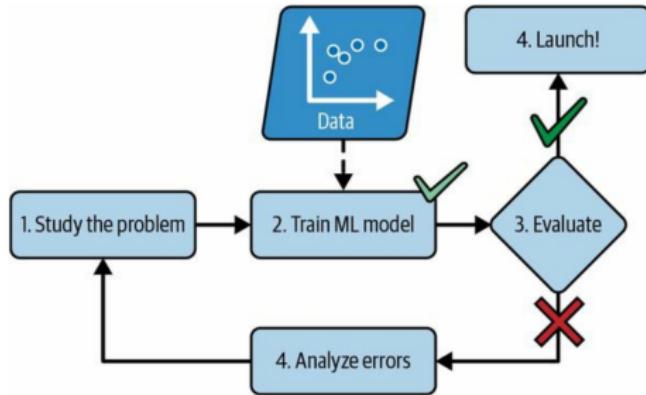


Figure: The machine learning approach



# What is ML

## Traditional vs. Machine Learning-based solutions

Traditional approach:

- Expert knowledge
- High interpretability
- Well-known and typical scenarios
- Lacking access to sufficient amount of data

Machine learning-based approach:

- Data-rich scenarios
- Unseen settings
- Adaptability for various conditions
- Difficulty of deriving a governing model



# What is Machine Learning

## Why ML?

Automatic adaptation for complex problems

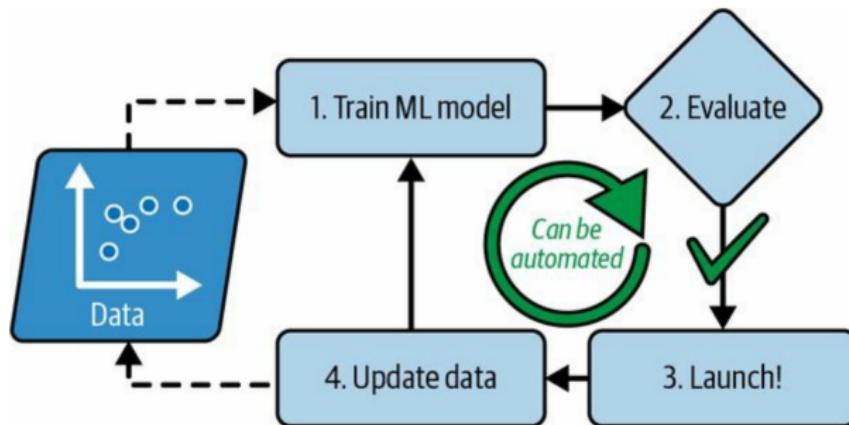


Figure: Automatically adapting to change



# What is Machine Learning

## Why ML?

Inspect ML models to see what they have learned (*not always possible though*)

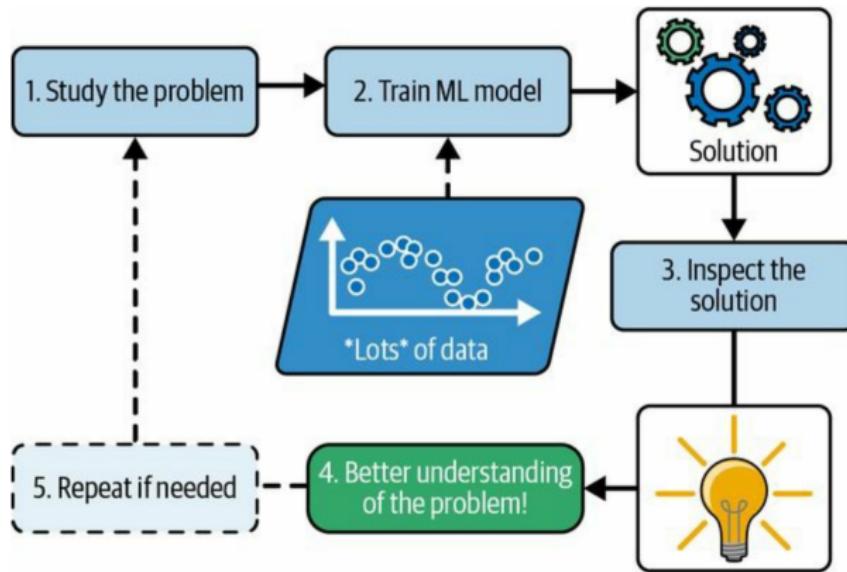


Figure: ML can help humans learn



# What is Machine Learning

## When ML?

- Problems with the traditional solutions being a long list of rules
- Complex problems with the traditional solutions being no good
- Fluctuating environments
- Revealing insights about the data



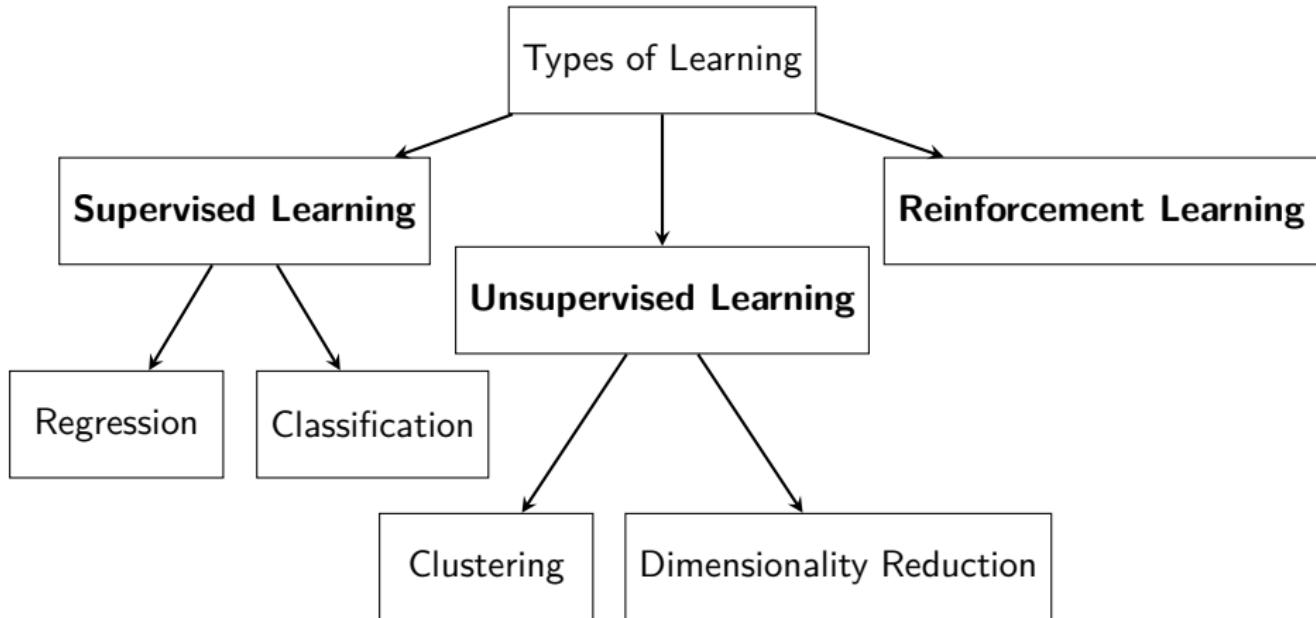
# What is Machine Learning

## Examples of Applications

- Detecting tumors in brain scans  
(*CNNs/Transformers*)
- Forecasting a company's revenue next year  
(*Regression, Random forest, Artificial neural network*)
- Representing a complex, high-dimensional dataset in a clear and insightful diagram  
(*Dimensionality reduction*)
- Building an intelligent bot for a game  
(*RL*)



# What is Machine Learning

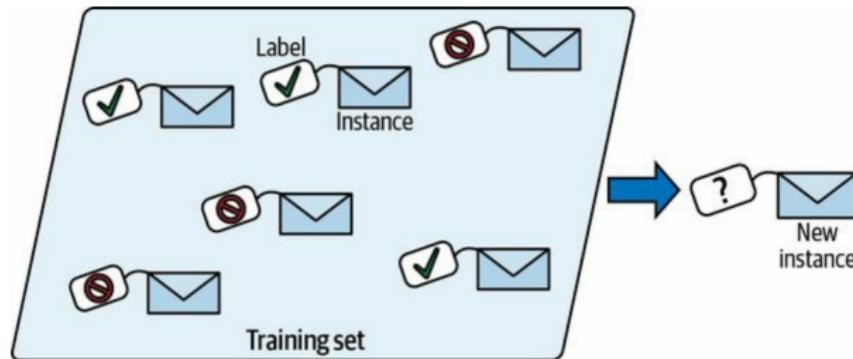


- \* Some modern learning paradigms, such as semi-supervised learning, are not mentioned above.
- \* Deep learning, Deep Generative Modelling, etc. are not explicitly discussed in the domain of ML.



# What is Machine Learning

## Supervised Learning

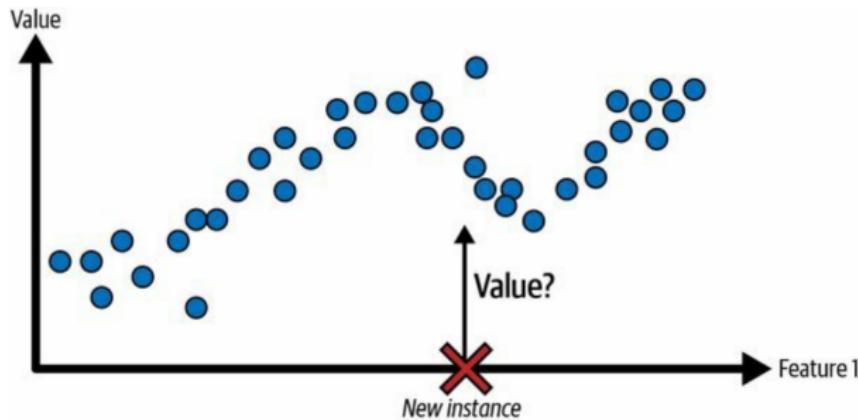


**Figure:** A labeled training set for spam classification (an example of supervised learning)



# What is Machine Learning

## Supervised Learning - An Example



**Figure:** A regression problem: predict a value (or multiple values), given an input feature (or multiple input features)



# What is Machine Learning

## Unsupervised Learning

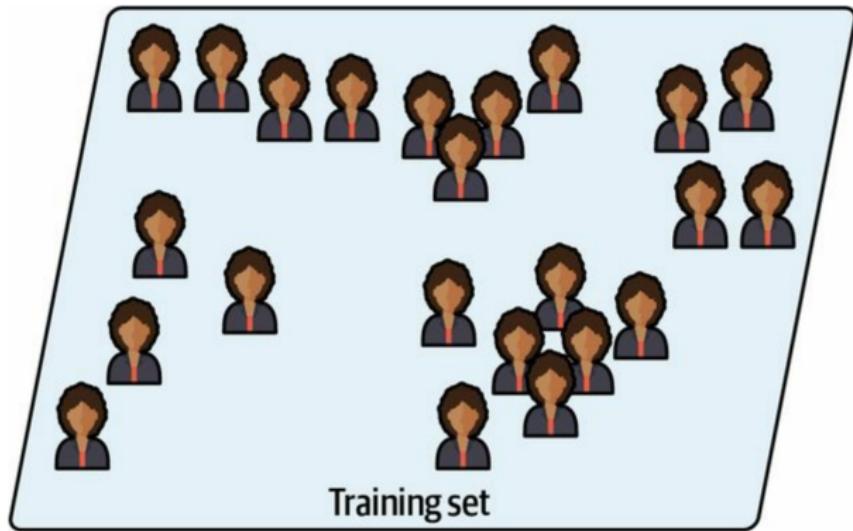


Figure: An unlabeled training set for unsupervised learning



# What is Machine Learning

## Unsupervised Learning - An Example

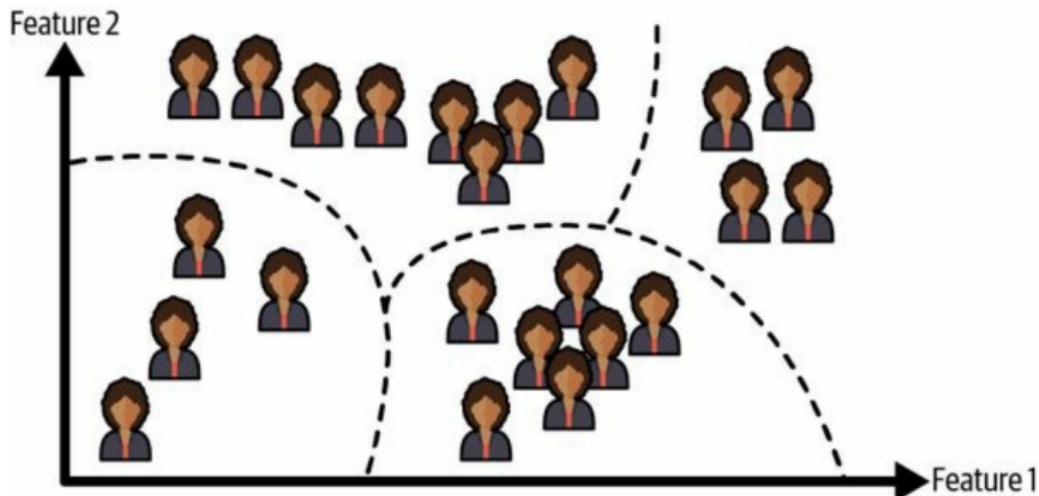


Figure: Clustering



# What is Machine Learning

## Unsupervised Learning - An Example

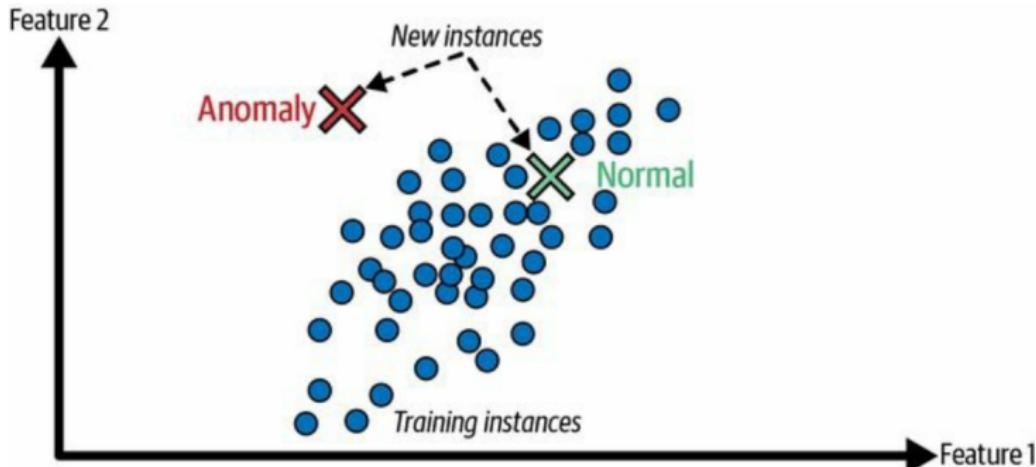


Figure: Anomaly detection

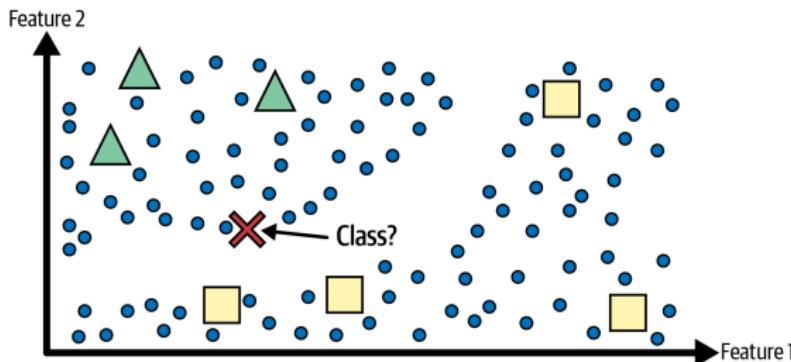


# What is Machine Learning

## Semi-supervised learning

Combines unsupervised and supervised learning

- leverages both unlabeled and partially labeled data



**Figure:** Semi-supervised learning with two classes (triangles and squares): the unlabeled examples (circles) help classify a new instance (the cross) into the triangle class rather than the square class, even though it is closer to the labeled squares



# What is Machine Learning

## Self-Supervised Learning

Generating a labeled dataset from a fully unlabeled dataset

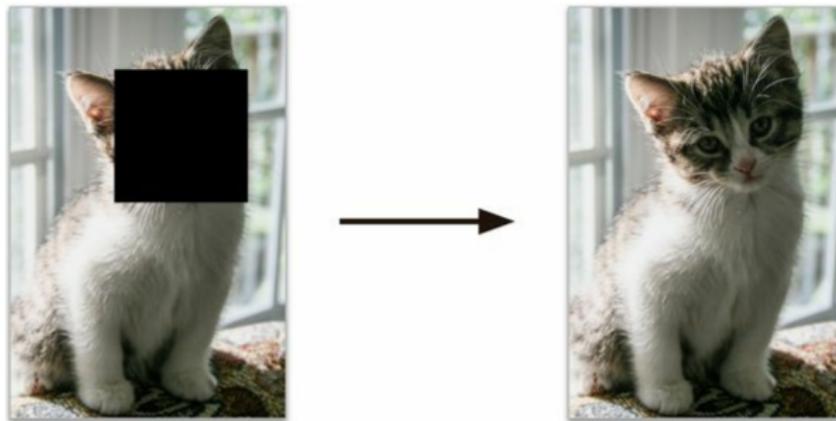


Figure: Self-supervised learning example: input (left) and target (right)



# What is Machine Learning

## Reinforcement Learning

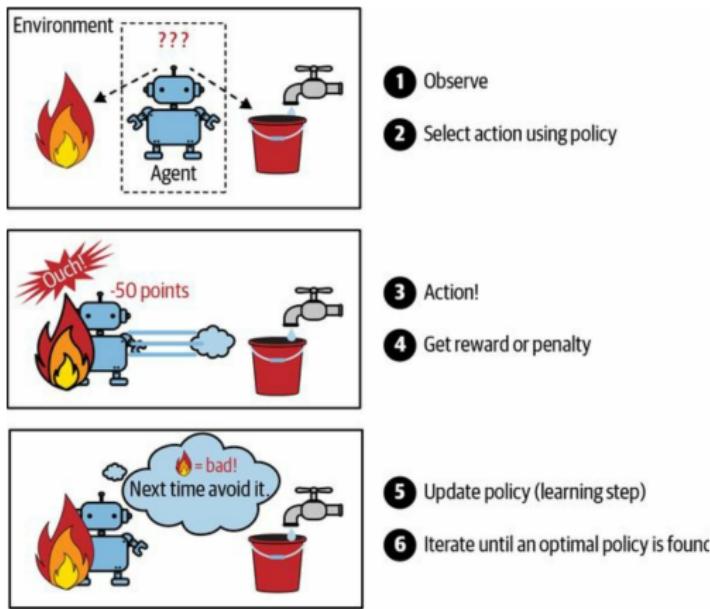


Figure: Reinforcement learning



# What is Machine Learning

## Batch Learning vs. Online Learning

### Batch Learning (Offline Learning)

- incapable of learning incrementally
- train using all available data
- training before launching into production
- susceptible to *model rot* or *data drift*
- a lot of computing resources (CPU, memory space, etc.)



# What is Machine Learning

## Batch Learning vs. Online Learning

### Online Learning

- capable of learning incrementally
- train using mini-batches
- capturing new data on the fly
- out-of-core learning
- adapt quickly to changing data

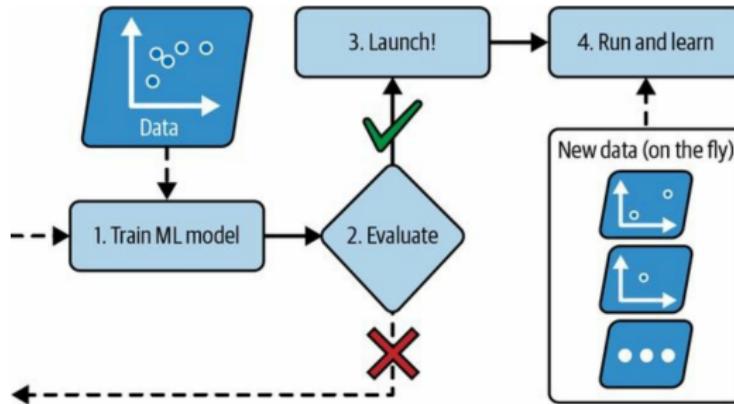


# What is Machine Learning

## Batch Learning vs. Online Learning

### Online Learning

- A model is trained, deployed, and continuously updated with new data.



**Figure:** In online learning, a model is trained and launched into production, and then it keeps learning as new data comes in



# What is Machine Learning

## Batch Learning vs. Online Learning

### Online Learning

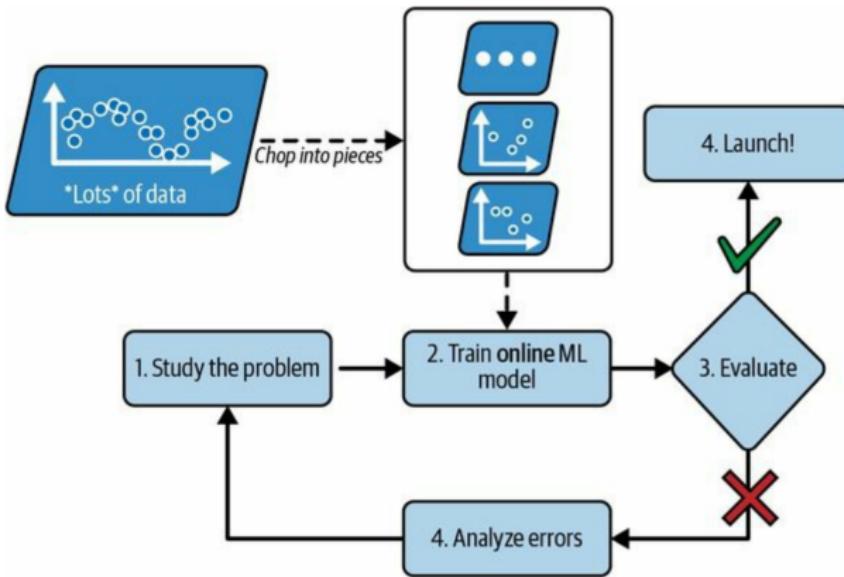


Figure: Using online learning to handle huge datasets



# What is Machine Learning

## Instance-Based Learning vs. Model-Based Learning

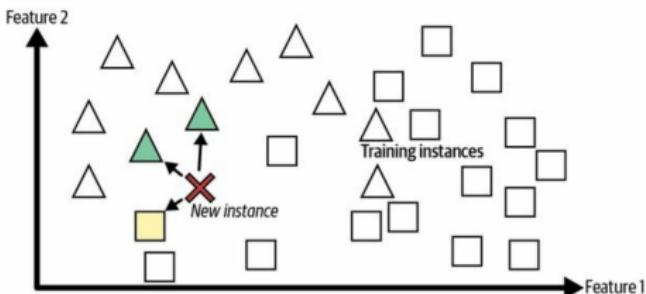


Figure: Instance-based learning

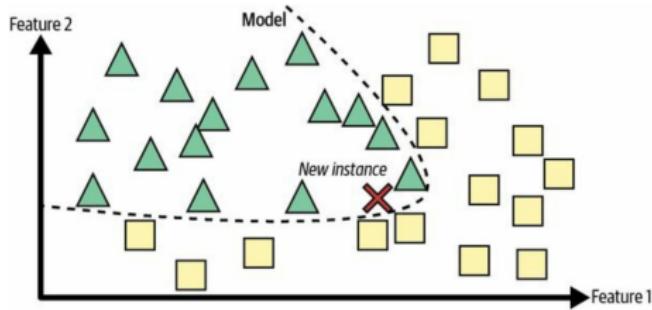


Figure: Model-based learning



# What is Machine Learning

## Main Challenges of Machine Learning

### 1. Insufficient Quantity of Training Data

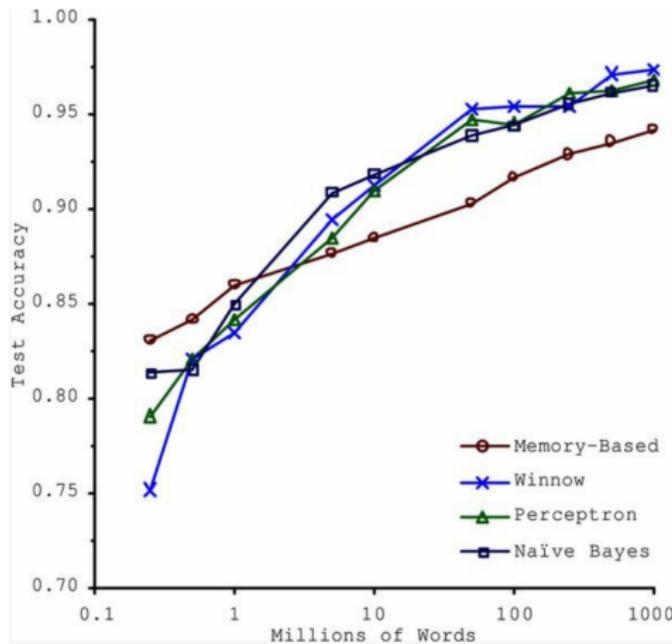


Figure: The importance of data versus algorithms



# What is Machine Learning

## Main Challenges of Machine Learning

### 2. Nonrepresentative Training Data

Training data should be representative of the new cases to generalize to

- too small samples → sampling noise
- very large samples → sampling bias



# What is Machine Learning

## Main Challenges of Machine Learning

### 3. Poor-Quality Data

Errors, outliers, noise, etc.

- Discard the outliers or fix the errors manually
- Handling missing features (ignore feature, ignore data, or fill in the missing values)



# What is Machine Learning

## Main Challenges of Machine Learning

### 4. Irrelevant Features

Feature engineering:

- *Feature selection* (selecting the most useful features)
- *Feature extraction* (combining existing features to produce a useful one)
- Gathering new data → Creating new features



# What is Machine Learning

## Main Challenges of Machine Learning

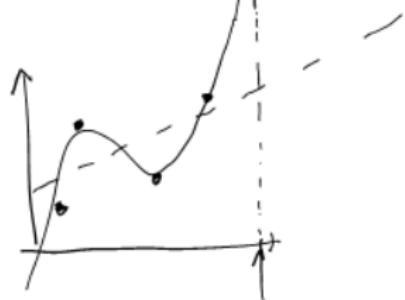
### 5. Overfitting the Training Data

Performing well on training data but not generalizing well

Complex relative to the amount and noisiness of the training data

Possible solutions:

- Simplifying or constraining the model
- Gather more training data
- Reduce the noise in the training data



# What is Machine Learning

## Main Challenges of Machine Learning

### 6. Underfitting the Training Data

Too simple to learn the underlying structure of data

Possible solutions:

- Select a model with more parameters
- Feed better features (feature engineering)
- Reduce the constraints



# What is Machine Learning

## Testing and Validating

### Hyperparameter Tuning and Model Selection

- Train the model on the *training set*
- Test the model on the *test set*
- *Generalization error*: The error rate on new cases
- Evaluate the model on the test set → Estimating the generalization error
- The value above indicates how good your model performs on unseen data
- Common 80-20 splitting

But, what if the model is the best model only for *that particular set*?



# What is Machine Learning

## Testing and Validation

### Hyperparameter Tuning and Model Selection

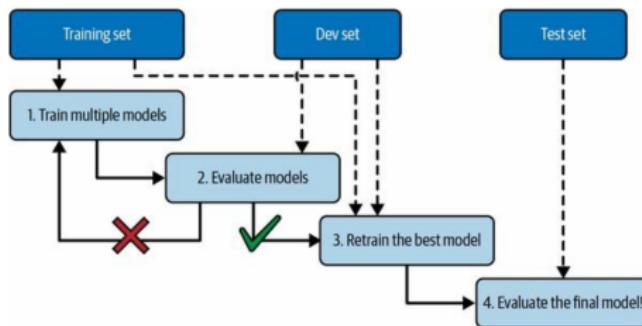


Figure: Model selection using holdout validation

Validation set, too small or too large → cross validation



# What is Machine Learning

## Data Mismatch

- Representativity of the test and validation (development) sets
- How to decide the poor performance is due to model overfitting or data mismatch —> using train-dev set



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# Mathematical Foundations

- **Linear Algebra**
- Probability & Statistics
- Calculus
- Optimization



# Mathematical Foundations: Linear Algebra

- Linear Algebra: The study of vectors and their manipulations
- Any mathematical object that satisfies the following two properties can be considered a **vector**:
  - $\mathbf{x} + \mathbf{y} = \mathbf{z}$
  - $\lambda\mathbf{x} = \mathbf{w}, \lambda \in \mathbb{R}$
- Examples of vectors: polynomials, audio signals, elements of  $\mathbb{R}^n$



# Mathematical Foundations: Linear Algebra

## Definition (Matrix)

Matrix  $\mathbf{A}$  is an  $m \cdot n$ -tuple of elements

$$\mathbf{A} = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{bmatrix}, \quad a_{ij} \in \mathbb{R}.$$



# Mathematical Foundations: Linear Algebra

## Definition (Matrix Addition and Multiplication)

The sum of two matrices  $\mathbf{A} \in \mathbb{R}^{m \times n}$ ,  $\mathbf{B} \in \mathbb{R}^{m \times n}$ :

$$\mathbf{A} + \mathbf{B} := \begin{bmatrix} a_{11} + b_{11} & \dots & a_{1n} + b_{1n} \\ \vdots & & \vdots \\ a_{m1} + b_{m1} & \dots & a_{mn} + b_{mn} \end{bmatrix} \in \mathbb{R}^{m \times n}.$$

For matrices  $\mathbf{A} \in \mathbb{R}^{m \times n}$ ,  $\mathbf{B} \in \mathbb{R}^{n \times k}$ , the elements of the product  $\mathbf{C} = \mathbf{AB} \in \mathbb{R}^{m \times k}$  are:

$$c_{ij} = \sum_{l=1}^n a_{il}b_{lj}, \quad i = 1, \dots, m, \quad j = 1, \dots, k.$$



# Mathematical Foundations: Linear Algebra

## Definition (Associativity)

$$\forall \mathbf{A} \in \mathbb{R}^{m \times n}, \mathbf{B} \in \mathbb{R}^{n \times p}, \mathbf{C} \in \mathbb{R}^{p \times q} : (\mathbf{AB})\mathbf{C} = \mathbf{A}(\mathbf{BC})$$

## Definition (Distributivity)

$$\begin{aligned}\forall \mathbf{A}, \mathbf{B} \in \mathbb{R}^{m \times n}, \mathbf{C}, \mathbf{D} \in \mathbb{R}^{n \times p} : & (\mathbf{A} + \mathbf{B})\mathbf{C} = \mathbf{AC} + \mathbf{BC} \\ & \mathbf{A}(\mathbf{C} + \mathbf{D}) = \mathbf{AC} + \mathbf{AD}\end{aligned}$$



# Mathematical Foundations: Linear Algebra

## Definition (Inverse)

For  $\mathbf{A} \in \mathbb{R}^{n \times n}$ ,  $\mathbf{B} \in \mathbb{R}^{n \times n}$  is the *inverse* of  $\mathbf{A}$  and denoted as  $\mathbf{A}^{-1}$  if:

$$\mathbf{AB} = \mathbf{I}_n = \mathbf{BA}$$

The inverse does exist  $\rightarrow \mathbf{A}$  is *invertible/nonsingular*

## Definition (Transpose)

For  $\mathbf{A} \in \mathbb{R}^{m \times n}$ ,  $\mathbf{B} \in \mathbb{R}^{n \times m}$  is the *transpose* of  $\mathbf{A}$  and denoted as  $\mathbf{A}^T$  if:

$$b_{ij} = a_{ji}$$

If  $\mathbf{A} = \mathbf{A}^T \rightarrow \mathbf{A}$  is *symmetric*



# Mathematical Foundations: Linear Algebra

A system of linear equations as below

$$a_{11}x_1 + \cdots + a_{1n}x_n = b_1$$

⋮

$$a_{m1}x_1 + \cdots + a_{mn}x_n = b_m$$

can be formulated using matrices notation as

$$\mathbf{Ax} = \mathbf{b}.$$

$$\downarrow$$
$$\begin{bmatrix} a_{11} & a_{1n} \\ a_{m1} & a_{mn} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \\ \vdots \\ b_m \end{bmatrix}$$

How to solve them?



# Mathematical Foundations: Linear Algebra

**Example 1.** For  $a \in \mathbb{R}$ , we seek all solutions of the following system of equations:

$$\begin{array}{ccccccccc} -2x_1 & + & 4x_2 & - & 2x_3 & - & x_4 & + & 4x_5 = -3 \\ 4x_1 & - & 8x_2 & + & 3x_3 & - & 3x_4 & + & x_5 = 2 \\ x_1 & - & 2x_2 & + & x_3 & - & x_4 & + & x_5 = 0 \\ x_1 & - & -2x_2 & & & - & 3x_4 & + & 4x_5 = a \end{array}$$



# Mathematical Foundations: Linear Algebra

## Example 1.

$$\mathbf{A}\mathbf{x} = \mathbf{b} \xrightarrow{\text{augmented matrix}} [\mathbf{A} \mid \mathbf{b}]:$$

$$\left[ \begin{array}{ccccc|c} -2 & 4 & -2 & -1 & 4 & -3 \\ 4 & -8 & 3 & -3 & 1 & 2 \\ 1 & -2 & 1 & -1 & 1 & 0 \\ 1 & -2 & 0 & -3 & 4 & a \end{array} \right]$$

After applying some *elementary transformations*:

$$\rightsquigarrow \left[ \begin{array}{ccccc|c} 1 & -2 & 1 & -1 & 1 & 0 \\ 0 & 0 & 1 & -1 & 3 & -2 \\ 0 & 0 & 0 & 1 & -2 & 1 \\ 0 & 0 & 0 & 0 & 0 & a+1 \end{array} \right]$$

Known as *row-echelon form*.

Only for  $a = 1$  this system can be solved.



# Mathematical Foundations: Linear Algebra

## Example 1.

A *particular solution* is

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{bmatrix} = \begin{bmatrix} 2 \\ 0 \\ -1 \\ 1 \\ 0 \end{bmatrix}.$$

The *general solution* is

$$\left\{ \mathbf{x} \in \mathbb{R}^5 : \mathbf{x} = \begin{bmatrix} 2 \\ 0 \\ -1 \\ 1 \\ 0 \end{bmatrix} + \lambda_1 \begin{bmatrix} 2 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} + \lambda_2 \begin{bmatrix} 2 \\ 0 \\ -1 \\ 2 \\ 1 \end{bmatrix}, \quad \lambda_1, \lambda_2 \in \mathbb{R} \right\}.$$



## Definition (Row-Echelon Form)

A matrix is in row-echelon form if

- All rows that contain only zeros are at the bottom of the matrix; correspondingly, all rows that contain at least one nonzero element are on top of rows that contain only zeros.
- Looking at nonzero rows only, the first nonzero number from the left (also called the *pivot*) is always strictly to the right of the pivot of the row above it.



# Mathematical Foundations: Linear Algebra

## Definition (Reduced Row-Echelon Form)

An equation system is in *rref* or *row canonical form* if

- It is in row-echelon form.
- Every pivot is 1.
- The pivot is the only non-zero entry in its column.

## Definition

**Gaussian elimination** is an algorithm that performs elementary transformations to bring a system of linear equations into reduced row-echelon form.



# Mathematical Foundations: Linear Algebra

**Example 2.** Calculating an Inverse Matrix by Gaussian Elimination:

$$\mathbf{A} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 2 & 0 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

*augmented matrix*

$$\left[ \begin{array}{cccc|cccc} 1 & 0 & 2 & 0 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 2 & 0 & 1 & 0 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \end{array} \right]$$



# Mathematical Foundations: Linear Algebra

## Example 2.

After using Gaussian Elimination to reach rref:

$$\left[ \begin{array}{cccc|cccc} 1 & 0 & 0 & 0 & -1 & 2 & -2 & 2 \\ 0 & 1 & 0 & 0 & 1 & -1 & 2 & -2 \\ 0 & 0 & 1 & 0 & 1 & -1 & 1 & -1 \\ 0 & 0 & 0 & 1 & -1 & 0 & -1 & 2 \end{array} \right]$$

Thus,

$$\mathbf{A}^{-1} = \begin{bmatrix} -1 & 2 & -2 & 2 \\ 1 & -1 & 2 & -2 \\ 1 & -1 & 1 & -1 \\ -1 & 0 & -1 & 2 \end{bmatrix}$$

Check this by  $\mathbf{AA}^{-1} = \mathbf{I}$

