1. La ve virolve urmatoarele evafii de ordin ni

a)
$$x^{1V} = 1 + 2$$
, $x(0) = 1$, $x'(0) = 2$, $x''(0) = -1$, $x'''(0) = 0$

$$x^{IV} = f(t)$$

•
$$x''' = 5 x'' dt = 5t dt + 25 dt = \frac{t^2}{2} + 2t + C_{\eta}$$

•
$$x'' = 5 x''' dt = \frac{1}{2} 5t^2 dt + 2 5t dt + c_1 5 dt = \frac{t^3}{6} + t^2 + c_1 t + c_2$$

$$-x' = 5x''dt = 5\frac{t^3}{6}dt + 5t^2dt + 5c_1tdt + c_25dt$$

$$= \frac{1}{6} \cdot \frac{t^{9}}{4} + \frac{t^{3}}{3} + c_{1} + \frac{t^{2}}{2} + c_{2} + c_{3} + \frac{t^{4}}{24} + \frac{t^{3}}{3} + c_{1} + \frac{t^{2}}{2} + c_{2} + c_{3}$$

$$= \frac{7}{24} \cdot \frac{t^5}{5} + \frac{7}{3} \cdot \frac{t^4}{4} + \frac{c_7}{2} \cdot \frac{t^3}{3} + c_2 \cdot \frac{t^2}{2} + c_3 t + c_4$$

$$\left[X = \frac{t^{5}}{120} + \frac{t^{4}}{12} + C_{1} + \frac{t^{3}}{6} + C_{2} + \frac{t^{2}}{2} + C_{3} + C_{4}\right]$$

•
$$x(0) = [C_4 = 1]$$
• $x^{1}(0) = [C_3 = 2]$
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$$x''' = f(t)$$

$$-x' = \int x'' dt = -\int cost dt + \int cint dt + C_1 \int dt$$
$$= -cost + C_1 + C_2$$

$$X = xort - xinf + c_1 \frac{t^2}{z} + c_2 f + c_3$$

•
$$\chi'(0) = 1 + C_3 = 1 \Rightarrow C_3 = 0$$

• $\chi'(0) = -1 + C_2 = 2 \Rightarrow C_2 = 3$
• $\chi''(0) = -1 + C_1 = 3 \Rightarrow C_1 = 4$

d)
$$x'' = \frac{1}{t}, x(1) = 7, x'(1) = 2$$

 $x'' = f(t)$

= + Sn(H) - Sndt + Cn Sdt = + Sn(+) - + + Cn + + Cz

$$X = t ln |t| - t + c_1 t + c_2$$

•
$$x'(n) = |C_1 = 2|$$

• $x(n) = |C_1 = 2|$
• $x(n) = -1 + 2 + C_2 = 1 \implies |C_2 = 0|$

$$\rho = \sqrt{x_{pc} = t \ln |t| + t}$$

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2. La re rezolve armatoorele quati de ordin n:

a)
$$k^{x''} - (x'')^2 = t + 7$$
.
 $F(t_1 x'') = 0$

· Foren schimborea de functie x"= y.

$$\begin{cases} x^{7} - y^{2} = t + 1 = (-2) e^{7} - y^{2} - 1 = t = (-2) e^{7} + 2 = (-2) dy \\ (-2) e^{7} - 2 = (-2) e^{7} - 2 = (-2) e^{7} + 2 = (-2) e^$$

•
$$x = \int x^{3} dt = \int (2^{7}(\gamma - 1) - \frac{2\gamma^{3}}{3} + C_{1})(2^{7} - 2\gamma) d\gamma$$

= $(2^{7})^{2}(\gamma - 1) - 2\gamma 2^{7}(\gamma - 1) - \frac{2\gamma^{3}}{3} \cdot 2^{7} + 2\gamma \cdot \frac{2\gamma^{3}}{3} + C_{1}2^{7} - C_{1} \cdot 2\gamma$

$$X = \frac{(27^{-3})e^{27}}{4} - (27^2 - 67 + 6)e^{7} - \frac{(27^3 - 67^2 + 127 - 12)e^{7}}{3} + \frac{47^5}{15} +$$

$$+ c_1 e^{7} + c_1 \gamma^2 + c_2, \quad t = e^{7} - \gamma^2 - \gamma$$

$$\kappa$$
) $\chi^{11} + lm \chi^{11} = t - 5$
 $F(t, \chi'') = 0$

* Form schimborea de functie x'' = y $y + \ln y = t - 5 = y + \ln y + 5 = t = \ell(y) = 0 dt = (1 + \frac{1}{7}) dy$ $x' = 5 \times '' dt = 5 y(1 + \frac{1}{7}) dy = 5 (y + 1) dy = \frac{2^2}{2} + y + C_1$

$$x = \frac{3^{3}}{6} + \frac{2^{2}}{4} + \frac{2^{2}}{2} + y + c_{1}y + c_{1}$$

3. Là re rezolve unnotoorele evalu de ordin n:

$$[x'-y]$$
 (=) $x''=y$) (=) $y'+y'tgt= \sin zt$ (&c. dif. afina)

$$\frac{dy}{dt} = -y t y t = \frac{7}{3} dy = (-t y t) dt = \frac{7}{3} dy = -\frac{5}{5} t y t dt$$

$$(C(t) \cdot cost)' + (C(t) \cdot cost) t_2 t = rin 2t$$

$$C'(t)$$
 rost = rinzt

$$(x) + (x')^2 = 0, x(1) = 2, x'(1) = 3$$

$$F(t,x',x'')=0;$$

$$\frac{[x'=y](z)}{y'+\frac{2}{t^2}}(z) x''=y' (z) t^2 y' + 2y^2 = 0 | t^2$$

(le su vorisbile reparabile)

$$\gamma' = \frac{-2}{1^{2}} \gamma^{2} (t) \frac{d\gamma}{dt} = \frac{-2}{1^{2}} \gamma^{2} (t) \frac{\eta}{\gamma^{2}} d\gamma = \frac{-2}{1^{2}} dt (t) \frac{5}{1^{2}} d\gamma = \frac{5}{1^{2}} d\tau (t) \frac{5}{1^{2}} d\tau + \frac{5}{1^{2}} d\tau (t) \frac{5}{1^{2}} d\tau = \frac{5}{1^{2}} d\tau (t) \frac{5}{1^{2}} d\tau + \frac{5}{1^{2}} d\tau (t) \frac{5}{1^{2}} d\tau + \frac{5}{1^{2}} d\tau (t)$$

$$(n+t^{2}) \gamma^{1} = 2^{t} \gamma \Leftrightarrow \frac{d\gamma}{dt} (n+t^{2}) = 2^{t} \gamma \Leftrightarrow \frac{\gamma}{\gamma} d\gamma = \frac{2t}{n+t^{2}} dt \Leftrightarrow$$

$$(x) \frac{\gamma}{\gamma} d\gamma = \frac{2t}{n+t^{2}} dt (x) \ln |\gamma| = 2n[t^{2}+1) + C \Rightarrow \gamma = C(t^{2}+1)$$

$$(x) = \gamma = C(t^{2}+1)$$

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$$(x) = \zeta ((t^{2}+1)) dt = C(\frac{t^{3}}{3}+1) + C \eta$$

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$$(x) = \zeta ((t^{2}+1)) dt = \zeta ((t^{2}+1)$$

 $-x = 5x^{(1)}dt = 5(-ce^{-t} + c_1 + c_2 + c_2 + c_3) =$

 $x = ce^{-t} + c_1 \frac{t^3}{6} + c_2 \frac{t^2}{2} + c_3 t + c_4$

4. La re violve umatoorele ecuatie de ordin n:

$$a) t^2 \cdot x \cdot x'' = (x - tx')^2$$

$$F(t, x, x', x'') = \theta$$

$$E(t, xx_1) = t_2 x x_1 - (x - tx_1) = x_2 \cdot E(t, x_1x_1) x_1$$

$$= x_2 (t_2 x x_1) - x_2 (x - tx_1) x_2$$

$$= x_2 (t_2 x x_1) - (x - tx_1) x_2 \cdot E(t, x_1x_1) x_1$$

$$\bullet | \overrightarrow{x' = x \gamma} \Rightarrow x'' = x' \gamma + x \gamma' = x \gamma^2 + x \gamma'$$

$$t^2 \times (x^2 + x^2) - (x - t \times y)^2 = 0$$

$$t^2x^2y^2 + t^2x^2y^1 - (x^2 - 2tx^2y + 12x^2y^2) = 0$$

Etopa 1:
$$\gamma' = \frac{-2}{t} \gamma(e) \frac{d\gamma}{dt} = \frac{-2}{t} \gamma(e) \frac{1}{\gamma} d\gamma = \frac{-2}{t} dt(e) \frac{1}{2} \frac{1}{2} d\gamma = \frac{-2}{t} dt(e)$$

$$C'(t) t^{-1} = \frac{1}{t^2}$$
 (3) $C'(t) = 1$ (7) $C(t) = 5 \cdot 1 dt = t + C_1$

$$f_0 = (t + c_1)t^{-2} = t^{-1} + c_1t^{-2}$$

$$\gamma = \gamma_0 + \gamma_0 = ct^{-2} + t^{-1} + c_1t^{-2} = t^{-1} + ct^{-2}$$

· Den
$$y = \frac{x'}{x}$$
 (=) $t^{-\gamma} + Ct^{-2} = \frac{x'}{x}$ (=) $\frac{dx}{x} = (t^{-\gamma} + Ct^{-2})dt$ (=)

(=)
$$5\frac{dx}{x} = 5(1^{-7}+C1^{-2})At(0) In |x| = In |t| - \frac{c}{t} + c_1 =) \times = c_1 t - e^{\frac{-c}{t}}$$

$$\times = c_1 + \ell^{\frac{-C}{t}}$$

6)
$$t \times x^{11} + t(x^{1})^{2} - xx^{1} = 0$$

$$F(t,x)^{1}, x^{1} = 0$$

$$F(t,x)^{1}, x^{1}, x^{1} = 0$$

$$F(t,x)^{1}, x^{1$$

In [M = 3 In (t) + (=) [No = (+3)

Etonaz: 90 = C(t) +3

$$C'(t)t^{3} - C(t)3t^{2} - 3\frac{1}{t} \cdot C(t)t^{3} = 2$$

$$C'(t)t^{3} = 2(=) C'(t) = \frac{2}{t^{3}} \iff C(t) = \int \frac{2}{t^{3}} dt \iff C(t) = \frac{-7}{t^{3}} + C_{1}$$

$$V_{0} = \left(\frac{-7}{t^{2}} + C_{1}\right)t^{3} = -t + C_{1}t^{3}$$

$$M = M_{0} + V_{0} = -t + C_{1}t^{3} + Ct^{3} = -t + Ct^{3}$$

$$M = -t + Ct^{3}$$

$$V_{0} = \frac{1}{A} = 2 = \frac{7}{-t + Ct^{3}}$$

$$V_{0} = \frac{1}{A} = 2 = \frac{7}{-t + Ct^{3}}$$

•
$$7 = \frac{1}{\mu} (=) = \frac{1}{-t+c+3}$$

$$-\gamma = 2 + \frac{7}{t} = \gamma = \frac{\gamma}{-t + ct^3} + \frac{1}{t}$$

$$-\gamma = \frac{x'}{x} \approx \frac{x'}{x} = \frac{1}{-t+c+\delta} + \frac{1}{t} \approx \frac{dx}{x} = \left(\frac{7}{-t+c+\delta} + \frac{1}{t}\right) dt \approx$$

$$(=) \int \frac{dx}{x} dx = \int \left(\frac{1}{-t + ct^3} + \frac{1}{t} \right) dt$$

$$\lim_{x \to \infty} |x| = \frac{\ln|ct^2 - 1|}{z} - c_1 = \lim_{x \to \infty} |(ct^2 - 1)^{\frac{1}{2}} \cdot c_1|$$

$$x = c_1 \cdot (ct^2 - 1)^{\frac{1}{2}}$$

La re rezolve umotoorele scuati de ordin n:

$$F(x, x', x'') = 0$$

•
$$dy = -x dx = 5 dy = -5x dx = 2 + C$$

•
$$\gamma = \frac{dx}{dt} = -\frac{x^2}{2} + C = \frac{dx}{dt} = \frac{dx}{dt} = \frac{dx}{dt} = \frac{dx}{dt} = \frac{dx}{dt} = \frac{1}{2} + C$$

$$\left[t \cdot c_1 = 5 \frac{7}{\frac{-\lambda^2}{2} + c} dx \right]$$

(a)
$$x - x^{(1)} + 3 x^{1} x^{11} = 0$$

$$F(x_1\lambda', x'', x'') = 0$$

$$\frac{1}{y} = \frac{dy}{dt} = x^{1} \Rightarrow x^{2} \Rightarrow x^{3} \Rightarrow x^{4} \Rightarrow x^{2} \Rightarrow x^{2}$$

$$-x-\gamma^2\frac{d\gamma}{d^2x}+3\cdot\gamma\cdot\gamma\frac{d\gamma}{dx}=0 : \gamma^2\frac{d\gamma}{dx}$$

$$x \cdot \frac{1}{dx} + 3 = 0$$
 (3) $\int \frac{1}{x} dx = \frac{-1}{3}$ (3) $f_{x}(x) + C = \frac{-1}{3}$ (5) $f_{x}(x) = 0$

$$(z) x = c l^{\frac{-1}{3}}$$